

Answer 4

To set up the linear combination with undetermined coefficients, we look at the right side of the given nonhomogeneous differential equation: $x^3 + x + e^{-2x}$

We can try three undetermined coefficients:

One for the highest degree term x^3 , we will call that constant k_1 : $k_1 x^3$

" " " x term " " " " " k_2 : $k_2 x$

" " " constant " " " " " k_3 : $k_3 e^{-2x}$

So the linear combination with undetermined coefficients is:

$$y = k_1 x^3 + k_2 x + k_3 e^{-2x}$$

* (where k_1 , k_2 and k_3 are undetermined coefficients to be found)

As a result, the linear combination of functions with undetermined literal coefficients for this equation is:

$$y = k_1 x^3 + k_2 x + k_3 e^{-2x}$$