# Overview

This assignment is focused on binary classification performance metrics. You will calculate the Accuracy, the confusion matrix, and a simple ROC curve manually on a simple example. Afterwards, you will assess the performance of multiple binary classifiers using caret to manage the resampling process and the yardstick package to calculate several performance metrics in a more realistic application. You will use Accuracy, the ROC curve, and the ROC AUC to compare multiple models and select the best one. Lastly, you will compare the models using the calibration curve.

**IMPORTANT**: The RMarkdown assumes you have downloaded the 3 data sets (CSV files) to the same directory you saved the template Rmarkdown file. If you do not have the 3 CSV files in the correct location, the data will not be loaded correctly.

#### IMPORTANT!!!

Certain code chunks are created for you. Each code chunk has eval=FALSE set in the chunk options. You MUST change it to be eval=TRUE in order for the code chunks to be evaluated when rendering the document.

You are free to add more code chunks if you would like.

# Load packages

library(tidyverse)

The tidyverse is loaded for you in the code chunk below.

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr
            1.1.2
                     v readr
                                2.1.4
## v forcats
           1.0.0
                     v stringr
                                1.5.0
## v ggplot2
            3.4.3
                     v tibble
                                3.2.1
## v lubridate 1.9.2
                     v tidyr
                                1.3.0
## v purrr
             1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                 masks stats::lag()
```

## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error

The other packages, caret and yardstick, will be loaded as needed later in the assignment.

# Problem 01

The code chunk below reads in a data set that you will work with in Problems 1, 2 and 3. A glimpse is printed for you which shows three variables, an input x, a model predicted event probability, pred\_prob, and the observed output class, obs\_class. A binary classifier has already been trained for you. That model's predicted probability (pred\_prob) is provided with the observed binary outcome (obs\_class). You will use this data set to get experience with binary classification performance metrics.

Pipe the model\_pred\_df data set into the count() function to display the number of unique values of the obs\_class variable.

```
model_pred_df %>% count(obs_class)
```

#### SOLUTION

1b)

1a)

You should see that one of the values of obs\_class is the event of interest and is named "event".

Use the mean() function to determine the fraction (or proportion) of the observations that correspond to the event of interest. Is the data set a balanced data set?

```
mean(model_pred_df$obs_class == "event")
```

### SOLUTION

## [1] 0.528

Is the data set balanced?

Yes, the data set is balanced because almost half of the observations is "event".

1c)

In lecture we discussed that regardless of the labels or classes associated with the binary response, we can encode the outcome as y = 1 if the "event" is observed and y = 0 if the "non\_event" is observed. You will encode the output with this 0/1 encoding.

The ifelse() function can help you perform this operation. The ifelse() function is a one-line if-statement which operates similar to the IF function in Excel. The basic syntax is:

```
ifelse(<conditional statement to check>, <value if TRUE>, <value if FALSE>)
```

Thus, the user must specify a condition to check as the first argument to the ifelse() function. The second argument is the value to return if the conditional statement is TRUE, and the second argument is the value to return if the conditional statement is FALSE.

You can use the ifelse() statement within a mutate() call to create a new column in the model\_pred\_df data set.

The code chunk below provides an example using the first 10 rows from the iris data set which is loaded with base R. The Sepal.Width variable is compared to a value of 3.5. If Sepal.Width is greater than 3.5 the new variable, width\_factor, is set equal to "greater than". However, if it is less than 3.5 the new variable is set to "less than".

```
Sepal.Length Sepal.Width Species width_factor
##
## 1
               5.1
                           3.5 setosa
                                           less than
## 2
               4.9
                           3.0 setosa
                                           less than
## 3
               4.7
                           3.2 setosa
                                          less than
## 4
               4.6
                                          less than
                           3.1 setosa
## 5
               5.0
                           3.6 setosa greater than
## 6
               5.4
                           3.9 setosa greater than
## 7
               4.6
                           3.4 setosa
                                           less than
## 8
               5.0
                           3.4 setosa
                                          less than
## 9
               4.4
                           2.9 setosa
                                          less than
               4.9
                           3.1 setosa
                                          less than
## 10
```

You will use the ifelse() function combined with mutate() to add a column to the model\_pred\_df tibble.

Pipe model\_pred\_df into a mutate() call in order to create a new column (variable) named y. The new variable, y, will equal the result of the ifelse() function. The conditional statement will be if obs\_class is equal to the "event". If TRUE assign y to equal the value 1. If FALSE, assign y to equal the value 0. Assign the result to the variable model\_pred\_df which overwrites the existing value.

```
model_pred_df <- model_pred_df %>%
  mutate(y = ifelse(obs_class == "event", 1, 0))
```

# SOLUTION

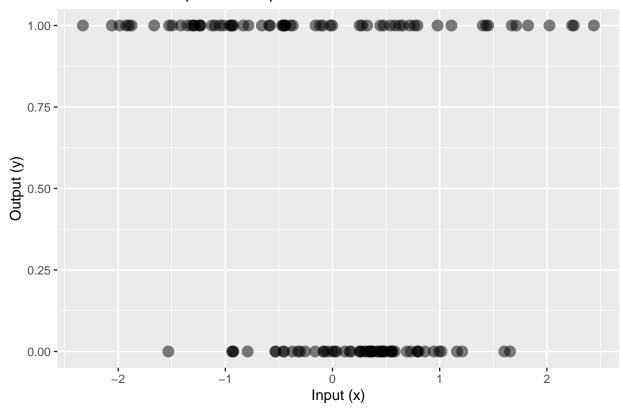
1d)

You will now visualize the observed binary outcome as encoded by 0 and 1.

Pipe the model\_pred\_df object into ggplot(). Create a scatter plot between the encoded output y and the input x. Set the marker size to be 3.5 and the transparency (alpha) to be 0.5.

```
scatter_plot <- model_pred_df %>%
  ggplot(aes(x = x, y = y)) +
  geom_point(size = 3.5, alpha = 0.5) +
  labs(x = "Input (x)", y = "Output (y)", title = "Scatter Plot of Input vs. Output")
print(scatter_plot)
```





### SOLUTION

#### 1e)

The model\_pred\_df includes a column (variable) for a model predicted event probability.

Use the summary() function to confirm that the lower an upper bounds on pred\_prob are in fact between 0 and 1.

```
summary(model_pred_df$pred_prob)
```

#### **SOLUTION**

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.2227 0.2323 0.3218 0.4547 0.6859 0.9988
```

### 1f)

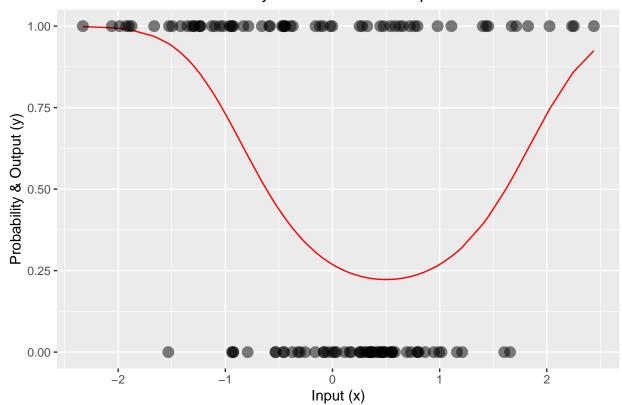
With the binary outcome encoded as 0/1 within the y variable we can overlay the model predicted probability on top of the observed binary response.

Use a geom\_line() to plot the predicted event probability, pred\_prob, with respect to the input x. Set the line color to be "red" within the geom\_line() call. Overlay the binary response with the encoded response y as a scatter plot with geom\_point(). Use the same marker size and transparency that you used for Problem 1d).

```
scatter_prob_plot <- model_pred_df %>%
ggplot(aes(x = x)) +
geom_line(aes(y = pred_prob), color = "red") +
```

```
geom_point(aes(y = y), size = 3.5, alpha = 0.5) +
labs(x = "Input (x)", y = "Probability & Output (y)", title = "Plot of Predicted Probability and Obserprint(scatter_prob_plot)
```

# Plot of Predicted Probability and Observed Response



#### **SOLUTION**

**1g**)

Does the observed binary response "follow" the model predicted probability?

### **SOLUTION** What do you think?

Yes, the observed binary response "follow" the model predicted probability. When the predicted probability is greater that 0.5, "event" observations are more than "non-event" observations. Similarly, when the predicted probability is less that 0.5, "non-event" observations are more than "event" observations.

### Problem 02

As you can see from the model\_pred\_df tibble, we have a model predicted probability but we do not have a corresponding classification.

# 2a)

In order to classify our predictions we must compare the predicted probability against a threshold. You will use ifelse() combined with mutate() to create a new variable pred\_class. If the predicted probability, pred\_prob, is greater than the threshold set the predicted class equal to "event". If the predicted probability, pred\_prob, is less than the threshold set the predicted class equal to the "non\_event".

Use a threshold value of 0.5 and create the new variable pred\_class such that the classification is "event" if the predicted probability is greater than the threshold and "non\_event"

if the predicted probability is less than the threshold. Assign the result to the new object model\_class\_0.5.

```
model_class_0.5 <- model_pred_df %>%
  mutate(pred_class = ifelse(pred_prob > 0.5, "event", "non_event"))
```

#### **SOLUTION**

**2**b)

You should now have a tibble that has a model classification and the observed binary outcome.

Calculate the Accuracy, the fraction of observations where the model classification is correct.

```
sum(model_class_0.5$pred_class == model_class_0.5$obs_class)/nrow(model_class_0.5)
```

### SOLUTION

## [1] 0.704

2c)

We discussed in lecture how there are additional metrics we can consider with binary classification. Specifically, we can consider how a classification is correct, and how a classification is incorrect. A simple way to determine the counts per combination of pred\_class and obs\_class is with the count() function.

Pipe model\_class\_0.5 into count() with pred\_class as the first argument and obs\_class as the second argument. You should see 4 combinations and the number of rows in the data set associated with each combination (the number or count is given by the n variable).

How many observations are associated with False-Positives? How many observations are associated with True-Negatives?

```
combinations <- model_class_0.5 %>%
  count(pred_class, obs_class)
print(combinations)
```

#### **SOLUTION**

```
## # A tibble: 4 x 3
##
    pred_class obs_class
                               n
##
     <chr>>
                <chr>
                           <int>
## 1 event
                event
                              35
## 2 event
                non event
                               6
## 3 non_event event
                              31
## 4 non_event non_event
                              53
```

your response here.

6 observations are associated with False-Positives and 53 observations are associated with True-Negatives.

2d)

You will now calculate the Sensitivity and False Positive Rate (FPR) associated with the model predicted classifications based on a threshold of 0.5. This question is left open ended. It is your choice as to how you calculate the Sensitivity and FPR. However, you CANNOT use an

existing function from a library which performs the calculations automatically for you. You are permitted to use dplyr data manipulation functions. Include as many code chunks as you feel are necessary.

```
TP_05 <- sum(model_class_0.5$pred_class == "event" & model_class_0.5$obs_class == "event")
FN_05 <- sum(model_class_0.5$pred_class == "non_event" & model_class_0.5$obs_class == "event")
TN_05 <- sum(model_class_0.5$pred_class == "non_event" & model_class_0.5$obs_class == "non_event")
FP_05 <- sum(model_class_0.5$pred_class == "event" & model_class_0.5$obs_class == "non_event")
Sensitivity_05 <- TP_05/(TP_05+FN_05)
FPR_05 <- 1-(TN_05/(FP_05+TN_05))</pre>

print(Sensitivity_05)
```

#### SOLUTION

```
## [1] 0.530303
print(FPR_05)
```

## [1] 0.1016949

**2e**)

We also discussed the ROC curve in addition to the confusion matrix. You will not have to calculate the ROC curve for a large number of threshold values. You will go through several calculations in order to demonstrate an understanding of the steps necessary to create an ROC curve.

The first action you must perform is to make classifications based on a different threshold compared to the default value of 0.5, which we used previously.

Pipe the model\_pred\_df tibble into a mutate() function again, but this time determine the classifications based on a threshold value of 0.7 instead of 0.5. Assign the result to the object model\_class\_0.7.

```
model_class_0.7 <- model_pred_df %>%
  mutate(pred_class = ifelse(pred_prob > 0.7, "event", "non_event"))
```

#### SOLUTION

2f)

Perform the same action as in Problem 2e), but this time for a threshold value of 0.3. Assign the result to the object model\_class\_0.3.

```
model_class_0.3 <- model_pred_df %>%
  mutate(pred_class = ifelse(pred_prob > 0.3, "event", "non_event"))
```

### **SOLUTION**

### Problem 3

You will continue with the binary classification application in this problem.

3a)

3c)

Calculate the Accuracy of the model classifications based on the 0.7 threshold. You CANNOT use an existing function that calculates Accuracy automatically for you. You are permitted to use dplyr data manipulation functions.

```
sum(model_class_0.7$pred_class == model_class_0.7$obs_class)/nrow(model_class_0.7)

SOLUTION
## [1] 0.672
3b)
```

Calculate the Sensitivity and Specificity of the model classifications based on the 0.7 threshold. Again you can calculate these however you wish. Except you cannot use a model function library that performs the calculations automatically for you.

Calculate the Accuracy of the model classifications based on the 0.3 threshold.

```
sum(model_class_0.3$pred_class == model_class_0.3$obs_class)/nrow(model_class_0.3)

SOLUTION
## [1] 0.712
3d)
```

Calculate the Sensitivity and Specificity of the model classifications based on the 0.3 threshold. Again you can calculate these however you wish. Except you cannot use a model function library that performs the calculations automatically for you.

```
TP_03 <- sum(model_class_0.3$pred_class == "event" & model_class_0.3$obs_class == "event")
FN_03 <- sum(model_class_0.3$pred_class == "non_event" & model_class_0.3$obs_class == "event")
TN_03 <- sum(model_class_0.3$pred_class == "non_event" & model_class_0.3$obs_class == "non_event")
FP_03 <- sum(model_class_0.3$pred_class == "event" & model_class_0.3$obs_class == "non_event")
Sensitivity_03 <- TP_03/(TP_03+FN_03)

FPR_03 <- 1-(TN_03/(FP_03+TN_03))

**FPR_03 <- 1-(TN_03/(FP_03+TN_03))</pre>

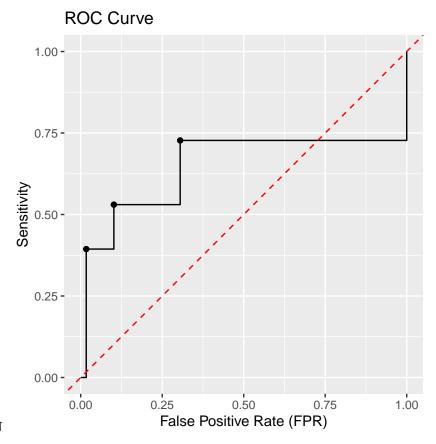
**FIR_03 <- 1-(TN_03/(FP_03+TN_03))

**FIR_03 <- TN_03/(FP_03+TN_03)

**FIR_03 <- TN_03/
```

You have calculated the Sensitivity and FPR at three different threshold values. You will plot your simple 3 point ROC curve and include a "45-degree" line as reference.

Use ggplot2 to plot your simple 3 point ROC curve. You must compile the necessary values into a data.frame or tibble. You must use geom\_point() to show the markers, geom\_abline() with slope=1 and intercept=0 to show the reference "45-degree" line. And you must use coord\_equal(xlim=c(0,1), ylim=c(0,1)) with your graphic. This way both axes are plotted between 0 and 1 and the axes are equal.



### **SOLUTION**

# Problem 04

You have practiced calculating several important binary classification performance metrics. Let's use those metrics in a more realistic application to compare multiple models. The code chunk below reads in data that you will use for model training. The data consists of 4 inputs, x1 through x4, and a binary outcome, y. The binary outcome is converted to a factor for you with the appropriate level order for modeling with caret.

```
train_data_path <- 'hw03_train_data.csv'

df <- readr::read_csv(train_data_path, col_names = TRUE)

## Rows: 155 Columns: 5

## -- Column specification ------

## Delimiter: ","

## chr (1): y

## dbl (4): x1, x2, x3, x4

##

## i Use `spec()` to retrieve the full column specification for this data.

## i Specify the column types or set `show_col_types = FALSE` to quiet this message.

df <- df %>%

mutate(y = factor(y, levels = c("event", "non_event")))
```

A glimpse of the data are provided to you below.

```
df %>% glimpse()
## Rows: 155
## Columns: 5
```

```
## $ x1 <dbl> -0.3260365, 0.5524619, -0.6749438, 0.2143595, 0.3107692, 1.1739663,~
## $ x2 <dbl> -2.823000119, 0.462973827, 2.132869726, -0.270486687, 0.248525349, ~
## $ x3 <dbl> 0.23917695, -0.50232861, -1.70387658, 0.52377224, 1.56417215, -2.46~
## $ x4 <dbl> -1.14362001, -0.30082496, -1.38891427, -2.02747975, 0.50521591, 0.7~
## $ y <fct> event, event, event, non_event, event, non_event, event, non_event,~
```

Are the levels of the binary outcome, y, balanced?

**SOLUTION** Add as many code chunks as you feel are necessary.

```
mean(df$y == "event")
## [1] 0.483871
```

Yes, the levels are balanced because almost half of the observations is "event".

4b)

Although it is best to explore the data in greater detail when we start a data analysis project, we will jump straight to modeling in this assignment.

Download and install yardstick if you have not done so already.

Load in the caret package and the yardstick packages below. Use a separate code chunk for each package.

**SOLUTION** Add the code chunks here.

```
library(caret)
## Loading required package: lattice
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
##
       lift
library(yardstick)
##
## Attaching package: 'yardstick'
## The following objects are masked from 'package:caret':
##
##
       precision, recall, sensitivity, specificity
## The following object is masked from 'package:readr':
##
##
       spec
4c)
```

Just as with regression problems, we must first specify the resampling scheme and primary performance metric when we use caret for classification problems. All students will use the same primary performance metric in this assignment. We will begin by focusing on the Accuracy. That said, you are free to decide the kind of resampling scheme you wish to use.

The resampling scheme is controlled by the trainControl() function, just as it was with regression problems. You must specify the arguments to the trainControl() function accordingly in this problem.

Specify the resampling scheme you wish to use and assign the result to the ctrl\_acc object. Specify the primary performance metric to be Accuracy by assigning 'Accuracy' to the metric\_acc argument.

```
ctrl_acc <- trainControl(method = "cv", number = 5)
metric_acc <- "Accuracy"</pre>
```

#### 4d)

You are going to train 8 binary classifiers in this problem. The different models will use different features derived from the 4 inputs. The 8 models must have the following features:

- model 1: linear additive features all inputs
- model 2: linear features and quadratic features all inputs
- model 3: linear features and quadratic features just inputs 1 and 2
- model 4: linear features and quadratic features just inputs 1 and 3
- model 5: linear features and quadratic features just inputs 1 and 4
- model 6: linear features and quadratic features just inputs 2 and 3
- model 7: linear features and quadratic features just inputs 2 and 4
- model 8: linear features and quadratic features just inputs 3 and 4

Model 1 is the conventional "linear method" for binary classification. All other models have linear and quadratic terms to allow capturing non-linear relationships with the event probability (just how that works will be discussed later in the semester). Model 2 creates the features from all four inputs. The remaining 6 models use the combinations of just two of the inputs. This scheme is trying to identify the best possible set of inputs to model the binary outcome in a step-wise like fashion. This is **not** an efficient way to identify the best set of features to use. Later in the semester, we will learn a much more efficient modeling approach that performs this operation for us!

You must complete the 8 code chunks below. Use the formula interface to create the features in the model, analogous to the approach used in the previous assignment. You must specify the method argument in the train() function to be "glm". You must specify the remaining arguments to train() accordingly.

The variable names and comments within the code chunks specify which model you are working with.

NOTE: The models are trained in separate code chunks that way you can run each model separately from the others.

```
metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
mod_1_acc
SOLUTION
## Generalized Linear Model
##
## 155 samples
##
     4 predictor
     2 classes: 'event', 'non_event'
##
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     Accuracy
                Kappa
##
     0.7483871 0.4960866
### model 2
set.seed(2021)
mod_2 = acc \leftarrow train(y \sim x1 + x2 + x3 + x4 + I(x1^2) + I(x2^2) + I(x3^2) + I(x4^2),
                        data = df,
                        method = "glm",
                        metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
mod_2_{acc}
## Generalized Linear Model
##
## 155 samples
##
    4 predictor
##
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (8), scaled (8)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     Accuracy
                Kappa
     0.7870968 0.5729577
### model 3
set.seed(2021)
mod_3_acc \leftarrow train(y \sim x1 + x2 + I(x1^2) + I(x2^2),
                        data = df,
                        method = "glm",
                        metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
```

## Generalized Linear Model

mod\_3\_acc

```
##
## 155 samples
    2 predictor
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     Accuracy Kappa
##
     0.8
               0.5979811
### model 4
set.seed(2021)
mod_4_acc \leftarrow train(y \sim x1 + x3 + I(x1^2) + I(x3^2),
                        data = df,
                        method = "glm",
                        metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
mod_4_acc
## Generalized Linear Model
##
## 155 samples
     2 predictor
##
##
    2 classes: 'event', 'non_event'
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     Accuracy Kappa
##
     0.6
               0.2045638
### model 5
set.seed(2021)
mod_5_acc \leftarrow train(y \sim x1 + x4 + I(x1^2) + I(x4^2),
                        data = df,
                        method = "glm",
                        metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
mod_5_acc
## Generalized Linear Model
##
## 155 samples
    2 predictor
##
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
```

```
## Resampling results:
##
##
     Accuracy Kappa
               0.2003237
##
     0.6
### model 6
set.seed(2021)
mod_6_acc \leftarrow train(y \sim x2 + x3 + I(x2^2) + I(x3^2),
                        data = df,
                        method = "glm",
                        metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
mod_6_acc
## Generalized Linear Model
##
## 155 samples
    2 predictor
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     Accuracy
               Kappa
     0.7806452 0.5592538
##
### model 7
set.seed(2021)
mod_7_acc \leftarrow train(y \sim x2 + x4 + I(x2^2) + I(x4^2),
                        data = df,
                        method = "glm",
                        metric = metric_acc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_acc)
mod_7_acc
## Generalized Linear Model
## 155 samples
##
    2 predictor
##
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
     Accuracy
                Kappa
     0.7806452 0.5585457
### model 8
set.seed(2021)
mod_8_acc \leftarrow train(y \sim x3 + x4 + I(x3^2) + I(x4^2),
```

```
data = df,
    method = "glm",
    metric = metric_acc,
    preProcess = c("center", "scale"),
    trControl = ctrl_acc)
mod_8_acc
```

```
## Generalized Linear Model
##
## 155 samples
##
    2 predictor
     2 classes: 'event', 'non_event'
##
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     Accuracy
                Kappa
     0.5612903 0.1140718
##
4e)
```

You will now compile all resample results together and compare the models based on their Accuracy.

Complete the first code chunk below which assigns the models to the appropriate field within the resamples() function.

Then use the summary() function to summarize the Accuracy across the resamples and visualize the resample averaged performance with the dotplot() function from caret. In the function calls to both summary() and dotplot(), set the metric argument equal to 'Accuracy'.

Which model is the best based on Accuracy? Are you confident it's the best?

HINT: The field names within the list contained in the resamples() call correspond to the model object you should use.

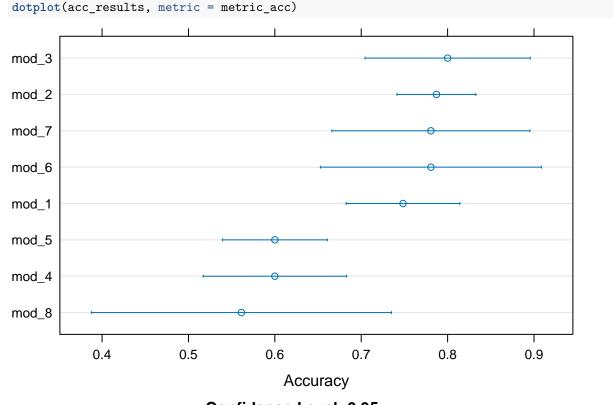
**SOLUTION** Summarize the results across the resamples.

```
summary(acc_results, metric = metric_acc)
##
```

```
## Call:
## summary.resamples(object = acc_results, metric = metric_acc)
##
## Models: mod_1, mod_2, mod_3, mod_4, mod_5, mod_6, mod_7, mod_8
## Number of resamples: 5
```

```
##
## Accuracy
##
                     1st Qu.
                                Median
## mod_1 0.6774194 0.7096774 0.7741935 0.7483871 0.7741935 0.8064516
## mod 2 0.7419355 0.7741935 0.7741935 0.7870968 0.8064516 0.8387097
                                                                         0
## mod 3 0.7096774 0.7419355 0.8064516 0.8000000 0.8387097 0.9032258
                                                                         0
## mod 4 0.5483871 0.5483871 0.5806452 0.6000000 0.6129032 0.7096774
## mod 5 0.5483871 0.5806452 0.5806452 0.6000000 0.6129032 0.6774194
                                                                         0
## mod 6 0.6451613 0.7096774 0.8064516 0.7806452 0.8387097 0.9032258
                                                                         0
## mod_7 0.6774194 0.7096774 0.7741935 0.7806452 0.8387097 0.9032258
                                                                         0
## mod_8 0.3870968 0.5161290 0.5483871 0.5612903 0.5806452 0.7741935
                                                                         0
```

Visualize the resample averaged Accuracy per model.



Confidence Level: 0.95

Which model is the best?

Based on the Accuracy values, mod\_3 has the highest accuaracy of 0.8000000, making it the best-performing model.

4f)

Next, you will consider how a model was correct and how a model was wrong via the confusion matrix. You are allowed to use the <code>confusionMatrix()</code> function from the <code>caret</code> package in this assignment to create the confusion matrix. A <code>caret</code> model object can be passed as the argument to the <code>confusionMatrix()</code> function. The function will then calculate the average confusion matrix across all resample test-sets. The resulting confusion matrix is displayed with percentages instead of counts, as shown in the lecture slides. The interpretations however are the same.

Use the confusionMatrix() function to display the confusion matrix for the top two and worst

two models according to Accuracy.

How do the False-Positive and False-Negative behavior compare between these four models?

**SOLUTION** Add as many code chunks as you feel are necessary.

```
confusionMatrix(mod_3_acc)
## Cross-Validated (5 fold) Confusion Matrix
##
## (entries are percentual average cell counts across resamples)
##
##
              Reference
## Prediction event non_event
##
    event
                36.1
                           7.7
    non_event 12.3
                          43.9
##
##
   Accuracy (average): 0.8
confusionMatrix(mod_2_acc)
## Cross-Validated (5 fold) Confusion Matrix
##
## (entries are percentual average cell counts across resamples)
##
##
              Reference
## Prediction event non_event
                36.8
##
                           9.7
     event
    non_event 11.6
                          41.9
##
##
  Accuracy (average): 0.7871
confusionMatrix(mod_4_acc)
## Cross-Validated (5 fold) Confusion Matrix
##
## (entries are percentual average cell counts across resamples)
##
##
              Reference
## Prediction event non_event
##
     event
                33.5
                          25.2
##
    non_event 14.8
                          26.5
##
  Accuracy (average): 0.6
confusionMatrix(mod_8_acc)
## Cross-Validated (5 fold) Confusion Matrix
##
## (entries are percentual average cell counts across resamples)
##
##
              Reference
## Prediction event non_event
##
     event
                20.6
                          16.1
    non event 27.7
                          35.5
##
##
## Accuracy (average): 0.5613
```

The formulas for False Positive Rate (FPR) and False Negative Rate (FNR) are as follows:

```
FPR = FP / (FP + TN) FNR = FN / (FN + TP)
```

By utilizing these formulas with the values from confusion matrices, we can observe that both FPR and FNR exhibit an increasing trend, from the best-performing model to the worst-performing model among the four models.

# Problem 05

Now that you have compared the models based on Accuracy, it is time to consider another performance metric. The Accuracy is calculated using a single threshold value. You will now examine the model performance across all possible thresholds by studying the ROC curve.

5a)

You will ultimately visually compare the ROC curves for the different models. Unfortunately with caret, we need to make several changes to the trainControl() function in order to support such comparisons. The code chunk below is started for you by including the necessary arguments you will need to visualize the ROC curves later.

You must complete the code chunk by specifying the same resampling scheme you used in Problem 4c). You must also specify the primary performance metric as 'ROC'. That is how caret knows it must calculate the Area Under the Curve (AUC) for the ROC curve.

# SOLUTION

# 5b)

You will retrain the same set of 8 models that you trained in Problem 4d), but this time using the ROC AUC as the primary performance metric.

Complete the code chunks below so that you train the 8 models again, but this time focusing on the ROC AUC. The object name and comments within the code chunks specify the model you should use.

# SOLUTION

```
## Generalized Linear Model
##
## 155 samples
    4 predictor
##
    2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     ROC
             Sens
                         Spec
     0.8025 0.7466667 0.75
##
### model 2
set.seed(2021)
mod_2 = roc \leftarrow train(y \sim x1 + x2 + x3 + x4 + I(x1^2) + I(x2^2) + I(x3^2) + I(x4^2),
                        data = df,
                        method = "glm",
                       metric = metric_roc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_roc)
mod_2_roc
## Generalized Linear Model
## 155 samples
##
    4 predictor
##
     2 classes: 'event', 'non event'
##
## Pre-processing: centered (8), scaled (8)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     ROC
                Sens Spec
##
    0.9066667 0.76 0.8125
### model 3
set.seed(2021)
mod_3 roc \leftarrow train(y \sim x1 + x2 + I(x1^2) + I(x2^2),
                        data = df,
                        method = "glm",
                       metric = metric_roc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_roc)
mod_3_roc
## Generalized Linear Model
## 155 samples
     2 predictor
##
     2 classes: 'event', 'non_event'
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
```

```
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     ROC
                      Spec
           Sens
##
     0.92 0.7466667 0.85
### model 4
set.seed(2021)
mod_4_{roc} \leftarrow train(y \sim x1 + x3 + I(x1^2) + I(x3^2),
                       data = df,
                       method = "glm",
                       metric = metric_roc,
                       preProcess = c("center", "scale"),
                       trControl = ctrl_roc)
mod_4_roc
## Generalized Linear Model
## 155 samples
##
    2 predictor
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
    ROC
                Sens
                           Spec
     ##
### model 5
set.seed(2021)
mod_5 roc \leftarrow train(y \sim x1 + x4 + I(x1^2) + I(x4^2),
                       data = df,
                       method = "glm",
                       metric = metric_roc,
                       preProcess = c("center", "scale"),
                       trControl = ctrl_roc)
mod_5_roc
## Generalized Linear Model
##
## 155 samples
     2 predictor
     2 classes: 'event', 'non_event'
##
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
                Sens
                           Spec
##
     0.6341667 0.6133333 0.5875
### model 6
set.seed(2021)
```

```
mod_6 roc \leftarrow train(y \sim x2 + x3 + I(x2^2) + I(x3^2),
                        data = df,
                        method = "glm",
                        metric = metric_roc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_roc)
mod_6_roc
## Generalized Linear Model
## 155 samples
##
    2 predictor
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     ROC
                 Sens
                            Spec
##
     0.8458333 0.7333333 0.825
### model 7
set.seed(2021)
mod_7 roc \leftarrow train(y \sim x2 + x4 + I(x2^2) + I(x4^2),
                        data = df,
                        method = "glm",
                        metric = metric_roc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_roc)
mod_7_roc
## Generalized Linear Model
##
## 155 samples
     2 predictor
     2 classes: 'event', 'non_event'
##
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
##
     ROC
             Sens
                         Spec
     0.8475 0.7066667 0.85
### model 8
set.seed(2021)
mod_8 roc \leftarrow train(y \sim x3 + x4 + I(x3^2) + I(x4^2),
                        data = df,
                        method = "glm",
                        metric = metric_roc,
                        preProcess = c("center", "scale"),
                        trControl = ctrl_roc)
mod_8_roc
```

```
## Generalized Linear Model
##
## 155 samples
     2 predictor
##
##
     2 classes: 'event', 'non_event'
##
## Pre-processing: centered (4), scaled (4)
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 124, 124, 124, 124, 124
## Resampling results:
##
     ROC
##
           Sens
                       Spec
                      0.6875
##
     0.52 0.4266667
5c)
```

You will now compile all resample results together and compare the models based on their area under the ROC curve.

Complete the first code chunk below which assigns the models to the appropriate field within the resamples() function.

Then use the summary() function to summarize the ROC AUC across the resamples and visualize the resample averaged performance with the dotplot() function from caret. In the function calls to both summary() and dotplot(), set the metric argument equal to 'ROC'.

Which model is the best based on ROC AUC? Are you confident it's the best?

HINT: The field names within the list contained in the resamples() call correspond to the model object you should use.

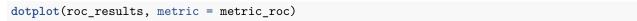
**SOLUTION** Summarize the results across the resamples.

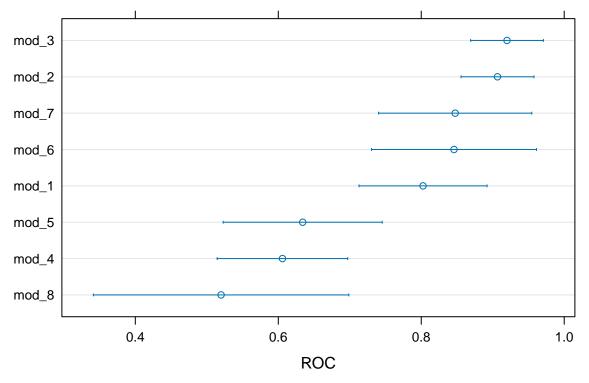
```
summary(roc_results, metric = metric_roc)
```

```
##
## Call:
## summary.resamples(object = roc_results, metric = metric_roc)
##
## Models: mod_1, mod_2, mod_3, mod_4, mod_5, mod_6, mod_7, mod_8
## Number of resamples: 5
##
## ROC
              Min.
                     1st Qu.
                                Median
                                             Mean
                                                    3rd Qu.
                                                                 Max. NA's
## mod_1 0.6916667 0.7958333 0.8083333 0.8025000 0.8250000 0.8916667
                                                                          0
## mod_2 0.8625000 0.8750000 0.9083333 0.9066667 0.9208333 0.9666667
                                                                          0
## mod_3 0.8541667 0.9083333 0.9375000 0.9200000 0.9416667 0.9583333
                                                                          0
```

```
## mod_4 0.5500000 0.5583333 0.5750000 0.6058333 0.6166667 0.7291667 0  
## mod_5 0.5166667 0.5750000 0.6416667 0.6341667 0.7041667 0.7333333 0  
## mod_6 0.7166667 0.7833333 0.8791667 0.8458333 0.9125000 0.9375000 0  
## mod_7 0.7083333 0.8291667 0.8666667 0.8475000 0.9083333 0.9250000 0  
## mod_8 0.3875000 0.4333333 0.4750000 0.5200000 0.5500000 0.7541667 0
```

Visualize the resample averaged ROC AUC per model.





Confidence Level: 0.95

Which model is the best?

Based on the ROC AUC values, mod\_3 has the highest mean area under the ROC curve with value of 0.9200000, making it the best-performing model.

**5d**)

By default, two other metrics are calculated by caret when we use the ROC AUC as the primary performance metric. Unlike ROC AUC, these two metrics are calculated with the default threshold. caret labels the the Sensitivity as the Sens metric and the Specificity as the Spec metric.

Use the summary() and dotplot() functions again, but do not specify a metric. Just provide the roc\_results as the input argument to the functions.

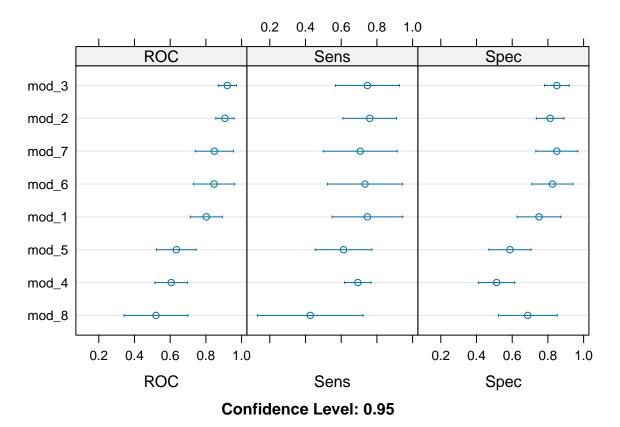
Which model has the highest True-Positive Rate at the default threshold? Which model has the lowest False-Positive Rate at the default threshold?

**SOLUTION** Add as many code chunks and as much text as you feel are necessary.

```
summary(roc_results)
```

##

```
## Call:
## summary.resamples(object = roc_results)
## Models: mod_1, mod_2, mod_3, mod_4, mod_5, mod_6, mod_7, mod_8
## Number of resamples: 5
##
## ROC
##
             Min.
                    1st Qu.
                               Median
                                           Mean
                                                  3rd Qu.
## mod 1 0.6916667 0.7958333 0.8083333 0.8025000 0.8250000 0.8916667
## mod_2 0.8625000 0.8750000 0.9083333 0.9066667 0.9208333 0.9666667
## mod_3 0.8541667 0.9083333 0.9375000 0.9200000 0.9416667 0.9583333
## mod_4 0.5500000 0.5583333 0.5750000 0.6058333 0.6166667 0.7291667
## mod_5 0.5166667 0.5750000 0.6416667 0.6341667 0.7041667 0.7333333
## mod_6 0.7166667 0.7833333 0.8791667 0.8458333 0.9125000 0.9375000
## mod_7 0.7083333 0.8291667 0.8666667 0.8475000 0.9083333 0.9250000
## mod_8 0.3875000 0.4333333 0.4750000 0.5200000 0.5500000 0.7541667
##
## Sens
##
                    1st Qu.
                               Median
                                                  3rd Qu.
             Min.
                                           Mean
## mod 1 0.4666667 0.8000000 0.8000000 0.7466667 0.8000000 0.8666667
## mod_2 0.6000000 0.7333333 0.7333333 0.7600000 0.8000000 0.9333333
## mod 3 0.5333333 0.7333333 0.7333333 0.7466667 0.8000000 0.9333333
## mod_4 0.6666667 0.6666667 0.6666667 0.6933333 0.6666667 0.8000000
## mod 5 0.4666667 0.5333333 0.6000000 0.6133333 0.6666667 0.8000000
## mod 6 0.4666667 0.7333333 0.7333333 0.8000000 0.9333333
## mod 7 0.4666667 0.6666667 0.7333333 0.7066667 0.7333333 0.9333333
## mod_8 0.1333333 0.3333333 0.4266667 0.6000000 0.7333333
##
## Spec
##
          Min. 1st Qu. Median
                                Mean 3rd Qu.
                                               Max. NA's
## mod_1 0.6250 0.6875 0.7500 0.7500 0.8125 0.8750
## mod_2 0.7500 0.7500 0.8125 0.8125 0.8750 0.8750
                                                       0
## mod_3 0.7500 0.8750 0.8750 0.8500 0.8750 0.8750
## mod_4 0.4375 0.4375 0.5000 0.5125 0.5625 0.6250
## mod 5 0.5000 0.5625 0.5625 0.5875 0.5625 0.7500
## mod_6 0.6875 0.8125 0.8125 0.8250 0.8750 0.9375
## mod 7 0.6875 0.8750 0.8750 0.8500 0.8750 0.9375
## mod_8 0.5000 0.6250 0.6875 0.6875 0.8125 0.8125
dotplot(roc_results)
```



 $\operatorname{mod}_{2}$  has the highest TPR with mean 0.7600000.

 $mod_3$  has the lowest FPR with mean 1-0.8500=0.1500.

### **5e**)

In order to visualize the ROC curve we need to understand how the resample hold-out test predictions are stored within the caret model objects. By default, hold-out test set predictions are not retained, in order to conserve memory. However, the ctrl\_roc object set savePredictions = TRUE which overrides the default behavior and stores each resample test-set predictions.

The predictions are contained with the \$pred field of the caret model object. The code chunk below displays the first few rows of the predictions for the mod\_1\_roc result for you. Note that the code chunk below is not evaluated by default. When you execute the code chunk below, you will see 7 columns. The column obs is the observed outcome and the column event is the predicted probability of the event. The pred column is the model classified outcome based on the default threshold of 50%. The rowIndex is the row from the original data set and serves to identify the row correctly. The Resample column tells us which resample fold the test point was associated with.

# mod\_1\_roc\$pred %>% tibble::as\_tibble()

```
# A tibble: 155 x 7
##
      pred
##
                 obs
                            event non_event rowIndex parameter Resample
##
      <fct>
                 <fct>
                            <dbl>
                                       <dbl>
                                                <int> <chr>
                                                                 <chr>
                                      0.751
                                                    8 none
                                                                 Fold1
##
    1 non_event non_event 0.249
##
    2 non_event non_event 0.175
                                      0.825
                                                   12 none
                                                                 Fold1
                                      0.869
                                                   13 none
                                                                 Fold1
##
    3 non_event non_event 0.131
##
    4 event
                 event
                            0.785
                                      0.215
                                                   21 none
                                                                 Fold1
##
    5 non_event event
                            0.285
                                      0.715
                                                   27
                                                      none
                                                                 Fold1
    6 non_event non_event 0.442
                                      0.558
                                                   39 none
                                                                 Fold1
```

```
0.565
                                                   40 none
                                                                 Fold1
    7 non event non event 0.435
##
    8 event
                 event
                           0.800
                                      0.200
                                                   43 none
                                                                Fold1
                 non event 0.698
                                                   48 none
   9 event
                                      0.302
                                                                 Fold1
## 10 non_event event
                           0.384
                                      0.616
                                                                 Fold1
                                                   52 none
## # i 145 more rows
```

The ROC curve is calculated by comparing the model predicted probability to all possible thresholds to create many different classifications. Those different classifications are used to calculate many different confusion matrices. Thus, the columns of primary interest in the prediction object displayed above are the obs and event columns.

You manually created 3 points on the ROC curve previously in this assignment. Do NOT worry, you do NOT need to repeat those actions here! Instead you will use the roc\_curve() function from the yardstick package to create the ROC curve data for you. The roc\_curve() function has three primary arguments. The first is a data object which contains the predictions in a "tidy" format. The second is the name of the column that corresponds to the observed outcome (the truth or reference). The third is the name of the column in the data set that corresponds to the model predicted event probability.

Pipe the prediction data object for the mod\_1\_roc caret object to the roc\_curve(). The obs column is the observed outcome and the event column is the model predicted event probability. Display the result to the screen to confirm the roc\_curve() function worked. If it did the first few rows should correspond to very low threshold values.

Why does the sensitivity have values at or near 1 when the .threshold is so low?

```
roc_data5e <- roc_curve(mod_1_roc$pred,obs, event)
print(roc_data5e)</pre>
```

#### SOLUTION

```
## # A tibble: 157 x 3
##
       .threshold specificity sensitivity
##
            <dbl>
                          <dbl>
                                       <dbl>
##
    1
       -Inf
                        0
                                       1
##
    2
                        0
           0.0153
                                       1
    3
           0.0289
                        0
                                       0.987
##
    4
           0.0364
                        0
                                       0.973
##
##
    5
           0.0458
                        0
                                       0.96
##
    6
           0.0528
                        0.0125
                                       0.96
##
    7
           0.0559
                        0.0125
                                       0.947
##
    8
           0.0625
                        0.0250
                                       0.947
##
    9
           0.0765
                        0.0375
                                       0.947
## 10
           0.0796
                        0.0500
                                       0.947
## # i 147 more rows
```

What do you think?

When the threshold is so low, the prediction is classified as "event" in each case, which makes FN=0.

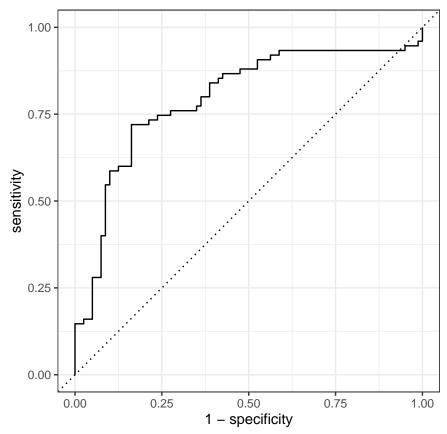
Sensitivity=TP/(TP+FN)=TP/TP=1 in the case when threshold is so low.

**5f**)

You will now visualize the ROC curve associated with mod\_1\_roc.

Repeat the same steps you performed in 5e) above, except pipe the result to the autoplot() method.

```
roc_data5f <- roc_curve(mod_1_roc$pred,obs, event)
roc_data5f %>% autoplot()
```



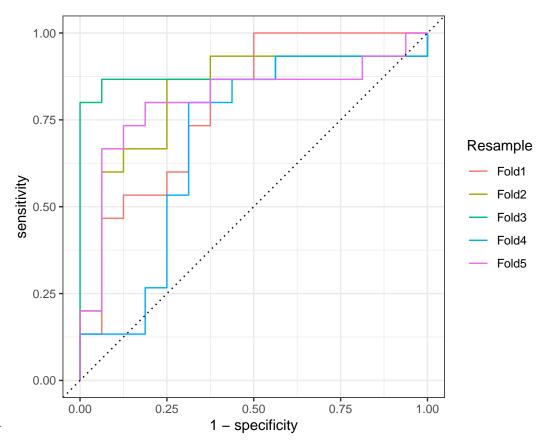
### SOLUTION

**5g**)

The ROC curve displayed in 5f) is the resample averaged ROC curve. You can examine the individual resample hold-out test set ROC curves by specifying a grouping structure with the group\_by() function. This can help you get a sense of the variability in the ROC curve.

Pipe the prediction object associated with mod\_1\_roc to the group\_by() function where you specify the grouping variable to be Resample. Pipe the result to roc\_curve() where you specify the same arguments as in the previous questions. Finally, pipe the result to autoplot().

```
roc_data5g <- mod_1_roc$pred %>% group_by(Resample)
roc_data5gg <- roc_data5g %>%roc_curve(obs, event)
autoplot(roc_data5gg)
```



### SOLUTION

# 5h)

A function is defined for you in the code chunk below. This function compiles all model results together to enable comparing their ROC curves.

The code chunk below is also completed for you. It passes the caret model objects with the saved predictions to the compile\_all\_model\_preds() function. The result is printed for you below so you can see the column names. Notice there is a new column model\_name which stores the name of the model associated with the resample hold-out test set predictions. By default the code chunk below is not executed.

## # A tibble: 1,240 x 4

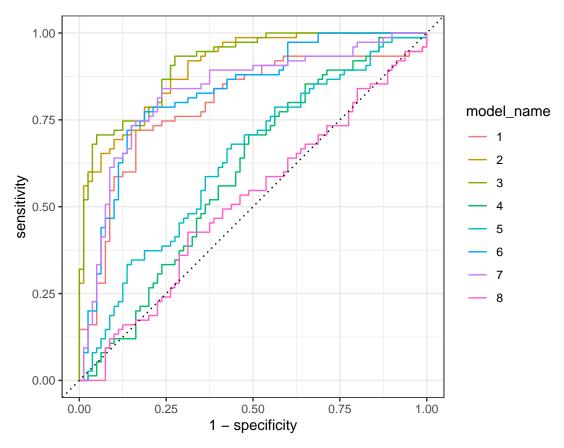
```
##
      obs
                event Resample model_name
##
      <fct>
                <dbl> <chr>
                               <chr>>
##
   1 non event 0.249 Fold1
  2 non_event 0.175 Fold1
                               1
##
##
   3 non_event 0.131 Fold1
                               1
##
  4 event
                0.785 Fold1
                               1
  5 event
               0.285 Fold1
##
   6 non_event 0.442 Fold1
                               1
##
   7 non_event 0.435 Fold1
                               1
##
  8 event
                0.800 Fold1
                               1
## 9 non_event 0.698 Fold1
                               1
## 10 event
                0.384 Fold1
                               1
## # i 1,230 more rows
```

You will now create a figure which displays the resample averaged ROC curve for each model.

Pipe the all\_model\_preds object to group\_by() and specify the grouping variable as model\_name. Pipe the result to roc\_curve() and specify the arguments accordingly. Pipe the result to autoplot() to generate the figure.

Which model is the best? Is the result consistent with the ROC AUC summary metrics you calculated previously? Which model is closest to a "completely ineffective model" and why is that so?

```
roc_curves5h <- all_model_preds %>%
  group_by(model_name) %>%
  roc_curve(obs, event)
autoplot(roc_curves5h)
```



SOLUTION

What do you think?

- 1) The best model is Model 3. Because the area under the ROC curve is the highest in that case.
- 2) The results are consistent with ROC AUC summary metrics I calculated previously. The best models are Model 3 and Model 2, the worst Model is Model 8 in both cases.
- 3) Model 8 is closest to "completely ineffective model", because its ROC curve is close to the line y=x.

# Problem 06

The performance metrics you have focused on up to this point are point-wise comparison metrics which evaluate the classification performance of a model. As discussed in lecture, binary classifier performance can also be measured based on the **calibration** between the predicted probability and the observed event proportion. The performance is represented graphically via the **calibration curve** which visualizes the correlation between the model predictions and the observed proportion of the event.

Regardless of your rankings in the previous questions, you will compare the performance of model 1, model 3, and model 8 with the calibration curve. Although multiple functions exist to create the calibration curve, you **must** create the calibration curve manually in this problem. You are only allowed to use functions from the dplyr and ggplot2 packages. You are **not** allowed to use any third party function to calculate the calibration curve in this problem.

In the two previous problems, you used resampling to assess model performance. We could create the calibration curve based on the resample fold test sets, but we will instead start simpler and use a dedicated hold-out set that is different from the training data. The hold-out set is read in for you in the code chunk below.

test\_data\_path <- 'hw03\_test\_data.csv'</pre>

```
df_test <- readr::read_csv(test_data_path, col_names = TRUE)

## Rows: 120 Columns: 5

## -- Column specification ------

## Delimiter: ","

## chr (1): y

## dbl (4): x1, x2, x3, x4

##

## i Use `spec()` to retrieve the full column specification for this data.

## is Specify the column types or set `show_col_types = FALSE` to quiet this message.

df_test <- df_test %>%

mutate(y = factor(y, levels = c("event", "non_event")))
```

The code chunk below shows a glimpse of the test set, which demonstrates the test set has the same column names as the training set.

```
df_test %>% glimpse()

## Rows: 120

## Columns: 5

## $ x1 <dbl> -0.226126900, 1.573924144, -1.054455037, 0.083051357, 0.424592933, ~

## $ x2 <dbl> -0.3361453, 0.5445463, 0.5837157, -0.8979020, -0.6339053, -0.641050~

## $ x3 <dbl> -1.22092445, -0.41352769, 2.45375479, -0.31070519, 0.40871874, 0.15~

## $ x4 <dbl> 0.59734091, 1.16494692, 0.41455929, 0.03209814, -0.91177742, 0.1022~

## $ y <fct> event, non_event, non_event, non_event, non_event, non_event, non_event
```

The first step to create the calibration curve requires making predictions. The predict() function for a caret trained object function has two main arguments. The first is the model object we will use to make predictions with and the second, newdata, is the data set to predict. The input columns must have the same names as the inputs to the training data that trained the model.

By default, a binary classifier will return the classifications assuming a 50% threshold. As discussed in lecture, the calibration curve does not work with classifications. Instead we need the predicted probability! We can override the default prediction behavior by setting additional arguments to the predict() function. Specifically, the type argument instructs the model to return a "type" of prediction. We want the predicted probability and so you must set type = 'prob' in the predict() function call.

Predict the hold-out test set using model 1 and assign the result to the variable pred\_test\_1. Return the predicted probability by setting the type argument to 'prob'.

Print the data type of the pred\_test\_1 object to the screen and use the head() function to display the "top" of the object.

HINT: It does not matter whether you use the model 1 assessed based on Accuracy or ROC in this problem.

```
pred_test_1 <- predict(mod_1_roc,newdata = df_test,type = 'prob')
class(pred_test_1)</pre>
```

#### SOLUTION

```
## [1] "data.frame"
```

### head(pred\_test\_1)

```
## event non_event
## 1 0.2607671 0.7392329
## 2 0.7113031 0.2886969
## 3 0.7467320 0.2532680
## 4 0.1964256 0.8035744
## 5 0.3579798 0.6420202
## 6 0.2867937 0.7132063

6b)
```

Your pred\_test\_1 object should have 2 columns. The event column gives the predicted probability that y == 'event' and the non\_event column stores the predicted probability that y == 'non\_event'.

What is the relationship between the values in the event column and the non\_event column?

### **SOLUTION** What do you think?

In each row, the sum of the values equals 1, which is expected in binary classification.

#### 6c)

The code chunk below binds the columns in pred\_test\_1 with the df\_test dataframe to create a new dataframe which includes the predicted probability of the event and the observed output, y, for the hold-out test set. PLEASE NOTE: the code chunk below is NOT evaluated by default. You must change the eval chunk option to make sure the code chunk is executed when you render the report.

```
test_df_1 <- df_test %>% bind_cols(pred_test_1)
```

As discussed in lecture, the calibration curve bins or lumps the predicted probability into uniformly spaced intervals. The empirical proportion of the event within each bin must be calculated. Thus, you need to convert the numeric predicted probability into a discrete or categorical variable.

A simple, yet effective, approach for categorizing a continuous variable is the cut() function. The cut function is demonstrated in the code chunk below. The variable x is a column within a tibble (a dataframe). The x variable consists of integers between 0 and 100. The x variable is "cut" or divided into bins with **break points** at values of 0, 10, 20, 30, etc. The break points are created using the seq() function from 0 to 100 by increments of 10. The tibble is piped to the count() function to count the number of rows associated with each unique value of the  $x_bin$ . Pay close attention to the displayed values of  $x_bin$ . The values of  $x_bin$  show the "cut" or "divided" intervals.

```
## # A tibble: 10 x 2
##
      x_bins
                     n
##
      <fct>
                 <int>
    1 [0,10]
##
                    11
    2 (10,20]
                    10
##
    3 (20,30]
                    10
    4 (30,40]
##
                    10
    5 (40,50]
##
                    10
    6 (50,60]
                    10
```

```
## 7 (60,70] 10
## 8 (70,80] 10
## 9 (80,90] 10
## 10 (90,100] 10
```

You must use the cut() function to bin the predicted probability associated with model 1 into 10 bins. Think carefully about how to specify the breaks argument to cut() so that the probability is divided into 10 uniform intervals.

Pipe test\_df\_1 to mutate() and create a variable pred\_bin by cutting the predicted probability into 10 uniform intervals. Assign the result to the test\_df\_1\_b object.

HINT: You should not pipe the result to count() as the previous code chunk did. The count() function was used to show the *levels* of the created discrete variable.

```
test_df_1_b <- test_df_1 %>%
  mutate(pred_bin = cut(event, breaks = seq(0, 1, by = 0.1), include.lowest = TRUE))
```

#### SOLUTION

6d)

Use the count() function to count the number of rows associated with each unique value of pred\_bin in the test\_df\_1\_b object. Display the result to the screen. How many unique values are displayed?

```
result6d <- test_df_1_b %>%
  count(pred_bin)
result6d
```

#### SOLUTION

**6e**)

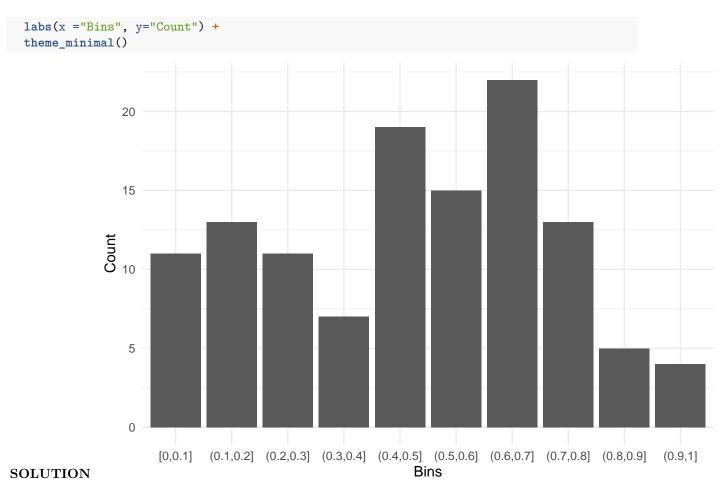
```
## # A tibble: 10 x 2
##
      pred bin
                     n
##
      <fct>
                 <int>
   1 [0,0.1]
                    11
   2 (0.1,0.2]
##
                    13
##
   3 (0.2,0.3]
                    11
                    7
##
   4 (0.3,0.4]
##
  5 (0.4,0.5]
                    19
  6 (0.5,0.6]
##
                    15
   7 (0.6,0.7]
                    22
##
## 8 (0.7,0.8]
                    13
## 9 (0.8,0.9]
                     5
## 10 (0.9,1]
                     4
```

Show the counts per bin again but this time visualize the counts with a bar chart.

show the country per our again but this time that because with a surface.

Create a bar chart with ggplot2 for the counts associated with unique value of pred\_bin.

```
ggplot(result6d, aes(x=pred_bin, y=n)) +
geom_bar(stat = "identity") +
```



6f)

As shown in the lecture slides, we can create a stacked bar chart to get a rough idea about the number of events and non-events within each predicted probability bin. This is simple to do with ggplot2 by using the fill aesthetic associated with the geom\_bar() geometric object.

Create a stacked bar chart with ggplot2 where the fill aesthetic is mapped to the observed binary outcome. Overrid the default fill color scheme by including the scale\_color\_brewer() function after the geom\_bar() layer. Set the palette argument in scale\_color\_brewer() to 'Set1'.

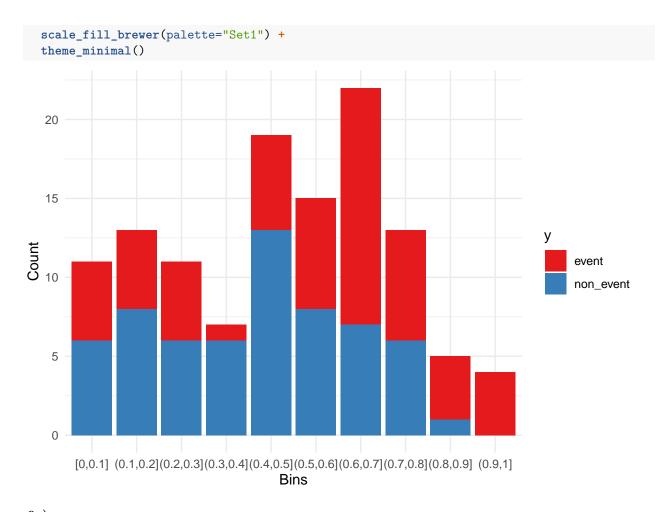
Do any bins consist of only events? Do any bins consist of only non-events?

*HINT*: Which variable in the test\_df\_1 tibble corresponds to the observed outcome?

## **SOLUTION** What do you think?

- 1) "y" variable corresponds to the observed outcome.
- 2) The 95% bin consist of only events.
- 3) There are no bins consist of only non-events.

```
ggplot(test_df_1_b, aes(x=pred_bin, fill=y)) +
  geom_bar() +
  labs(x="Bins", y="Count") +
```



# **6g**)

Instead of showing the counts within each bin, let's change the bar chart so the maximum height is 1. The stacked bar chart will therefore show the proportion of events and non-events within each predicted probability bin.

Recreate the stacked bar chart from the previous problem, but this time set the position argument to 'fill' within the geom\_bar() layer. The position argument should be specified outside the aes() function with geom\_bar(). You must continue to map the fill aesthetic to the observed outcome.

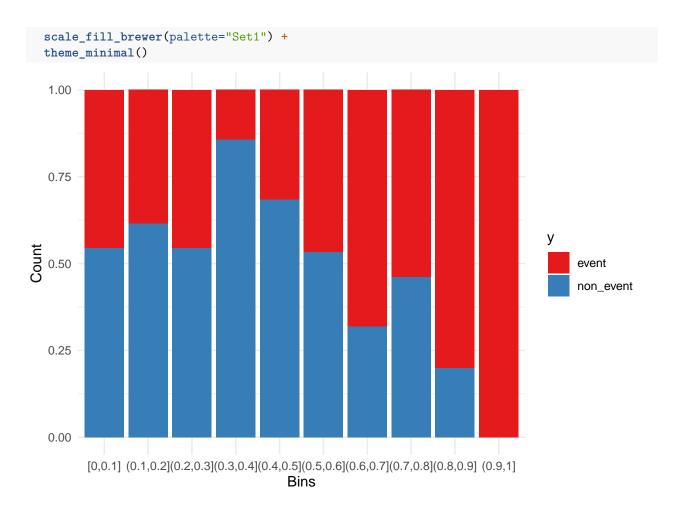
Are the empirical proptions of the event consistent with the predicted probability for model 1?

HINT: Pay close attention to the bar chart colors!

#### **SOLUTION** What do you think?

- 1) For these bins the empirical proptions of the event are looking consistent with the predicted probability for model 1: 95%, 85%, 65%, 55%.
- 2) For these bins the empirical proptions of the event are NOT looking consistent with the predicted probability for model 1: 5%, 15%, 25%, 35%, 45%, 75%.

```
ggplot(test_df_1_b, aes(x=pred_bin, fill=y)) +
  geom_bar(position='fill') +
  labs(x="Bins", y="Count") +
```



## Problem 07

The bar chart visualized in Problem 06 is the calibration curve for model 1, but that is not how calibration curves are typically displayed. As shown in lecture, calibration curves are visualized as scatter plots with lines connecting the markers. The previous problem was used to demonstrate the proportion of the event per bin. In this problem, you will calculate the proportion of the event manually in each bin.

This problem is open ended. You are free to calculate the event proportions however you want, as long as you do **NOT** use existing calibration curve functions. You are only allowed to use functions within dplyr and ggplot2 in this problem.

7a)

Calculate the empirical proportion of events within each predicted probability bin associated with model 1. Although you are free to perform the calculations however you like, the results should be stored in a tibble (dataframe) named my\_calcurve\_1 object. Your object should have columns for the pred\_bin, the event proportion in the bin named prop\_event, and the midpoint of the bin named mid\_bin. Your my\_calcurve\_1 object can have other columns, but those three columns are required.

**SOLUTION** Add as many code chunks as you feel are necessary.

```
### create prop_event column
bin_event_c <- numeric(10)
for (i in 1:nrow(test_df_1_b)) {</pre>
```

```
if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "[0,0.1]") {bin_event_c[1] = bin_event_c[1] +
}
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.1,0.2]") {bin_event_c[2] = bin_event_c[2]
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.2,0.3]") {bin_event_c[3] = bin_event_c[3]
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.3,0.4]") {bin_event_c[4] = bin_event_c[4]
}
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.4,0.5]") {bin_event_c[5] = bin_event_c[5]
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.5,0.6]") {bin_event_c[6] = bin_event_c[6]
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.6,0.7]") {bin_event_c[7] = bin_event_c[7]
}
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.7,0.8]") {bin_event_c[8] = bin_event_c[8]
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.8,0.9]") {bin_event_c[9] = bin_event_c[9]
}
for (i in 1:nrow(test_df_1_b)) {
  if(test_df_1_b$y[i] == "event" && test_df_1_b$pred_bin[i] == "(0.9,1]") {bin_event_c[10] = bin_event_c[10]
bin_prop <- numeric(10)</pre>
for (i in 1:10) {
  bin_prop[i]=bin_event_c[i]/result6d$n[i]}
### Add prop_event column to my_calcurve_1
my_calcurve_1 <- result6d %>%
  mutate(prop_event = bin_prop)
### Create mid_bin column
bin_m <- numeric(10)</pre>
for (i in 1:10) {
 bin_m[i]=(i-0.5)/10
### Add mid_bin column to my_calcurve_1
my_calcurve_1 <- my_calcurve_1 %>%
 mutate(mid_bin = bin_m)
### Display my_calcurve_1 in the final form
my_calcurve_1 <- my_calcurve_1 %>% select(-n)
my_calcurve_1
## # A tibble: 10 x 3
##
      pred_bin prop_event mid_bin
##
      <fct>
                      <dbl>
                              <dbl>
```

## 1 [0,0.1]

0.455

0.05

```
2(0.1,0.2]
                     0.385
                              0.15
## 3 (0.2,0.3]
                     0.455
                              0.25
## 4 (0.3,0.4]
                     0.143
                              0.35
## 5 (0.4,0.5]
                     0.316
                              0.45
## 6 (0.5,0.6]
                     0.467
                              0.55
  7 (0.6,0.7]
                     0.682
##
                              0.65
  8 (0.7,0.8]
                     0.538
                              0.75
## 9 (0.8,0.9]
                     0.8
                              0.85
## 10 (0.9,1]
                     1
                              0.95
```

## 7b)

You will now create the calibration curve associated with model 1's predictions on the hold-out test set! You must use the my\_calcurve\_1 object created in Problem 7a).

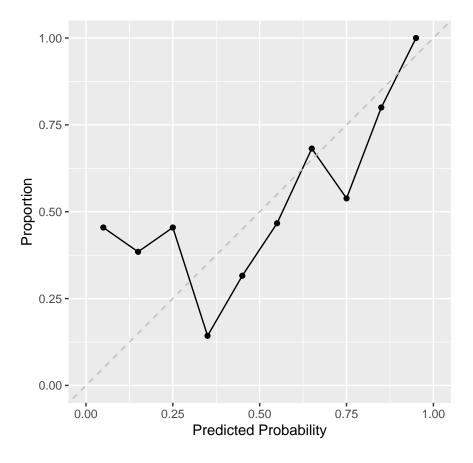
Pipe the my\_calcurve\_1 object to ggplot() and map mid\_bin and prop\_event to the x and y aesthetics, respectively. Include geom\_line() and geom\_point() layers and a geom\_abline() layer. Set the geom\_abline() arguments as slope=1, intercept=0, color='grey', and linetype='dashed'. Include coord\_equal() with xlim = c(0,1) and ylim = c(0,1).

Is the calibration curve consistent with your stacked filled barchart created previously? Pay close attention to the colors in the bar chart when comparing them!

### **SOLUTION** What do you think?

Yes, the calibration curve consistent with the stacked filled barchart I created previously. For example, in bin (0.9,1] the bardchart was full of red (events), and in the calibration curve, corresponding proportion for 0.95 prediction is 1 (as expected).

```
ggplot(my_calcurve_1, aes(x=mid_bin,y=prop_event)) +
  geom_line() +
  geom_point() +
  geom_abline(intercept=0,slope=1, color = 'grey', linetype='dashed') +
  coord_equal(xlim = c(0,1), ylim = c(0,1)) +
  labs(x="Predicted Probability", y="Proportion")
```



## **7c**)

Now it's time to create the necessary objects associated with model 3 and model 8. As we started with model 1, we must predict the hold-out test set and return the predicted event probabilities.

Predict the hold-out test set using model 3 and model 8. Assign the results to the variables pred\_test\_3 and pred\_test\_8 for model 3 and model 8, respectively.

```
pred_test_3 <- predict(mod_3_roc,newdata = df_test,type = 'prob')
pred_test_8 <- predict(mod_8_roc,newdata = df_test,type = 'prob')</pre>
```

### **SOLUTION**

## 7d)

The code chunk below is completed for you. The model 3 and model 8 predictions are combined with the hold-out test set data so you have the predicted probabilities and observed outcome within a tibble (dataframe). **PLEASE NOTE**: the code chunk below is **NOT** evaluated by default. You must change the **eval** chunk option to make sure the code chunk is executed when you render the report.

```
test_df_3 <- df_test %>% bind_cols(pred_test_3)
test_df_8 <- df_test %>% bind_cols(pred_test_8)
```

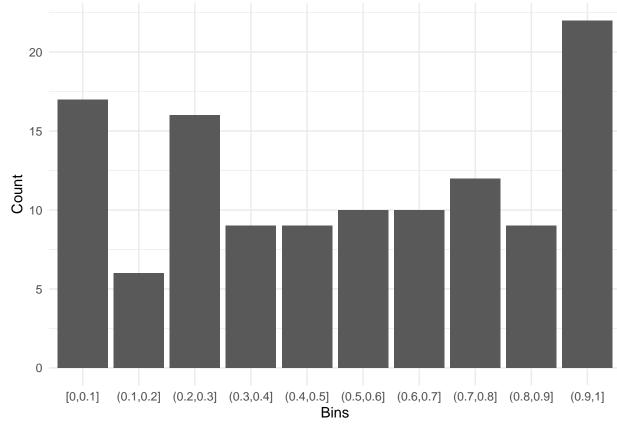
You must create the categorical predicted probability bins for model 3 and model 8 using the cut() function. Assign the results to the test\_df\_3\_b and test\_df\_8\_b objects for model 3 and model 8, respectively.

```
test_df_3_b <- test_df_3 %>%
  mutate(pred_bin = cut(event, breaks = seq(0, 1, by = 0.1), include.lowest = TRUE))
test_df_8_b <- test_df_8 %>%
  mutate(pred_bin = cut(event, breaks = seq(0, 1, by = 0.1), include.lowest = TRUE))
```

7e)

Use ggplot2 to visualize the number of observations per bin for model 3 with a bar chart.

```
result7e <- test_df_3_b %>%
  count(pred_bin)
ggplot(result7e, aes(x=pred_bin, y=n)) +
  geom_bar(stat = "identity") +
  labs(x = "Bins", y="Count") +
  theme_minimal()
```



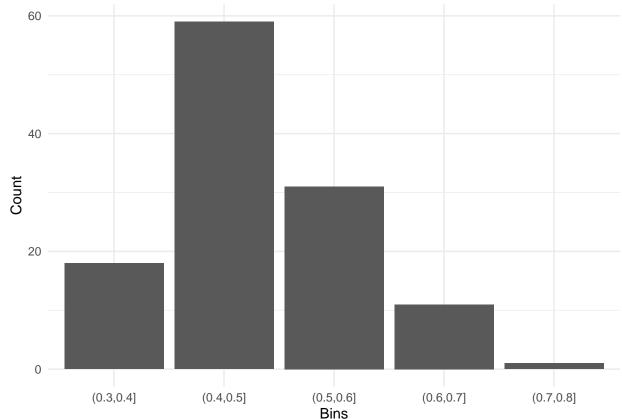
SOLUTION

**7f**)

Use ggplot2 to visualize the number of observations per bin for model 8 with a bar chart.

```
result7f <- test_df_8_b %>%
  count(pred_bin)
```

```
ggplot(result7f, aes(x=pred_bin, y=n)) +
geom_bar(stat = "identity") +
labs(x ="Bins", y="Count") +
theme_minimal()
```



## Problem 08

Rather than using the stacked filled bar charts to represent the calibration curve for models 3 and 8, let's jump straight to creating the calibration curve object for the two models.

### 8a)

Calculate the empirical proportion of events within each predicted probability bin associated with model 3. Although you are free to perform the calculations however you like, the results should be stored in a tibble (dataframe) named my\_calcurve\_3 object. Your object should have columns for the pred\_bin, the event proportion in the bin named prop\_event, and the midpoint of the bin named mid\_bin. Your my\_calcurve\_3 object can have other columns, but those three columns are required.

**SOLUTION** Add as many code chunks as you feel are necessary.

```
### create prop_event column
bin_event_c3 <- numeric(10)
for (i in 1:nrow(test_df_3_b)) {
   if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "[0,0.1]") {bin_event_c3[1] = bin_event_c3[1] }
for (i in 1:nrow(test_df_3_b)) {</pre>
```

```
if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.1,0.2]") {bin_event_c3[2] = bin_event_c3
}
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.2,0.3]") {bin_event_c3[3] = bin_event_c3
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.3,0.4]") {bin_event_c3[4] = bin_event_c3
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.4,0.5]") {bin_event_c3[5] = bin_event_c3
}
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.5,0.6]") {bin_event_c3[6] = bin_event_c3
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.6,0.7]") {bin_event_c3[7] = bin_event_c3
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.7,0.8]") {bin_event_c3[8] = bin_event_c3
}
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.8,0.9]") {bin_event_c3[9] = bin_event_c3
for (i in 1:nrow(test_df_3_b)) {
    if(test_df_3_b$y[i] == "event" && test_df_3_b$pred_bin[i] == "(0.9,1]") {bin_event_c3[10] = bin_event_c3[10] = bin_event_c3[10]
bin_prop3 <- numeric(10)</pre>
for (i in 1:10) {
    bin_prop3[i]=bin_event_c3[i]/result7e$n[i]}
### Add prop_event column to my_calcurve_3
my_calcurve_3 <- result7e %>%
    mutate(prop_event = bin_prop3)
### Create mid_bin column
bin_m3 <- numeric(10)</pre>
for (i in 1:10) {
    bin_m3[i]=(i-0.5)/10
### Add mid_bin column to my_calcurve_3
my_calcurve_3 <- my_calcurve_3 %>%
   mutate(mid_bin = bin_m3)
### Display my_calcurve_3 in the final form
my_calcurve_3 <- my_calcurve_3 %>% select(-n)
my_calcurve_3
## # A tibble: 10 x 3
##
            pred_bin prop_event mid_bin
##
            <fct>
                                            <dbl>
                                                             <dbl>
## 1 [0,0.1]
                                            0.118
                                                               0.05
## 2 (0.1,0.2]
                                            0.167
                                                               0.15
## 3 (0.2,0.3]
                                            0.312
                                                               0.25
## 4 (0.3,0.4]
                                            0.333
                                                              0.35
```

```
## 5 (0.4,0.5]
                     0.111
                               0.45
                     0.6
## 6 (0.5,0.6]
                               0.55
## 7 (0.6,0.7]
                     0.6
                               0.65
## 8 (0.7,0.8]
                     0.583
                               0.75
## 9 (0.8,0.9]
                     0.778
                               0.85
## 10 (0.9,1]
                     0.955
                               0.95
8b)
```

Calculate the empirical propotion of events within each predicted probability bin associated with model 8. Although you are free to perform the calculations however you like, the results should be stored in a tibble (dataframe) named my\_calcurve\_8 object. Your object should have columns for the pred\_bin, the event proportion in the bin named prop\_event, and the midpoint of the bin named mid\_bin. Your my\_calcurve\_8 object can have other columns, but those three columns are required.

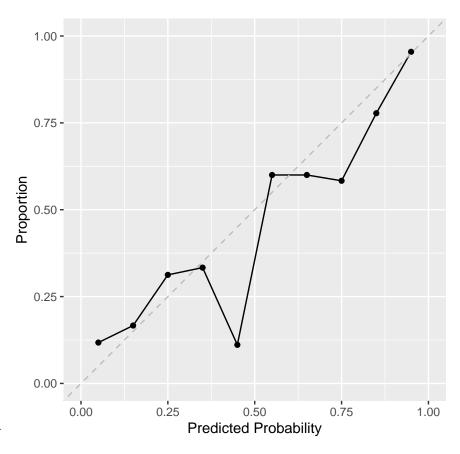
**SOLUTION** Add as many code chunks as you feel are necessary.

```
### create prop_event column
bin_event_c8 <- numeric(10)</pre>
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "[0,0.1]") {bin_event_c8[1] = bin_event_c8[1]
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.1,0.2]") {bin_event_c8[2] = bin_event_c8
}
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.2,0.3]") {bin_event_c8[3] = bin_event_c8
}
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.3,0.4]") {bin_event_c8[4] = bin_event_c8
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.4,0.5]") {bin_event_c8[5] = bin_event_c8
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.5,0.6]") {bin_event_c8[6] = bin_event_c8
}
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.6,0.7]") {bin_event_c8[7] = bin_event_c8
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.7,0.8]") {bin_event_c8[8] = bin_event_c8
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.8,0.9]") {bin_event_c8[9] = bin_event_c8
}
for (i in 1:nrow(test_df_8_b)) {
  if(test_df_8_b$y[i] == "event" && test_df_8_b$pred_bin[i] == "(0.9,1]") {bin_event_c8[10] = bin_event_c8[
bin_prop8 <- numeric(5)</pre>
for (i in 1:5) {
  bin_prop8[i]=bin_event_c8[i+3]/result7f$n[i]}
### Add prop_event column to my_calcurve_8
```

```
my_calcurve_8 <- result7f %>%
  mutate(prop_event = bin_prop8)
### Create mid bin column
bin m8 <- numeric(5)</pre>
for (i in 1:5) {
 bin_m8[i]=(i+3-0.5)/10
### Add mid_bin column to my_calcurve_8
my_calcurve_8 <- my_calcurve_8 %>%
 mutate(mid_bin = bin_m8)
### Add rows to my_calcurve_8 where prop_event = 0 to display the full calibration curve
my_calcurve_8 <- my_calcurve_8 %>% select(-n)
new_row1 \leftarrow tibble(pred_bin = "(0.2,0.3]", prop_event = 0, mid_bin=0.25)
my_calcurve_8 <- add_row(my_calcurve_8, .before = 1, !!!new_row1)</pre>
new_row2 <- tibble(pred_bin = "(0.1,0.2]", prop_event = 0, mid_bin=0.15)</pre>
my_calcurve_8 <- add_row(my_calcurve_8, .before = 1, !!!new_row2)</pre>
new_row3 \leftarrow tibble(pred_bin = "[0,0.1]", prop_event = 0, mid_bin=0.05)
my_calcurve_8 <- add_row(my_calcurve_8, .before = 1, !!!new_row3)</pre>
new_row4 <- tibble(pred_bin = "(0.8,0.9]", prop_event = 0, mid_bin=0.85)</pre>
my_calcurve_8 <- add_row(my_calcurve_8, .after = 8, !!!new_row4)</pre>
new_row5 <- tibble(pred_bin = "(0.9,1]", prop_event = 0, mid_bin=0.95)</pre>
my_calcurve_8 <- add_row(my_calcurve_8, .after = 9, !!!new_row5)</pre>
### Display my_calcurve_8 in the final form
my_calcurve_8
## # A tibble: 10 x 3
##
      pred_bin prop_event mid_bin
##
      <chr>
                      <dbl>
                              <dbl>
## 1 [0,0.1]
                               0.05
                      0
## 2 (0.1,0.2]
                      0
                               0.15
## 3 (0.2,0.3]
                      0
                               0.25
## 4 (0.3,0.4]
                      0.444
                               0.35
## 5 (0.4,0.5]
                      0.492
                               0.45
## 6 (0.5,0.6]
                      0.484
                               0.55
## 7 (0.6,0.7]
                     0.636
                               0.65
## 8 (0.7,0.8]
                     0
                               0.75
## 9 (0.8,0.9]
                      0
                               0.85
## 10 (0.9,1]
                               0.95
8c)
```

Visualize the calibration curve for model 3 using the approach described in Problem 7b).

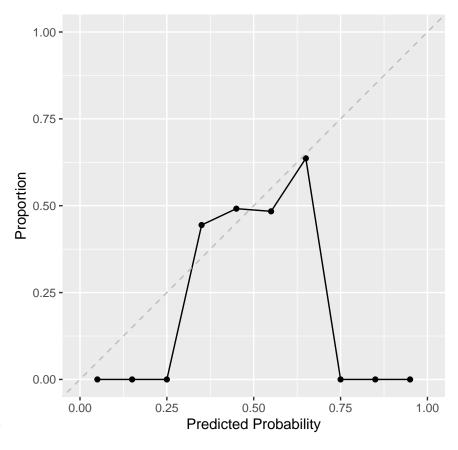
```
ggplot(my_calcurve_3, aes(x=mid_bin,y=prop_event)) +
  geom_line() +
  geom_point() +
  geom_abline(intercept=0,slope=1, color = 'grey', linetype='dashed') +
  coord_equal(xlim = c(0,1), ylim = c(0,1)) +
  labs(x="Predicted Probability", y="Proportion")
```



8d)

Visualize the calibration curve for model 8 using the approach described in Problem 7b).

```
ggplot(my_calcurve_8, aes(x=mid_bin,y=prop_event)) +
  geom_line() +
  geom_point() +
  geom_abline(intercept=0,slope=1, color = 'grey', linetype='dashed') +
  coord_equal(xlim = c(0,1), ylim = c(0,1)) +
  labs(x="Predicted Probability", y="Proportion")
```



8d)

Based on your calibration curves, which of the three models appears the most well calibrated? Is it easy obvious which model performs better using this approach? What are the most obvious aspects of performance based on your calibration curves?

## **SOLUTION** What do you think?

- 1) The most well calibrated model is Model 3 because in this model the proportion values corresponding to predicted probability lie more close to y=x line compared to the other models.
- 2) It is easy to observe which model performs better using this approach. You just need to check which calibration curve is "close" to the line y=x.
- 3) Model 8 generates fewer bins. It means there are more samples per bin. Too few bins limits the ability to check model performance over wide range of conditions.

### Problem 09

Calibration curves are created by executing many tedious steps. Although you had to perform those steps manually in this assignment there are existing functions which perform the necessary calculations for you. One such function is the caret::calibration() function. You will use that function in this problem to practice easily creating calibration curves. The caret::calibration() function works with resampled results, but for consistency with the previous problems, we will use with the hold-out test set predictions associated with the df\_test data set.

The caret::calibration() function has 3 main arguments. The first argument is a formula, the second argument is the data set, and third is the number of bins to use. The formula follows a specific pattern:

<binary output variable> ~ <event probability variable>

The formula therefore gives the binary outcome variable name to the **left** of the tilde and the variable name for the event probability to the **right** of the tilde. These names **must** match the column names in the data set assigned to the **data** argument. The number of bins is specified by the **cuts** argument.

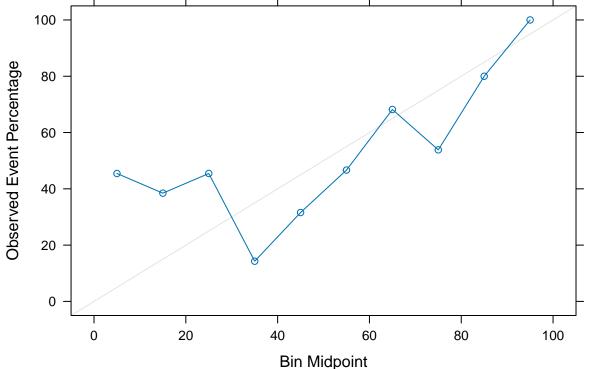
9a)

Create the calibration curve associated with model 1's hold-out test predictions using the caret::calibration() function. Specify the formula to be consistent with the test\_df\_1 data set. Assign the test\_df\_1 object to the data argument and assign cuts = 10. Pipe the result to the xyplot() function.

Is the created calibration curve consistent with your manually created curve from the previous problems?

**SOLUTION** Yes, the created calibration curve is consistent with my manually created curve from the previous problem.

calibration\_curve1 <- calibration(y ~ event, test\_df\_1, cuts = 10)
xyplot(calibration\_curve1)</pre>



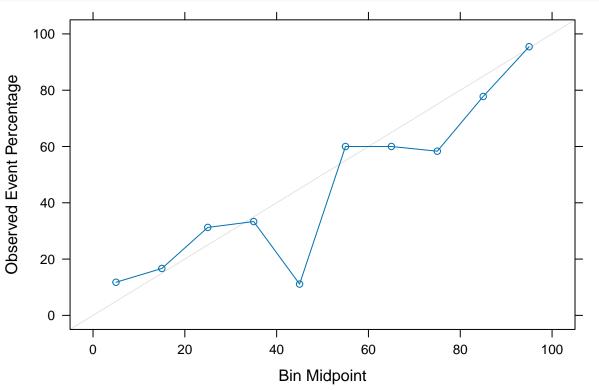
9b)

Create the calibration curve associated with model 3's hold-out test predictions using the caret::calibration() function. Specify the formula to be consistent with the test\_df\_3 data set. Assign the test\_df\_3 object to the data argument and assign cuts = 10. Pipe the result to the xyplot() function.

Is the created calibration curve consistent with your manually created curve from the previous problems?

**SOLUTION** Yes, the created calibration curve is consistent with my manually created curve from the previous problem.

```
calibration_curve3 <- calibration(y ~ event, test_df_3, cuts = 10)
xyplot(calibration_curve3)</pre>
```



9c)

Create the calibration curve associated with model 8's hold-out test predictions using the caret::calibration() function. Specify the formula to be consistent with the test\_df\_8 data set. Assign the test\_df\_8 object to the data argument and assign cuts = 10. Pipe the result to the xyplot() function.

Is the created calibration curve consistent with your manually created curve from the previous problems?

**SOLUTION** Yes, the created calibration curve is consistent with my manually created curve from the previous problem.

```
calibration_curve8 <- calibration(y ~ event, test_df_8, cuts = 10)
xyplot(calibration_curve8)</pre>
```

