Verification of the wave equation

```
HoldForm \begin{bmatrix} v^2 D[y[x, vt], \{x, 2\}] & v^2 & D[y[x, vt], \{t, 2\}] \end{bmatrix} // TraditionalForm (*We want to verify this*)

v^2 \frac{\partial^2 y(x, vt)}{\partial x^2} = \frac{\partial^2 y(x, vt)}{\partial t^2}

y[x_-, t_-] := Exp[-(x + t)^2] // Quiet; (*The equation of the wave, has to have this form: y(x,t) = y(x_-vt). I have put four examples, try whatever comes to your mind*)

y[x_-, t_-] := \frac{1}{(x + t)^2 + 1} // Quiet;

y[x_-, t_-] := Exp[-Abs[x + t]] // Quiet;

y[x_-, t_-] := \frac{t}{(x + t)} (*Not a wave:*)

SameQ[FullSimplify[v^2D[y[x, vt], {x, 2}]], FullSimplify[D[y[x, vt], {t, 2}]]] (*You can test this with different difinitions of y(x,t)*)

True

v^2D[y[x, vt], {x, 2}] // FullSimplify (*If you want to check the derivatives yourself*)
D[y[x, vt], {t, 2}] // FullSimplify

2e^{-(tv-x)^2}v^2 (-1+2 (tv+x)<sup>2</sup>)
```

Interactive plot

