PDC REPORT

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Sequential Performance:

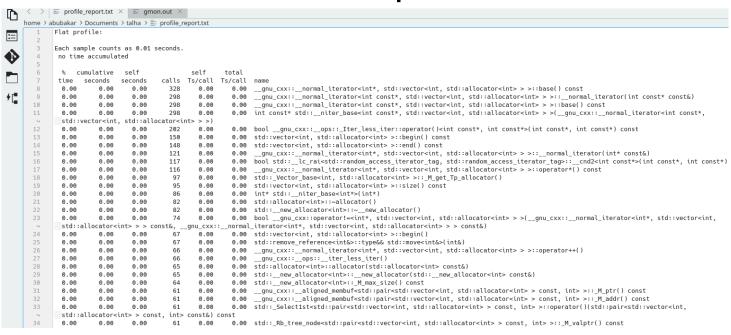
```
abubakar@HP:~/Documents/talha$ time ./s
Enter n: 4
Level-order traversal of IST T1:
1234 |
2 1 3 4 |
2 1 4 3 | 2 3 1 4 |
1 2 4 3 | 2 3 4 1 | 3 2 1 4 |
2 4 3 1 | 3 1 2 4 | 3 2 4 1 |
2 4 1 3 | 4 2 3 1 | 1 3 2 4 | 3 4 2 1 |
4 2 1 3 | 3 4 1 2 | 4 3 2 1 |
4 1 2 3 | 3 1 4 2 | 4 3 1 2 |
1 4 2 3 | 1 3 4 2 | 4 1 3 2 |
1432 I
Level-order traversal of IST T2:
1234 I
1324 |
1 3 4 2 | 3 1 2 4 |
1 4 3 2 | 3 1 4 2 | 3 2 1 4 |
1 4 2 3 | 4 1 3 2 | 3 4 1 2 | 2 3 1 4 |
1 2 4 3 | 4 1 2 3 | 3 4 2 1 | 4 3 1 2 | 2 1 3 4 |
4 2 1 3 | 3 2 4 1 | 4 3 2 1 |
2 4 1 3 | 2 3 4 1 | 4 2 3 1 |
2 1 4 3 | 2 4 3 1 |
Level-order traversal of IST T3:
1234 |
1243 |
1 4 2 3 | 2 1 4 3 |
1 4 3 2 | 4 1 2 3 | 2 1 3 4 | 2 4 1 3 |
1 3 4 2 | 4 1 3 2 | 2 4 3 1 | 4 2 1 3 |
1 3 2 4 | 3 1 4 2 | 4 3 1 2 | 2 3 4 1 | 4 2 3 1 |
3 1 2 4 | 3 4 1 2 | 2 3 1 4 | 3 2 4 1 | 4 3 2 1 |
3 2 1 4 | 3 4 2 1 |
real
        0m0.964s
        0m0.000s
user
        0m0.002s
sys
```

For n=9

```
2 3 8 4 5 9 6 | 1 7 2 3 4 8 9 5 6 | 1 7 2 3 9 4 8 5 6
                                                        1
                                                            2
8 1 2 3 4 9 5 6 7 | 1 8 2 3 9 4 5 6 7 | 1 2 8 9 3 4 5 6 7 |
                                                            192
6 | 1 9 2 3 8 4 5 7 6 | 9 1 2 3 4 8 5 7 6
                                          1 1 8 2 3 4 7 5
                                                          6
8 5 6 | 1 2 8 3 7 4 5 6 9 | 1 8 2 3 7 4 5 9 6 | 1 2 8 3 7 4 9 5 6
3 4 5 9 6 | 1 2 7 8 3 4 9 5 6 | 1 2 7 3 8 9 4 5 6 | 1 2 7 9 3 8 4
2 3 9 8 4 5 6 | 1 7 2 9 3 4 8 5 6 | 1 7 9 2 3 4 5 8 6 | 1 9 7 2 3
8 1 2 3 9 4 5 6 7 | 1 8 2 9 3 4 5 6 7 | 1 9 8 2 3 4 5 6 7 | 9 1 2
 | 8 1 2 3 4 7 9 5 6 | 1 8 2 3 4 9 7 5 6 | 1 2 8 3 9 4 7 5
                                                            6
4 5 6 | 1 2 3 8 9 7 4 5 6 | 1 2 9 3 8 7 4 5 6 | 1 9 2 3 7 8 4 5 6
3 8 4 5 6 | 1 9 2 7 3 4 8 5 6 | 9 1 2 7 3 4 5 8 6 | 1 7 2 8 3 4 5
7 2 3 4 5 6 8 | 7 1 2 3 8 4 5 6 9 | 7 1 2 8 3 4 5 9 6 | 7 1 2 3 8
8 1 2 9 3 4 5 6 7 | 1 8 9 2 3 4 5 6 7 | 9 1 8 2 3 4 5 6 7 | 8 1 2
6 | 1 9 2 8 3 4 7 5 6 | 9 1 2 3 8 4 7 5 6 | 8 1 2 3 7 4 5 6 9 | 8
5 6 9 | 8 1 2 7 3 4 5 9 6 | 1 8 2 7 3 4 9 5 6 | 1 2 8 7 3 9 4 5 6
3 4 9 5 6 | 1 7 2 8 3 9 4 5 6 | 1 7 2 9 8 3 4 5 6 | 1 7 9 2 3 8 4
2 9 3 8 4 5 6 | 7 1 9 2 3 4 8 5 6 | 7 9 1 2 3 4 5 8 6 | 9 7 1 2 3
8 1 9 2 3 4 5 6 7 | 9 8 1 2 3 4 5 6 7 | 8 1 2 9 3 4 5 7 6 | 1 8 9
6 | 1 8 2 3 9 7 4 5 6 | 1 2 8 9 3 7 4 5 6 | 1 9 2 8 3 7 4 5 6 | 9
4 5 6 | 9 1 2 7 3 8 4 5 6 | 1 8 7 2 3 4 5 6 9 | 8 1 7 2 3 4 5 9 6
3 4 5 6 9 | 7 8 1 2 3 4 5 9 6 | 7 1 8 2 3 4 9 5 6 | 7 1 2 8 3 9 4
8 9 1 2 3 4 5 6 7 | 8 1 9 2 3 4 5 7 6 | 9 8 1 2 3 4 5 7 6 | 8 1 2
6 | 8 1 2 7 3 9 4 5 6 | 1 8 2 7 9 3 4 5 6 | 1 2 8 9 7 3 4 5 6 | 1
4 5 6 | 1 9 7 2 8 3 4 5 6 | 9 1 7 2 3 8 4 5 6 | 7 8 1 2 3 4 5 6 9
3 4 8 5 6 |
8 9 1 2 3 4 5 7 6 | 8 1 9 2 3 4 7 5 6 | 9 8 1 2 3 4 7 5 6 | 8 1 2
6 | 8 1 7 2 3 9 4 5 6 | 1 8 7 2 9 3 4 5 6 | 1 7 8 9 2 3 4 5 6 | 1
4 5 6 | 7 9 1 2 8 3 4 5 6 | 9 7 1 2 3 8 4 5 6
8 9 1 2 3 4 7 5 6 | 8 1 9 2 3 7 4 5 6 | 9 8 1 2 3 7 4 5 6 | 8 1 2 9
6 | 8 7 1 2 3 9 4 5 6 | 7 8 1 2 9 3 4 5 6 | 7 1 8 9 2 3 4 5 6 | 7
8 9 1 2 3 7 4 5 6 | 8 1 9 2 7 3 4 5 6 | 9 8 1 2 7 3 4 5 6 | 8 1 7
6 I
8 9 1 2 7 3 4 5 6 | 8 1 9 7 2 3 4 5 6 | 9 8 1 7 2 3 4 5 6 | 8 7 1 9
8 9 1 7 2 3 4 5 6 | 8 7 9 1 2 3 4 5 6 | 9 8 7 1 2 3 4 5 6 |
8 9 7 1 2 3 4 5 6 |
```

real 0m22.753s user 0m16.800s sys 0m0.272s

Profile Report:



OpenMP Performance(n=9):

```
1 1 2 9 3 4 8 7
                     5 6
                        | 192
                                3 4 7 8 5 6
                                              9 1
                                                  2 3 4 7 5 8 6
                                                                   2 3 8
                                                                         7 4 5 6
                                                                                 9
     8 6
           9 1
               2 3
                   7 4 5 6 8
                                2 7
                                    3 8 4 5 6 9
                                                  1 2 7 8
                                                         3 4 5 9 6 |
                                                                       2 7 3 8 4
                                                                                 9 5
                                                                                     6
                                                                                        1
     4 5 9 6
               1 7
                   2 3 4 8 9 5 6 | 1 7 2 3 9 4 8 5 6
                                                      172934586
                                                                         1 7 9 2
                                                                                 3 4
                                                                                      68
     3 4 9 5 6 7 | 1 8
                       2 3 9 4 5 6 7 | 1
                                        2 8 9 3 4
                                                  5 6
                                                     7 | 1 9 2 8 3 4 5 6
                                                                             Q 1
                                                                                        5
                   6 | 9 1 2 3 4
                                        | 182347
                                                           8 1 2
       2 3 8 4
               5 7
                                8 5 7 6
                                                      5 6 9
                                                                   3 4 7 5 9 6
                                                                                        4
     1 1 2 8 3 7 4 5 6 9
                        | 182374596 | 1283
                                                      7 4 9
                                                           5 6
                                                                   2 3 8
                                                                         79
                                                               | 1
                                                                                 6
                                                                             4 5
     96 | 127834956 | 1
                                2 7
                                    3 8 9
                                          4 5 6 | 1 2 7 9
                                                         3 8 4 5 6 | 1
                                                                       29
                                                                             3 4
                                                                                         1
     8 4 5 6 |
                   2 9
                                              5 8 6 |
               1 7
                       3 4 8 5 6 | 1 7 9 2
                                          3 4
                                                      1 9
                                                           2 3 4 5 6 8
                                                                         7 1 2
                                                                                       6 9
     3 9 4 5 6 7 | 1 8 2 9 3 4 5 6 7 | 1 9 8 2 3 4
                                                     7 | 9 1 2 8 3 4 5 6
 1 2
                                                  5 6
                                                                             8 1
                                                                                 2 3
                                                                                        5
               9 5 6 | 1 8 2 3 4
                                        1 2 8 3 9 4 7 5 6
                                                           1 2 9 8 3 4 7 5 6
   8
     1 2 3 4 7
                                                                               | 1 9
                                9 7
                                    5 6
                                                                                       3 8
     1 2 3 8 9 7 4 5 6
                        | 1 2 9 3 8
                                            | 1 9 2 3 7 8 4 5 6 | 9 1 2 3 7 4
                                    7 4 5 6
                                                                             8 5
                                                                                 6
                                                                                       2 8
                                                                       7 8 2 3 4
     5 6 | 1 9 2 7
                   3 4 8 5 6 | 9 1 2 7 3 4 5 8 6 | 1 7
                                                      2834569
                                                                   | 1
  2 3 4 5 6 8 |
               7 1 2 3 8 4 5 6 9 | 7 1 2 8 3 4 5 9 6 |
                                                      7 1 2 3 8 4 9 5 6
                                                                         7 1 2 3 9 8
                                                                                       5 6
     9 3 4 5 6 7 | 1 8 9 2 3 4 5 6 7 | 9 1 8 2 3 4
8 1 2
                                                  5 6 7 | 8 1 2 3 9 4 5 7 6
                                                                           | 1829
                                                                                        5
     9 2 8 3 4 7 5 6 | 9 1 2 3 8 4 7 5 6
                                        | 8 1 2 3 7 4 5 6 9
6 | 1
                                                           | 8 1 2 3 7 4 9 5 6 | 1 8
   9
     | 8 1 2 7 3 4 5 9 6 | 1 8 2
                                7 3 4 9 5 6
                                            | 1 2 8 7 3 9 4 5 6 | 1 2 7 8 9 3 4 5 6 | 1
                                                                                       29
                                                      9238456 | 197234856
     56 | 17
               2839456 | 172983456 | 17
                                    9 1 2 3 4 5 8 6
   3 8 4 5 6 |
               7 1 9 2 3 4 8 5 6 |
                                                      9
                                                       7 1 2 3 4 5 6 8
 19
     2 3 4 5 6 7 |
                   981234567 | 812934576
                                                       | 189234576 | 9182345
     8 2 3 9 7 4 5 6 | 1 2 8 9 3 7 4 5 6 | 1 9 2 8 3 7 4 5 6 | 9 1 2 3 8 7 4 5 6 |
6 | 1
                                                                                       7 3
     9 1 2 7
4 5
   6
               3 8 4 5 6 | 1 8 7
                                2 3 4 5 6 9 | 8 1 7 2 3 4 5 9 6 | 1 8 7 2 3 4 9 5 6
3 4 5 6 9 | 7 8 1 2 3 4 5 9 6 | 7 1 8 2 3 4 9 5 6 | 7 1 2 8 3 9 4 5 6 | 7 1 2 9 8 3 4 5
 9 1 2 3 4 5 6 7 | 8 1 9 2 3 4 5 7 6 | 9 8 1 2 3 4 5 7 6 | 8 1 2 9 3 4 7 5 6
                                                                           | 1 8 9 2
   8 1 2 7 3 9 4 5 6 | 1 8 2 7 9 3 4 5 6 | 1 2 8 9 7 3 4 5 6 | 1 9 2 8 7 3 4 5 6 | 9 1 2 7 8
   6 | 1 9 7 2 8 3 4 5 6 | 9 1 7 2 3 8 4 5 6 | 7 8 1 2 3 4 5 6 9 | 8 7 1 2 3 4 5 9 6 | 7 8 1
4 5
3 4 8 5 6 |
8 9 1 2 3 4 5 7 6 | 8 <u>1</u> 9 2 3 4 7 5 6 | 9 8 1 2 3 4 7 5 6 | 8 1 2 9 3 7 4 5 6 | 1 8 9 2 3 7 4
 | 8 1 7 2 3 9 4 5 6 | 1 8 7 2 9 3 4 5 6 | 1 7 8 9 2 3 4 5 6 | 1 9 7 8 2 3 4 5 6 | 9 1 7 2 8
4 5 6 | 7 9 1 2 8 3 4 5 6 | 9 7 1 2 3 8 4 5 6 |
8 9 1 2 3 4 7 5 6 | 8 1 9 2 3 7 4 5 6 | 9 8 1 2 3 7 4 5 6 | 8 1 2 9 7 3 4 5 6 | 1 8 9 2 7 3 4
6 | 8 7 1 2 3 9 4 5 6 | 7 8 1 2 9 3 4 5 6 | 7 1 8 9 2 3 4 5 6 | 7 9 1 8 2 3 4 5 6 | 9 7 1 2 8
8 9 1 2 3 7 4 5 6 | 8 1 9 2 7 3 4 5 6 | 9 8 1 2 7 3 4 5 6 | 8 1 7 9 2 3 4 5 6 | 1 8 9 7 2 3 4
6 I
8 9 1 2 7 3 4 5 6 | 8 1 9 7 2 3 4 5 6 | 9 8 1 7 2 3 4 5 6 | 8 7 1 9 2 3 4 5 6 | 7 8 9 1 2 3 4
8 9 1 7 2 3 4 5 6 | 8 7 9 1 2 3 4 5 6 | 9 8 7 1 2 3 4 5 6 |
8 9 7 1 2 3 4 5 6 |
real
       0m12.097s
user
        0m8.548s
        0m0.215s
sys
abubakar@HP:~/Documents/talha$
```

Profile Report:

```
    □ profile_report.txt ×
abubakar > Documents > talha > = profile_report.txt
 Flat profile:
  Each sample counts as 0.01 seconds.
   no time accumulated
                                       calls Ts/call Ts/call name
           seconds
   time
                         seconds
                                        2274
                                                                        __gnu_cxx::__normal_iterator<int*, std::vector<int, std::allocator<int> > >::base() const
                                                                        __gnu_cxx::_normal_iterator<int*, std::vector<int', std::allocator<int> > >::operator*() const bool __gnu_cxx::_normal_iterator<int*, std::vector<int, std::allocator<int> > >(__gnu_cxx::_normal_iterator<int*, std::vector<int,
    0.00
                 0.00
                             0.00
                                          861
                                                    0.00
                                                                0.00
     0.00
                 0.00
                             0.00
                                          789
                                                    0.00
                                                               normal_iterator<int*, std::vector<int, std::allocator<int> > const6)

0.00 __gnu_cxx::__normal_iterator<int*, std::vector<int, std::allocator<int> > >::_normal_iterator(int* const6)

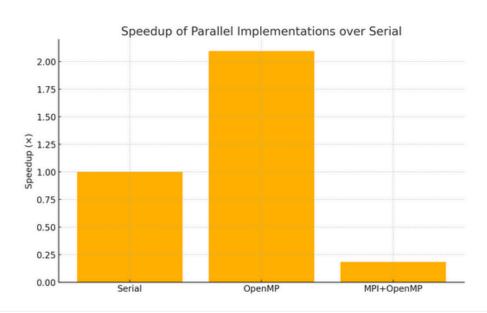
0.00 __gnu_cxx::__normal_iterator<int*, std::vector<int, std::allocator<int> > >::operator++()

0.00 _int* std::__niter_base<int*>(int*)
    std::allocator<int> > const&,
                                                 gnu_cxx::
     0.00
                             0.00
                                                    0.00
                 0.00
     0.00
                 0.00
                             0.00
                                                    0.00
     0.00
                 0.00
                             0.00
                                          475
                                                    0.00
                                                                        std::vector<int, std::allocator<int> >::size() const
     0.00
                 0.00
                             0.00
                                          390
                                                    0.00
                                                                0.00
                                                                        std::_Vector_base<int, std::allocator<int> >::_M_get_Tp_allocator()
std::vector<int, std::allocator<int> >::begin()
     0.00
                 0.00
                             0.00
                                          345
                                                    0.00
                                                                0.00
                                                                        int const& std::forward<int const&>(std::remove_reference<int const&>::type&)
                             0.00
                                          339
                                                                        std::vector<int, std::allocator<int> >::end()
     0.00
                 0.00
                                                    0.00
                                                                0.00
     0.00
                 0.00
                             0.00
                                          317
                                                    0.00
                                                                0.00
                                                                        operator new(unsigned long, void*)
std::__new_allocator<int>::_M_max_size() const
                             0.00
     0.00
                 0.00
                                          281
                                                    0.00
                                                                0.00
     0.00
                                                                        std::vector<std::vector<int, std::allocator<int> >, std::allocator<std::vector<int, std::allocator<int> > >::operator[]
    (unsigned long)
     0.00
                                          261
                                                    0.00
                                                                        std::vector<int, std::allocator<int> >* std::__addressof<std::vector<int, std::allocator<int> > >(std::vector<int,
    std::allocator<int> >&)
     0.00
                                                                        std::__new_allocator<int>::~_new_allocator()
std::_Vector_base<int, std::allocator<int> >::_M_deallocate(int*, unsigned long)
     0.00
                 0.00
                             0.00
                                          252
                                                    0.00
                                                                0.00
                                                                0.00
     0.00
                             0.00
                                                    0.00
                 0.00
                                                                        std::remove_reference<int&>::type&& std::move<int&>(int&)
std::_Vector_base<int, std::allocator<int>>::_M_get_Tp_allocator() const
     0.00
                 0.00
                             0.00
                                          233
                                                    0.00
                                                                0.00
                             0.00
                                          193
     0.00
                 0.00
                                                    0.00
                                                                0.00
     0.00
                 0.00
                              0.00
                                                    0.00
                                                                        std::_Vector_base<int, std::allocator<int> >::_Vector_impl::~_Vector_impl()
                                                                        void std::_Destroy_aux<true>::__destroy<int*>(int*, int*)
std::_Vector_base<int, std::allocator<int> >::~_Vector_base()
     0.00
                 0.00
                             0.00
                                          175
                                                    0.00
                                                                0.00
                                                                        std::vector<int, std::allocator<int> >::operator[](unsigned long)
std::vector<int, std::allocator<int> >::~vector()
     0.00
                 0.00
                             0.00
                                          175
                                                    0.00
                                                                0.00
                                                                        void std::_Destroy<int*>(int*, int*)
std::__new_allocator<int>::__new_allocator<int> const&)
     0.00
                 0.00
                             0.00
                                          172
                                                    0.00
                             0.00
     0.00
                 0.00
                                          168
                                                    0.00
                                                                0.00
     0.00
                 0.00
                             0.00
                                          167
                                                    0.00
                                                                        std::allocator<int>::allocator(std::allocator<int> const&)
                                                                        void std::_Destroy<int*, int>(int*, int*, std::allocator<int>&)
                             0.00
     0.00
                 0.00
```

OpenMP and MPI Performance:

```
user@user-Precision-7510:~$ mpic++ -fopenmp a.cpp -o hello
a.cpp: In function 'void level_order_tree(const Permutation&, const IST&)':
a.cpp:50:22: warning: structured bindings only available with '-std=c++17' or '-std=gnu++17'
   50 I
             for (const auto &[child, parent] : tree) {
a.cpp:55:16: warning: structured bindings only available with '-std=c++17' or '-std=gnu++17'
             for (auto &[parent, children] : children map) {
   55 I
a.cpp: In function 'std::vector<int> serializeIST(const IST&, int)':
a.cpp:146:22: warning: structured bindings only available with '-std=c++17' or '-std=gnu++17'
            for (const auto& [child, parent] : ist) {
user@user-Precision-7510:~$ scp hello user@192.168.18.129:~/
hello
user@user-Precision-7510:~$ mpirun -np 4 --hostfile hosts --prefix /usr/local ./hello
Degree: 9
Degree: 9
Degree: 9
Degree: 9
Total execution time: 90.8495 seconds.
```

SpeedUp Graph:



Performance Table

Speedup([3])	Execution Time (s)	Implementation
1.00	16.34	Serial
2.10	7.80	OpenMP
0.18	88.823	MPI + OpenMP