PHYS213- FORMULA SHEET Term202

Relations

| Relations | | |
|--|---|--|
| $e_{tot} = a\sigma T^4$ | $T\lambda_{max} = 2.898 \times 10^{-3} \text{ m. K}$ | $u(\lambda) = \frac{8\pi h c \lambda^{-5}}{e^{hc/\lambda KT} - 1}$ |
| E = nhf | $K_{max} = \frac{1}{2}mv^2 = eV_s$ $\lambda' - \lambda_o = \frac{h}{m_e c}(1 - \cos\theta)$ | $K_{max} = hf - \phi$ |
| $2d\sin\theta = n\lambda$ | $\lambda' - \lambda_o = \frac{h}{m_e c} (1 - \cos \theta)$ | m = ZIT |
| $F = k \frac{(Z_1 e)(Z_2 e)}{r^2}$ | $U = k \frac{(Z_1 e)(Z_2 e)}{r}$ | $\Delta n = \frac{k^2 Z^2 e^4 N n A}{4R^2 K \sin^4(\varphi/2)}$ |
| $\frac{1}{\lambda} = R\left(\frac{1}{n_f^2} - \frac{1}{n_i^2}\right)$ | $L=m_e v r=n\hbar$ | $\frac{e}{m_e} = \frac{V\theta}{B^2 ld}$ |
| $r_n = \frac{n^2 a_0}{Z}$ | $E_n = -\frac{13.6Z^2}{n^2}$ | $\lambda = \frac{h}{p}$ |
| $v_p = \frac{\omega}{k}$ | $v_g = \frac{d\omega}{dk}$ | $v_g = v_p + k \frac{dv_p}{dk}$ |
| $\Delta x \Delta p_x \ge \frac{\hbar}{2}$ | $\Delta E \Delta t \ge \frac{\hbar}{2}$ | $D\sin\theta = D\frac{y}{L} = \begin{cases} n\lambda\\ (n+0.5)\lambda \end{cases}$ |
| $T = \frac{1}{f} = \frac{2\pi r}{v}$ | $\lambda_{min} = \frac{1.24 \times 10^3}{V} nm$ | qE = qvB |
| $T = \frac{1}{f} = \frac{2\pi t}{v}$ $\int_{-\infty}^{\infty} \psi ^2 dx = 1$ | $P(x) = \int_{a}^{b} \psi ^2 dx$ | $\langle Q \rangle = \int_{-\infty}^{\infty} \psi^* \ Q \ \psi \ dx$ |
| $\psi_n(x) = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right)$ | $E_n = \frac{n^2 \pi^2 \hbar^2}{2mL^2}$ | $\Psi(x,t) = \psi(x)e^{-i\omega t}$ |
| $\psi_n(x,t) = Ae^{i(kx-\omega t)}$ | $\Delta Q = \sqrt{\langle Q^2 \rangle - \langle Q \rangle^2}$ | $[Q]\psi = q\psi$ |
| $[P_x] = \frac{\hbar}{i} \frac{\partial}{\partial x}$ | $[E] = i\hbar \frac{\partial}{\partial t}$ | $[K] = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2}$ |
| $[H] = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} + U(x)$ | $P_x = n \frac{\pi \hbar}{L}$ | $\left \vec{L} \right = \hbar \sqrt{\ell (\ell + 1)}$ |
| $L_z=m_\ell\hbar$ | $P(r) = r^2 \big R_{n,\ell}(r) \big ^2$ | $\langle r \rangle = \int_0^\infty r P(r) \ dr$ |

$$E_n = \left(n + \frac{1}{2}\right)\hbar\omega$$

$$T(E) = \left\{1 + \frac{1}{4} \left[\frac{U^2}{E(U - E)} \right] \sinh^2(\alpha L) \right\}^{-1} \qquad \alpha = \frac{\sqrt{2m(U - E)}}{\hbar}$$

$$T(E) = \left\{1 + \frac{1}{4} \left[\frac{E^2}{U(E-u)} \right] \sin^2(\alpha' L) \right\}^{-1} \qquad \alpha' = \frac{\sqrt{2m(E-U)}}{\hbar}$$

$$-\frac{\hbar^2}{2m}\frac{\partial^2 \Psi(x,t)}{\partial x^2} + U(x)\Psi(x,t) = i\hbar \frac{\partial \Psi(x,t)}{\partial t}$$

$$\int_0^\infty x^n e^{-x} dx = n! \qquad \qquad \int_0^\infty z^2 e^{-az^2} dz = \frac{1}{4a} \sqrt{\frac{\pi}{a}} , \ a > 0$$

$$E_{n_1,n_2,n_3} = \frac{\pi^2 \hbar^2}{2m} \left(\frac{n_1^2}{L_1^2} + \frac{n_2^2}{L_2^2} + \frac{n_3^2}{L_3^2} \right)$$

$$\Psi(r,\theta,\phi,t) = R_{n,\ell}(r) Y_{\ell}^{m_{\ell}}(\theta,\phi) e^{-i\omega t}$$

Constants:

| $e = 1.6 \times 10^{-19} $ C | $m_e = 9.11 \times 10^{-31} \text{kg}$ | $h = 6.626 \times 10^{-34} \text{ J.s}, \hbar = h/2\pi$ |
|----------------------------------|---|--|
| $c = 3 \times 10^8 \text{ m/s}$ | $m_p = 1.67 \times 10^{-27} \text{kg}$ | $k = 9 \times 10^9 \text{ N.m}^2/\text{C}^2$ |
| hc = 1240 eV.nm | $R = 1.0973 \times 10^7 \text{ m}^{-1}$ | $\sigma = 5.67 \times 10^{-8} \mathrm{W.m^{-2}.K^{-4}}$ |
| $\lambda_c = 0.00243 \text{ nm}$ | $a_0 = 0.0529 \text{ nm}$ | $k_B = 1.38 \times 10^{-23} \text{ J/K}$ |