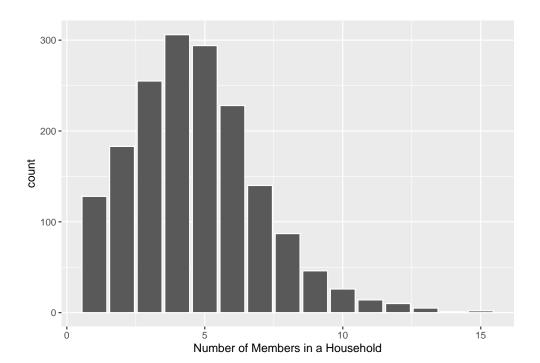
# project2\_test

 ${\rm Group}\_01$ 

2021/7/7

# Introduction

Data come from the FIES (Family Income and Expenditure Survey) recorded in the Philippines. The survey, which is undertaken every three years, is aimed at providing data on family income and expenditure. The data obtained from this survey are from different regions across the Philippines.



```
Total.Number.of.Family.members
                                     n percent
                                   128
                                          7.4%
                                2
                                         10.6%
                                   183
                                3
                                   255
                                         14.8%
                                4
                                   306
                                         17.7%
                                5
                                   294
                                          17.0%
                                6
                                   228
                                          13.2%
                                7
                                   140
                                          8.1%
                                           5.0%
                                8
                                    87
                                9
                                    46
                                           2.7%
                               10
                                    26
                                           1.5%
```

```
0.8%
   11
        14
               0.6%
   12
        10
              0.3%
   13
         5
   14
               0.1%
         1
   15
         2
               0.1%
Total 1725 100.0%
```

#### Total.Number.of.Family.members Total.Number.of.Family.members 1.00000000 Total.Household.Income 0.19228742 Total.Food.Expenditure 0.46924215 Household.Head.Age -0.06541636 House.Floor.Area -0.01415702 House.Age -0.07003586 Number.of.bedrooms 0.07207630 Electricity 0.09193871 Total. Household. Income Total. Food. Expenditure Total.Number.of.Family.members 0.19228742 0.469242145 Total.Household.Income 1.00000000 0.611494530 Total.Food.Expenditure 0.61149453 1.00000000 Household.Head.Age 0.06280405 -0.051724735 House.Floor.Area 0.23413840 0.124320633 House.Age 0.02471720 0.006725185 Number.of.bedrooms 0.44137375 0.355734454 Electricity 0.14866655 0.198610366 Household.Head.Age House.Floor.Area House.Age Total.Number.of.Family.members -0.06541636 -0.01415702 -0.070035856 Total.Household.Income 0.06280405 0.23413840 0.024717197 Total.Food.Expenditure 0.12432063 0.006725185 -0.05172474 Household.Head.Age 0.09057216 0.218079293 1.00000000 House.Floor.Area 0.09057216 1.00000000 0.074265080 House.Age 0.07426508 1.000000000 0.21807929 Number.of.bedrooms 0.15415511 0.37399081 0.123180471 0.10693465 0.085327324 Electricity -0.01304412 Number.of.bedrooms Electricity Total.Number.of.Family.members 0.0720763 0.09193871 Total.Household.Income 0.4413738 0.14866655 Total.Food.Expenditure 0.3557345 0.19861037 Household.Head.Age 0.1541551 -0.01304412 House.Floor.Area 0.3739908 0.10693465 House.Age 0.1231805 0.08532732 Number.of.bedrooms 1.0000000 0.21376315 Electricity 0.2137632 1.00000000

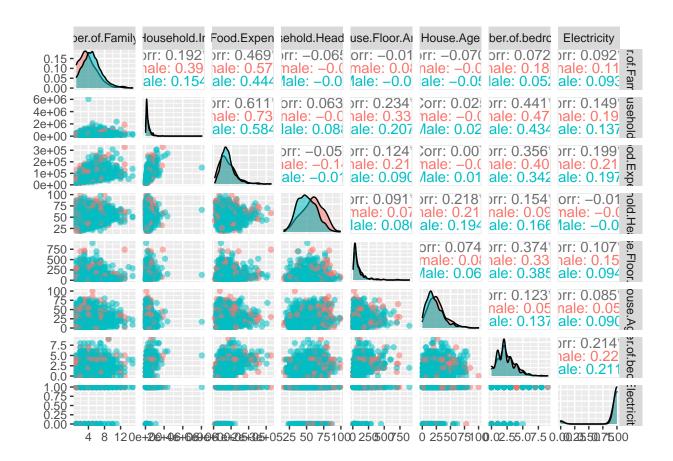


Table 1: Summary statistics of numerical variables

Variable	Missing	Complete	Mean	SD	Min.	1st Q.	Median	3rd Q.	
Total.Number.of.Family.members	0	1	4.67	2.33	1	3	4	6	
Total.Household.Income	0	1	269540.48	274564.17	11988	118565	188580	328335	6
Total.Food.Expenditure	0	1	80352.78	41194.36	6781	51922	73578	98493	
Household.Head.Age	0	1	52.23	14.52	17	41	52	63	
House.Floor.Area	0	1	90.92	99.20	5	32	54	102	
House.Age	0	1	22.98	15.32	0	12	20	31	
Number.of.bedrooms	0	1	2.26	1.44	0	1	2	3	
Electricity	0	1	0.93	0.26	0	1	1	1	

Type.of.Household n percent
Extended Family 569 33.0%
Single Family 1148 66.6%
Two or More Nonrelated Persons/Members 8 0.5%
Total 1725 100.0%

Household.Head.Sex n percent
Female 369 21.4%
Male 1356 78.6%
Total 1725 100.0%

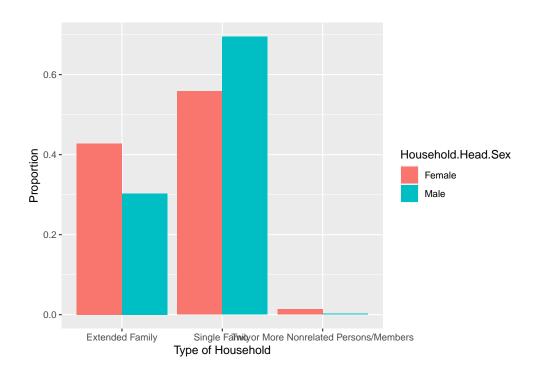
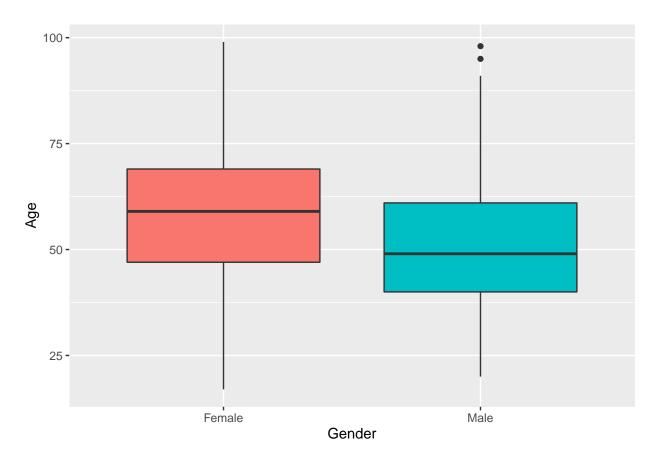


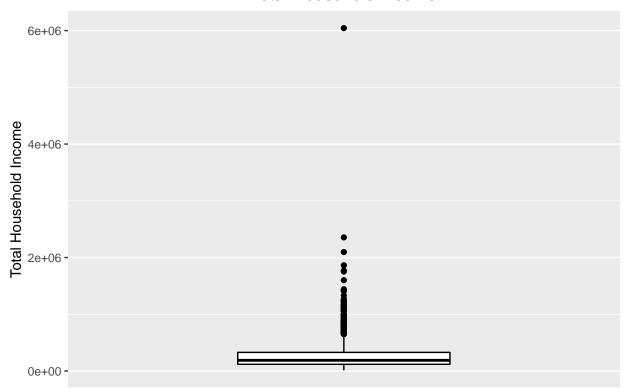
Figure 1: Barplot of household head'ssex by type of household

# Gender & Age

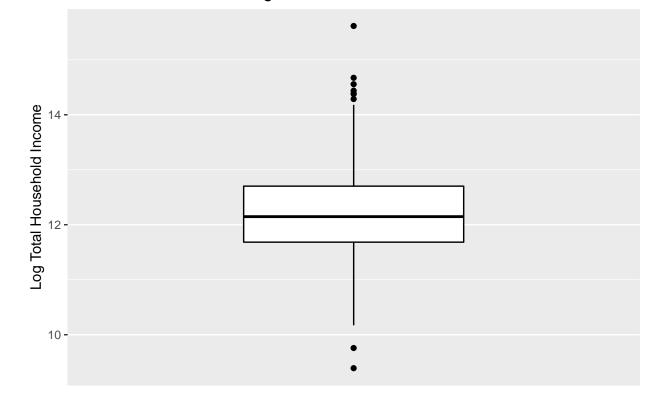


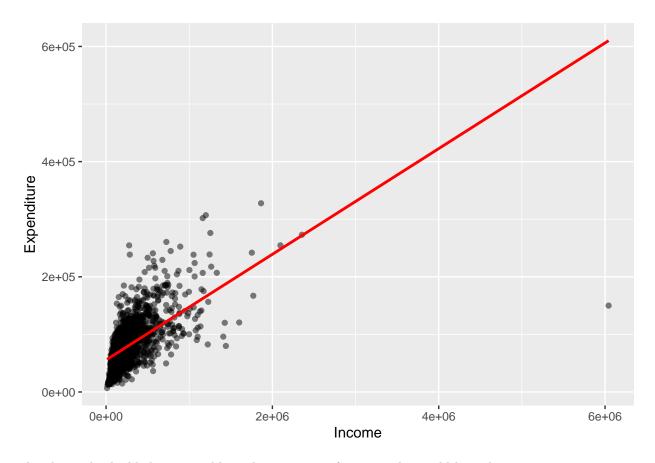
# Household Income Balance

# Total Household Income

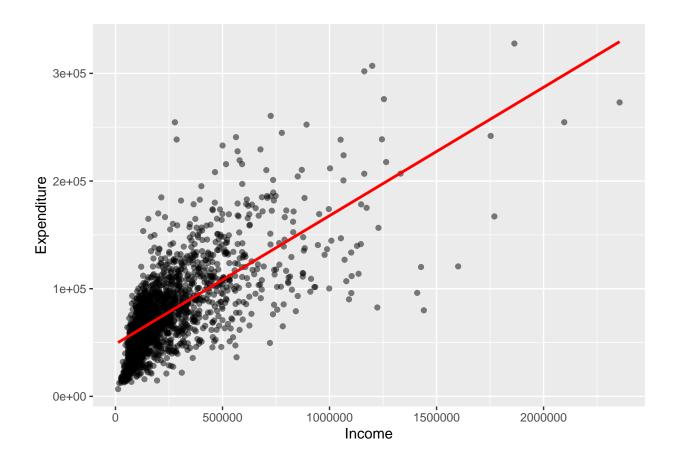


# Log Total Household Income





The above plot highlights a possible outlier in terms of income, this could be a data entry error or just an outlier. Removing this observation from the data set and plotting provides the following scatter diagram.



#### Model

```
Subset selection object
Call: regsubsets.formula(Total.Number.of.Family.members ~ ., data = data,
    nvmax = 10)
10 Variables (and intercept)
                                                        Forced in Forced out
Total.Household.Income
                                                            FALSE
                                                                       FALSE
Total.Food.Expenditure
                                                            FALSE
                                                                        FALSE
Household.Head.SexMale
                                                            FALSE
                                                                       FALSE
Household.Head.Age
                                                            FALSE
                                                                       FALSE
Type.of.HouseholdSingle Family
                                                            FALSE
                                                                       FALSE
Type.of.HouseholdTwo or More Nonrelated Persons/Members
                                                            FALSE
                                                                       FALSE
House.Floor.Area
                                                            FALSE
                                                                       FALSE
House.Age
                                                            FALSE
                                                                       FALSE
Number.of.bedrooms
                                                            FALSE
                                                                       FALSE
Electricity
                                                            FALSE
                                                                       FALSE
1 subsets of each size up to 10
Selection Algorithm: exhaustive
          Total.Household.Income Total.Food.Expenditure Household.Head.SexMale
  (1)
          11 11
                                 "*"
  (1)
3 (1)
                                 "*"
                                                         "*"
                                 "*"
          "*"
                                                         "*"
4 (1)
5 (1)
                                 "*"
                                                         "*"
```

```
"*"
6 (1)
         "*"
                                                       "*"
         "*"
                                "*"
                                                       "*"
7
  (1)
                                "*"
8 (1)
         "*"
                                                       "*"
9 (1)
         "*"
                                "*"
                                                       "*"
                                "*"
                                                       "*"
10 (1) "*"
         Household. Head. Age Type. of. Household Single Family
1 (1)
         11 11
                             "*"
         11 11
  (1)
3
  (1)
         11 11
                             "*"
4 (1)
         11 11
                             "*"
5 (1)
6
         11 11
                             "*"
  (1)
7
                             "*"
  (1)
                             "*"
         "*"
8 (1)
9 (1)
                             "*"
10 (1) "*"
                             "*"
          Type.of.HouseholdTwo or More Nonrelated Persons/Members
  (1)
         11 11
2 (1)
         11 11
3 (1)
4
 (1)
5 (1)
         11 11
6 (1)
7
  (1)
8 (1)
9 (1)
         "*"
10 (1) "*"
         House.Floor.Area House.Age Number.of.bedrooms Electricity
1 (1)
                          ......
                                    .. ..
                                                       .. ..
         11 11
2 (1)
                           11 11
         11 11
3
  (1)
                          11 11
                                    11 11
4 (1)
         11 11
5 (1)
         11 11
                          "*"
                                    11 11
         11 11
                          "*"
6 (1)
                          "*"
         11 11
                                    "*"
7
  (1)
         "*"
                           "*"
                                    "*"
8 (1)
                          "*"
                                    "*"
9 (1)
         "*"
10 (1) "*"
                           "*"
          CP
                BIC
Adj.R2
           8
                  6
Call:
glm(formula = Total.Number.of.Family.members ~ Total.Household.Income +
   Total.Food.Expenditure + Household.Head.Age + House.Floor.Area +
   House.Age + Number.of.bedrooms + Electricity, data = data)
Deviance Residuals:
             1Q
                  Median
                               3Q
                                       Max
-5.5671 -1.4626 -0.3084
                           1.2037 10.7417
Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
                       2.746e+00 2.667e-01 10.298 < 2e-16 ***
(Intercept)
```

```
Total.Household.Income -1.022e-06 2.384e-07 -4.287 1.91e-05 ***
Total.Food.Expenditure 3.197e-05 1.540e-06 20.759 < 2e-16 ***
Household.Head.Age -4.491e-04 3.520e-03 -0.128 0.89850
House.Floor.Area -7.261e-04 5.357e-04 -1.355 0.17550
House.Age -9.472e-03 3.301e-03 -2.870 0.00416 **
Number.of.bedrooms -9.756e-02 4.121e-02 -2.367 0.01802 *
Electricity 1.696e-01 1.929e-01 0.879 0.37955 ---
```

Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for gaussian family taken to be 4.130968)

Null deviance: 9384.0 on 1724 degrees of freedom Residual deviance: 7092.9 on 1717 degrees of freedom

AIC: 7352.3

Number of Fisher Scoring iterations: 2

#### Call:

glm(formula = Total.Number.of.Family.members ~ Total.Household.Income +
 Total.Food.Expenditure + House.Age + Number.of.bedrooms,
 data = data)

### Deviance Residuals:

Min 1Q Median 3Q Max -5.5796 -1.4561 -0.3048 1.1778 10.6187

#### Coefficients:

Estimate Std. Error t value Pr(>|t|)

(Intercept) 2.828e+00 1.375e-01 20.560 < 2e-16 \*\*\*

Total.Household.Income -1.061e-06 2.364e-07 -4.487 7.71e-06 \*\*\*

Total.Food.Expenditure 3.229e-05 1.513e-06 21.340 < 2e-16 \*\*\*

House.Age -9.507e-03 3.223e-03 -2.950 0.00322 \*\*

Number.of.bedrooms -1.103e-01 3.855e-02 -2.862 0.00425 \*\*

Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for gaussian family taken to be 4.129948)

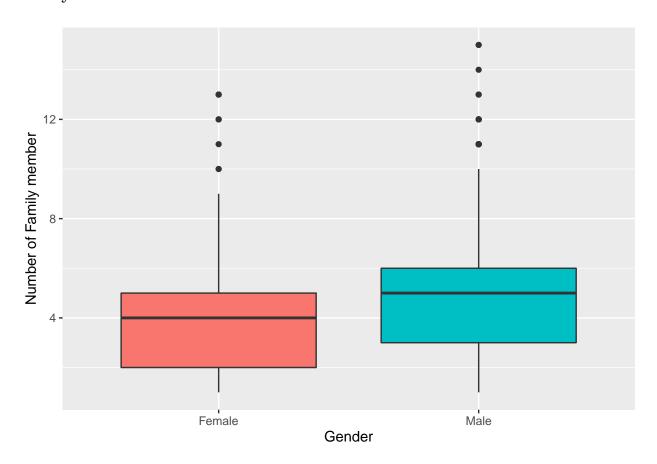
Null deviance: 9384.0 on 1724 degrees of freedom Residual deviance: 7103.5 on 1720 degrees of freedom

AIC: 7348.8

Number of Fisher Scoring iterations: 2

Model	AIC	BIC
Full Model	7352.25	7401.33
Significant Factors Model	7348.84	7381.56

### Family Members & Gender



Hence we can see that the male household head's number of family members tend to be more then the female's.

## Log-odds

```
glm(formula = Household.Head.Sex ~ Total.Number.of.Family.members,
   family = binomial(link = "logit"), data = data.sex_number)
Deviance Residuals:
   Min
             1Q
                  Median
                                3Q
                                        Max
-2.4219
         0.4705
                   0.6602
                            0.7163
                                     0.9054
Coefficients:
                               Estimate Std. Error z value Pr(>|z|)
(Intercept)
                               0.49674
                                           0.13174
                                                     3.771 0.000163 ***
Total.Number.of.Family.members 0.18319
                                           0.02844
                                                     6.442 1.18e-10 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 1790.9 on 1724 degrees of freedom
```

Residual deviance: 1745.4 on 1723 degrees of freedom

AIC: 1749.4

Number of Fisher Scoring iterations: 4

[1] "Female" "Male"

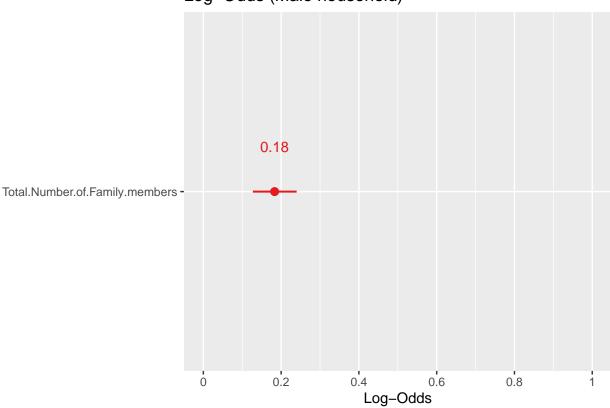
$$\ln\left(\frac{p}{1-p}\right) = \alpha + \beta \cdot \text{number of family members} = 0.5 + 0.18 \cdot \text{number of family members},$$

Where p = Prob(Male) and 1 - p = Prob(Female). Hence, the log-odds of the household being male increase by 0.18 for every one unit increase in number of family members. This provides us with a point estimate of how the log-odds changes with age.

However, we are also interested in producing a 95% confidence interval for these log-odds.

	2.5 %	97.5 %
(Intercept)	0.2388990	0.7555347
Total.Number.of.Family.members	0.1282353	0.2397474

## Log-Odds (Male household)



Now, let's add the estimates of the log-odds to our data set:

# Odds

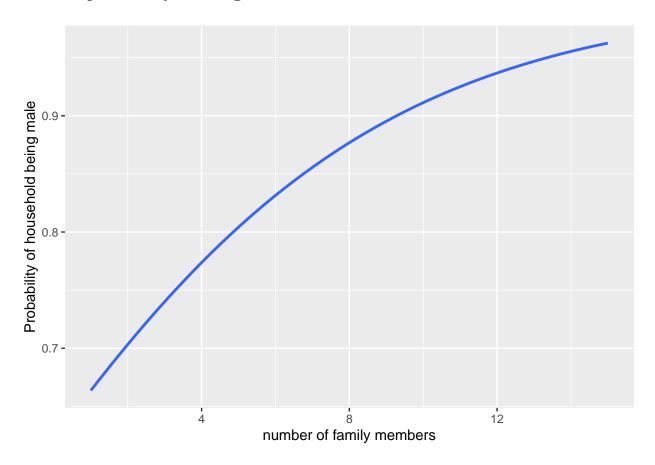
# Odds (Male household)



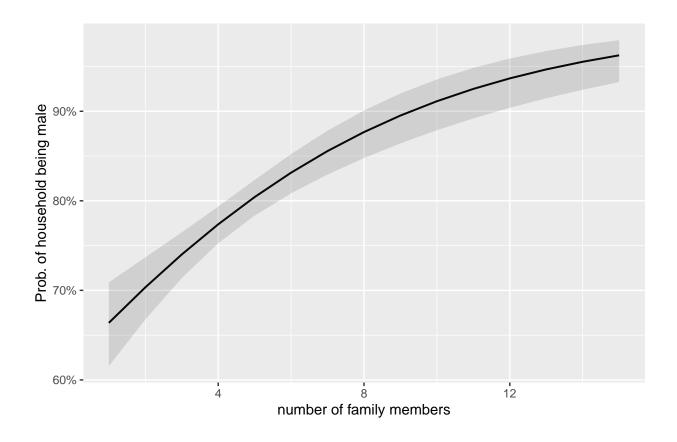
Now, let's add the estimates of the odds to our data set:

# Probabilities

# Plot the probability of being male



\$Total.Number.of.Family.members



## GLM

### Call:

```
glm(formula = Total.Number.of.Family.members ~ Total.Household.Income +
    Total.Food.Expenditure + Household.Head.Sex + Household.Head.Age +
    Type.of.Household + House.Floor.Area + House.Age + Number.of.bedrooms +
    Electricity, family = binomial(link = "logit"), data = data)
```

#### Deviance Residuals:

Min	1Q	Median	3Q	Max
-4.2298	0.0000	0.0291	0.1946	1.8561

#### Coefficients:

	Estimate	Std. Error
(Intercept)	1.944e+01	6.821e+02
Total.Household.Income	-3.557e-06	1.017e-06
Total.Food.Expenditure	1.048e-04	9.895e-06
Household.Head.SexMale	1.143e+00	2.734e-01
Household.Head.Age	-5.534e-03	7.499e-03
Type.of.HouseholdSingle Family	-2.243e+01	6.821e+02
Type.of.HouseholdTwo or More Nonrelated Persons/Members	-7.011e+00	9.230e+03
House.Floor.Area	1.484e-03	1.224e-03
House.Age	-9.422e-04	7.817e-03
Number.of.bedrooms	-1.774e-01	1.034e-01
Electricity	3.235e-01	3.411e-01

```
z value Pr(>|z|)
(Intercept)
                                                          0.028 0.977268
Total.Household.Income
                                                         -3.497 0.000471 ***
Total.Food.Expenditure
                                                         10.595 < 2e-16 ***
Household.Head.SexMale
                                                          4.181 2.91e-05 ***
Household.Head.Age
                                                         -0.738 0.460510
Type.of.HouseholdSingle Family
                                                         -0.033 0.973771
Type.of.HouseholdTwo or More Nonrelated Persons/Members -0.001 0.999394
House.Floor.Area
                                                          1.212 0.225414
House.Age
                                                         -0.121 0.904055
Number.of.bedrooms
                                                         -1.715 0.086317 .
                                                          0.948 0.343015
Electricity
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 912.10 on 1724 degrees of freedom
Residual deviance: 448.76 on 1714 degrees of freedom
AIC: 470.76
Number of Fisher Scoring iterations: 20
glm(formula = Total.Number.of.Family.members ~ (Total.Household.Income +
   Total.Food.Expenditure + Household.Head.Age + Type.of.Household +
    House.Floor.Area + House.Age + Number.of.bedrooms + Electricity) *
   Household.Head.Sex, family = binomial(link = "logit"), data = data)
Deviance Residuals:
   Min
              10
                 Median
                                3Q
                                        Max
-3.8031
         0.0000 0.0179 0.1650
                                     1.8853
Coefficients:
                                                                                 Estimate
(Intercept)
                                                                                2.047e+01
Total.Household.Income
                                                                               -1.270e-06
Total.Food.Expenditure
                                                                                7.284e-05
Household.Head.Age
                                                                               -3.633e-02
Type.of.HouseholdSingle Family
                                                                               -1.963e+01
Type.of.HouseholdTwo or More Nonrelated Persons/Members
                                                                               -3.269e+00
House.Floor.Area
                                                                                6.403e-03
House.Age
                                                                               -2.041e-03
Number.of.bedrooms
                                                                               -1.696e-01
Electricity
                                                                               -1.269e+00
Household.Head.SexMale
                                                                                2.751e-02
Total.Household.Income:Household.Head.SexMale
                                                                               -2.883e-06
Total.Food.Expenditure:Household.Head.SexMale
                                                                                5.175e-05
Household.Head.Age:Household.Head.SexMale
                                                                                4.213e-02
Type.of.HouseholdSingle Family:Household.Head.SexMale
                                                                               -4.123e+00
Type.of.HouseholdTwo or More Nonrelated Persons/Members:Household.Head.SexMale -5.502e+00
House.Floor.Area:Household.Head.SexMale
                                                                               -6.356e-03
House.Age:Household.Head.SexMale
                                                                                2.190e-03
```

-3.489e-02

Number.of.bedrooms:Household.Head.SexMale

Electricity:Household.Head.SexMale	1.999e+00
	Std. Error
(Intercept)	1.884e+03
Total.Household.Income	2.334e-06
Total.Food.Expenditure	1.502e-05
Household.Head.Age	1.423e-02
Type.of.HouseholdSingle Family	1.884e+03
Type.of.HouseholdTwo or More Nonrelated Persons/Members	1.234e+04
House.Floor.Area	3.016e-03
House. Age	1.535e-02
Number.of.bedrooms	2.101e-01
Electricity	7.165e-01
Household. Head. SexMale	2.021e+03
Total.Household.Income:Household.Head.SexMale	2.612e-06
Total.Food.Expenditure:Household.Head.SexMale	2.026e-05
Household.Head.Age:Household.Head.SexMale	1.702e-02
Type.of.HouseholdSingle Family:Household.Head.SexMale	2.021e+03
Type.of.HouseholdTwo or More Nonrelated Persons/Members:Household.Head.SexMale	1.905e+04
House.Floor.Area:Household.Head.SexMale	3.348e-03
House.Age:Household.Head.SexMale	1.807e-02
Number.of.bedrooms:Household.Head.SexMale	2.451e-01
Electricity:Household.Head.SexMale	8.175e-01
( <del>-</del>	z value
(Intercept)	0.011
Total.Household.Income	-0.544
Total.Food.Expenditure	4.849
Household. Head. Age	-2.552
Type.of.HouseholdSingle Family	-0.010
Type.of.HouseholdTwo or More Nonrelated Persons/Members	0.000
House.Floor.Area	2.123
House. Age	-0.133
Number.of.bedrooms	-0.807
Electricity	-1.772
Household.Head.SexMale	0.000
Total.Household.Income:Household.Head.SexMale	-1.104
Total.Food.Expenditure:Household.Head.SexMale	2.554
Household.Head.Age:Household.Head.SexMale	2.476
Type.of.HouseholdSingle Family:Household.Head.SexMale	-0.002
Type.of.HouseholdTwo or More Nonrelated Persons/Members:Household.Head.SexMale	0.000
House.Floor.Area:Household.Head.SexMale	-1.899
House.Age:Household.Head.SexMale	0.121
Number.of.bedrooms:Household.Head.SexMale	-0.142
Electricity:Household.Head.SexMale	2.445
	Pr(> z )
(Intercept)	0.9913
Total.Household.Income	0.5863
Total.Food.Expenditure	1.24e-06
Household. Head. Age	0.0107
Type.of.HouseholdSingle Family	0.9917
Type.of.HouseholdTwo or More Nonrelated Persons/Members	0.9998
House.Floor.Area	0.0337
House. Age	0.8942
Number.of.bedrooms	0.4197
Electricity	0.0765

Household.Head.SexMale Total.Household.Income:Household.Head.SexMale Total.Food.Expenditure:Household.Head.SexMale Household.Head.Age:Household.Head.SexMale Type.of.HouseholdSingle Family:Household.Head.SexMale Type.of.HouseholdTwo or More Nonrelated Persons/Members:Household.Head.SexMale House.Floor.Area:Household.Head.SexMale House.Age:Household.Head.SexMale Number.of.bedrooms:Household.Head.SexMale Electricity:Household.Head.SexMale	1.0000 0.2698 0.0107 0.0133 0.9984 0.9998 0.0576 0.9035 0.8868 0.0145
(Intercept)	
Total.Household.Income	
Total.Food.Expenditure	***
Household.Head.Age	*
Type.of.HouseholdSingle Family	
Type.of.HouseholdTwo or More Nonrelated Persons/Members	
House.Floor.Area	*
House.Age	
Number.of.bedrooms	
Electricity	•
Household.Head.SexMale Total.Household.Income:Household.Head.SexMale	
	*
Total.Food.Expenditure:Household.Head.SexMale Household.Head.Age:Household.Head.SexMale	*
Type.of.HouseholdSingle Family:Household.Head.SexMale	•
Type.of.HouseholdTwo or More Nonrelated Persons/Members:Household.Head.SexMale	
House.Floor.Area:Household.Head.SexMale	
House. Age: Household. Head. SexMale	•
Number.of.bedrooms:Household.Head.SexMale	
Electricity: Household. Head. SexMale	*
Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1	
(Dispersion parameter for binomial family taken to be 1)	
Null deviance: 912.1 on 1724 degrees of freedom	
Residual deviance: 426.7 on 1705 degrees of freedom	
AIC: 466.7	

Number of Fisher Scoring iterations: 20

Model	AIC	BIC
No Interactions Interactions with Head of Household Sex	470.76 466.70	000