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## Convolutional Neural Networks (CNNs / ConvNets)

Convolutional Neural Networks are very similar to ordinary Neural Networks from the previous chapter: they are made up of neurons that have learnable weights and biases. Each neuron receives some inputs, performs a dot product and optionally follows it with a non-linearity. The whole network still expresses a single differentiable score function: from the raw image pixels on one end to class scores at the other. And they still have a loss function (e.g. SVM/Softmax) on the last (fully-connected) layer and all the tips/tricks we developed for learning regular Neural Networks still apply.

So what does change? ConvNet architectures make the explicit assumption that the inputs are images, which allows us to encode certain properties into the architecture. These then make the forward function more efficient to implement and vastly reduce the amount of parameters in the network.

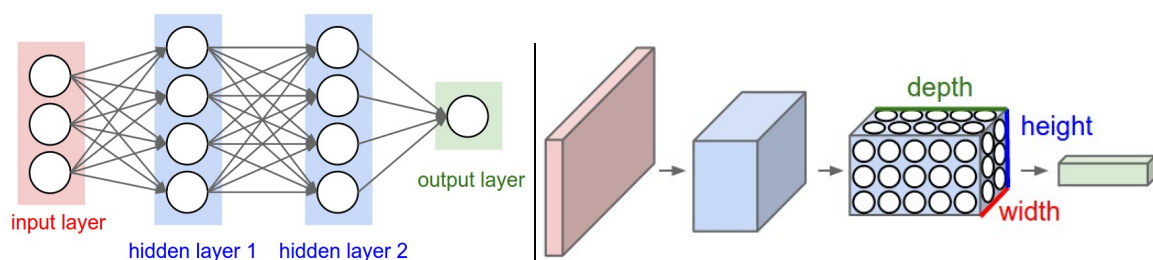
## Architecture Overview

*Recall: Regular Neural Nets.* As we saw in the previous chapter, Neural Networks receive an input (a single vector), and transform it through a series of *hidden layers*. Each hidden layer is made up of a set of neurons, where each neuron is fully connected to all neurons in the previous layer, and where neurons in a single layer function completely independently and do not share

any connections. The last fully-connected layer is called the “output layer” and in classification settings it represents the class scores.

*Regular Neural Nets don't scale well to full images.* In CIFAR-10, images are only of size  $32 \times 32 \times 3$  (32 wide, 32 high, 3 color channels), so a single fully-connected neuron in a first hidden layer of a regular Neural Network would have  $32 \times 32 \times 3 = 3072$  weights. This amount still seems manageable, but clearly this fully-connected structure does not scale to larger images. For example, an image of more respectable size, e.g.  $200 \times 200 \times 3$ , would lead to neurons that have  $200 \times 200 \times 3 = 120,000$  weights. Moreover, we would almost certainly want to have several such neurons, so the parameters would add up quickly! Clearly, this full connectivity is wasteful and the huge number of parameters would quickly lead to overfitting.

*3D volumes of neurons.* Convolutional Neural Networks take advantage of the fact that the input consists of images and they constrain the architecture in a more sensible way. In particular, unlike a regular Neural Network, the layers of a ConvNet have neurons arranged in 3 dimensions: **width, height, depth**. (Note that the word *depth* here refers to the third dimension of an activation volume, not to the depth of a full Neural Network, which can refer to the total number of layers in a network.) For example, the input images in CIFAR-10 are an input volume of activations, and the volume has dimensions  $32 \times 32 \times 3$  (width, height, depth respectively). As we will soon see, the neurons in a layer will only be connected to a small region of the layer before it, instead of all of the neurons in a fully-connected manner. Moreover, the final output layer would for CIFAR-10 have dimensions  $1 \times 1 \times 10$ , because by the end of the ConvNet architecture we will reduce the full image into a single vector of class scores, arranged along the depth dimension. Here is a visualization:



Left: A regular 3-layer Neural Network. Right: A ConvNet arranges its neurons in three dimensions (width, height, depth), as visualized in one of the layers. Every layer of a ConvNet transforms the 3D input volume to a 3D output volume of neuron activations. In this example, the red input layer holds the image, so its width and height would be the dimensions of the image, and the depth would be 3 (Red, Green, Blue channels).

*A ConvNet is made up of Layers. Every Layer has a simple API: It transforms an input 3D volume to an output 3D volume with some differentiable function that may or may not have parameters.*

# Layers used to build ConvNets

As we described above, a simple ConvNet is a sequence of layers, and every layer of a ConvNet transforms one volume of activations to another through a differentiable function. We use three main types of layers to build ConvNet architectures: **Convolutional Layer**, **Pooling Layer**, and **Fully-Connected Layer** (exactly as seen in regular Neural Networks). We will stack these layers to form a full ConvNet **architecture**.

*Example Architecture: Overview.* We will go into more details below, but a simple ConvNet for CIFAR-10 classification could have the architecture [INPUT - CONV - RELU - POOL - FC]. In more detail:

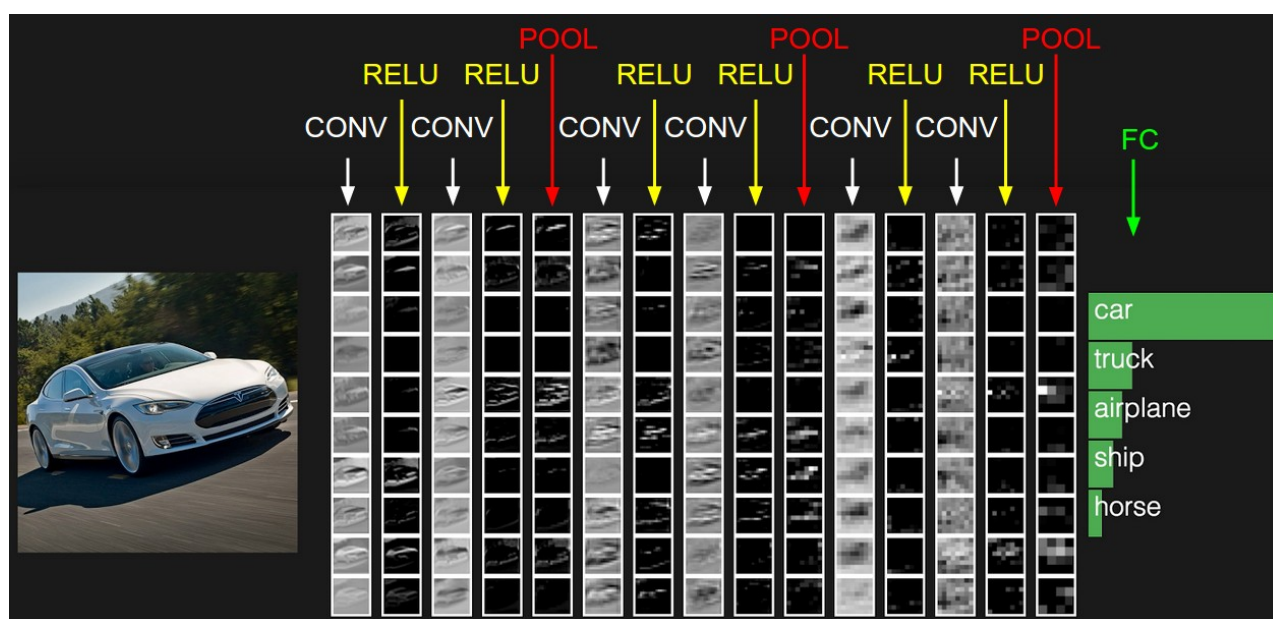
- INPUT [32x32x3] will hold the raw pixel values of the image, in this case an image of width 32, height 32, and with three color channels R,G,B.
- CONV layer will compute the output of neurons that are connected to local regions in the input, each computing a dot product between their weights and a small region they are connected to in the input volume. This may result in volume such as [32x32x12] if we decided to use 12 filters.
- RELU layer will apply an elementwise activation function, such as the  $\max(0, x)$  thresholding at zero. This leaves the size of the volume unchanged ([32x32x12]).
- POOL layer will perform a downsampling operation along the spatial dimensions (width, height), resulting in volume such as [16x16x12].
- FC (i.e. fully-connected) layer will compute the class scores, resulting in volume of size [1x1x10], where each of the 10 numbers correspond to a class score, such as among the 10 categories of CIFAR-10. As with ordinary Neural Networks and as the name implies, each neuron in this layer will be connected to all the numbers in the previous volume.

In this way, ConvNets transform the original image layer by layer from the original pixel values to the final class scores. Note that some layers contain parameters and other don't. In particular, the CONV/FC layers perform transformations that are a function of not only the activations in the input volume, but also of the parameters (the weights and biases of the neurons). On the other hand, the RELU/POOL layers will implement a fixed function. The parameters in the CONV/FC layers will be trained with gradient descent so that the class scores that the ConvNet computes are consistent with the labels in the training set for each image.

In summary:

- A ConvNet architecture is in the simplest case a list of Layers that transform the image volume into an output volume (e.g. holding the class scores)
- There are a few distinct types of Layers (e.g. CONV/FC/RELU/POOL are by far the most popular)
- Each Layer accepts an input 3D volume and transforms it to an output 3D volume through a differentiable function
- Each Layer may or may not have parameters (e.g. CONV/FC do, RELU/POOL don't)

- Each Layer may or may not have additional hyperparameters (e.g. CONV/FC/POOL do, RELU doesn't)



The activations of an example ConvNet architecture. The initial volume stores the raw image pixels (left) and the last volume stores the class scores (right). Each volume of activations along the processing path is shown as a column. Since it's difficult to visualize 3D volumes, we lay out each volume's slices in rows. The last layer volume holds the scores for each class, but here we only visualize the sorted top 5 scores, and print the labels of each one. The full [web-based demo](#) is shown in the header of our website. The architecture shown here is a tiny VGG Net, which we will discuss later.

We now describe the individual layers and the details of their hyperparameters and their connectivities.

## Convolutional Layer

The Conv layer is the core building block of a Convolutional Network that does most of the computational heavy lifting.

**Overview and intuition without brain stuff.** Lets first discuss what the CONV layer computes without brain/neuron analogies. The CONV layer's parameters consist of a set of learnable filters. Every filter is small spatially (along width and height), but extends through the full depth of the input volume. For example, a typical filter on a first layer of a ConvNet might have size 5x5x3 (i.e. 5 pixels width and height, and 3 because images have depth 3, the color channels). During the forward pass, we slide (more precisely, convolve) each filter across the width and height of the input volume and compute dot products between the entries of the filter and the input at any position. As we slide the filter over the width and height of the input volume we will produce a 2-dimensional activation map that gives the responses of that filter at every spatial position. Intuitively, the network will learn filters that activate when they see some type of visual feature such as an edge of some orientation or a blotch of some color on the first layer, or eventually

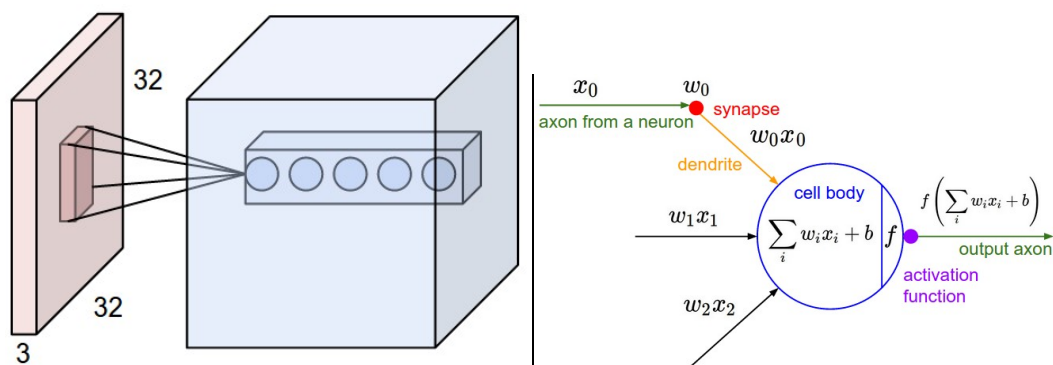
entire honeycomb or wheel-like patterns on higher layers of the network. Now, we will have an entire set of filters in each CONV layer (e.g. 12 filters), and each of them will produce a separate 2-dimensional activation map. We will stack these activation maps along the depth dimension and produce the output volume.

**The brain view.** If you're a fan of the brain/neuron analogies, every entry in the 3D output volume can also be interpreted as an output of a neuron that looks at only a small region in the input and shares parameters with all neurons to the left and right spatially (since these numbers all result from applying the same filter). We now discuss the details of the neuron connectivities, their arrangement in space, and their parameter sharing scheme.

**Local Connectivity.** When dealing with high-dimensional inputs such as images, as we saw above it is impractical to connect neurons to all neurons in the previous volume. Instead, we will connect each neuron to only a local region of the input volume. The spatial extent of this connectivity is a hyperparameter called the **receptive field** of the neuron (equivalently this is the filter size). The extent of the connectivity along the depth axis is always equal to the depth of the input volume. It is important to emphasize again this asymmetry in how we treat the spatial dimensions (width and height) and the depth dimension: The connections are local in space (along width and height), but always full along the entire depth of the input volume.

*Example 1.* For example, suppose that the input volume has size  $[32 \times 32 \times 3]$ , (e.g. an RGB CIFAR-10 image). If the receptive field (or the filter size) is  $5 \times 5$ , then each neuron in the Conv Layer will have weights to a  $[5 \times 5 \times 3]$  region in the input volume, for a total of  $5 \times 5 \times 3 = 75$  weights (and +1 bias parameter). Notice that the extent of the connectivity along the depth axis must be 3, since this is the depth of the input volume.

*Example 2.* Suppose an input volume had size  $[16 \times 16 \times 20]$ . Then using an example receptive field size of  $3 \times 3$ , every neuron in the Conv Layer would now have a total of  $3 \times 3 \times 20 = 180$  connections to the input volume. Notice that, again, the connectivity is local in space (e.g.  $3 \times 3$ ), but full along the input depth (20).



**Left:** An example input volume in red (e.g. a  $32 \times 32 \times 3$  CIFAR-10 image), and an example volume of neurons in the first Convolutional layer. Each neuron in the convolutional layer is connected only to a local region in the input volume spatially, but to the full depth (i.e. all color channels). Note, there are multiple neurons (5 in this example) along the depth, all looking at the same region in the input - see discussion of depth columns in text below. **Right:** The neurons from the Neural Network chapter remain

unchanged: They still compute a dot product of their weights with the input followed by a non-linearity, but their connectivity is now restricted to be local spatially.

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**Spatial arrangement.** We have explained the connectivity of each neuron in the Conv Layer to the input volume, but we haven't yet discussed how many neurons there are in the output volume or how they are arranged. Three hyperparameters control the size of the output volume: the **depth**, **stride** and **zero-padding**. We discuss these next:

1. First, the **depth** of the output volume is a hyperparameter: it corresponds to the number of filters we would like to use, each learning to look for something different in the input. For example, if the first Convolutional Layer takes as input the raw image, then different neurons along the depth dimension may activate in presence of various oriented edged, or blobs of color. We will refer to a set of neurons that are all looking at the same region of the input as a **depth column** (some people also prefer the term *fibre*).
2. Second, we must specify the **stride** with which we slide the filter. When the stride is 1 then we move the filters one pixel at a time. When the stride is 2 (or uncommonly 3 or more, though this is rare in practice) then the filters jump 2 pixels at a time as we slide them around. This will produce smaller output volumes spatially.
3. As we will soon see, sometimes it will be convenient to pad the input volume with zeros around the border. The size of this **zero-padding** is a hyperparameter. The nice feature of zero padding is that it will allow us to control the spatial size of the output volumes (most commonly as we'll see soon we will use it to exactly preserve the spatial size of the input volume so the input and output width and height are the same).

We can compute the spatial size of the output volume as a function of the input volume size ( $W$ ), the receptive field size of the Conv Layer neurons ( $F$ ), the stride with which they are applied ( $S$ ), and the amount of zero padding used ( $P$ ) on the border. You can convince yourself that the correct formula for calculating how many neurons "fit" is given by  $(W - F + 2P)/S + 1$ . For example for a 7x7 input and a 3x3 filter with stride 1 and pad 0 we would get a 5x5 output. With stride 2 we would get a 3x3 output. Lets also see one more graphical example:

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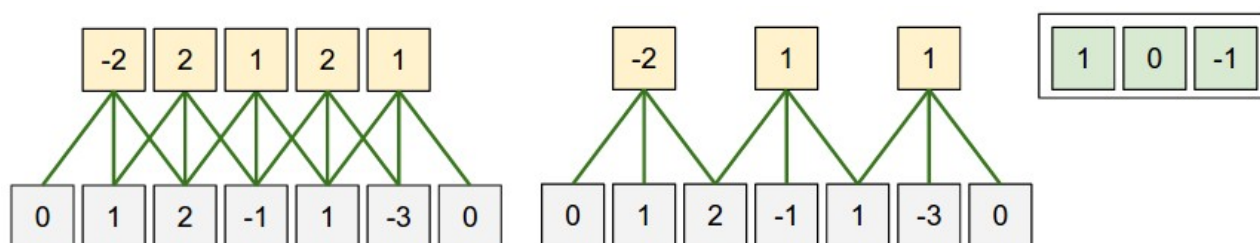


Illustration of spatial arrangement. In this example there is only one spatial dimension (x-axis), one neuron with a receptive field size of  $F = 3$ , the input size is  $W = 5$ , and there is zero padding of  $P = 1$ . **Left:** The neuron strided across the input in stride of  $S = 1$ , giving output of size  $(5 - 3 + 2)/1 + 1 = 5$ . **Right:** The neuron uses stride of  $S = 2$ , giving output of size  $(5 - 3 + 2)/2 + 1 = 3$ . Notice that stride  $S = 3$  could not be used since it wouldn't fit neatly across the volume. In terms of the equation, this can be determined since  $(5 - 3 + 2) = 4$  is not divisible by 3.

The neuron weights are in this example [1,0,-1] (shown on very right), and its bias is zero. These weights are shared across all yellow neurons (see parameter sharing below).

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*Use of zero-padding.* In the example above on left, note that the input dimension was 5 and the output dimension was equal: also 5. This worked out so because our receptive fields were 3 and we used zero padding of 1. If there was no zero-padding used, then the output volume would have had spatial dimension of only 3, because that it is how many neurons would have "fit" across the original input. In general, setting zero padding to be  $P = (F - 1)/2$  when the stride is  $S = 1$  ensures that the input volume and output volume will have the same size spatially. It is very common to use zero-padding in this way and we will discuss the full reasons when we talk more about ConvNet architectures.

*Constraints on strides.* Note again that the spatial arrangement hyperparameters have mutual constraints. For example, when the input has size  $W = 10$ , no zero-padding is used  $P = 0$ , and the filter size is  $F = 3$ , then it would be impossible to use stride  $S = 2$ , since  $(W - F + 2P)/S + 1 = (10 - 3 + 0)/2 + 1 = 4.5$ , i.e. not an integer, indicating that the neurons don't "fit" neatly and symmetrically across the input. Therefore, this setting of the hyperparameters is considered to be invalid, and a ConvNet library could throw an exception or zero pad the rest to make it fit, or crop the input to make it fit, or something. As we will see in the ConvNet architectures section, sizing the ConvNets appropriately so that all the dimensions "work out" can be a real headache, which the use of zero-padding and some design guidelines will significantly alleviate.

*Real-world example.* The [Krizhevsky et al.](#) architecture that won the ImageNet challenge in 2012 accepted images of size [227x227x3]. On the first Convolutional Layer, it used neurons with receptive field size  $F = 11$ , stride  $S = 4$  and no zero padding  $P = 0$ . Since  $(227 - 11)/4 + 1 = 55$ , and since the Conv layer had a depth of  $K = 96$ , the Conv layer output volume had size [55x55x96]. Each of the 55\*55\*96 neurons in this volume was connected to a region of size [11x11x3] in the input volume. Moreover, all 96 neurons in each depth column are connected to the same [11x11x3] region of the input, but of course with different weights. As a fun aside, if you read the actual paper it claims that the input images were 224x224, which is surely incorrect because  $(224 - 11)/4 + 1$  is quite clearly not an integer. This has confused many people in the history of ConvNets and little is known about what happened. My own best guess is that Alex used zero-padding of 3 extra pixels that he does not mention in the paper.

**Parameter Sharing.** Parameter sharing scheme is used in Convolutional Layers to control the number of parameters. Using the real-world example above, we see that there are 55\*55\*96 = 290,400 neurons in the first Conv Layer, and each has 11\*11\*3 = 363 weights and 1 bias. Together, this adds up to 290400 \* 364 = 105,705,600 parameters on the first layer of the ConvNet alone. Clearly, this number is very high.

It turns out that we can dramatically reduce the number of parameters by making one reasonable assumption: That if one feature is useful to compute at some spatial position (x,y),



then it should also be useful to compute at a different position  $(x_2, y_2)$ . In other words, denoting a single 2-dimensional slice of depth as a **depth slice** (e.g. a volume of size  $[55 \times 55 \times 96]$  has 96 depth slices, each of size  $[55 \times 55]$ ), we are going to constrain the neurons in each depth slice to use the same weights and bias. With this parameter sharing scheme, the first Conv Layer in our example would now have only 96 unique set of weights (one for each depth slice), for a total of  $96 \times 11 \times 11 \times 3 = 34,848$  unique weights, or 34,944 parameters (+96 biases). Alternatively, all  $55 \times 55$  neurons in each depth slice will now be using the same parameters. In practice during backpropagation, every neuron in the volume will compute the gradient for its weights, but these gradients will be added up across each depth slice and only update a single set of weights per slice.

Notice that if all neurons in a single depth slice are using the same weight vector, then the forward pass of the CONV layer can in each depth slice be computed as a **convolution** of the neuron's weights with the input volume (Hence the name: Convolutional Layer). This is why it is common to refer to the sets of weights as a **filter** (or a **kernel**), that is convolved with the input.

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Example filters learned by Krizhevsky et al. Each of the 96 filters shown here is of size  $[11 \times 11 \times 3]$ , and each one is shared by the  $55 \times 55$  neurons in one depth slice. Notice that the parameter sharing assumption is relatively reasonable: If detecting a horizontal edge is important at some location in the image, it should intuitively be useful at some other location as well due to the translationally-invariant structure of images. There is therefore no need to relearn to detect a horizontal edge at every one of the  $55 \times 55$  distinct locations in the Conv layer output volume.

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Note that sometimes the parameter sharing assumption may not make sense. This is especially the case when the input images to a ConvNet have some specific centered structure, where we should expect, for example, that completely different features should be learned on one side of the image than another. One practical example is when the input are faces that have been centered in the image. You might expect that different eye-specific or hair-specific features could (and should) be learned in different spatial locations. In that case it is common to relax the parameter sharing scheme, and instead simply call the layer a **Locally-Connected Layer**.



**Numpy examples.** To make the discussion above more concrete, let's express the same ideas but in code and with a specific example. Suppose that the input volume is a numpy array `X`. Then:

- A *depth column* (or a *fibre*) at position `(x,y)` would be the activations `X[x,y,:]`.
- A *depth slice*, or equivalently an *activation map* at depth `d` would be the activations `X[:, :, d]`.

*Conv Layer Example.* Suppose that the input volume `X` has shape `X.shape: (11,11,4)`. Suppose further that we use no zero padding ( $P = 0$ ), that the filter size is  $F = 5$ , and that the stride is  $S = 2$ . The output volume would therefore have spatial size  $(11-5)/2+1 = 4$ , giving a volume with width and height of 4. The activation map in the output volume (call it `V`), would then look as follows (only some of the elements are computed in this example):

- `V[0,0,0] = np.sum(X[:5,:5,:] * w0) + b0`
- `V[1,0,0] = np.sum(X[2:7,:5,:] * w0) + b0`
- `V[2,0,0] = np.sum(X[4:9,:5,:] * w0) + b0`
- `V[3,0,0] = np.sum(X[6:11,:5,:] * w0) + b0`

Remember that in numpy, the operation `*` above denotes elementwise multiplication between the arrays. Notice also that the weight vector `w0` is the weight vector of that neuron and `b0` is the bias. Here, `w0` is assumed to be of shape `w0.shape: (5,5,4)`, since the filter size is 5 and the depth of the input volume is 4. Notice that at each point, we are computing the dot product as seen before in ordinary neural networks. Also, we see that we are using the same weight and bias (due to parameter sharing), and where the dimensions along the width are increasing in steps of 2 (i.e. the stride). To construct a second activation map in the output volume, we would have:

- `V[0,0,1] = np.sum(X[:5,:5,:] * w1) + b1`
- `V[1,0,1] = np.sum(X[2:7,:5,:] * w1) + b1`
- `V[2,0,1] = np.sum(X[4:9,:5,:] * w1) + b1`
- `V[3,0,1] = np.sum(X[6:11,:5,:] * w1) + b1`
- `V[0,1,1] = np.sum(X[:5,2:7,:] * w1) + b1` (example of going along y)
- `V[2,3,1] = np.sum(X[4:9,6:11,:] * w1) + b1` (or along both)

where we see that we are indexing into the second depth dimension in `V` (at index 1) because we are computing the second activation map, and that a different set of parameters (`w1`) is now used. In the example above, we are for brevity leaving out some of the other operations the Conv Layer would perform to fill the other parts of the output array `V`. Additionally, recall that these activation maps are often followed elementwise through an activation function such as ReLU, but this is not shown here.

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .
- Produces a volume of size  $W_2 \times H_2 \times D_2$  where:
  - $W_2 = (W_1 - F + 2P)/S + 1$
  - $H_2 = (H_1 - F + 2P)/S + 1$  (i.e. width and height are computed equally by symmetry)
  - $D_2 = K$
- With parameter sharing, it introduces  $F \cdot F \cdot D_1$  weights per filter, for a total of  $(F \cdot F \cdot D_1) \cdot K$  weights and  $K$  biases.
- In the output volume, the  $d$ -th depth slice (of size  $W_2 \times H_2$ ) is the result of performing a valid convolution of the  $d$ -th filter over the input volume with a stride of  $S$ , and then offset by  $d$ -th bias.

A common setting of the hyperparameters is  $F = 3, S = 1, P = 1$ . However, there are common conventions and rules of thumb that motivate these hyperparameters. See the [ConvNet architectures](#) section below.

**Convolution Demo.** Below is a running demo of a CONV layer. Since 3D volumes are hard to visualize, all the volumes (the input volume (in blue), the weight volumes (in red), the output volume (in green)) are visualized with each depth slice stacked in rows. The input volume is of size  $W_1 = 5, H_1 = 5, D_1 = 3$ , and the CONV layer parameters are  $K = 2, F = 3, S = 2, P = 1$ . That is, we have two filters of size  $3 \times 3$ , and they are applied with a stride of 2. Therefore, the output volume size has spatial size  $(5 - 3 + 2)/2 + 1 = 3$ . Moreover, notice that a padding of  $P = 1$  is applied to the input volume, making the outer border of the input volume zero. The visualization below iterates over the output activations (green), and shows that each element is computed by elementwise multiplying the highlighted input (blue) with the filter (red), summing it up, and then offsetting the result by the bias.

Input Volume (+pad 1) (7x7x3)

$x[:, :, 0]$						
0	0	0	0	0	0	0
0	2	0	2	1	0	0
0	2	1	0	2	0	0
0	2	1	1	0	0	0
0	0	0	2	2	0	0
0	0	1	0	2	0	0
0	0	0	0	0	0	0
$x[:, :, 1]$						
0	0	0	0	0	0	0
0	1	1	0	2	0	0
0	1	2	0	1	0	0
0	2	2	2	1	1	0
0	2	1	2	2	0	0
0	0	0	1	2	0	0
0	0	0	0	0	0	0
$x[:, :, 2]$						
0	0	0	0	0	0	0
0	0	1	0	1	2	0
0	0	2	1	0	2	0
0	1	2	2	0	0	0
0	1	0	0	2	1	0
0	1	0	2	0	0	0
0	0	0	0	0	0	0

Filter W0 (3x3x3)

$w0[:, :, 0]$		
-1	0	1
-1	0	-1
-1	-1	1
$w0[:, :, 1]$		
0	1	0
0	0	0
-1	1	1
$w0[:, :, 2]$		
0	0	1
0	0	0
1	-1	-1
Bias $b0$ (1x1x1)		
$b0[:, :, 0]$		
1		

Filter W1 (3x3x3)

$w1[:, :, 0]$		
1	1	1
1	1	0
1	0	-1
$w1[:, :, 1]$		
-1	0	0
0	0	-1
-1	1	-1
$w1[:, :, 2]$		
-1	0	0
-1	0	1
0	1	-1
Bias $b1$ (1x1x1)		
$b1[:, :, 0]$		
0		

Output

$o[:, :]$	
1	1
6	2
2	4
$o[:, :]$	
-2	-3
7	-7
0	2

toggle movement

**Implementation as Matrix Multiplication.** Note that the convolution operation essentially performs dot products between the filters and local regions of the input. A common implementation pattern of the CONV layer is to take advantage of this fact and formulate the forward pass of a convolutional layer as one big matrix multiply as follows:

1. The local regions in the input image are stretched out into columns in an operation commonly called **im2col**. For example, if the input is  $[227 \times 227 \times 3]$  and it is to be convolved with  $11 \times 11 \times 3$  filters at stride 4, then we would take  $[11 \times 11 \times 3]$  blocks of pixels in the input and stretch each block into a column vector of size  $11 \times 11 \times 3 = 363$ . Iterating this process in the input at stride of 4 gives  $(227-11)/4+1 = 55$  locations along both width and height, leading to an output matrix **x\_col** of *im2col* of size  $[363 \times 3025]$ , where every column is

a stretched out receptive field and there are  $55 \times 55 = 3025$  of them in total. Note that since the receptive fields overlap, every number in the input volume may be duplicated in multiple distinct columns.

2. The weights of the CONV layer are similarly stretched out into rows. For example, if there are 96 filters of size  $[1 \times 1 \times 1 \times 3]$  this would give a matrix `W_row` of size  $[96 \times 363]$ .
3. The result of a convolution is now equivalent to performing one large matrix multiply `np.dot(W_row, X_col)`, which evaluates the dot product between every filter and every receptive field location. In our example, the output of this operation would be  $[96 \times 3025]$ , giving the output of the dot product of each filter at each location.
4. The result must finally be reshaped back to its proper output dimension  $[55 \times 55 \times 96]$ .

This approach has the downside that it can use a lot of memory, since some values in the input volume are replicated multiple times in `X_col`. However, the benefit is that there are many very efficient implementations of Matrix Multiplication that we can take advantage of (for example, in the commonly used [BLAS](#) API). Moreover, the same *im2col* idea can be reused to perform the pooling operation, which we discuss next.

**Backpropagation.** The backward pass for a convolution operation (for both the data and the weights) is also a convolution (but with spatially-flipped filters). This is easy to derive in the 1-dimensional case with a toy example (not expanded on for now).

**1x1 convolution.** As an aside, several papers use  $1 \times 1$  convolutions, as first investigated by [Network in Network](#). Some people are at first confused to see  $1 \times 1$  convolutions especially when they come from signal processing background. Normally signals are 2-dimensional so  $1 \times 1$  convolutions do not make sense (it's just pointwise scaling). However, in ConvNets this is not the case because one must remember that we operate over 3-dimensional volumes, and that the filters always extend through the full depth of the input volume. For example, if the input is  $[32 \times 32 \times 3]$  then doing  $1 \times 1$  convolutions would effectively be doing 3-dimensional dot products (since the input depth is 3 channels).

**Dilated convolutions.** A recent development (e.g. see [paper by Fisher Yu and Vladlen Koltun](#)) is to introduce one more hyperparameter to the CONV layer called the *dilation*. So far we've only discussed CONV filters that are contiguous. However, it's possible to have filters that have spaces between each cell, called dilation. As an example, in one dimension a filter `w` of size 3 would compute over input `x` the following: `w[0]*x[0] + w[1]*x[1] + w[2]*x[2]`. This is dilation of 0. For dilation 1 the filter would instead compute `w[0]*x[0] + w[1]*x[2] + w[2]*x[4]`; In other words there is a gap of 1 between the applications. This can be very useful in some settings to use in conjunction with 0-dilated filters because it allows you to merge spatial information across the inputs much more aggressively with fewer layers. For example, if you stack two  $3 \times 3$  CONV layers on top of each other than you can convince yourself that the neurons on the 2nd layer are a function of a  $5 \times 5$  patch of the input (we would say that the *effective receptive field* of these neurons is  $5 \times 5$ ). If we use dilated convolutions then this effective receptive field would grow much quicker.

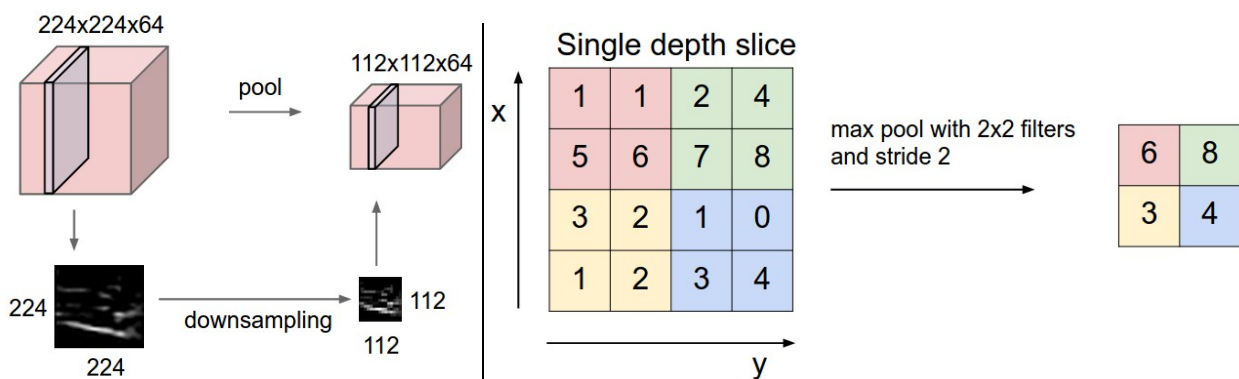
## Pooling Layer

It is common to periodically insert a Pooling layer in-between successive Conv layers in a ConvNet architecture. Its function is to progressively reduce the spatial size of the representation to reduce the amount of parameters and computation in the network, and hence to also control overfitting. The Pooling Layer operates independently on every depth slice of the input and resizes it spatially, using the MAX operation. The most common form is a pooling layer with filters of size  $2 \times 2$  applied with a stride of 2 downsamples every depth slice in the input by 2 along both width and height, discarding 75% of the activations. Every MAX operation would in this case be taking a max over 4 numbers (little  $2 \times 2$  region in some depth slice). The depth dimension remains unchanged. More generally, the pooling layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires two hyperparameters:
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
- Produces a volume of size  $W_2 \times H_2 \times D_2$  where:
  - $W_2 = (W_1 - F)/S + 1$
  - $H_2 = (H_1 - F)/S + 1$
  - $D_2 = D_1$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

It is worth noting that there are only two commonly seen variations of the max pooling layer found in practice: A pooling layer with  $F = 3, S = 2$  (also called overlapping pooling), and more commonly  $F = 2, S = 2$ . Pooling sizes with larger receptive fields are too destructive.

**General pooling.** In addition to max pooling, the pooling units can also perform other functions, such as *average pooling* or even *L2-norm pooling*. Average pooling was often used historically but has recently fallen out of favor compared to the max pooling operation, which has been shown to work better in practice.



Pooling layer downsamples the volume spatially, independently in each depth slice of the input volume.

**Left:** In this example, the input volume of size  $[224 \times 224 \times 64]$  is pooled with filter size 2, stride 2 into output volume of size  $[112 \times 112 \times 64]$ . Notice that the volume depth is preserved. **Right:** The most

common downsampling operation is max, giving rise to **max pooling**, here shown with a stride of 2. That is, each max is taken over 4 numbers (little 2x2 square).

---

**Backpropagation.** Recall from the backpropagation chapter that the backward pass for a  $\max(x, y)$  operation has a simple interpretation as only routing the gradient to the input that had the highest value in the forward pass. Hence, during the forward pass of a pooling layer it is common to keep track of the index of the max activation (sometimes also called *the switches*) so that gradient routing is efficient during backpropagation.

**Getting rid of pooling.** Many people dislike the pooling operation and think that we can get away without it. For example, [Striving for Simplicity: The All Convolutional Net](#) proposes to discard the pooling layer in favor of architecture that only consists of repeated CONV layers. To reduce the size of the representation they suggest using larger stride in CONV layer once in a while. Discarding pooling layers has also been found to be important in training good generative models, such as variational autoencoders (VAEs) or generative adversarial networks (GANs). It seems likely that future architectures will feature very few to no pooling layers.

## Normalization Layer

Many types of normalization layers have been proposed for use in ConvNet architectures, sometimes with the intentions of implementing inhibition schemes observed in the biological brain. However, these layers have since fallen out of favor because in practice their contribution has been shown to be minimal, if any. For various types of normalizations, see the discussion in Alex Krizhevsky's [cuda-convnet library API](#).

## Fully-connected layer

Neurons in a fully connected layer have full connections to all activations in the previous layer, as seen in regular Neural Networks. Their activations can hence be computed with a matrix multiplication followed by a bias offset. See the *Neural Network* section of the notes for more information.

## Converting FC layers to CONV layers

It is worth noting that the only difference between FC and CONV layers is that the neurons in the CONV layer are connected only to a local region in the input, and that many of the neurons in a CONV volume share parameters. However, the neurons in both layers still compute dot products, so their functional form is identical. Therefore, it turns out that it's possible to convert between FC and CONV layers:

- For any CONV layer there is an FC layer that implements the same forward function. The weight matrix would be a large matrix that is mostly zero except for at certain blocks (due



to local connectivity) where the weights in many of the blocks are equal (due to parameter sharing).

- Conversely, any FC layer can be converted to a CONV layer. For example, an FC layer with  $K = 4096$  that is looking at some input volume of size  $7 \times 7 \times 512$  can be equivalently expressed as a CONV layer with  $F = 7, P = 0, S = 1, K = 4096$ . In other words, we are setting the filter size to be exactly the size of the input volume, and hence the output will simply be  $1 \times 1 \times 4096$  since only a single depth column "fits" across the input volume, giving identical result as the initial FC layer.

**FC->CONV conversion.** Of these two conversions, the ability to convert an FC layer to a CONV layer is particularly useful in practice. Consider a ConvNet architecture that takes a  $224 \times 224 \times 3$  image, and then uses a series of CONV layers and POOL layers to reduce the image to an activations volume of size  $7 \times 7 \times 512$  (in an AlexNet architecture that we'll see later, this is done by use of 5 pooling layers that downsample the input spatially by a factor of two each time, making the final spatial size  $224/2/2/2/2/2 = 7$ ). From there, an AlexNet uses two FC layers of size 4096 and finally the last FC layers with 1000 neurons that compute the class scores. We can convert each of these three FC layers to CONV layers as described above:

- Replace the first FC layer that looks at  $[7 \times 7 \times 512]$  volume with a CONV layer that uses filter size  $F = 7$ , giving output volume  $[1 \times 1 \times 4096]$ .
- Replace the second FC layer with a CONV layer that uses filter size  $F = 1$ , giving output volume  $[1 \times 1 \times 4096]$
- Replace the last FC layer similarly, with  $F = 1$ , giving final output  $[1 \times 1 \times 1000]$

Each of these conversions could in practice involve manipulating (e.g. reshaping) the weight matrix  $W$  in each FC layer into CONV layer filters. It turns out that this conversion allows us to "slide" the original ConvNet very efficiently across many spatial positions in a larger image, in a single forward pass.

For example, if  $224 \times 224$  image gives a volume of size  $[7 \times 7 \times 512]$  - i.e. a reduction by 32, then forwarding an image of size  $384 \times 384$  through the converted architecture would give the equivalent volume in size  $[12 \times 12 \times 512]$ , since  $384/32 = 12$ . Following through with the next 3 CONV layers that we just converted from FC layers would now give the final volume of size  $[6 \times 6 \times 1000]$ , since  $(12 - 7)/1 + 1 = 6$ . Note that instead of a single vector of class scores of size  $[1 \times 1 \times 1000]$ , we're now getting an entire  $6 \times 6$  array of class scores across the  $384 \times 384$  image.

*Evaluating the original ConvNet (with FC layers) independently across  $224 \times 224$  crops of the  $384 \times 384$  image in strides of 32 pixels gives an identical result to forwarding the converted ConvNet one time.*

Naturally, forwarding the converted ConvNet a single time is much more efficient than iterating the original ConvNet over all those 36 locations, since the 36 evaluations share computation. This trick is often used in practice to get better performance, where for example, it is common

to resize an image to make it bigger, use a converted ConvNet to evaluate the class scores at many spatial positions and then average the class scores.

Lastly, what if we wanted to efficiently apply the original ConvNet over the image but at a stride smaller than 32 pixels? We could achieve this with multiple forward passes. For example, note that if we wanted to use a stride of 16 pixels we could do so by combining the volumes received by forwarding the converted ConvNet twice: First over the original image and second over the image but with the image shifted spatially by 16 pixels along both width and height.

- An IPython Notebook on [Net Surgery](#) shows how to perform the conversion in practice, in code (using Caffe)

## ConvNet Architectures

We have seen that Convolutional Networks are commonly made up of only three layer types: CONV, POOL (we assume Max pool unless stated otherwise) and FC (short for fully-connected). We will also explicitly write the RELU activation function as a layer, which applies elementwise non-linearity. In this section we discuss how these are commonly stacked together to form entire ConvNets.

### Layer Patterns

The most common form of a ConvNet architecture stacks a few CONV-RELU layers, follows them with POOL layers, and repeats this pattern until the image has been merged spatially to a small size. At some point, it is common to transition to fully-connected layers. The last fully-connected layer holds the output, such as the class scores. In other words, the most common ConvNet architecture follows the pattern:

```
INPUT -> [[CONV -> RELU]*N -> POOL?]*M -> [FC -> RELU]*K -> FC
```

where the `*` indicates repetition, and the `POOL?` indicates an optional pooling layer. Moreover, `N >= 0` (and usually `N <= 3`), `M >= 0`, `K >= 0` (and usually `K < 3`). For example, here are some common ConvNet architectures you may see that follow this pattern:

- `INPUT -> FC`, implements a linear classifier. Here `N = M = K = 0`.
- `INPUT -> CONV -> RELU -> FC`
- `INPUT -> [CONV -> RELU -> POOL]*2 -> FC -> RELU -> FC`. Here we see that there is a single CONV layer between every POOL layer.
- `INPUT -> [CONV -> RELU -> CONV -> RELU -> POOL]*3 -> [FC -> RELU]*2 -> FC`  
Here we see two CONV layers stacked before every POOL layer. This is generally a good idea for larger and deeper networks, because multiple stacked CONV layers can develop more complex features of the input volume before the destructive pooling operation.

*Prefer a stack of small filter CONV to one large receptive field CONV layer.* Suppose that you stack three 3x3 CONV layers on top of each other (with non-linearities in between, of course). In this arrangement, each neuron on the first CONV layer has a 3x3 view of the input volume. A neuron on the second CONV layer has a 3x3 view of the first CONV layer, and hence by extension a 5x5 view of the input volume. Similarly, a neuron on the third CONV layer has a 3x3 view of the 2nd CONV layer, and hence a 7x7 view of the input volume. Suppose that instead of these three layers of 3x3 CONV, we only wanted to use a single CONV layer with 7x7 receptive fields. These neurons would have a receptive field size of the input volume that is identical in spatial extent (7x7), but with several disadvantages. First, the neurons would be computing a linear function over the input, while the three stacks of CONV layers contain non-linearities that make their features more expressive. Second, if we suppose that all the volumes have  $C$  channels, then it can be seen that the single 7x7 CONV layer would contain  $C \times (7 \times 7 \times C) = 49C^2$  parameters, while the three 3x3 CONV layers would only contain  $3 \times (C \times (3 \times 3 \times C)) = 27C^2$  parameters. Intuitively, stacking CONV layers with tiny filters as opposed to having one CONV layer with big filters allows us to express more powerful features of the input, and with fewer parameters. As a practical disadvantage, we might need more memory to hold all the intermediate CONV layer results if we plan to do backpropagation.

**Recent departures.** It should be noted that the conventional paradigm of a linear list of layers has recently been challenged, in Google's Inception architectures and also in current (state of the art) Residual Networks from Microsoft Research Asia. Both of these (see details below in case studies section) feature more intricate and different connectivity structures.

**In practice: use whatever works best on ImageNet.** If you're feeling a bit of a fatigue in thinking about the architectural decisions, you'll be pleased to know that in 90% or more of applications you should not have to worry about these. I like to summarize this point as "*don't be a hero*": Instead of rolling your own architecture for a problem, you should look at whatever architecture currently works best on ImageNet, download a pretrained model and finetune it on your data. You should rarely ever have to train a ConvNet from scratch or design one from scratch. I also made this point at the [Deep Learning school](#).

## Layer Sizing Patterns

Until now we've omitted mentions of common hyperparameters used in each of the layers in a ConvNet. We will first state the common rules of thumb for sizing the architectures and then follow the rules with a discussion of the notation:

The **input layer** (that contains the image) should be divisible by 2 many times. Common numbers include 32 (e.g. CIFAR-10), 64, 96 (e.g. STL-10), or 224 (e.g. common ImageNet ConvNets), 384, and 512.

The **conv layers** should be using small filters (e.g. 3x3 or at most 5x5), using a stride of  $S = 1$ , and crucially, padding the input volume with zeros in such way that the conv layer does not alter

the spatial dimensions of the input. That is, when  $F = 3$ , then using  $P = 1$  will retain the original size of the input. When  $F = 5$ ,  $P = 2$ . For a general  $F$ , it can be seen that  $P = (F - 1)/2$  preserves the input size. If you must use bigger filter sizes (such as 7x7 or so), it is only common to see this on the very first conv layer that is looking at the input image.

The **pool layers** are in charge of downsampling the spatial dimensions of the input. The most common setting is to use max-pooling with 2x2 receptive fields (i.e.  $F = 2$ ), and with a stride of 2 (i.e.  $S = 2$ ). Note that this discards exactly 75% of the activations in an input volume (due to downsampling by 2 in both width and height). Another slightly less common setting is to use 3x3 receptive fields with a stride of 2, but this makes. It is very uncommon to see receptive field sizes for max pooling that are larger than 3 because the pooling is then too lossy and aggressive. This usually leads to worse performance.

*Reducing sizing headaches.* The scheme presented above is pleasing because all the CONV layers preserve the spatial size of their input, while the POOL layers alone are in charge of down-sampling the volumes spatially. In an alternative scheme where we use strides greater than 1 or don't zero-pad the input in CONV layers, we would have to very carefully keep track of the input volumes throughout the CNN architecture and make sure that all strides and filters "work out", and that the ConvNet architecture is nicely and symmetrically wired.

*Why use stride of 1 in CONV?* Smaller strides work better in practice. Additionally, as already mentioned stride 1 allows us to leave all spatial down-sampling to the POOL layers, with the CONV layers only transforming the input volume depth-wise.

*Why use padding?* In addition to the aforementioned benefit of keeping the spatial sizes constant after CONV, doing this actually improves performance. If the CONV layers were to not zero-pad the inputs and only perform valid convolutions, then the size of the volumes would reduce by a small amount after each CONV, and the information at the borders would be "washed away" too quickly.

*Compromising based on memory constraints.* In some cases (especially early in the ConvNet architectures), the amount of memory can build up very quickly with the rules of thumb presented above. For example, filtering a 224x224x3 image with three 3x3 CONV layers with 64 filters each and padding 1 would create three activation volumes of size [224x224x64]. This amounts to a total of about 10 million activations, or 72MB of memory (per image, for both activations and gradients). Since GPUs are often bottlenecked by memory, it may be necessary to compromise. In practice, people prefer to make the compromise at only the first CONV layer of the network. For example, one compromise might be to use a first CONV layer with filter sizes of 7x7 and stride of 2 (as seen in a ZF net). As another example, an AlexNet uses filter sizes of 11x11 and stride of 4.

## Case studies

There are several architectures in the field of Convolutional Networks that have a name. The most common are:

- **LeNet.** The first successful applications of Convolutional Networks were developed by Yann LeCun in 1990's. Of these, the best known is the [LeNet](#) architecture that was used to read zip codes, digits, etc.
- **AlexNet.** The first work that popularized Convolutional Networks in Computer Vision was the [AlexNet](#), developed by Alex Krizhevsky, Ilya Sutskever and Geoff Hinton. The AlexNet was submitted to the [ImageNet ILSVRC challenge](#) in 2012 and significantly outperformed the second runner-up (top 5 error of 16% compared to runner-up with 26% error). The Network had a very similar architecture to LeNet, but was deeper, bigger, and featured Convolutional Layers stacked on top of each other (previously it was common to only have a single CONV layer always immediately followed by a POOL layer).
- **ZF Net.** The ILSVRC 2013 winner was a Convolutional Network from Matthew Zeiler and Rob Fergus. It became known as the [ZFNet](#) (short for Zeiler & Fergus Net). It was an improvement on AlexNet by tweaking the architecture hyperparameters, in particular by expanding the size of the middle convolutional layers and making the stride and filter size on the first layer smaller.
- **GoogLeNet.** The ILSVRC 2014 winner was a Convolutional Network from [Szegedy et al.](#) from Google. Its main contribution was the development of an *Inception Module* that dramatically reduced the number of parameters in the network (4M, compared to AlexNet with 60M). Additionally, this paper uses Average Pooling instead of Fully Connected layers at the top of the ConvNet, eliminating a large amount of parameters that do not seem to matter much. There are also several followup versions to the GoogLeNet, most recently [Inception-v4](#).
- **VGGNet.** The runner-up in ILSVRC 2014 was the network from Karen Simonyan and Andrew Zisserman that became known as the [VGGNet](#). Its main contribution was in showing that the depth of the network is a critical component for good performance. Their final best network contains 16 CONV/FC layers and, appealingly, features an extremely homogeneous architecture that only performs 3x3 convolutions and 2x2 pooling from the beginning to the end. Their [pretrained model](#) is available for plug and play use in Caffe. A downside of the VGGNet is that it is more expensive to evaluate and uses a lot more memory and parameters (140M). Most of these parameters are in the first fully connected layer, and it was since found that these FC layers can be removed with no performance downgrade, significantly reducing the number of necessary parameters.
- **ResNet.** [Residual Network](#) developed by Kaiming He et al. was the winner of ILSVRC 2015. It features special *skip connections* and a heavy use of [batch normalization](#). The architecture is also missing fully connected layers at the end of the network. The reader is also referred to Kaiming's presentation ([video](#), [slides](#)), and some [recent experiments](#) that reproduce these networks in Torch. ResNets are currently by far state of the art Convolutional Neural Network models and are the default choice for using ConvNets in practice (as of May 10, 2016). In particular, also see more recent developments that tweak

the original architecture from [Kaiming He et al. Identity Mappings in Deep Residual Networks](#) (published March 2016).

**VGGNet in detail.** Lets break down the [VGGNet](#) in more detail as a case study. The whole VGGNet is composed of CONV layers that perform 3x3 convolutions with stride 1 and pad 1, and of POOL layers that perform 2x2 max pooling with stride 2 (and no padding). We can write out the size of the representation at each step of the processing and keep track of both the representation size and the total number of weights:

```
INPUT: [224x224x3]      memory: 224*224*3=150K  weights: 0
CONV3-64: [224x224x64]  memory: 224*224*64=3.2M  weights: (3*3*3)*64 = 1,728
CONV3-64: [224x224x64]  memory: 224*224*64=3.2M  weights: (3*3*64)*64 = 368,640
POOL2: [112x112x64]     memory: 112*112*64=800K  weights: 0
CONV3-128: [112x112x128] memory: 112*112*128=1.6M weights: (3*3*64)*128 = 737,280
CONV3-128: [112x112x128] memory: 112*112*128=1.6M weights: (3*3*128)*128 = 1,474,560
POOL2: [56x56x128]      memory: 56*56*128=400K  weights: 0
CONV3-256: [56x56x256]  memory: 56*56*256=800K  weights: (3*3*128)*256 = 2,949,120
CONV3-256: [56x56x256]  memory: 56*56*256=800K  weights: (3*3*256)*256 = 5,898,240
CONV3-256: [56x56x256]  memory: 56*56*256=800K  weights: (3*3*256)*256 = 5,898,240
POOL2: [28x28x256]      memory: 28*28*256=200K  weights: 0
CONV3-512: [28x28x512]  memory: 28*28*512=400K  weights: (3*3*256)*512 = 5,898,240
CONV3-512: [28x28x512]  memory: 28*28*512=400K  weights: (3*3*512)*512 = 7,864,320
CONV3-512: [28x28x512]  memory: 28*28*512=400K  weights: (3*3*512)*512 = 7,864,320
POOL2: [14x14x512]      memory: 14*14*512=100K  weights: 0
CONV3-512: [14x14x512]  memory: 14*14*512=100K  weights: (3*3*512)*512 = 7,864,320
CONV3-512: [14x14x512]  memory: 14*14*512=100K  weights: (3*3*512)*512 = 7,864,320
CONV3-512: [14x14x512]  memory: 14*14*512=100K  weights: (3*3*512)*512 = 7,864,320
POOL2: [7x7x512]        memory: 7*7*512=25K   weights: 0
FC: [1x1x4096]           memory: 4096  weights: 7*7*512*4096 = 102,760,448
FC: [1x1x4096]           memory: 4096  weights: 4096*4096 = 16,777,216
FC: [1x1x1000]           memory: 1000  weights: 4096*1000 = 4,096,000

TOTAL memory: 24M * 4 bytes ~= 93MB / image (only forward! ~*2 for bwd)
TOTAL params: 138M parameters
```

As is common with Convolutional Networks, notice that most of the memory (and also compute time) is used in the early CONV layers, and that most of the parameters are in the last FC layers. In this particular case, the first FC layer contains 100M weights, out of a total of 140M.

## Computational Considerations

The largest bottleneck to be aware of when constructing ConvNet architectures is the memory bottleneck. Many modern GPUs have a limit of 3/4/6GB memory, with the best GPUs having about 12GB of memory. There are three major sources of memory to keep track of:



- From the intermediate volume sizes: These are the raw number of **activations** at every layer of the ConvNet, and also their gradients (of equal size). Usually, most of the activations are on the earlier layers of a ConvNet (i.e. first Conv Layers). These are kept around because they are needed for backpropagation, but a clever implementation that runs a ConvNet only at test time could in principle reduce this by a huge amount, by only storing the current activations at any layer and discarding the previous activations on layers below.
- From the parameter sizes: These are the numbers that hold the network **parameters**, their gradients during backpropagation, and commonly also a step cache if the optimization is using momentum, Adagrad, or RMSProp. Therefore, the memory to store the parameter vector alone must usually be multiplied by a factor of at least 3 or so.
- Every ConvNet implementation has to maintain **miscellaneous** memory, such as the image data batches, perhaps their augmented versions, etc.

Once you have a rough estimate of the total number of values (for activations, gradients, and misc), the number should be converted to size in GB. Take the number of values, multiply by 4 to get the raw number of bytes (since every floating point is 4 bytes, or maybe by 8 for double precision), and then divide by 1024 multiple times to get the amount of memory in KB, MB, and finally GB. If your network doesn't fit, a common heuristic to "make it fit" is to decrease the batch size, since most of the memory is usually consumed by the activations.

## Additional Resources

Additional resources related to implementation:

- [Soumith benchmarks for CONV performance](#)
- [ConvNetJS CIFAR-10 demo](#) allows you to play with ConvNet architectures and see the results and computations in real time, in the browser.
- [Caffe](#), one of the popular ConvNet libraries.
- [State of the art ResNets in Torch7](#)

 [cs231n](#)

 [cs231n](#)

[karpathy@cs.stanford.edu](mailto:karpathy@cs.stanford.edu)