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# BMS College of Engineering, Bangalore-560019

(Autonomous Institute, Affiliated to VTU, Belgaum)

# **December 2016 Semester End Main Examinations**

Course: Engineering Mathematics -1 Duration: 3 hrs
Course Code: 15MA1ICMAT Max Marks: 100

Date: 16.12.2016

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Instructions: Answer any five full questions choosing one from each unit.

#### UNIT 1

1 a) If 
$$y = \left(x + \sqrt{x^2 - 1}\right)^m$$
, then prove that 
$$\left(x^2 - 1\right) y_{n+2} + \left(2n + 1\right) x y_{n+1} + \left(n^2 - m^2\right) y_n = 0.$$

- b) Write the Maclaurin's series for  $f(x) = \log(1 + e^x)$  up to the third degree terms.
- Obtain an expression for angle between tangent and radius vector for the polar curve  $r = f(\theta)$ .

#### **UNIT 2**

2 a) If 
$$u = e^{x} y$$
, then show that  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = \frac{1}{u} \left\{ \left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial u}{\partial y} \right)^2 \right\}$ .

- b) Expand  $f(x, y) = e^x \log(1+y)$  in powers of x and y up to third degree terms.
- c) If  $u = \frac{x+y}{1-xy}$ ,  $v = \tan^{-1} x + \tan^{-1} y$ , then show that u and v are functionally dependent.

#### OR

3 a) If 
$$\theta = t^n e^{-r^2/4t}$$
, what value of *n* will make  $\frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial \theta}{\partial r} \right) = \frac{\partial \theta}{\partial t}$ .

b) If 
$$u = f(2x-3y, 3y-4z, 4z-2x)$$
 then show that  $\frac{1}{2}\frac{\partial u}{\partial x} + \frac{1}{3}\frac{\partial u}{\partial y} + \frac{1}{4}\frac{\partial u}{\partial z} = 0$ .

c) Find the extreme values for the function  $f(x, y) = x^3 + y^3 - 3x - 12y + 20$ .

## UNIT 3

4 a) Solve the differential equation: 
$$x^3 \frac{dy}{dx} - x^2 y = -y^4 \cos x$$
.

- Show that the family of parabolas  $y^2 = 4a(x+a)$  is self-orthogonal, where a is a parameter.
- c) A body originally at  $80^{\circ}c$  cools down to  $60^{\circ}c$  in 20 minutes, the temperature of the air being  $40^{\circ}c$ . What will be the temperature of the body after 20 minutes from the original?

## **UNIT 4**

5 a) Solve:  $\frac{d^3y}{dx^3} - 7\frac{dy}{dx} - 6y = e^{2x}(1+x)$ .

- b) Apply the method of variation of parameters to solve,  $\frac{d^2y}{dx^2} + a^2y = \tan ax$ .
- c) Find the current in the RLC circuit connected in series, given  $R = 400\Omega$ , L = 0.12H, C = 0.04F,  $E = 120\sin 20t$  volts. Assume zero initial current and charge.

### OR

6 a) Solve: 
$$\frac{d^2y}{dx^2} - y = (1+x^2)e^x + x\sin x$$

- b) Solve:  $(3x-2)^2 y'' 3(3x-2)y' = 9(3x-2)\sin[\log(3x-2)]$ .
- c) A 32 *lb* weight is suspended from a coil spring stretches the spring to 2ft. The weight is then pulled down 6 inches from the equilibrium position and released at
  - t = 0. Find the motion of the weight, if the resistance of the medium is  $4\frac{dx}{dt}$ .

# UNIT 5

- 7 a) Find the area of the cardioid  $r = a(1-\cos\theta)$ .
  - b) Obtain the reduction formula for  $\int_{0}^{\pi/2} \sin^{m} x \cos^{n} x dx$  7
  - c) Obtain the series solution of Bessel's differential equation.

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