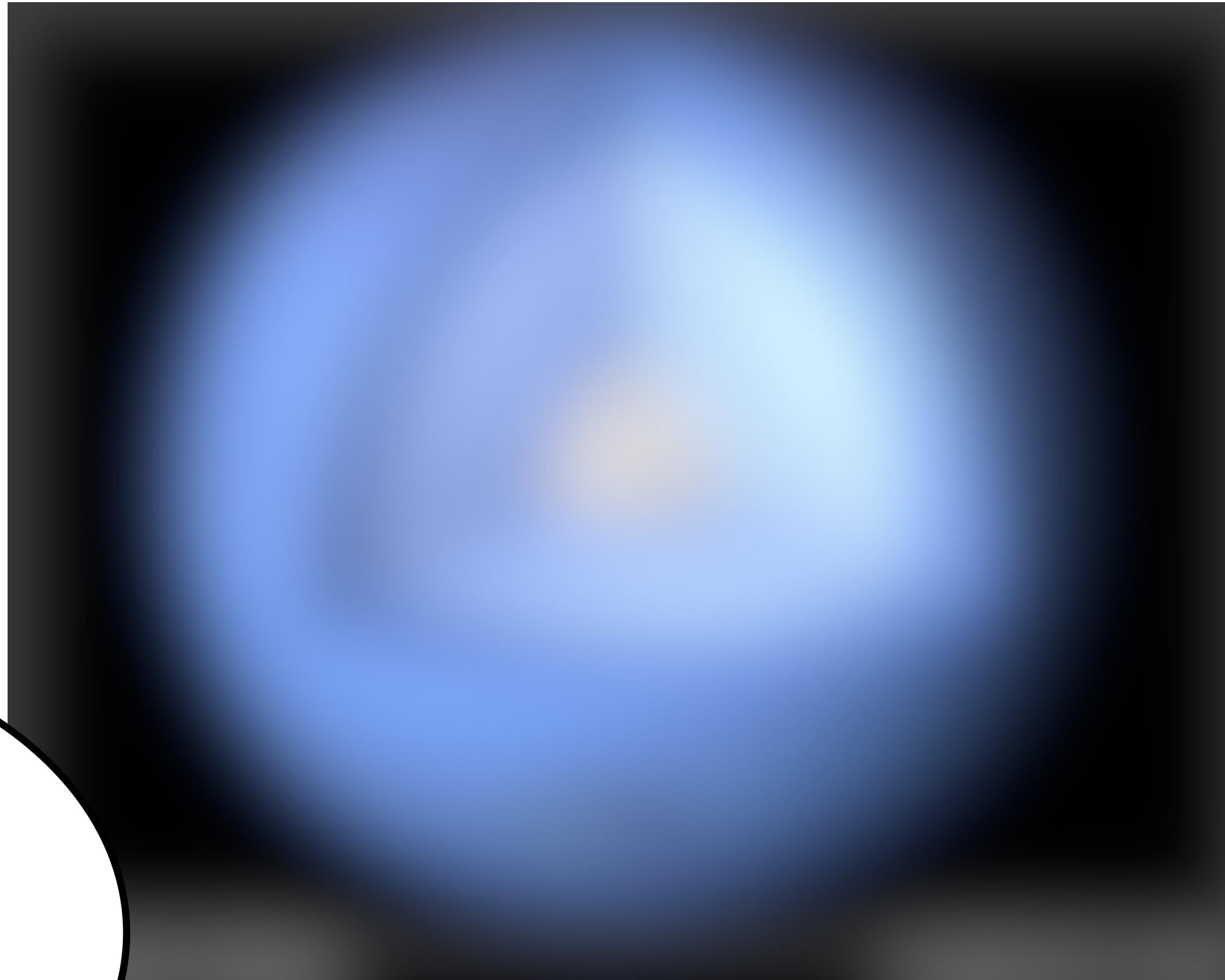


# Interior Structure and Energy Balance of Uranus and Neptune



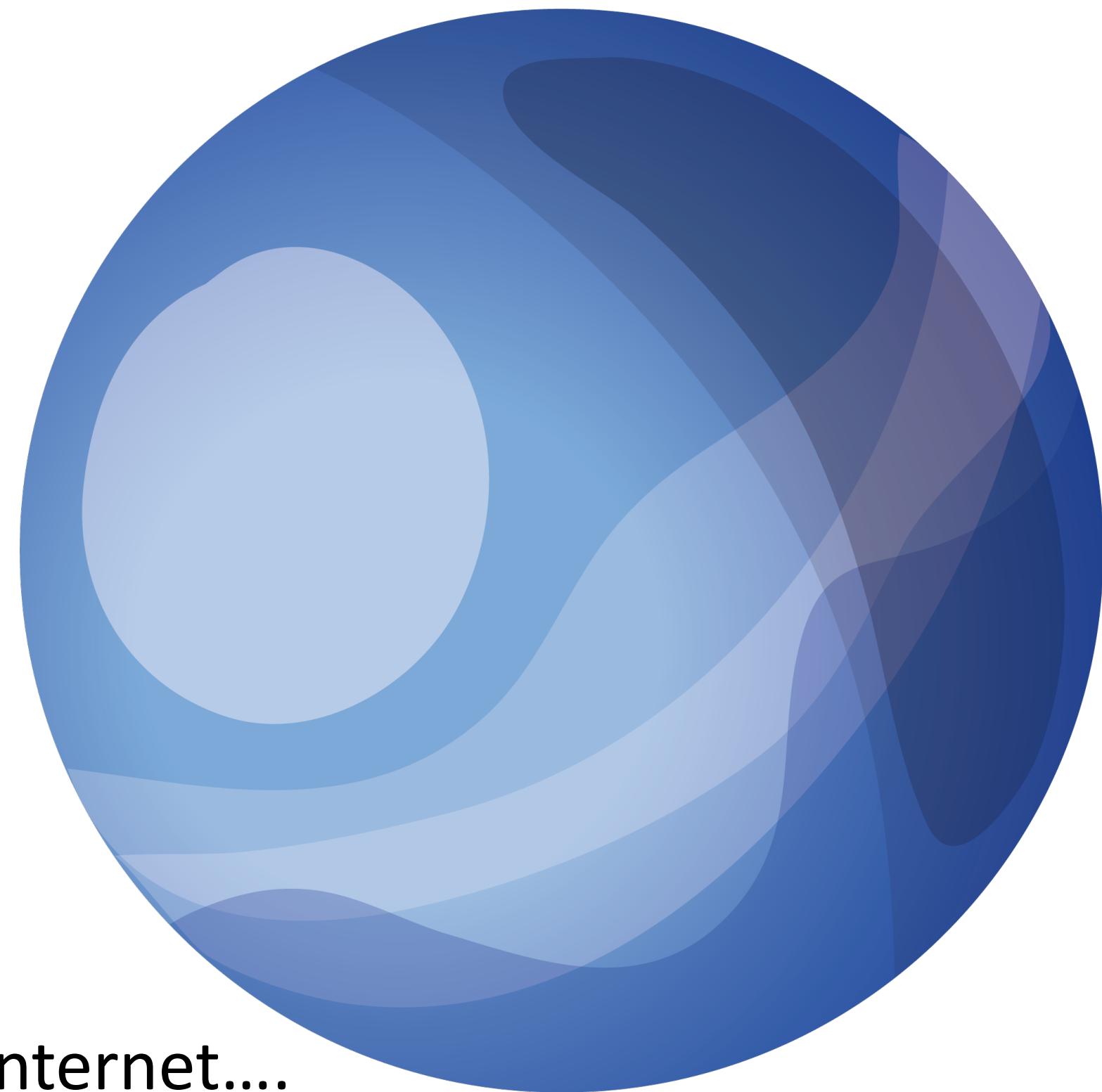
Jonathan Fortney  
OWL, University of California, Santa Cruz

# Talk Outline

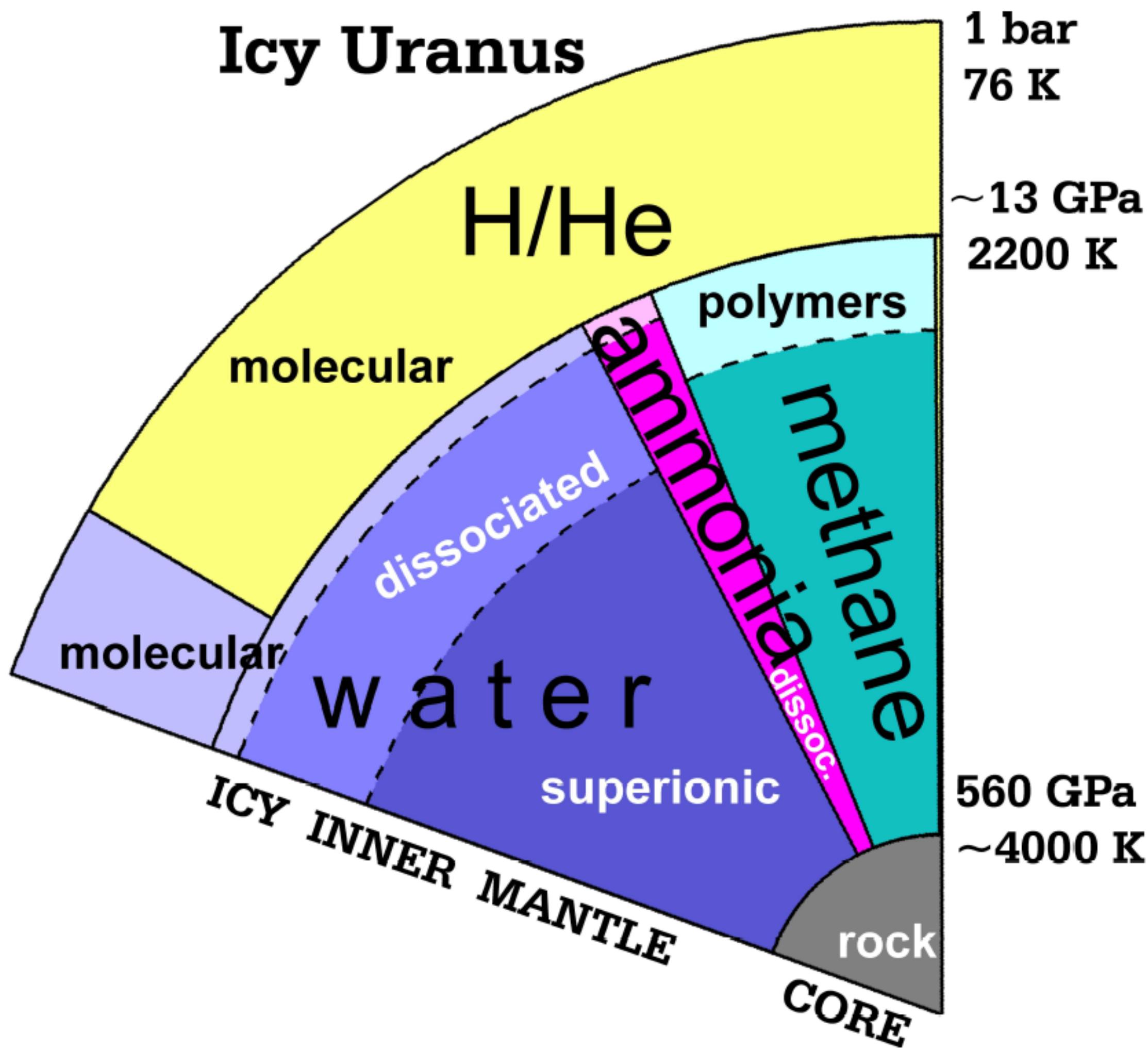
- Interior Structure Models and Their Current Limitations
- Heat Flow Measurements and Their Implications for the Planets
- What can we measure or calculate to improve the situation?



Fun clip art from the internet....

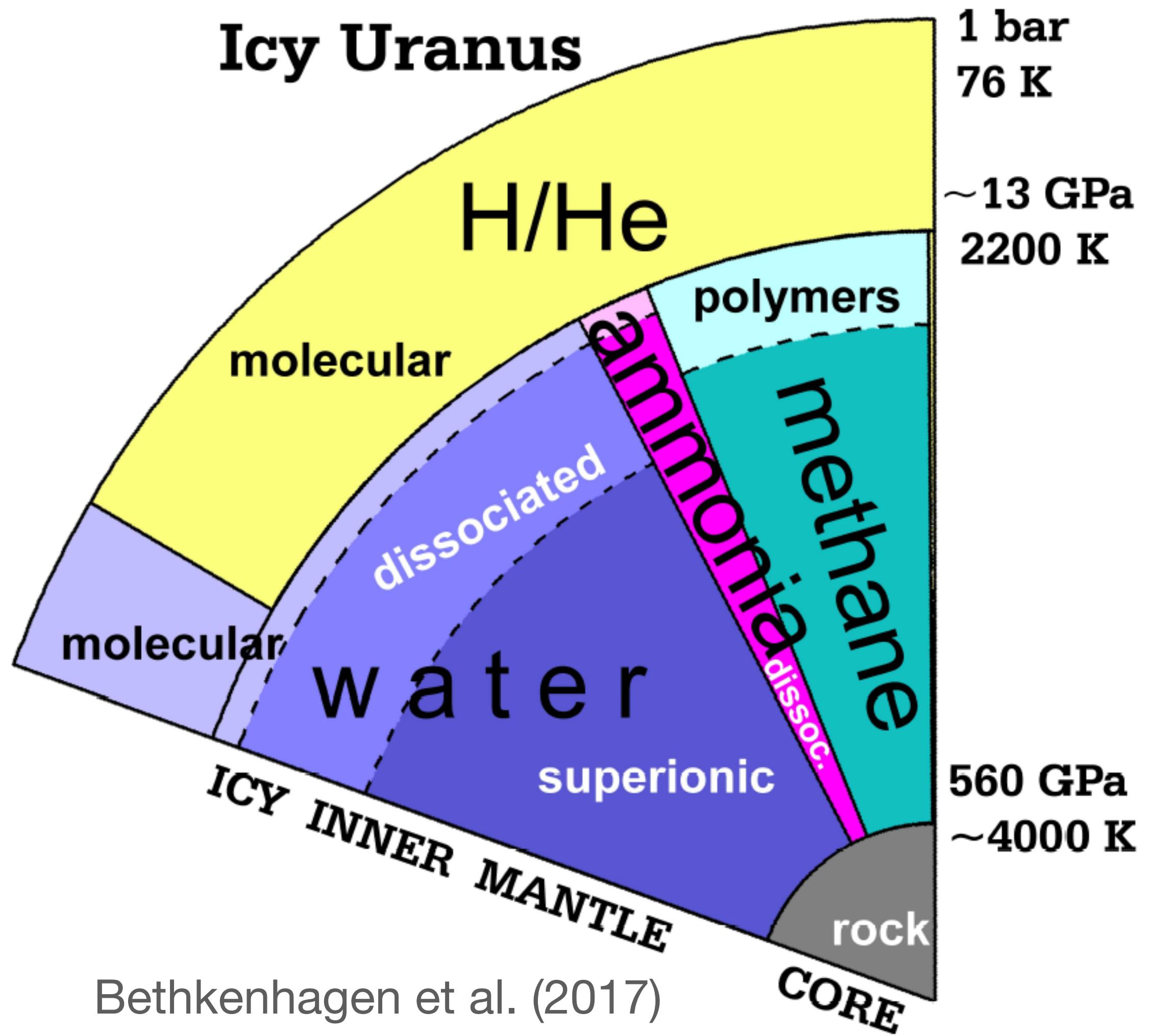


# Interior Models: Vital Points



- 3-layer structure paradigm
  - H/He layer, atop fluid ice layer, atop rocky core
  - Nice visual!
- Outer layers denser than H/He — significant “metal” enrichment
- Inner layers typically a bit less dense than ices
- Are layers real anyway?
  - Model assumptions / convenience important in our “understanding”

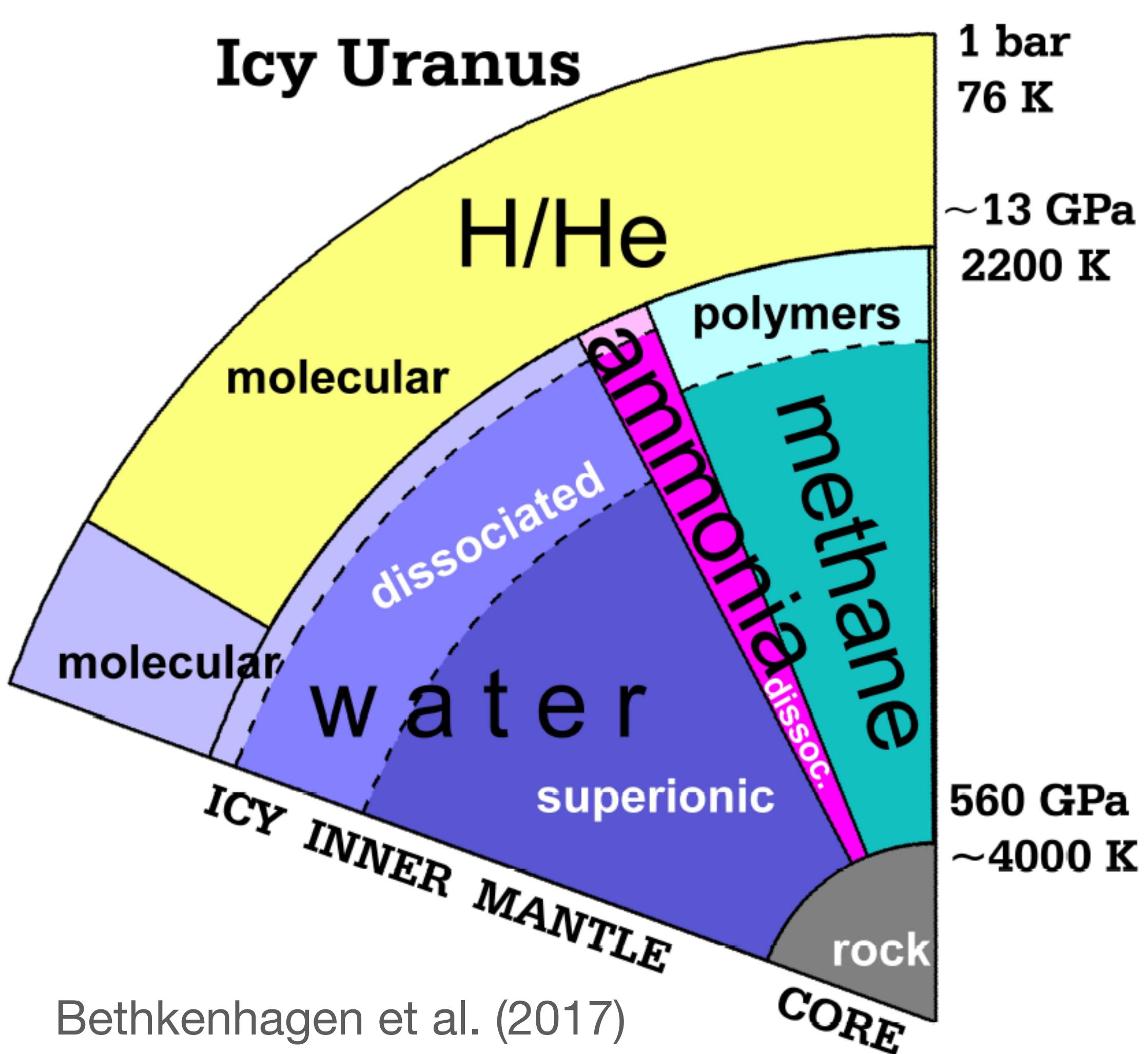
# Interior Models



- Bulk densities of both planets suggest “watery” interiors
  - But high pressure rock + H/He can also mimic density of water
- Standard models find interior ice:rock ratios of ~3:1 to 20:1 (!)
  - Very strongly suggests that such a simple picture is not reality
  - Icy satellites suggest more like 1:1?
  - (Pluto is 70% rock)

Parameter	U1	N1
$Z_1$	0.17	0.30
$Z_2$	0.915	0.833
$M_c (M_{\oplus})$	0.61	3.15
$T_c (K)$	6000	5500
$P_c (\text{Mbar})$	5.5	6.0
$P_0 (\text{Mbar})$	8.3	16.4
$M_Z (M_{\oplus})$	12.4	14.4
I:R	19.2	3.7

# Interior Models: Room for Flexibility



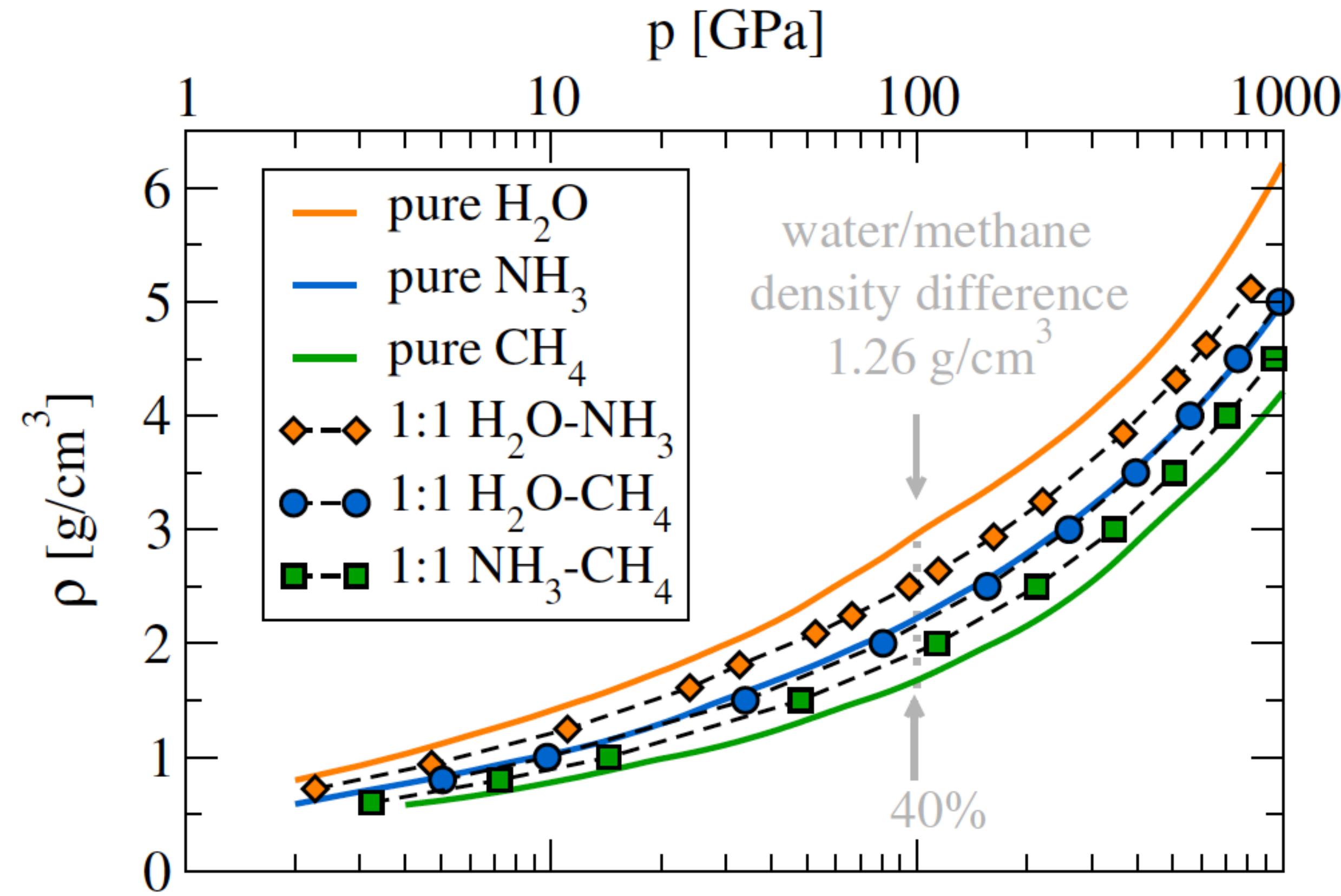
Bethkenhagen et al. (2017)

- Large disparity in heat flow between the two (factor of at least 10) suggests interior gradients possible, which can alter flux carried to the surface
  - Potentially much hotter interiors, leading to lower densities, allowing more rock
  - Mixtures between H/He and water, and water and rock, allow for more rocks

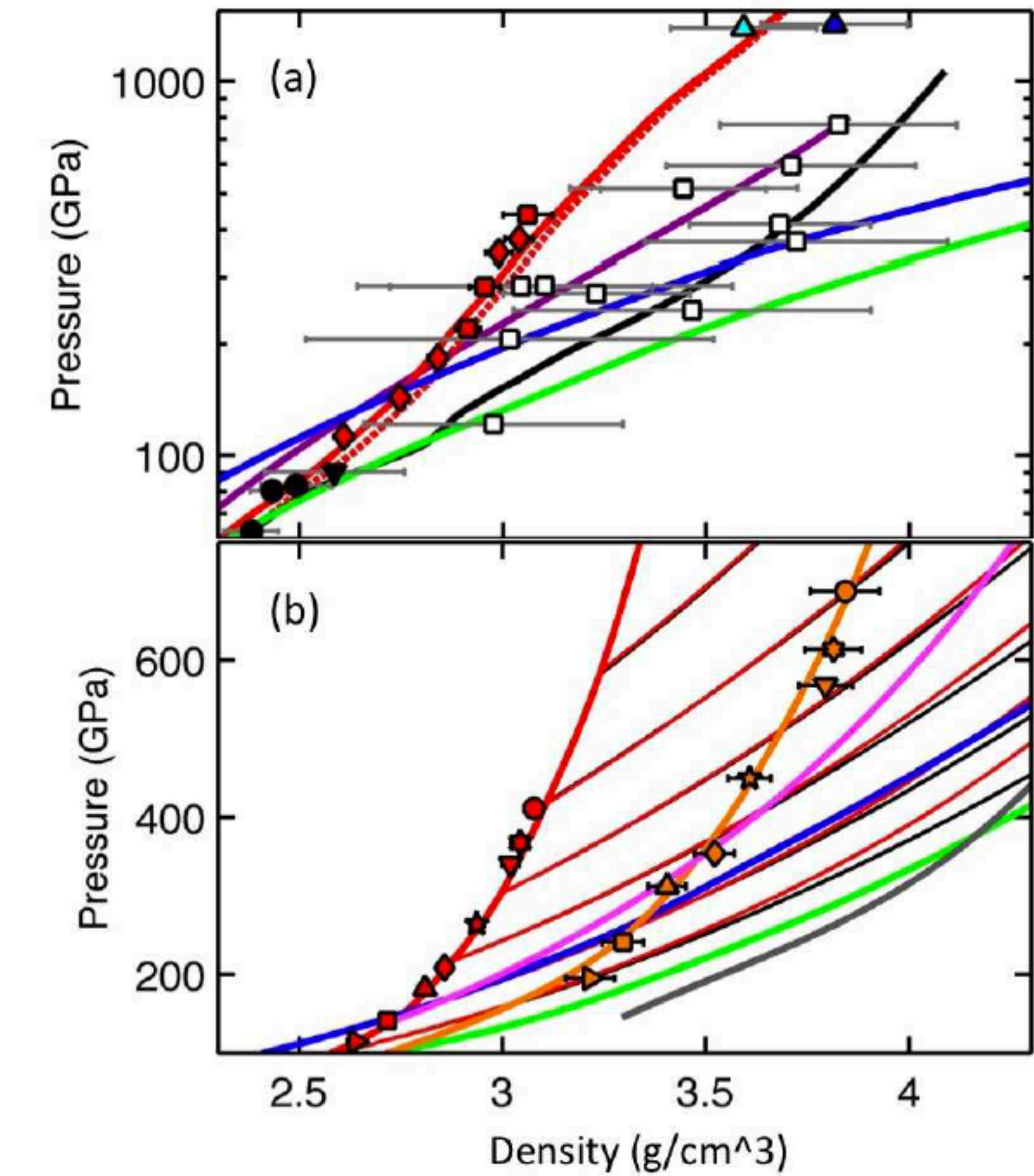
# Interior Models: EOS Improvements

- We have recently seen essential advances in the equations of state (EOS) of water, ammonia, methane
- Still room for new work on their mixtures, phase separation, and “high pressure chemistry”
- One can use these EOS for improved models, but only up to a point, as their use still relies on modeling assumptions

# First principles EOS, being validated



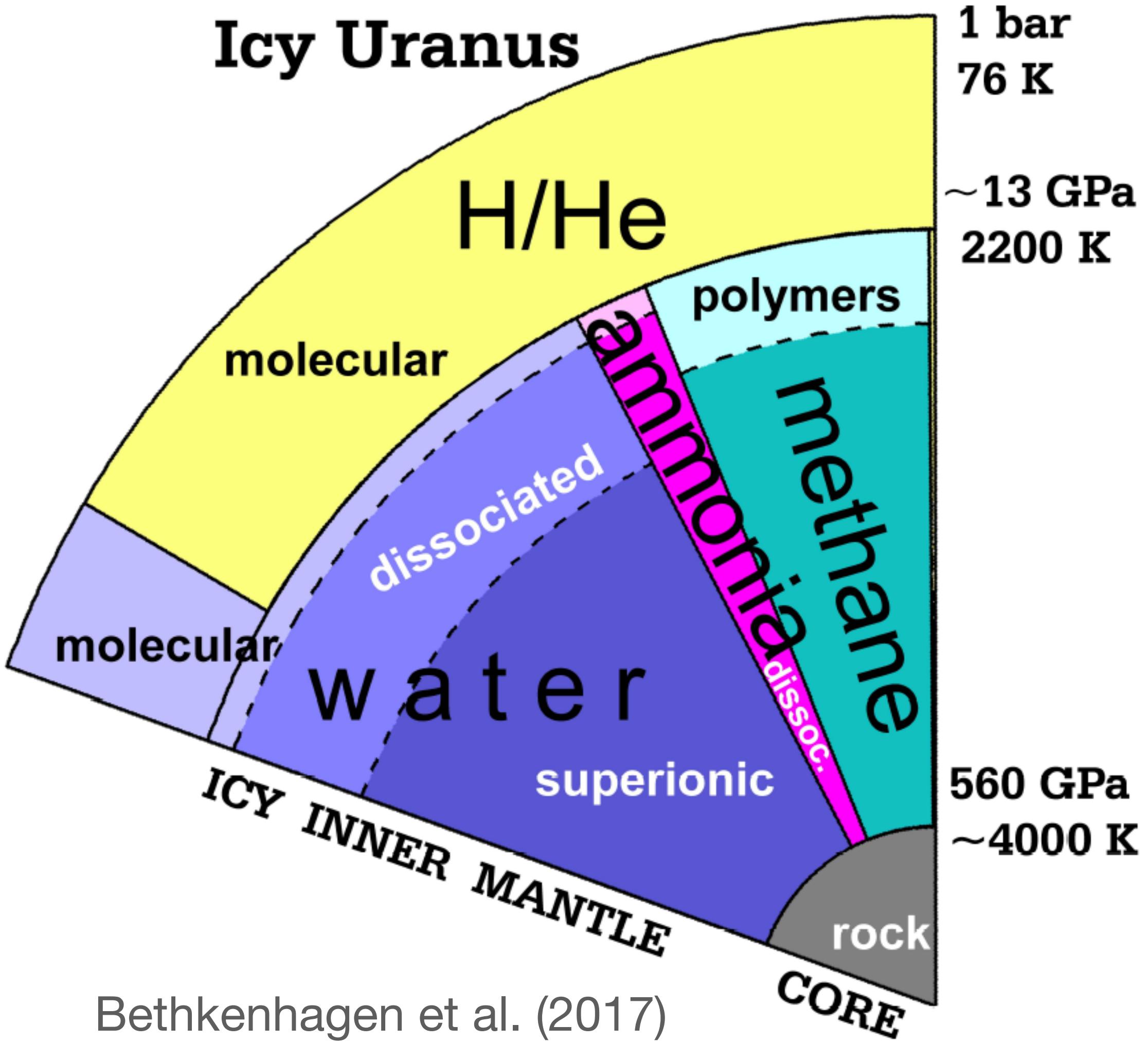
Bethkenhagen et al. (2017): Ab initio simulations of high-pressure fluid icy mixtures



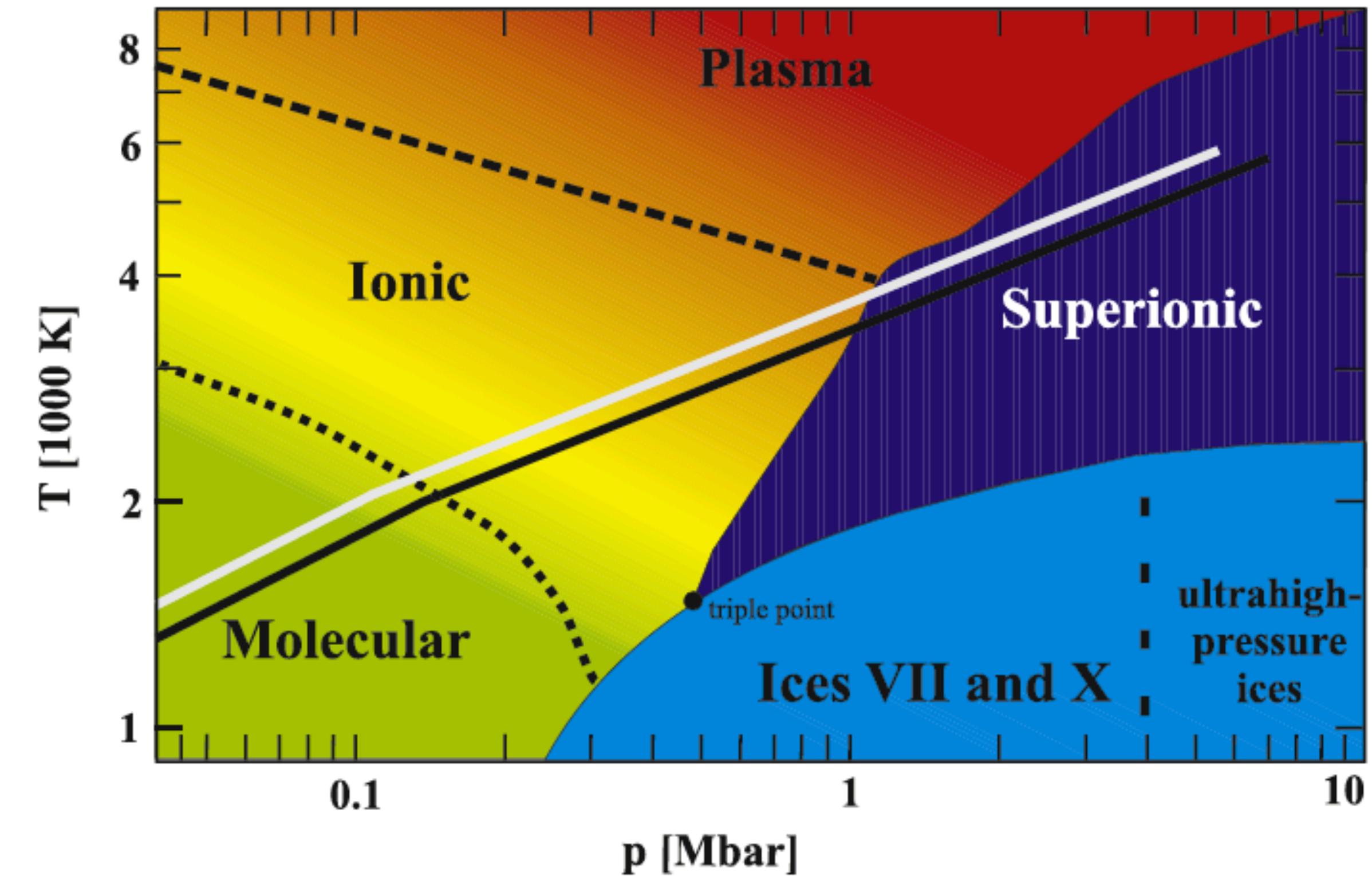
Knudson et al. (2012): Shocked water to 7 Mbar validates ab initio water EOS

# Strange Phases of Matter

Icy Uranus



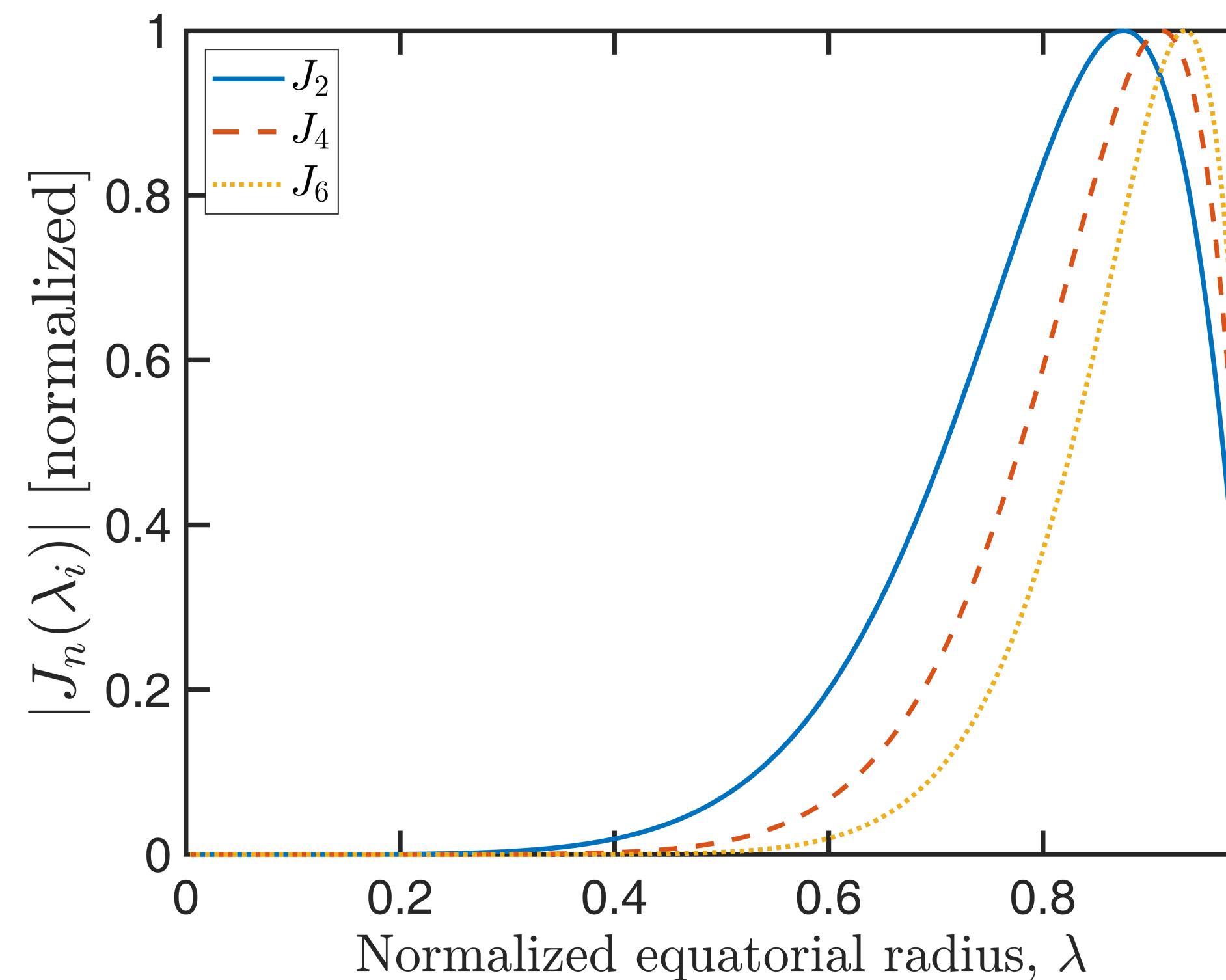
Redmer et al. (2011)



Superionic Water: The O is  
a lattice but the H is a fluid

# Interior Models: Exploring Uncertainties

- Given that so much of our current constraints are based upon given modeling frameworks, is there a way to more efficiently explore phase space?

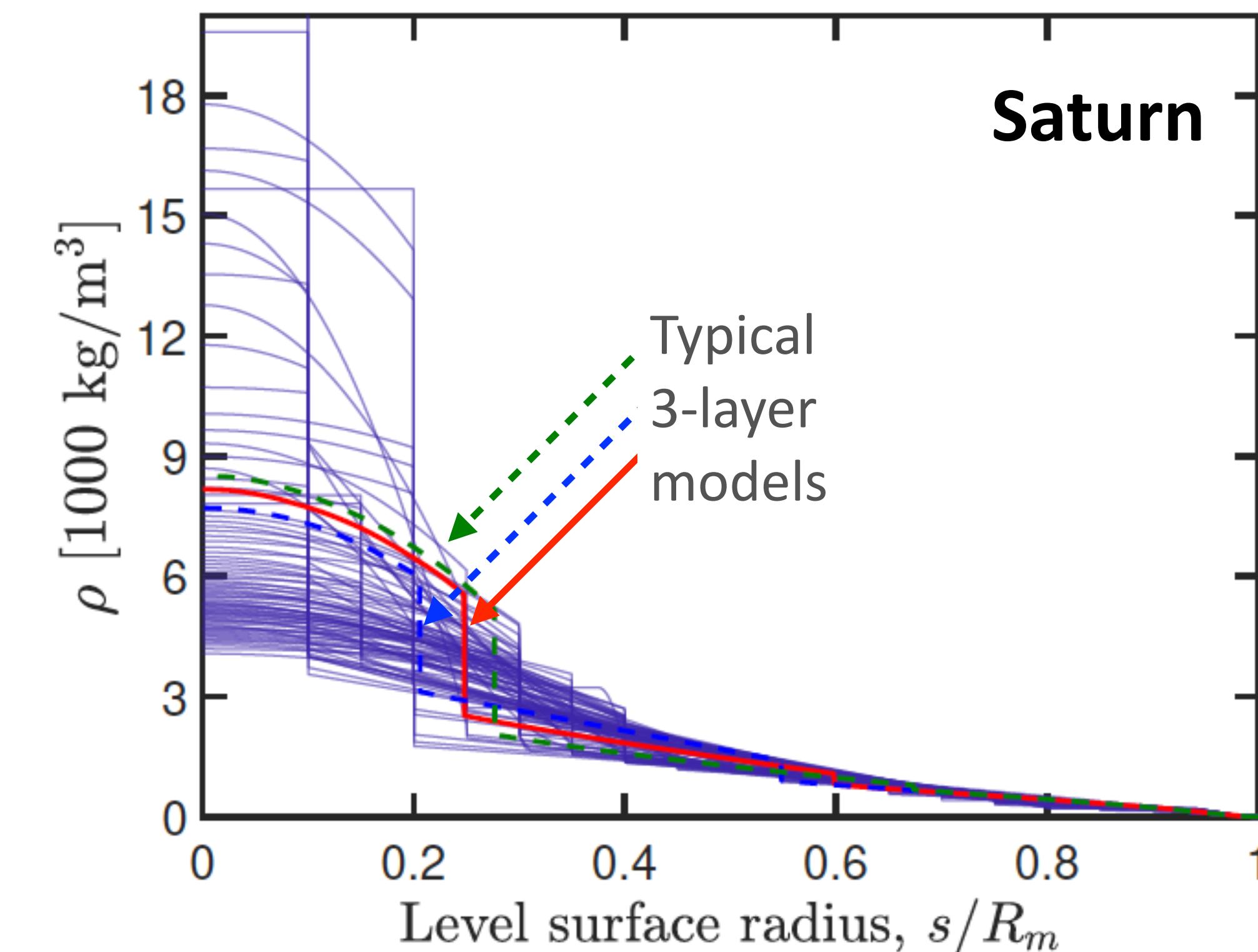
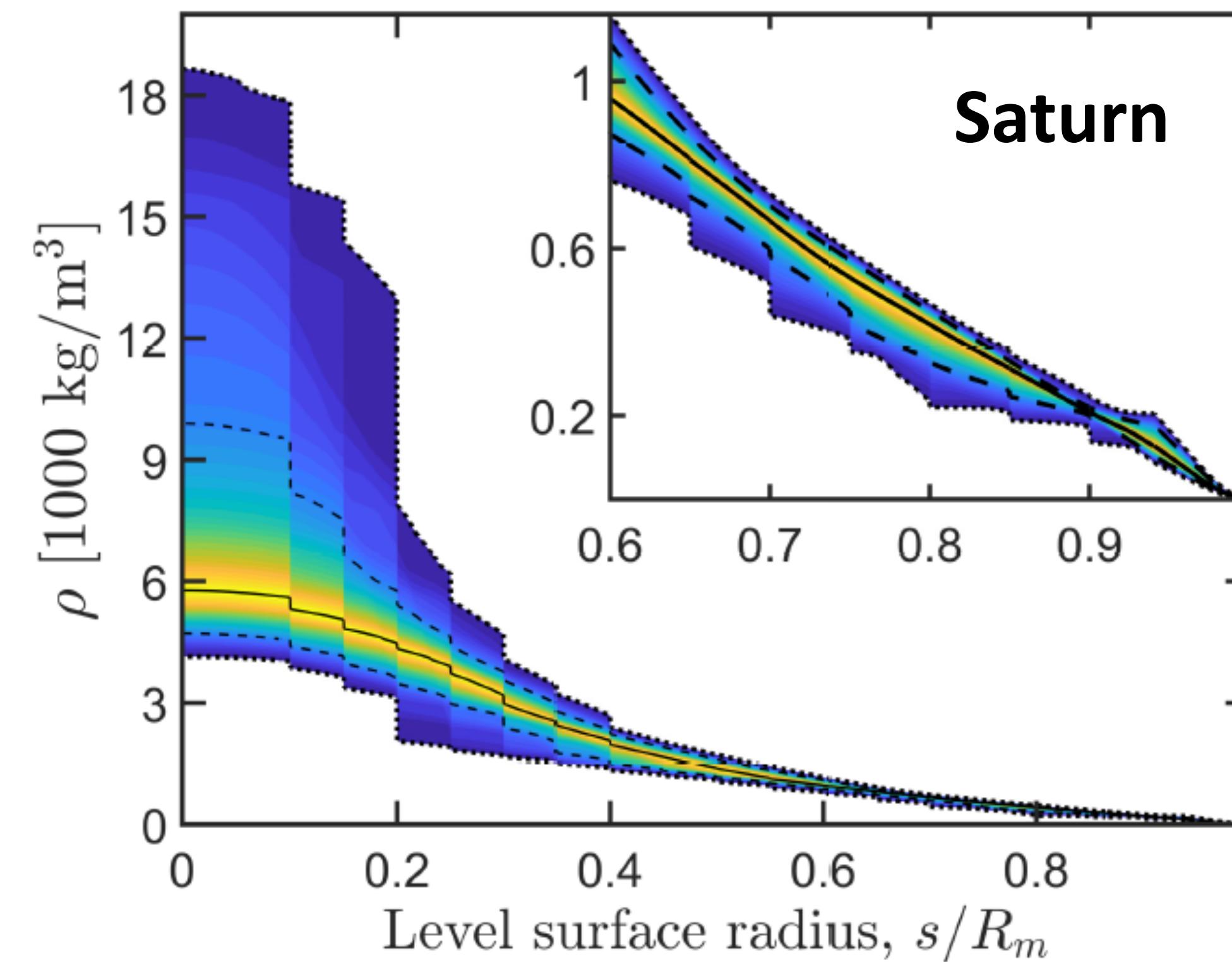


$$\begin{aligned} M &= \iiint \rho(r, \theta) d^3\tau, \\ J_{2i} &= -\frac{1}{MR_{\text{eq}}^{2i}} \iiint \rho(r, \theta) r^{2i} P_{2i}(\cos \theta) d^3\tau, \end{aligned}$$

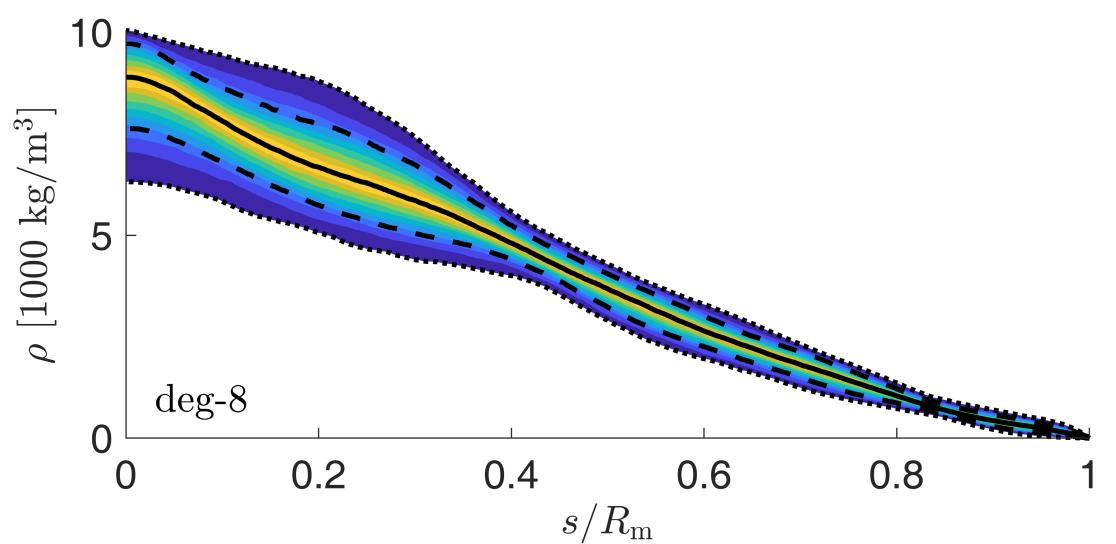
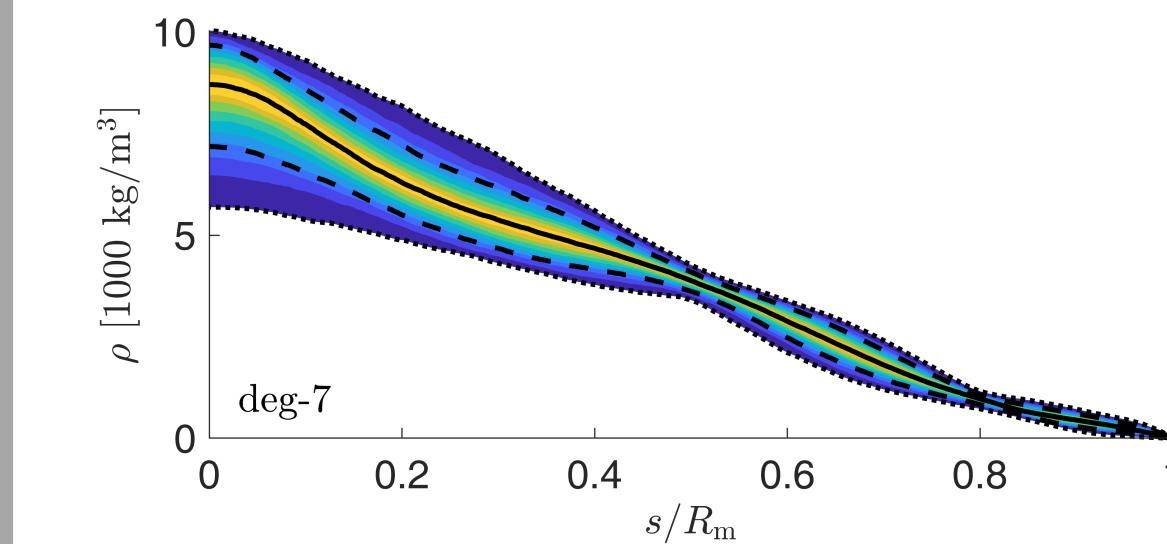
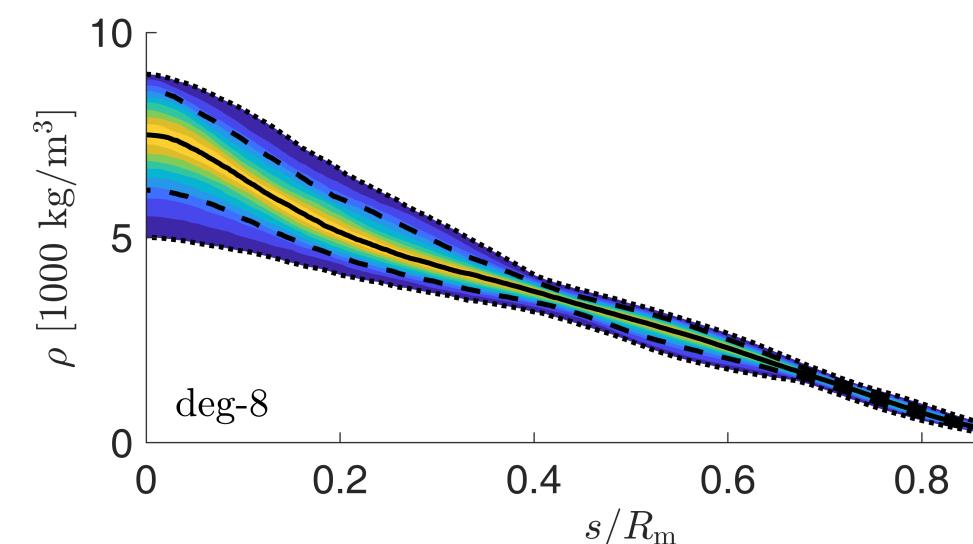
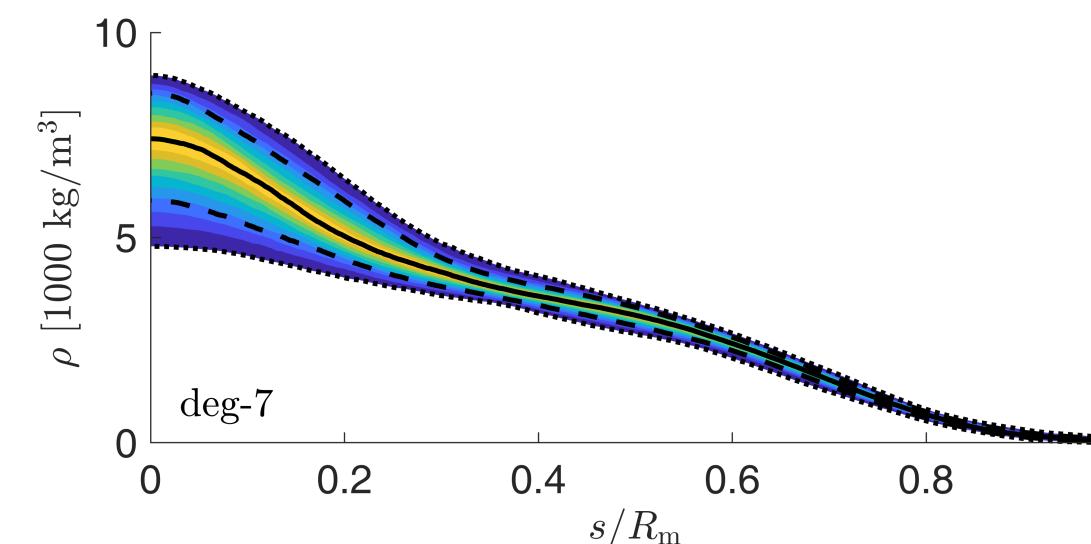
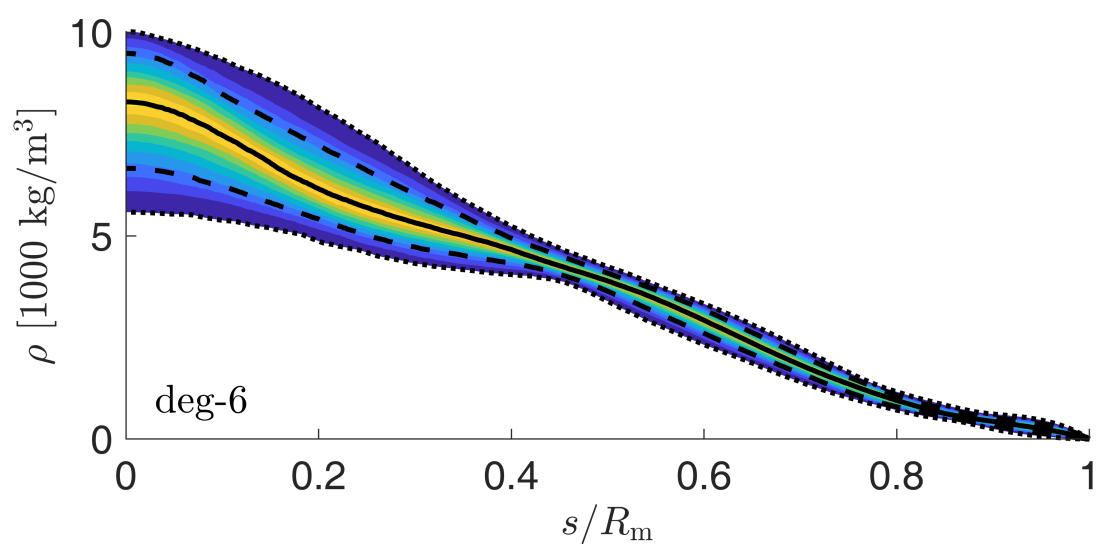
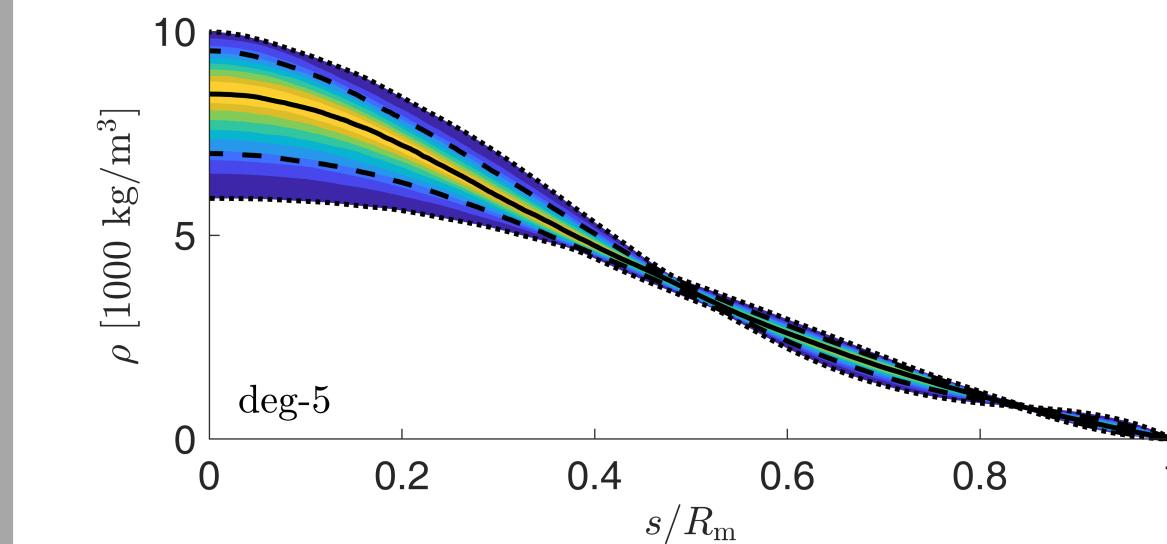
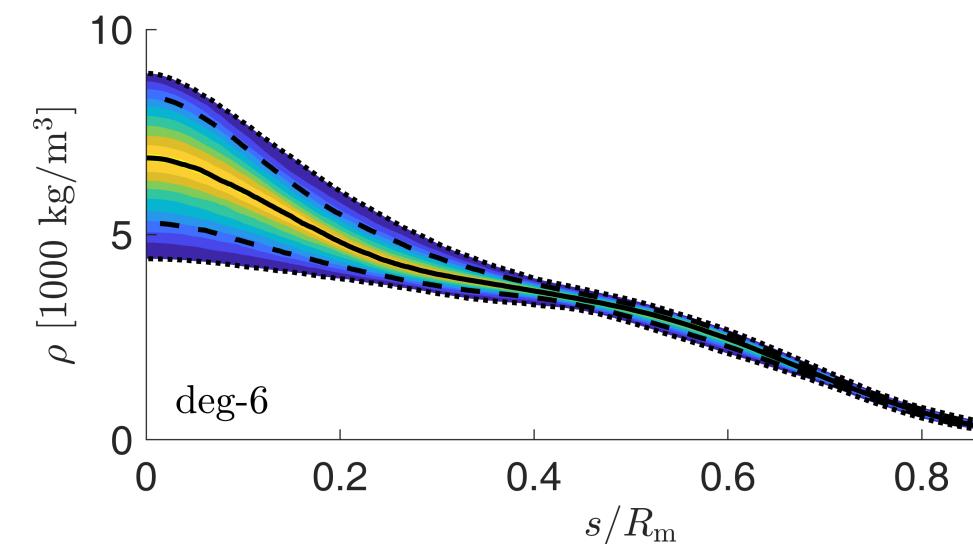
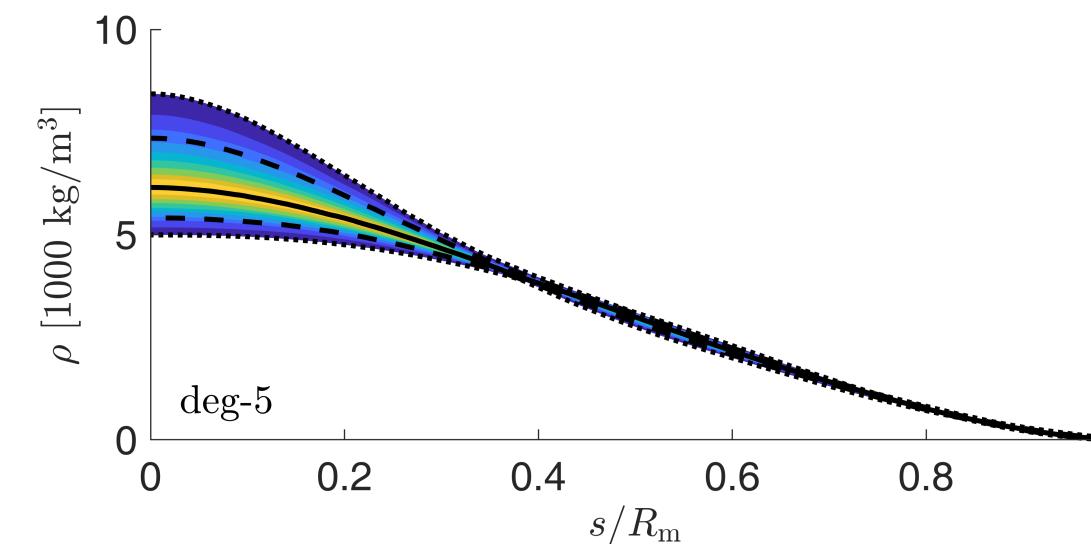
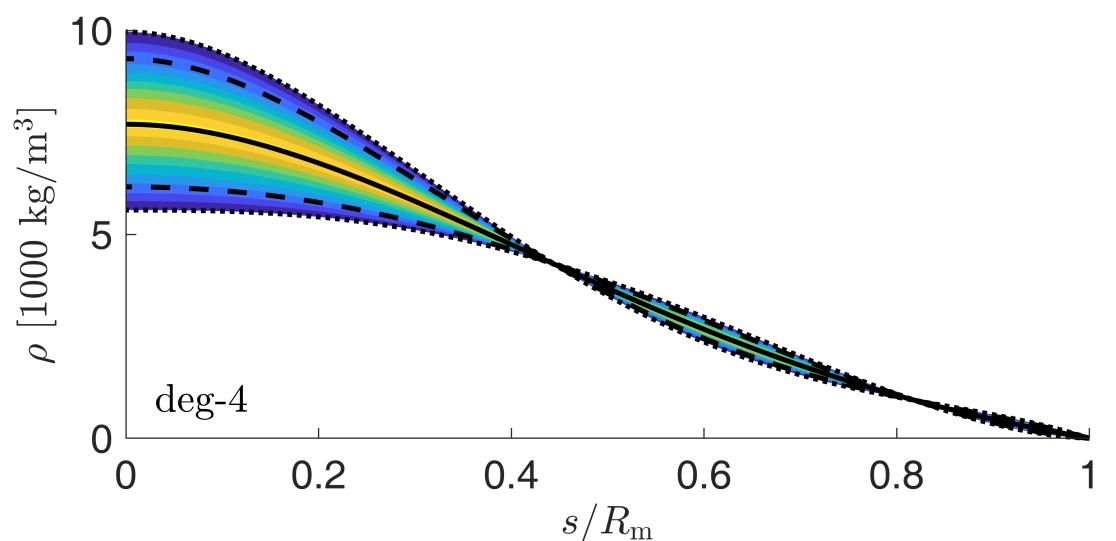
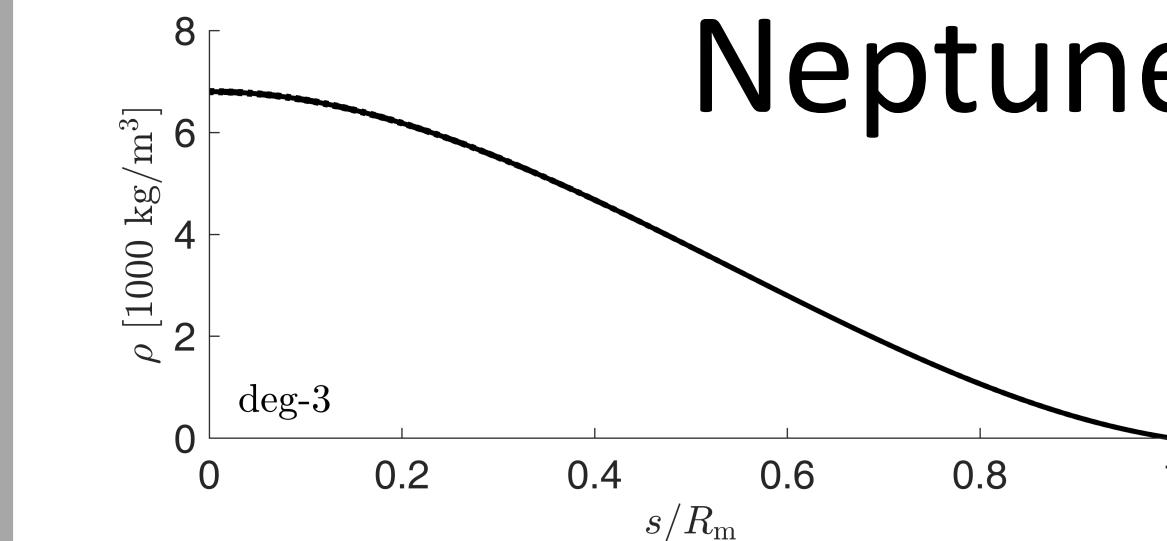
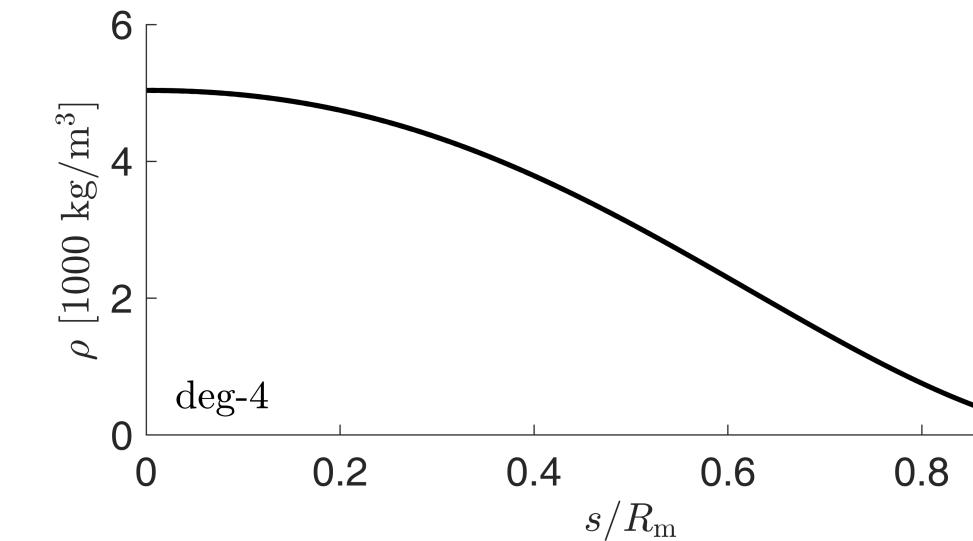
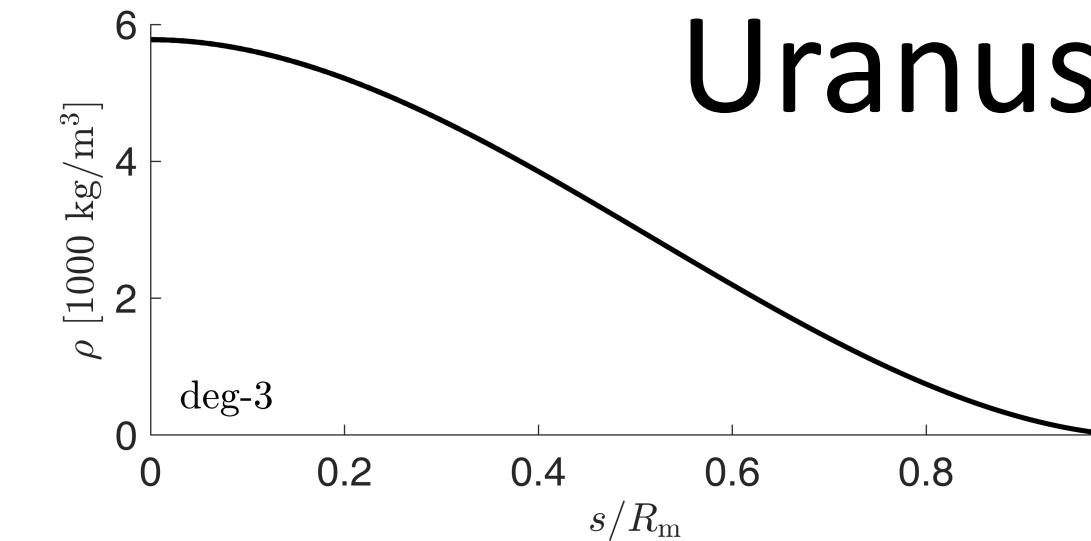
$J_n$  gravitational moments are integrals only over density

# New Methods of Interior Modeling: A Truer View of Uncertainty

- A Bayesian MCMC-driven method to explore all possible interior density profiles that are consistent with gravity data, without needing EOS or a particular modeling framework
- Movshovitz, Fortney, et al. (2019), *Cassini* Grand Finale data for **Saturn**
- Majority of solutions point to a lower density “dilute” core

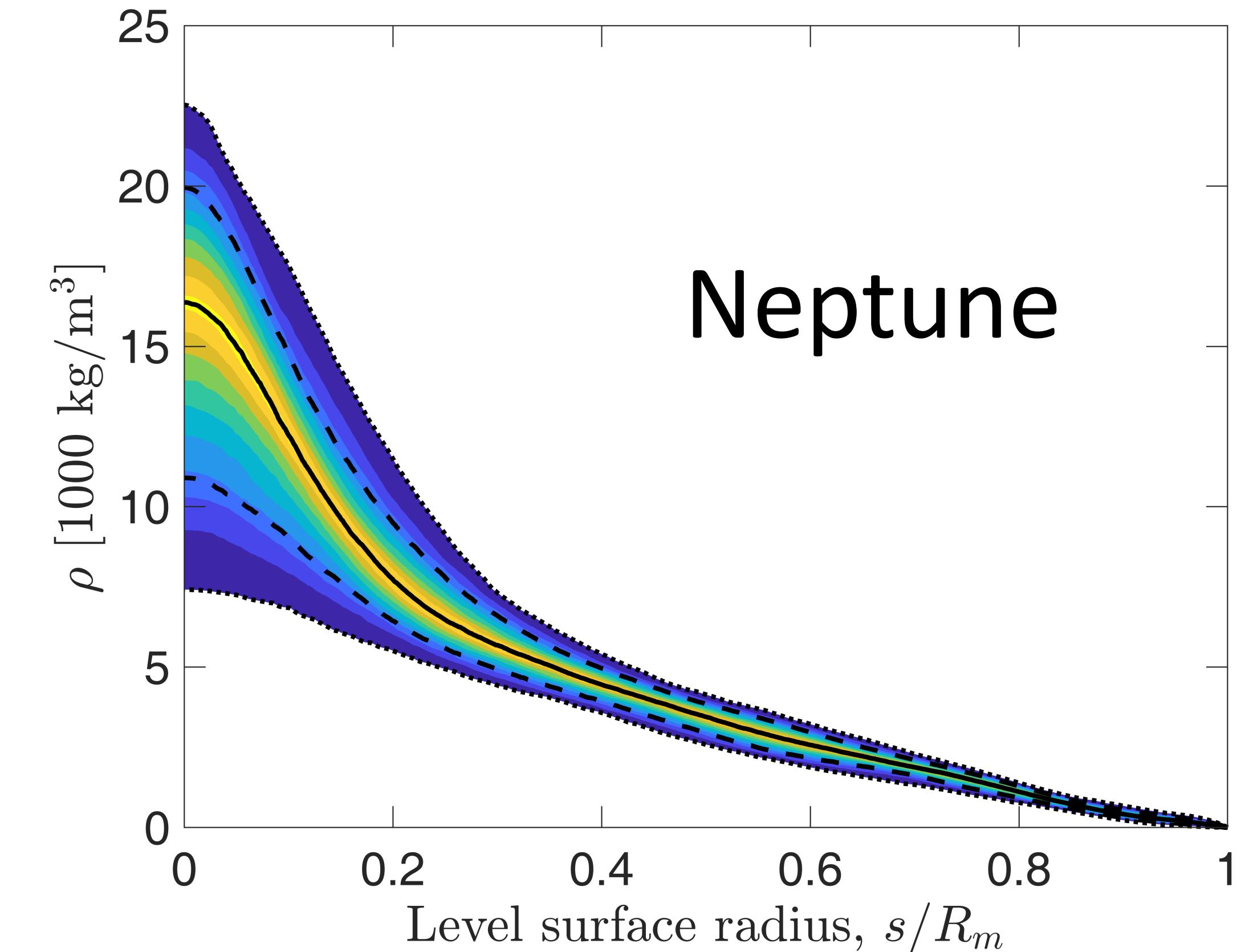
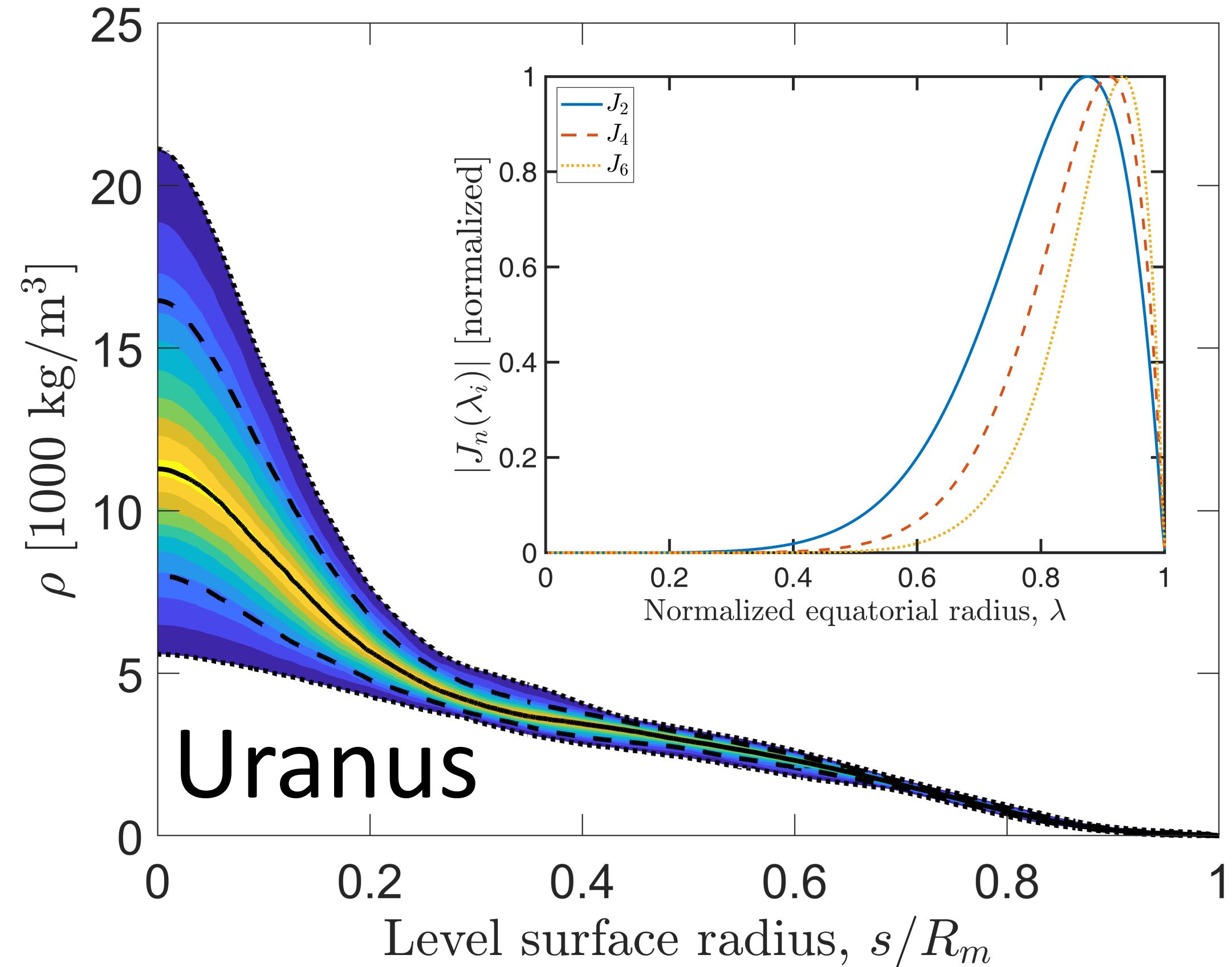


# New Methods of Interior Modeling: Preliminary Uranus & Neptune



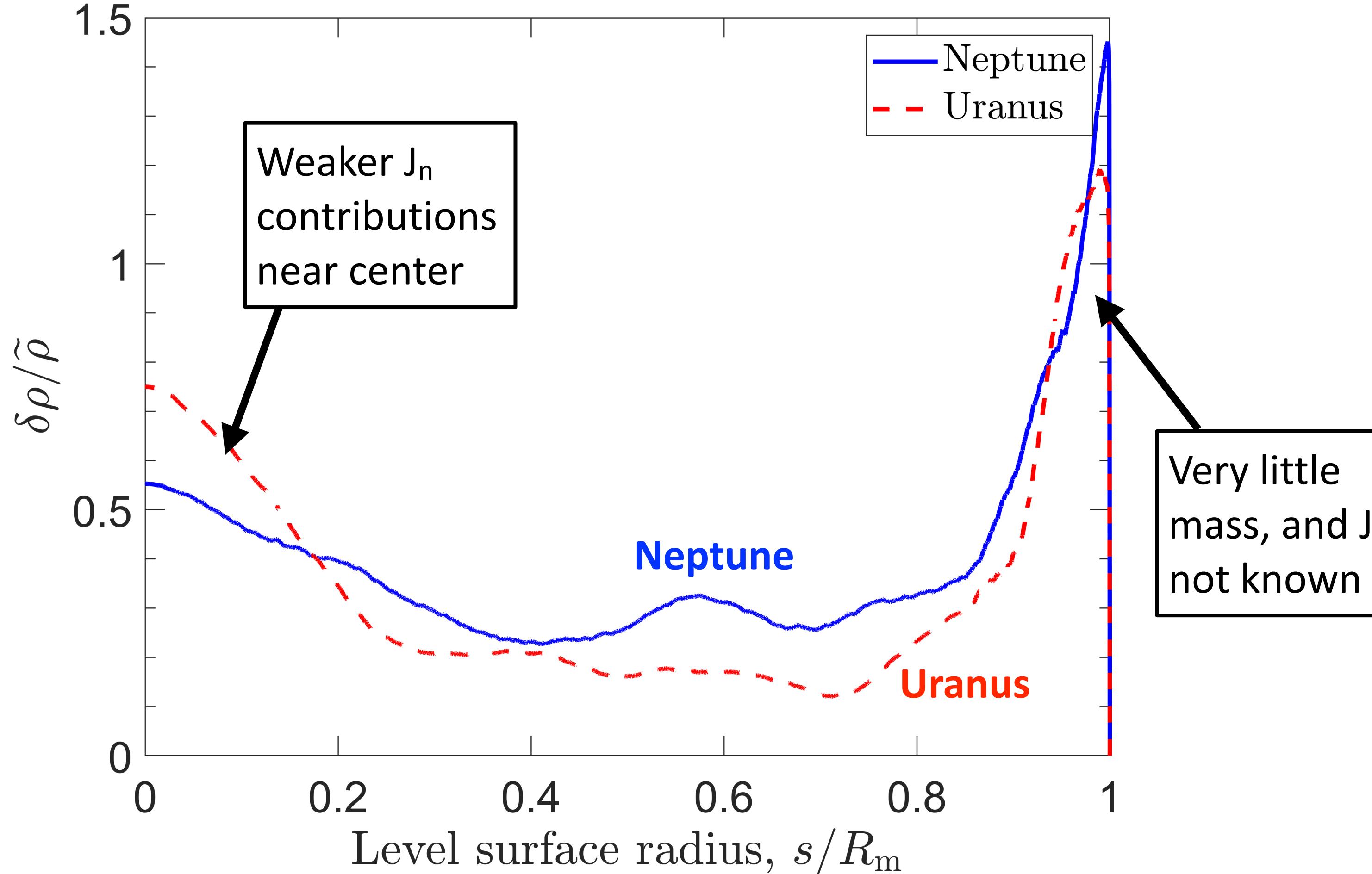
- An exploration of how polynomial degree effects ability to explore a wide phase space of solutions, motivated by work of Helled et al.

# New Methods of Interior Modeling: Preliminary Uranus & Neptune

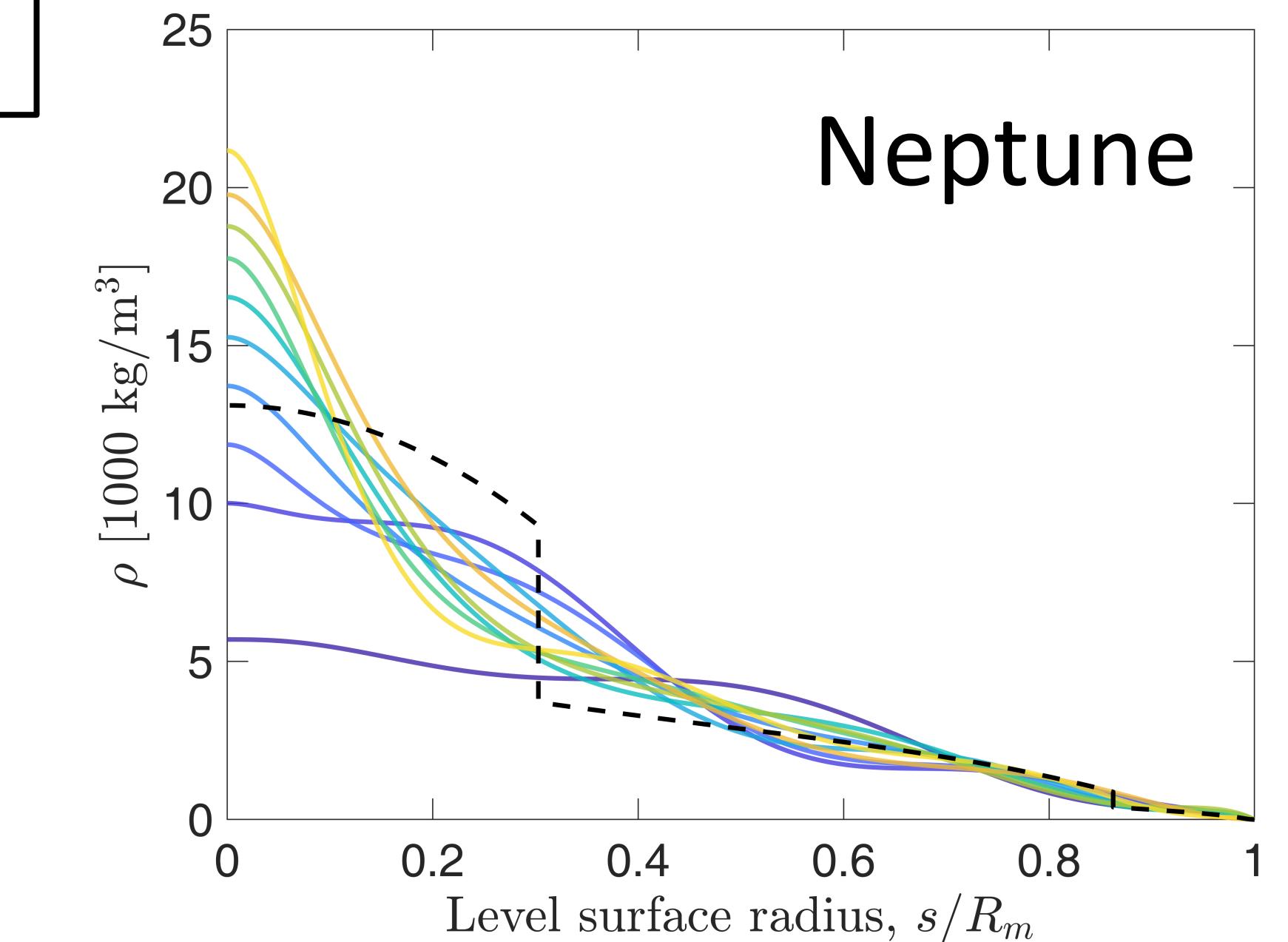
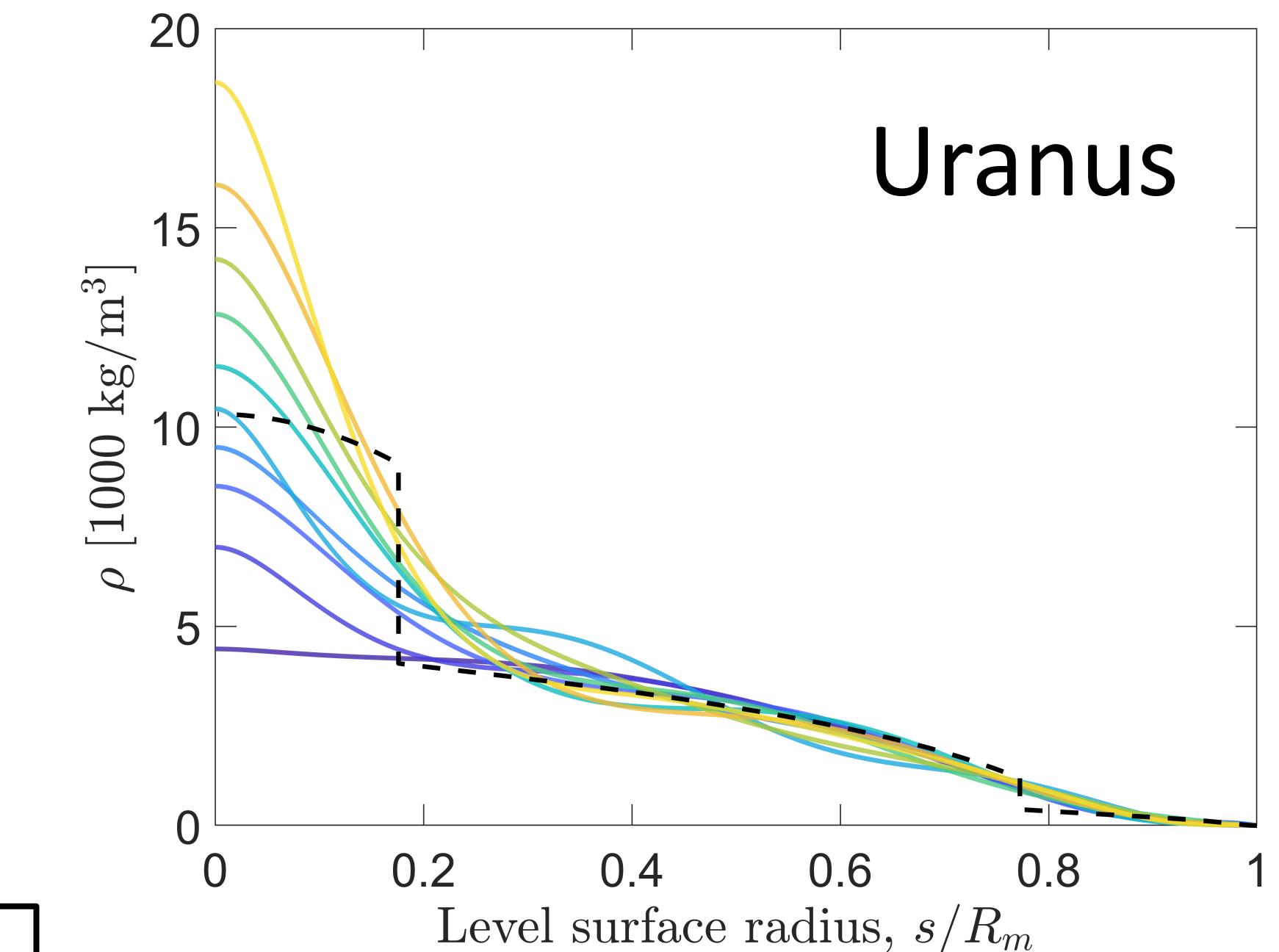


- Polynomial interior density profiles above shown to 8th degree
- Uranus gravitational field is better determined – tighter constraints

# Preliminary Uranus & Neptune



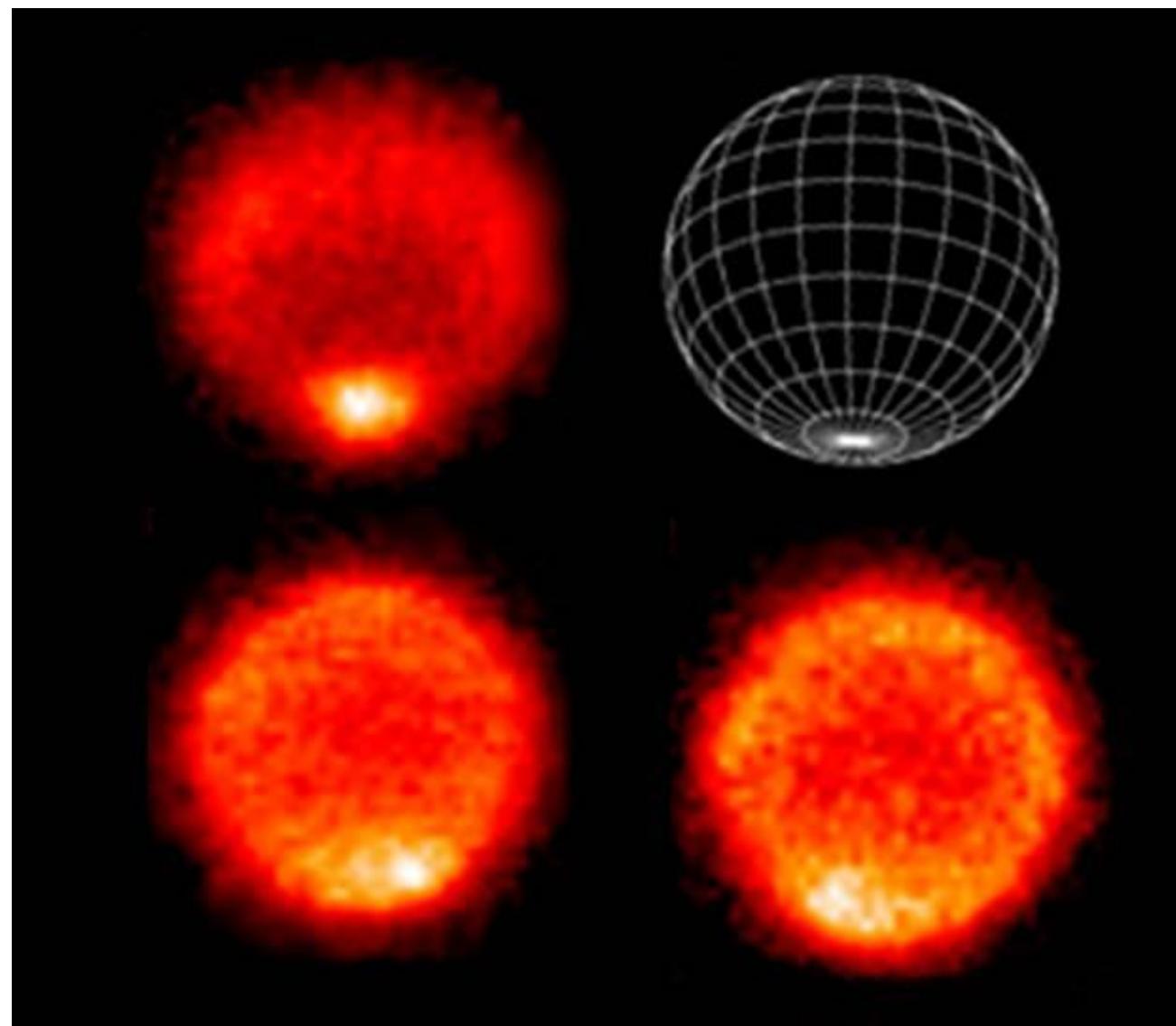
- Neptune's density is less well constrained
- Uranus's gravitational field is better determined



# Energy Balance: A Complementary Observable

$$T_{\text{eff}}^4 = T_{\text{eq}}^4 + T_{\text{int}}^4$$

- Total Thermal Flux
- Measurable!



- Thermal Flux Due to Absorbed and Re-Radiated Sunlight
  - Depends on the Bond Albedo,  $A_B$ : the ratio of reflected Solar Power to the Incident Power
  - $A_B$  requires observations over *all wavelengths and all phase angles*

- Thermal Flux from the Planet's Interior
  - Can only be determined if  $T_{\text{eq}}$  is known

# Energy Balance: A Complementary Observable

PEARL AND CONRATH: THE ENERGY BALANCE OF NEPTUNE

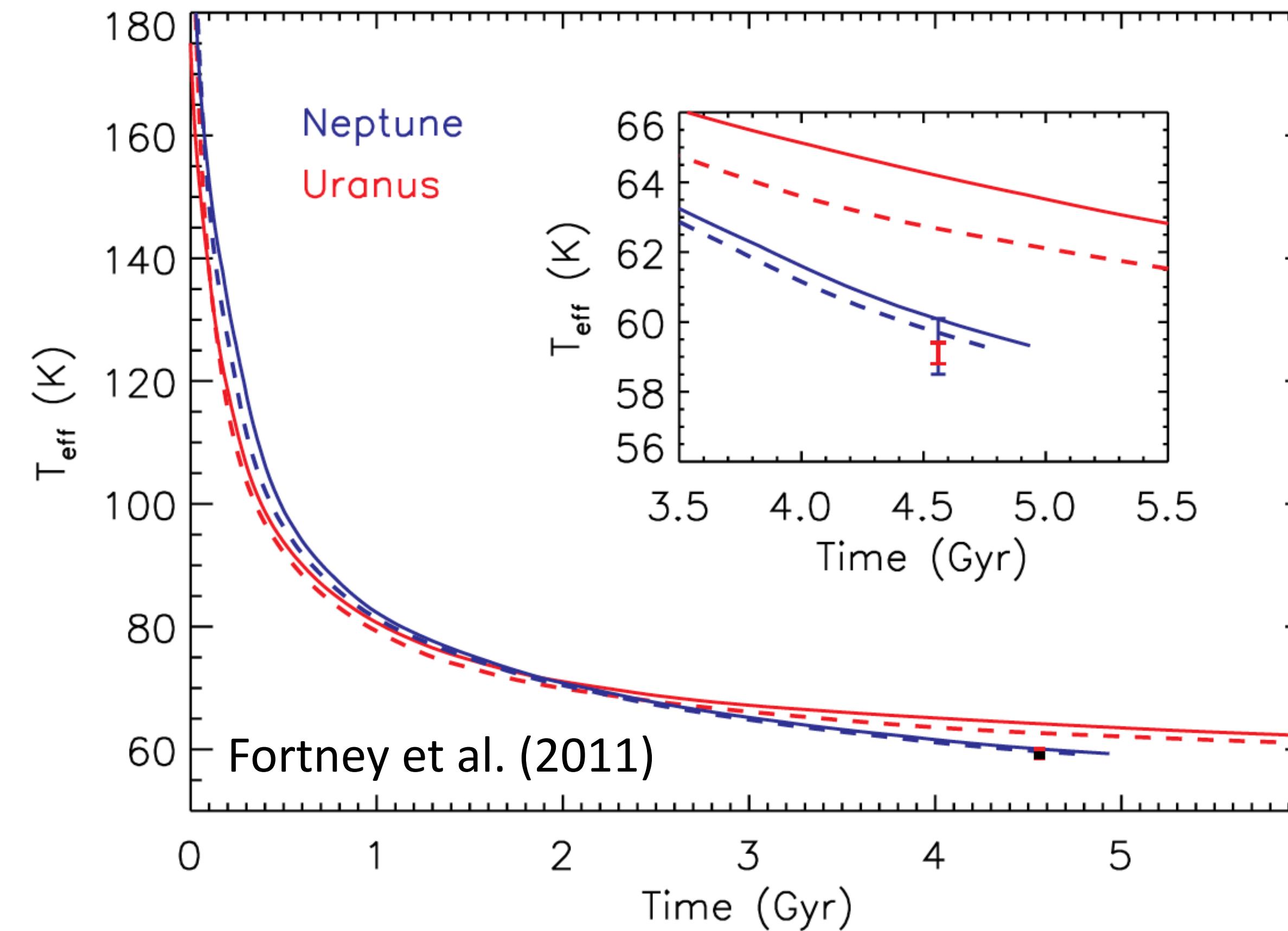
18,929

TABLE 7. The Energy Balance of the Outer Planets, as Determined From Voyager IRIS-Data

Parameter	Jupiter <sup>a</sup>	Saturn <sup>b</sup>	Uranus <sup>c</sup>	Neptune <sup>d</sup>
Geometric albedo <sup>e</sup>	0.274 ± 0.013	0.242 ± 0.012	0.215 ± 0.046	0.215 ± 0.050
Phase integral	1.25 ± 0.1	1.42 ± 0.1	1.40 ± 0.14	1.35 ± 0.16
Bond albedo <sup>e</sup>	0.343 ± 0.032	0.342 ± 0.030	0.300 ± 0.049	0.290 ± 0.067
Absorbed power, <sup>e</sup> 10 <sup>16</sup> W	50.14 ± 2.48	11.14 ± 0.50	0.526 ± 0.037	0.204 ± 0.019
Equilibrium temperature, <sup>e</sup> K	109.5 ± 1.4	82.4 ± 0.9	58.2 ± 1.0	46.6 ± 1.1
Emitted power, 10 <sup>16</sup> W	83.65 ± 0.84	19.77 ± 0.32	0.560 ± 0.011	0.534 ± 0.029
Effective temperature, K	124.4 ± 0.3	95.0 ± 0.4	59.1 ± 0.3	59.3 ± 0.8
Energy balance <sup>e</sup>	1.67 ± 0.09	1.78 ± 0.09	1.06 ± 0.08	2.61 ± 0.28
Internal power, 10 <sup>16</sup> W	33.5 ± 2.6	8.63 ± 0.60	0.034 ± 0.038	0.330 ± 0.035
Internal energy flux, 10 <sup>-4</sup> W/cm <sup>2</sup>	5.44 ± 0.43	2.01 ± 0.14	0.042 ± 0.047	0.433 ± 0.046
Internal power/unit mass, 10 <sup>-11</sup> W/kg	17.6 ± 1.4	15.2 ± 1.1	0.392 ± 0.441	3.22 ± 0.34
Luminosity: log( $L/L_0$ )	-9.062 ± 0.034	-9.651 ± 0.030	-12.054 <sup>+0.327</sup> <sub>-0.327</sub>	-11.025 ± 0.044

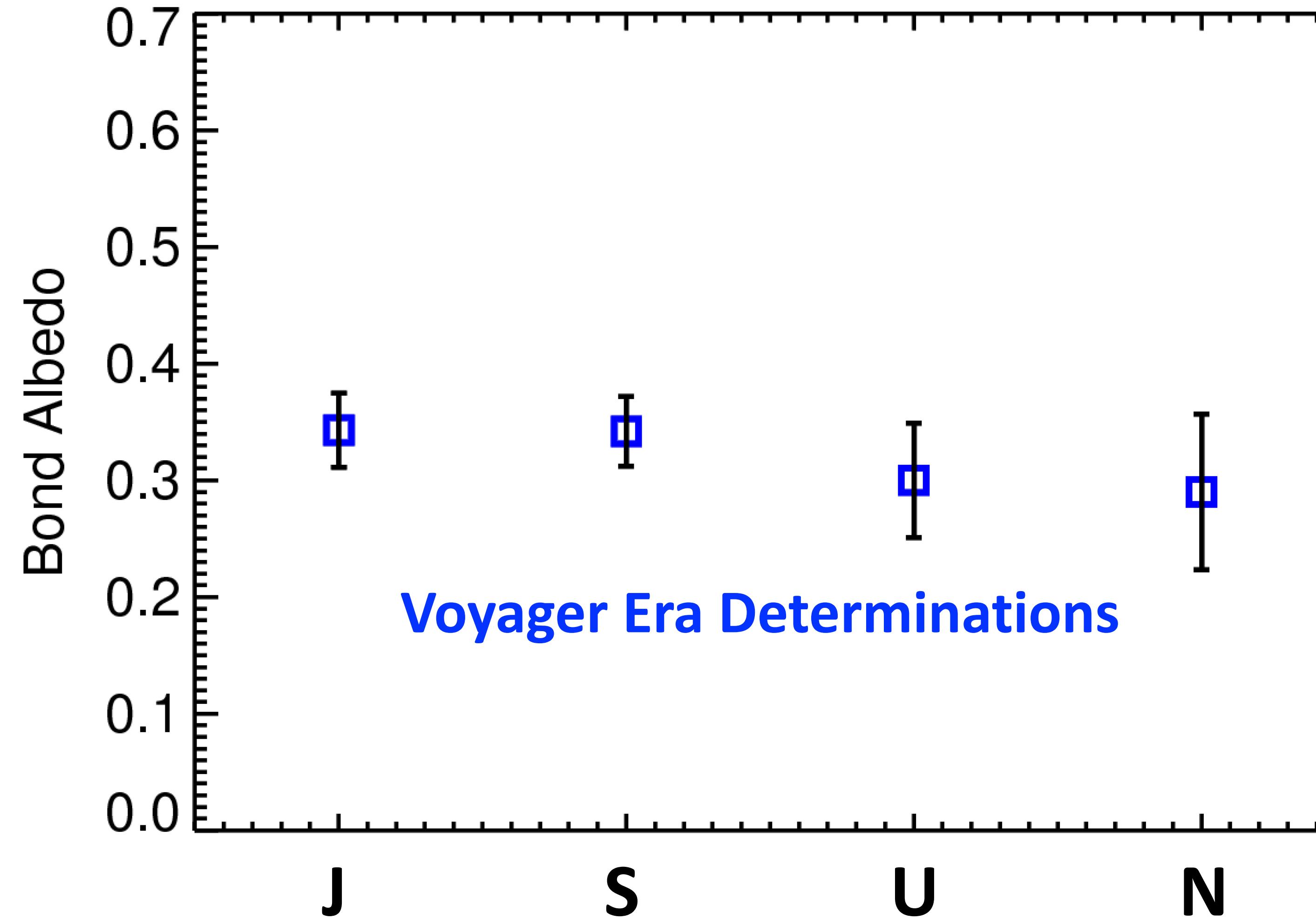
A Fantastic Legacy of the Voyager Missions

# Thermal Evolution Models Aim to Match $T_{\text{eff}}$ at 4.5 Gyr

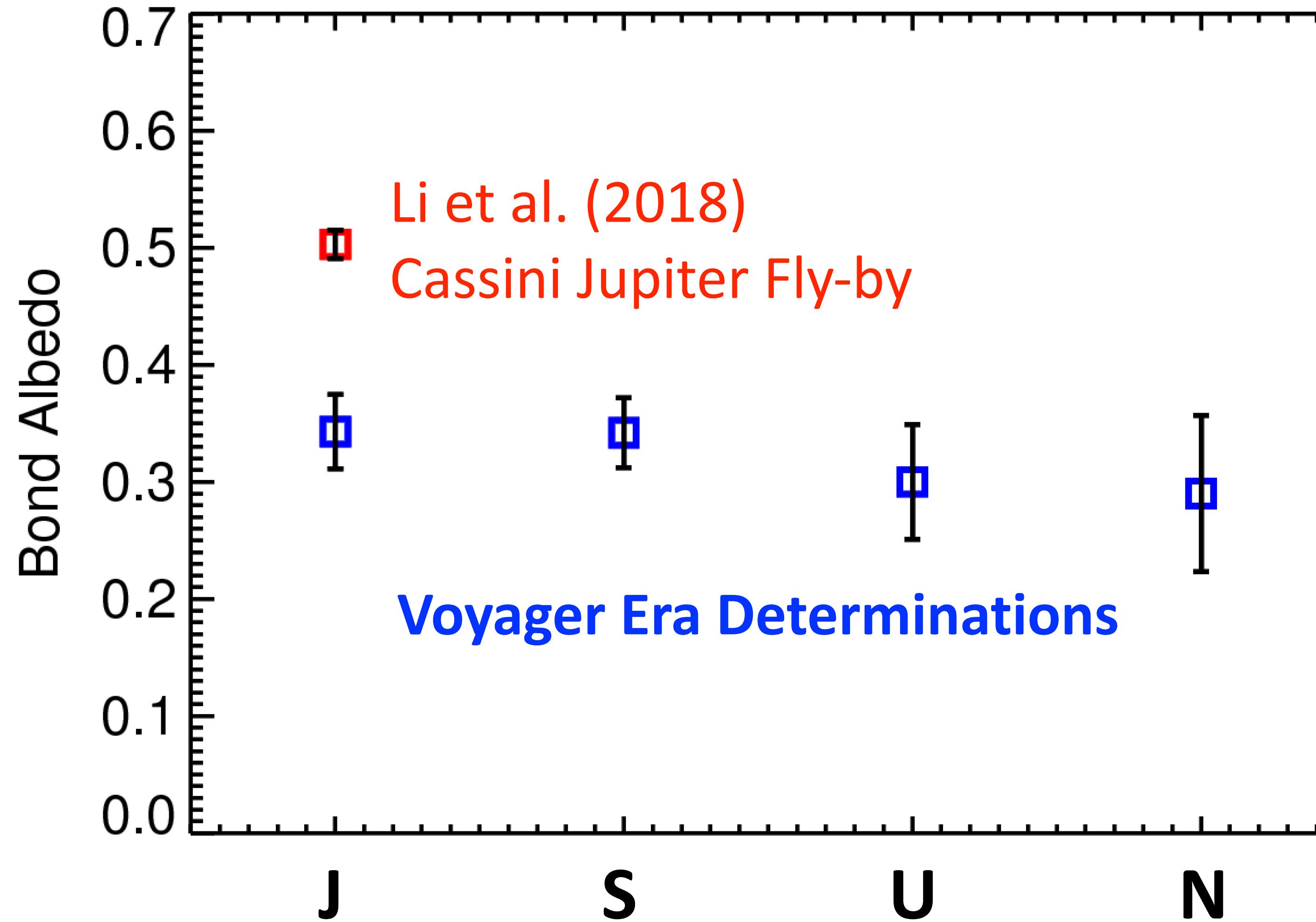


- Improved physics led Fortney & Nettelmann (2010) and Fortney et al. (2011) to find a good match for Neptune, and the “typical” poor match for Uranus, with “standard” 3-layer adiabatic models
- The interior model matters, and the energy balance values matter

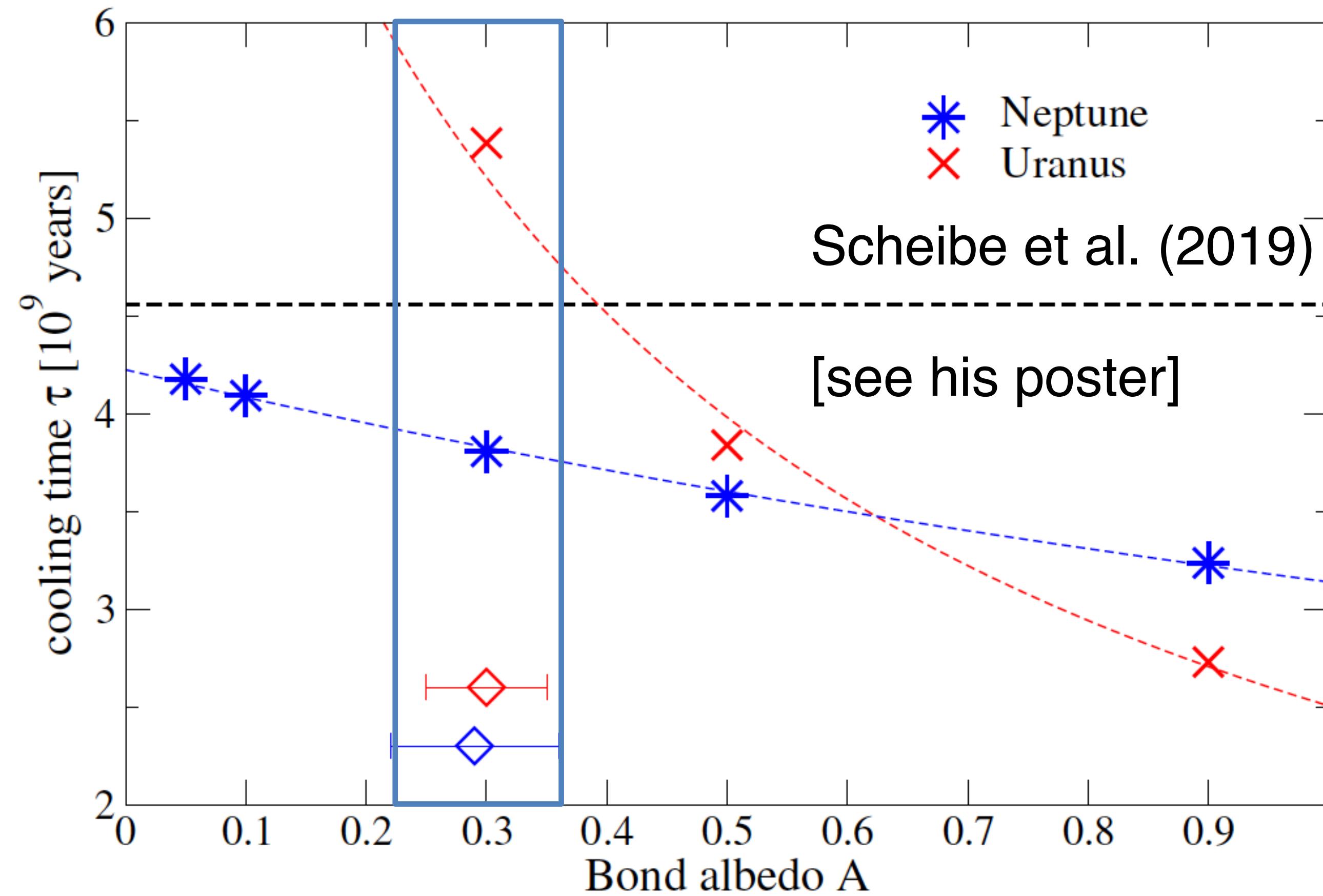
# Bond Albedos: Revisions in Order?



# Bond Albedos: Revisions in Order?



# Newly Revised Physics, Standard Models, Revised Story



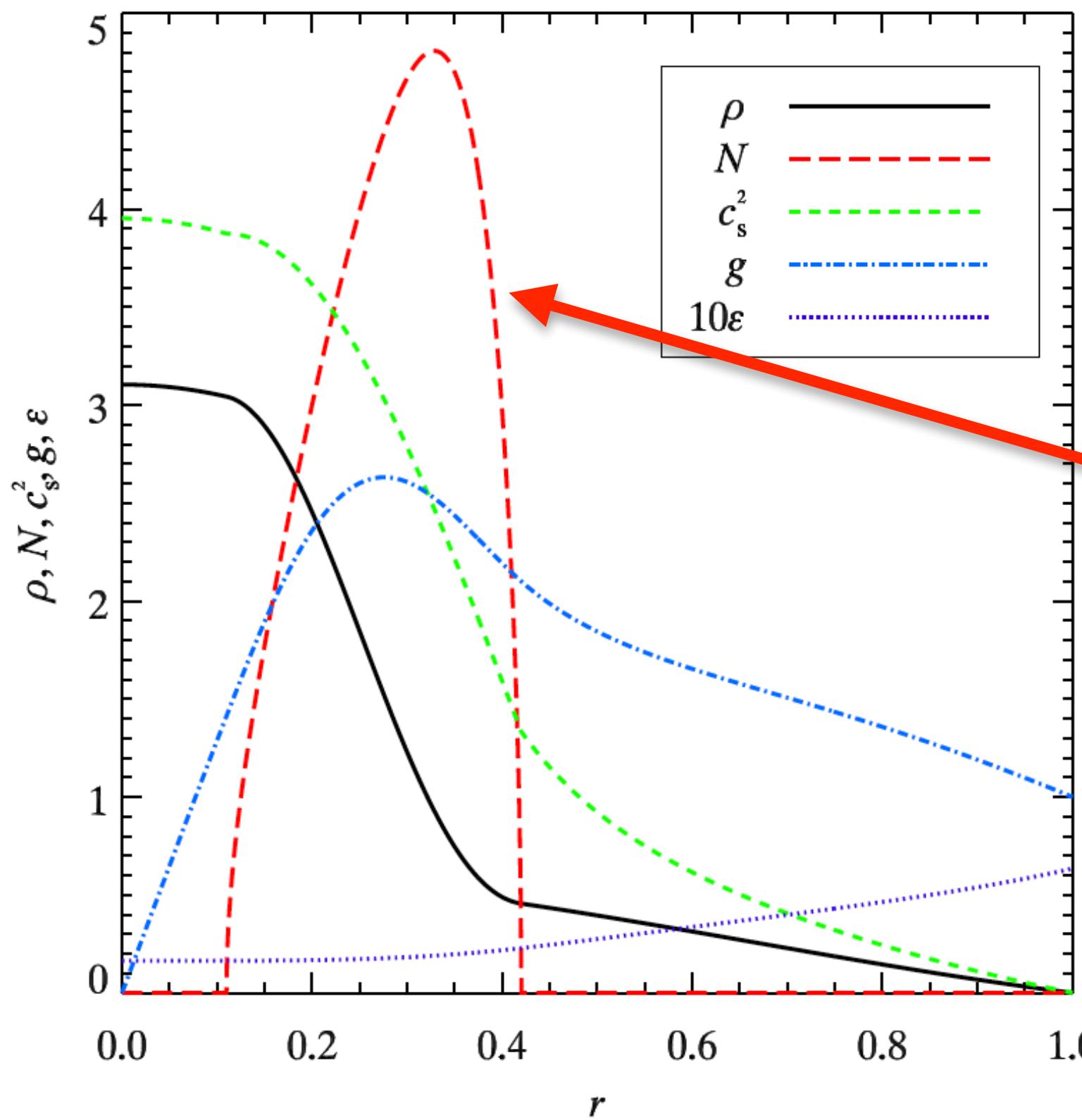
- Correct  $A_B$  value plays a large role in understanding Uranus thermal history
- Uranus is still underluminous today, but not that far off
- Neptune is overluminous today
- Still a large difference between the two, but neither is “simple”

# Paths Forward?

- Gravitational Field, for interior structure:
  - Uranus  $J_2$  and  $J_4$  already fairly precise
  - Neptune needs improvement in low order field
  - Constrain deep atmosphere dynamics:  $J_6$ ,  $J_8$ , + *[Soyuer poster]*
  - Improved rotation rate and shape determination
  
- Re-analysis of Voyager energy balance data + inclusion of high quality ground-based geometric albedo data *[Li poster]*

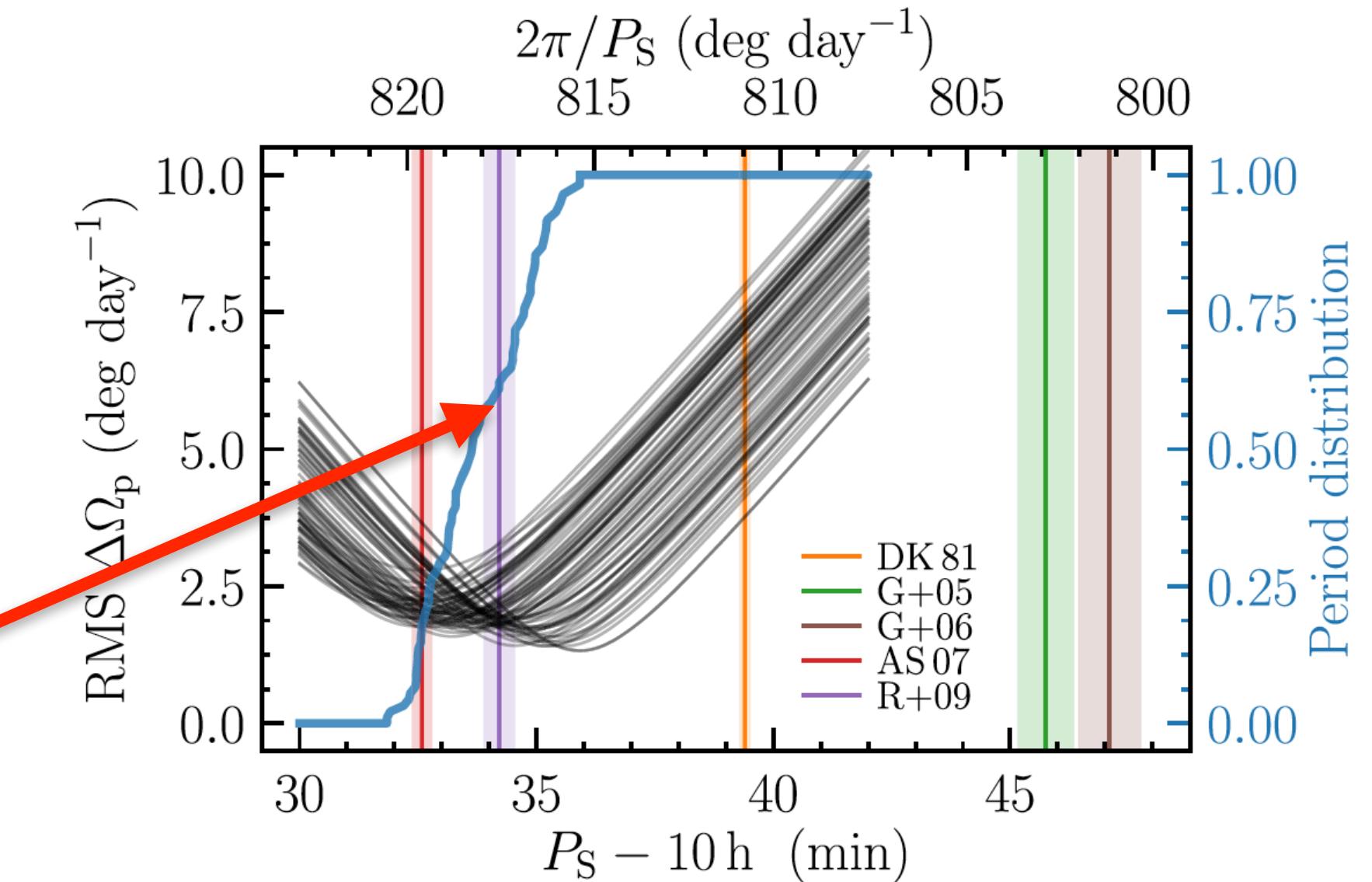
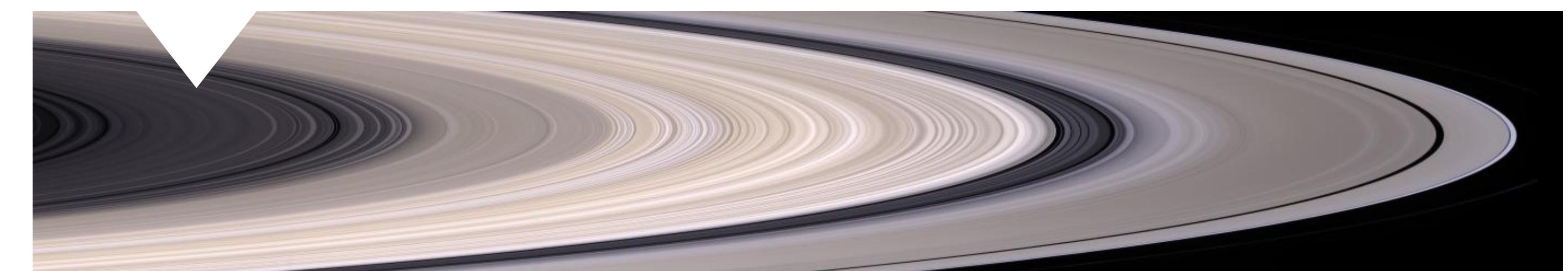
# Additional Paths Forward?

- **Seismic investigations** for an entirely new axis for information on the interior
  - Location of layer boundaries (are there layer boundaries?)
  - Non-adiabatic regions that support g-modes [*Friedson & Hedman posters*]



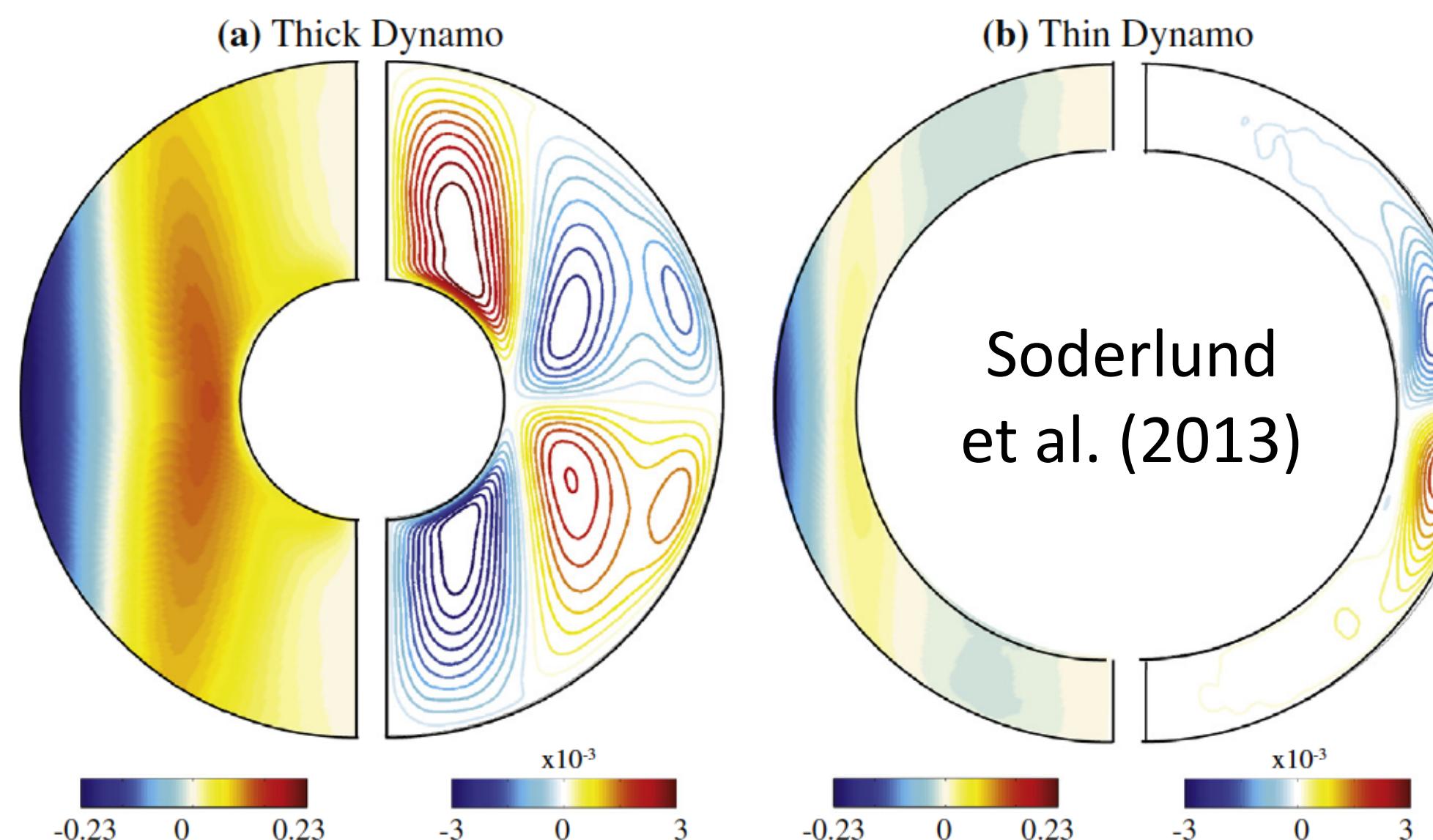
Fuller (2014):  
Eroded Core  
in Saturn

Mankovich et al (2019):  
Precise Rotation Period



# Additional Paths Forward?

- **Seismic investigations** for an entirely new axis for information on the interior
  - Location of layer boundaries (are there layer boundaries?)
  - Non-adiabatic regions that support g-modes [*Friedson & Hedman posters*]
  - A much better understanding of the **magnetic field and dynamo** will feed back directly into improvements in knowledge of the structure



While challenging, a consistent picture involving the dynamo, interior conductivity, and interior convection will be necessary to get past our current lack of understanding

# Additional Paths Forward?

- **Seismic investigations** for an entirely new axis for information on the interior
  - Location of layer boundaries (are there layer boundaries?)
  - Non-adiabatic regions that support g-modes [*Friedson & Hedman posters*]
  - A much better understanding of the **magnetic field and dynamo** will feed back directly into improvements in knowledge of the structure
- **Entry probe** for temperature structure and atmospheric abundances
  - *Juno*-like microwave sounding for ~100+ bars?
  - **More experiments and theoretical investigations of mixtures** and possible phase separation for mixtures relevant to the ice giants [*Millot talk, Weds*]