

I first define the terms in Eq. A13 and Eq. A14 which are also in Eq. A16, as well.

$$term\_1 := \frac{x \theta^2}{(x\_0 \cdot \text{HankelH1}(2, x\_0) + \text{HankelH1}(1, x\_0))};$$

$$\frac{x \theta^2}{x\_0 \text{HankelH1}(2, x\_0) + \text{HankelH1}(1, x\_0)} \quad (1)$$

$$term\_2 := \frac{x \theta}{\text{HankelH1}(1, x\_0)};$$

$$\frac{x \theta}{\text{HankelH1}(1, x\_0)} \quad (2)$$

Then I define the terms other than term\_1 and term\_2 and integrate them as they are in Eq. A12.

$$const := \frac{B\_0}{2 \cdot x} \cdot \sin(a) \cdot \exp(I \cdot (x + etha));$$

$$\frac{1}{2} \frac{B\_0 \sin(a) e^{I(x + etha)}}{x} \quad (3)$$

$$B\_theta := I \cdot const \cdot (term\_1 - term\_2) \cdot \cos(a);$$

$$\frac{1}{x} \left( \frac{1}{2} I B\_0 \sin(a) e^{I(x + etha)} \left( \frac{x \theta^2}{x\_0 \text{HankelH1}(2, x\_0) + \text{HankelH1}(1, x\_0)} - \frac{x \theta}{\text{HankelH1}(1, x\_0)} \right) \cos(a) \right) \quad (4)$$

$$B\_phi := -const \cdot (term\_1 \cdot \cos(2 \cdot a) - term\_2);$$

$$- \frac{1}{2} \frac{1}{x} \left( B\_0 \sin(a) e^{I(x + etha)} \left( \frac{x \theta^2 \cos(2 a)}{x\_0 \text{HankelH1}(2, x\_0) + \text{HankelH1}(1, x\_0)} - \frac{x \theta}{\text{HankelH1}(1, x\_0)} \right) \right) \quad (5)$$

$$const2 := \frac{eps\_0 \cdot c^4 \cdot x^2}{w^2};$$

$$\frac{eps\_0 c^4 x^2}{w^2} \quad (6)$$

$$In \cdot w \cdot wdot = const2 \cdot 2 \cdot \text{Pi} \cdot \int ( (B\_theta^2 + B\_phi^2) \cdot \sin(a), a = 0 .. \text{Pi} )$$

(I haven't execute the line above because it turns into a weird formula with all of the constants etc. It is written below, part by part.)

Then, without the constants, the integral turns into this form:

$$term := (t1 \cos(2 a) - t2)^2 + (t1 - t2)^2 \cos(a)^2;$$

$$(t1 \cos(2 a) - t2)^2 + (t1 - t2)^2 \cos(a)^2 \quad (7)$$

$$term3 := term \cdot \sin(a);$$

$$((t1 \cos(2 a) - t2)^2 + (t1 - t2)^2 \cos(a)^2) \sin(a) \quad (8)$$

$int(c \cdot term3, a = 0 .. \pi);$

$$\frac{8}{15} c (3 t^2 + 5 t^2) \quad (9)$$

Since  $t^2$  is a higher order term, we can neglect it. Then, our equation would become:

$$In \cdot w \cdot wdot = \frac{4 \cdot \pi \cdot B \cdot \theta^2 \cdot r \cdot \theta^6 \cdot w^4 \sin(a)^2}{\mu_0 \cdot c^3} \cdot \frac{1}{x \cdot \theta^6} \left( \frac{1}{3} term_1 + \frac{1}{5} term_2 \right); \quad (10)$$

$In w wdot$

$$= \frac{1}{\mu_0 c^3 x \cdot \theta^6} \left( 4 \pi B \cdot \theta^2 r \cdot \theta^6 w^4 \sin(a)^2 \left( \frac{1}{3} 1 / (x \cdot \theta \text{HankelH1}(2, x \cdot \theta) \right. \right. \\ \left. \left. + \text{HankelH1}(1, x \cdot \theta) x \cdot \theta^2 + \frac{1}{5} \frac{x \cdot \theta}{\text{HankelH1}(1, x \cdot \theta)} \right) \right)$$

Here the problem comes: in the paper (Melatos '97) the part with Hankel functions in paranthesis with the denominator  $1/x \cdot \theta^6$  turns into a polynomial statement as:

$$\frac{1}{x \cdot \theta^6} \cdot \left[ \frac{1}{3 \cdot (x \cdot \theta^2 + 1)} + \frac{x \cdot \theta^4}{5 \cdot (x \cdot \theta^6 - 3 \cdot x \cdot \theta^4 + 36)} \right]$$