

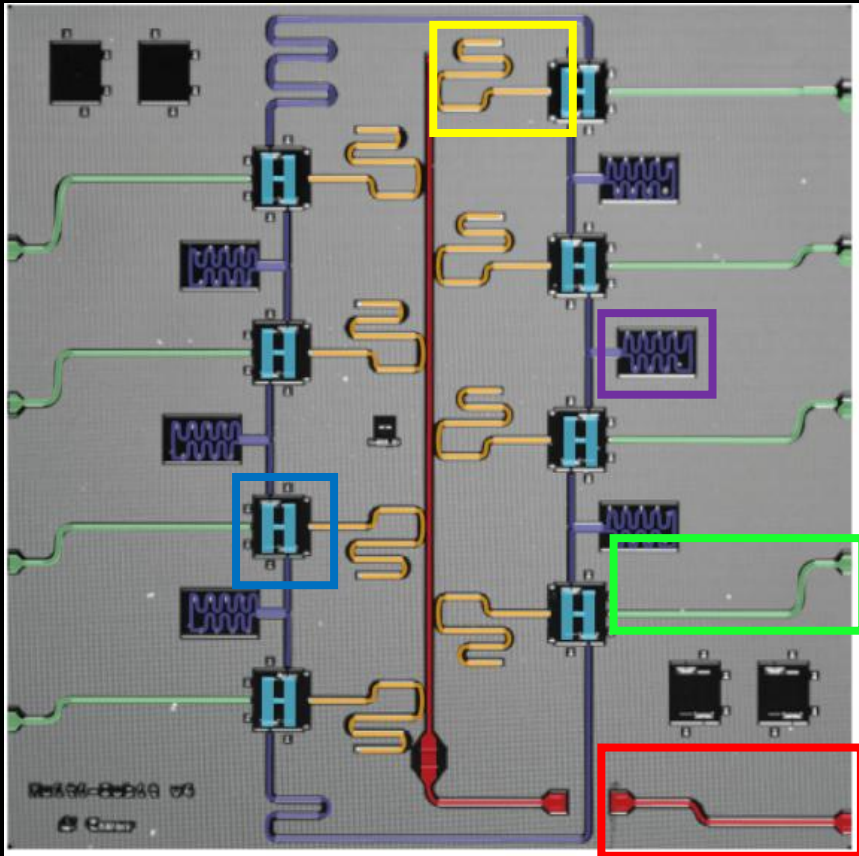
# Coplanar waveguide resonators

Mahmoud Almansouri

# Outline and outcomes

- Superconducting Quantum circuits
- Resonator's noise sources
- Design parameters to consider
- Input-output coupling
- Worked examples
- Full design workflow
- Use cases

# Superconducting quantum circuit



Main components:

1. Resonator CPWr.

2. Qubit (nonlinear inductor).

Complementary:  
3. Coupler for entanglement CPWr.

4. Drive line CPWr.

5. Readout line CPWr.

- Resonators are used in quantum circuits for:
  - Entanglement (qubit-qubit coupling).
  - Readout filtering and readout channel.
  - Control and drive of qubit states.
- Therefore, better resonators means less noise in the circuit.

# What is resonator's loss or noise?

$$Q = \frac{\textit{Energy stored}}{\textit{Energy lost per cycle}}$$

## Internal losses ( $Q_i$ ):

Physical loss sources causes the stored energy in the resonator to dissipate. This is measured assuming the resonator is in complete isolation from all other circuit components.

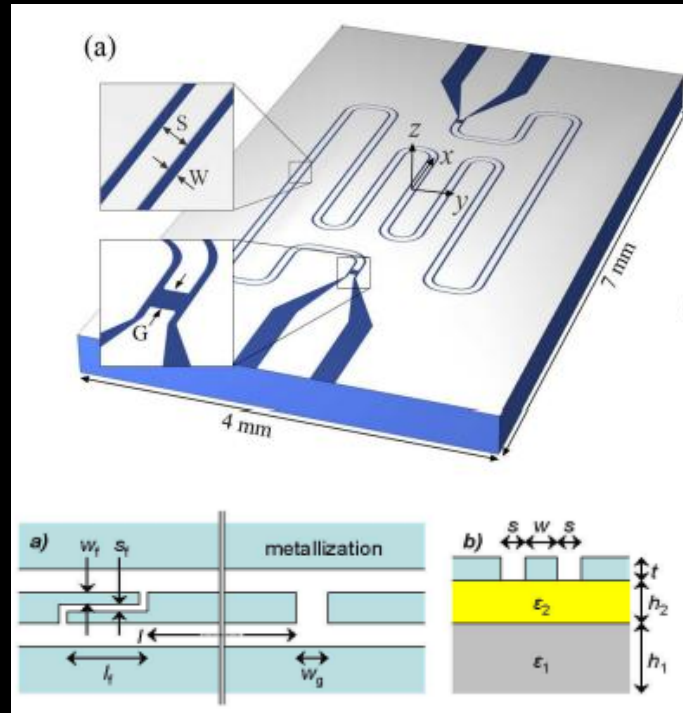
- Fabrication defects
- Metal contamination
- Substrate loss tangent

## External losses ( $Q_e$ ):

Simulated loss is determined by capacitive or inductive coupling between the circuit components using a simulation software.

- Crosstalk between circuit elements.
- Strong coupling between drive lines or readout line.

# Design parameters in resonators



- Frequency:  $f = \frac{c}{\sqrt{\epsilon_{eff}}} \frac{1}{2l}$  or  $f = \frac{c}{\sqrt{\epsilon_{eff}}} \frac{1}{4l}$
- Characteristic impedance:  $Z_o = \sqrt{L_l / C_l}$
- External quality factor ( $Q_e$ )
- Capacitance and coupling.

- HFSS
- CST
- COMSOL

Where:

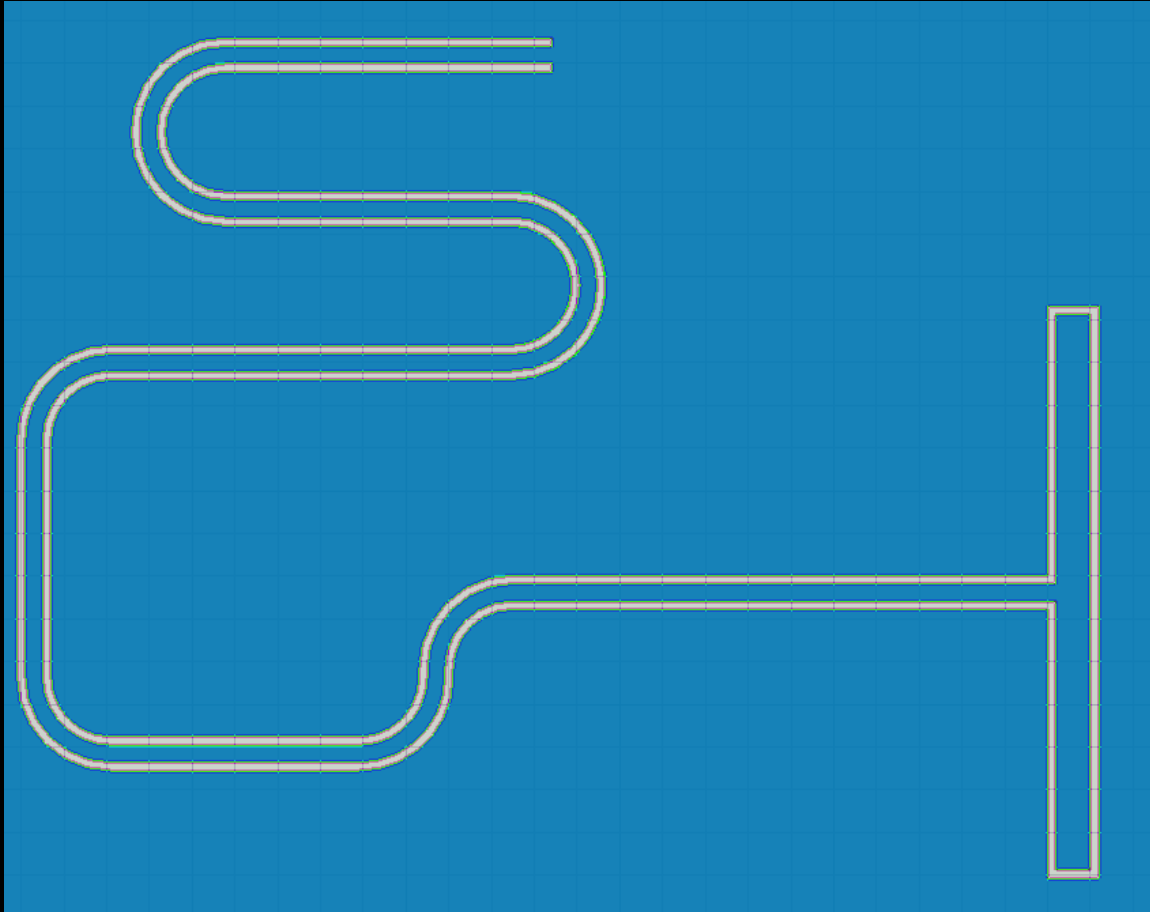
$$L_l = \frac{\mu_0}{4} \frac{K(k'_0)}{K(k_0)} \text{ and } C_l = 4\epsilon_0\epsilon_{eff} \frac{K(k_0)}{K(k'_0)}$$

$$k_0 = \frac{w}{w+2s} \text{ and } k'_0 = \sqrt{1 - k_0^2}$$

Typically W:S is 2:1 ( $w=20 \mu\text{m}$  and  $s=10 \mu\text{m}$ ):

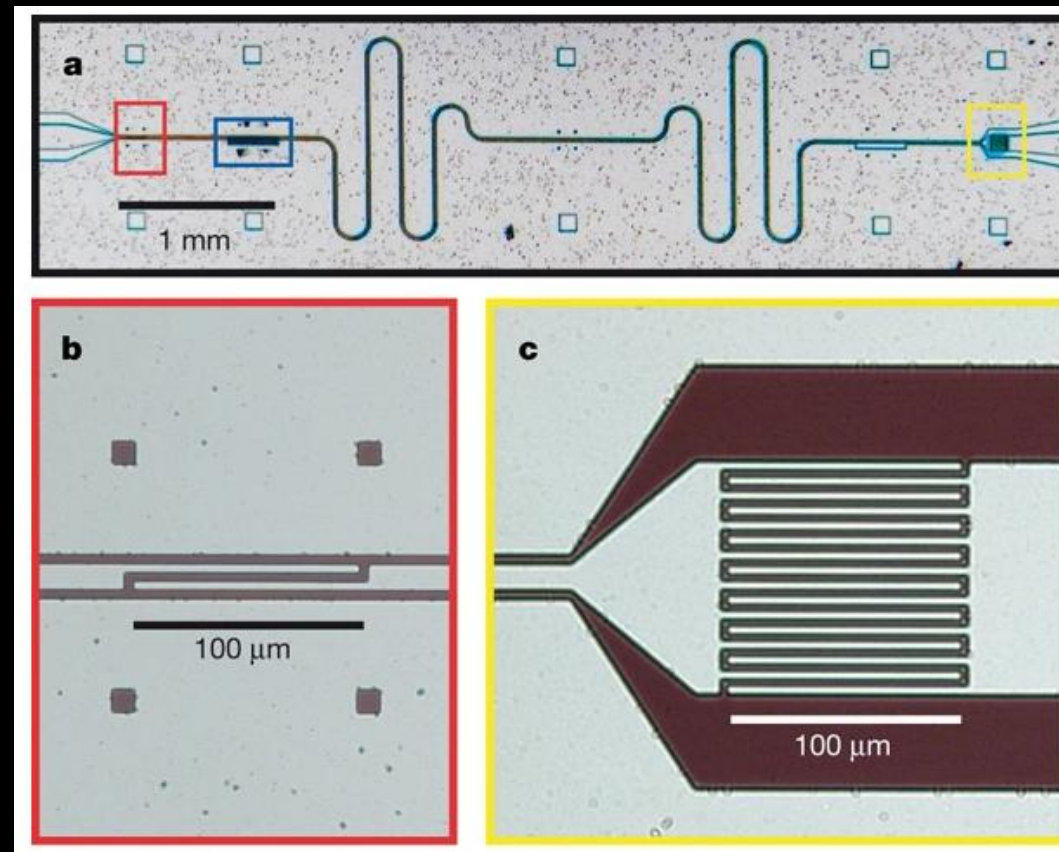
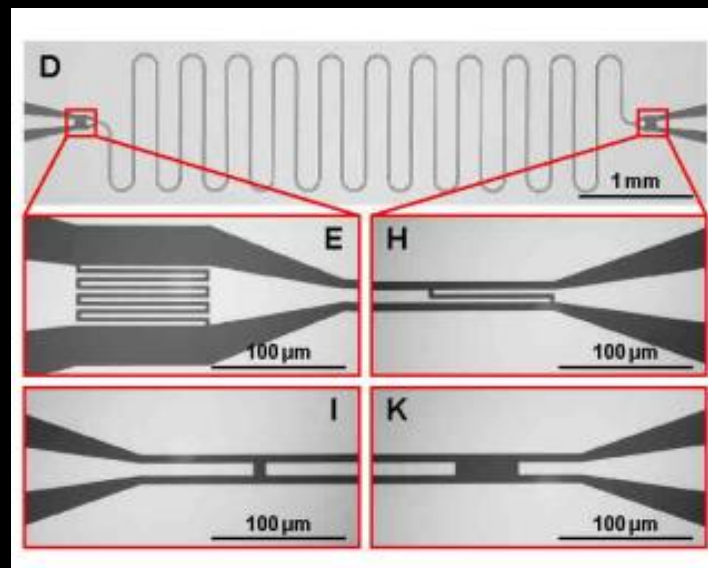
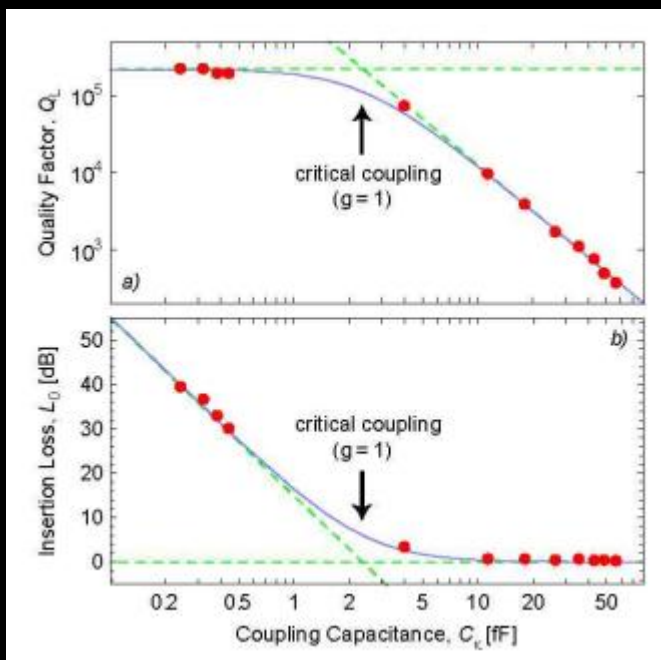
$$k_0 = 0.5 \text{ and } k'_0 = 0.866 \longrightarrow L_l = 402 \text{ nH/m and } C_l = 145 \text{ pF/m} \longrightarrow Z_o = 52.65 \Omega$$

# Example of a resonator design



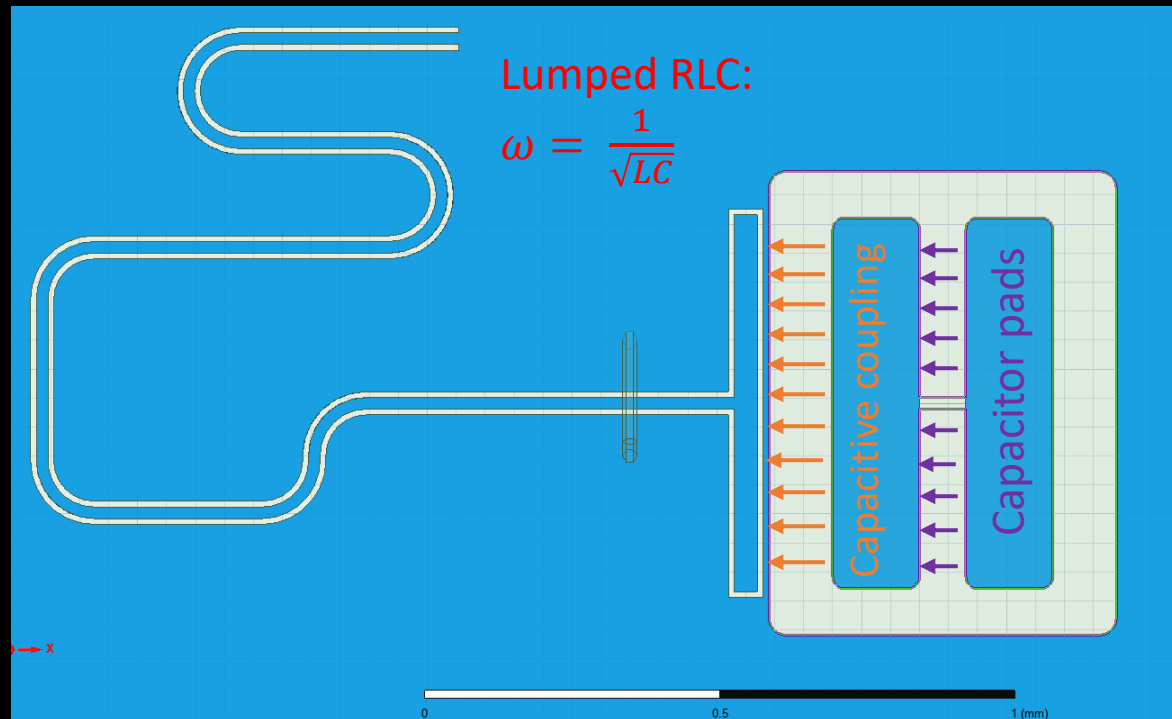
- Middle conductor to gap is 2:1
- Total length corresponds to 6 GHz
- Blue is the metal (Perfect E) and white is silicon.

# Input-output coupling



# More on capacitive coupling

- Capacitive coupling is also important in terms of connecting different circuit elements.



All capacitances are computed with Maxwell 3D including:

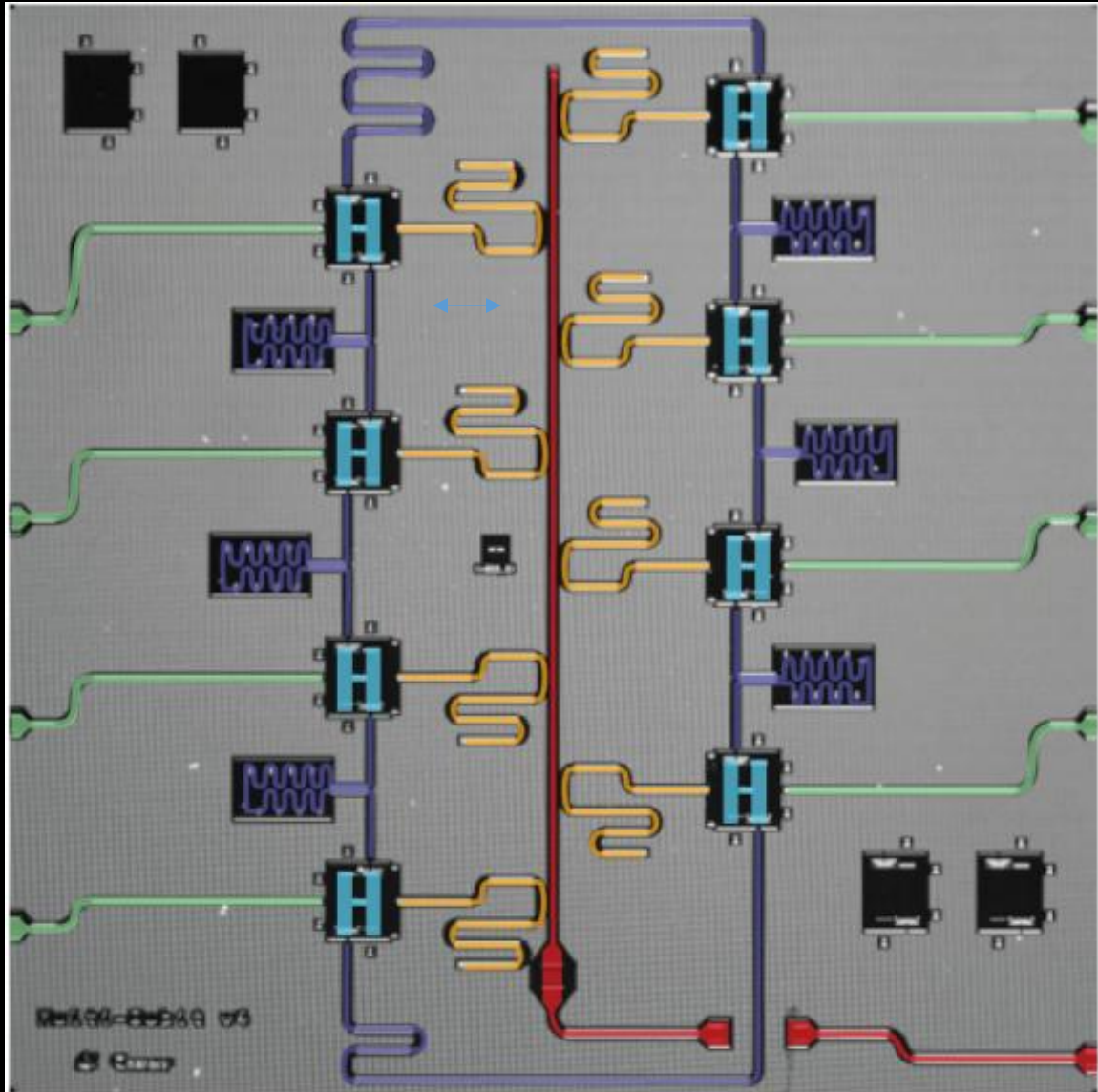
- Capacitor pads
- Qubit-resonator coupling
- Resonator-readout coupling
- Qubit-qubit coupling

Additionally:

The coupling strength can be estimated from the external quality factor of each component on HFSS.



# Complete design workflow



## Full design steps:

- Draw coplanar structures for all resonators and readout lines:
  - Adjust the frequencies based on length
  - Adjust the impedance matching (2:1)
  - Adjust the external Q
- Qubit pads:
  - Optimize the capacitance with Maxwell 3D to get the qubit frequency
  - Reach the desired coupling by optimizing  $Q_e$  and capacitance.
  - Apply lumped RLC  $\sim 12$  nH box to simulate the frequency classically.
    - For accurate frequency and anharmonicity use PyEPR instead.

# Discussion:use cases

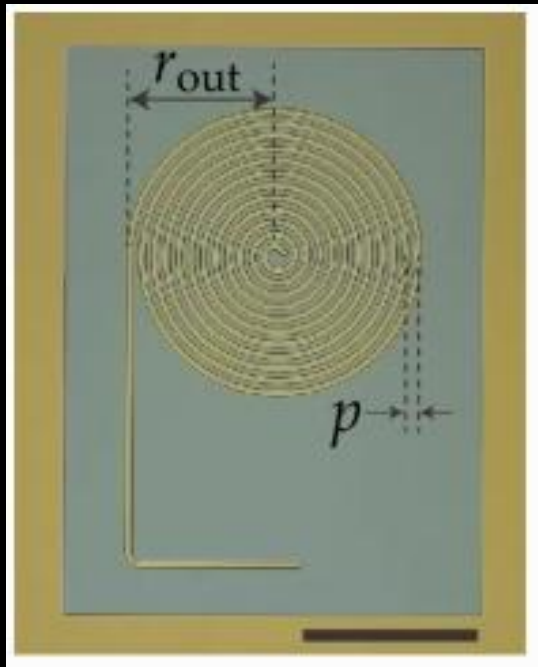
- Algorithm specific design
  - High kinetic inductance
  - Compact fields and resonators
  - Remote entanglement
- 
- All of the above are based on the design principles we discussed.

Thanks

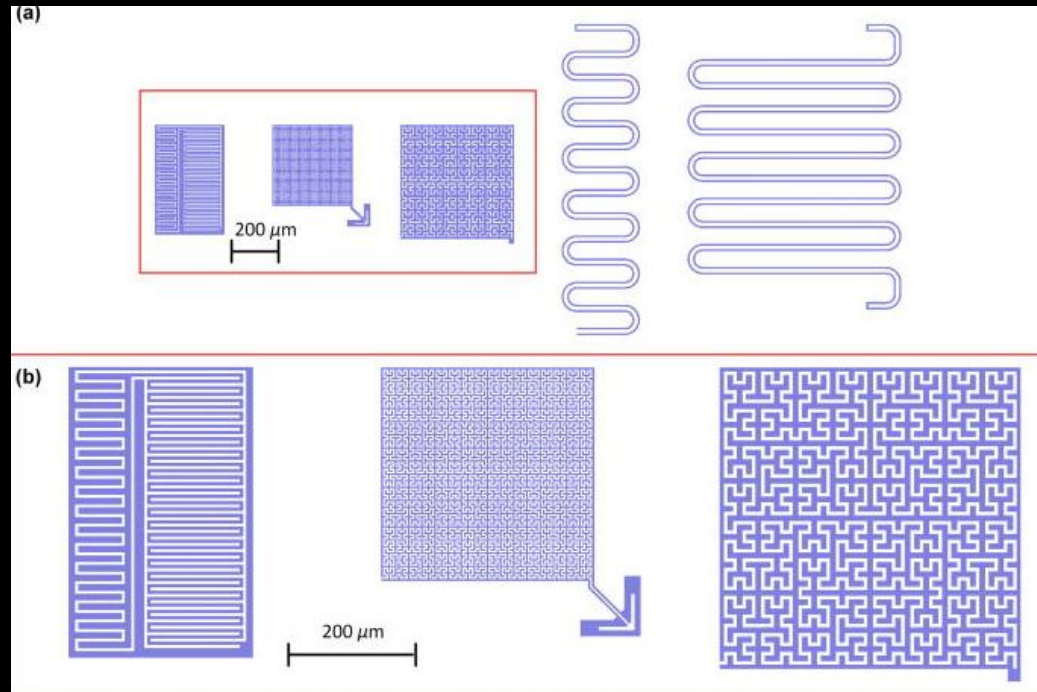
Questions?

# Design geometry and field intensity can also change $Q_i$

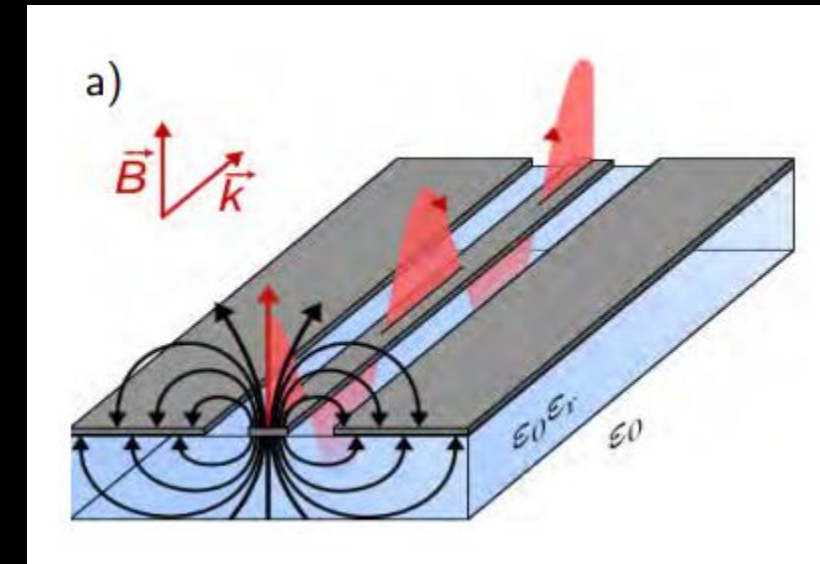
Spiral geometry (10M  $Q_i$ )



Spiral geometry (100K  $Q_i$ )

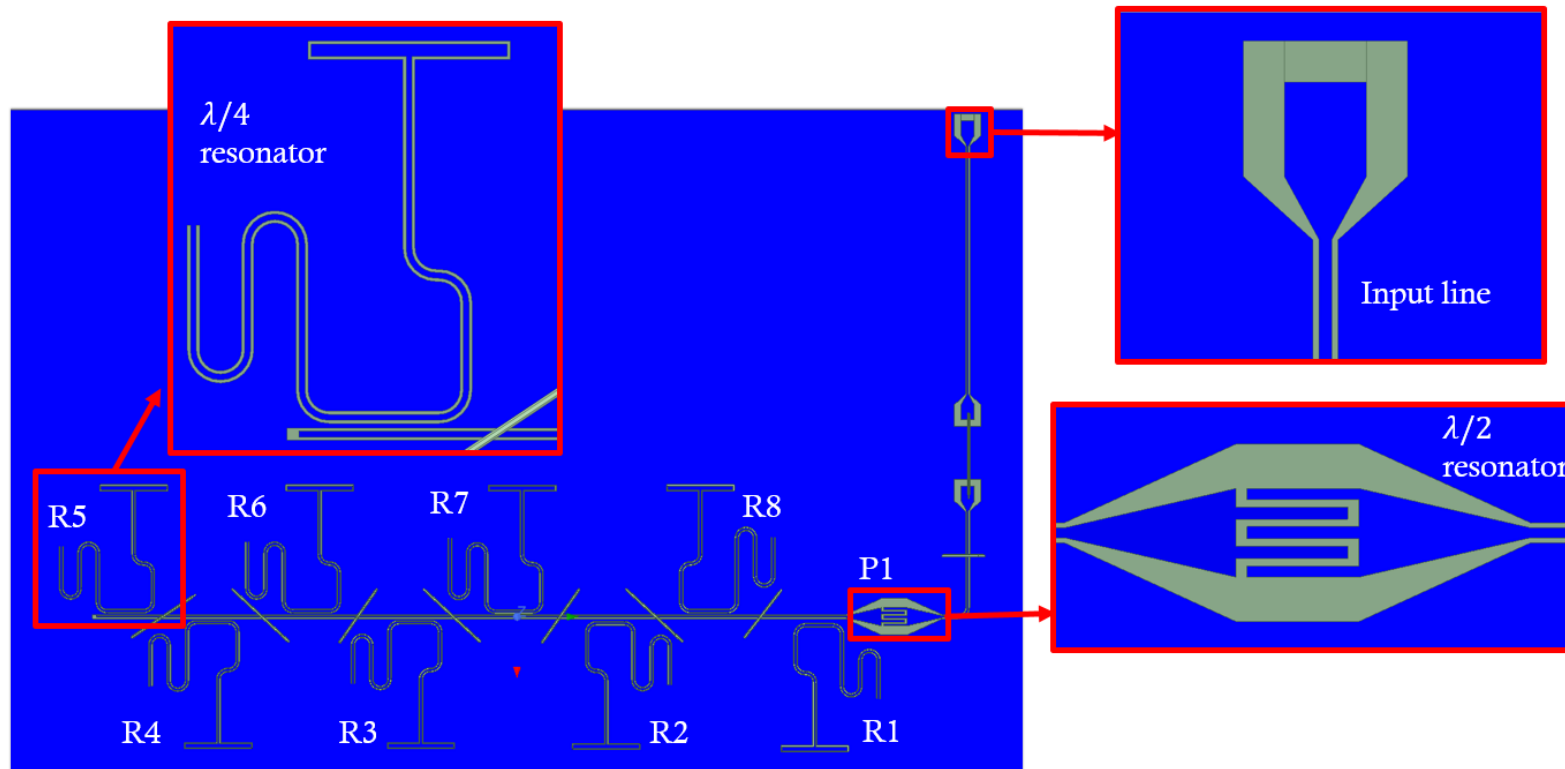


CPW geometry (2-6M  $Q_i$ )



# Example on how to design resonators on HFSS

Mode 2	6.22718 +j 0.000912640	3411.63
Mode 3	6.30231 +j 0.000716784	4396.24
Mode 4	6.37433 +j 0.00120086	2654.07
Mode 5	6.44766 +j 0.000801508	4022.21
Mode 6	6.52060 +j 0.00114187	2855.22
Mode 7	6.59587 +j 0.00273451	1206.04
Mode 8	6.66570 +j 0.00195929	1701.05
Mode 9	6.74680 +j 0.000807601	4177.06
Mode 10	6.85900 +j 0.275826	12.4436



- Blue is the metal of the CPW.
- Green is the substrate.
- The finger capacitors determines the coupling to the measurement instruments.