



# Dynamics of Ice Giant Planets

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Ice Giant Systems 2020

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THE UNIVERSITY OF TEXAS AT AUSTIN

Image: E. Karkoschka

# Outline

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- 1) Planetary Magnetic Fields
- 2) Ice Giant Dynamos
- 3) Looking Ahead

# Outline

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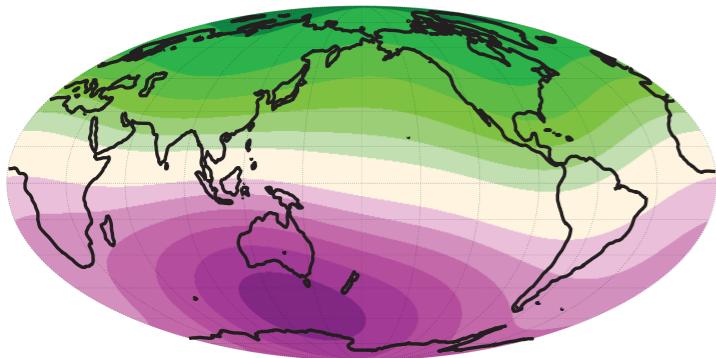
- 1) Planetary Magnetic Fields
- 2) Ice Giant Dynamos
- 3) Looking Ahead

# Planetary Magnetic Fields

- Surface radial magnetic fields  $(l_{max} \leq 3)$

## Terrestrial

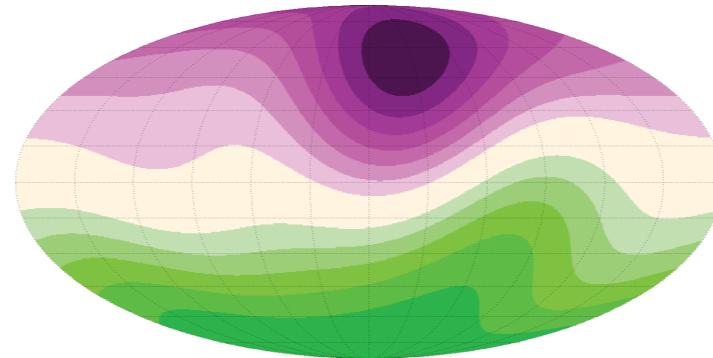
**Earth**



-80  $\mu\text{T}$       80  $\mu\text{T}$

## Gas Giant

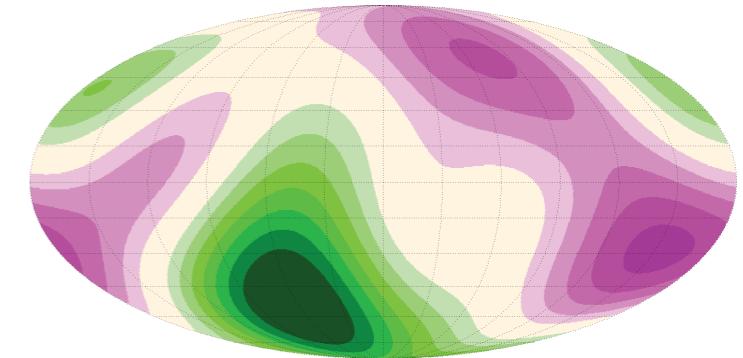
**Jupiter**



-1200  $\mu\text{T}$       1200  $\mu\text{T}$

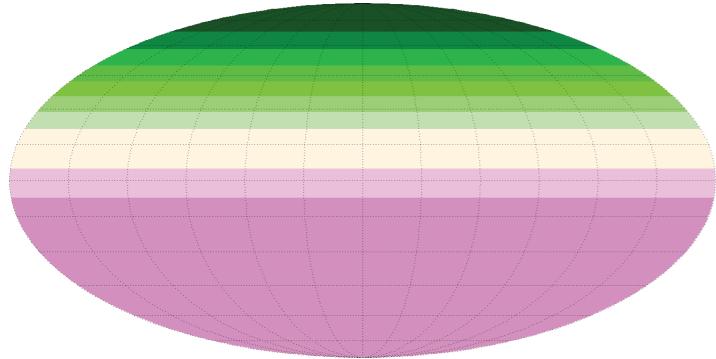
## Ice Giant

**Uranus**



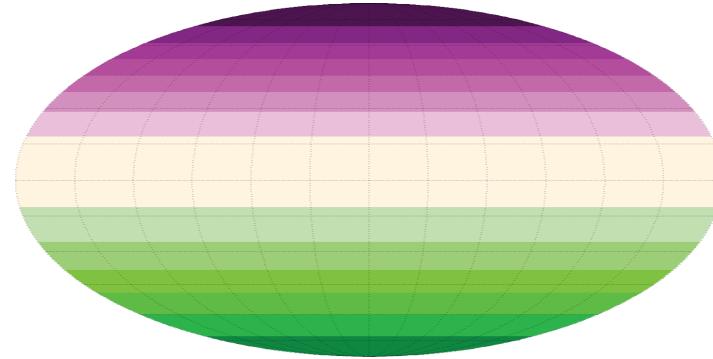
-100  $\mu\text{T}$       100  $\mu\text{T}$

**Mercury**



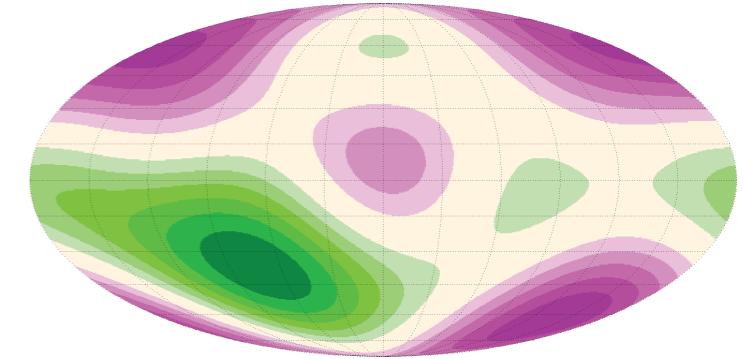
-0.6  $\mu\text{T}$       0.6  $\mu\text{T}$

**Saturn**



-60  $\mu\text{T}$       60  $\mu\text{T}$

**Neptune**



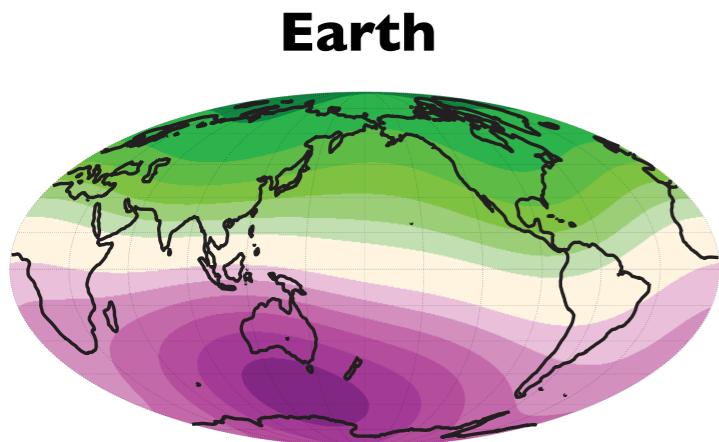
-100  $\mu\text{T}$       100  $\mu\text{T}$

Data taken from Uno et al. (2009), Kivelson et al. (2002), Yu et al. (2010), Burton et al. (2009), and Holme and Bloxham (1996).

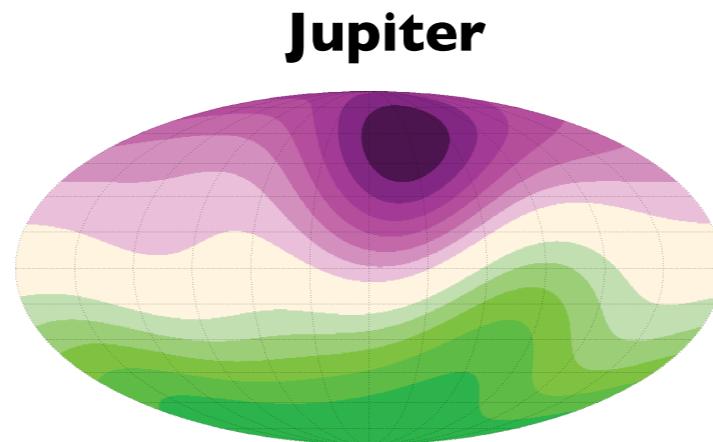
# Planetary Magnetic Fields

- Diverse magnetic field characteristics  $(l_{max} \leq 3)$

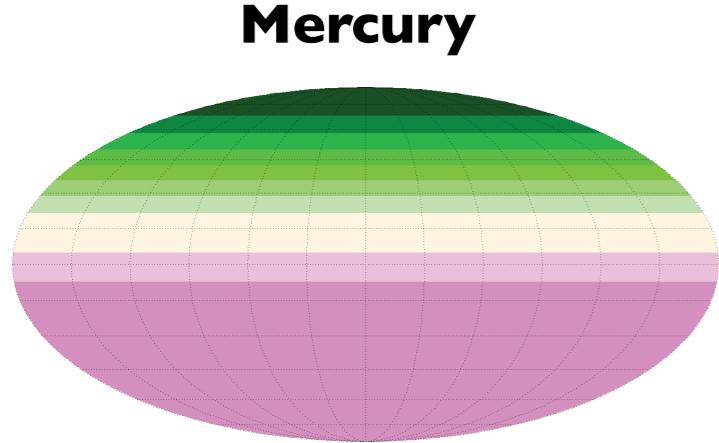
## Axial, Dipolar



-80 μT      80 μT

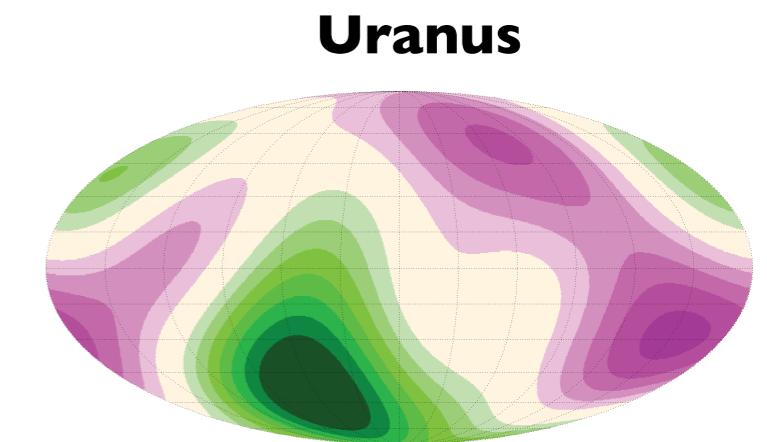


-1200 μT      1200 μT

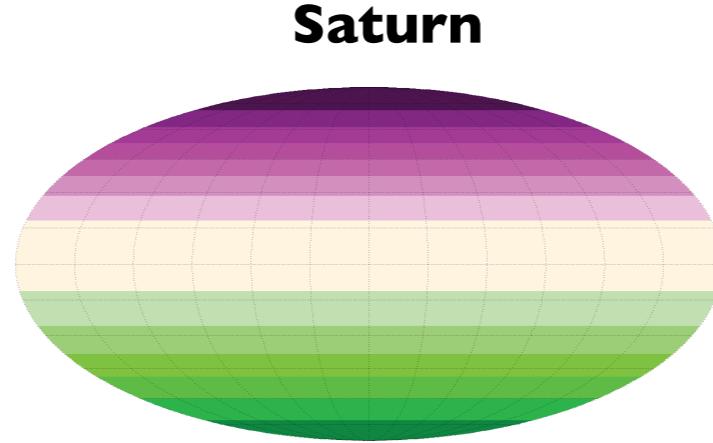


-0.6 μT      0.6 μT

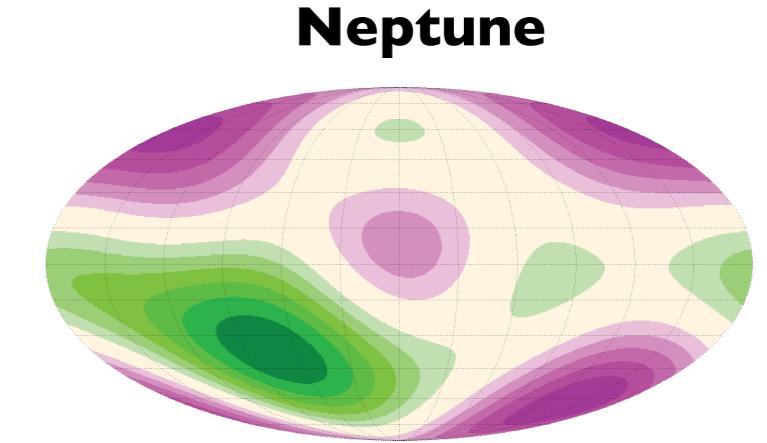
## Non-Axial, Multipolar



-100 μT      100 μT



-60 μT      60 μT

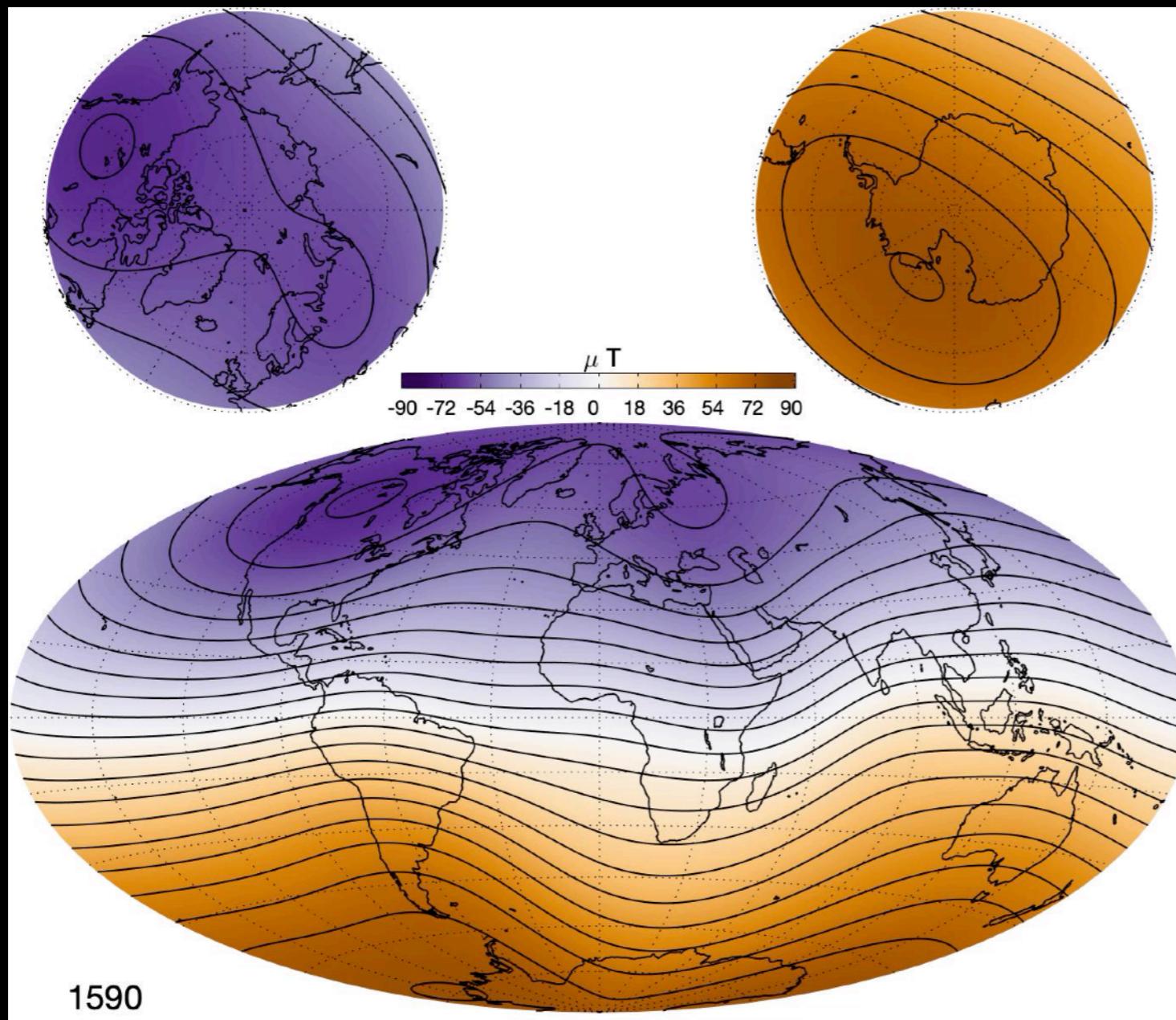


-100 μT      100 μT

Data taken from Uno et al. (2009), Kivelson et al. (2002), Yu et al. (2010), Burton et al. (2009), and Holme and Bloxham (1996).

# Planetary Magnetic Fields

- Secular variation has been measured for the Earth

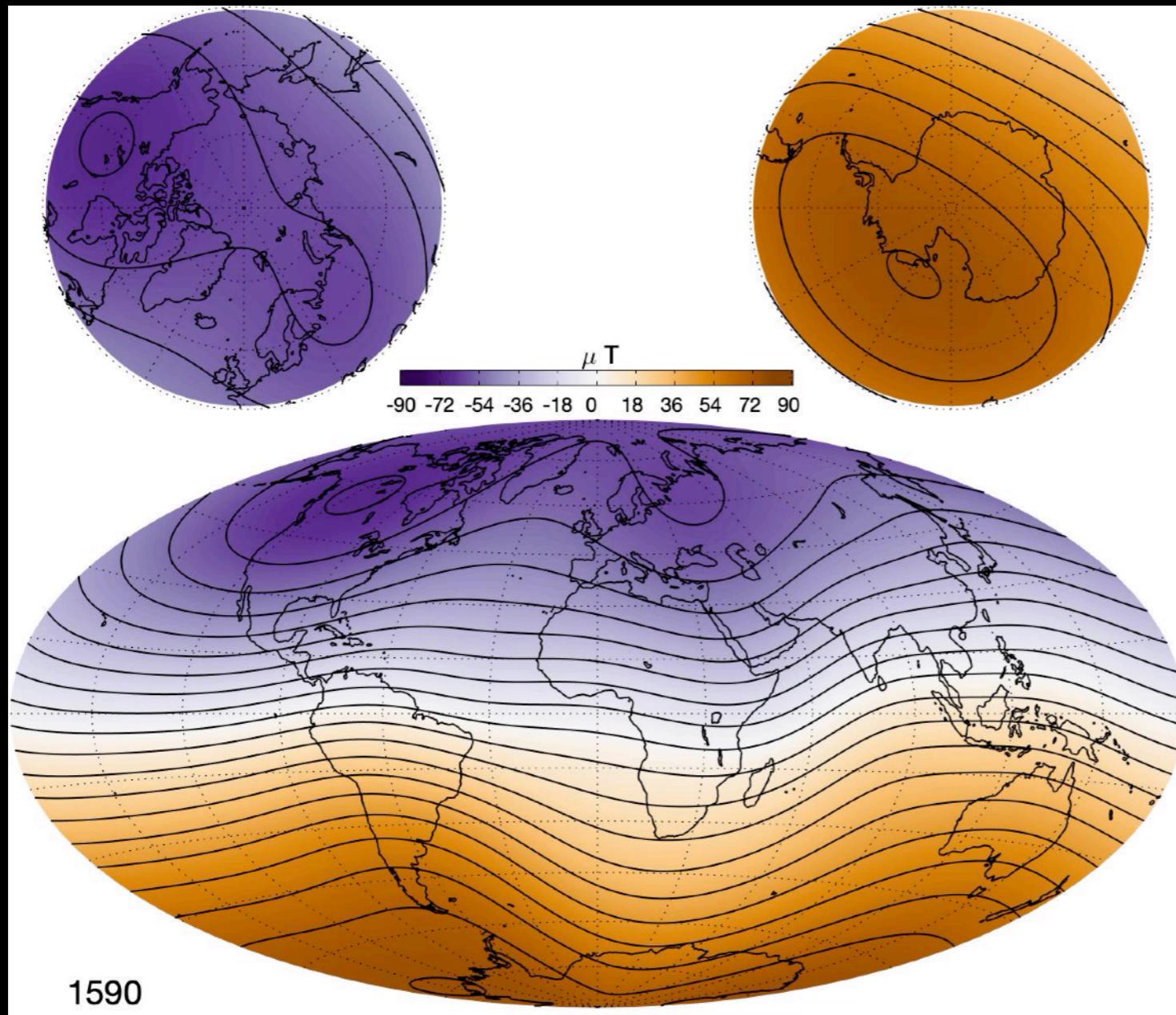


430 years (1590-2020)

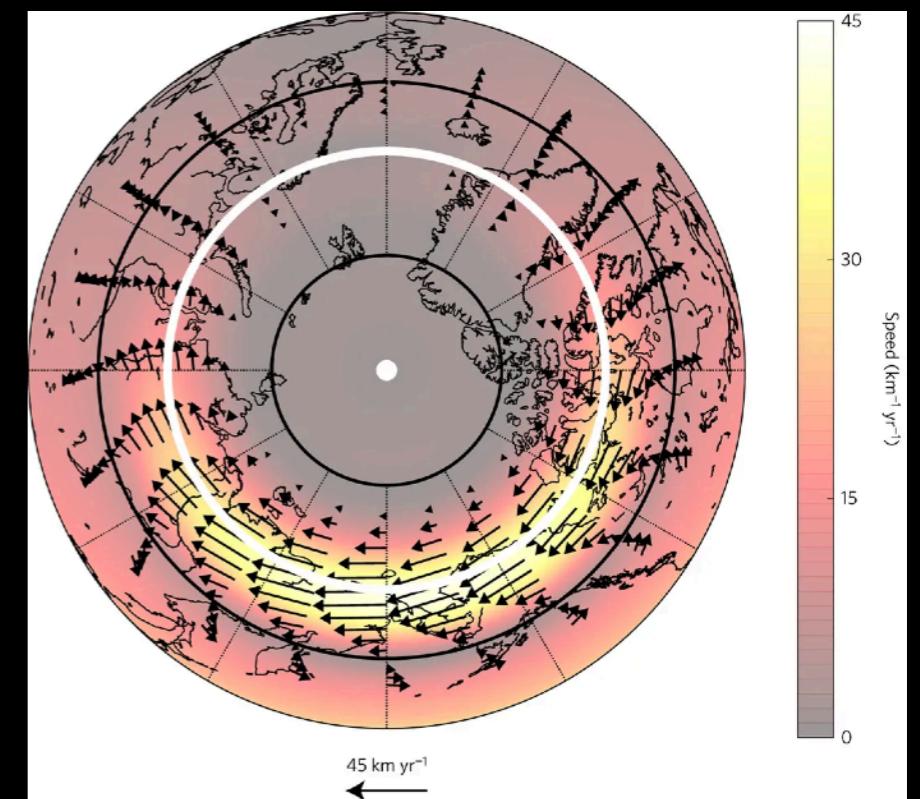
Jackson et al., 2000; Sabaka et al., 2004; Finlay et al., 2020, in prep

# Planetary Magnetic Fields

- Secular variation has been measured for the Earth

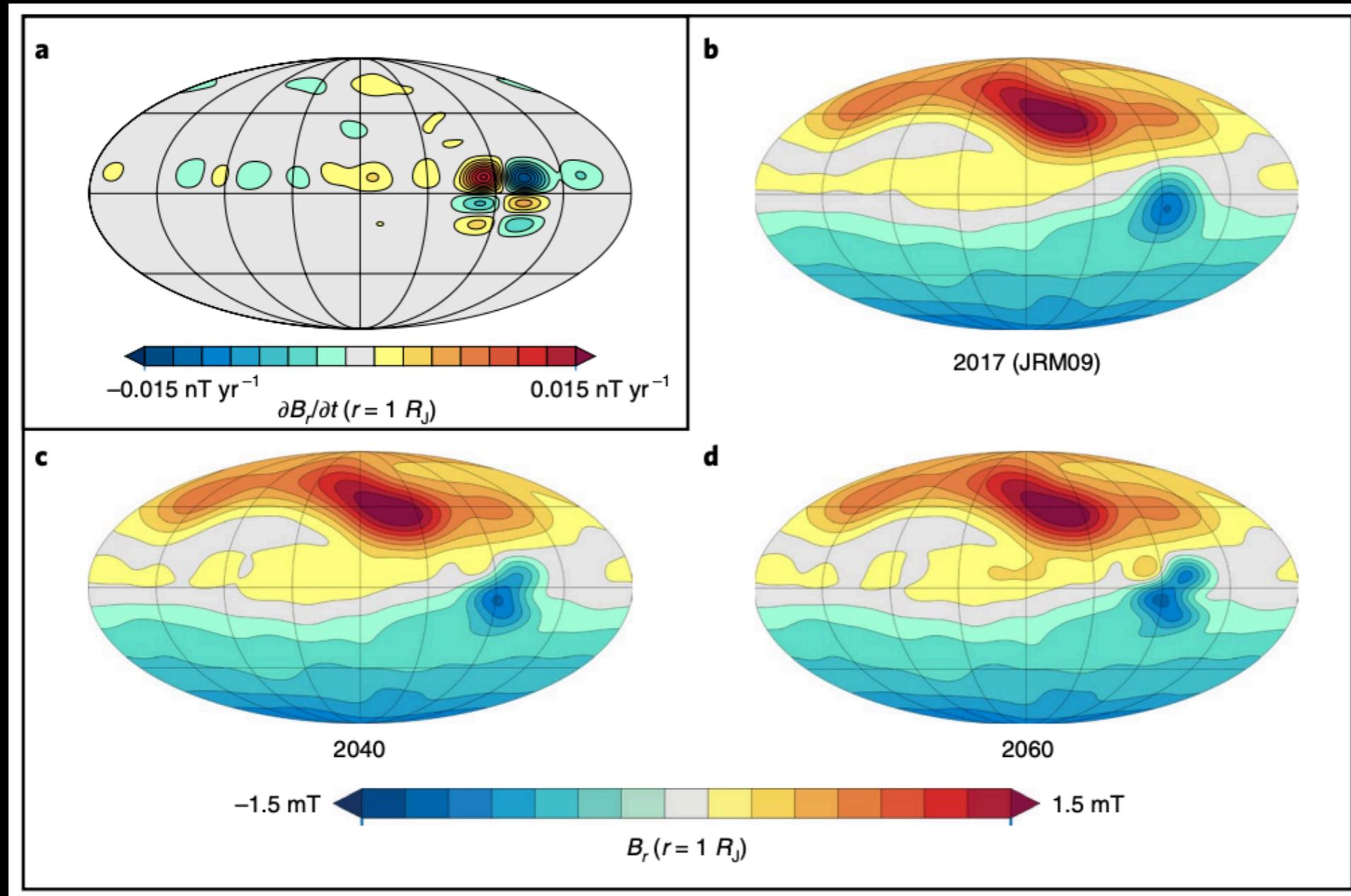


Infer core flows



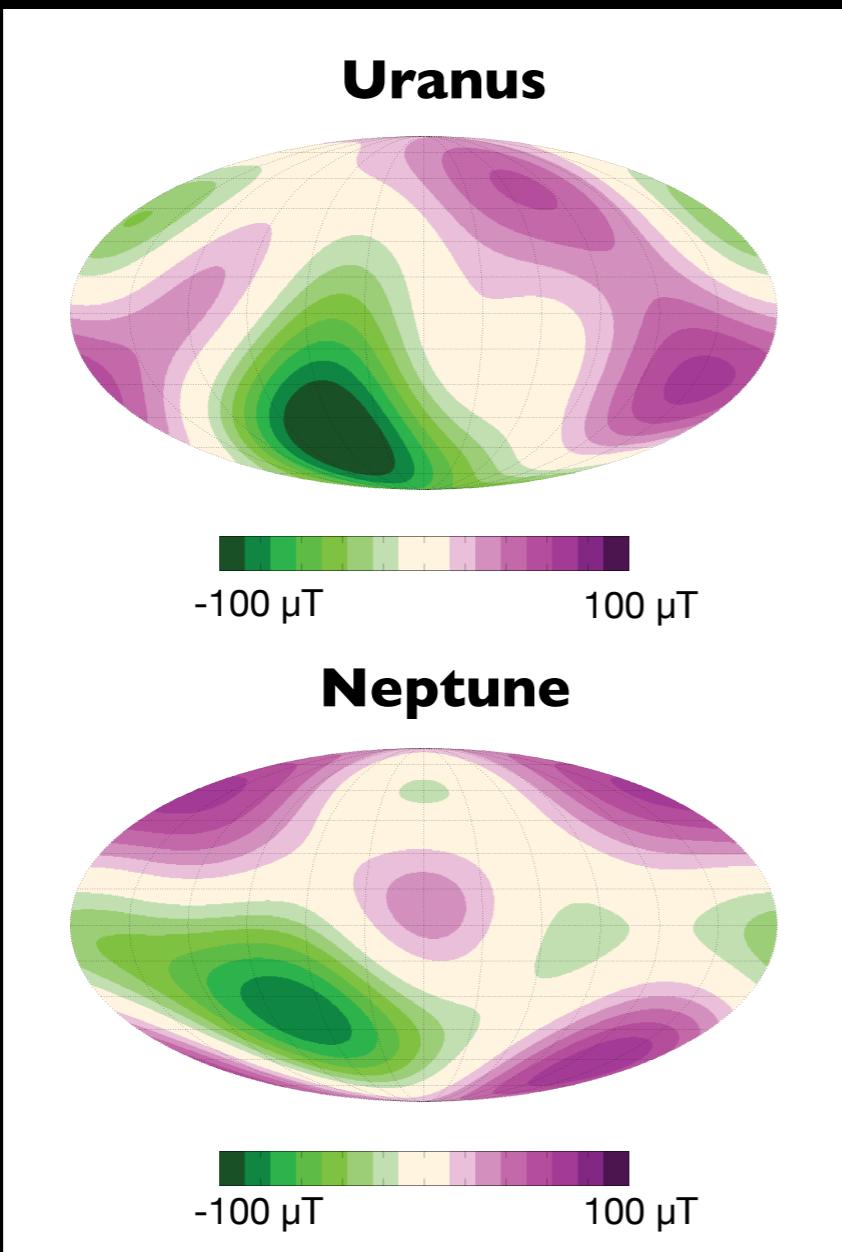
# Planetary Magnetic Fields

- Secular variation has been measured for Jupiter



# Planetary Magnetic Fields

- No knowledge of secular variation for the ice giants



— → ?

— → ?

# Planetary Magnetic Fields

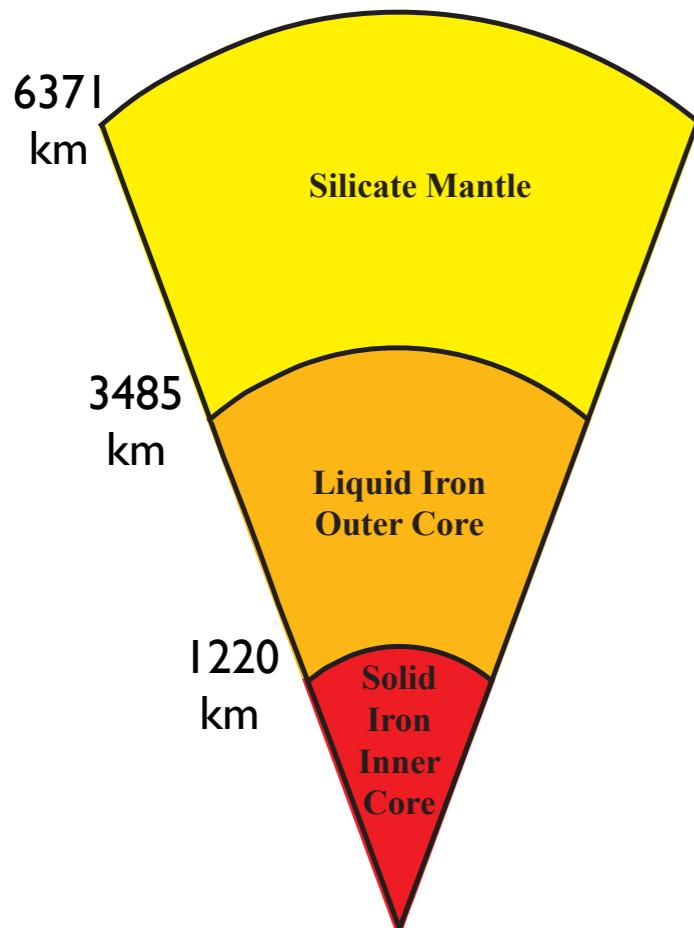
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- What controls the morphology, strength, and evolution of planetary magnetic fields?
- Comparative planetology serves as natural laboratory for hypothesis tests
  - Why do the ice giants have non-axisymmetric, multipolar magnetic fields while the gas giants have axial, dipole-dominated magnetic fields?
  - Why do the ice giants, Saturn, and Earth have similar magnetic field strengths?
  - Do the ice giants undergo secular variation?

# Dynamo Generation

- Geomagnetic field generated by convective-driven dynamo in iron core

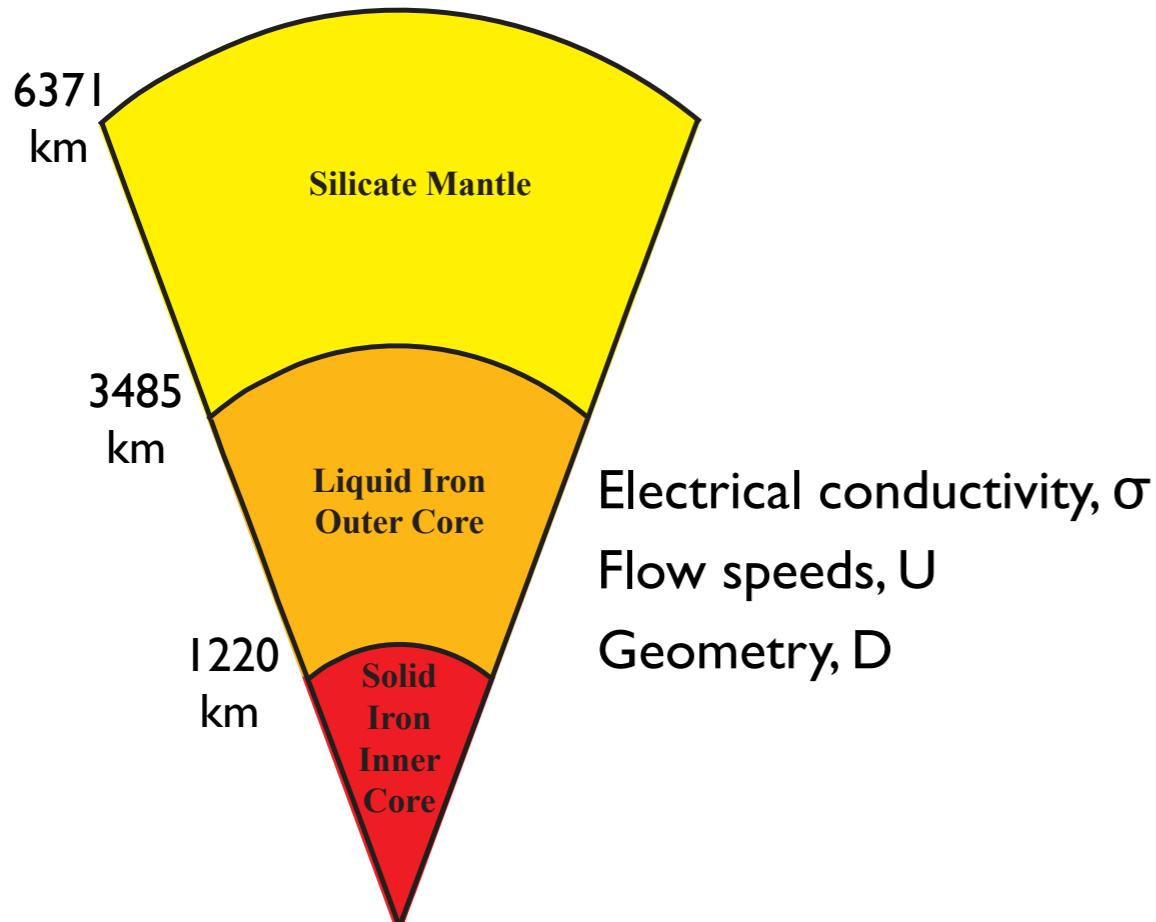
## Terrestrial



# Dynamo Generation

- Geomagnetic field generated by convective-driven dynamo in iron core

## Terrestrial

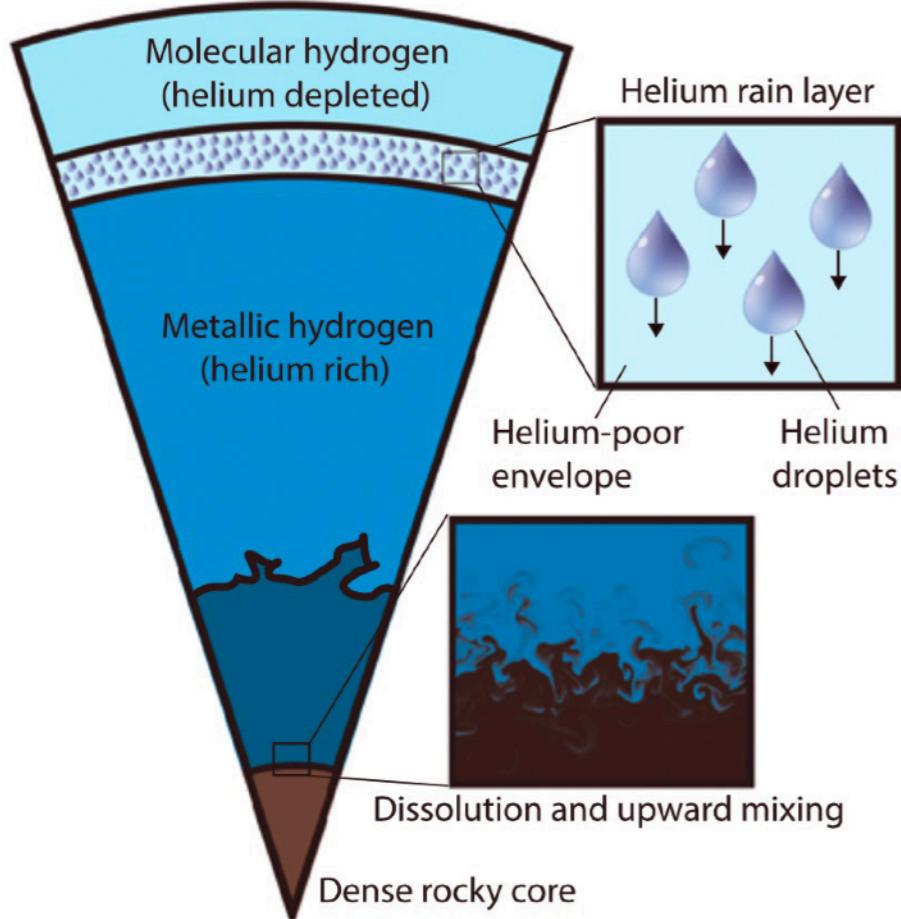


$$\frac{\partial \mathbf{B}}{\partial t} = \underbrace{\nabla \times (\mathbf{u} \times \mathbf{B})}_{\text{Temporal}} + \underbrace{\frac{1}{\mu_0 \sigma} \nabla^2 \mathbf{B}}_{\text{Induction}} - \underbrace{\frac{\eta}{\mu_0 \sigma} \mathbf{B}}_{\text{Diffusion}}$$
$$Rm = \frac{\text{Magnetic induction}}{\text{Magnetic diffusion}} = \mu_0 \sigma U D \gtrsim 10^2$$

# Dynamo Generation

- Magnetic fields generated by convectively-driven dynamos in electrically conducting fluid regions

## Jupiter

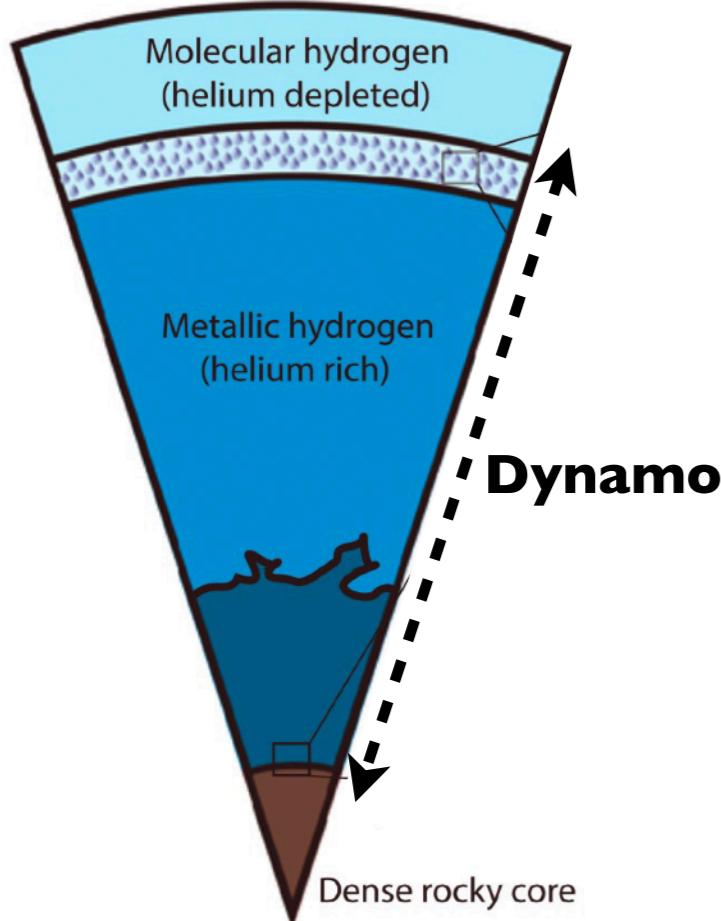


Wahl et al. (2017)

# Dynamo Generation

- Magnetic fields generated by convectively-driven dynamos in electrically conducting fluid regions

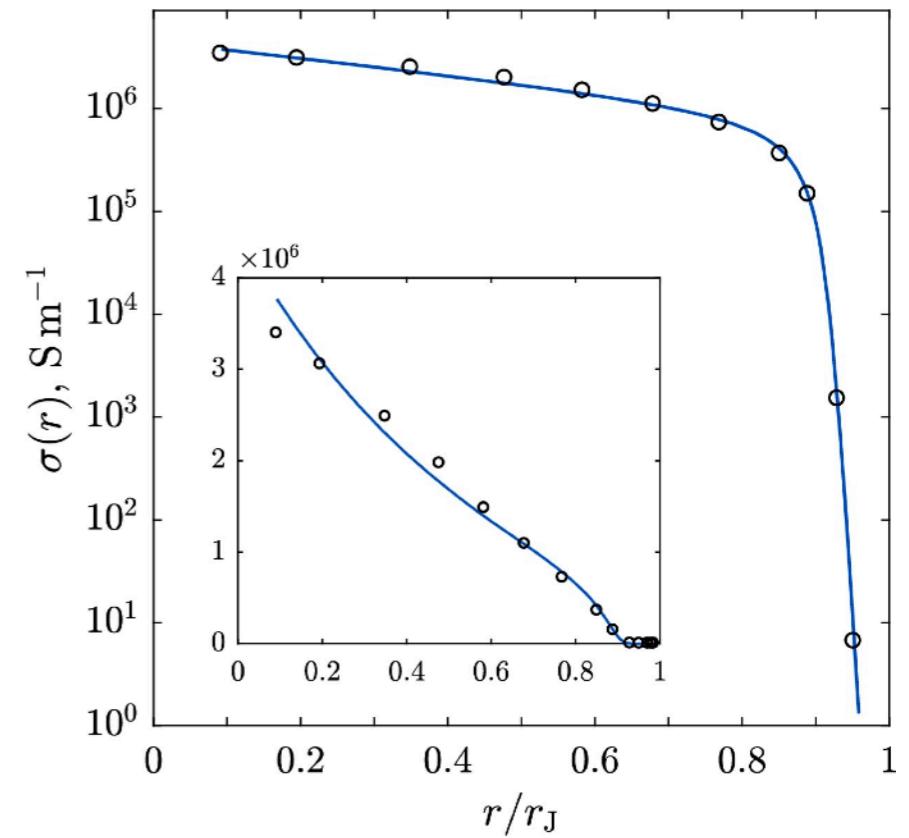
## Jupiter



$$Rm = \mu_0 \sigma U D \gtrsim 10^2$$

Electrical conductivity,  $\sigma$   
Flow speeds,  $U$   
Geometry,  $D$

Wahl et al. (2017)

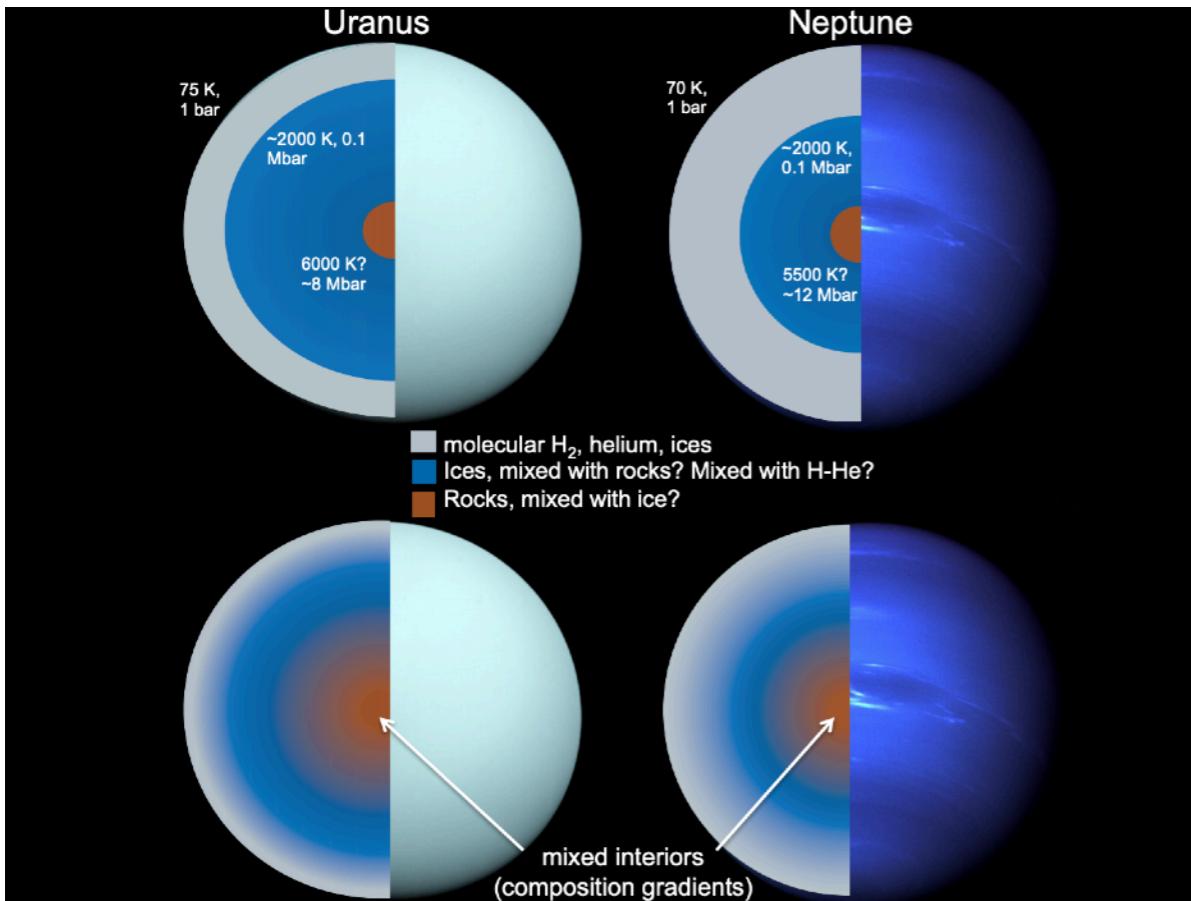


French et al. (2012); Tsang and Jones (2020)

# Dynamo Generation

- Magnetic fields generated by convectively-driven dynamos in electrically conducting fluid regions

## Ice Giants

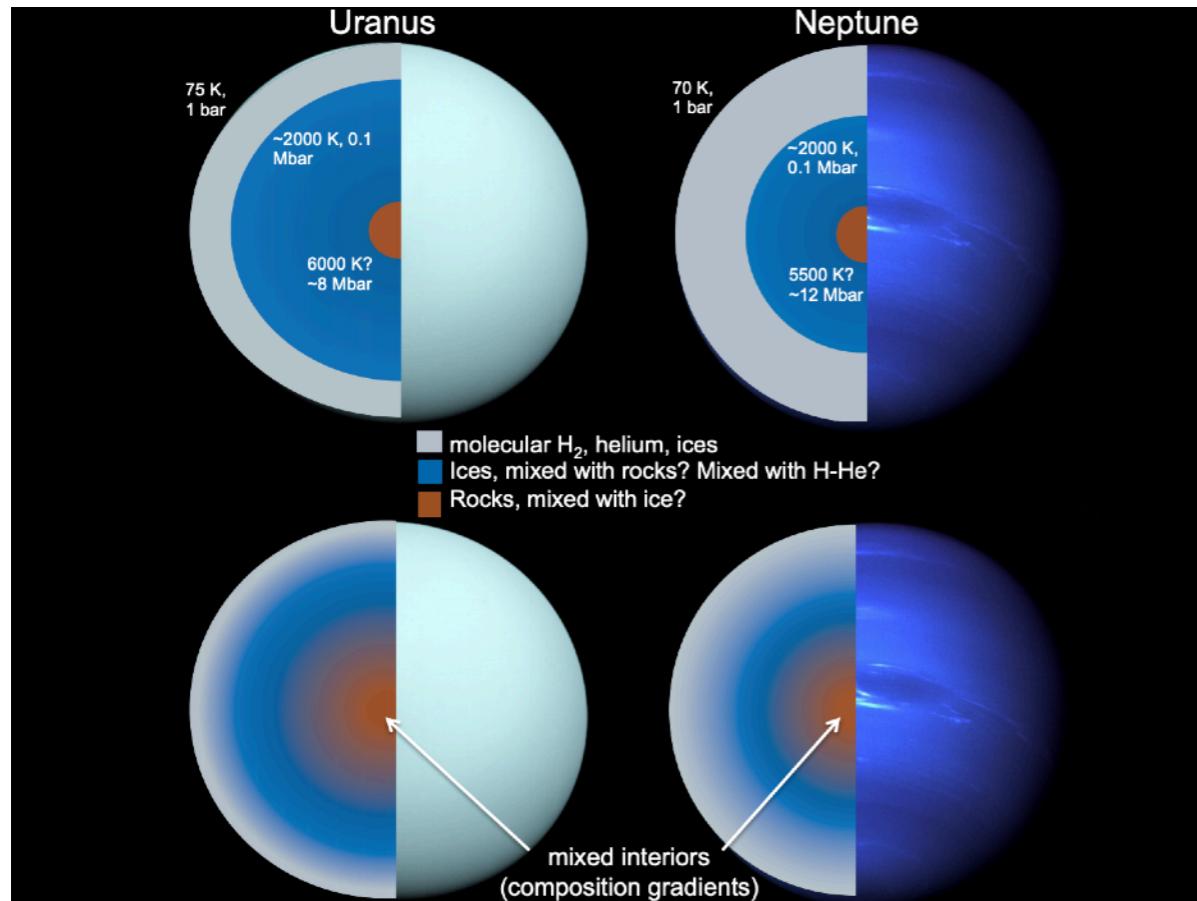


Helled et al. (2020)

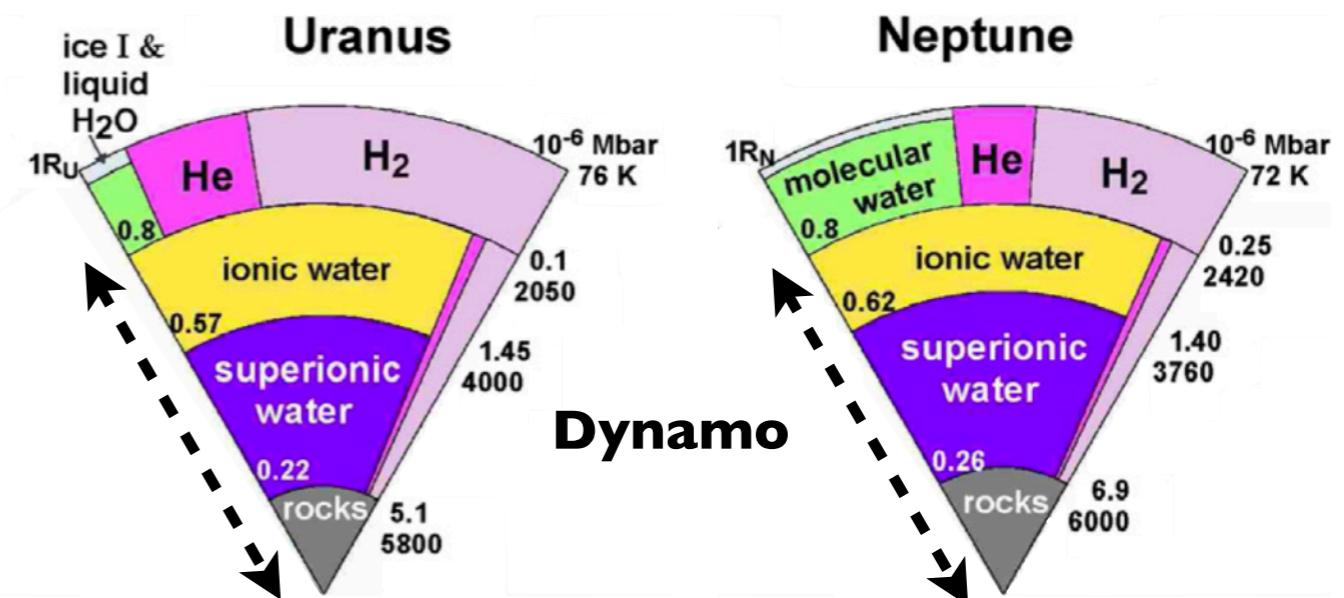
# Dynamo Generation

- Magnetic fields generated by convectively-driven dynamos in electrically conducting fluid regions

## Ice Giants



Helled et al. (2020)



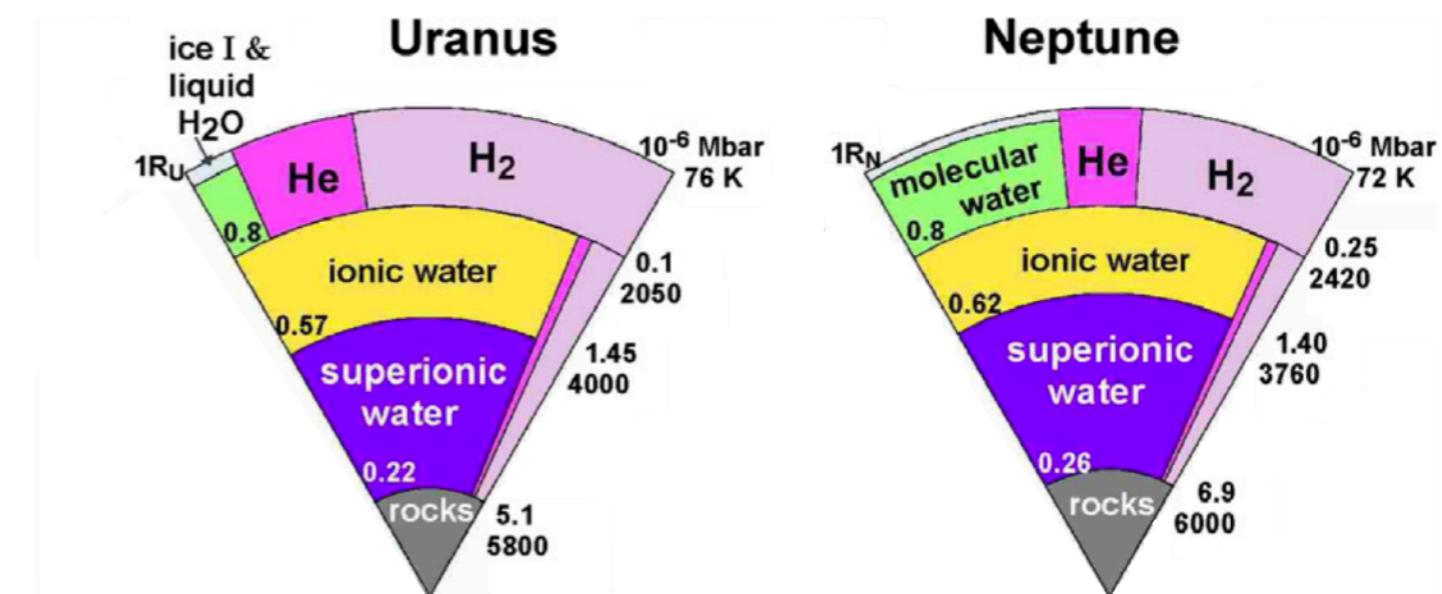
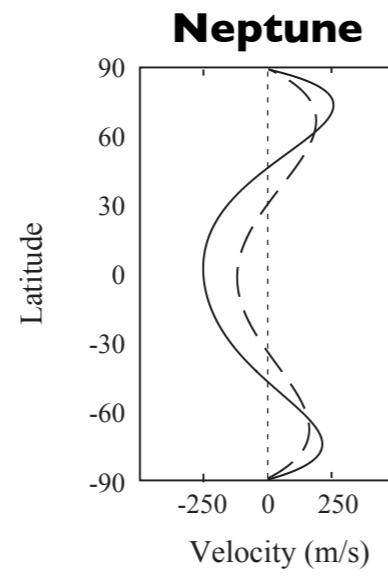
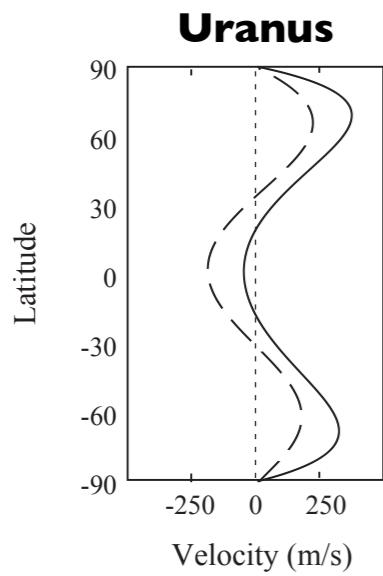
Redmer et al. (2011)

# Dynamo Generation

- The interior and atmosphere may be coupled dynamically

## Ice Giants

- Do the zonal winds interact with dynamo generation?



Soderlund et al. (2013)

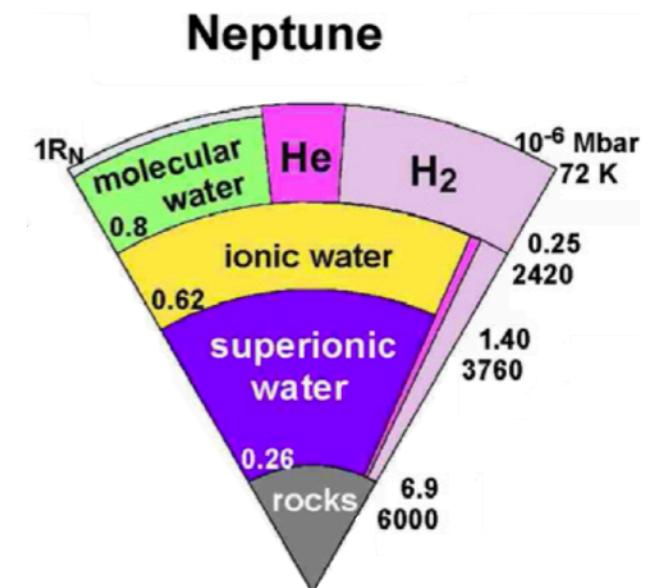
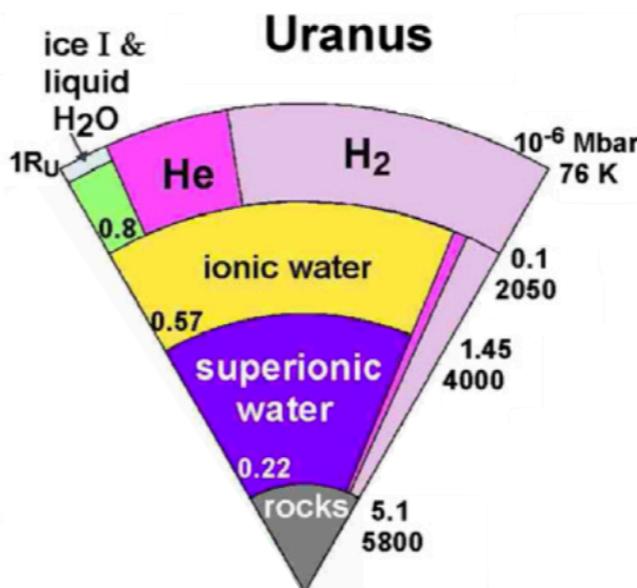
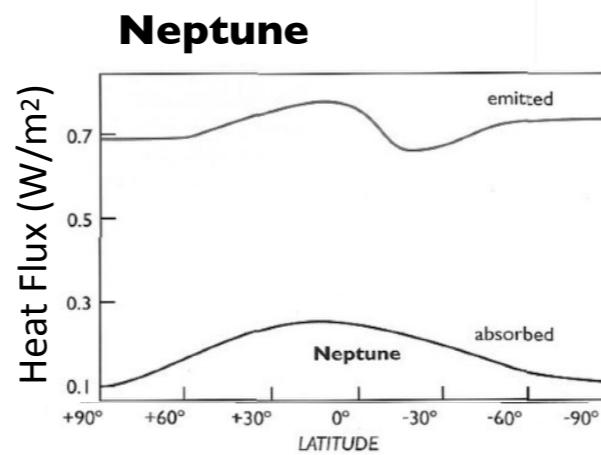
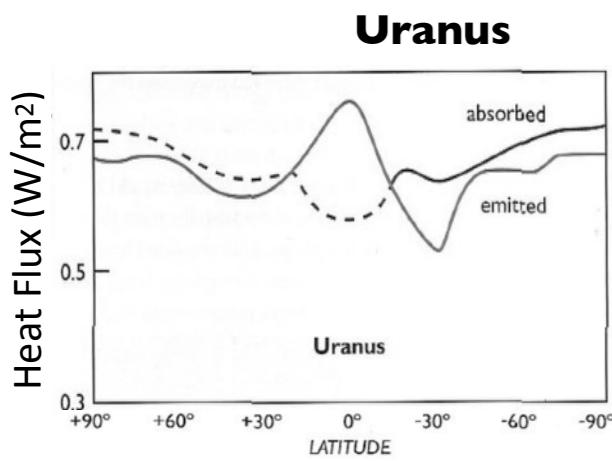
Redmer et al. (2011)

# Dynamo Generation

- The interior and atmosphere may be coupled dynamically

## Ice Giants

- Do stable layers exist in the interior?



# Planetary Dynamos

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- By studying magnetic fields, we learn about a planet's internal structure, composition, dynamics, and evolution

# Outline

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- 1) Planetary Magnetic Fields
- 2) Ice Giant Dynamos
- 3) Looking Ahead

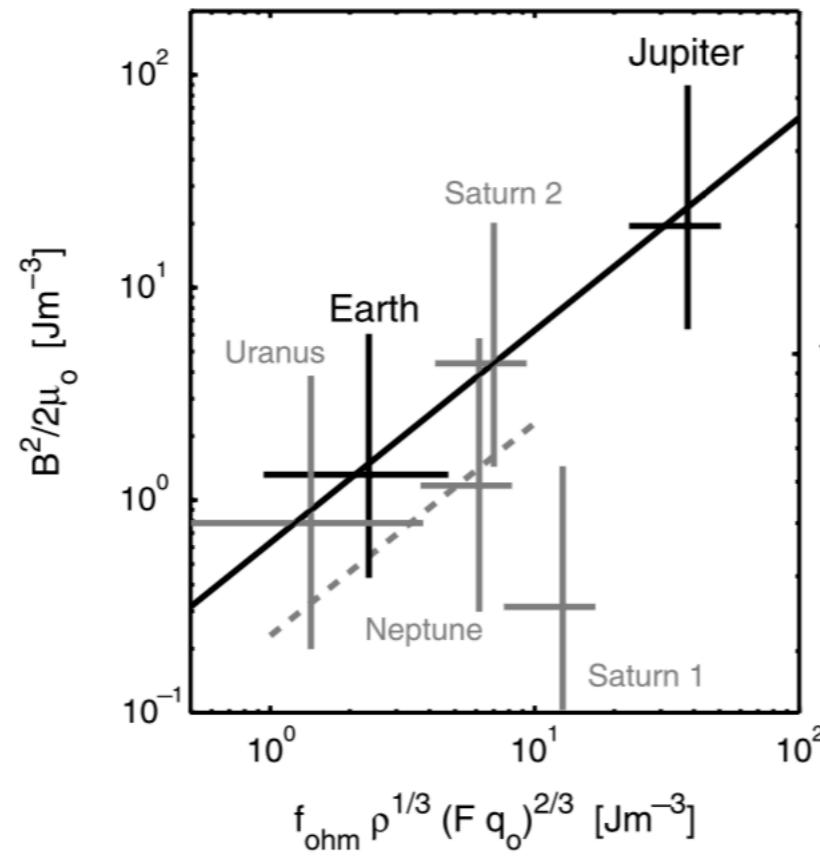
# Magnetic Field Strength

- Numerous scaling laws have been proposed to predict magnetic field strengths

#	Rule	Author	Remark
1	$B_p R_p^3 \propto (\rho \Omega R_p^5)^a$	e.g. Russell (1978)	magnetic Bode law
2	$B^2 \propto \rho \Omega^2 R_c^2$	Busse (1976)	
3	$B^2 \propto \rho \Omega \sigma^{-1}$	Stevenson (1979)	Elsasser number rule
4	$B^2 \propto \rho R_c^3 q_c \sigma$	Stevenson (1984)	at low energy flux
5	$B^2 \propto \rho \Omega R_c^{5/3} q_c^{1/3}$	Curtis and Ness (1986, modified)	mixing length theory
6	$B^2 \propto \rho \Omega^{3/2} R_c \sigma^{-1/2}$	Mizutani et al. (1992)	
7	$B^2 \propto \rho \Omega^2 R_c$	Sano (1993)	
8	$B^2 \propto \rho \Omega^{1/2} R_c^{3/2} q_c^{1/2}$	Starchenko and Jones (2002)	MAC balance
9	$B^2 \propto \rho R_c^{4/3} q_c^{2/3}$	Christensen and Aubert (2006)	energy flux scaling

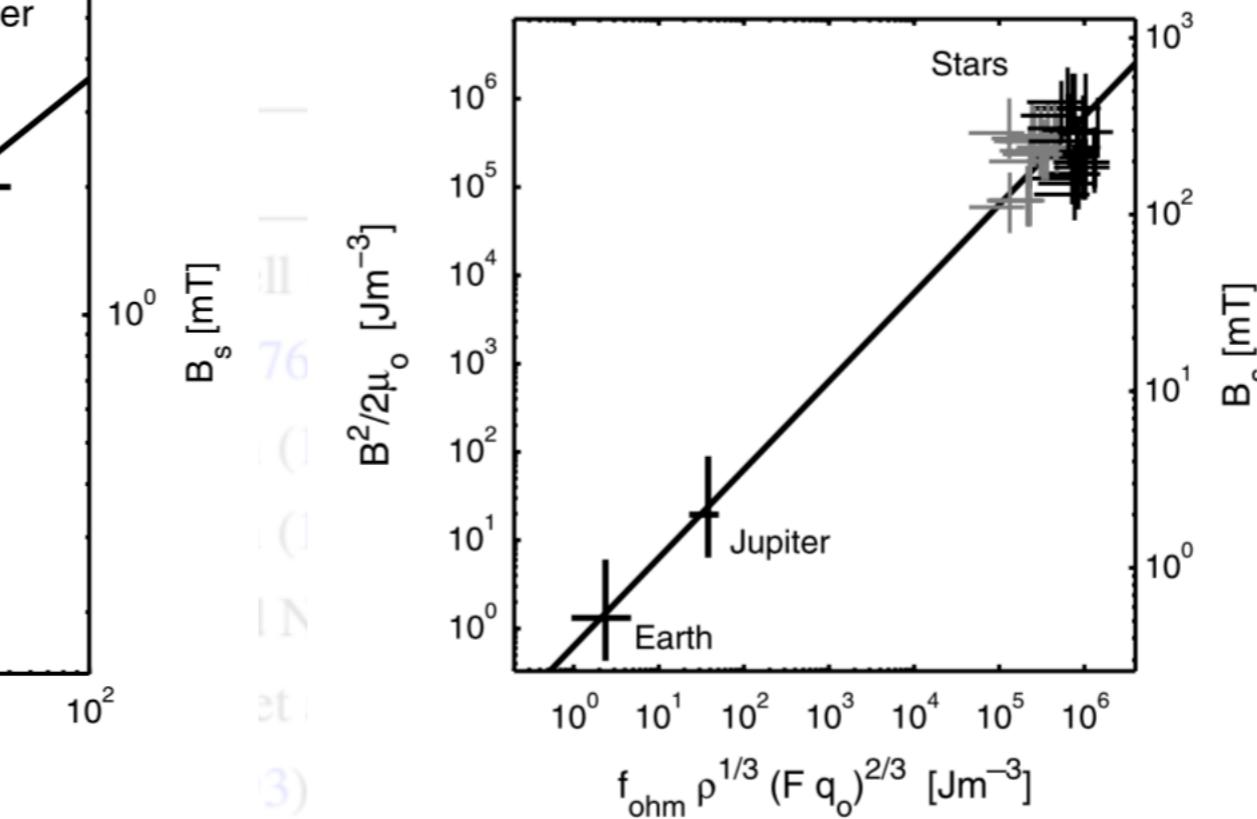
# Magnetic Field Strength

- Energy flux scaling does a reasonable job explaining (most) planetary and stellar field strengths



$$B^2 \propto \rho \Omega^{1/2} R_c^{5/2} q_c^{1/2}$$

$$B^2 \propto \rho R_c^{4/3} q_c^{2/3}$$



Starchenko and Jones (2002)

Christensen and Aubert (2006)

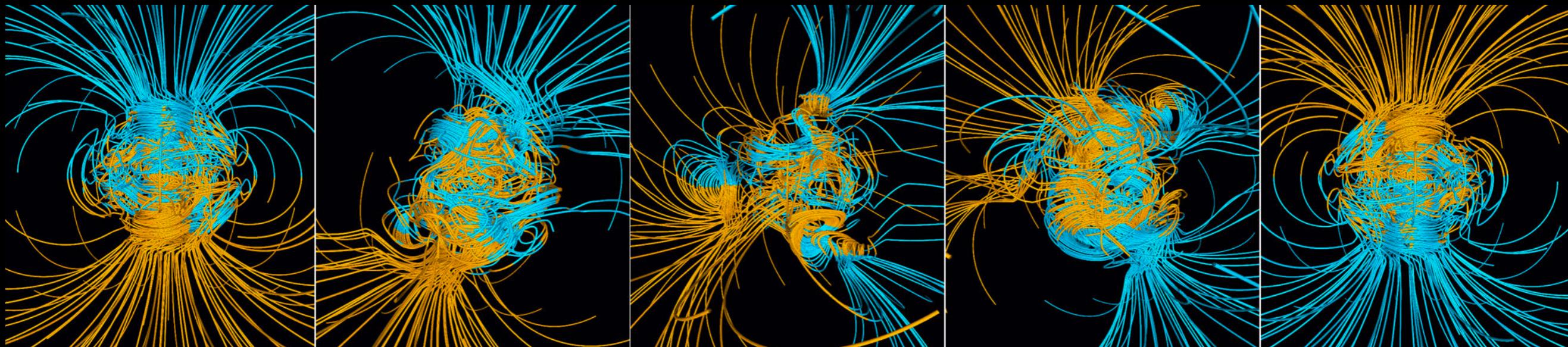
MAC balance

energy flux scaling

Christensen (2010)

# Magnetic Field Morphology

- Numerous hypotheses have been proposed to explain the multipolar magnetic field morphologies
  - Mid-reversal, but very unlikely to be occurring simultaneously at both Uranus and Neptune

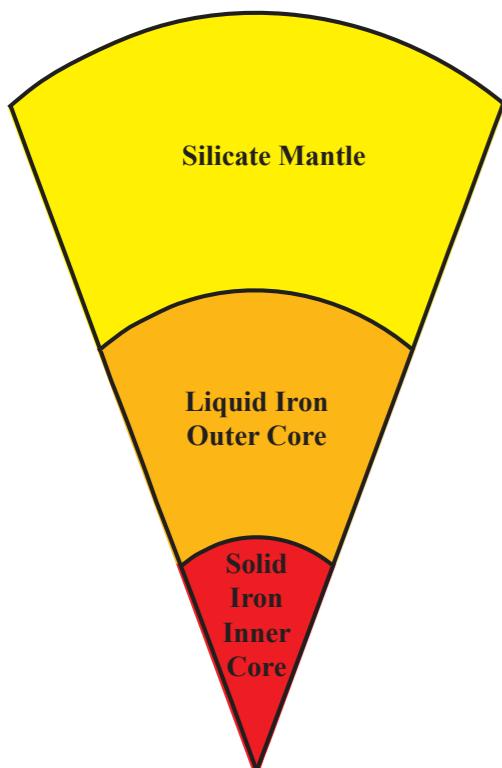


Credit: Glatzmaier, Plait

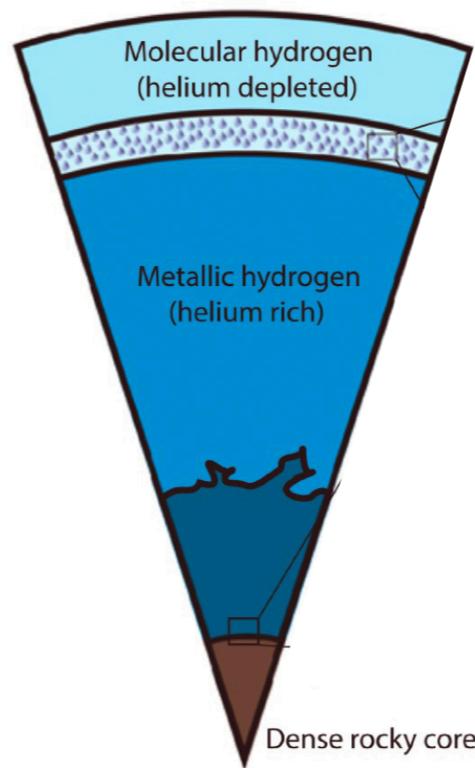
# Magnetic Field Morphology

- Differences in dynamo source regions may explain planetary magnetic field differences
  - Geometry and Dynamics/Composition

**Terrestrial**

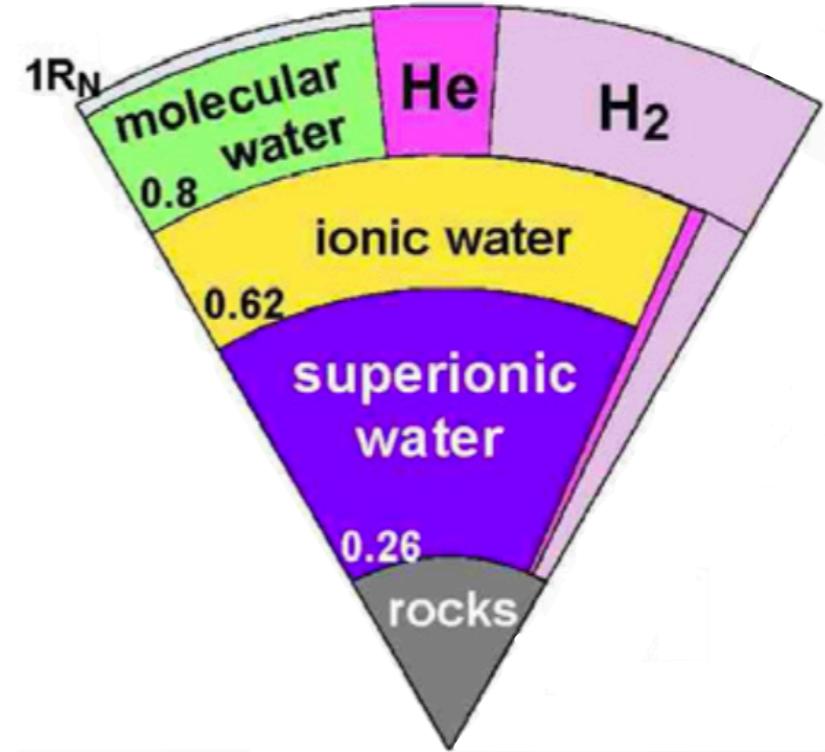


**Gas Giant**



Wahl et al. (2017)

**Ice Giant**

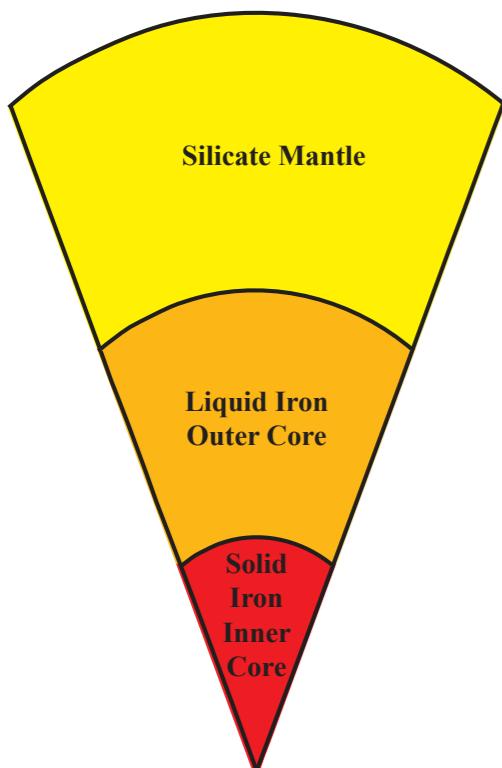


Redmer et al. (2011)

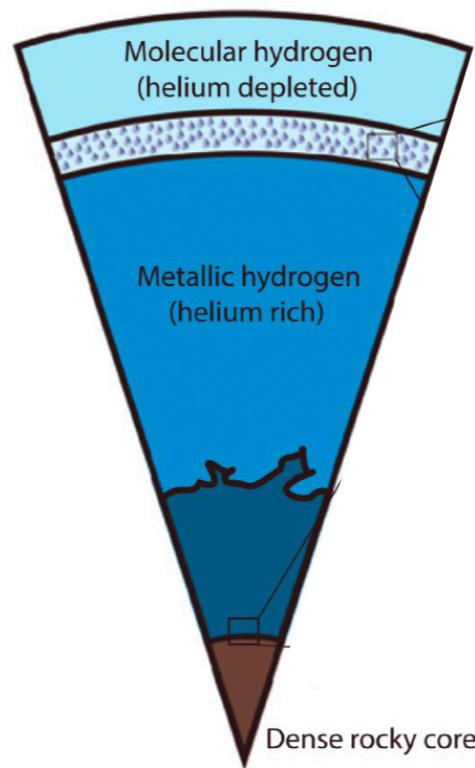
# Magnetic Field Morphology

- Hypothesis: The ice giants have multipolar dynamos because their convective regions are geometrically thin with a deep stably stratified layer (Hubbard et al., 1995; Stanley and Bloxham, 2004)

**Terrestrial**

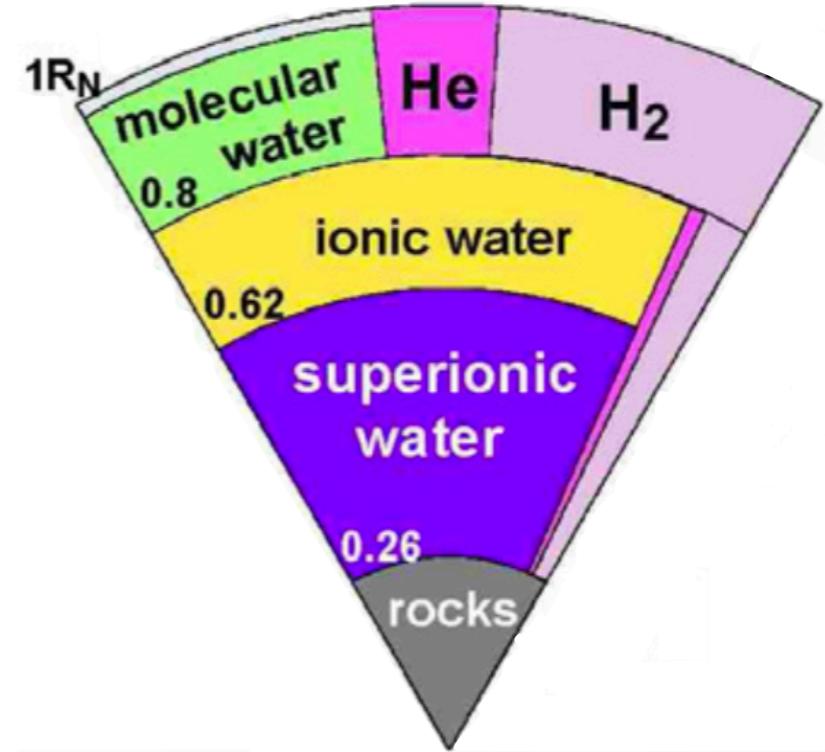


**Gas Giant**



Wahl et al. (2017)

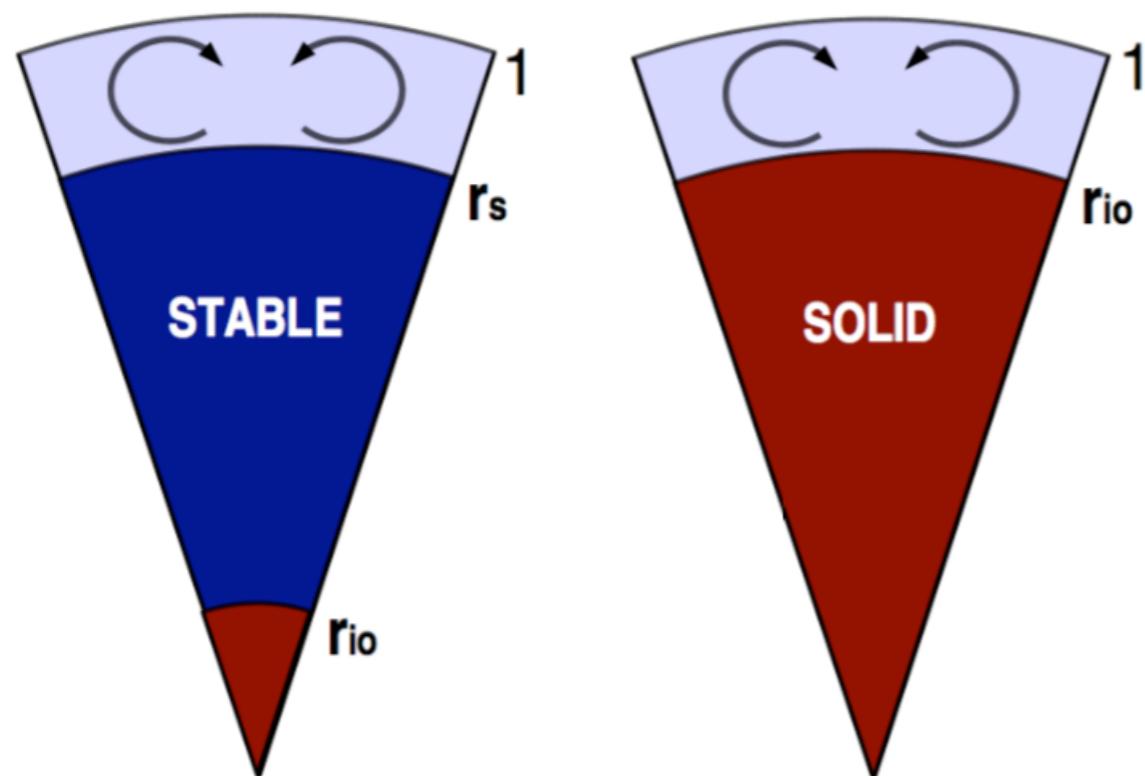
**Ice Giant**



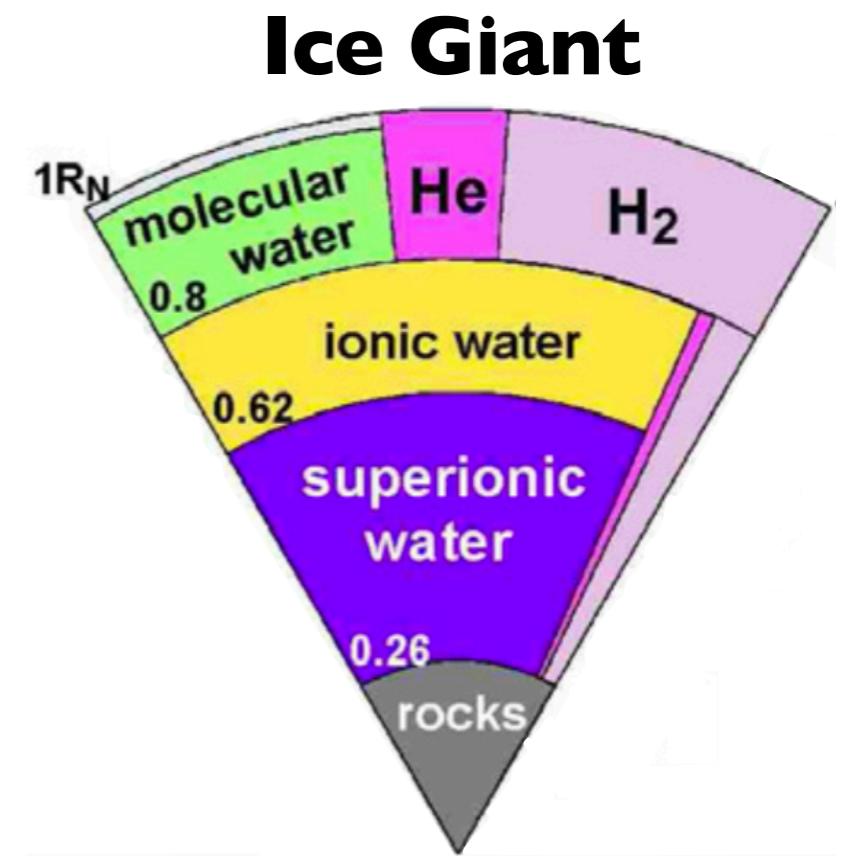
Redmer et al. (2011)

# Numerical Dynamo Models

- Hypothesis Test: Dynamo models that vary the thickness of a stable liquid layer and the size of a solid inner core (Stanley and Bloxham, 2004, 2006)



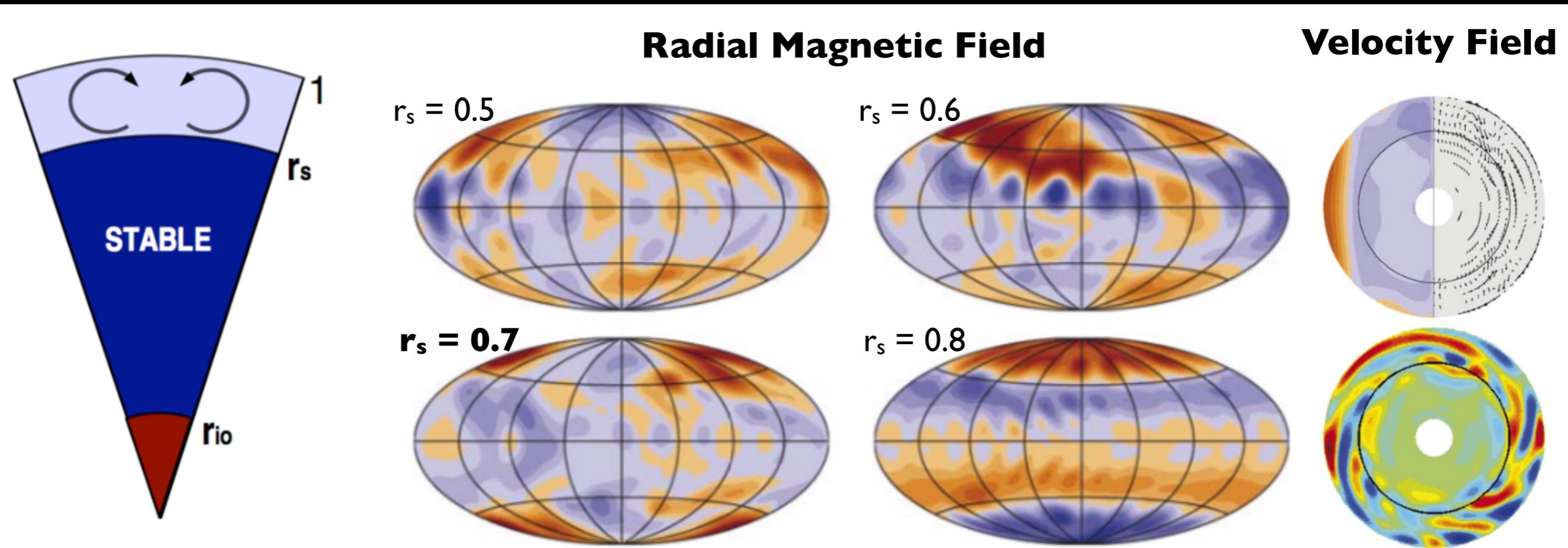
Stanley and Bloxham (2004, 2006)



Redmer et al. (2011)

# Numerical Dynamo Models

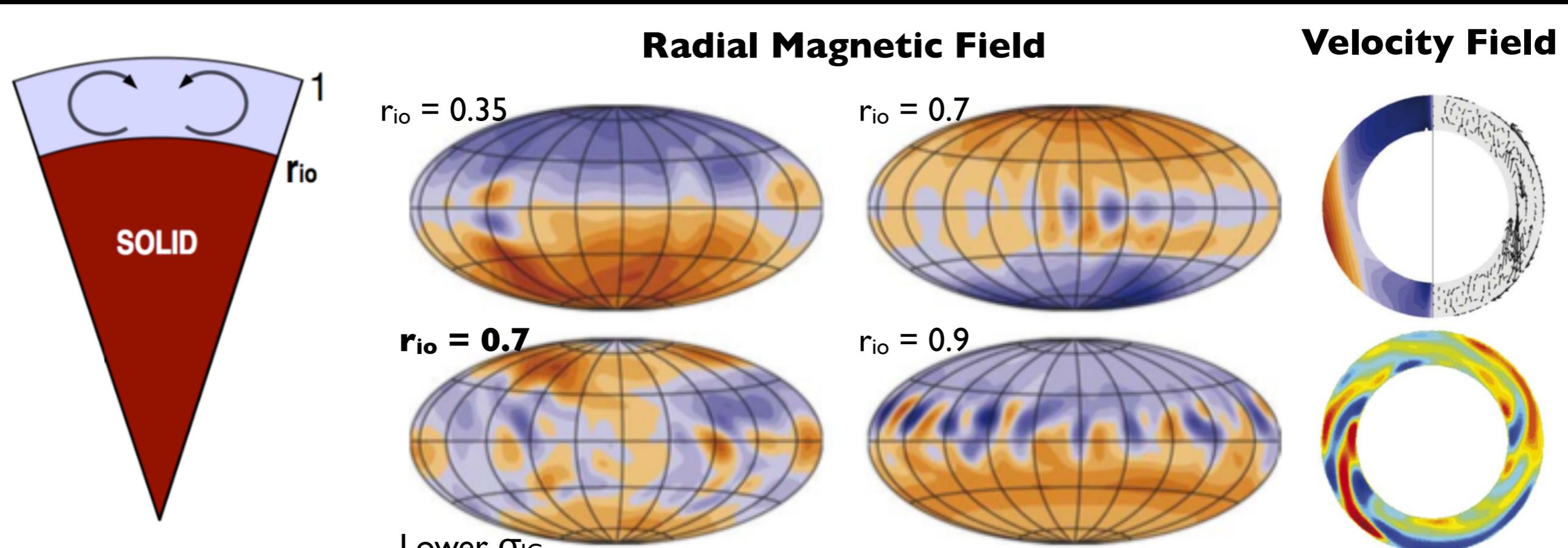
- Models with a thin convective region and stable fluid layer generate multipolar, non-axisymmetric magnetic fields
  - Columnar convection, prograde equatorial jet



Stanley and Bloxham (2004, 2006)

# Numerical Dynamo Models

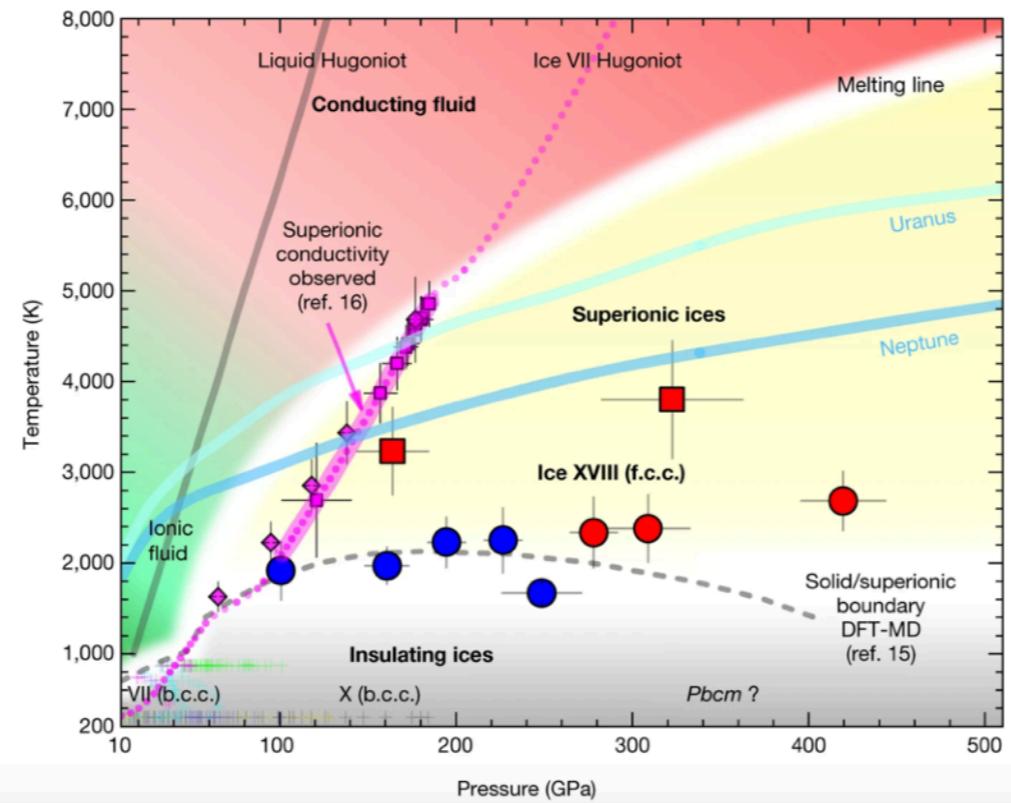
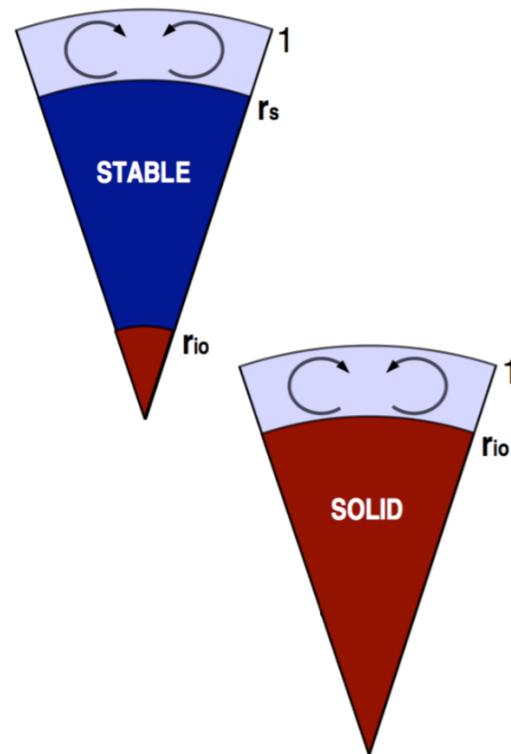
- Models with a thin convective region and solid inner core only generate multipolar, non-axisymmetric magnetic fields if the core has lower conductivity
  - Columnar convection, prograde equatorial jet



Stanley and Bloxham (2004, 2006)

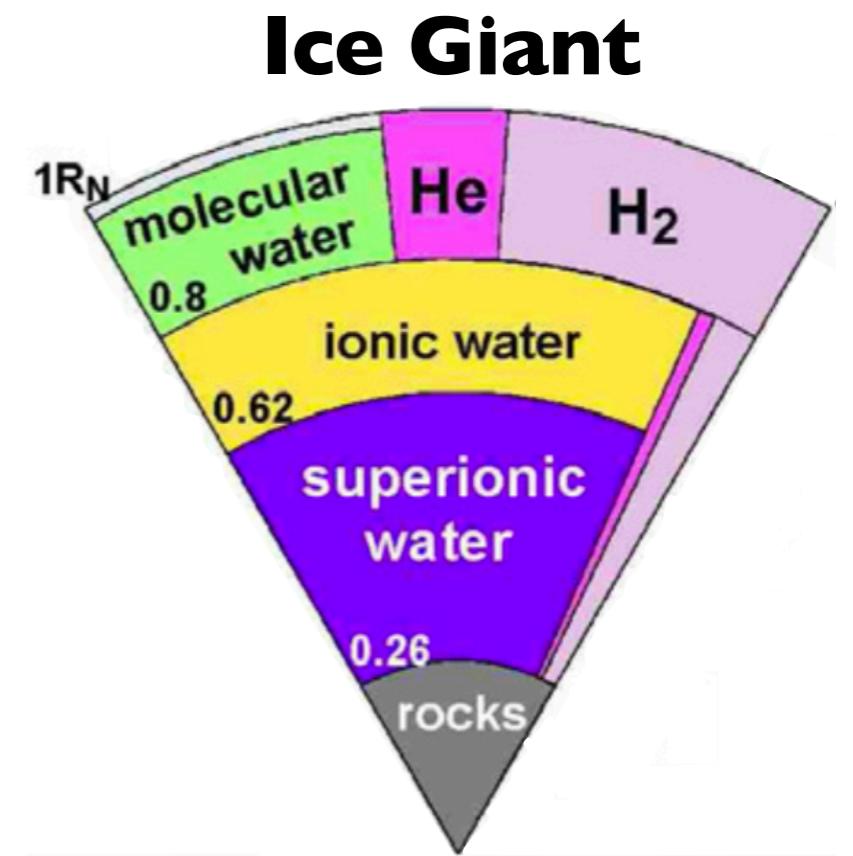
# Numerical Dynamo Models

- Hypothesis: Multipolar dynamos due to convection in a thin shell geometry with deep stable fluid layer or deep weakly conducting solid layer
  - Superionic ices behave similar to a solid (Millot et al., 2019)



Stanley and Bloxham (2004, 2006)

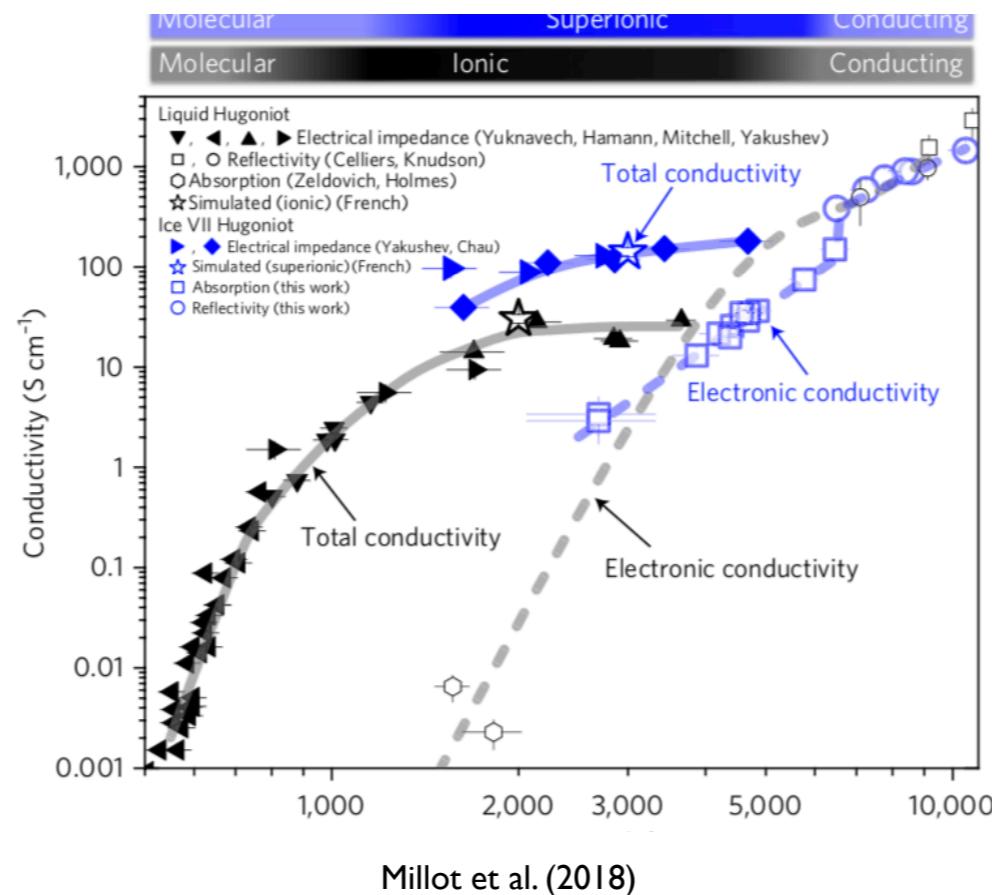
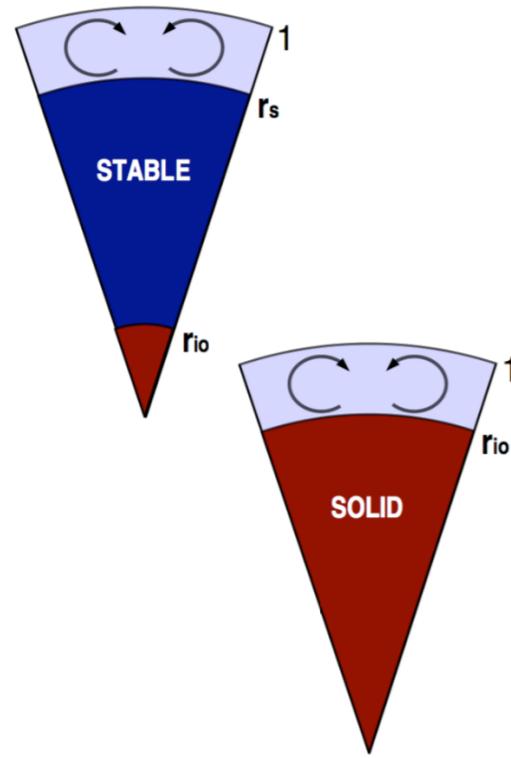
Millot et al. (2019)



Redmer et al. (2011)

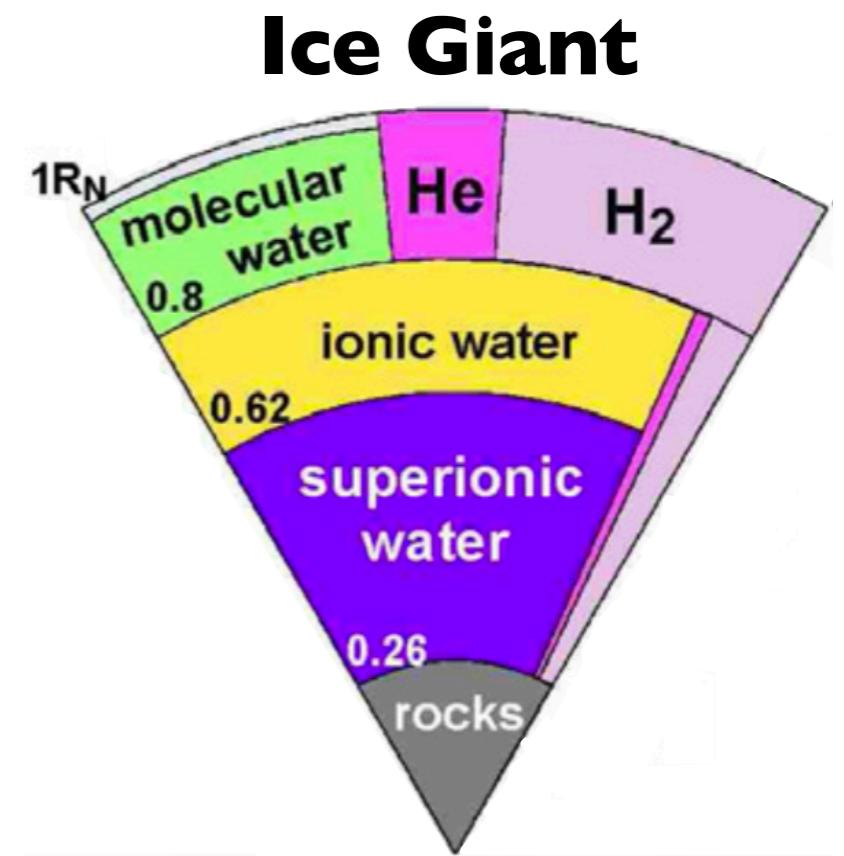
# Numerical Dynamo Models

- Hypothesis: Multipolar dynamos due to convection in a thin shell geometry with deep stable fluid layer or deep weakly conducting solid layer
  - Superionic more conductive than ionic (Millot et al., 2018)



Stanley and Bloxham (2004, 2006)

Millot et al. (2018)

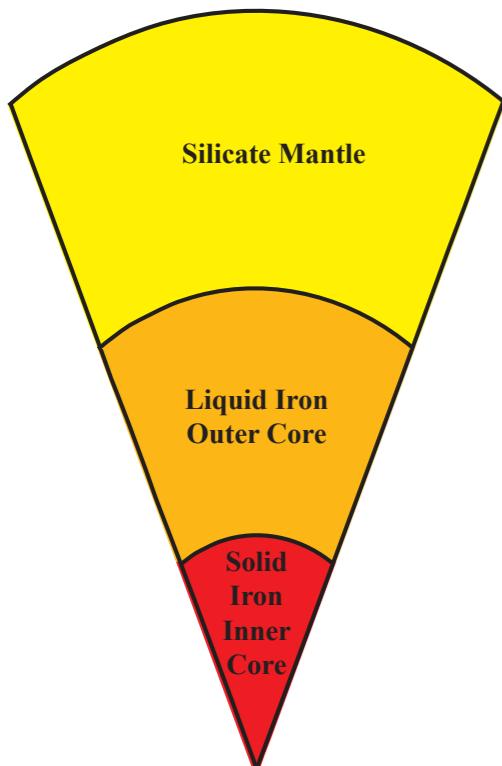


Redmer et al. (2011)

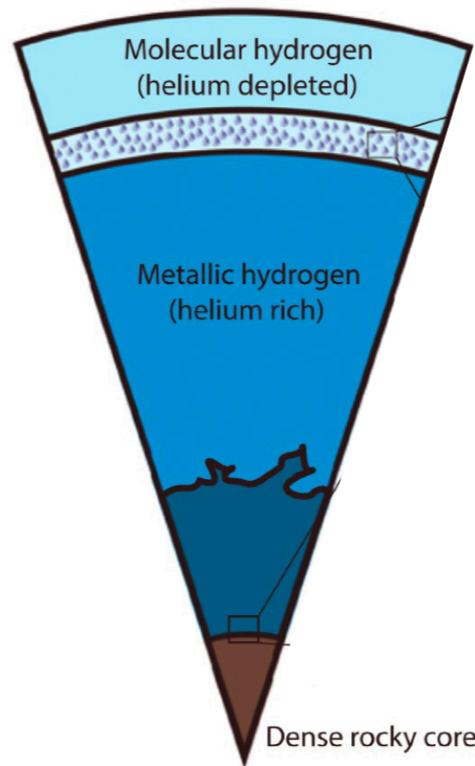
# Magnetic Field Morphology

- Hypothesis: The ice giants have multipolar dynamos because convective turbulence in their interiors is weakly constrained by rotation (Aurnou et al., 2007; Soderlund et al., 2013; King and Aurnou, 2013)

**Terrestrial**

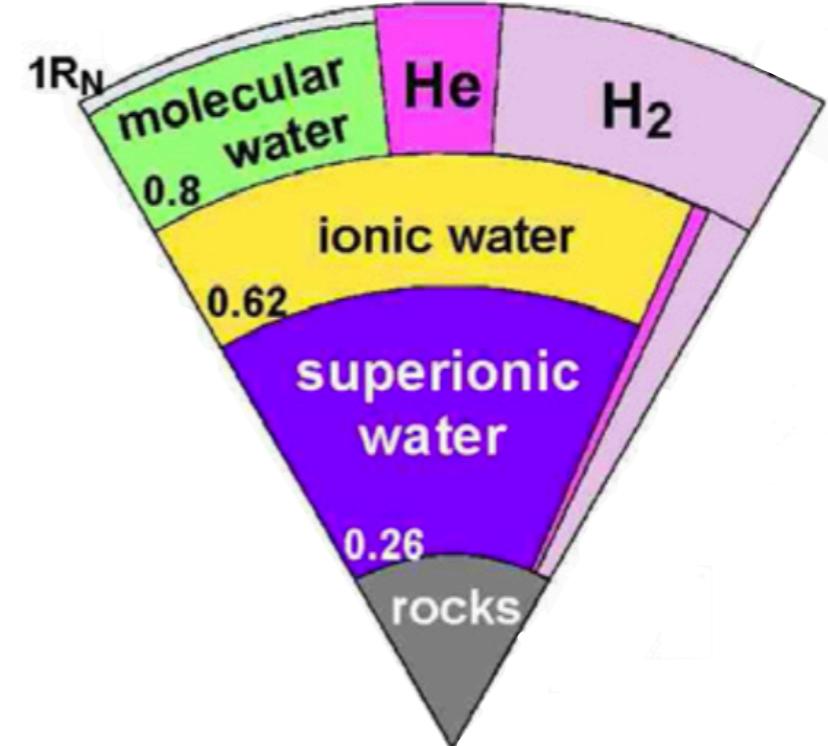


**Gas Giant**



Wahl et al. (2017)

**Ice Giant**

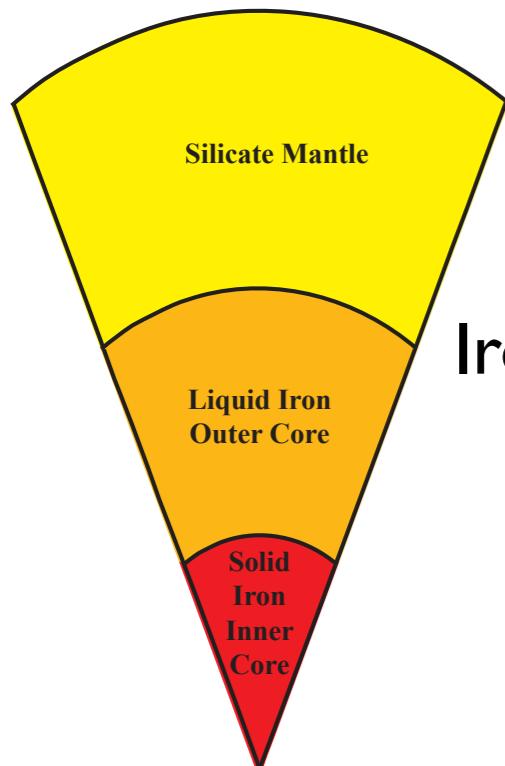


Redmer et al. (2011)

# Magnetic Field Morphology

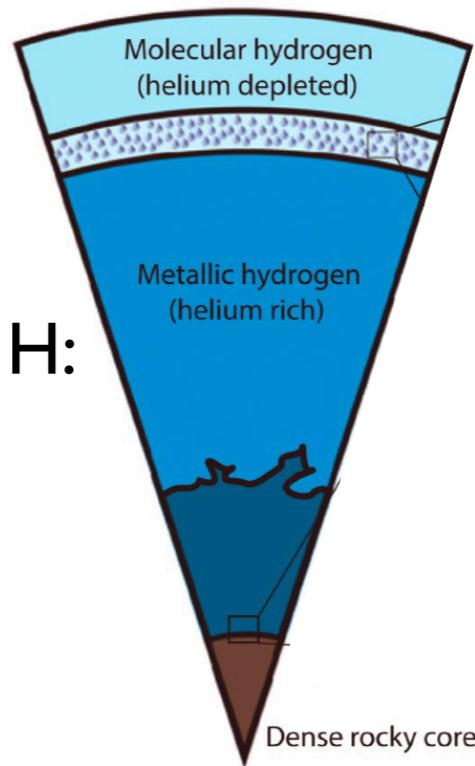
- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities ( $Pr$ )
  - Terrestrial and giant planet dynamo regions are liquid metals vs ionic water in ice giants

**Terrestrial**



Iron, Metallic H:  
 $Pr < 1$

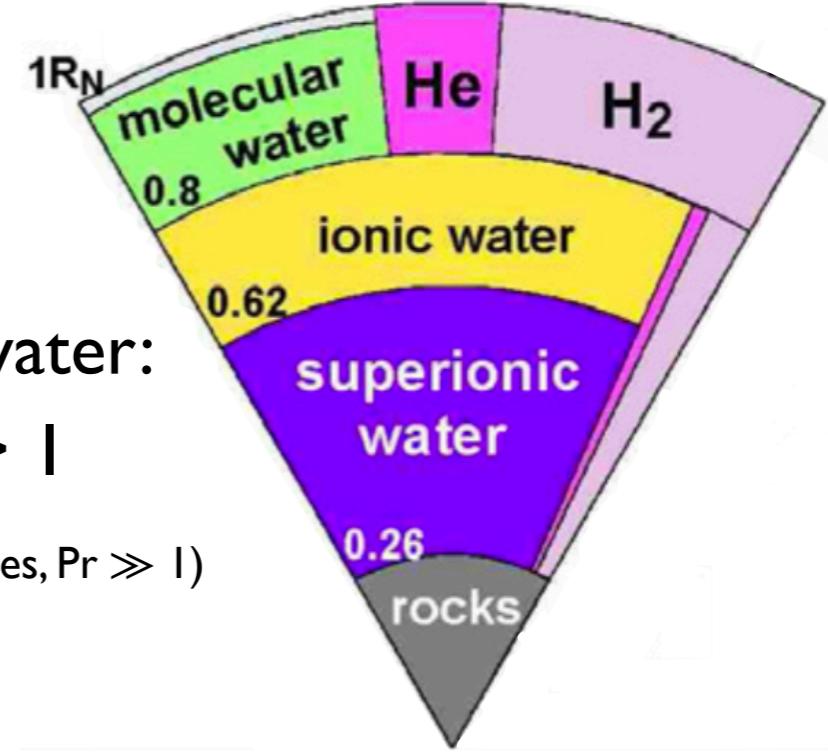
**Gas Giant**



Wahl et al. (2017)

Ionic water:  
 $Pr > 1$   
(mantle silicates,  $Pr \gg 1$ )

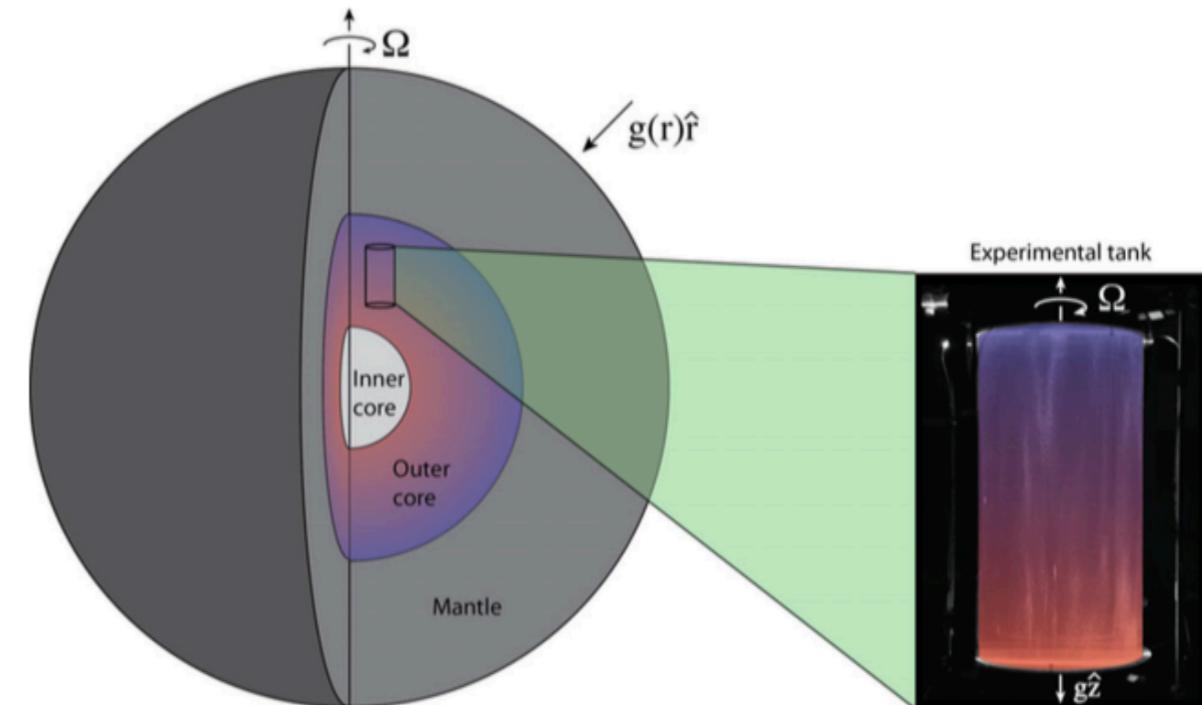
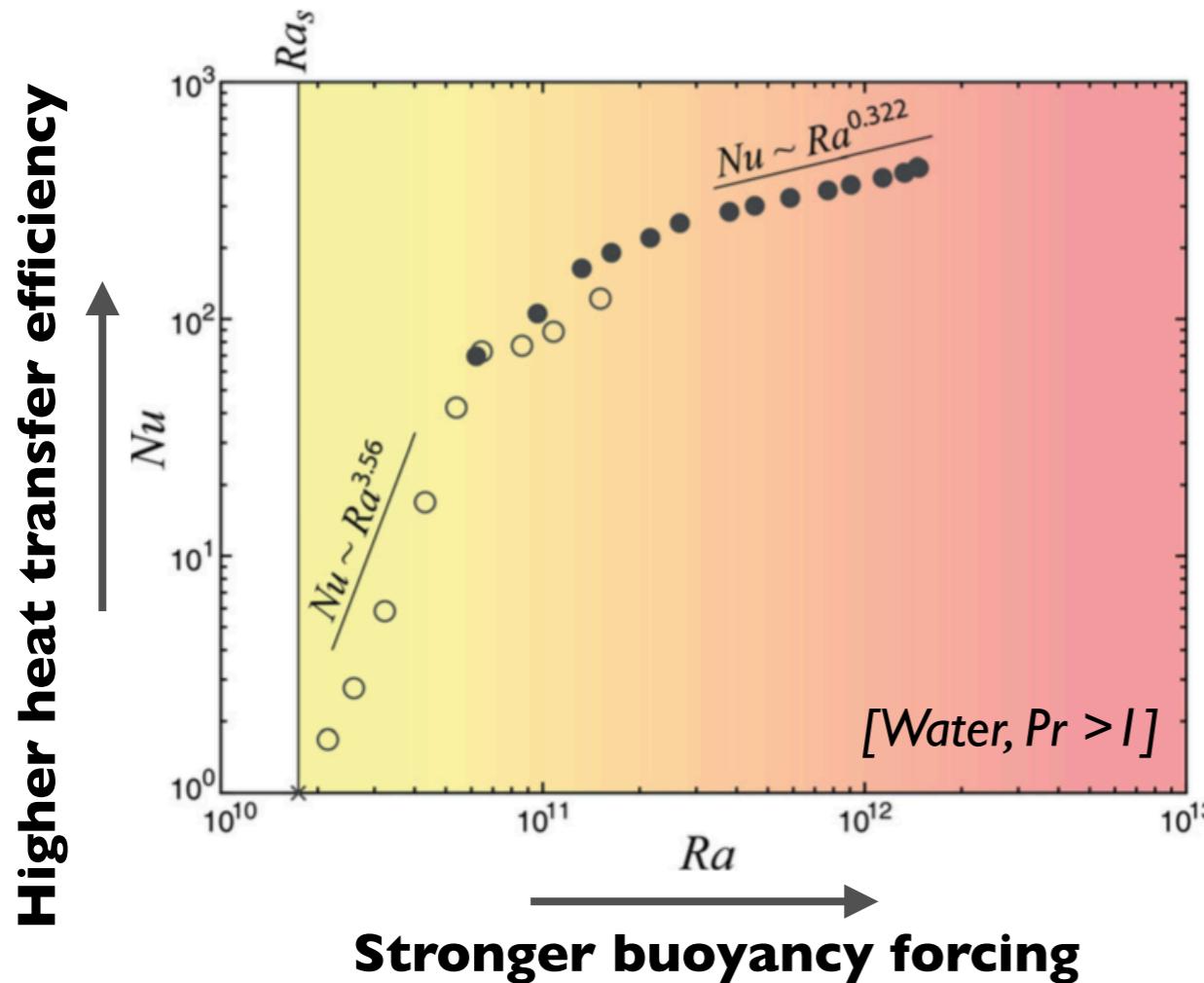
**Ice Giant**



Redmer et al. (2011)

# Magnetic Field Morphology

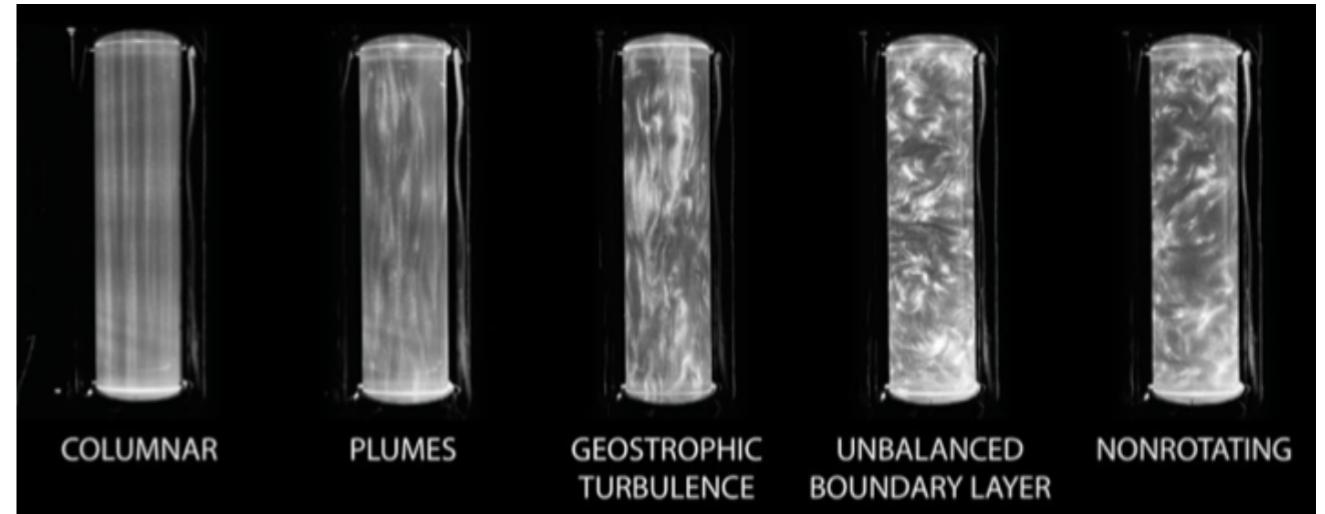
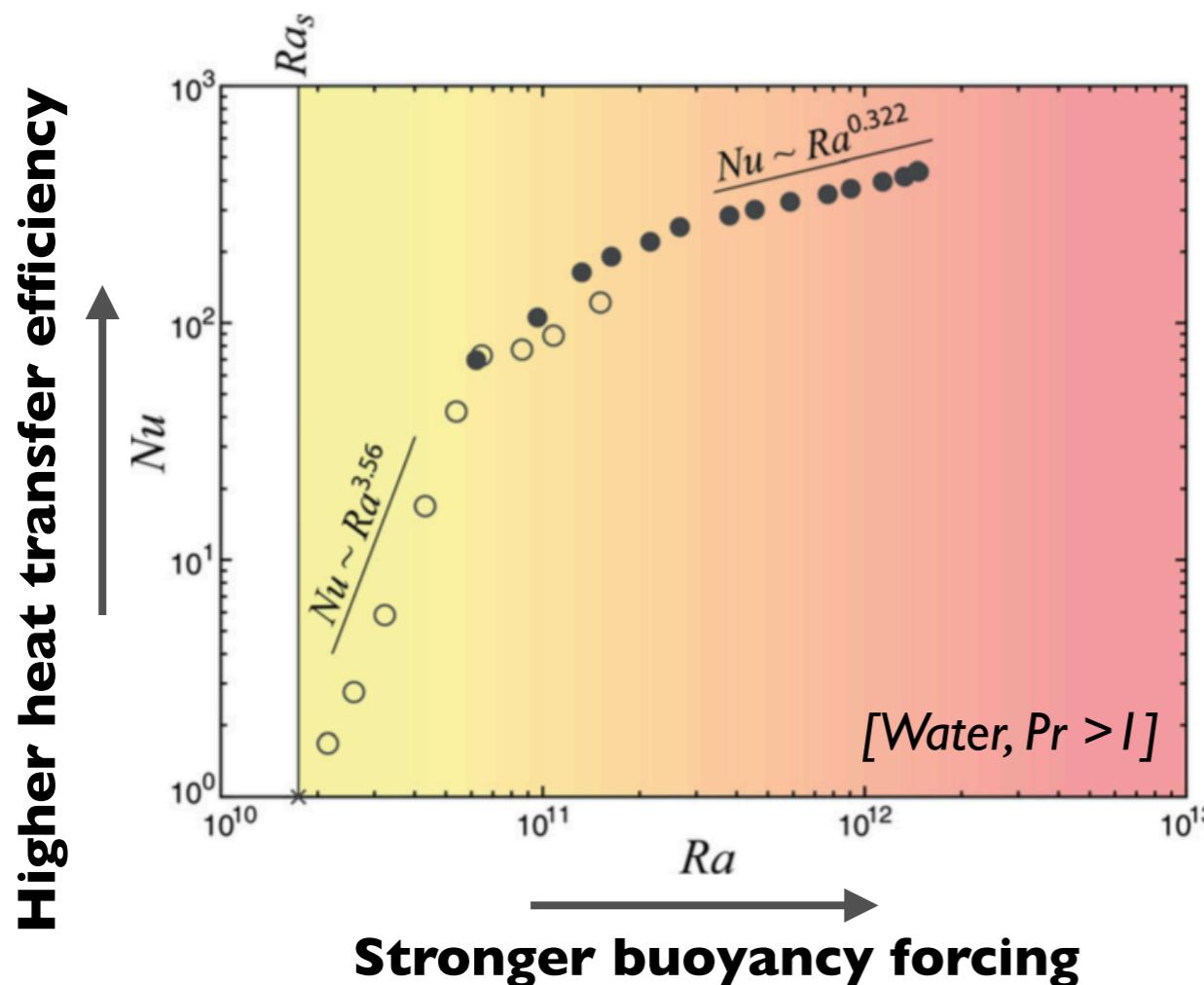
- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities  
(King & Aurnou, 2013)



Cheng et al. (2015, 2018)

# Magnetic Field Morphology

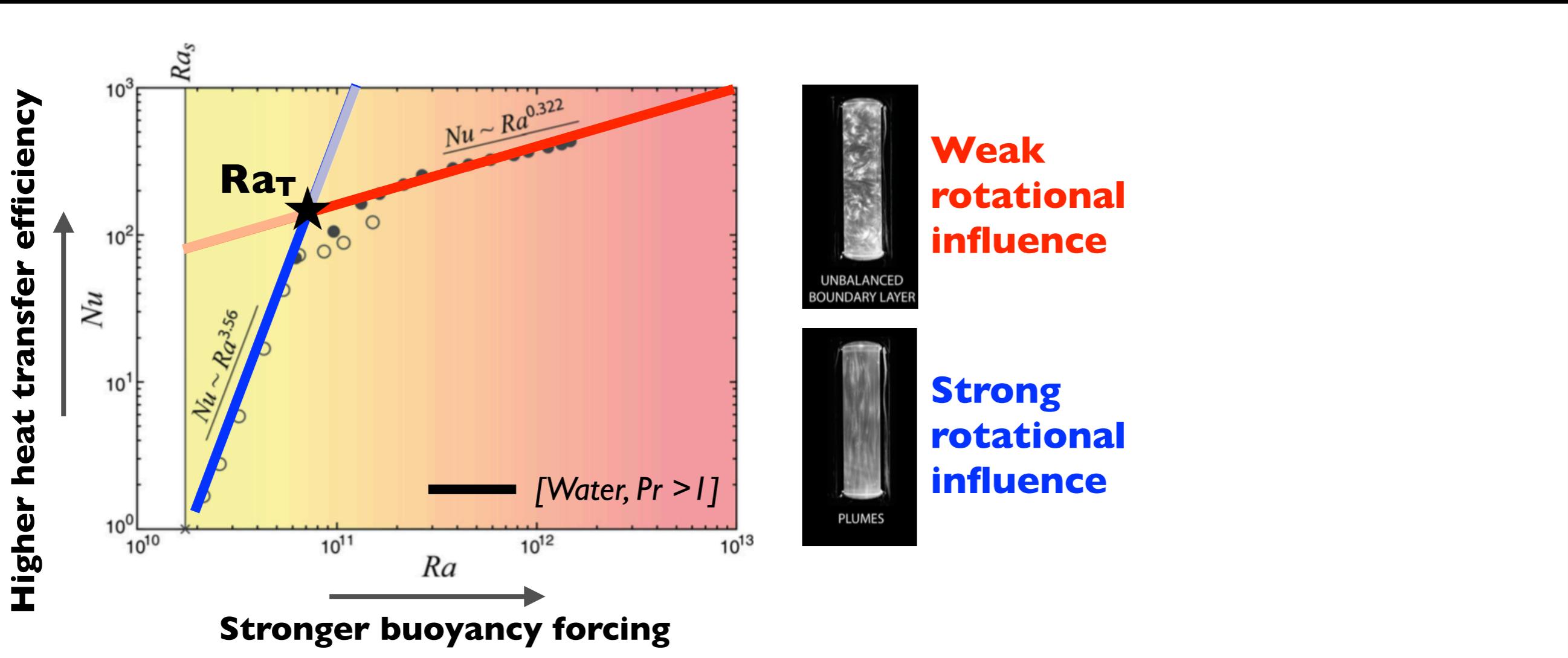
- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities  
(King & Aurnou, 2013)



**Planform of convection changes as the influence of rotation decreases**

# Magnetic Field Morphology

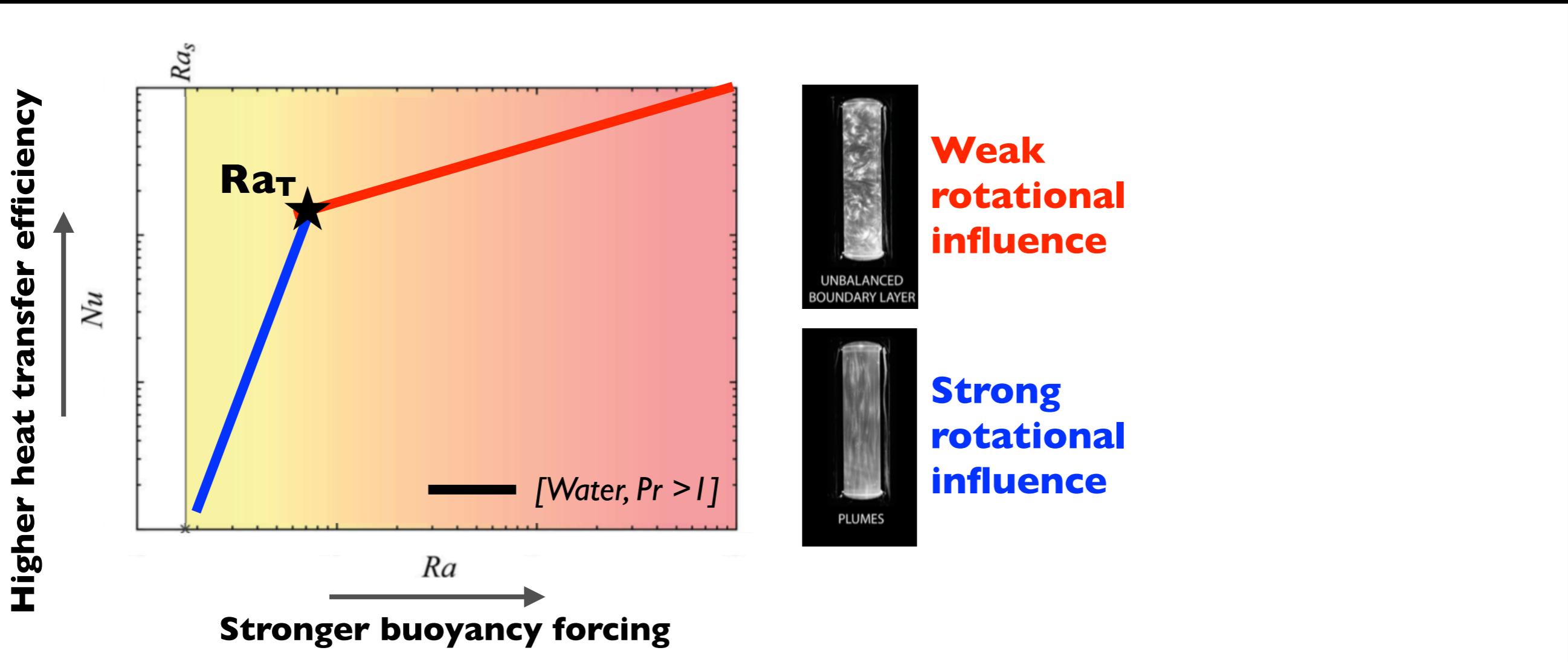
- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities  
(King & Aurnou, 2013)



Cheng et al. (2015, 2018)

# Magnetic Field Morphology

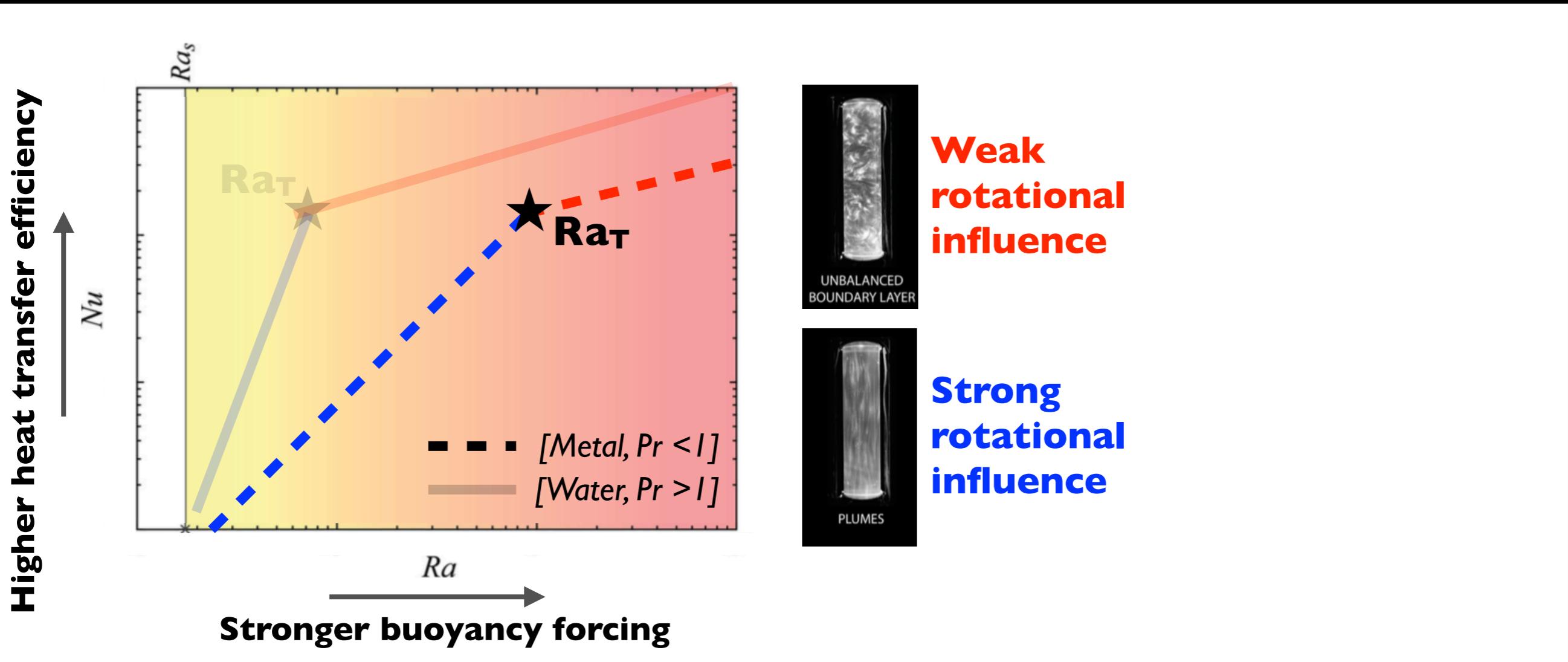
- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities  
(King & Aurnou, 2013)



Cheng et al. (2015, 2018)

# Magnetic Field Morphology

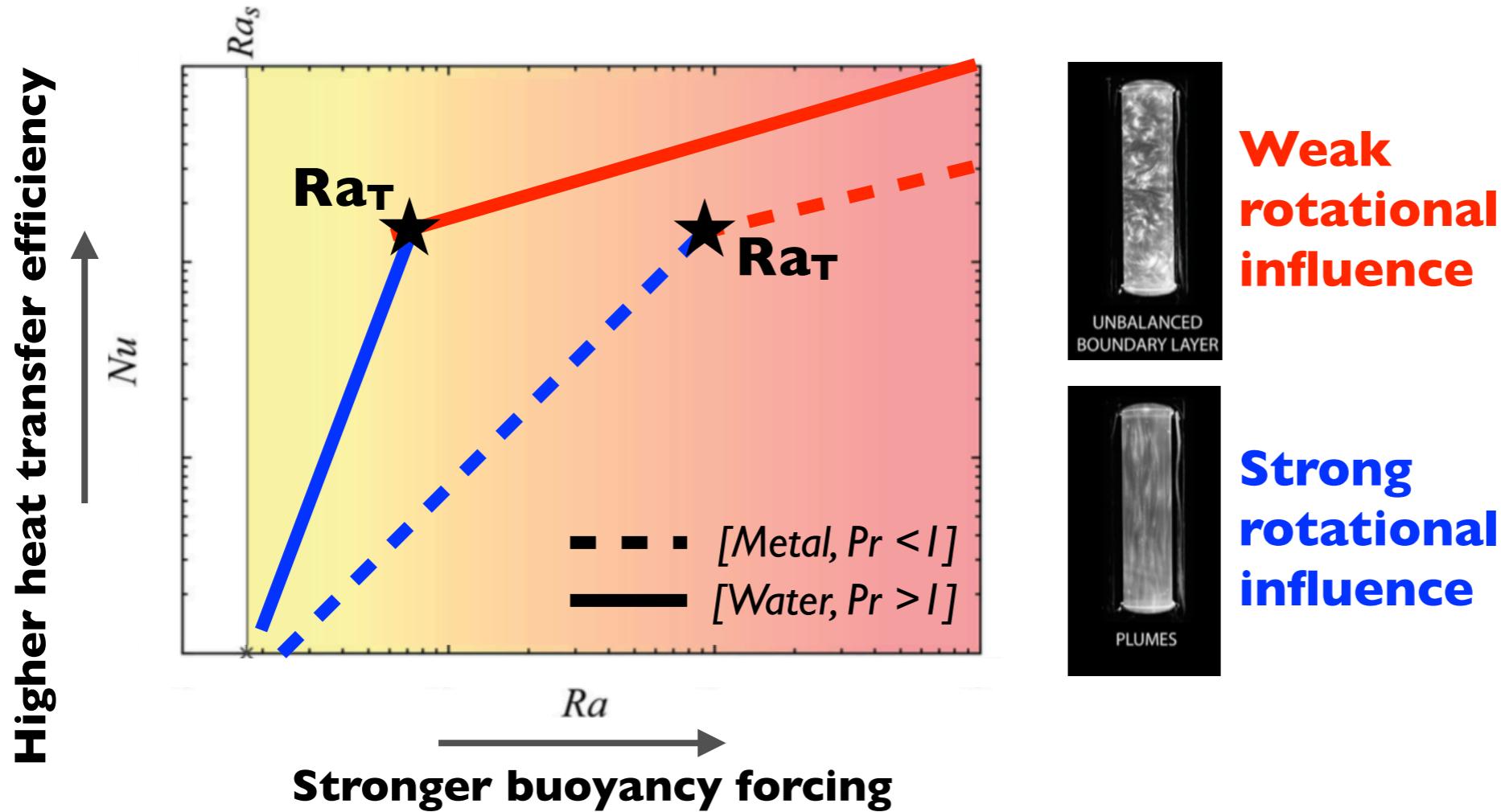
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# Magnetic Field Morphology

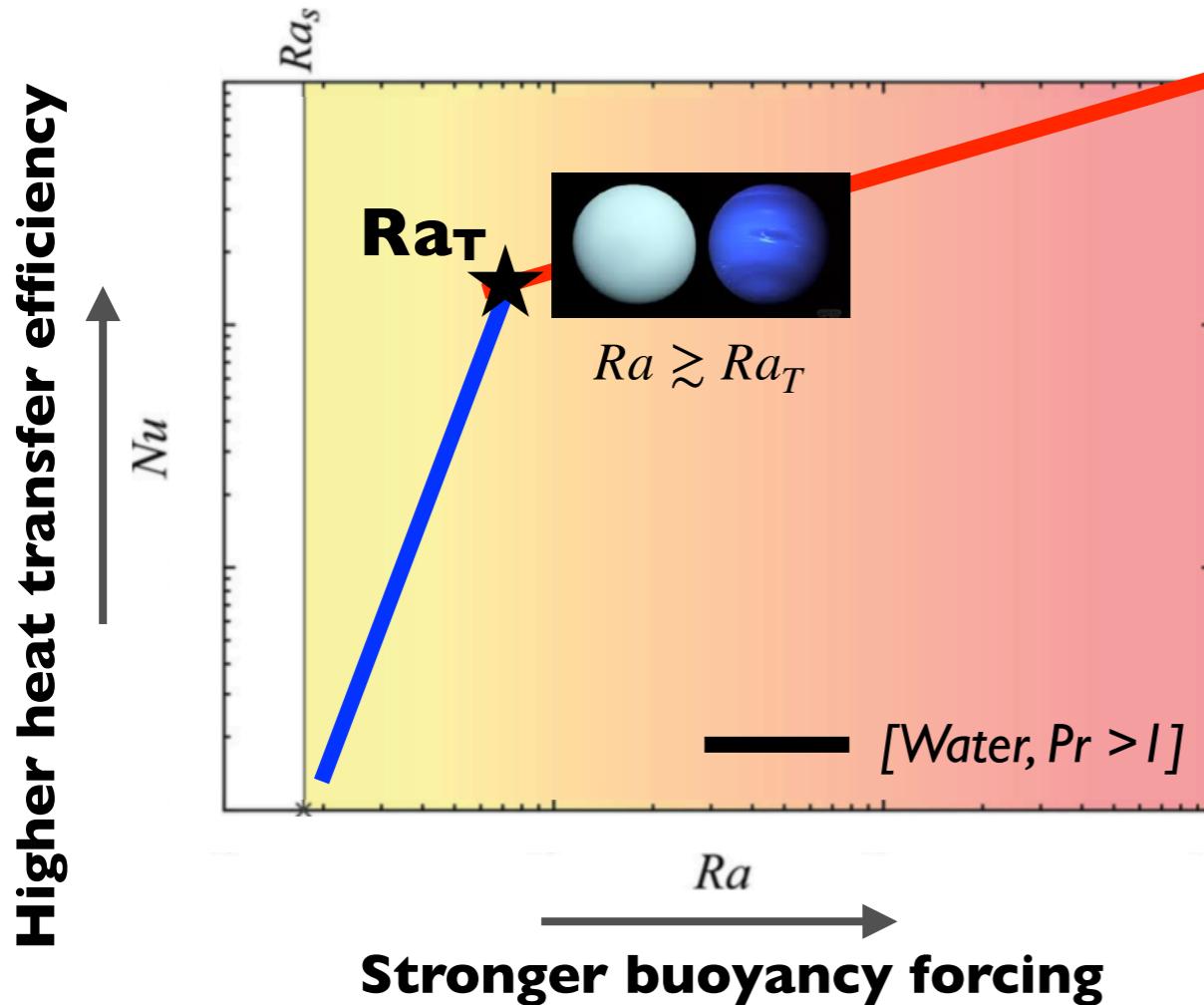
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Transition to weakly rotating convection requires stronger buoyancy forcing for liquid metals

# Giant Planet Dichotomy

- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities  
*(King & Aurnou, 2013)*

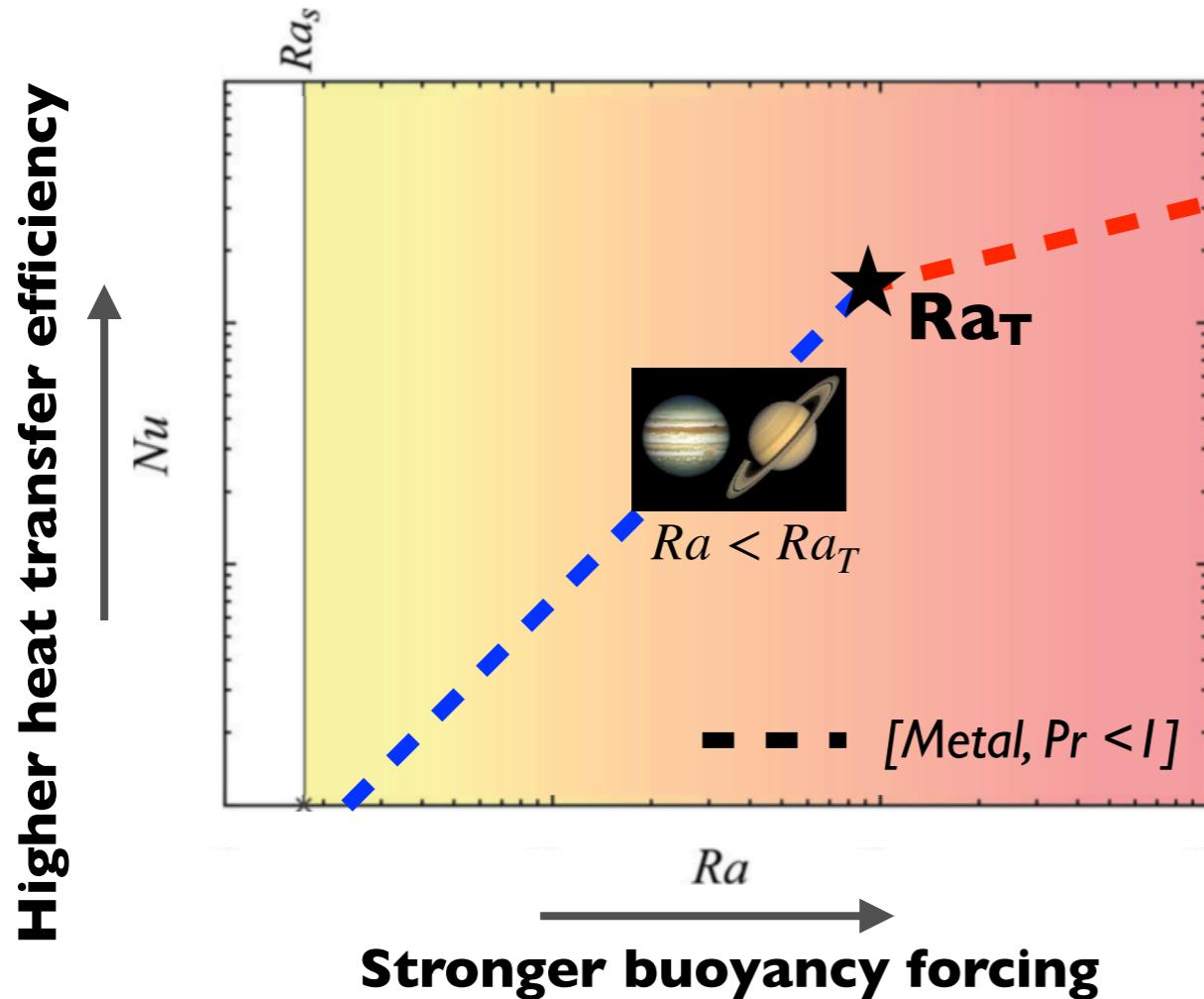


**Weak rotational influence**

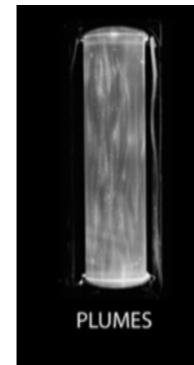
Convection in ice giant interiors is predicted to be weakly constrained by rotation

# Giant Planet Dichotomy

- Heat transfer efficiency regime transition depends on the ratio of momentum/thermal diffusivities  
(King & Aurnou, 2013)



Convection in gas giant interiors is predicted to be strongly constrained by rotation

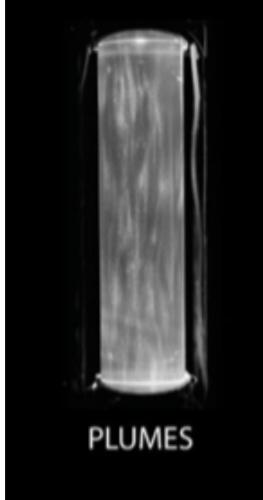


**Strong rotational influence**

# Giant Planet Dichotomy

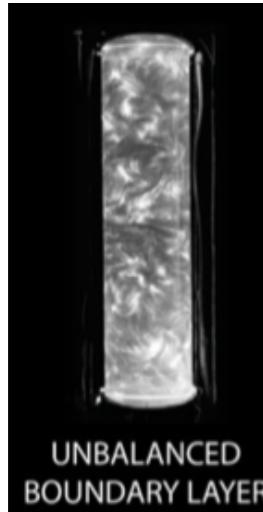
- The ice giants may have unique magnetic field characteristics because of differences in their convective regimes compared against the gas giants

## Gas Giants



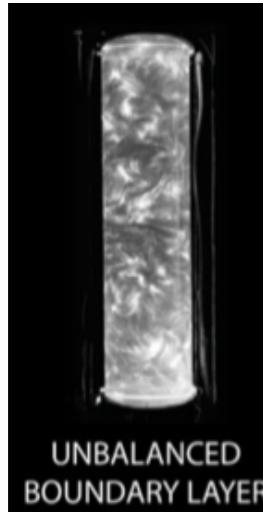
**Strong  
rotational  
influence**

Convection strongly constrained by rotation  
will generate gas giant-style dynamos



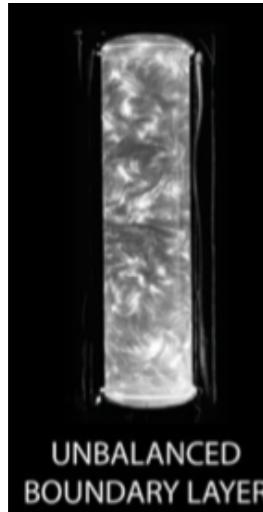
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rotational  
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**Weak  
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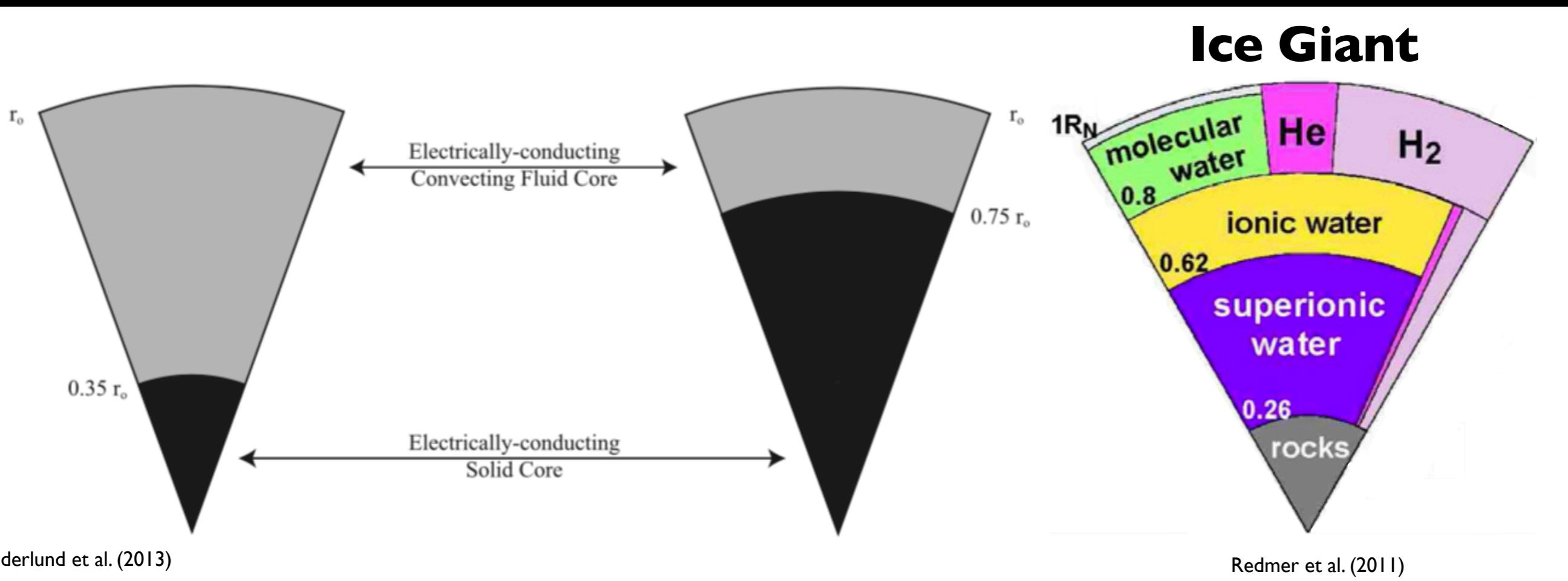
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## Ice Giants

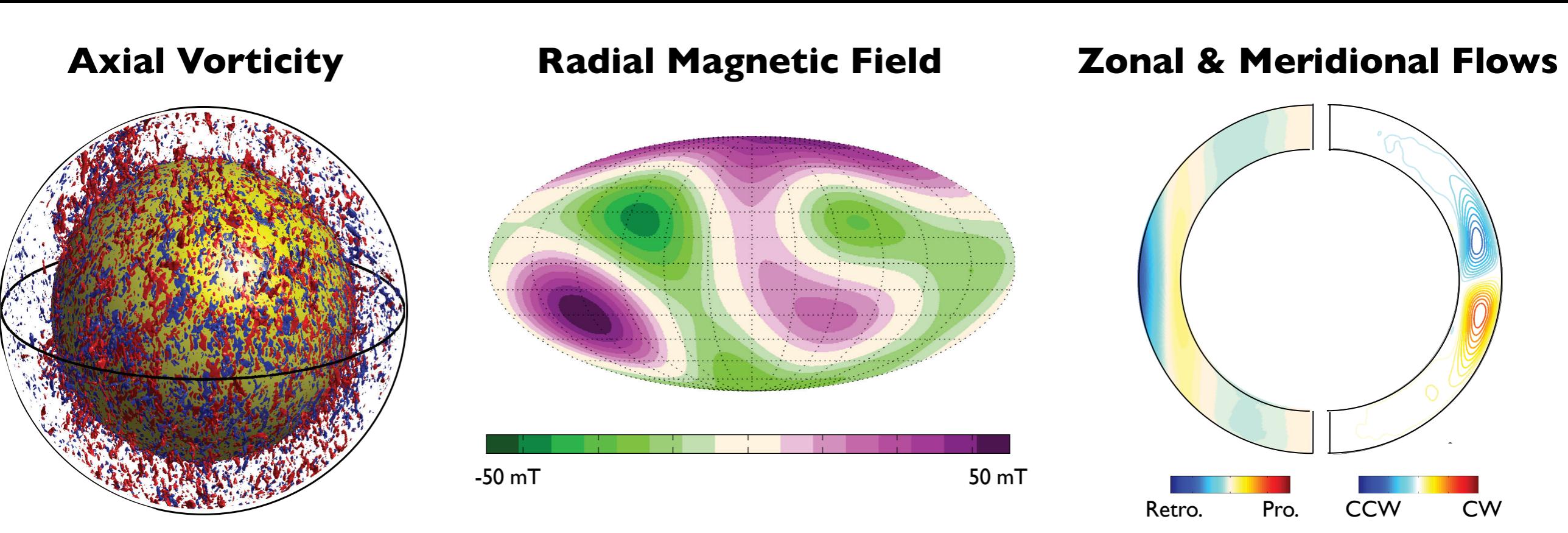
# Numerical Dynamo Models

- Hypothesis Test: Dynamo models with convection weakly constrained by rotation and different inner core sizes (Soderlund et al., 2013)



# Numerical Dynamo Models

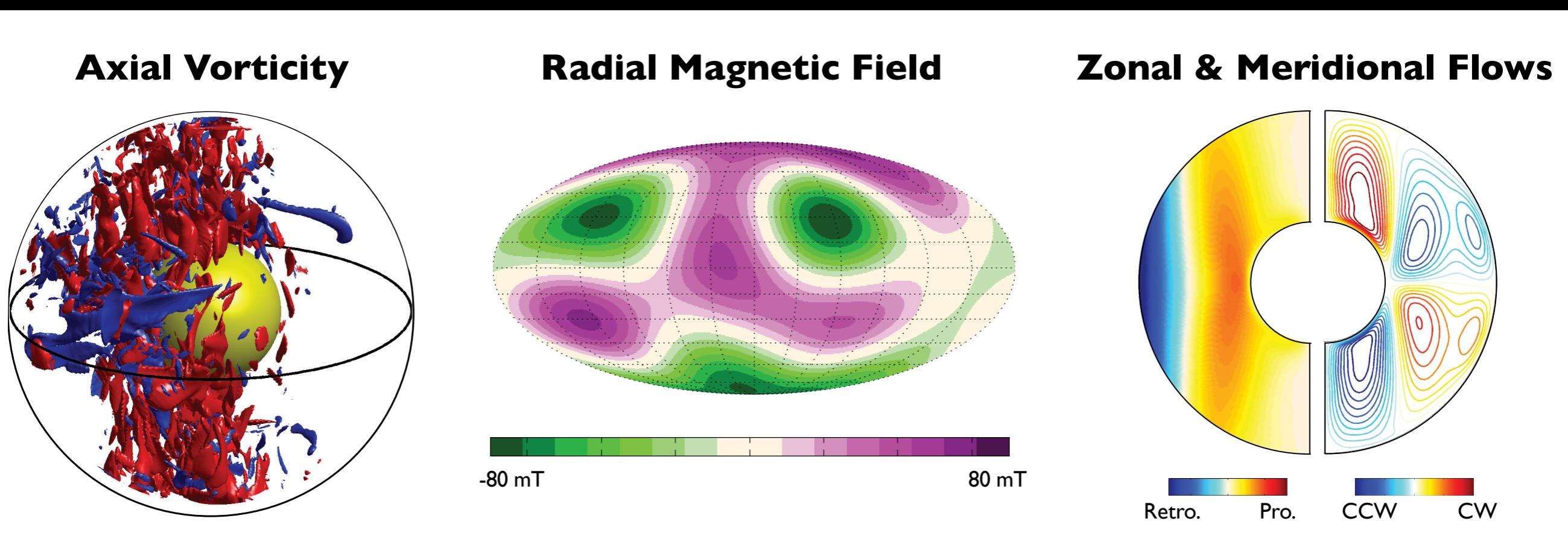
- Models with a thin convective region, solid inner core, and 3D turbulence generate multipolar, non-axisymmetric magnetic fields
    - Retrograde zonal jet, Hadley-like circulation cells



Soderlund et al. (2013)

# Numerical Dynamo Models

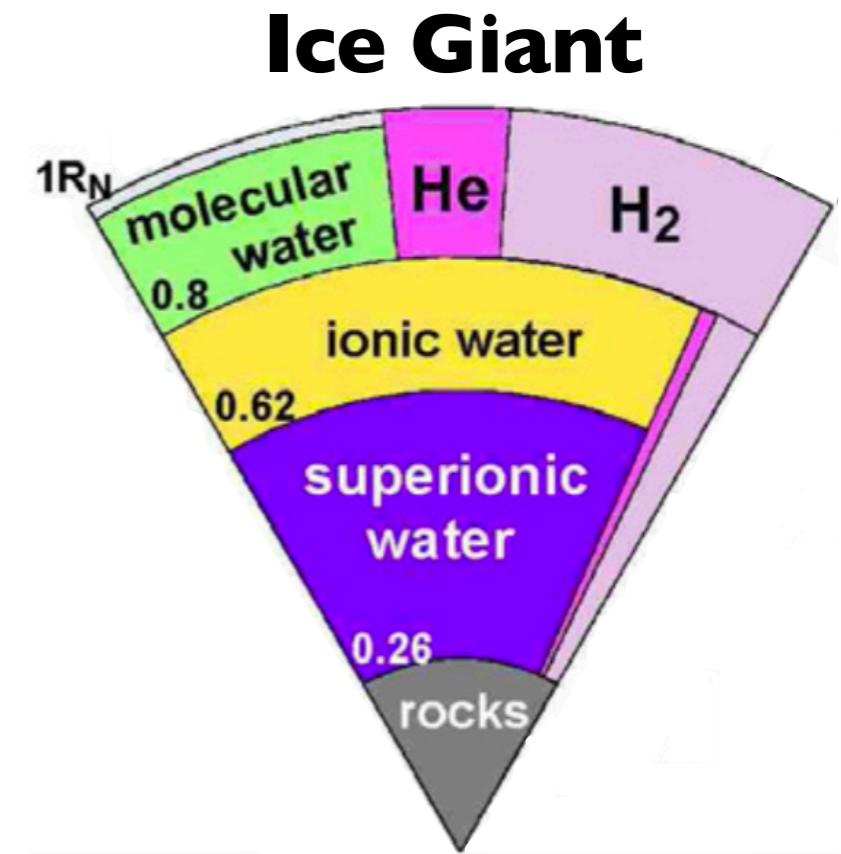
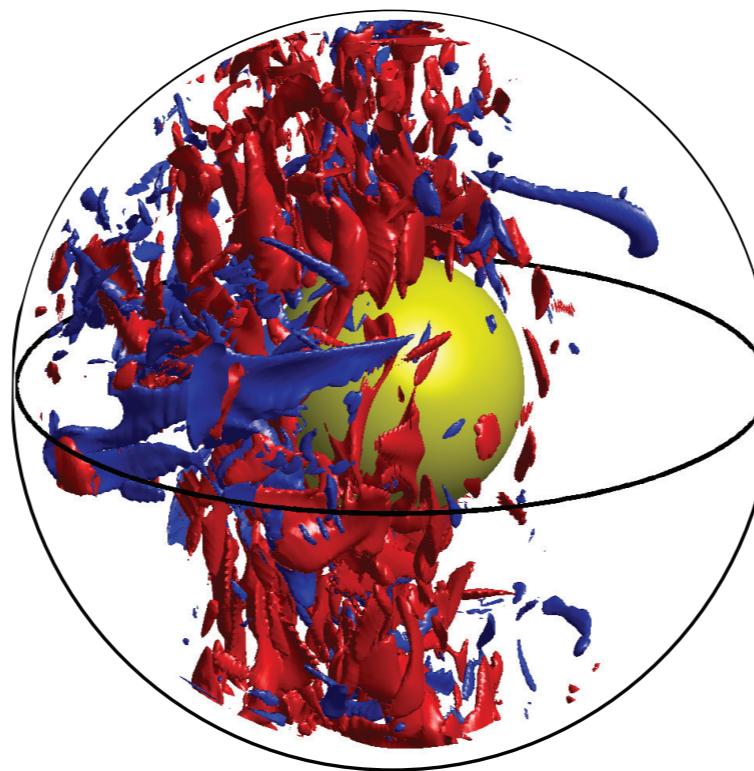
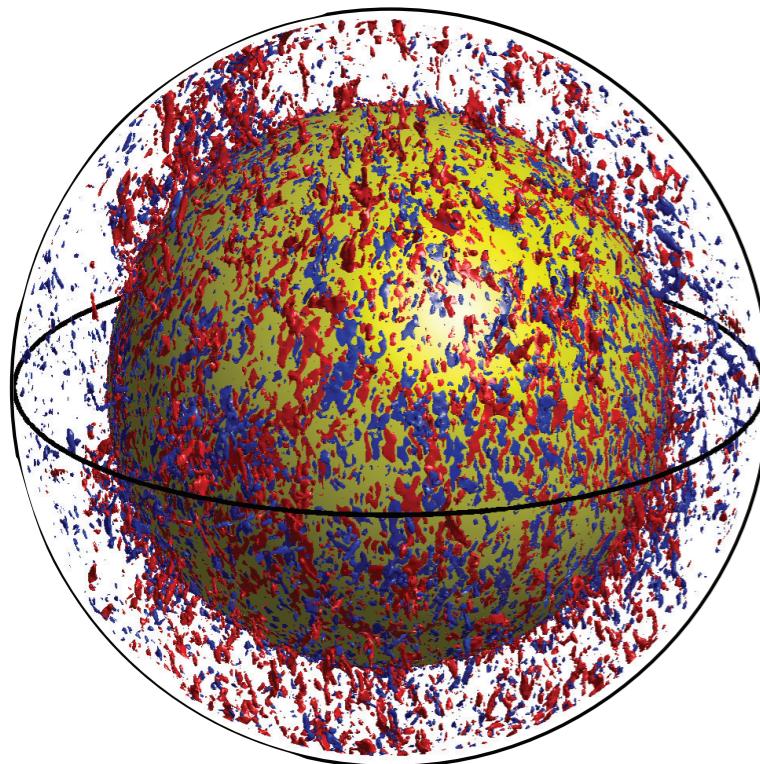
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Soderlund et al. (2013)

# Magnetic Field Morphology

- ✓ Hypothesis: The ice giants have multipolar dynamos because convective turbulence in their interiors is weakly constrained by rotation (Aurnou et al., 2007; Soderlund et al., 2013; King and Aurnou, 2013)



# Giant Planet Dynamos

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- Theoretical, laboratory, and numerical modeling are useful tools for studying planetary magnetic fields
  - Magnetic field strength for both planets and stars generally consistent with energy flux scaling law
  - Diversity of magnetic field morphologies appears to be a consequence of differences in dynamo source regions
    - Convection in a thin shell geometry with deep stable fluid layer or deep weakly conducting solid layer
    - Convection that is weakly constrained by rotation, regardless of shell geometry

# Outline

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- 1) Planetary Magnetic Fields
- 2) Ice Giant Dynamos
- 3) Looking Ahead

# Looking Ahead

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- A new ice giant mission, combined with advances in material properties and fluid dynamic theory, would provide additional constraints on dynamo models and test their predictions
- Determine the configuration of the intrinsic magnetic field (*magnetic field magnitude, morphology, and variability*)
- Constrain the structure, composition, and dynamics of the interior (*gravitational moments, magnetic field, planetary oscillations, internal heat flux maps, radial electrical conductivity and rheology profiles*)