

Error in pBCS-S.C. CPMC

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1 Introduction

For the "worried part" we discussed before, I found that due to some mistake it converged to the wrong results in S.C.CPMC with exact input and when I correct, it then converge to the correct results. (Please check the Figure.1)

There are two main "hard to understand" parts in the experiments of Error in pBCS S.C. CPMC

1. With exact density matrix from ED, we can get following pBCS state and with Variational Method the error between the density matrix of pBCS and Ground state can be minimized.

However, we found that in 4*4 u=8 3up 3dn, 4*4 u=8 5up 5dn, 4*4 u=8 7up 7dn the mixed density matrix $\langle FE|C_i^\dagger C_j|pBCS\rangle/\langle FE|pBCS\rangle$ always equal to $\langle FE|C_i^\dagger C_j|FE\rangle/\langle FE|FE\rangle$. ("FE" means "Free electrons")

2. With exact density matrix from ED and extrapolation, statistic error must cover exact error ($ExactDensityMatrix - DensityMatrixfromCPMC$) . However in system 4*4 u=8 3up 3dn and 4*4 u=8 7up 7dn, systemic error always exist. Because of degeneracy?

Also there is one small question: how to get a good results in 4*4 u=8 3up 3dn with CPMC like Hao's "Symmetry" paper?

2 Results

Figure 1: This is the results of 4 by 4 2-D Hubbard model in PBS with 7up 7dn electrons. 20 step S.C. CPMC with "Analytic Decomposed pBCS" trial wave functions.

Error in Density, extrapolate, Exact input pBCS CPMC									
4477u8 t0.01t0.02 Exact Energy:-11.875287631894714 step 20 Energy:-11.86421714 0.01674376 -11.36972425 0.00284917									
Exact Nsample: 20 Nwalker: 500*2*20									
real	imag			real	imag	error	real abs(exact-cpmc)	imag abs(exact-cpmc)	
0.4375	0			0.431053	2.08E-05	2.17E-03	0.006447019	2.07513E-05	
0.132315	4.47E-03			0.129476	-3.39E-03	2.03E-03	0.002838677	0.007862298	
0.4375	0			0.440519	1.04E-04	2.56E-03	0.003019348	0.000104109	
						1.06E+00	1.24E+01	2.74E+00	
4477u8 with t0.01t0.02 input Exact Energy:-11.8688 step 20 Energy:-11.89700886 0.01264702 -11.42273882 0.00347112									
Exact Nsample: 20 Nwalker: 500*2*20									
real	imag			real	imag	error	real abs(exact-cpmc)	imag abs(exact-cpmc)	
0.4375	0			0.434426	1.52E-06	1.87E-03	0.003074049	1.52376E-06	
0.140854	0			0.129763	6.93E-06	1.88E-03	0.011090724	6.92843E-06	
0.4375	0			0.437924	-5.23E-06	1.58E-03	0.000424262	5.23312E-06	
						1.08E+00	8.19E+00	5.91E-03	

Figure 2: This is the results of 4 by 4 2-D Hubbard model in PBS with 3up 3dn electrons, "Analytic", "DET" and "FE" are "Analytic Decomposed pBCS", "Determinant Decomposed pBCS" and "Free Electrons" trial wave functions.

Error in Density, extrapolate, Exact input pBCS CPMC									
4433u8 Exact Energy:-14.7235403 Energy:-14.45620188 0.04688154 -14.13803685 0.0069 Energy:-14.37520483 0.02654943 -14.14105856 0.0031 Energy:-14.37024105 0.02282915 -14.13616755 0.00143155									
Exact Nsample: 5 Nwalker: 500*4 Error ABS(Exact-CPMC) Nsample: 10 Nwalker: 500*4 Error ABS(Exact-CPMC) Nsample: 20 Nwalker: 500*4 Error ABS(Exact-CPMC)									
0.1875		0.194188812	5.78E-03	0.005689		0.195082504	2.90E-03	0.007583	0.197547126 2.08E-03 0.010047
0.1875		0.201927973	5.30E-03	0.014428		0.200189528	3.19E-03	0.01269	0.201581582 1.82E-03 0.014082
		2.72E+00	2.97E+00			2.00E+00	2.47E+00		1.42E+00 2.19E+00

Figure 3: This is the results of 4 by 4 2-D Hubbard model in PBS with 5up 5dn electrons, "Analytic", "DET" and "FE" are "Analytic Decomposed pBCS", "Determinant Decomposed pBCS" and "Free Electrons" trial wave functions.

Error in Density, extrapolate, Exact input pBCS CPMC									
4455u8 Exact Energy: Analytic step 1 Energy:-17.45047399 0.05233907 -17.6341 Analytic step 1 Energy:-17.48395020 0.03169573 -17.62970079 Analytic step 1 Energy:-17.43572441 0.02470176 -17.63823991 0.00266869									
Exact Nsample: 5 Nwalker: 500*4 error abs(exact-cpmc) Nsample: 10 Nwalker: 500*4 error abs(exact-cpmc) Nsample: 20 Nwalker: 500*4 error abs(exact-cpmc)									
0.3125		0.313523057	4.28E-03	0.001023		0.311046278	1.47E-03	0.001454	0.313709897 1.62E-03 0.00121
0.3125		0.312244648	1.89E-03	0.000285		0.313786409	4.96E-03	0.00128	0.31086138 3.95E-03 0.00119
		2.54E+00	2.195605			1.93E+00	1.7678		1.42E+00 1.404117
DET step 1 Energy:-17.53840230 0.07492043 -17.4447396/DET step 1 Energy:-17.46658851 0.01599752 -17.44785561 0.02621622 -17.44871372 0.00359000									
Exact Nsample: 5 Nwalker: 500*4 error abs(exact-cpmc) Nsample: 10 Nwalker: 500*4 error abs(exact-cpmc) Nsample: 20 Nwalker: 500*4 error abs(exact-cpmc)									
0.3125		0.31198012	4.46E-03	0.00052		0.313423995	2.91E-03	0.000924	0.313337831 1.90E-03 0.000838
0.3125		0.307727689	3.18E-03	0.004772		0.313177431	4.85E-03	0.000677	0.311494321 1.86E-03 0.001006
		2.50E+00	2.339496			1.90E+00	1.837722		1.51E+00 1.415466
FE step 1 Energy:-17.45587549 0.04011663 -17.45087672 FE step 1 Energy:-17.47736162 0.03355420 -17.44830195 0.01747667895 0.02275442 -17.45142914 0.00304038									
Exact Nsample: 5 Nwalker: 500*4 error abs(exact-cpmc) Nsample: 10 Nwalker: 500*4 error abs(exact-cpmc) Nsample: 20 Nwalker: 500*4 error abs(exact-cpmc)									
0.3125		0.316154197	7.07E-03	0.003654		0.314971574	4.03E-03	0.002472	0.315619603 2.18E-03 0.00312
0.3125		0.308877554	2.41E-03	0.003622		0.310400338	2.21E-03	0.00021	0.311995392 1.69E-03 0.000505
		2.45E+00	2.223363			1.79E+00	1.66393		1.28E+00 1.259751

Figure 4: This is the results of 4 by 4 2-D Hubbard model in PBS with 7up 7dn electrons. CPMC with "Analytic Decomposed pBCS" trial wave functions.

Error in Density, extrapolate, Exact Extrapolate									
4477u8 t0.01t0.02 Exact Energy:-11.94277480 0.11438742 -11.40644238 0.02 step 1 Energy:-11.89983622 0.08053707 -11.39274051 0.02 step 1 Energy:-11.85013709 0.05106370 -11.36726030 0.00897944									
Exact Nsample: 5 Nwalker: 500*4 real imag error real abs(exact-cpmc) real imag error real abs(exact-cpmc) real imag error real abs(exact-cpmc) real imag error real abs(exact-cpmc)									
0.4375	0			0.440525	-5.48E-04	1.11E-02	0.003025	0.000548	0.42885 2.51E-04 9.73E-03 0.00895 0.000251
0.132315	4.47E-03			0.131414	-2.65E-03	3.97E-03	0.0009	0.007102	0.122207 -2.26E-03 6.00E-03 0.001098 0.00673
0.4375	0			0.472916	-7.29E-04	1.11E-02	0.035416	0.000729	0.420339 -4.14E-04 9.11E-03 0.017161 0.000414
				6.09E+00	1.53E+01	3.91E+00			5.72E+00 1.50E+01 3.17E+00
4477u8 with t0.01t0.02 input Exact Energy:-11.8688 step 1 Energy:-11.87210960 0.05635029 -11.42729617 0.00945646									
Exact Nsample: 20 Nwalker: 500*4 real imag error real abs(exact-cpmc) real imag error real abs(exact-cpmc)									
0.4375	0			0.426261	3.53E-06	5.51E-03	0.011239	3.53E-06	
0.140854	0			0.137516	-1.83E-05	7.40E-03	0.003338	1.83E-05	
0.4375	0			0.440952	-6.24E-05	8.64E-03	0.003450	6.24E-05	
							3.31E+00	9.06E+00	2.70E-02

Figure 5: The error between the Density Matrix of Analytic pBCS, VMpBCS and Exact Denisty Matrix.

Figure 10 consists of two line plots. The left plot shows the number of iterations for the 'Exact' method (blue line), 'pBGS' (orange line), and 'VMpBGS' (grey line) across 16 iterations. The y-axis ranges from 0.00E+00 to 1.00E+00. The 'Exact' method shows a sharp increase in iterations around iteration 12, reaching approximately 0.95. The 'pBGS' and 'VMpBGS' methods show a similar sharp increase around iteration 12, reaching approximately 0.90. The right plot shows the number of iterations for 'pBGS' (orange line) and 'VMpBGS' (grey line) across 16 iterations. The y-axis ranges from 0 to 0.06. The 'pBGS' method shows a sharp increase in iterations around iteration 12, reaching approximately 0.055. The 'VMpBGS' method shows a similar sharp increase around iteration 12, reaching approximately 0.05.