

ii).

Area is given by

$$\begin{aligned} \left| \int_{-1}^1 x^2 \right| + \left| \int_{-1}^1 -x^2 \right| &= 2 \left| \int_{-1}^1 x^2 \right| \\ &= 2 \left(\frac{1}{3} - \frac{-1}{3} \right) \\ &= \frac{4}{3} \end{aligned}$$

iv).

First, note that $f(x)$ intersects $h(x)$ at $x = -\sqrt{2}, \sqrt{2}$, $g(x)$ intersects $f(x)$ at $\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$, and the x axis at $-1, 1$. Given this, the area is given by:

$$\begin{aligned} &= \int_{-\sqrt{2}}^{\sqrt{2}} 2 - \int_{-\sqrt{2}}^{\sqrt{2}} x^2 - \int_{-1}^1 1 - x^2 + \left(\int_{\frac{-1}{\sqrt{2}}}^{\frac{1}{\sqrt{2}}} x^2 + 2 \int_1^{\sqrt{2}} 1 - x^2 \right) \\ &= \frac{8\sqrt{2}}{3} - 2 + \frac{2}{3} + \frac{1}{3\sqrt{2}} + 2\sqrt{2} - 1 - \frac{4\sqrt{2}}{3} + \frac{2}{3} \\ &= \frac{7}{\sqrt{2}} - \frac{8}{3} \end{aligned}$$

vi).

Know \sqrt{x} is x^2 "rotated" ninety degrees, and know it intersects with the vertical line at $y = \sqrt{2}$. So, really, this is same as finding:

$$\begin{aligned} \int_0^{\sqrt{2}} 2 - \int_0^{\sqrt{2}} x^2 &= 2\sqrt{2} - \frac{2\sqrt{2}}{3} \\ &= \frac{4\sqrt{2}}{3} \end{aligned}$$