

HW1

1. (36%) Convert the following numbers from the given base to other three bases listed in the table (to the 4th digit after radix point):

Decimal	Binary	Octal	Hexadecimal
76.28	1001100.0100	114.2172	4C.47AE
9.625	1001.1010	11.5	9.A
48.37不屬於8進位，故無解		48.37	
127.140625	1111111.0010	177.11	7F.24

1.

$$\begin{array}{r}
 2 \overline{) 76} \rightarrow 0.28 \times 2 = 0.56 \\
 2 \overline{) 56} \rightarrow 0.56 \times 2 = 1.12 \\
 2 \overline{) 12} \rightarrow 0.12 \times 2 = 0.24 \\
 2 \overline{) 24} \rightarrow 0.24 \times 2 = 0.48 \\
 2 \overline{) 48} \rightarrow 1
 \end{array}$$

$$(76.28)_{10} = (1001100.0100)_2$$

$$(1001100)_2 = (114)_8$$

$$\begin{array}{l}
 0.28 \times 8 = 2.24 \text{ -2} \\
 0.24 \times 8 = 1.92 \text{ -1} \\
 0.92 \times 8 = 7.36 \text{ -7} \\
 0.36 \times 8 = 2.88 \text{ -2}
 \end{array}$$

$$(76.28)_{10} = (114.2172)_8$$

$$(1001100)_2 = (4C)_{16}$$

$$\begin{array}{l}
 0.28 \times 16 = 4.48 \text{ -4} \\
 0.48 \times 16 = 7.68 \text{ -7} \\
 0.68 \times 16 = 10.88 \text{ -10(A)} \\
 0.88 \times 16 = 14.08 \text{ -14(E)}
 \end{array}$$

$$(76.28)_{10} = (4C.47AE)_{16}$$

2.

$$\begin{array}{l}
 1001.1010 \\
 = 2^3 \times 1 + 2^2 \times 1 + 2^1 \times 1 + 2^0 \times 1 \\
 = 8 + 4 + 2 + 1 \\
 = 15
 \end{array}$$

$$(1001.1010)_2 = (9.625)_{10}$$

$$(1001)_2 = (11)_8$$

$$0.625 \times 8 = 5 \text{ -5}$$

$$(1001.1010)_2 = (11.5)_8$$

$$(1001)_2 = (9)_{16}$$

$$0.625 \times 16 = 10 \text{ -10(A)}$$

$$(1001.1010)_2 = (9.A)_{16}$$

4.

$$\begin{array}{l}
 7F.24 \\
 = 16^1 \times 7 + 16^0 \times 15 + 16^{-1} \times 2 + 16^{-2} \times 4 \\
 = 112 + 15 + 0.125 + 0.015625 \\
 = 127.140625
 \end{array}$$

$$(7F.24)_{16} = (127.140625)_{10}$$

$$(1F)_{16} = (01111111)_2$$

$$\begin{array}{l}
 0.140625 \times 2 = 0.28 \text{ -0} \\
 0.28 \times 2 = 0.56 \text{ -0} \\
 0.56 \times 2 = 1.12 \text{ -1} \\
 0.12 \times 2 = 0.24 \text{ -0}
 \end{array}$$

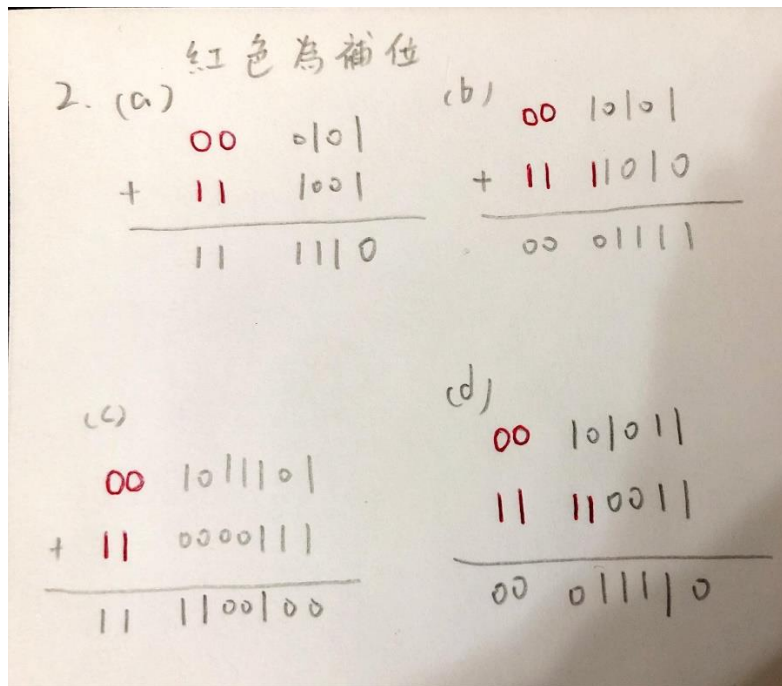
$$(7F.24)_{16} = (1111111.0010)_2$$

$$(1111111)_2 = (177)_8$$

$$\begin{array}{l}
 0.140625 \times 8 = 1.125 \text{ -1} \\
 0.125 \times 8 = 1 \text{ -1}
 \end{array}$$

$$(7F.24)_{16} = (177.11)_8$$

2. (16%) Perform the subtraction with the following unsigned binary numbers by taking the 2's complement of the subtrahend. (a) $0101 - 0111$, (b) $10101 - 0110$, (c) $1011101 - 1111001$, (d) $101011 - 1101$.



3. (16%) Convert decimal +29 and +75 to binary, using the signed-2's-complement representation and enough digits to accommodate the numbers, Then, perform the binary equivalent of $(+29)+(-75)$ and $(-29)+(-75)$ using addition. Convert the answers back to decimal and verify that they are correct.

$$29 = 16 + 8 + 4 + 1 = 2^4 + 2^3 + 2^2 + 2^0 \Rightarrow 00011101_{(2)}$$

$$75 = 64 + 8 + 2 + 1 = 2^6 + 2^3 + 2^1 + 2^0 \Rightarrow 01001011_{(2)}$$

$$-29 = 11100010 + 1 = 11100011_{(2)}$$

$$-75 = 10110100 + 1 = 10110101_{(2)}$$

$$(+29) + (-75)$$

$$\begin{array}{r} 00011101 \\ +) 10110101 \\ \hline 11010010_{(2)} \end{array}$$

$$\hookrightarrow -128 + 64 + 16 + 2 = -46_{(10)}$$

\Rightarrow sum is correct

$$(-29) + (-75)$$

$$\begin{array}{r} 11100011 \\ +) 10110101 \\ \hline 110011000 \end{array}$$

$$\hookrightarrow -256 + 128 + 16 + 8 = -104_{(10)}$$

\Rightarrow sum is correct

4. (8%) Write the word “NTHU” in ASCII using an eight-bit code including the space. Treat the leftmost bit of each character as a parity bit. Each 8-bit code should have even parity.

字元	十進位	十六進位	二進位	Ans: Even parity
N	78	4E	0100 1110	0100 1110
T	84	54	0101 0100	1101 0100
H	72	48	0100 1000	0100 1000
U	85	55	0101 0101	0101 0101

判斷是否為偶數個1，否則改最左位1

5. (8%) For an 8-bit sequence is 1001 0101. What is its content if it represents (a) two decimal digits in BCD? (b) two decimal number in the Excess-3 code? (c) an 8-bit unsigned number? (d) an 8-bit signed number?

5.

(a) $(1001\ 0101)_{\text{BCD}} = (2^3 + 2^0) \times 10^1 + (2^2 + 2^0) \times 10^0 = (95)_{10}$

(b) 查表知 $(1001\ 0101)_{\text{Excess-3}} = (62)_{10}$

Decimal Digit	BCD 8421	2421	Excess-3	8, 4, -2, -1
0	0000	0000	0011	0000
1	0001	0001	0100	0111
2	0010	0010	0101	0110
3	0011	0011	0110	0101
4	0100	0100	0111	0100
5	0101	1011	1000	1011
6	0110	1100	1001	1010
7	0111	1101	1010	1001
8	1000	1110	1011	1000
9	1001	1111	1100	1111
Unused bit combinations	1010	0101	0000	0001
	1011	0110	0001	0010
	1100	0111	0010	0011
	1101	1000	1101	1100
	1110	1001	1110	1101
	1111	1010	1111	1110

(c) $(1001\ 0101)_{\text{unsigned number}} = (2^7 + 2^4 + 2^2 + 2^0)_{10} = (149)_{10}$

(d) $(1001\ 0101)_{\text{signed number}} = (-2^7 + 2^4 + 2^2 + 2^0)_{10} = -(107)_{10}$

6. (4%) If you have 20 books and want to give each book a unique id with a binary number. If we want to use as least as possible the number of bits as the id, how many bits do you need?

(sol)

$$2^5 > 20 > 2^4$$

Ans : 5 bit

7. (12%) Find the Gray code sequence of 14 code words.

$M = 2k = 14$, $k = 7$

D	$d_3 d_2 d_1 d_0$	MSB ↑ $g_3 g_2 g_1 g_0$
0	0 0 0 0	0 0 0 0
1	0 0 0 1	0 0 0 1
2	0 0 1 0	0 0 1 1
3	0 0 1 1	0 0 1 0
4	0 1 0 0	0 1 1 0
5	0 1 0 1	0 1 1 1
6	0 1 1 0	0 1 0 1
7	0 1 1 1	1 1 0 1
8	1 0 0 0	1 1 1 1
9	1 0 0 1	1 1 1 0
10	1 0 1 0	1 0 1 0
11	1 0 1 1	1 0 1 1
12	1 1 0 0	1 0 0 1
13	1 1 0 1	1 0 0 0

First half $\frac{M}{2}$ codes

1° let MSB = 0 (g_3) , 2° $g_2 = d_3 \oplus d_2$
 $g_1 = d_2 \oplus d_1$
 $g_0 = d_1 \oplus d_0$

rest half $\frac{M}{2}$ code

3° copy & reverse the first half $g_2 g_1 g_0$
 4° let MSB $g_3 = 1$