# Estimating Interrater Reliability from Planned-Missing Data

## Demonstration of the ICC4IRR application

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**Contributors**

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**ICC4IRR Application**

https://tasospsy.shinyapps.io/icc4irr_app/

**Example Data**

https://github.com/icc4irr/app/blob/main/sample-data/Example_ratings_EARLI2025.csv

# Motivating example: Teaching Quality

Education researchers use **observation instruments** to evaluate teaching quality

Example: **Educational inspectors** *(raters)* evaluate **teaching skills** *(attribute)* of **teachers** *(subjects)*

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Such ratings are used in **practice** and in **research**

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Such ratings are used in **practice** and in **research**

**In practice** to make decision
about teachers or schools.

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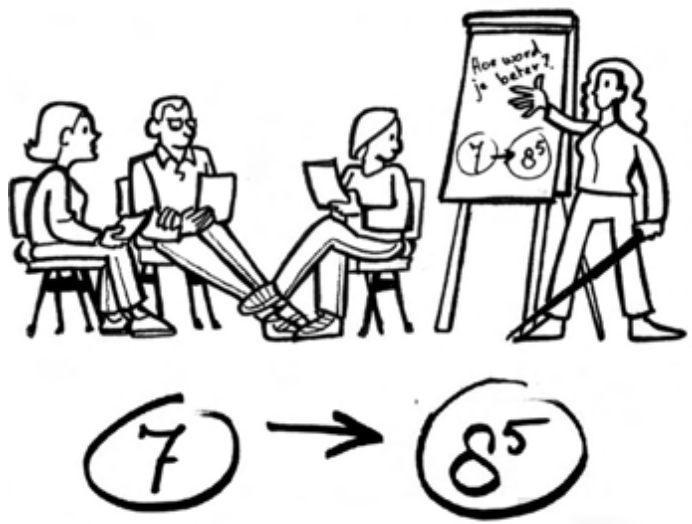
Such ratings are used in **practice** and in **research**

**In practice** to make decision about teachers or schools.


**In research** to study differences across teachers or schools.
For example in intervention studies.



# Motivating example: Teaching Quality

**Important** that (the variation in) observed scores originate in differences across teachers or schools, and as little as possible in rater effects.

| **Use of scores** | **Problems due to rater effects (noise)** |
|---|---|
| Regression techniques | **(Attenuation) Bias and loss of precision** |
| Decisions about individuals | **Incorrect decisions** |

$\rightarrow$ Important to investigate the **interrater reliability** (IRR).

# Intraclass correlation coefficients

## Intraclass correlation coefficients (ICCs) for Interrater reliability (IRR)

To which degree can we differentiate between subjects, hence generalize subject scores over raters?

(Bartko, 1966; McGraw & Wong, 1996; Shrout & Fleiss, 1979)

- Applicable to quantitative data
- Rooted in Generalizability theory (Cronbach et al., 1963)
- Coefficients for absolute and relative decision making
- Available for $\geq 2$ raters

# Intraclass correlation coefficients

Psychological Methods
1996, Vol. 1, No. 1, 30–46


1082-989X/96/$3.00

## Forming Inferences About Some Intraclass Correlation Coefficients

Kenneth O. McGraw
University of Mississippi

S. P. Wong
University of Memphis

Although intraclass correlation coefficients (ICCs) are commonly used in behavioral measurement, psychometrics, and behavioral genetics, procedures

## ıtions: Uses in Assessing Rater Reliability

Patrick E. Shrout and Joseph L. Fleiss
Division of Biostatistics
Columbia University, School of Public Health

Reliability coefficients often take the form of intraclass correlation coefficients. In this article, guidelines are given for choosing among six different forms of the intraclass correlation for reliability studies in which $n$ targets are rated by $k$ judges. Relevant to the choice of the coefficient are the appropriate statistical model for the reliability study and the applications to be made of the reliability results. Confidence intervals for each of the forms are reviewed.

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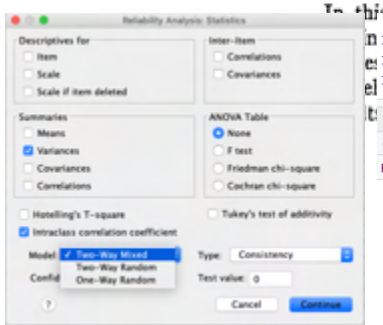


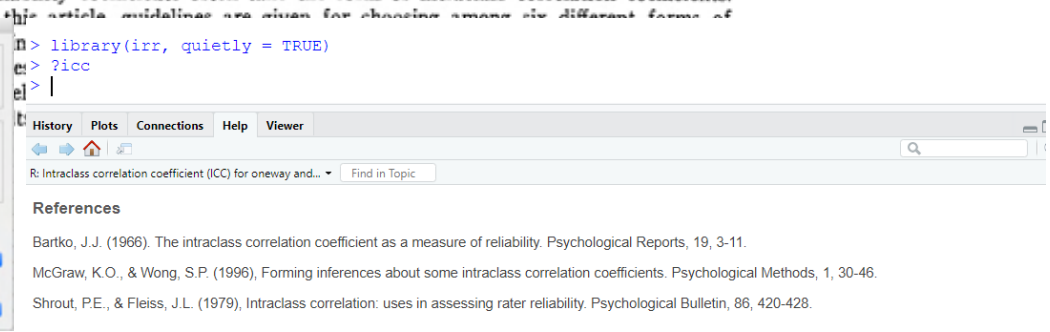

## Two-Way Data

- Each subject is assessed by the same $k \geq 2$ raters.

| Subject | Rater | | |
|---|---|---|---|
| | 1 | 2 | 3 |
| 1 | $y_{11}$ | $y_{12}$ | $y_{13}$ |
| 2 | $y_{21}$ | $y_{22}$ | $y_{23}$ |
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$$\sigma_y^2 = \sigma_s^2 + \sigma_r^2 + \sigma_{sr.e}^2$$

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## Interrater Consistency

$$ICC(C,k) = \frac{\sigma_s^2}{\sigma_s^2 + \frac{\sigma_{sr.e}^2}{k}}$$

# Practice: Planned-Missing Data

## Complete data

- ICC definitions *and* estimation methods require complete data

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## Incomplete data

- Most educational studies use a planned-missing design. For example:

| Teacher | Educational Inspector | | |
|---|---|---|---|
| | 1 | 2 | 3 |
| 1 | $y_{11}$ | $y_{12}$ | – |
| 2 | $y_{21}$ | – | $y_{23}$ |
| 3 | – | $y_{32}$ | $y_{33}$ |
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# ICCs for planned-missing data

Ten Hove, Jorgensen and Van der Ark (2024). Updated Guidelines on Selecting ICCs for IRR.

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$$ICC(A,k) = \frac{\sigma_s^2}{\sigma_s^2 + \frac{\sigma_r^2 + \sigma_{sr}^2}{k}}$$

Account for unbalanced number of raters:

$$ICC(A,\hat{k}) = \frac{\sigma_s^2}{\sigma_s^2 + \frac{\sigma_r^2 + \sigma_{sr}^2}{\hat{k}}}$$

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## Interrater Consistency

$$ICC(C,k) = \frac{\sigma_s^2}{\sigma_s^2 + \frac{\sigma_{sr}^2}{k}}$$

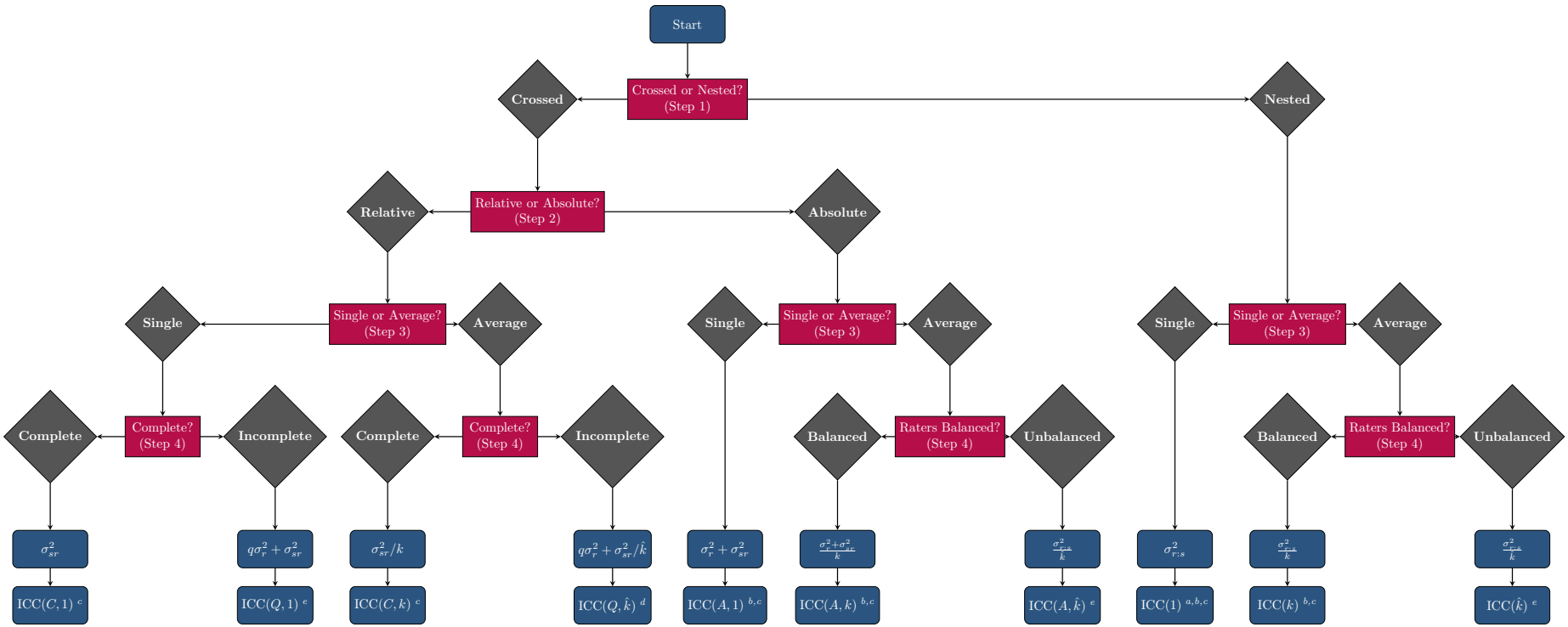
Account for partial non-overlapping raters:

$$ICC(Q,\hat{k}) = \frac{\sigma_s^2}{\sigma_s^2 + q * \sigma_r^2 + \frac{\sigma_{sr}^2}{\hat{k}}}$$

$$\hat{k} = \left(\frac{k_1^{-1} + k_2^{-1} + \ldots + k_l^{-1}}{N_s}\right)^{-1}; q = \frac{1}{\hat{k}} - \frac{\sum_i \sum_{i'} \frac{k_{i,i'}}{k_i k_{i'}}}{N_s(N_s - 1)}$$

# Overview ICC Selection

See: Ten Hove, Jorgensen and Van der Ark (2024). Updated Guidelines on Selecting an ICC for IRR.



# Estimating ICCs from Planned-Missing Data

## Compared three estimation methods for ICCs:

- **MCMC**: Markov chain Monte Carlo Estimation of hierarchical models (LoPilato et al., 2015; Ten Hove et al., 2020, 2021)
- **MLE-R**: Maximum likelihood estimation of **R**andom effects models (Marcoulides, 1990; cf. Jiang, 2018; Ten Hove et al., 2021)
- **MLE-CF**: Maximum likelihood estimation of **C**ommon-**F**actor models (Jorgensen, 2021; Marcoulides, 1996; Vispoel et al., 2018a, 2019))

For various design factors (e.g., $K, N, \hat{k}, \sigma^2$)

## Based on (*among other things*):

- Computational accuracy
- 95% (B)CI coverage rates

SCAN ME

# Estimating ICCs from Planned-Missing Data

## AND what if..

A different observational design were used?

## Examples of Planned Missing Designs

(1) **Random** Rater Assignment

| Subject | Rater | | | |
|---|---|---|---|---|
| | 1 | 2 | 3 | 4 |
| 1 | x | | x | |
| 2 | | x | x | |
| 3 | | | x | x |
| 4 | x | x | | |
| 5 | x | | | x |
| 6 | | x | x | |

(2) **Anker** Rater

| Subject | Rater | | | |
|---|---|---|---|---|
| | 1 | 2 | 3 | 4 |
| 1 | x | x | | |
| 2 | x | | x | |
| 3 | x | | | x |
| 4 | x | x | | |
| 5 | x | | x | |
| 6 | x | | | x |

(3) **Blocks** of Raters

| Subject | Rater | | | |
|---|---|---|---|---|
| | 1 | 2 | 3 | 4 |
| 1 | x | x | | |
| 2 | x | x | | |
| 3 | x | x | | |
| 4 | | | x | x |
| 5 | | | x | x |
| 6 | | | x | x |

# Conclusions

- **Simulation 1: MLE of random effects models** useful for estimating ICCs for IRR from typical observational studies
  - *Also* most **User-friendly** because it converges in most conditions and only takes seconds.
- **Simulation 2:** Type of (planned missing) design does not matter much with respect to (SE) bias and coverage of ICCs

Conclusion: **MLE of random effects models** very useful for (interrater)reliability studies.

# Current Work: ICC4IRR application

- **Under Development**: Shiny app to estimate ICCs for IRR

  Psychogiopoulos, Koopman & Ten Hove (2025)

- **In progress**: Tutorial and guidance in planning rater studies

# ICC4IRR application


## ABOUT THIS APP

ICC4IRR is a shiny application to estimate interrater reliability (IRR) from quantitative planned incomplete data, resulting from observation studies in which raters (partly) vary across subjects.

AUTHORS:

Tasos Psychogyiopoulos, Letty Koopman and Debby ten Hove

CONTACT:

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CITE AS:

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ADDITIONAL REFERENCES

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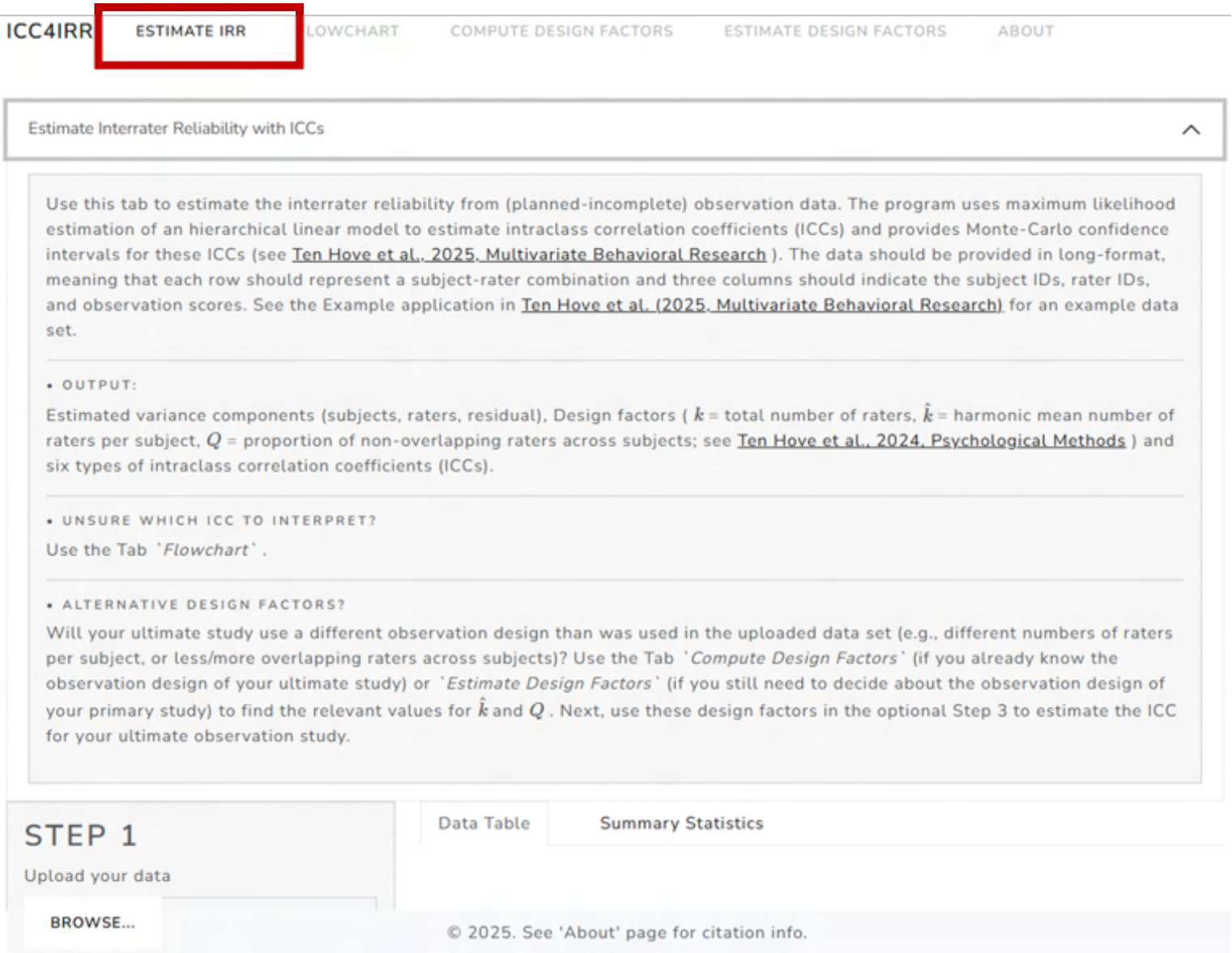

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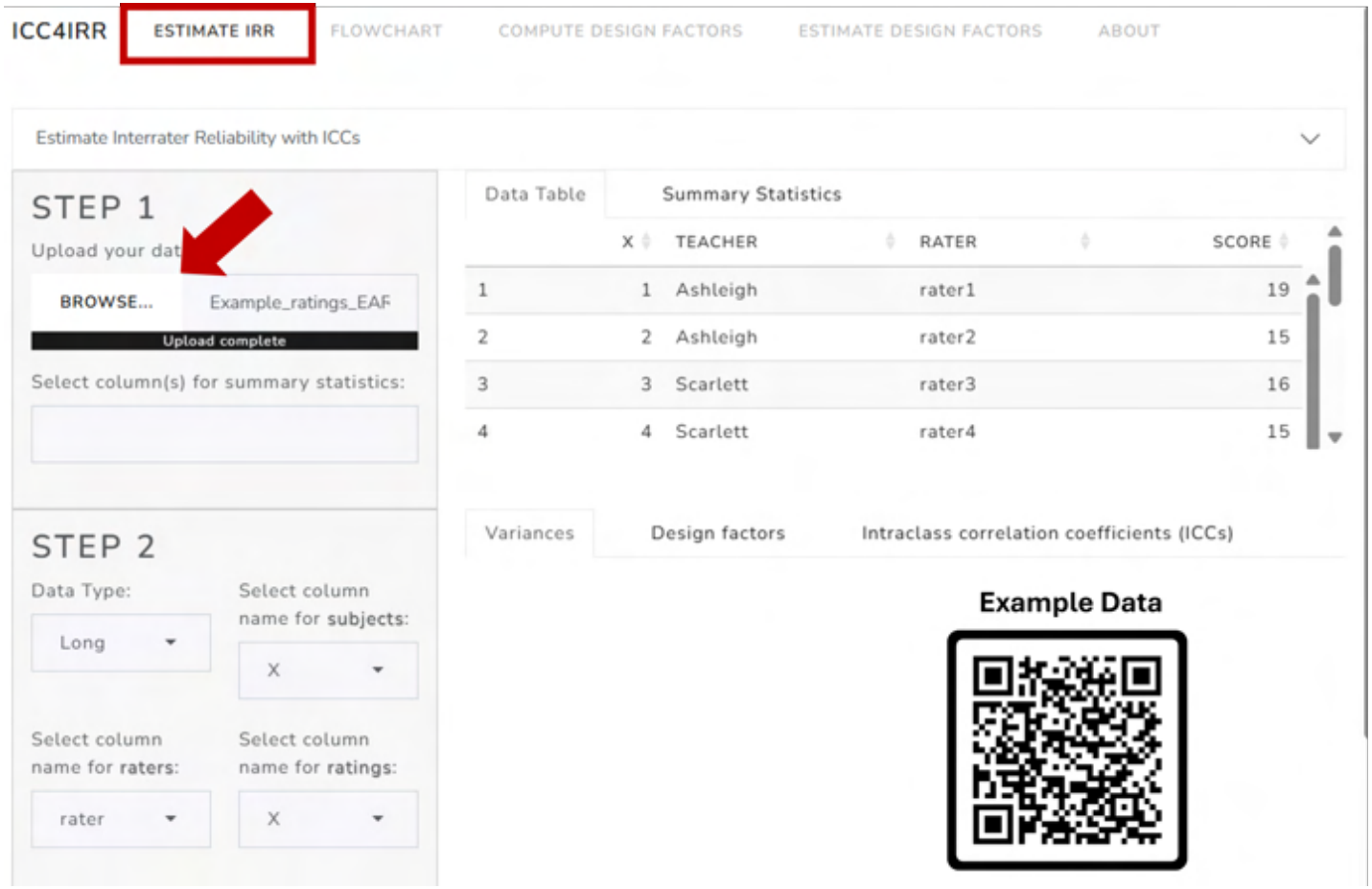

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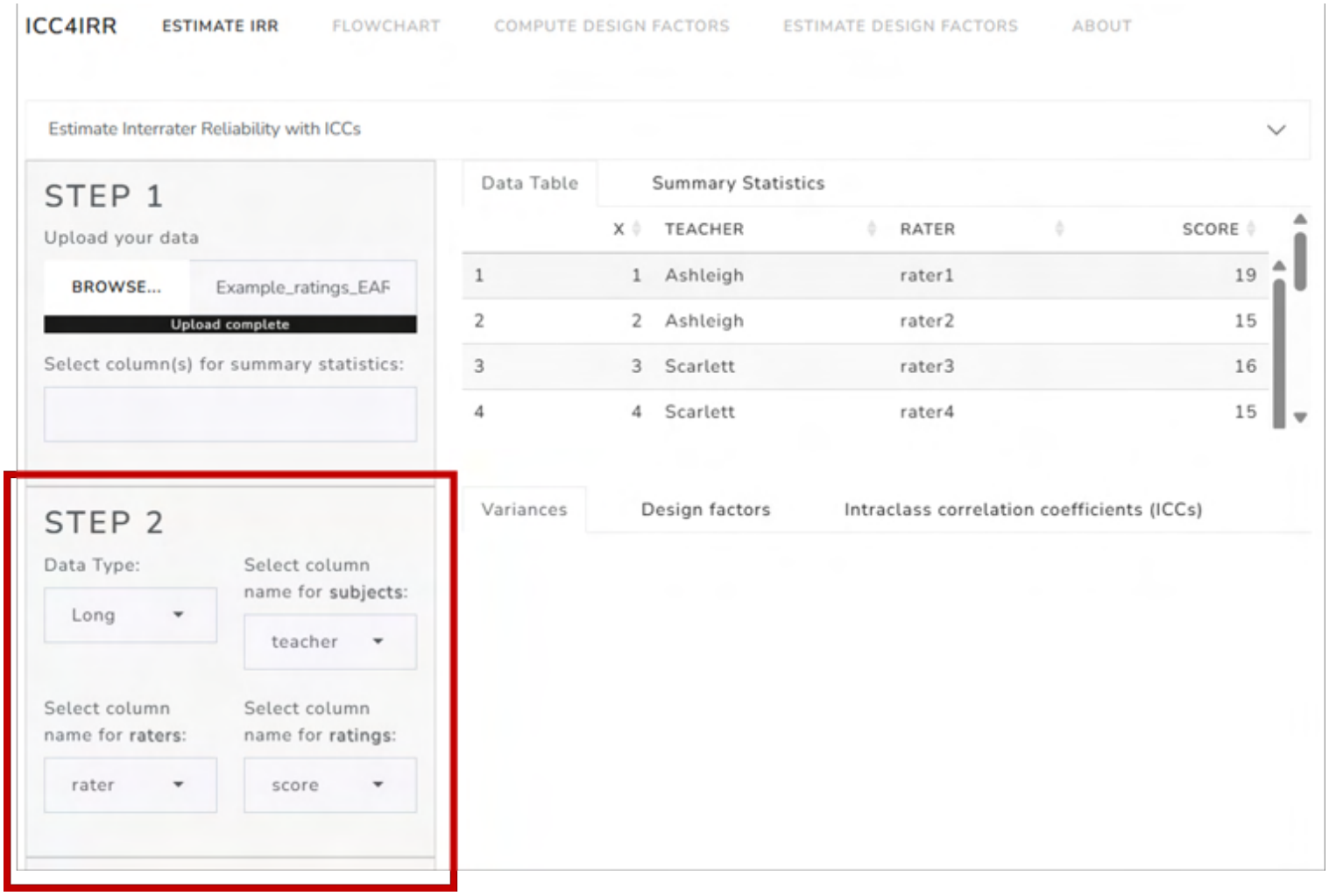

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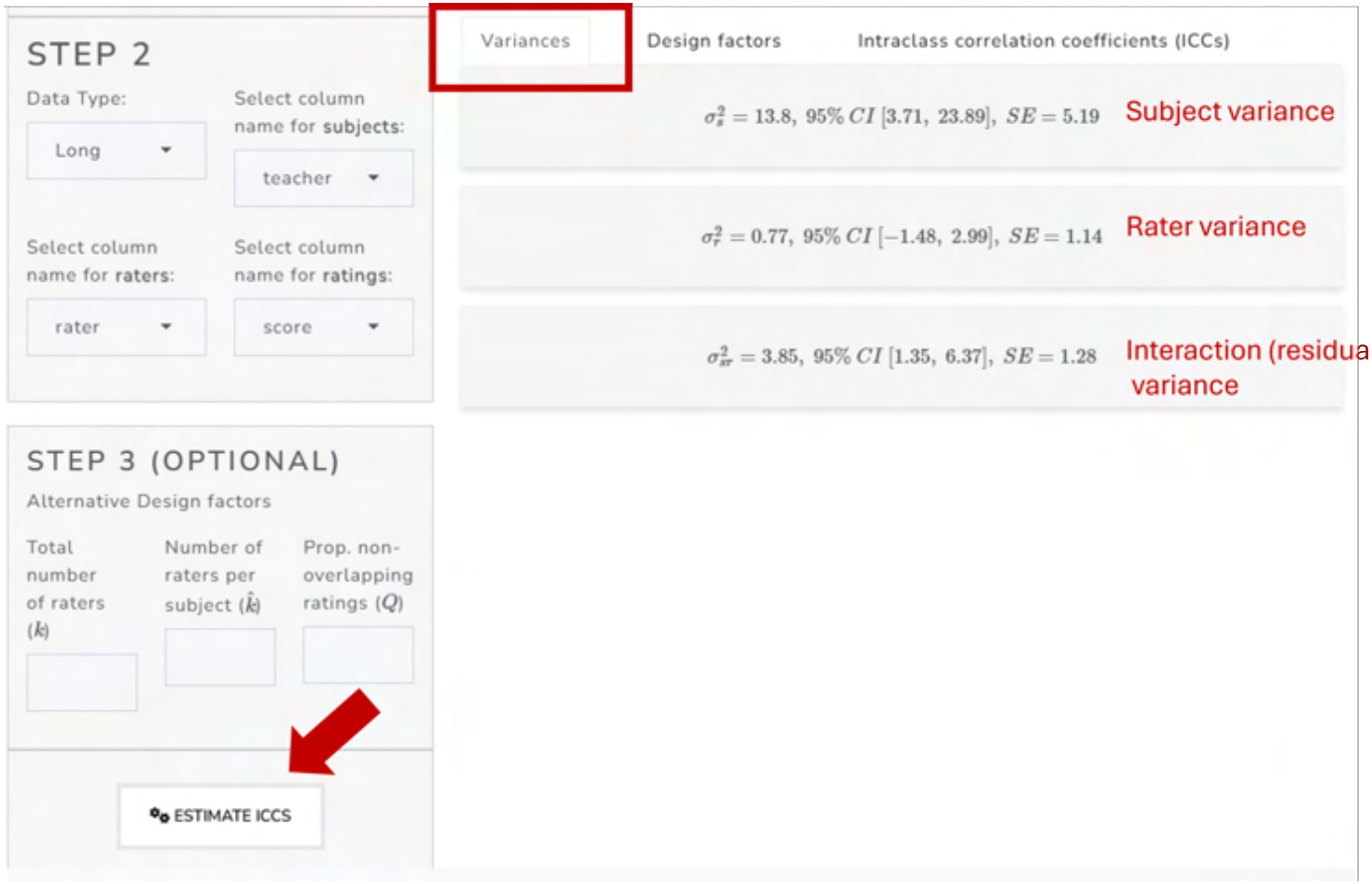

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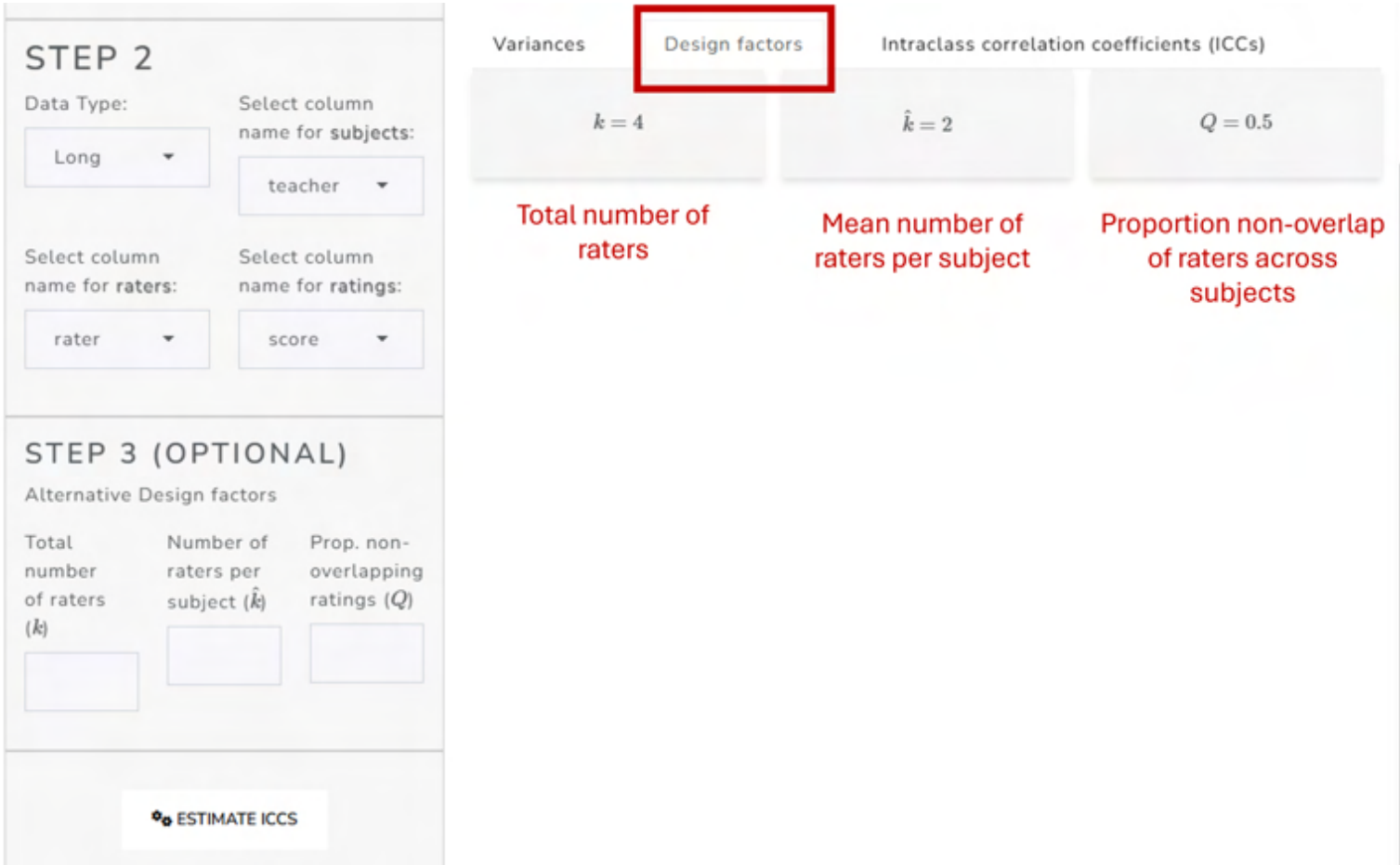

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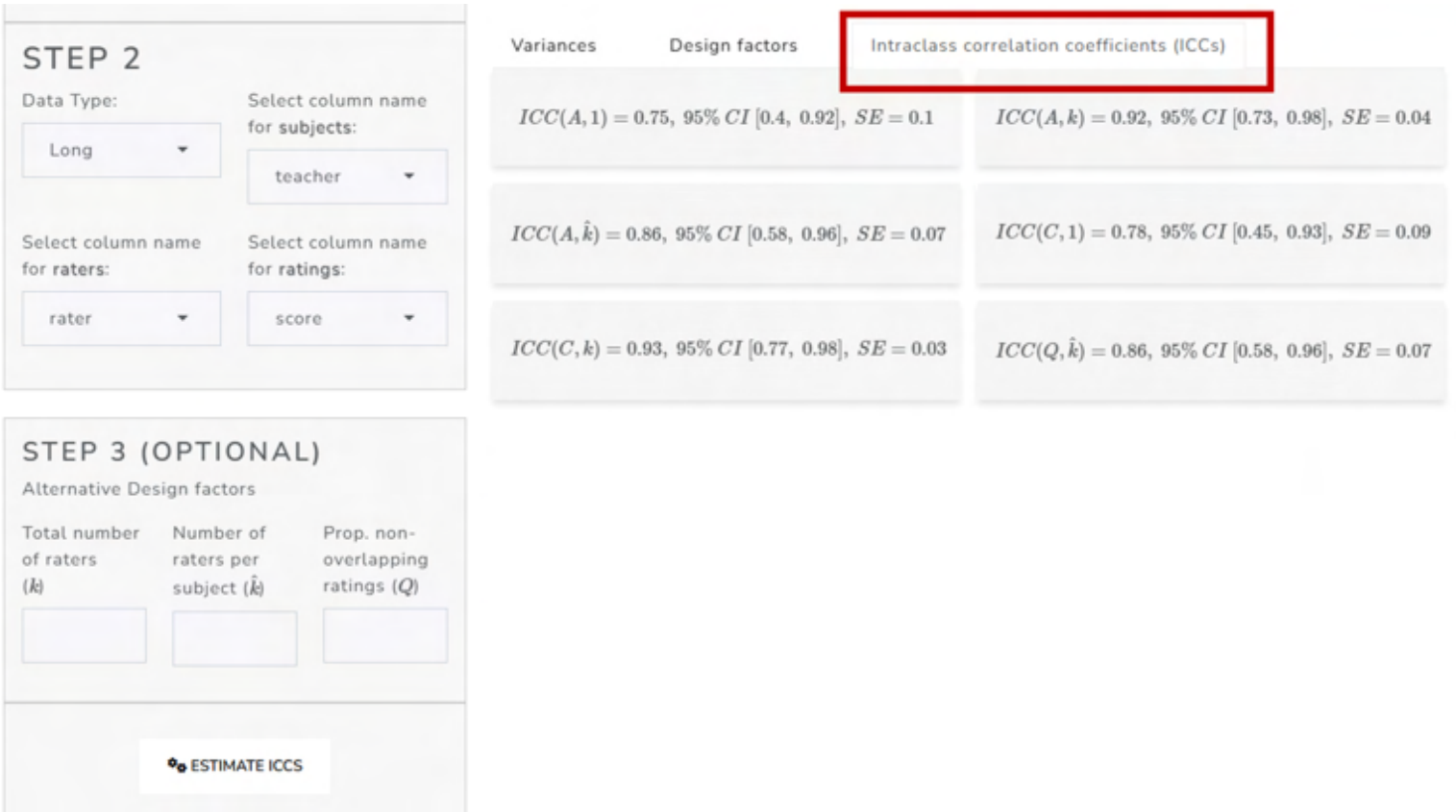

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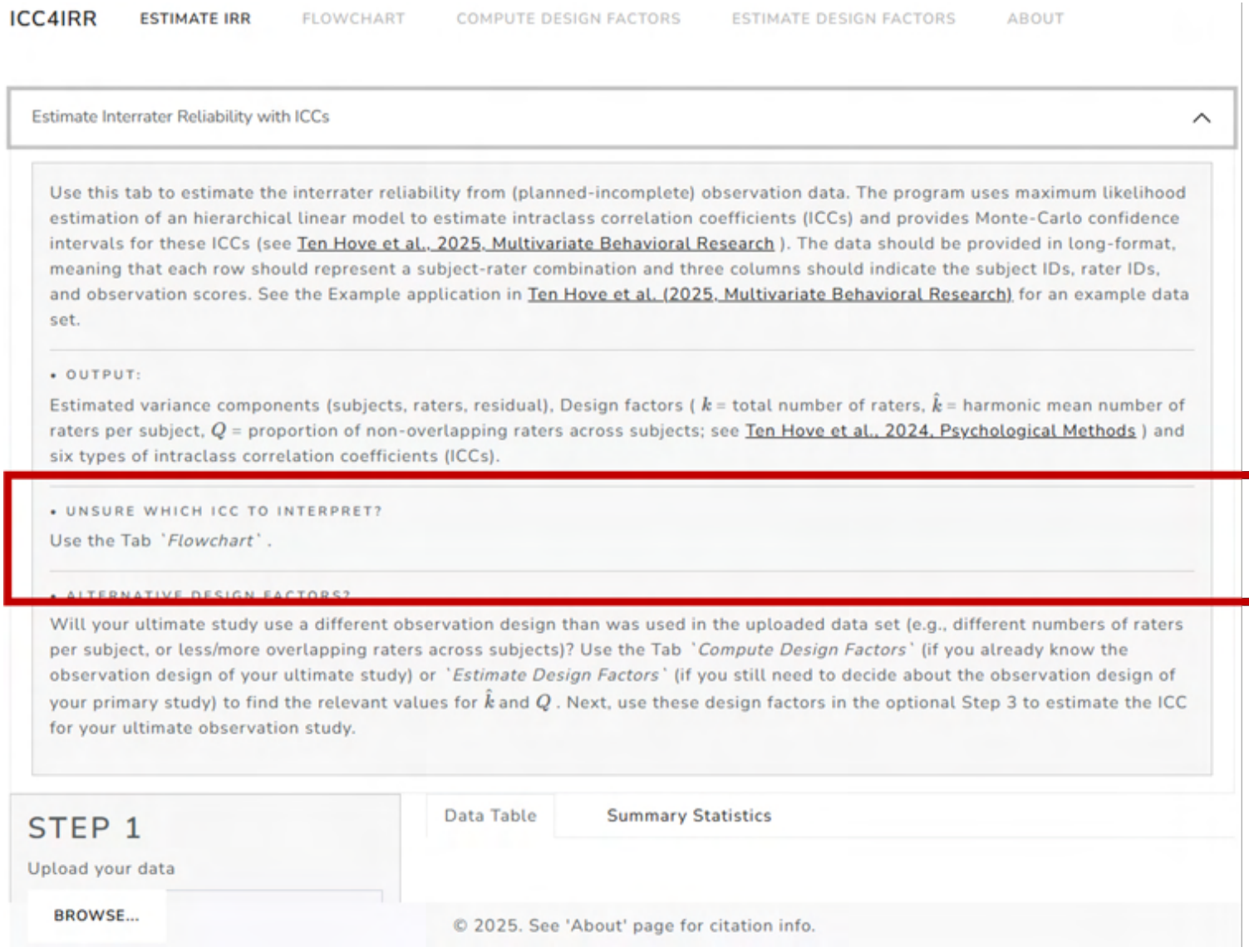

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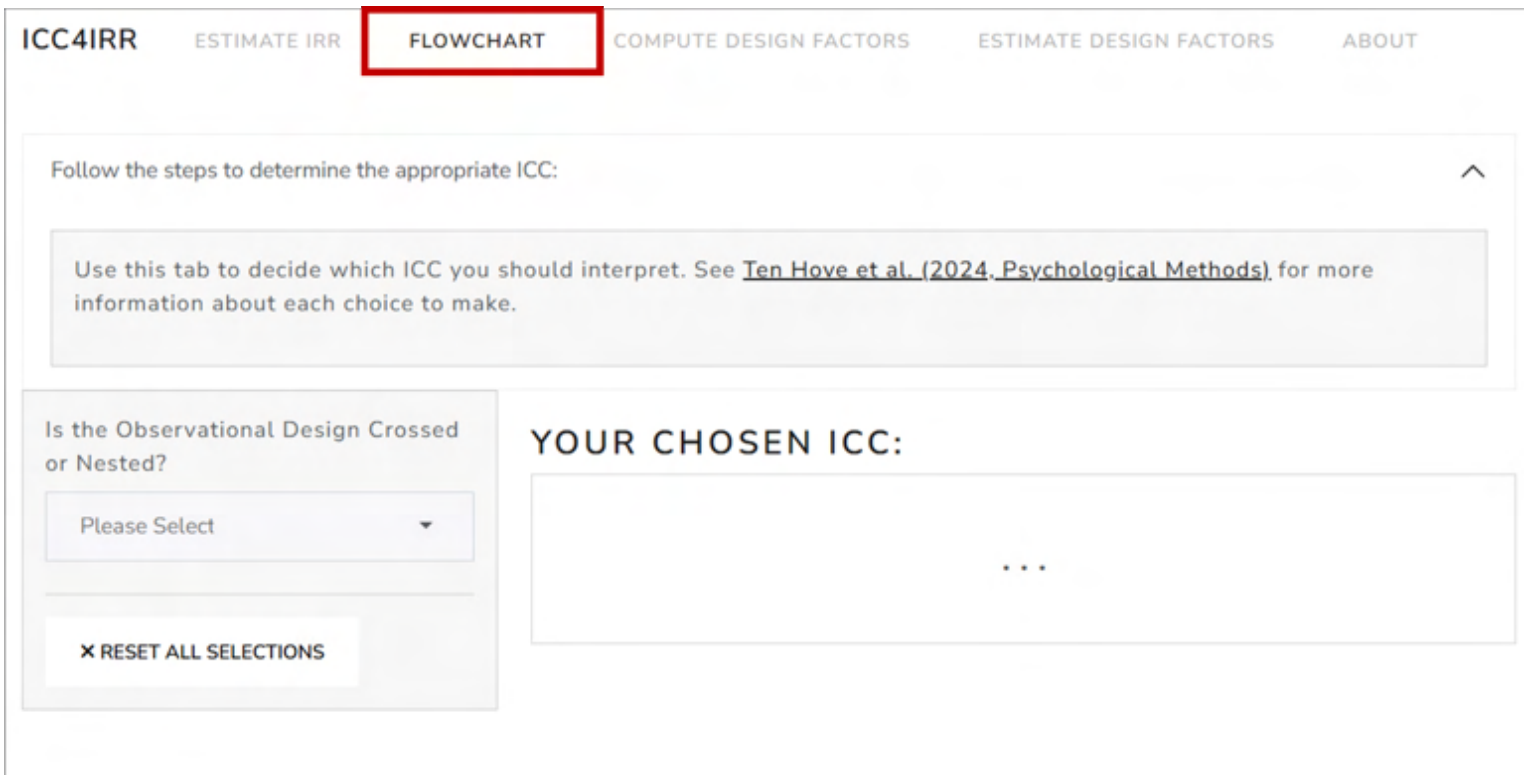

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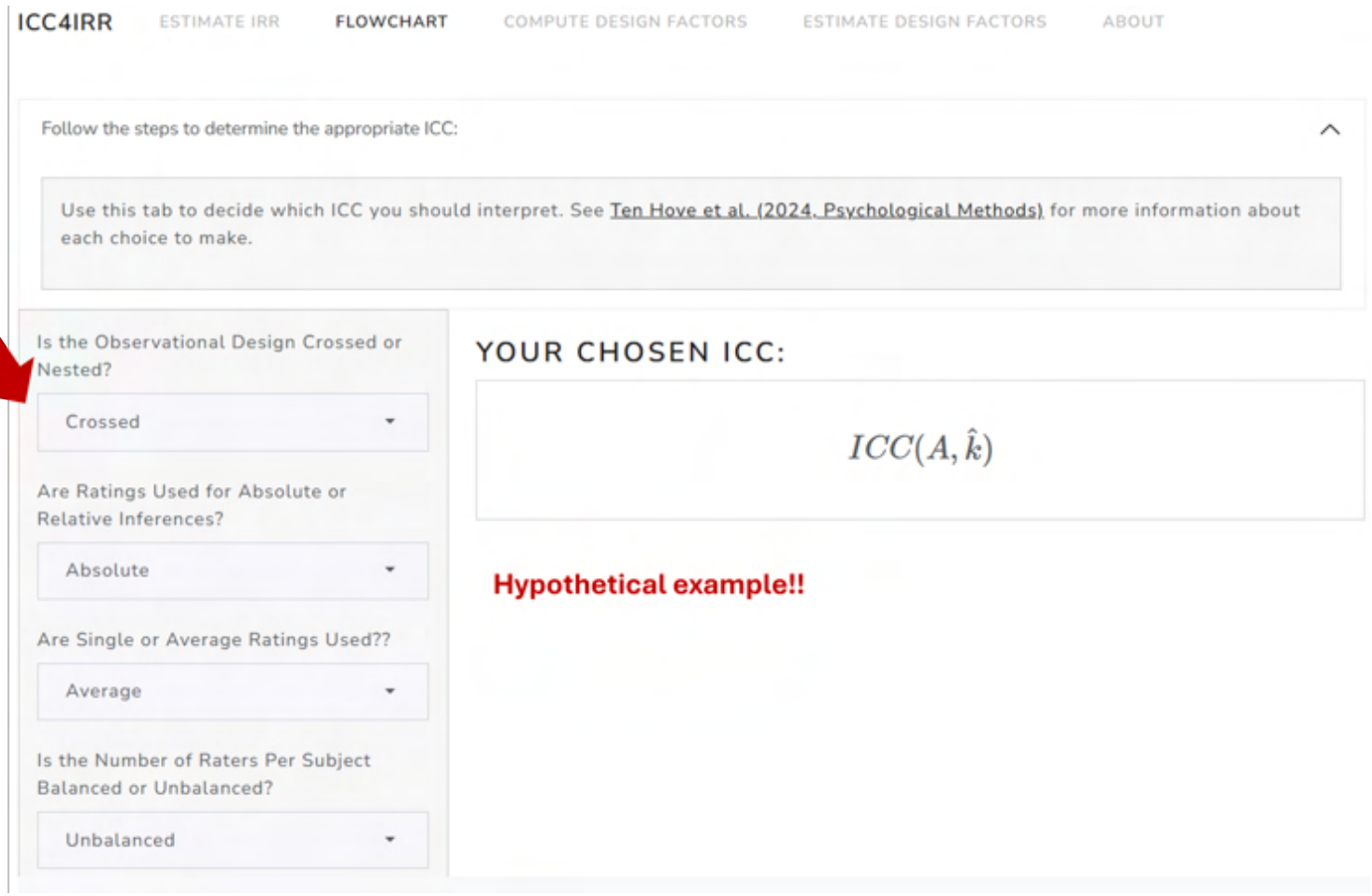

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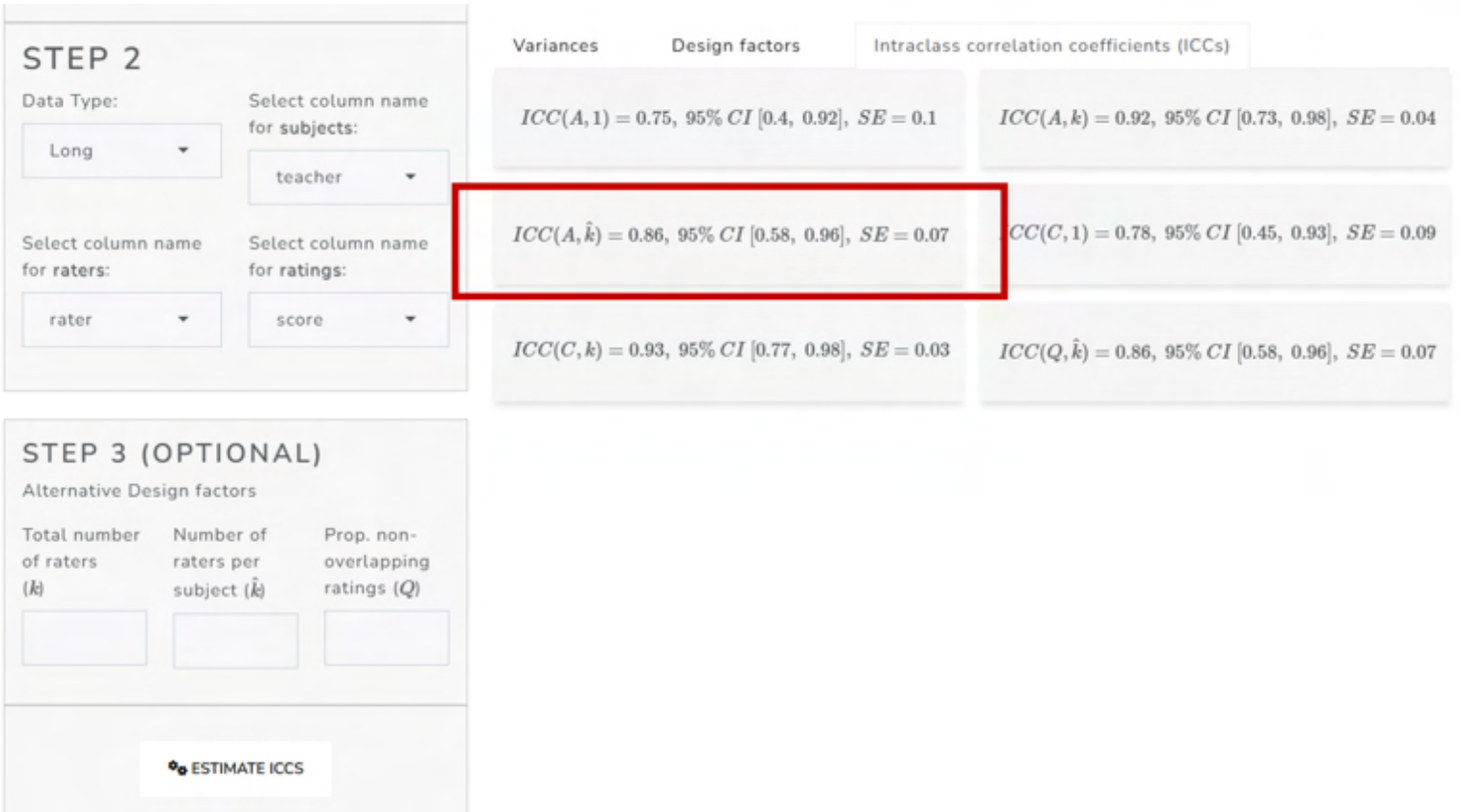

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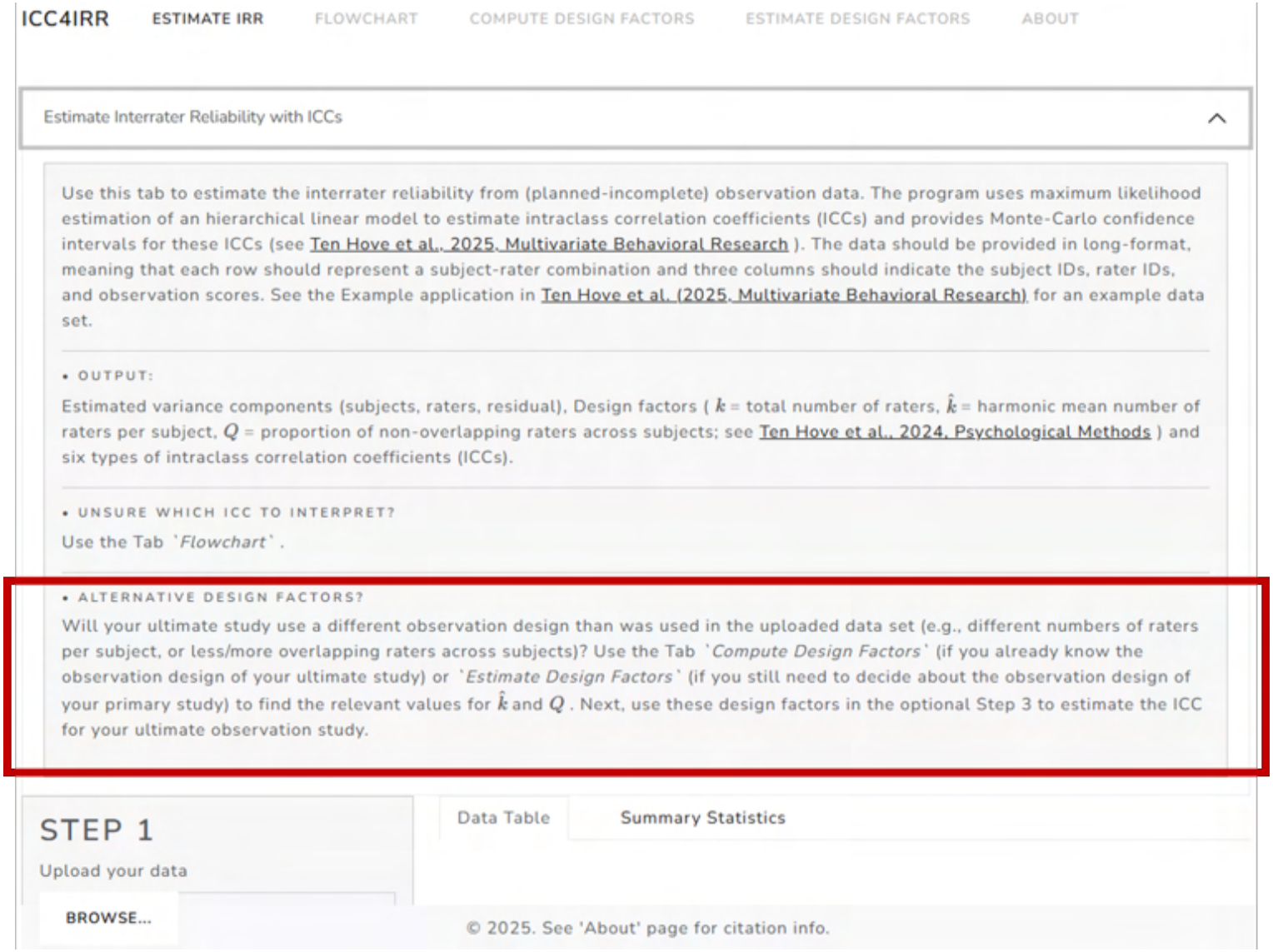

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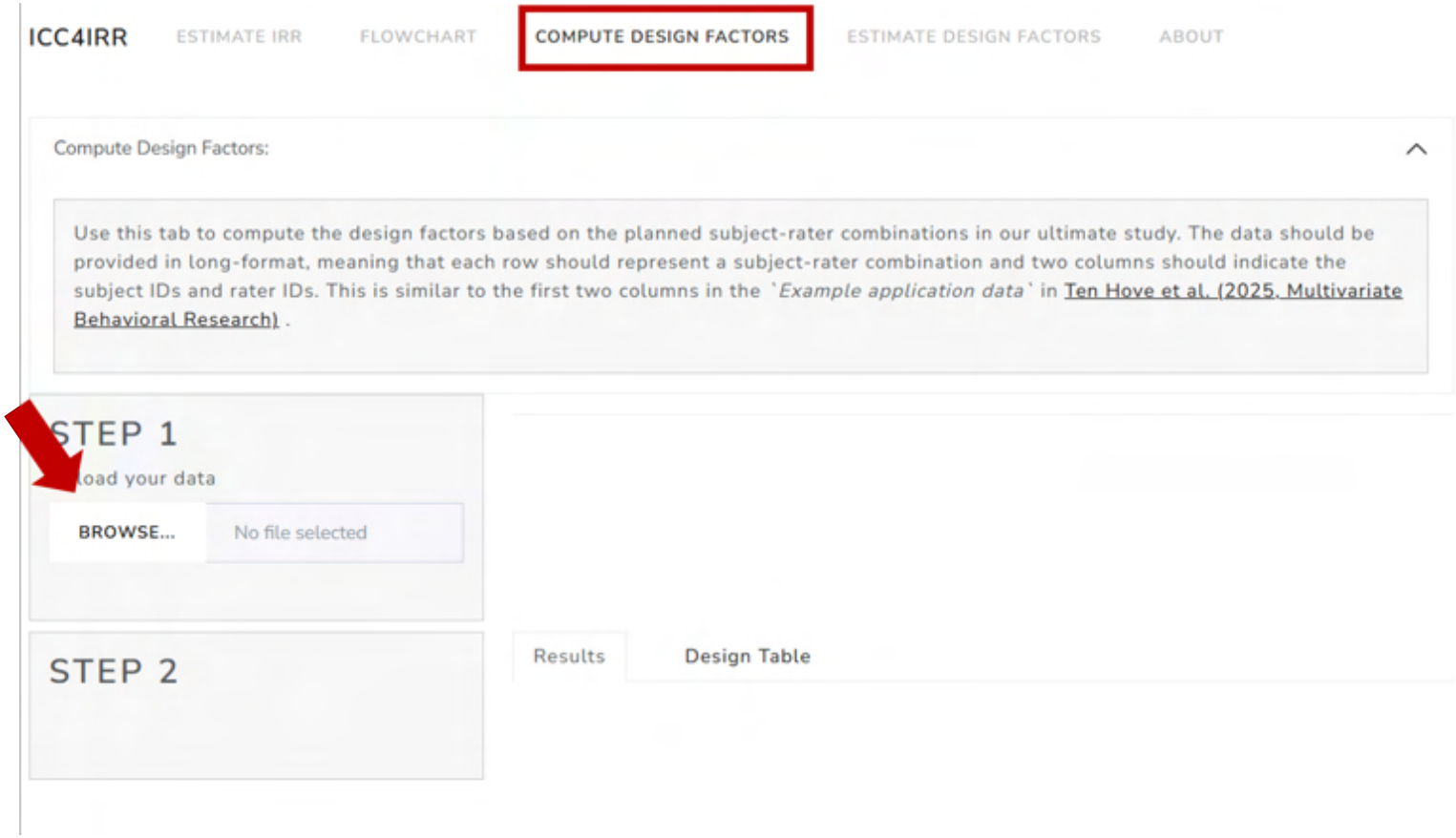

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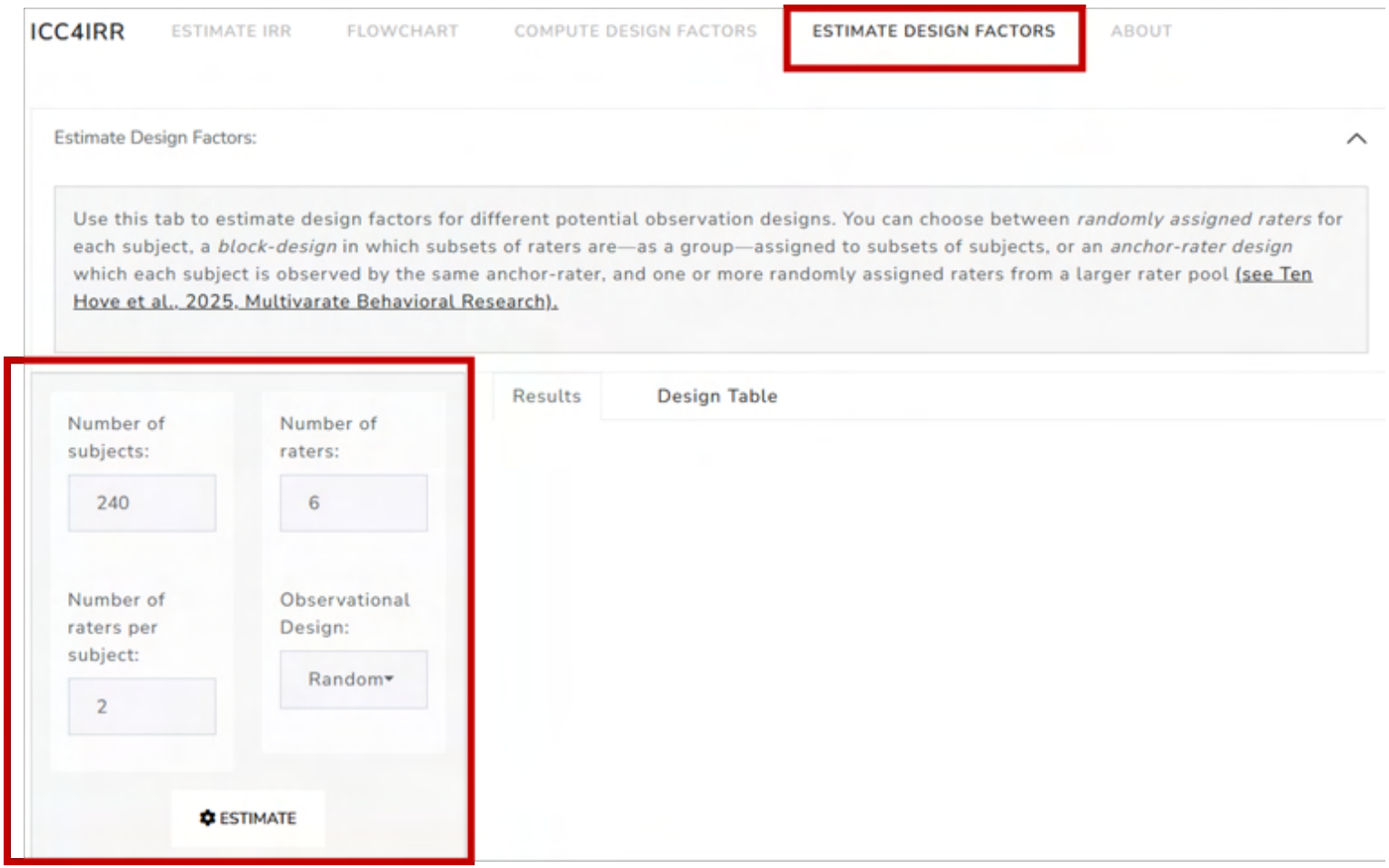

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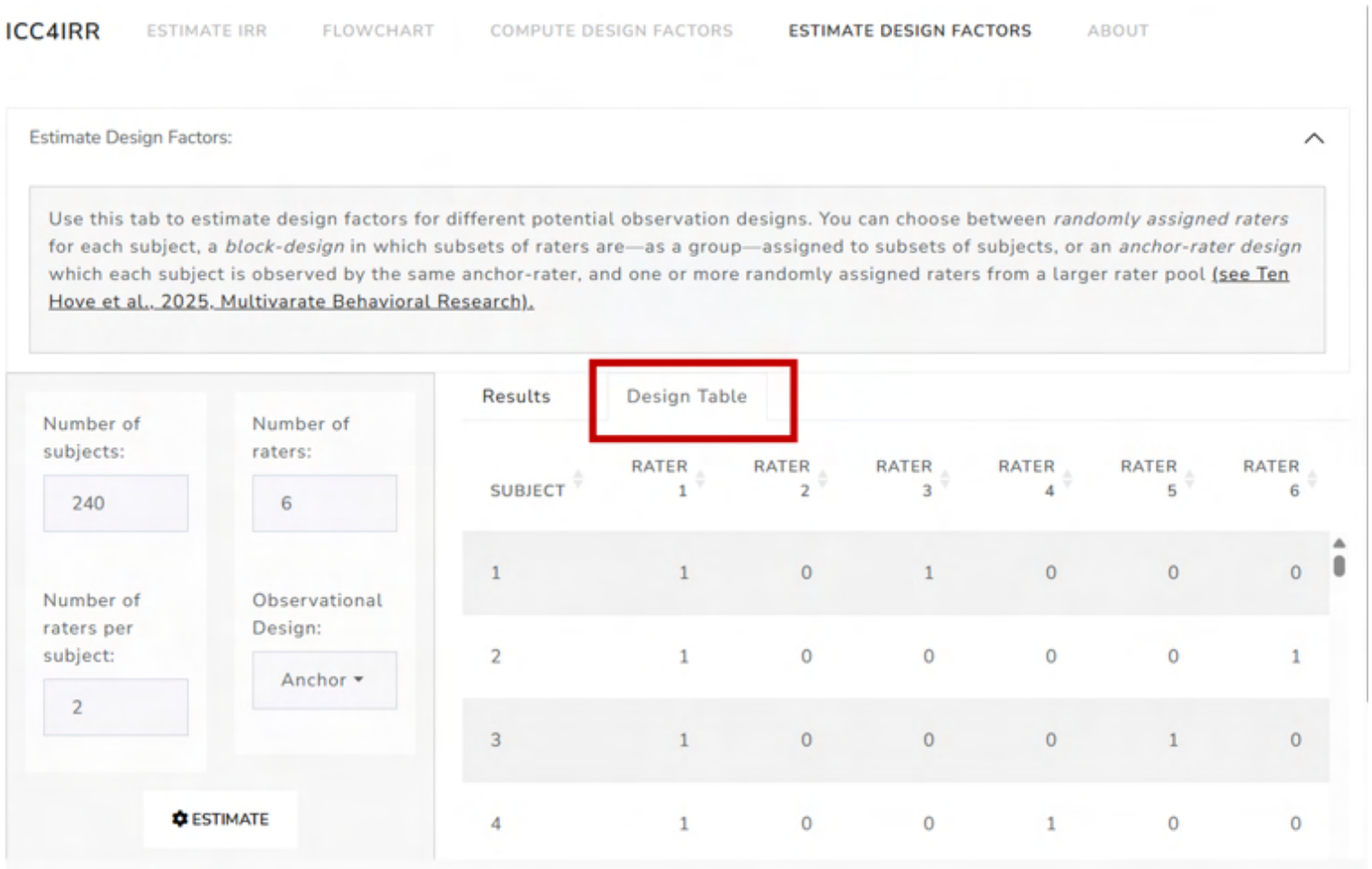

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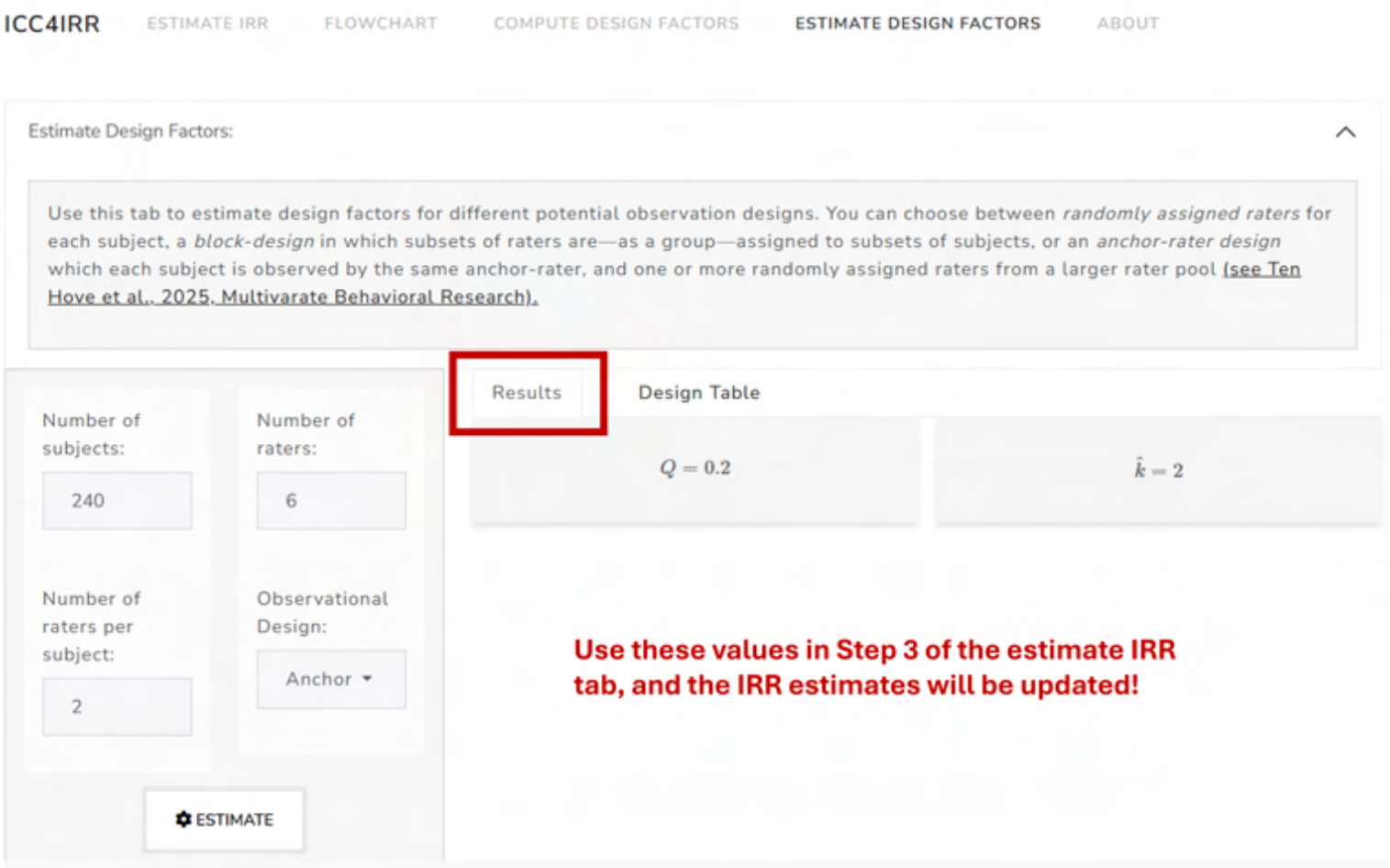

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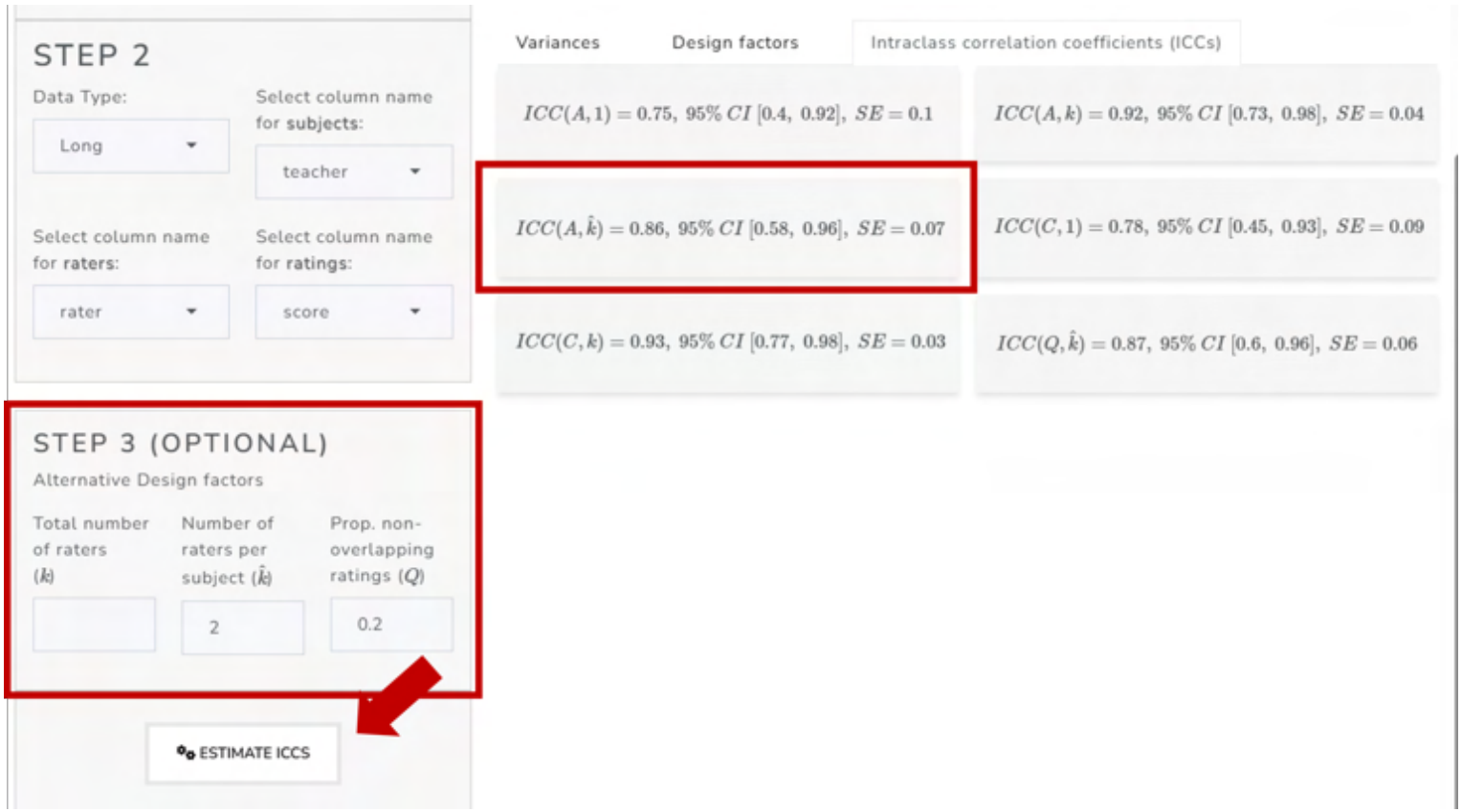

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# Thanks for your attention!

## Questions or suggestions?

D.ten.Hove@VU.nl

All software code on **GITHUB**:


ICC4IRR Shiny app:

# Key References


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