

University of Adelaide

Deeplearning for multi-label scene classification

by

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A thesis submitted in fulfillment for the
degree of Master

Under Supervised by
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February 2016

Declaration of Authorship

I, Junjie Zhang, declare that this thesis titled and the work presented in it are my own.
I confirm that:

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- Where any part of this thesis has previously been submitted for a degree or any other qualification at the University of Adelaide or any other institution, this has been clearly stated.
- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work.
- I have acknowledged all main sources of help.
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Abstract

Scene classification is an important field in computer vision. For similar weather condition, there are some obstacles for extracting features from outdoor images. In this thesis, we present a novel approach to classify cloudy and sunny weather. Inspired by recent study of a deep convolutional neural network and the spatial pyramid matching, we generate a model based on the ImageNet dataset. Starting with parameters learned from the other classification task, we fine-tune the model via the outdoor images. Experiment demonstrates that our classifier can achieve the state of the art accuracy.

Multi-label learning is a variant of supervised learning where the task is to learn a set of examples, which can belong to multiple classes. This is a version of popular multi-class classification problems in which each sample has one class label only. It can apply in a wide range of applications, which include text categorisation, semantic image labelling etc.. A lot of research work has been done on multi-label learning with different approaches. In this thesis, I trained a neural network from scratch up based on the generated artificial images. The model is learned by minimising error function based on the Hamming distance, through the backpropagation. The model has high capability of generalisation.

Acknowledgements

I am grateful to my major supervisor, Prof. Chunhua Shen, and co-supervisor, Dr. Qinfeng Shi, whose expertise, understanding, and warmly support made it possible for me to work on the neural network that is of great interest to me. It is a pleasure working with them. Prof. Shen's dedication and keen interest to help his students had been solely and mainly responsible for completing my work. His timely advice, meticulous scrutiny, and scholarly advice have helped me to accomplish the tasks.

I would like to thank for my co-supervisor, Qinfeng Shi, for his time and effort on helping me understand research work and knowledge of machine learning.

I thank PhD candidate Teng Li who cooperated to work on the Weather Classification project. We set up experiment environment, analysed test results and discussed approaches. His prompt inspirations, timely suggestions with kindness, and enthusiasm work attitude have helped to achieve the perfect classification accuracy.

I am extremely thankful to research fellow, Guoshen Lin, for his kind help and discussion about the weather classification and the multi-label classification.

I would also like to thank staffs and visitors in the Australian Center for Visual Technologies (ACVT). Attending the reading group has enriched my knowledge in Computer Vision and learned a lot from them.

Finally, I would like to warmly thank the staffs in the School of Computer Science at the University of Adelaide. Julie Mayo, Sharyn Liersh and Jo Rogers have done excellent jobs on administration which helps students to be focus on their research work.

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Abbreviations

SVM	Support Vector Machine
ANNs	Artificial Neural Networks
ROI	Rogin of Interest
SIFT	Scale Invariant Feature Transform
SGD	Stochastic Gradient Descent
BP	BackPropagation
MLE	Maximum Likelihood Estimation
MAP	Maximum A Posteriori
CNN	Convolutional Neural Network
ReLU	Rectified Linear Unit
SPM	Spatial Pyramid Matching
SPP	Spatial Pyramid Pooling
GPU	Graphics Processing Unit
BR	Binary Relevance Classifier
CC	Classifier Chains Classifier
CML	Collective Multi-Label Classifier

Part I

Weather Classification

Chapter 1

Introduction

1.1 Overview

The computer is one of the most significant inventions in history. It provides huge power in the data processing field, like computer vision. Also, computer systems can aid people in daily life, for example driverless vehicles. However, the human brain still has compelling advantage in some fields, such as identifying our keys in our pocket by feel. The complex processes of taking in raw data and taking action based on the pattern are regarded as pattern recognition. Pattern recognition has been important for people in daily life for a long period and the human brain has developed an advanced neural and cognitive capacity for such tasks.

Weather classification is one of the most important pattern recognition tasks which relates to our work and lives. There are several major kinds of weather conditions, such as sunny, cloudy, rainy. People can classify them easily through their eyes. However, it is not an easy job for machines, especially in literature on computer vision.

In this thesis, we describe an approach to this problem of weather classification based upon the major big trend in machine learning, and more precisely, deep learning. It differs from the feature detectors method, which extracts features manually, and then trains a model to perform classification.

Compared to shadow learning which includes decision trees, SVM and naive bayes, deep learning passes input data through several non-linearity functions to generate features

and performs classification based on those features. It generates a mapping and finds the optimal solution.

1.2 Statistical Pattern Recognition

In the statistical approach, a pattern is represented in terms of d -dimensional feature vectors and each element of the vector describes some subjects of the example. In brief, three components are essential for statistical pattern recognition. The first one is a representation of the model. The second one is an error function used to evaluate the performance of the model. The third one is an optimisation method for learning a model.

1.3 Artificial Neural Networks (ANNs)

Artificial neural networks were proposed in the mid-20th century. The term is inspired by the structure of neural networks in the human brain. It is one of the most successful statistical learning models used to approximate functions. Learning with ANNs yields an effective learning paradigm and has achieved cutting-edge performance in object classification.

The single-layer ANNs have shown great success for a simple model. For increasingly complex models and applications, multi-layer ANNs have exhibited the power of features learning. With hardware being developing at the same time, the demand for more efficient optimising and model evaluation methods has increased promptly.

Recent development in ANNs has greatly advanced the performance of state-of-the-art visual recognition systems. With implementing deep convolutional neural networks, ANNs achieve top accuracy in the ImageNet Challenge. The model has been used in related fields and performs well in pattern recognition.

1.4 Weather Classification

Weather classification is an important task in daily life. In this thesis, we are focused on two classes of weather conditions, sunny and cloudy.

There are some obstacles in front of weather classification. Firstly, because the number of inputting pixels is high, for example a 500×500 RPG image including 750,000 pixels, computation is expensive. Secondly, some simple middle level image characters are difficult to be recognised by machines, such as light, shading, sun shine. It is still not easy to detect these characters with high accuracy. Thirdly, there are no decisive features, such as brightness and lightness, to classify scenes. And sun shine can be both found in sunny and cloudy weather. Last but not least, outdoor images have various backgrounds.

Chapter 2

Background

2.1 Related Work

There has been much research done on the task of weather classification. Most works follow the procedure of extracting features and then performing classification [15–18]. Some works use low-level features, like colour [19], texture [20, 21]. Some works use filters or segmentation [20, 22] to extract high-level features, such as sky, shadow [11]. Some works use statistical measurement methods [12, 16] to analyse low-level feature distributions.

Generally, the traditional methods follow three basic steps [16, 23]. First, some Regions of Interest (ROIs), such as sky and shadow, are extracted from a weather image. Then, histogram descriptors are used to represent the difference between them. Finally, a classifier is trained based on the extracted features.

Most previous works are based on the discriminative model. They extract human recognisable features to classify images. This type of shadow learning depends mainly on the quality of features and human’s prior knowledge. An image without prior features or with poor features is difficult to be classified. Furthermore, the methods require a lot of work on data pre-processing and are not flexible. The approaches depend on structural information to categorise an image into one of the classes. Structural information is concluded from illumination invariant features, like SIFT. However, previous works have limitation on classifying diverse images. It is difficult to list all the factors which determinate the weather conditions.

2.2 Single-Layer ANNs

Artificial neurons were introduced as information processing devices more than fifty years ago [24]. Following the early work, perceptrons were deployed in layers to perform pattern recognition tasks. A lot of resources were invested in the research capability of learning perceptrons theoretically and experimentally. As shown in figure 2.1, a perceptron computes a weighted summation of its n inputs and then thresholds the result to give a binary output y . We can treat n input data as an vector with n elements, and represent the vector as either class A (for output +1) or class B (for output -1).

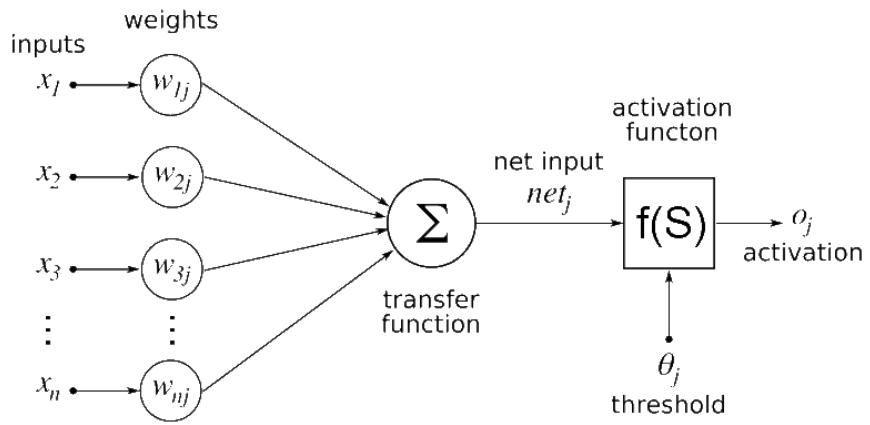


FIGURE 2.1: Diagram of a perceptron [1].

Each output is updated according to the equation:

$$y_i = f(h_i) = f \left(\sum_j w_{ij} x_j \right) \quad (2.1)$$

where x_j is the j th input, y_i is the i th output, and h_i is the net input into the node. The weight w_{ij} connects the j th input and the i th output, and the threshold function $f(h)$ is the activation function and usually makes up the form

$$f(x) = sign(x) = \begin{cases} -1 & h < 0 \\ 1 & h \geq 0 \end{cases} \quad (2.2)$$

and it is plotted out in figure 2.2

Besides the threshold function, there are several deterministic activation functions.

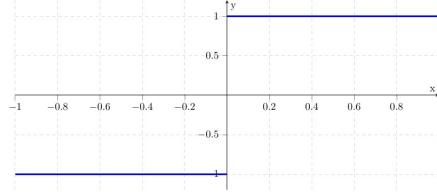


FIGURE 2.2: Threshold function

- Linear function

$$f(x) = x \quad (2.3)$$

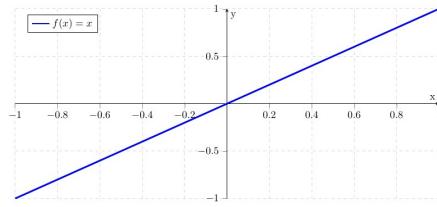


FIGURE 2.3: Linear function

- Sigmoid function

$$f(x) = \frac{1}{1 + e^{-x}} \quad (2.4)$$

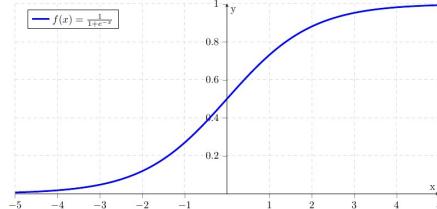


FIGURE 2.4: Sigmoid function

- Tanh function

$$f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} \quad (2.5)$$

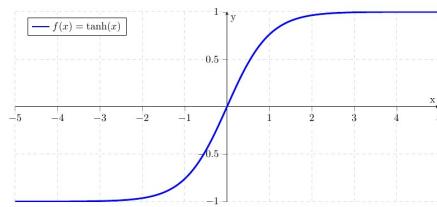


FIGURE 2.5: Tanh function

We can also represent equation 2.2 in vector notation, as in

$$y = f(h) = f(w \cdot x) \quad (2.6)$$

where w and x can be regarded as $n \times 1$ dimensional column vectors, and n is the dimension number of the input data. The term $w \cdot x$ in equation 2.6 constructs a $(n - 1)$ -dimension hyperplane which passes the origin. The hyperplane can be shifted by adding a parameter to equation 2.1, for example

$$y = f(h) = f(w \cdot x + b) \quad (2.7)$$

We can have the same effect by putting a constant value 1 and increasing the size of x and w by one. The extra weight w with fixed value 1 is called *bias weight*. It is adaptive like other weights and provides flexibility to hyperplane. Then we get:

$$y = f(h) = f\left(\sum_{i=0}^n w_i x_i\right) \quad (2.8)$$

The aim of learning is to find a set of weights w_i so that:

$$\begin{aligned} y &= f\left(\sum_{i=0}^n w_i x_i\right) = 1 \quad x \in ClassA \\ y &= f\left(\sum_{i=0}^n w_i x_i\right) = 0 \quad x \in ClassB \end{aligned}$$

The single-layer neural network is simple to implement, while it can only support a linear decision boundary. We can build a simple neural network to acquire intuition behind the mathematical theory. The network has no bias and one neuron which means it has one weight, w_1 . We implement a logistic sigmoid activation function on the dot product of input data and weight w_1 . Therefore, the network can map the input data a_0 onto an output a_{out} based on the function

$$a_{out} = f(a_0 w_1) \quad (2.9)$$

where $f()$ is the logistic function. Given that an input data 1 maps to an output data 1, we can compute the value of the error function for each possible value of w_1 . Feeding value of w_1 in range $(-10, 10)$, we can plot the error surface in figure 2.6.

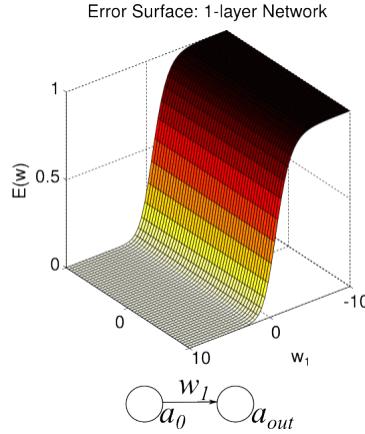


FIGURE 2.6: The error surface for a single layer neural network [2].

The single-layer neural network has a decision boundary which is linear. However, the boundary is limited. The limitation can be illustrated by two types of datasets in figure 2.7 .



FIGURE 2.7: Two types of dataset. The left one can be separated by a single layer neural network. The right one cannot be separated by a single neural network. Generated from [3].

2.3 Multi-Layer Networks

Single-Layer networks have limitation of representing complex functions. We are seeking to learn the nonlinearity from samples. To improve the representation capability, we can stack layers network. This is the approach of multi-layer neural networks. multi-layer neural networks implement linear discriminants via mapping the input data to

a nonlinear space. They can use fairly simple algorithms to learn the form of the nonlinearity from training data.

In the thesis, we limit multi-layer neural networks in the subset of feedforward neural networks. Feedforward neural networks can provide a general mechanism for representing nonlinear functional mapping between a set of input data and a set of output labels. Figure 2.8 is a feedforward neural network having two layers of adaptive weights.

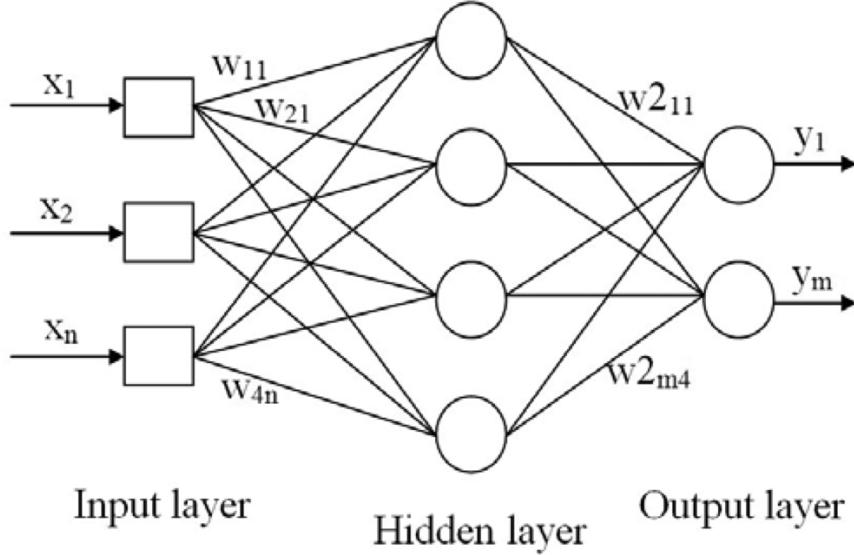


FIGURE 2.8: Diagram of a feedforward neural network [4].

In the example, the middle column perceptrons act as hidden neurons. The network has n inputs, 4 hidden neurons and m output neurons. The network diagram represents the function in the form

$$y_m = \hat{f} \left(\sum_{j=0}^m w_{j4}^{(2)} f \left(\sum_{i=0}^n w_{4i}^{(1)} x_i \right) \right) \quad (2.10)$$

In equation 2.10, the outer activation function could be different with the inner one.

There are some activation functions, including sigmoid and tanh functions. The sigmoid function, also named the logistic function, can be represented as:

$$f(x) = \frac{1}{1 + e^{-x}} \quad (2.11)$$

Its outputs lie in the range $(0, 1)$. We can do a linear transformation $\hat{x} = x/2$ on the input data and a linear transformation $\hat{y} = 2y - 1$ on the output. Then we can get an

equivalent activation function \tanh which can be represented as:

$$f(x) = \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} \quad (2.12)$$

With enough hidden neurons, a three-layer neural network is capable of approximating any function. In other words, the network performs an arbitrary accuracy to classification problems in theory.

We can use a simple example to illustrate the power of the multi-layer neural network. In this example, we have one input, one hidden neuron and one output. There is no bias in the input layer and hidden layer. There are two weights existing in the network, (w_1, w_2) , and the output can be calculated via

$$a_{out} = f(f(a_0 w_1) w_2) \quad (2.13)$$

where $f()$ is the sigmoid function. With varying w_1 and w_2 , the error surface can be represented in figure 2.9. And the samples, which cannot be separated by a single-layer

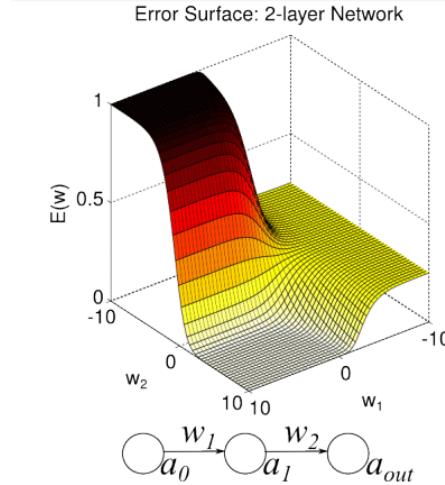


FIGURE 2.9: The error surface for a multi-layer neural network [2].

neural network, can be classified by a multi-layer neural network correctly.

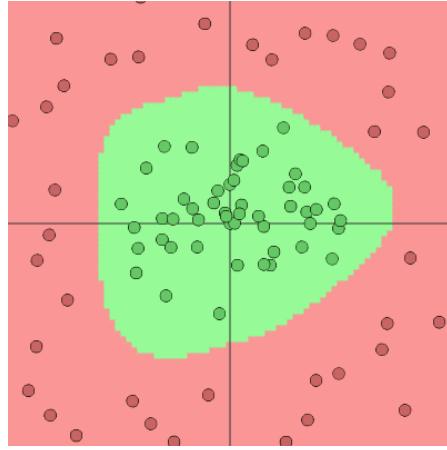


FIGURE 2.10: A multi-layer neural network can separate a complicated dataset. Generated from [3].

2.4 Stochastic Gradient Descent (SGD)

Because the weight space in neural networks is continuous, optimal weights values can be learned through optimisation algorithms. The error function is defined as:

$$L(f_w) = \sum L(y, f_w(x)) \quad (2.14)$$

Gradient descent is a first-order optimisation algorithm which starts from a random point, and finds a nearby minimum point. It can converge to a minimum value.

The SGD is a subtype of gradient descent. It only considers a single training point and moves to a nearby point based on

$$w = w - \eta \Delta L(w) = w - \eta \sum_{i=1}^n \Delta L_i(w) \quad (2.15)$$

where η is the learning rate and $L_i(w)$ is the value of the error function at the i th sample. The Robbins-Siegmund theorem [25] provides the approaches to almost surely convergence to a global minimum under relatively mild assumptions, moreover, it is fast and effective in most circumstances.

2.5 Backpropagation

Multi-layer neural networks can represent mapping from the input data to the output classes. One challenge is to learn a suitable mapping method from the training dataset.

This will be resolved by a popular learning algorithm, backpropagation.

Because activation functions are differentiable, the activation of output neurons can be propagated to the hidden neurons with respect to weights and bias. If we have an error function, we can evaluate derivatives of the error and update the weights to minimise the error function via some optimisation methods.

Backpropagation can be applied to find the derivatives of an error function related to the weights and bias in the network via two stages. First, the derivatives of the error functions, for instance sum-of-squares and Jacobian, must be evaluated with respect to the weights. Second, a variety of optimisation schemes can be implemented to compute the adjustment of weights based on the derivatives. After passing data through the network, we can get the predicted classes. It updates weight changes based on the gradient descent. Given that the network has i inputs, h hidden neurons and k outputs. The update equation can be represented as:

$$w(j+1) = w(j) + \Delta w(j) \quad (2.16)$$

where $\Delta w(j)$ defined as:

$$\Delta w(j) = -\eta \frac{\partial E}{\partial w} \quad (2.17)$$

The weights, locating in the hidden layer connecting to the output layer, are updated by

$$\Delta w(jk) = -\eta \frac{\partial E}{\partial w_{jk}} = -\eta \delta_k y_j \quad (2.18)$$

where

$$\delta_k = \frac{\partial E}{\partial a_k} = (y_k - t_k)y_k(1 - y_k)$$

The weights in the other hidden layer are updated by

$$\Delta w(ij) = -\eta \frac{\partial E}{\partial w_{ij}} = -\eta \delta_j y_i \quad (2.19)$$

where

$$\delta_j = \frac{\partial E}{\partial a_j} = \sum_k \delta_k w_{jk} y_j (1 - y_j)$$

The δ_j of a hidden neuron is based on the δ_k of the output linked neurons. To minimise the error function E by gradient descent, it needs the backwards propagation of errors.

2.5.1 Training protocols

In supervised learning, training dataset consists of data with labels. We can use the neural networks to find the output of the training data and learn optimal weights. There are mainly three types of training protocols, stochastic, batch and online training. In stochastic training, we randomly choose samples from the training dataset and update weights every time. In batch training, we use some samples and pass them through the network, then update weights based on the error value. In online training, each sample of the training dataset is used once and weights are updated each time. We usually define one time of passing all training dataset through neural networks as one epoch.

It is worth noting batch learning. In large scale applications, the training dataset can consist over millions of samples. It is time consuming to compute the error function over all training dataset in order to update weights once. It is a practical approach to compute the gradient over a batch of training dataset. Does it have harmful effects on generalisation? It depends on the correlations among the training dataset. Consider there are more than one million images in the ImageNet dataset which is made up of only 1000 categories. If the images in a batch are selected evenly from each category, the gradient from the batch is a reasonable approximation of that of the full training dataset. Therefore, batch learning leads to faster convergence by evaluating the batch gradients to update weights frequently.

2.6 Overfitting and Regularization

Overfitting is a common phenomenon that a model has high performance on the training dataset, but the model performs poorly on the testing dataset in classification tasks. Thus, a classification problem with two classes and two input variables, (left figure in 2.11), shows decent decision boundaries. With increasing complexity of the model, the decision boundaries become more complex and fit the training dataset extremely well. From the example in figure 2.11, it is clear that a model, whose complexity is neither too small nor too large, has the best generalisation performance.

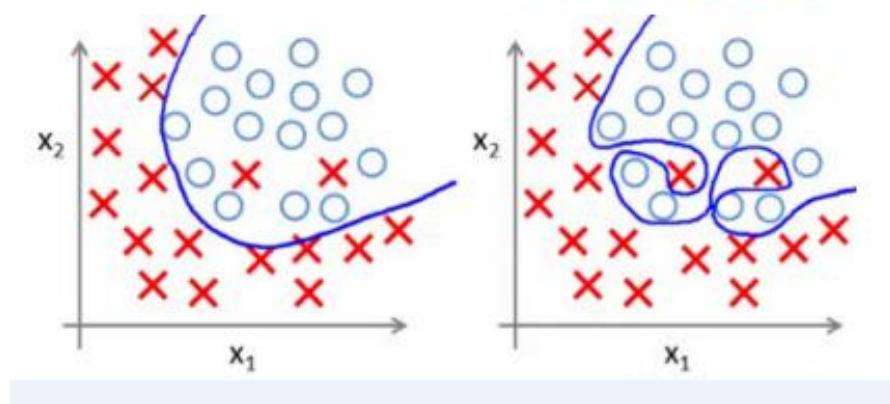


FIGURE 2.11: Overfitting example, the left one has a decent generalisation performance and the right one is overfitting [5].

In order to find the optimal complexity of the neural network, there are mainly two approaches. One is to change the adaptive parameters, like neuron numbers in hidden layers. This is named structural stabilisation. It can be approached from two directions. We can start from a small network and increase layer numbers or neuron numbers in the training process and arrive at an effective neural network architecture. The other one is to start from a large network and prune out layers or neurons in the training process to achieve the optimal network. Another fundamental basic method to control the complexity of a model is regularisation which includes adding a penalty term in the error function. The degree of regularisation can be adjusted by scaling the term via a multiplicative parameter.

Regularisation helps to smooth the decision boundary surface by introducing a penalty term Ω to the error function

$$\hat{E} = E + \lambda\Omega \quad (2.20)$$

where E is the standard error function, then λ adjusts the extent of the penalty Ω effect on the solution. The task of learning is to minimise the total error function \hat{E} . It needs to compute the derivatives of Ω with respect to the weights efficiently. A model, which has high accuracy in the training dataset, has a small value for E . At the same time, the smooth error surface of neural networks gives a small value on Ω .

A number of regularisers have been performed in applications, like weight decay, early stopping, training with noise, weight sharing etc..

2.6.1 Weight Decay

In order to smooth the decision boundary surface, weight values should be small. The weight decay regulariser can be represented as:

$$\Omega = \frac{1}{2} \sum_i w_i^2 \quad (2.21)$$

where the sum includes all weights and bias. Weight decay of this form leads to major improvement in empirical generalisation [26]. Intuitively, in equation 2.21, the smaller the weights are, the better the regulariser is. Usually, the derivatives of the total error function with respect to the weight are used to train the neural network. The network is trained by gradient descent in the continuous time limit. The weights will evolve with time t

$$\frac{w}{t} = -\eta \nabla E = -\eta \lambda w \quad (2.22)$$

where η is the learning rate. And the equation has solution

$$w(t) = w(0)e^{(-\eta \lambda t)} \quad (2.23)$$

and the exponential function reduces weights to zero quickly. Weight decay is also named L2 regularisation.

2.6.2 Dropout

Neural networks with deep layers and a large amount of neurons is a powerful learning machine. However, the more parameters the network has, the easier it is overfitting. Recently, dropout [6] is a simple and extremely effective regularisation technique which complements the other methods. At training process, random neurons are selected with some probability p to update their associated weights, and the others are inactive. In other words, only a reduced network is trained. At the testing process, there is no dropout applied and all neurons are active. The dropout method is replaced by performing a scaling of layer outputs by the same probability p . This method can maintain the outputs of neurons to be the same in both training and testing process. For example, if a neuron has p probability to be dropped out in the training process, the neuron should give an output l without dropout in the testing stage. Then we should

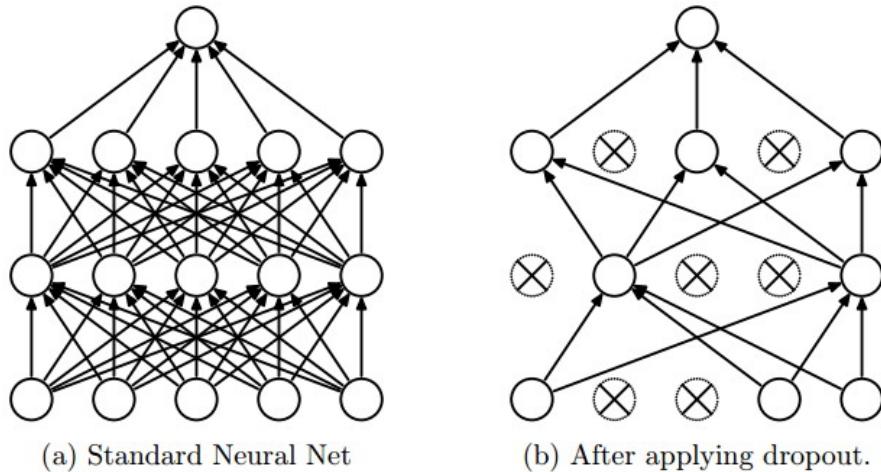


FIGURE 2.12: Illustration of dropout [6].

apply $(p * l + (1 - p) * 0)$ on the output, because the output has $(1 - p)$ probability to be 0.

2.7 Softmax Classifier

Softmax function, also named normalised exponential, is a generalisation of the logistic function which squeezes a d -dimension arbitrary real values vector to the same dimension vector of real values in the range $(0, 1)$ that add up to be 1. Because softmax function is the gradient log normaliser of categorical probability distribution, it can be used in probabilistic multiclass classification problems.

Softmax function derives from log linear models and interprets the weights in terms of convenient odds ratios. It can constrain the input values of the final layer to be positive and sum of them to be 1.

A softmax layer begins the same way as the normal layer which forms the weighted inputs $z_j^L = \sum_k w_{jk}^L x_k^{L-1} + b_j^L$ where L is the layer number, k is the input data number and j is the output neuron number. Then it implements a softmax function to the z_j^L and activates the j output neuron:

$$f_j(z) = \frac{e^{z_j}}{\sum_k e^{z_k}} \quad (2.24)$$

Equation 2.24 implies that the output values are all positive and the sum of all values $\sum_k a_k$ is 1.

The softmax classifier can be used to handle a multiclass classification. For a training dataset $(x_1, y_1), \dots, (x_m, y_m), y_i \in \{1, 2, \dots, K\}$ of m labelled samples, the label y have K different values.

To an unseen sample x , we will use a hypothesis to estimate the probability $P(y = k|x)$ for each value $k = 1, \dots, K$. For example, we want to compute the probability of the class label on each of K different possible values. The neural network will then output a K dimensional vector which represents K estimated probabilities.

$$h_W(x) = \begin{bmatrix} P(y = 1|x; W) \\ P(y = 2|x; W) \\ \vdots \\ P(y = K|x; W) \end{bmatrix} = \frac{1}{\sum_{j=1}^K \exp(W^{(j)\top} x)} \begin{bmatrix} \exp(W^{(1)\top} x) \\ \exp(W^{(2)\top} x) \\ \vdots \\ \exp(W^{(K)\top} x) \end{bmatrix} \quad (2.25)$$

Where W^j are the weights of the model and the normalised distribution ensures that the sum is one.

The cross entropy can interpret the softmax classifier. The cross entropy between actual distribution p and a predicted distribution q is represented as:

$$H(p, q) = - \sum_x p(x) \log q(x) \quad (2.26)$$

Hence, the task of the softmax classifier is to minimise the cross entropy between the actual distribution and the predicted distribution.

In other words, the softmax classifier can be interpreted in probability view. Given a sample (x_i, y_i) and parameters W , we can compute the normalised probability:

$$P(y_i | x_i; W) = \frac{e^{f_{y_i}}}{\sum_j e^{f_j}} \quad (2.27)$$

where f_{y_i} is the score predicted by the model with weights W . Therefore the normalised probabilities are computed by exponentiating the values and divided by the sum of all values. We can minimise the negative log likelihood of the ground truth labels by performing Max Likelihood Estimation(MLE). Aside from MLE, Maximum a Posteriori(MAP) can evaluate the performance of a model.

2.7.1 Practical issues

From a numerical view, the exponential computation is easy to overflow. Thus, the output of the softmax function is not numerically stable through computing $e^{f_{y_i}}$ and $\sum_j e^{f_{y_j}}$ directly. The implementation requires a normalisation trick. It is mathematically equivalent to multiplying a constant C with both the top and bottom of the fraction.

$$\frac{e^{f_{y_i}}}{\sum_j e^{f_j}} = \frac{Ce^{f_{y_i}}}{C \sum_j e^{f_j}} = \frac{e^{f_{y_i} + \log C}}{\sum_j e^{f_j + \log C}} \quad (2.28)$$

where C can be any positive value. The constant C does not change the output value, but it improves the numerical stability of the computation. An experienced choice of C is to set $\log C = -\max f_j$, and it can shift the vector f to preserve the highest value as 0.

2.7.2 Error function

An error function is used to evaluate performance of a model. We will generate an error function for softmax regression. An indicator function, $I\{\cdot\}$, is introduced to represent the accuracy for each label. If the predicted result corresponds to the actual label, say $y^{(i)} = k$, the indicator function returns 1, otherwise 0. The error function will be defined as:

$$L(W) = - \left[\sum_{i=1}^m \sum_{k=1}^K I\{y^{(i)} = k\} \log \frac{\exp(W^{(k)\top} x^{(i)})}{\sum_{j=1}^K \exp(W^{(j)\top} x^{(i)})} \right] \quad (2.29)$$

where this generates the logistic regression error function

$$\begin{aligned} L(W) &= - \left[\sum_{i=1}^m (1 - y^{(i)}) \log(1 - h_W(x^{(i)})) + y^{(i)} \log h_W(x^{(i)}) \right] \\ &= - \left[\sum_{i=1}^m \sum_{k=0}^1 I\{y^{(i)} = k\} \log P(y^{(i)} = k | x^{(i)}; W) \right] \end{aligned} \quad (2.30) \quad (2.31)$$

Similar to the logistic regression error function, the softmax error function sums over the predicted different K values of the classes. In the softmax regression, the posterior probability distribution can be represented:

$$P(y^{(i)} = k | x^{(i)}; W) = \frac{\exp(W^{(k)\top} x^{(i)})}{\sum_{j=1}^K \exp(W^{(j)\top} x^{(i)})} \quad (2.32)$$

It is difficult to solve equation 2.30. Usually an optimisation algorithm can approximate optimal values. Taking derivative with respect to weights, we can compute the entire gradient

$$\nabla_{W^{(k)}} L(W) = - \sum_{i=1}^m \left[x^{(i)} \left(1\{y^{(i)} = k\} - P(y^{(i)} = k | x^{(i)}; W) \right) \right] \quad (2.33)$$

We can take partial derivative of $L(W)$ with respect to the j th element of $W^{(k)}$.

2.8 Convolutional Neural Networks (CNN)

Convolutional Neural Networks [27] are widely applied in image understanding and achieve top rank in an image classification competition [13]. Compared to regular neural networks, CNN architecture assumes that the inputs are images and pixels are related in the local region.

CNN architecture has neurons arranged in 3 dimensions, width, height and depth. For example, there is an image which has dimensions $32 \times 32 \times 3$. The neurons in a layer will connect to a customised region of the previous layer. Moreover, the final output layer has dimensions $1 \times 1 \times d$, where d is the number of classes. The dimensions are reduced from 3072 to d . The output is a single vector of class scores.

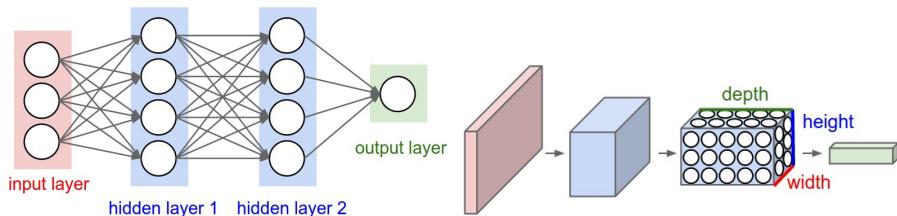


FIGURE 2.13: The left is a fully connect regular neural network. The right is a CNN in 3 dimensions [7].

2.8.1 Layers in CNN

CNN have four main types of layers, including convolutional layers, Relu layers, pooling layers and fully connected layers. Every layer transforms the input to the output via a differentiable function.

1. Convolutional Layer

2. ReLU Layer
3. Pooling Layer
4. Fully Connected Layer

Following the layers, CNN transforms an image from a set of pixel values to final class scores.

Convolutional Layer is the key component of CNN and its output can be represented as neurons shaped in 3D volume. A set of learning filters make up the convolutional layer's parameters. Although the size of filter is flexible, it usually chooses small size. During the feedforward process, each filter slides across the input volume and produces a 2-dimensional feature map. In each slide, the input and the filter perform a dot product computation. If there are some specific features at some spatial positions, they can be learnt by the filters.

Local connectivity is the key properties of CNN. Regular neural networks use fully connected layers. Computation is unaffordable for normal size images, even with high capability hardware. Instead, each neuron connects a local region of the input only. There are two main benefits from local connectivity. One is reducing parameters significantly and controlling overfitting. The other is for a key image property. Pixels are strongly correlated with nearby pixels. This can be regarded as a local receptive field which can retrieve information from subregions of an image.

To control the output volume arrangement, three parameters are introduced. They are depth, stride and zero-padding. In a convolutional layer, depth controls the number of neurons which connect the same subregion of the input volume. All the neurons learn the different features from the input volume. For example, the neurons along the depth in the convolutional layer can activate existence of various edges, colour, etc.. Stride is another

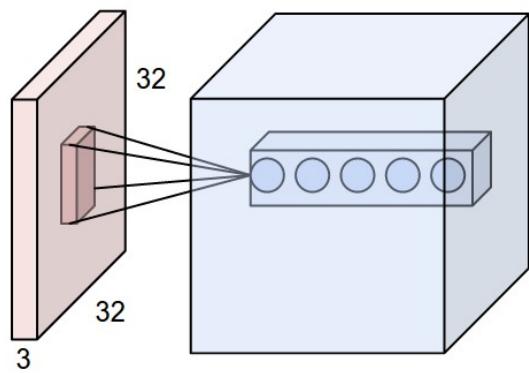


FIGURE 2.14: Diagram for depth in a convolutional layer [7].

parameter which controls the spatial position of the nearby depth column of neurons. The smaller the stride is, the more overlapping receptive fields are shared by the nearby columns. Zero-padding on border helps to resize output volume to the same dimension with the input volume.

A scheme, named parameter sharing, is implemented in convolutional layers to limit the number of parameters. The scheme supposes that a filter, which is helpful to compute at some spatial positions, should be helpful to compute another position.

ReLU Layer is the abbreviation of Rectified Linear Units. The neurons in the layer operate the non-saturating activation function $f(x) = \max(0, x)$ over the result of dot product in convolutional layers. The layer increases non-linearity to network without losing the receptive fields of convolutional layers.

Pooling Layer is a mechanism of downsampling. It is usually appended after convolutional layers to progressively decrease the spatial size of feature maps. It decreases network parameters. At the same time, it makes the neurons in the layer to be relatively insensitive to small shifts of images.

Fully Connected Layer takes feature maps, which have high level representation, from previous layers. The difference with convolutional layer is that it connects to all neurons in the previous layer instead of a receptive field.

2.9 Spatial Pyramid Matching (SPM)

Spatial pyramid matching [8] is used to classify high-level semantic attributes, based on low-level features. The method subdivides an image in several different levels of resolution and counts features falling in each spatial bin. It extends bags of features method and derives spatial information from images.

Let two sets of vectors X and Y be in a d -dimensional feature space. SPM could find the approximate correspondence between them. In brief, SPM places a chain of grids over the feature space and counts sum of matches occurring at each level of resolution. The points falling into the same grid are matched and the match points in finer resolutions have higher weights. Specifically, a chain of grids at resolutions $0, \dots, L$, have $2^0, \dots, 2^L$ cells respectively. H_X^l and H_Y^l are the histograms of X and Y at the l resolution, thus

Spatial Pyramid Matching (SPM)

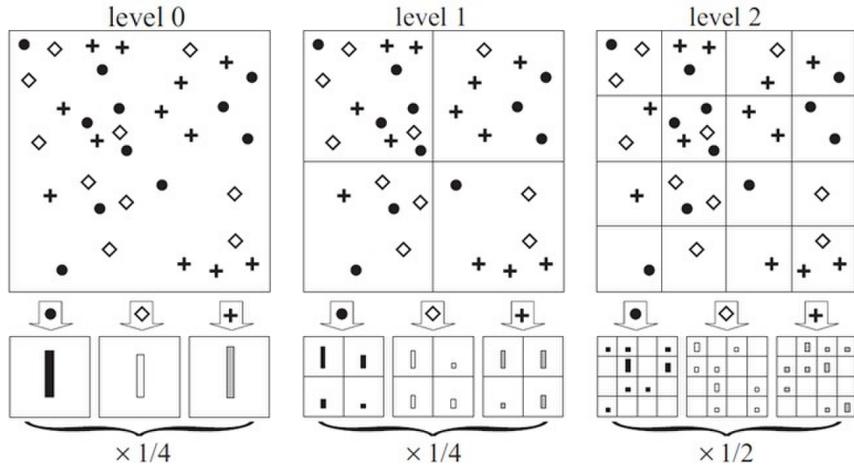


FIGURE 2.15: Diagram of the Spatial Pyramid Matching [8].

the number of points in the i th cell from X and Y can be represented as $H_X^l(i)$ and $H_Y^l(i)$. The histogram intersection function denotes the number of matches at level l

$$I(H_X^l, H_Y^l) = \sum_{i=1}^D \min(H_X^l(i), H_Y^l(i)) \quad (2.34)$$

Because the match points found in the l level include the match points found in the finer level $l+1$, the number of new match points at level l is $I^l - I^{l+1}$. The weight assigned to level l is $\frac{1}{2^{L-l}}$. Putting all together, the pyramid match kernel can be represented:

$$K^L(X, Y) = I^L + \sum_{l=0}^{L-1} \frac{1}{2^{L-l}} (I^l - I^{l+1}) \quad (2.35)$$

$$= \frac{1}{2^L} I^0 + \sum_{l=1}^L \frac{1}{2^{L-l+1}} I^l \quad (2.36)$$

We perform SPM in a 2-dimensional image space and apply standard vector quantisation in the feature space. All feature vectors are quantised into M discrete types and only the same type of features match to one another. Two sets of 2-dimensional vectors, X_m and Y_m , represent the coordinate of the features of type m in the individual image. The match kernel of two images is the sum of total channel kernels

$$K^L(X, Y) = \sum_{m=1}^M K^L(X_m, Y_m) \quad (2.37)$$

2.10 Transfer Learning

In the literature on machine learning, transfer learning [28] focuses on storing knowledge from one domain and applying it to a related problem. In other words, the relevant knowledge, learned from previous tasks, can be applied to new tasks. The closer a new job relates to previous knowledge, the more easily it can be solved. In contrast, other machine learning methods solve problems independently.

Transfer learning has three benefits. The first one is to save time on preprocessing data. Collecting and processing raw data are time consuming and expensive in each task. It can reduce volume of required data significantly, because of existing knowledge extracted from previous learning tasks. The second one is to reduce time on training a model from scratch up. Usually, training a model from scratch up is time consuming. The last one is to avoid the risk of overfitting. With insufficient training data, a complicated model is easy to overfitting. Transfer learning method can control overfitting because of existing knowledge.

Traditional ML vs. TL

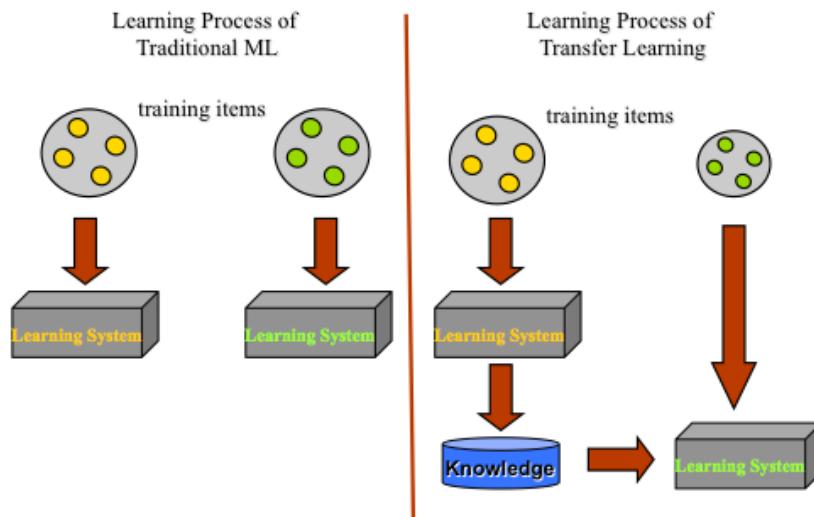


FIGURE 2.16: The left is traditional machine learning method. The right is transfer learning [9].

A domain can be represented

$$D = \{X, P(X)\} \quad (2.38)$$

where X is the feature space and $P(X)$ is the marginal probability distribution.

In transfer learning, there are two main challenges:

1. Which part of previous knowledge is useful to the new task?
2. How to represent the existing knowledge in the new model?

The first challenge arise, when we evaluate the relation between the previous knowledge and the current task. The correlated knowledge for the task can improve the performance of a model. Meanwhile, the unrelated and negative correlated knowledge are useless, even harmful. After evaluating the useful knowledge, new learning algorithms should be developed to transfer the knowledge. This leads to the second challenge. Because knowledge have different representations, translation process must keep accuracy and minimise loss of knowledge.

Chapter 3

Methodology

3.1 Dataset

There are over 15 million labelled images in the ImageNet database which has 22,000 categories. The images were collected from the Internet and labelled manually. From 2010, the competition, named the ImageNet Large-Scale Visual Recognition Challenge(ILSVRC) [10], has been held annually. The competition uses a subset of dataset which contains 1000 images in 1000 categories. With 50,000 validation images and 150,000 testing images, there are over 1 million images in total.



FIGURE 3.1: 2 Figures from the ImageNet [10].

The weather dataset [11] contains 10,000 images for two categories evenly, cloudy and sunny. They were collected from three sources, the Sun Dataset [29], the Labelme

Dataset [30] and the website, Flickr. They were classified manually and similar images were removed. No unambiguous images exist in the dataset.

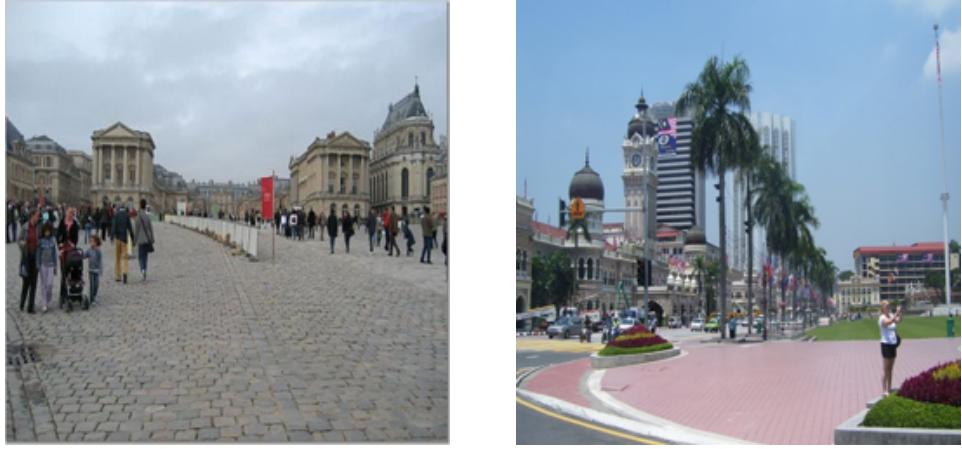


FIGURE 3.2: 2 Figures from the Weather Dataset [11].

In general, the two datasets are different. The ImageNet dataset is for object classification and the weather dataset is for scene classification.

3.2 Data Argumentation

CNN architecture [13] has about 60 million parameters, and it is easy to overfit. Data argumentation can reduce the risk of overfitting. The dataset is artificially enlarged by cropping and horizontal reflecting images. For each 256×256 image, five 224×224 patches are extracted from four corners and center, then they are reflected horizontally. 10 patches are extracted from one image in total. Figures 3.3 illustrates the method of data argumentation.

3.3 Spatial Pyramid Pooling (SPP)

Features, which are useful for scene classification, can be at any spatial position in an image. This could be a problem to CNN, because the architecture suits to recognise objects in the center of images. A SPP layer can help to solve the problem.

A SPP layer is deployed behind the fifth convolutional layer. A set of bins are set to discern different local information from the output of the fifth convolutional layer.



FIGURE 3.3: A set of cropped patches from original image

Assuming dimensions of feature maps are $a \times a$ and the bin size is n , each window size is $\lceil a/n \rceil$ and stride size is $\lfloor a/n \rfloor$, where $\lceil \cdot \rceil$ and $\lfloor \cdot \rfloor$ denote the ceiling and flooring operations. For the l level pyramid, there are l SPP layers. The layers will be concatenated into a fully connected layer. The bin sizes can be set to 1, 2, 3 and 6 for the SPP layers.

With the help of the SPP layer, most features of different scales are taken into account.

3.4 Convolutional Neural Networks Architecture

Due to significant performance of the AlexNet [13] which is a deep neural network, we train a model based on the network architecture. The architecture of the network has seven hidden adaptive layers, which are five convolutional layers and two fully connected layers. The network is very deep and has a huge number of parameters. It was implemented on two GPUs in the original experiment. The model achieves 62.5% accuracy rates with one prediction and 83% accuracy rates with five predictions in the competition.

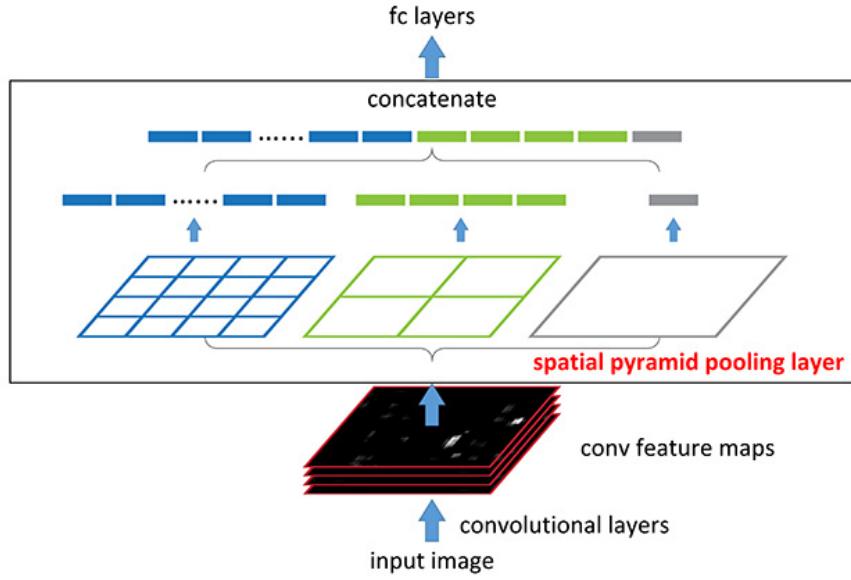


FIGURE 3.4: Diagram of the SPP layer [12]

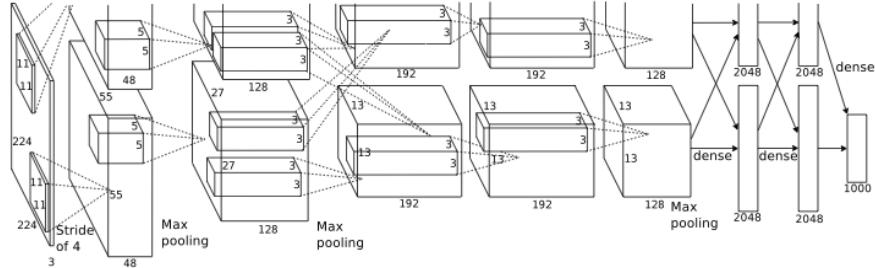


FIGURE 3.5: Architecture of the AlexNet [13]

The network uses ReLU [31] as the activation function, which learns a model faster than tanh function does.

In the network, there are three types of layers and they play different roles in the model. The input data dimension is $224 \times 224 \times 3$. In the first convolutional layer, there are 96 kernels with size 11×11 . The stride size is 4 and the outputs are 96 neurons. A following max pooling layer downsamples the spatial dimension. The second layer scans the output of the previous pooling layer with 256 kernels with size 5×5 . The third layer owns 384 kernels with size 3×3 . The fourth layer has 384 kernels with size 3×3 and the last layer has 256 kernels with size 3×3 . After the convolutional layers, two fully connected layers have 4096 neurons each. At the end of network, there is a softmax layer with 1000 outputs.

Layer Name	Layer Description
Input	224×224 RGB image
CONV1	11×11 conv, 96 ReLU neurons, stride 4
POOL1	3×3 max pooling, stride 2
CONV2	5×5 conv 256 ReLU neurons, stride 1
POOL2	3×3 max pooling, stride 2
CONV3	3×3 conv 384 ReLU neurons, stride 1
CONV4	3×3 conv 384 ReLU neurons, stride 1
CONV5	3×3 conv 256 ReLU neurons, stride 1
POOL5	3×3 max pooling, stride 2
SPP	bin size 1,2,3,6
FC6	fully connect, ReLU 4096 neurons
FC7	fully connect, ReLU 4096 neurons
FC8	fully connect, ReLU 1000 neurons
SOFTMAX	1000 way softmax

TABLE 3.1: Architecture of the model

Chapter 4

Experiment

The experiment environment includes hardware, which is i7 CPU, 8G RAM and a GeForce GTX 770, and software, which is Ubuntu Linux 14.04 and Caffe [32], a deep learning software framework. We trained a model by Caffe.

4.1 Training Neural Networks

We trained the model with the 1000-category ImageNet2012 dataset. We used the network architecture [33] which achieved an excellent accuracy in 2013 ImageNet Competition. We implemented SPP with CUDA C language and deployed it before the first fully connected layer.

In the experiment, a subset of the ImageNet dataset, which contains 1.2 million labelled high-resolution images depicting 1000 object categories and 50,000 validation images, is used as training dataset. Most images are multi-scale and some are grey. To feed them into the network conveniently, it is considered better to convert them to the same dimensions. The images are resized to 256×256 . Grey images are combined triple times to simulate RGB images. The model is trained on raw RGB values of pixels. The activation function is the ReLU, which guarantees fast training of the neural network.

$$f(x) = \max(0, x) \tag{4.1}$$

The model 3.5 is trained with a descent optimisation method, SGD. The batch size is 128, and the momentum is 0.9. In each layer, the weights are initialised with a Gaussian distribution which has the mean of 0, and the standard deviation of 0.01. The neuron bias, in the $Conv_2$, $Conv_4$, $Conv_5$ and fully connected layers, is initialized with value 1, while the other bias is initialised with value 0.

The learning rates are set equally for all layers. They are initialised at 0.01 and decrease with the stepdown policy which means that they would drop by a factor of 10 after each 100,000 iteration. In total, the learning rate drops 3 times and the accuracy keeps stable after 370,000 iterations.

The training is regularised via the techniques, including dropout and weight decay. The dropout regularisation is implemented at the two fully connected layers and the dropout ratio is 0.5. The neurons, which are dropped out, output zero and do not participate in the backpropagation process. Therefore, the neural network samples different architectures each time. This significantly decreases complex co-adaptations of neurons because they do not depend on the existence of other neurons. The weight decay, ϵ , is set to 0.0005 which means the new weights are shrunk according to

$$w^{new} = w^{old}(1 - \epsilon) \quad (4.2)$$

after each update.

4.2 Fine-tuning Model

There are two challenges to training on the original model. Firstly, the original CNN model is trained to classify images of 1000 categories. However, the current task is to classify the two weather scenes. This can be solved by reducing the outputs of the model from 1000 to 2. Secondly, the CNN architecture contains about 60 million parameters which are too many for the weather classification dataset. The target dataset has only 10000 images in total. The number of images is insufficient and the model is feasible to overfit. It can be solved by training a new model based on the existing CNN model. Because the learned model is close to optimism, only a tiny adjustment is needed.

The fine-tune transfers the weights of each layer from the previous model to the new model except for the last fully connected layer. The last layer is taken over by a new layer which contains the same amount of neurons equally to the class number. The weights in the replaced layer are initialized with random values. One advantage of fine-tune is to minimise risk of overfitting. The other is that weights reach optimal values quickly.

9000 images are used for training and 1000 images are reserved to test the model. The batch size is 128. There are 10000 iterations in the training process totally. Then the total training image number is 128×9000 . One epoch is that the total training images are fed into the network once. The training epochs are 142. The initial base learning rate is 0.001 and the rate is divided by 10 every 10 epochs. Because the weights in *FC8* are randomly initialised and they are not close to final optimization value, the learning rate for *FC8* is 10 times of the base learning rate to converge quickly.

4.3 Companion Experiments

In order to compare performance of the fine-tuned model, we did extra tests with extracting feature methods. We used a pre-trained model with the AlexNet architecture and extracted features from the layer *FC7*. We trained a SVM classifier based on the features and classified the test samples by it.

4.4 Experimental Results

The results in table 4.1 illustrates that the models, trained by the neural networks, have better performance than the extracting features method.

Methods	CNN+SVM	SPP+SVM	Finetune on CNN	Finetune on SPP
Accuracy	84.8%	82.1%	93.1%	93.98%

TABLE 4.1: The first test is extracting features from the pre-trained CNN model and training a SVM classifier. The second test is similar with the first except for extracting features from the CNN model with a SPP layer. The third test is fine-tuning the model with AlexNet architecture. The fourth test is fine-tuning the CNN model with a SPP layer

The fine-tuning process converge quick. After about 30 epochs, the accuracy rate exceeds 90%.

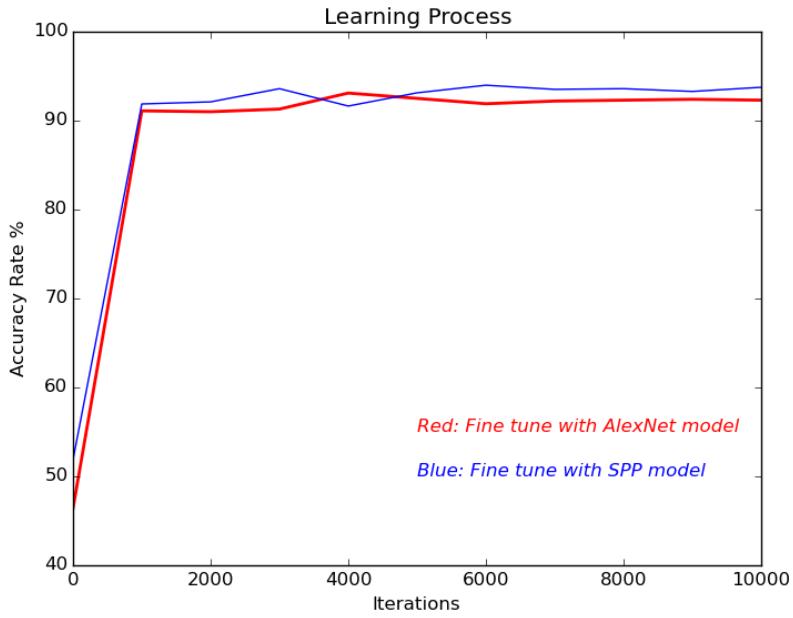


FIGURE 4.1: Learning Process

The learning process may overfit and it will definitely damage model generalisation capability. From figure 4.1, we find that there is no overfitting in the fine-tuning process.

In order to have a more detailed information of fine-tuning process, we investigate the training loss values. We plot the curve and the loss values during the first 200 iterations.

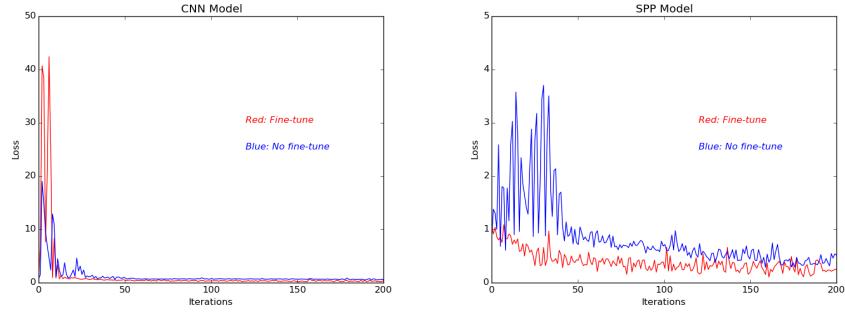


FIGURE 4.2: Training Loss

From figure 4.2, it is clear that the fine-tuning procedure produces a smoother loss curve and ceases at a higher accuracy rate. In the left figure, the loss value of the fine-tuning procedure is higher than the value of the no fine-tuning process at the beginning. Then it shrinks sharply and maintains lower than the value of the non fine-tuning process. In the right figure, we can find that initial loss values are less than those in the left figure. And the loss value of the fine-tuning process is less than the value in the non fine-tune

process. In short, fine-tune is an effective approach to train a new model. The model with SPP layers achieves high performance.

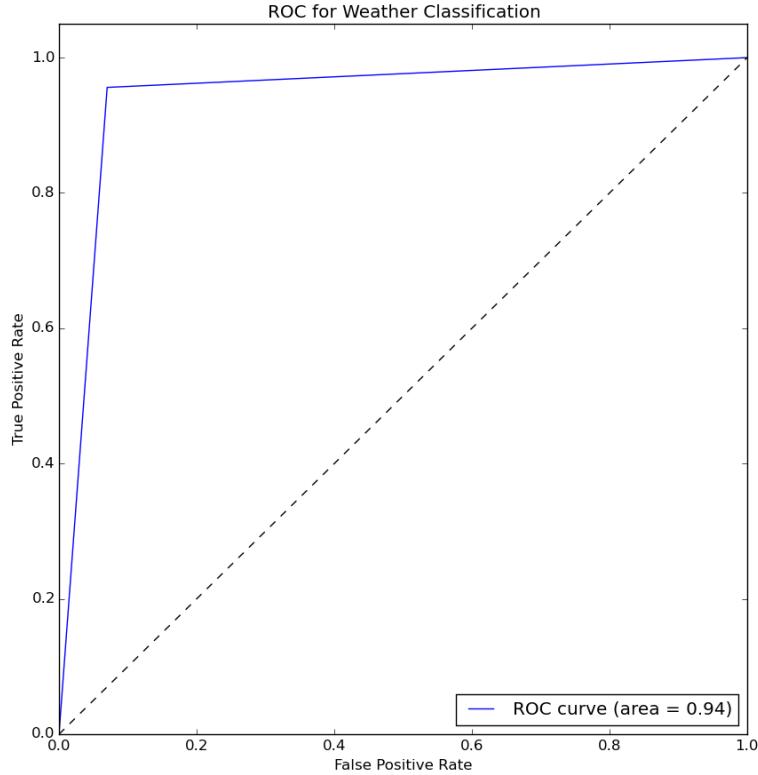


FIGURE 4.3: ROC Curve

4.5 Architecture Analysis

CNN has achieved excellent accuracy in the object classification field, although a full understanding of the mechanism is ambiguous. In order to have some intuition about CNN, we will analyse the network outputs.

The outputs of each layer have been treated as visual descriptors [34], and the vectors present some information from the outputs of previous layers. The front layers encode low-level features, and the rear layers are able to capture high-level information. In other words, an image is retrieved heuristically when it passes the convolutional layers.

Fully connected layers can be represented as a d -dimensional vector. The layer takes multidimensional outputs from the previous layer and flats the feature maps into a d -dimensional vector. The outputs of the second fully connected layer are feed into a classifier.

When a cloudy image is fed into the CNN, figure 4.4 shows the feature maps of convolutional layers. Because the filter size is too many, only parts of the filters are plotted in b-d.

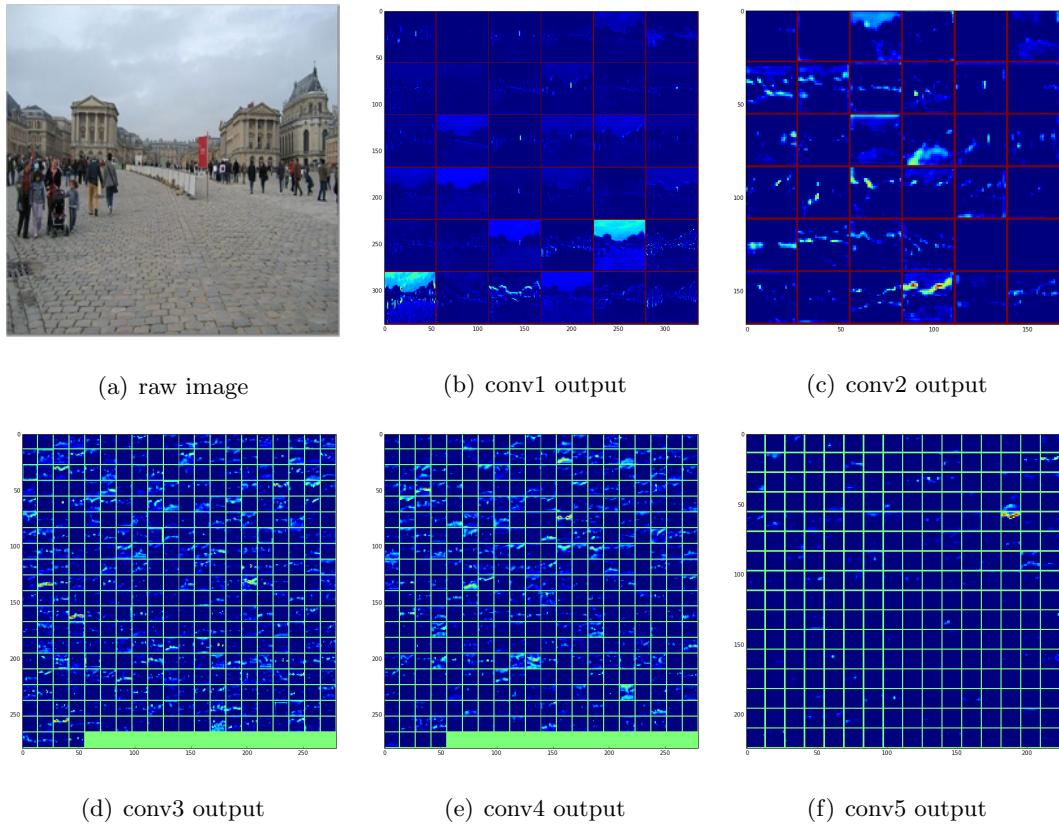


FIGURE 4.4: A cloudy image and the feature maps from convolutional layers

In figure 4.5, a sunny image is fed into CNN and the according outputs are plotted.

The outputs of $CONV1$ and $CONV2$ are still partly recognisable by people. The outputs of the $CONV3$ and $CONV4$ are unrecognisable. From the outputs of $CONV5$ for the sunny image, the position of sun light is highlighted by several filters. However, the according filters show no signs about the cloudy image.

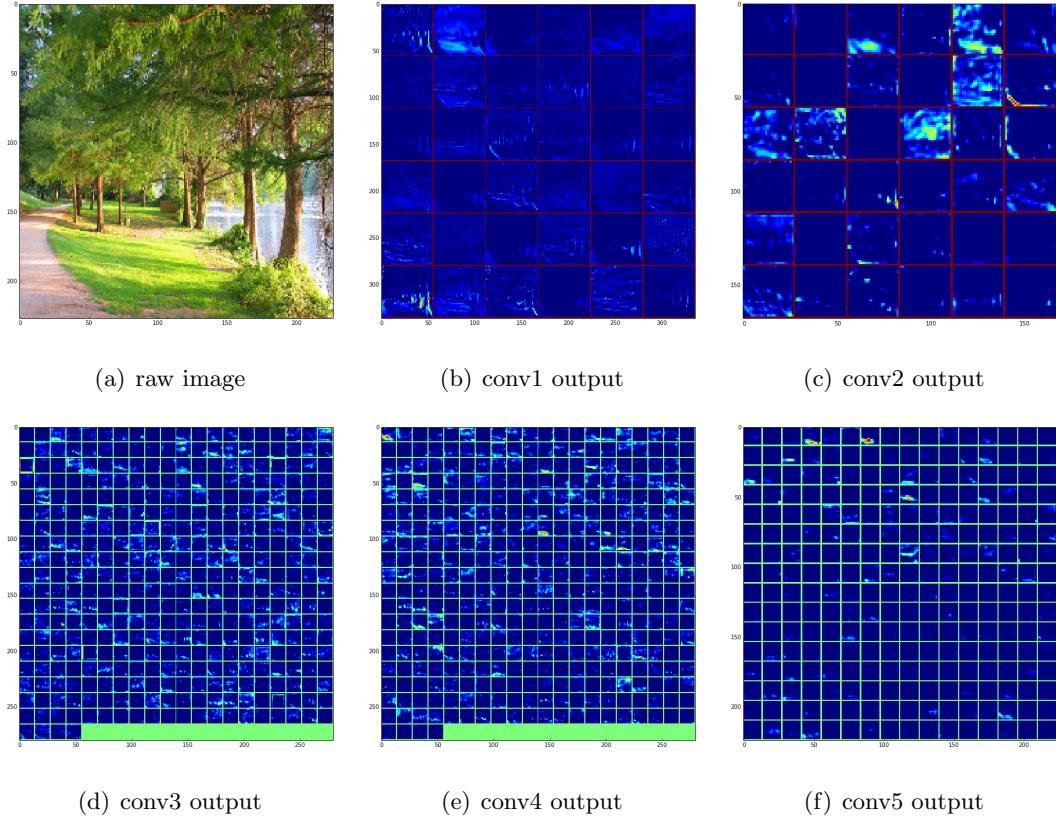


FIGURE 4.5: A sunny image and the feature maps from convolutional layers

4.6 Effects of SPP Layer

The outputs of SPP layers cannot be represented as visual descriptors, then only the feature maps of the convolutional layers are compared in the models. The outputs of *CONV1* and *CONV2* show that more features are recognisable in the SPP model. It illustrates that the SPP model has stronger representation capability than the CNN model does.

In figure 4.7, the histograms of the outputs from the layer *FC7* are displayed. Comparing histogram difference, the generated features of the SPP model is more divisible than those of the CNN model.

From the feature maps and histogram distributions, it is clear that the SPP model has strong representing capability and can generate divisible features to classifiers.

Image	Conv1	Conv2	Conv3	Conv4	Conv5
Image	Conv1	Conv2	Conv3	Conv4	Conv5

FIGURE 4.6: Visiualisation of feature maps from the CNN model and the SPP model. The upper images are from the CNN model and the lower images are from the fine-tuned model.

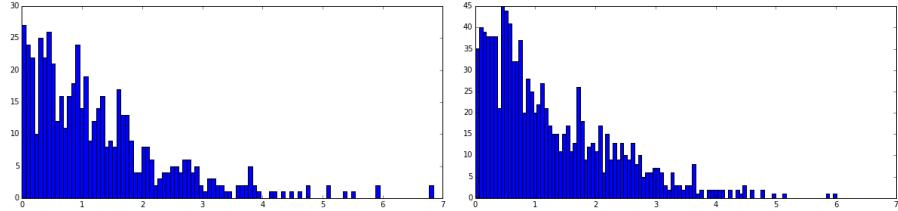


FIGURE 4.7: Histogram distribution of vectors from FC7. The left is from CNN model and the right is from the SPP model.

4.7 Error Results

The images in figure 4.8 are misclassified by the CNN model and the SPP Model. They are difficult to judge sunny or cloudy, even for people.

4.8 Conclusion and Future Work

In this experiment, we present an effective approach to perform weather classification through CNN and transfer learning. The result illustrates the strong capacity of CNN and the convenience of transfer learning. Compared with the traditional methods, which extracts features and trains a classifier based on the features, the CNN method does not depend on specific feature detectors and achieves high accuracy.

In the future, the full understanding of the CNN mechanism is a demanding work. And the work can be extended to multi-class weather classification and implemented in industry widely.

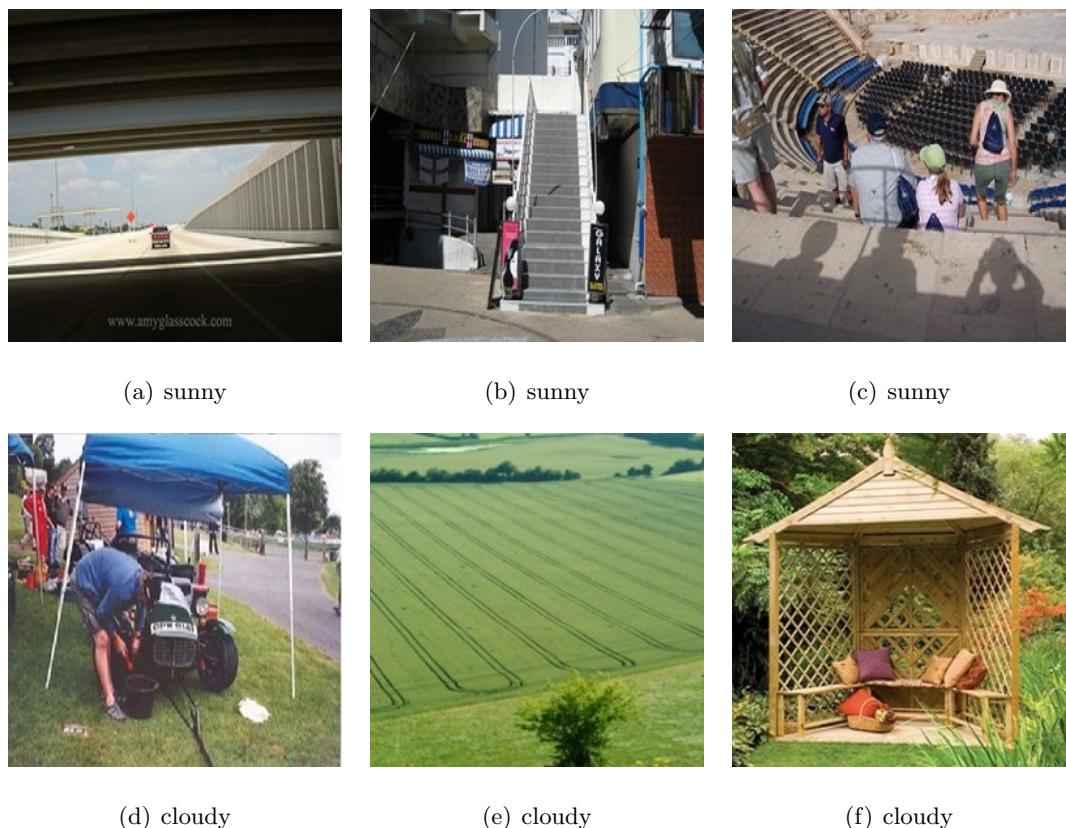


FIGURE 4.8: Misclassified images [11].

Part II

Multilabel Learning

Chapter 5

Introduction

5.1 Overview

In the literature on machine learning, multi-label classification is a variant of classification problem where each sample has several labels. In general, the task of multi-label learning is to train a model that can map inputs \mathbf{x} to a set of binary vectors \mathbf{y} . It differs with multi-class classification in terms of the output label space.



FIGURE 5.1: Example Image

The difference between single-label classification and multi-label classification is the number of output labels. In figure 5.1, we can classify it as a picture of a beach in

X_1	X_2	X_3	X_4	X_5	Y_1	Y_2	Y_3	Y_4
1	0.4	0.2	0	1	0	1	1	0
0	0.2	0.6	1	1	1	0	1	0
0	0.5	0.8	1	1	0	0	1	0
1	0.1	0.4	0	1	1	1	1	0
1	0.8	0.2	0	1	0	1	1	0
0	0.5	0.3	1	1	?	?	?	?

TABLE 5.1: Multilabel $Y_1, \dots, Y_L \in 2^L$

single-label classification problem $\in \{Yes, No\}$. In multi-label classification, we can tag beach, sea, chairs, sand for the picture $\in \{beach, sea, chairs, sand\}$.

In general, there are two main approaches to tackle the multi-label classification problem. One method is to transfer a multi-label problem into a set of binary classification problems which can be handled by a set of binary classifiers. The other one applies algorithms to classify multi-label images directly.

Several problem transformation methods can be applied to multi-label classification. A baseline method, the binary relevance method [35], trains one binary classifier for each label independently. Depending on the results of the classifiers, the combined model predicts all labels for a test sample. The method divides the problem into multiple binary works which are common in something with the one-vs-all method for multi-class classification. Problem transformation methods benefit from scalability and flexibility because single-label classifier can be implemented easily. SVM, Naive Bayes, and k Nearest Neighbor have been used in the method [35].

Other transformation methods include label powerset transformation. The method builds up one binary classifier for each label combination verified in the training dataset [36]. The random k -labelsets algorithm [37] utilises a multi-label powerset classifier which is trained on a random subset of the labels. Finally, a voting scheme predicts test samples via an ensemble method.

5.2 Multi-Label Learning

Let $X = R^d$ represent the domain of dataset and let $Y = 1, 2, \dots, L$ be the finite set of labels. Given that we have a set of training dataset $T = (x_1, Y_1), (x_2, Y_2), \dots, (x_l, Y_l)$ ($x_i \in X, Y_i \subset Y$) which are extracted from an unknown distribution D . Target of task is

to learn a multi-label classifier $h : X \rightarrow 2^y$ via optimising specific evaluation metric. However, instead of learning a multi-label classifier, we will learn a function f while $f(X) \rightarrow R^d$. Given that a high performance classifier can output a closer subset for labels in Y_i than those missing or exceeding in Y_i , then $f(x_i, y_1) > f(x_i, y_2)$ if $y_1 \in Y_i$ and $y_2 \notin Y_i$. We can transfer real valued function $f(\cdot, \cdot)$ to a ranking function $r(\cdot, \cdot)$ that maps the outputs of $f(x_i, y_1)$ to any $y \in Y$ if $f(x_i, y_1) > f(x_i, y_2)$. It is worth noting that the multi-label classifier $h(\cdot)$ can be derived from the function $f(\cdot, \cdot)$, where $h(x_i) = y | f(x_i, y) > t(x_i), y \in Y$, and $t(\cdot)$ is a threshold function.

Single-label and multi-class classification can be regarded as two degenerated variants of multi-label learning problem if each sample has only one single label. However, multi-label problem is much more difficult than traditional single-label problems because of high dimensional output space. For example, the number of label sets increases exponentially with increasing number of class labels. If there are 10 class labels for dataset, there are 2^{10} possible label sets maximum.

A huge combination of output labels is a challenge. One of methods is to investigate dependency among labels to reduce label space. For example, if an image labelled with *castle*, it would be highly labelled with *brick* and *mountain*. A movie, is labelled with *comedy*, is unlikely to be related to a *documentary*. Therefore, successful exploitation of label correlations is regarded as an effective approach to high accuracy multi-label learning machine. There are three strategies, depending on the order of the label correlation, to find the relation between labels. They are first order strategy, second order strategy and high order strategy.

The first order strategy treats the label by label independently and ignores correlation between labels. It can be regarded as decomposing a multi-label learning problem into a set of binary classification problems based on each label. The method benefits from simple computation and high efficiency. However, accuracy could be suboptimal because of ignoring the correlation of labels.

The second order strategy considers pairwise relations between labels. For example, the interaction between any pair of labels, or the ranking between related and unrelated labels. The method achieves good generalisation performance because the label correlations are investigated in some extent. In real world, there are higher order correlations than second order assumption in many applications.

The high order strategy investigates more than 2 order correlations among labels which can be the influence on each label or addressing connections among sub space of output labels. It is obvious that the high order strategy is more capable than the previous two strategies on the cost of complexity and intensive computation.

Chapter 6

Background

Compared to general classification, multi-label classification has different evaluation metrics and learning algorithms.

6.1 Evaluation Metrics

In supervised learning, different metrics, such as accuracy and area under the ROC curve, are used to evaluate the generalisation performance of a model. In the multi-label learning, evaluating performance is more complicated than single-label classification problems because of increasing number of labels simultaneously. Therefore, two main types of evaluation methods are implemented in multi-label learning, example-based metrics [38] and label-metrics [37].

The two types of metrics evaluate outputs of classifiers from different perspectives. Given that $S = (x_i, Y_i)$ is a test sample and $h(\cdot)$ is the learned multi-label classifier. The concept of example-based metrics is to achieve all class labels of each test sample, and then compute the mean value of the test sets to evaluate generalisation performance. Compared with considering all class labels simultaneously, label-based metrics evaluate performance by treating each class label separately and computing macro/micro-averaged value of all class labels.

In supervised classification, the ground truth output and the predicted output are compared for each test sample. So the results of each test sample can be assigned to one of the four categories:

- True Positive (TP) - label is positive and prediction is also positive
- True Negative (TN) - label is negative and prediction is also negative
- False Positive (FP) - label is negative but prediction is positive
- False Negative (FN) - label is positive but prediction is negative

Here we define a set D of N examples and Y_i to be a family of ground truth label sets and $P_i = h(x_i)$ to be a family of predicted label set. The union set of all unique labels is

$$L = \bigcup_{i=0}^{N-1} L_i \quad (6.1)$$

While the definition of indicator function I_A on a set A is presented:

$$I_A(x) = \begin{cases} 1 & \text{if } x \in A \\ 0 & \text{otherwise} \end{cases} \quad (6.2)$$

6.1.1 Example-based Metrics

Hamming Loss evaluates performance via counting the number of misclassification labels. The smaller value of hamming loss is, the better performance the model has.

$$\frac{1}{N \cdot |L|} \sum_{i=0}^{N-1} |L_i| + |P_i| - 2 |L_i \cap P_i| \quad (6.3)$$

Subset Accuracy evaluates the fraction of correctly predicted example while the predicted label set is identical to the ground truth label set. It is equivalent to traditional accuracy metric.

$$\frac{1}{N} \sum_{i=0}^{N-1} I_{\{L_i\}}(P_i) \quad (6.4)$$

Precision is defined as:

$$\frac{1}{N} \sum_{i=0}^{N-1} \frac{|L_i \cap P_i|}{|P_i|} \quad (6.5)$$

Recall is defined as:

$$\frac{1}{N} \sum_{i=0}^{N-1} \frac{|L_i \cap P_i|}{|L_i|} \quad (6.6)$$

Accuracy is defined as:

$$\frac{1}{N} \sum_{i=0}^{N-1} \frac{|L_i \cap P_i|}{|L_i| + |P_i| - |L_i \cap P_i|} \quad (6.7)$$

F1 Measure is an integrated version combined by harmonic mean of **Precision** and **Recall**.

$$\frac{1}{N} \sum_{i=0}^{N-1} 2 \frac{|P_i \cap L_i|}{|P_i| \cdot |L_i|} \quad (6.8)$$

6.1.2 Label-based Metrics

Macro Precision (precision averaged across all labels) is defined as:

$$PPV(\ell) = \frac{TP}{TP + FP} = \frac{\sum_{i=0}^{N-1} I_{P_i}(\ell) \cdot I_{L_i}(\ell)}{\sum_{i=0}^{N-1} I_{P_i}(\ell)} \quad (6.9)$$

Macro Recall (recall averaged across all labels) is defined as:

$$TPR(\ell) = \frac{TP}{P} = \frac{\sum_{i=0}^{N-1} I_{P_i}(\ell) \cdot I_{L_i}(\ell)}{\sum_{i=0}^{N-1} I_{L_i}(\ell)} \quad (6.10)$$

F1 Measure by label is the harmonic mean between **Precision** and **Recall**.

$$F1(\ell) = 2 \cdot \left(\frac{PPV(\ell) \cdot TPR(\ell)}{PPV(\ell) + TPR(\ell)} \right) \quad (6.11)$$

Micro Precision (precision averaged over all example/label pairs) is defined as:

$$\frac{TP}{TP + FP} = \frac{\sum_{i=0}^{N-1} |P_i \cap L_i|}{\sum_{i=0}^{N-1} |P_i \cap L_i| + \sum_{i=0}^{N-1} |P_i - L_i|} \quad (6.12)$$

Micro Recall (recall averaged over all the example/label pairs) is defined as:

$$\frac{TP}{TP + FN} = \frac{\sum_{i=0}^{N-1} |P_i \cap L_i|}{\sum_{i=0}^{N-1} |P_i \cap L_i| + \sum_{i=0}^{N-1} |L_i - P_i|} \quad (6.13)$$

Micro F1 Measure by label is the harmonic mean between **Micro Precision** and **Micro Recall**.

$$2 \cdot \frac{TP}{2 \cdot TP + FP + FN} = 2 \cdot \frac{\sum_{i=0}^{N-1} |P_i \cap L_i|}{2 \cdot \sum_{i=0}^{N-1} |P_i \cap L_i| + \sum_{i=0}^{N-1} |L_i - P_i| + \sum_{i=0}^{N-1} |P_i - L_i|} \quad (6.14)$$

For the label-based metrics, the larger metrics value means the higher generalisation performance.

With the previous metrics, there are diverse methods to evaluate model generalisation performance. In most multi-label classification, learning algorithms optimise one of the metrics. To make evaluation fair and precise, learning algorithms should be tested on different metrics to evaluate performance.

Most metrics are non-convex and discrete, and most algorithms turn to optimise alternative multi-label metrics. Recently, some researchers have been studying the consistency of multi-label learning [39].

6.2 Learning Algorithms

Algorithms play a key role in the literature on machine learning, and there is no exception in multi-label learning. The capability of representation is important to evaluate the performance of an algorithm. Moreover, some relating criterions can be used to measure performance. First, the broad spectrum should be considered. An algorithm should cover a range of algorithmic design strategies with unique characteristic. Second, it is reasonable to evaluate the impact which the algorithm poses on the multi-label learning settings. Last, computational complexity is a critical factor to evaluate an algorithm.

6.2.1 Problem Transformation Methods

6.2.1.1 Binary Relevance (BR)

The Binary Relevance method is an elementary algorithm which decomposes a multi-label learning problem into a set of independent binary classification problems, and each problem harmonises one label in the set $L = y_1, y_2, \dots, y_q$. The approach initially

transforms the multi-label dataset into q binary datasets $D_{y_i}(i = 1, 2, \dots, q)$, where each D_{Y_I} includes all samples of the multi-label dataset and has a single binary label to instruct if the dataset has or has no attribute to the relevant label. For example, if a sample has a positive value means that the sample owns the correlation label, otherwise, it does not own it. After transforming the dataset, a set of q binary classifiers, $H_i(E)(i = 1, 2, \dots, q)$, have been built up using the respective training dataset D_{y_i} .

$$H = \{C_{y_i}(x, y_i) \rightarrow y'_i \in \{0, 1\} | y \in L, i = 1, 2, \dots, q\} \quad (6.15)$$

To classify a test sample, the BR method outputs the collection of labels which are predicted with positive value by the independent binary classifiers.

The BR method combines computational efficiency and simple implementation. With a constant number of samples, the algorithm scales with size q of label set L . Supposing that each classifier has complexity $f(|X|, |D|)$, The method has complexity $O(q \times f(|X|, |D|))$. With a limit number of q , the method learns a model quickly and has an reasonable performance.

One of the disadvantages is the limitation to label relationship information. Unless all labels are independent, the method losses the correlations among labels.

6.2.1.2 Classifier Chains (CC)

To pursue a better performance, the CC method has been introduced in multi-label classification [35]. The method transforms multi-label learning problems into a chain of binary classifiers based on label dependence.

For a set of q labels L , the CC method learns q classifiers as BR does. In addition, it links all classifiers in feature space. Given that there are a set of samples $D(x, y_i)(i = 1, 2, \dots, q)$ where y_i is a subset of labels L and x is the domain of dataset. The original dataset is transformed into a set of q datasets in which the j th example is based on the previous dataset.

$$H = \{C_{y_i}(x, y_1, y_2, \dots, y_{i-1}) \rightarrow y'_i \in \{0, 1\} | y \in L, i = 1, 2, \dots, q\} \quad (6.16)$$

Thus it forms a chain of binary classifiers C_1, C_2, \dots, C_q . Each classifier C_i learns and predicts the binary association of label y_i based on the dataset x and all prior binary relevance predictions $y_j, j = 1, 2, \dots, i-1$. The learning process starts from C_1 and follows the chain sequentially. Therefore, C_1 determines $p(y_1|x)$, and sequential classifiers, C_2, \dots, C_q , determine $p(y_i|x_i, y_1, \dots, y_{i-1})$.

The CC method propagates label information through classifiers, and latter classifiers take account of previous predictions. This method can retrieve lost information among labels partly. At the same time, the method maintains advantages of BR, such as computation efficiency and memory efficiency. The computational complexity of the method is close to BR in terms of the number of labels and complexity of elemental classifiers C_i . As previous statement, the computational complexity of BR is $O(q \times f(|X|, |D|))$ where $f(|X|, |D|)$ represents the elemental classifier. With extra computation introduced by previous labels, the computational complexity of the CC is $O(q \times f(|X| + q, |D|))$, while the computation will be unaffordable in case of $q \gg |X|$.

6.2.2 Algorithm Adaptation Methods

6.2.2.1 Multi-label k-Nearest Neighbour (ML-kNN)

The algorithm adapts k-nearest Neighbour techniques to propose multi-label data and utilise the MAP to make prediction through reasoning embodied labelling information among neighbours [40].

Given dataset X and its label set Y , y represents an output vector for x where i -th element $y(i)$ is positive if $i \in Y$, otherwise it is negative. Given that $N(x)$ is the set of neighbours of x in the training dataset, we can compute a membership counting vector which represents the number of neighbours of x owning the l -th label.

$$C_x(i) = \sum_{a \in N(x)} y_a(i), i \in Y \quad (6.17)$$

To test a new sample t , the algorithm sorts out its category in the training dataset by kNN $N(t)$. H_1^l denotes that t has the label l and H_0^l denotes that t do not have the label

l . If j samples have the label l , $E_j^l(j \in 0, 1, \dots, k)$, the category vector y_t is determined by the MAP principle:

$$y_t(l) = \arg \max_{b \in \{0,1\}} P(H_b^l | E_{C_t(i)}^l) l \in Y \quad (6.18)$$

With the Bayesian rule, equation 6.18 can be represented as:

$$y_t(l) = \arg \max_{b \in \{0,1\}} P(H_b^l) P(E_{C_t(i)}^l | H_b^l) l \in Y \quad (6.19)$$

As stated in equation 6.19, the output of a test sample t is $y_t(l)$. It can be computed through prior probability $P(H_b^l) l \in Y, b \in \{0, 1\}$ and the posterior probability $P(E_j^l | H_b^l)(j \in \{0, 1, \dots, k\})$.

6.2.2.2 Collective Multi-label Classifier (CML)

Given that labels are highly interdependent in some scenarios, the CML explores multi-label conditional random field (CRF) classification models which learn parameters for each pair of labels directly [38].

In dataset (x, Y) , each sample has a corresponding random variables representation (x, y) , in which $y = (y_1, y_2, \dots, y_q)$ $y_i \in \{-1, 1\}$ is a binary label vector. If the sample contains j -th label, the j -th element of y is 1, otherwise -1. Then the aim is to learn the joint probability distribution $p(x, y)$.

The entropy of (x, y) is represented as $H_p(x, y)$ and gives the distribution $p(\cdot, \cdot)$ of (x, y) . The principle of maximum entropy can be achieved by maximising $H_p(x, y)$. The fact is expressed with constraints on the expectation of function $f(x, y)$. The expected value can be estimated from the training dataset

$$F_k = \frac{1}{m} \sum_{(x,y) \in D} f_k(x, y) \quad (6.20)$$

According to the normalisation constraint on $p(\cdot, \cdot)$, the optimal solution can be represented as:

$$p(y|x) = \frac{1}{Z(x)} \exp\left(\sum_{k \in K} \lambda_k \cdot f_k(x, y)\right) \quad (6.21)$$

Yielding to Gaussian distribution, parameters can be found in a convex log-posterior probability function. For a test sample x , the predicted label set follows to:

$$y_x = \arg \max_y p(y|x) \quad (6.22)$$

It is notable that the exact inference is only suitable for small label space via $\arg \max$, because it needs to reduce the search space of $\arg \max$ significantly via the pruning strategy. The CML is a second order approach.

Chapter 7

Methodology

7.1 Artificial Dataset

A dataset is generated artificially. Each image has three labels to represent colours, *red*, *green* and *blue*. The representation of colour combination follows colour wheels. If an image is a red hue only, it has a label for *red* while the label values of *green* and *blue* are negative. If an image has a hue close to *purple*, it has positive labels for *red* and *blue*, and negative label for *green*, and so on.

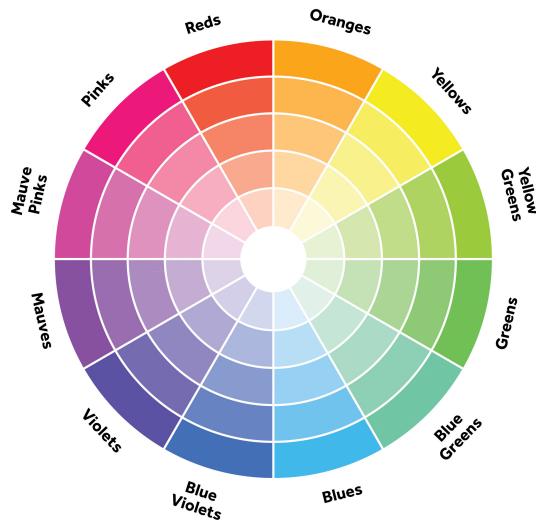


FIGURE 7.1: Colour Wheel Diagram [14]

For each sample x_i , it owns 3 labels $y_0, y_1, y_2, y_j \in \{-1, 1\}$ which represent *red*, *green* and *blue* respectively.

7.1.1 Generating Images

The RGB and HSV coordinate systems represent a geometric shape in colour space. The distance among colours contains little meaning. However, corresponding distance makes some intuitive sense and enable conversion possible between RGB and HSV coordinates.

The dataset consists of images with size 16×16 , therefore each image has 256 pixels. To generate an image, I generate a random floating point number h in the range $[0.0, 1.0)$ and use it as value for a hue via formulation

$$H = h + r * 0.4 - 0.2 \quad (r \in [0.0, 1.0)) \quad (7.1)$$

where r is another random float number. 2 random float numbers are generated for Saturation(S) and Value(V) values. The HSV values are converted to the RGB values and timed 255 for each pixel. Following that, an image with 256 pixels is generated. Because a RGB image is converted to a HSV image, the label values are based on the previous value h .

The dataset contains 1000 images in total. 960 images are training samples and 40 are test samples.

7.2 Artificial Neural Networks (ANNs)

ANNs is an approach to learning a non-linear function which can map a sample to several labels. The neurons in the first layer take a raw image, while the neurons in the last layer produce outputs. Between the first and last layer, the middle layers are called hidden layers because they do not connect to the external world directly. A 3 layer neural networks can represent any bounded degree polynomial under certain conditions [41]. The weights of neural network are learned by algorithms deployed over training dataset. One of the successful learning algorithms is the Backpropagation algorithm which updates weights by propagating error values computed by comparing prediction for each sample.

Two factors will be modified to adapt a neural network to perform multi-label classification. One factor is to design a new error function which fits the characteristics of

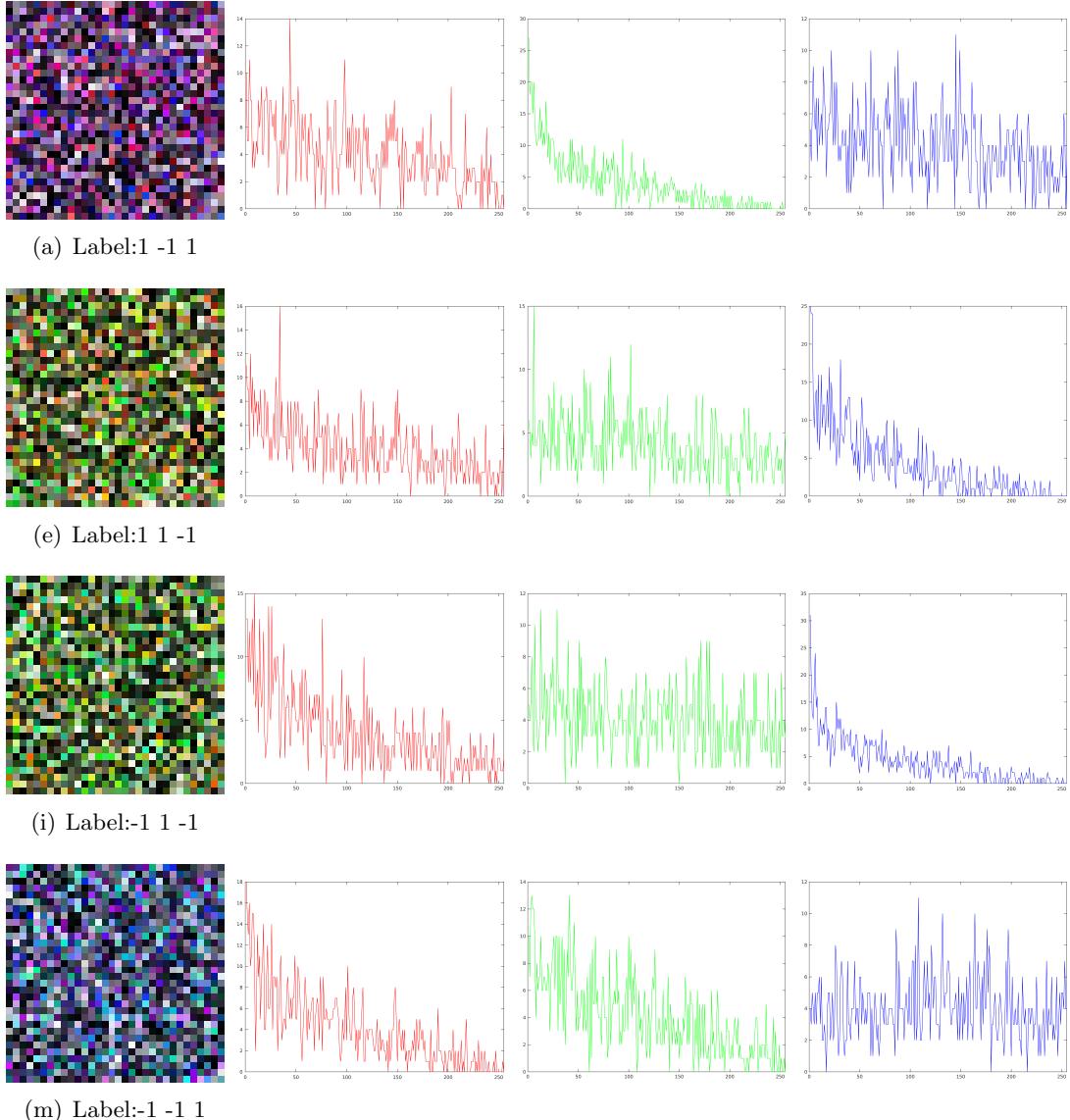


FIGURE 7.2: Multilabel samples and the RGB colour histograms. Three labels mean red, green and blue sequentially.

multi-label samples instead of single-label ones. The other is to select a moderate metric according to the new error function.

7.2.1 Network Architecture

Define $\mathcal{X} = \mathbb{R}^d$ as the sample space and $\mathcal{Y} = 1, 2, \dots, Q$ as the set of output labels. The training dataset is composed of m multi-label samples, $(x_1, Y_1), (x_2, Y_2), \dots, (x_m, Y_m)$, while each sample $x_i \in \mathcal{X}$ is represented as a d -dimension feature vector and a set of q labels associate with the feature vector. A neural network, in figure 7.3, can be built up to learn a model .

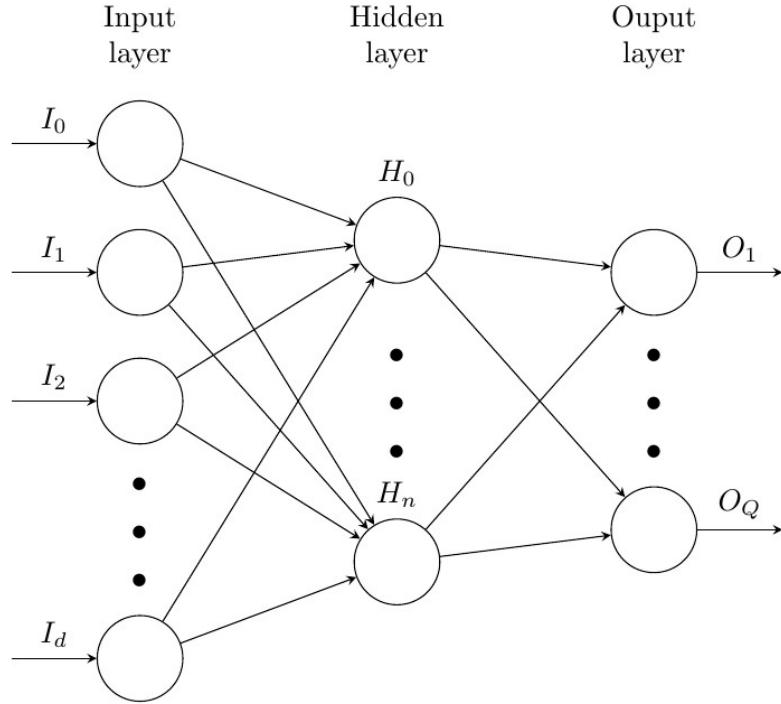


FIGURE 7.3: Network Topology For Multi-lable Classification

The network has d input neurons which correspond to a d -dimension feature vector, while the last Q neurons represent a combination of output labels. There is a hidden layer in figure 7.3 which owns n hidden neurons. The input layer is fully connected with the hidden layer and the same connecting method is deployed between the hidden layer and the output layer. There are $d \times n$ weights ($W_{ih}, 1 \leq i \leq d, 1 \leq h \leq n$) between the first two layers, and $n \times q$ weights ($W_{ho}, 1 \leq h \leq n, 1 \leq o \leq q$) between the latter two layers. The bias parameters are represented as I_0 and H_0 .

Because the task of multi-label learning is to predict labels of test samples, it needs to evaluate the global error of the model as:

$$E = \sum_{i=1}^m E_i \quad (7.2)$$

E_i is the error on the sample x_i which can be defined as:

$$E_i = \sum_{j=1}^Q (c_j^i - d_j^i)^2 \quad (7.3)$$

where $c_j^i = c_j(x_i)$ is the predicted j -th label on sample x_i , and d_j^i is the actual j -th label of sample x_i . The actual label has value of either $+1(j \in \mathcal{Y}_i)$ or $-1(j \notin \mathcal{Y}_i)$.

Various learning algorithms can be used to learn a model based on the training dataset. The backpropagation algorithm is used to learn from errors. However, the algorithm could be improper in multi-label learning because the error function 7.3 neglects the correlations among labels of a sample. In original BP algorithm, the error function 7.3 limits on individual label discrimination, whether a specific label $j \in \mathcal{Y}$ belongs to the sample x_i or not. It should take into consideration that labels in Y_i are more important than those outside of Y_i . A new global error function is defined as:

$$E = \sum_{i=1}^m E_i = \sum_{i=1}^m \frac{1}{|Y_i||\hat{Y}_i|} \sum_{(k,l) \in Y_i \times \hat{Y}_i} \exp(-(c_k^i - c_l^i)) \quad (7.4)$$

In the error function 7.4, the i -th errors on the i -th sample (x_i, Y_i) are accumulated. \hat{Y}_i is complementary set of Y_i in \mathcal{Y} and $|\cdot|$ computes the cardinality of a set. Specifically, the item, $c_k^i - c_l^i$, represents the difference between the predicted labels and the actual labels. The error function 7.4 shows that bigger difference leads to better performance. Additionally, the negation of the difference is put into the exponential function to sharply penalise the i -th term if c_k^i is much smaller than c_l^i . The sum of i -th error term accumulates difference between outputs of any pair of labels which are the one belonging to the sample and the other one not belonging to it. The sum is normalised by the numbers of all pairs, $|Y_i||\hat{Y}_i|$. And then, the correlations between pair labels are computed. In other words, labels in Y_i should get larger output values than labels in \hat{Y}_i .

As in the previous statement, the error function 7.4 calculates the difference between output labels. The task of learning is minimising the error function 7.4 via enlarging output values of labels belonging to the training samples and diminishing the output values of the labels not belonging to it. If the training dataset can cover the distribution of the whole sample space, the model can learn it through minimising error function by feeding training samples.

7.2.2 Error Function

The basic goal of regression problems is to figure out the conditional distribution of the output labels with the input samples. It is common to use a sum-of-squares error function.

The basic aim of classification problems is to figure out the posterior probabilities of class types with the input samples. Except for the sum-of-squares error function, there are some more approximate error functions which can be considered.

The central goal is to model the hidden generator of the samples instead of memorising the training samples. Therefore, the best prediction of an input sample can be found if the network can present a new value for the sample. Because the general and complete characterisation of the dataset is the probability density $p(x, t)$, it is available to decompose a joint probability density into the product of the conditional density of the labels, the input data and the density of the data,

$$p(x, t) = p(t|x)p(x) \quad (7.5)$$

where $p(t|x)$ represents the probability density of t if x is a distinct label and $p(x)$ represents the density of x

$$p(x) = \int p(t, x)dt \quad (7.6)$$

Most error functions can be obtained from the idea of maximum likelihood. For training dataset,

$$L = \prod_n p(t^n|x^n)p(x^n) \quad (7.7)$$

where each sample is chosen randomly from the same distribution and their probabilities can be multiplied. The error function can be represented by minimising the negative logarithm of the likelihood since the negative logarithm is a monotonic function.

$$E = -\ln L = -\sum_n \ln p(t^n|x^n) - \sum_n \ln p(x^n) \quad (7.8)$$

where E is notated as an error function. The task of learning is to model the conditional probability density $p(t|x)$. The second term is also independent with the parameters in neural networks. We can simplify the equation 7.8 to

$$E = -\ln L = -\sum_n \ln p(t^n|x^n) + C \quad (7.9)$$

It is worth noting that error functions are dependent on different assumptions of the forms of the conditional distribution $p(t|x)$. In this classification task, t represents labels which act as class members or the prediction of the probabilities of class members.

7.2.3 Cross Entropy

MSE is a common risk metric comparable to the predicted value of the squared error loss. It is easy to implement and its value is non-negative. However, it has the disadvantage of heavily weighting outliers [42].

Given that there are two discrete distributions $p(x)$ and $q(x)$ over the same variable x . The relative entropy, relating to the cross entropy, is a measurement of the distance between samples:

$$D_{pq}(p(x), q(x)) = \sum_x q(x) \ln \frac{q(x)}{p(x)} \quad (7.10)$$

where the relative entropy is not a true metric because equation 7.10 could not be symmetric in the interchange $p \leftrightarrow q$ and probably not satisfy the triangle inequality.

Cross entropy loss, also named logistic regression loss, is an alternative measurement of a probability distribution. The measure is commonly used in neural networks. It can be used to evaluate the posterior probabilities of class membership.

Given that training a neuron, which has several input data, x_1, x_2, \dots , with weights w_1, w_2, \dots , and a bias, b , the outputs, for example two classes, can be represented as the weighted sum of the input data.

$$a = f(x) = \sum_i w_i x_i + b \quad (7.11)$$

Then the cross entropy loss function is

$$C = -\frac{1}{n} \sum_x [y \ln a + (1 - y) \ln(1 - a)] \quad (7.12)$$

where n is the number of training samples, a is the predicted label and y is the actual label.

The cross entropy acts as an error function because of two properties. First, C is non-negative, because the items of logarithms are in the range $[0, 1]$. Second, if the prediction output is close to the actual value for all training samples, the loss value, C , will be close to 0. Given that $y = 0$ and the prediction value $a \approx 0$, the first item in equation 7.12 is 0 and the second is $-\ln(1 - a) \approx 0$. The similar situation occurs for conditions, $y = 1$

and $a \approx 1$. Therefore, the value of loss function will be small, if the prediction value is close to the actual value.

In total, the cross entropy tends to 0, when the neuron acts better at predicting the output y for total training inputs x . The two properties are basic to a loss function. Although the quadratic loss function satisfies the properties, the cross entropy has the advantage on avoiding the issue of learning curve slowing down. To illustrate the advantage, the partial derivative of the cross entropy loss function can be done with respect to the weights. Applying the chain rule twice on equation 7.12

$$\frac{\partial C}{\partial w_j} = -\frac{1}{n} \sum_x \left(\frac{y}{f(x)} - \frac{(1-y)}{1-f(x)} \right) \frac{\partial f}{\partial w_j} \quad (7.13)$$

$$= -\frac{1}{n} \sum_x \left(\frac{y}{f(x)} - \frac{(1-y)}{1-f(x)} \right) f'(x) x_j. \quad (7.14)$$

where the second one can be represented as

$$\frac{\partial C}{\partial w_j} = \frac{1}{n} \sum_x \frac{f'(x) x_j}{f(x)(1-f(x))} (f(x) - y) \quad (7.15)$$

Because the definition of sigmoid function is $f(x) = 1/(1 + e^{-x})$ and the derivative of sigmoid function is $f'(x) = f(x)(1 - f(x))$. Then the items $f'(x)$ and $f(x) = 1/(1 + e^{-x})$ are cancelled in the equation and the equation becomes

$$\frac{\partial C}{\partial w_j} = \frac{1}{n} \sum_x x_j (f(x) - y) \quad (7.16)$$

The equation 7.16 shows that the rate of learning weights is controlled by $f(x) - y$. The larger the error is, the faster the neuron learns. In particular, the property avoids the learning slowdown because the derivative item $f'(x)$ gets cancelled out in the quadratic cost.

In similar way, the bias can be computed by the partial derivative.

$$\frac{\partial C}{\partial b} = \frac{1}{n} \sum_x (f(x) - y) \quad (7.17)$$

7.2.4 Training and Testing

Following the training process, gradient descent is used to minimise the global error function with backpropagation.

To train a sample (x_i, Y_i) , in which x_i is the input data and Y_i is the associate labels, the predicted output labels computed by the neural network for is

$$c_k = f(netc_k + \theta_k) \quad (7.18)$$

where θ_k is the bias neurons of k layer, $f()$ is the activation function for the output neurons which is the $tanh$ function 2.12 in the task. $netc_k$ is the input data of the layer:

$$netc_k = \sum_{s=1}^M b_s w_{sk} \quad (7.19)$$

where w_{sk} is the weights for the layer s and layer k , b_s is the input vector, and M is the number of neurons in the hidden layer.

As $tanh$ function is differentiable, the general error of the k -th output neuron can be defined as:

$$d_k = -\frac{\partial E}{\partial netc_k} \quad (7.20)$$

combining with equation 7.18, we can get

$$d_k = -\frac{\partial E_i}{\partial c_j} \frac{\partial c_j}{\partial netc_k} = -\frac{\partial E_i}{\partial c_j} f'(netc_k + \theta_k) \quad (7.21)$$

Considering global error function 7.4

$$\frac{\partial E_i}{\partial c_j} = \begin{cases} -\frac{1}{|Y_i||\hat{Y}_i|} \sum_{l \in \hat{Y}_i} \exp(-(c_j - c_l)) & \text{if } j \in Y_i \\ \frac{1}{|Y_i||\hat{Y}_i|} \sum_{k \in Y_i} \exp(-(c_k - c_j)) & \text{if } j \in \hat{Y}_i \end{cases} \quad (7.22)$$

with derivation of $tanh$ function, and substituting it with equations 7.21 and 7.22 we can get

$$d_k = \begin{cases} \left(-\frac{1}{|Y_i||\hat{Y}_i|} \sum_{l \in \hat{Y}_i} \exp(-(c_j - c_l)) \right) (1 + c_j)(1 - c_j) & \text{if } j \in Y_i \\ \left(\frac{1}{|Y_i||\hat{Y}_i|} \sum_{k \in Y_i} \exp(-(c_k - c_j)) \right) (1 + c_j)(1 - c_j) & \text{if } j \in \hat{Y}_i \end{cases} \quad (7.23)$$

According to the previous method, we define the general error of the s -th hidden neuron:

$$e_s = -\frac{\partial E_i}{\partial netb_s} \quad (7.24)$$

with $b_s = f(netb_s + \lambda_s)$ and chain rule,

$$e_s = -\frac{\partial E_i}{\partial b_s} \frac{\partial b_s}{\partial netb_s} = -\left(\sum_{j=1}^Q \frac{\partial E_i}{\partial netc_j} \frac{\partial netc_j}{\partial b_s}\right) f'(netb_s + \lambda_s) \quad (7.25)$$

For $d_j = -\frac{\partial E_i}{\partial netc_j}$ and $netc_j = \sum_{s=1}^M b_s w_{sj}$, then

$$e_s = \left(\sum_{j=1}^Q d_j \times \frac{\partial(\sum_{s=1}^M b_s w_{sj})}{\partial b_s}\right) f'(netb_s + \lambda_s) = \left(\sum_{j=1}^Q d_j w_{sj}\right) f'(netb_s + \lambda_s) \quad (7.26)$$

As $f()$ is \tanh function, we get

$$e_s = \left(\sum_{j=1}^Q d_j w_{sj}\right) (1 + b_s)(1 - b_s) \quad (7.27)$$

The SGD is used to approximate the function.

$$\Delta w_{sj} = -\alpha \frac{\partial E_i}{\partial w_{sj}} = \alpha \frac{\partial E_i}{\partial netc_j} \frac{\partial netc_j}{\partial w_{sj}} = \alpha d_j b_s \quad (7.28)$$

$$\Delta v_{hs} = -\alpha \frac{\partial E_i}{\partial v_{hs}} = \alpha \frac{\partial E_i}{\partial netb_s} \frac{\partial netb_s}{\partial v_{hs}} = \alpha e_s a_h \quad (7.29)$$

while the bias is updated according to

$$\Delta \theta_j = \alpha d_j \quad \Delta \lambda_s = \alpha e_s \quad (7.30)$$

In previous equations, α is the learning rate whose value is in the range of [0.0 1.0].

In the training process, a learning algorithm has been set up with backpropagation. Moreover, training samples are fed into the neural network. After all training samples (x, Y) fed into the network, weights and bias are updated through equations 7.28 and 7.30. The training samples are fed into the network iteratively while global error value decreases. Finally, the error value converges to a minimum value.

In the testing process, the network predicts a sample which has a set of actual labels

$c_j (j = 1, 2, \dots, Q)$. Because the output value of each label is in range $[-1.0, 1.0]$, a threshold function $t(x)$ is used to determine the associate label set for the sample x . A large margin ranking system [43] is adopted to generalise the sets. $t(x)$ is a linear function, $t(x) = w^T \cdot c(x) + b$, where $c(x) = (c_1(x), c_2(x), \dots, c_Q(x))$ is a Q -dimension vector which represents j output labels of the sample. For every training sample $(x_i, Y_i) (1 \leq i \leq m)$, the relation between $c(x_i)$ and target value $t(x_i)$ is:

$$t(x_i) = \arg \max_t (|\{k|k \in Y_i, c_k^i \leq t\}| + |\{l|l \in \hat{Y}_i, c_l^i \geq t\}|) \quad (7.31)$$

If there are several minimum values and optimal values are in a division, the middle value of the division is chosen. The task of learning the parameters of threshold function is to solve the matrix equation $\Phi \cdot w' = t$. The matrix Φ has dimensions $m \times (Q + 1)$ in which i -th vector is $(c_1^i, c_2^i, \dots, c_Q^i, 1)$, and w' is a $(Q + 1)$ dimensional vector (w, b) and t is the m -dimension vector $(t(x_1), t(x_2), \dots, t(x_m))$. Linear least squares is used to find the solution of the equation. Given a sample x , the network predicts the output label vector $c(x)$ and the threshold value for x is gotten by solving equation $t(x) = w^T \cdot c(x) + b$.

The computational complexity of evaluating derivatives of the error function is linear with the neuron numbers. Three main components are composed of computation, feed-forward process, backpropagation process and updating weights process. In the feed-forward process, to compute b_i and c_j , the computation cost is mainly on evaluating the sums and activation function. In the backpropagation process, the computational complexity of d_k and e_s is $O(Q)$. In the updating weights process, the overall computational complexity is $O(W)$ where W is the total number of weights .

Chapter 8

Experiment

The experiment has the identical hardware and software environment as described in the weather classification project.

8.1 Dataset

We generate 1000 raw RGB images with size 16×16 . 40 images are reserved for testing and 960 images are used for training. Each image has 3 labels $y_i \in (-1, 1)$ representing three attributes, red, green and blue. If the image has a colour attribute, the corresponding label value is 1, otherwise -1 .

8.2 Details of Network

The neural network is built from scratch up. First, we need to determine how many layers needed for the network. In [44], Lippmann has proved that two hidden layers are able to create classification regions of arbitrary desired shape. However, Kolmogorov [45] showed that the superposition of continuous one-dimension function can represent a continuous function with several variables. Then we set up a neural network with one fully connected hidden layer between the input and output layers. Between two layers, we put a ReLU layer to apply the non-saturating activation function $f(x) = \max(0, x)$ which helps the decision function increase the non-linear properties.

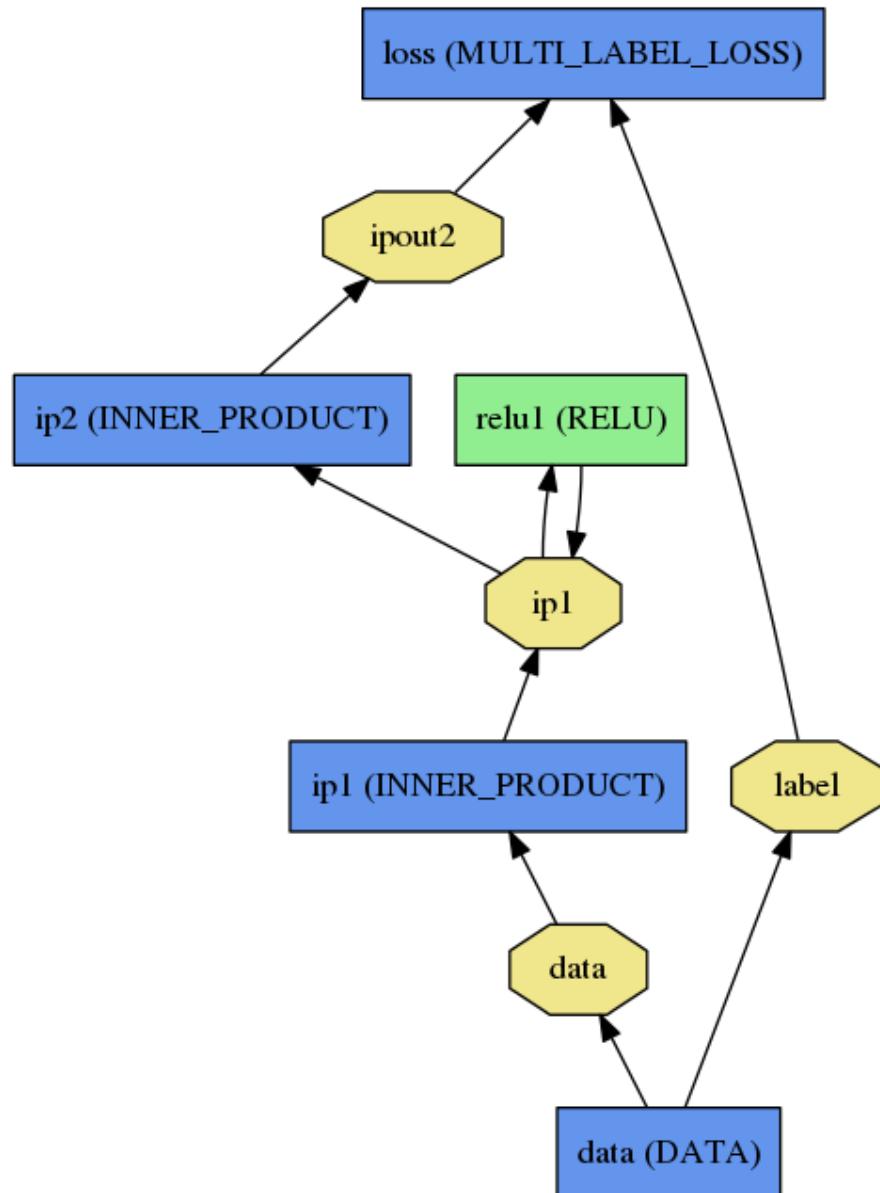


FIGURE 8.1: Network Topology

Following that, it needs to determine how many neurons needed in the hidden layer. The number of neurons in the hidden layer depends mainly on

1. Number of input and output neurons
2. Number of training samples
3. Layer connecting types
4. Training algorithms
5. Type of activation function

6. Regularisation

It is difficult to determine the best number of hidden neurons without evaluating several trained models and comparing the generalisation error rates among the models. Lacking hidden neurons will lead a high training error rate and poor generalisation performance because of underfitting and high bias. On the other hand, exceeding neurons will achieve a high training error rate and poor generalisation performance because of overfitting and high variance. One of crucial considerations is to evaluate the hidden neuron effects on the bias/variance trade-off.

There are many rules of thumb to determine the number of hidden neurons [46]

1. $\frac{2}{3}$ of the sum of the input neurons plus the output neurons.
2. Less than twice the size of the input layer.
3. Following geometric pyramid rule, between the number of input neurons and the output neurons.

It is time consuming to find the optimal number of hidden neurons. We will start from a number of neurons which is small and increase the number gradually by evaluating the performance of network.

The different layers are fully connected because we want to map each patch to the labels of the image. The information of each colour distributes in different positions of the image. The values of the weights and bias are initialised randomly. For weights, the *xavier* algorithm is applied to determine the scale of initialisation depending on the number of input and output neurons. The bias is simply initialised as a constant 0. The batch size is 40.

In the training process, the base learning rate is 0.0001. The learning rate of weights is equal to base learning rate, while the learning rate of bias is two times of the base learning rate. The parameter momentum is 0.9 to smooth the weight updating curve across iterations so that the learning process will be fast. The weight decay is 0.0005.

The evaluation metric is label-metric. Each label will be counted separately and statistics will be calculated in total.

Neuron number	Sensitivity	Specificity	Harmonic Mean	Precision	F1 Score
4	0.9245	0.9552	0.9396	0.9423	0.9333
50	0.9245	0.9701	0.9468	0.9608	0.9423
100	0.9623	0.9701	0.9662	0.9623	0.9623
150	0.9057	0.9552	0.9298	0.9412	0.9231
200	0.9811	1.0000	0.9905	1.0000	0.9905
250	0.9434	1.0000	0.9709	1.0000	0.9709
300	0.9811	0.9701	0.9756	0.9630	0.9720
350	0.9434	0.9701	0.9566	0.9615	0.9524
400	0.8868	0.9701	0.9266	0.9592	0.9216
450	0.9245	0.9701	0.9468	0.9608	0.9423
500	0.9622	0.9701	0.9662	0.9623	0.9623

TABLE 8.1: Test results for different number of hidden neurons.

8.3 Results

The test results with different number of hidden neurons are showed in table 8.1 and figure 8.2. Results show that the model with 200 neurons in the hidden layer has the best performance.

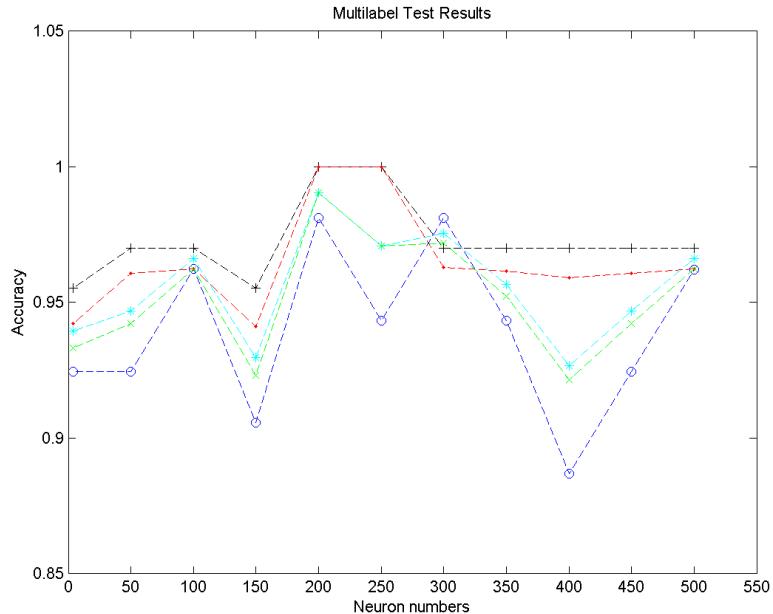


FIGURE 8.2: The test results for different number of hidden neurons. Blue circle for Sensitivity. Black plus for Specificity. Cyan star for Harmonic Mean. Red dot for Precision. Green x for F1 Score.

In figure 8.3, it shows that the learning speed is quick. After reaching high accuracy, the accuracy reverses stable.

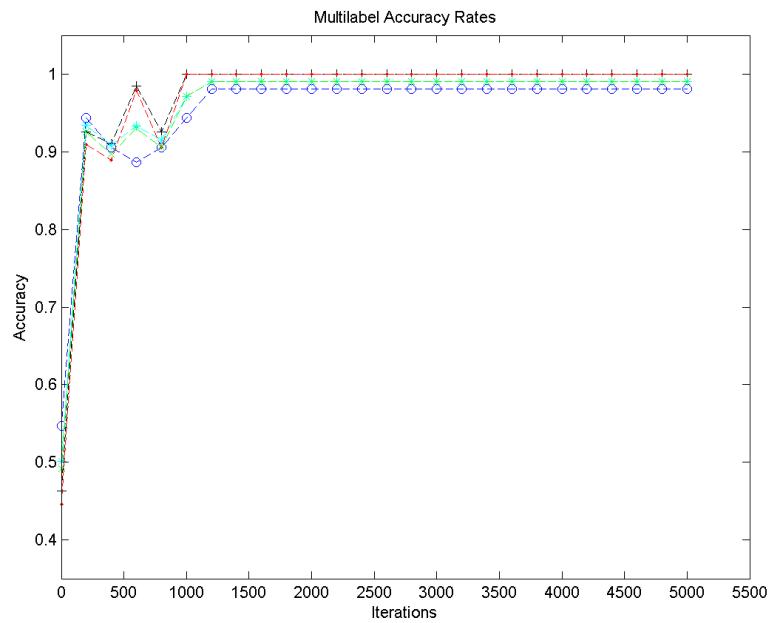


FIGURE 8.3: The learning speed for 200 neurons in the hidden layer. Blue circle for Sensitivity. Black plus for Specificity. Cyan star for Harmonic Mean. Red dot for Precision. Green x for F1 Score.

In figures 8.4 8.5, the ROC curve of test results shows that the average accuracy is high. In detail, the micro-accuracy for label 0(red) is the highest, followed by accuracies for label 1(green) and label 2(blue).

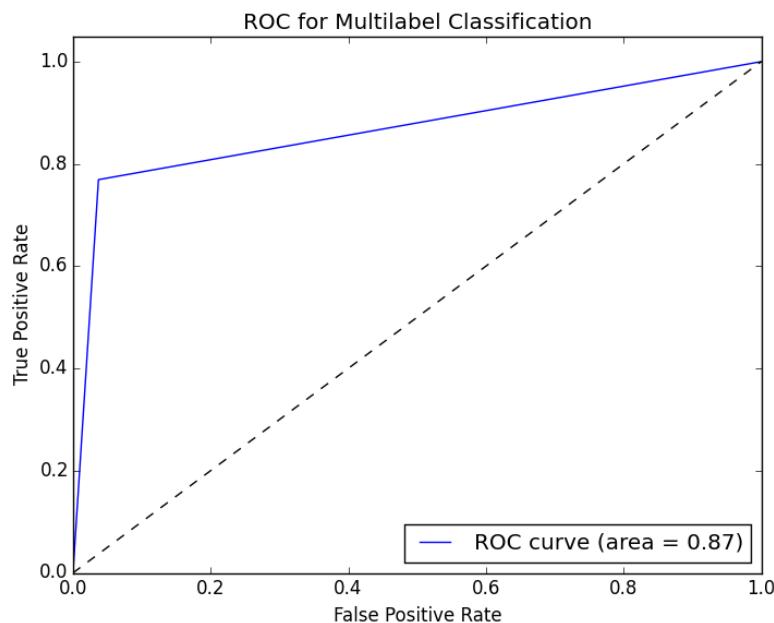


FIGURE 8.4: The ROC curve for 200 hidden neurons

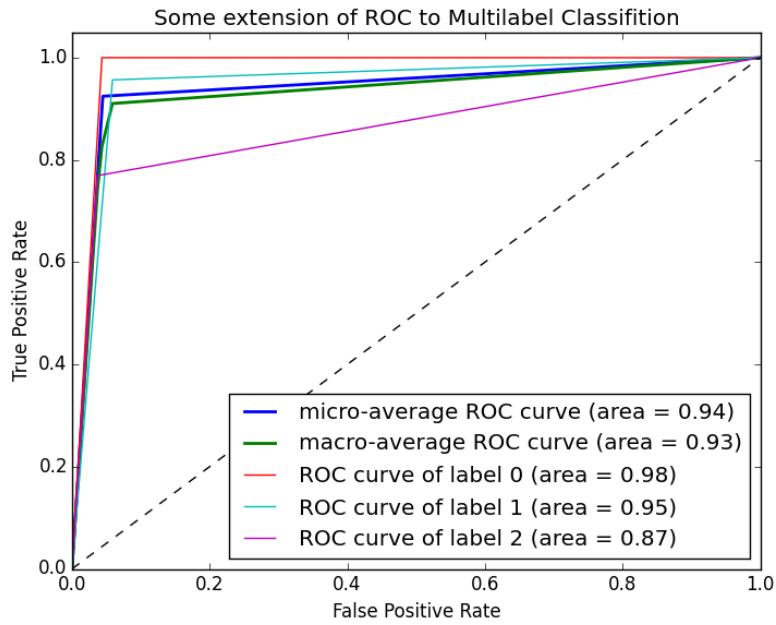


FIGURE 8.5: The ROC curve for 200 hidden neurons

8.4 Conclusion and Future Work

We have presented an effective approach to classifying multi-label images. With increasing label numbers, the correlation between data and labels is complex. A neural network maps data and labels efficiently and accurately. The updated loss function evaluates the model efficiently and quickly leads to optimisation.

The experiment shows that the neural network is able to do complex multi-label classification perfectly. In the experiment, classifying the artificial images achieves the high generalisation performance. It needs to update the network architecture for practical datasets in the future.

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