Q1)

$$\beta_{-}: {}^{196}Au \rightarrow {}^{196}Hg + e^{-} + \bar{\nu}$$

 $\beta_{+}: {}^{196}Au \rightarrow {}^{196}Pt + e^{+} + \nu$
 $\varepsilon: {}^{196}Au + e^{-} \rightarrow {}^{196}Hg + \nu$

$$Q_{\beta_{-}} = \left[m \left({}^{A}X \right) - m \left({}^{A}X' \right) \right] c^{2} = \left[195.966544 - 195.965807 \right] * 931.502 \; MeV$$

$$= 686.517 \; MeV$$

$$Q_{\beta_{+}} = \left[m \left({}^{A}X \right) - m \left({}^{A}X' \right) - 2m_{e} \right] c^{2} = \left[195.966544 - 195.964926 - 2 * 5.485803 \times 10^{-4} \right] * 931.502 \; MeV$$

$$= 485.163 \; MeV$$

$$Q_{\varepsilon} = \left[m \left({}^{A}X \right) - m \left({}^{A}X' \right) \right] c^{2} - B_{n} = \left[195.966544 - 195.964926 \right] * 931.502 \; MeV - 7.914861 \; MeV$$

$$= -6.40769 \; MeV$$

Q2)

$$\begin{array}{ll} a)\Delta I=2; & \Delta\pi=yes: \mbox{ First Forbidden} \\ b)\Delta I=2; & \Delta\pi=no: \mbox{ Second Forbidden} \\ c)\Delta I=3; & \Delta\pi=no: \mbox{ Second Forbidden} \\ d)\Delta I=0; & \Delta\pi=no: \mbox{ Allowed Decay} \\ e)\Delta I=0; & \Delta\pi=yes: \mbox{ First Forbidden} \end{array}$$

Q3)

First, we need to get the energy of the excited state of ^{20}Ne by employing conservation of Energy. E_1 represents the energy the excited state has over the ground state of ^{20}Ne :

$$^{20}Na \rightarrow ^{20}Ne^* + e^+ + \nu$$

$$E_1 = \left[m\left(^{20}Na\right) - m\left(^{20}Ne\right)\right] * c^2 - T_e$$

$$E_1 = \left[20.007344 - 19.992436\right] * 931.502 \ MeV - 5.55 \ MeV = 8.34 \ MeV$$

$$^{20}Ne^* \rightarrow ^{16}O + \alpha$$

$$E_2 = \left[m\left(^{20}Ne\right) - m\left(^{16}O\right) - m\left(^{4}He\right)\right] * c^2$$

$$E_2 = \left[19.992436 - 15.994915 - 4.002603\right] * 931.502 \ MeV = -4.73389$$

$$Q = E_1 + E_2 = 8.34 - 4.73389 = 3.61 \ MeV$$

$$T_{\alpha} = \frac{Q}{1 + \frac{m_{\alpha}}{m_{X'}}} = \frac{3.61}{1 + \frac{4.00150618}{15.994915}} \ MeV = 2.89 \ MeV$$

Q4)

a)
$$\rho*R=0.421*E-0.106 \implies R=\frac{0.421*E^{-0.106}}{\rho}=\frac{0.412*(3.58)^{-0.106}}{2.7}=0.133~cm$$
 b) For Al $\mu/\rho=5.006\times 10^{-2} \implies \mu=0.135~cm^{-1}.~t_{1/2}=12.36~hrs=44496~s$
$$A_0=10~mCi;~~by~\gamma:2.5~mCi$$

$$A=A_0e^{-\mu x}=2.5e^{-0.135*0.133}=2.46~mCi=91020000~Decays/s$$

$$N=\lambda A=\frac{\ln 2}{t_{1/2}}*A=\frac{\ln 2}{44496}*91020000=1418~photons$$
 c)

 $1 - \frac{N}{N_0} = 1 - \frac{\frac{\ln 2}{t_{1/2}} * A}{\frac{\ln 2}{t_{1/2}} * A_0} = 1 - \frac{A}{A_0} = 1 - \frac{2.46}{2.5} = 0.016 = 1.6\% \ Absorbed$

d) Compton Effect