

it is one of the ~~deadlock~~ cases present deadlock will not occur.

Mutual exclusion:  $\rightarrow$  NO two processes use the same single resource simultaneously  
i.e. only one process access a resource at a time

$\rightarrow$  Mutual should be true for deadlock

Hold and wait:  
process are holding atleast one resource and waiting for the acquisition of the additional resource

Circular wait  
 $\rightarrow$  There exist closed chain of process such that each process holds atleast one resource needed by the next process in the chain

(or)  
There exist a set of ~~processes~~  $\{P_0, P_1, P_2, \dots, P_m\}$

of waiting process such that  $P_0$  is waiting for resource that is held by  $P_1$ ,  $P_1$  is waiting for resource that is held by  $P_2$  or Resource that is held by  $\underline{P_0}$

NO preemption:

process can release only voluntarily  
of the resources held by the process

→ no resource can be removed from the  
process by holding it

### Resource Allocation Graph (RAG)

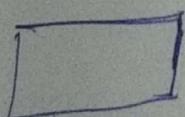
→ RAG denotes the current state of the  
system

state:  
→ how many processes available  
→ how many resources available  
→ how resources held by process

$$G = (V, E)$$

Here, vertices are represents the process & resources

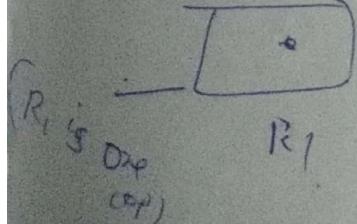
○ → process



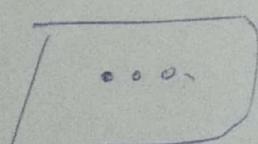
Resource

Single  
instance

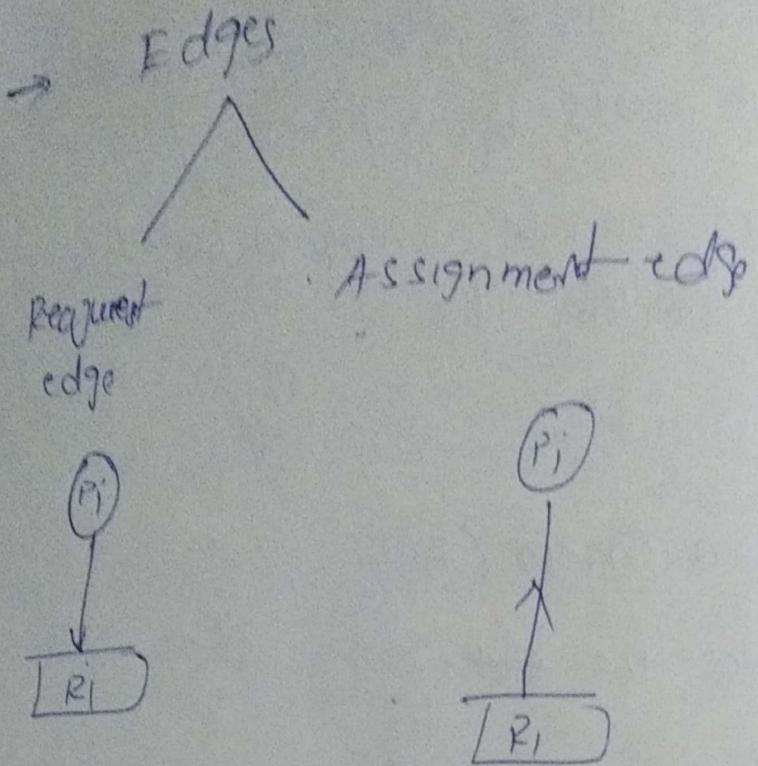
of Resource



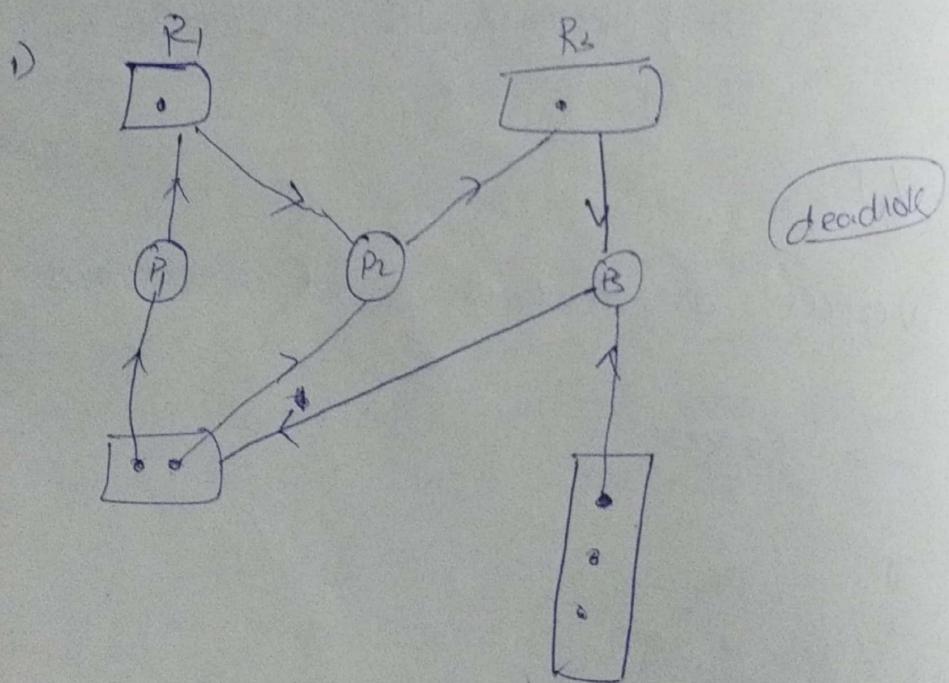
multiple instn  
of Resoures



$(R_2 \text{ is } O_{P_2})$



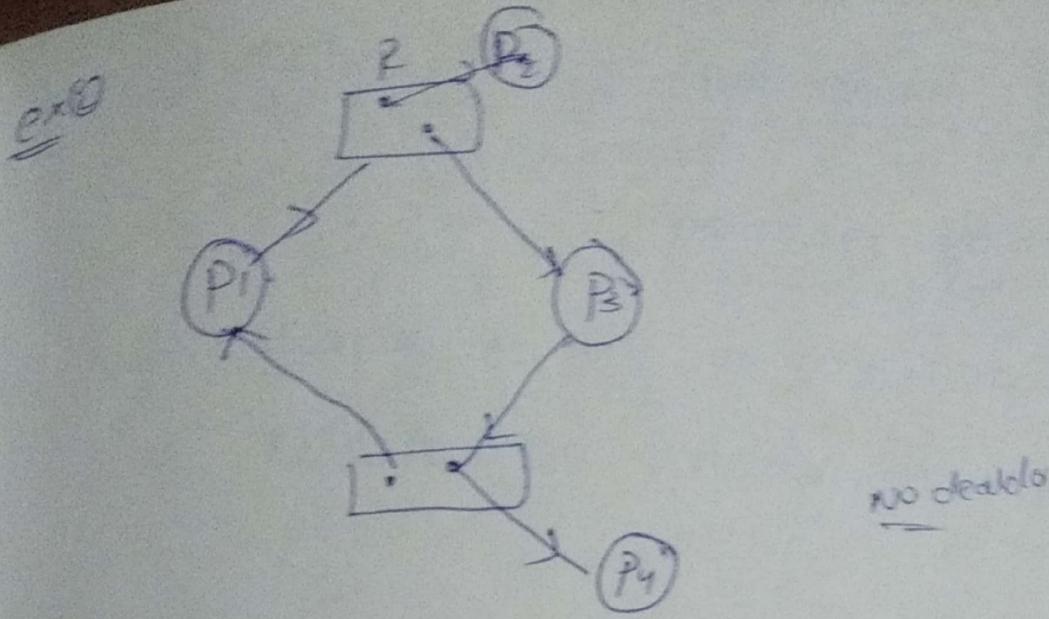
ex



$P_1 - P_2 - P_3 - A$

1) circular wait  
2) hold wait

④ it is a ~~dead~~ deadlock



P<sub>1</sub>-R<sub>2</sub>-P<sub>2</sub> → circular wait

→ ~~but~~ P<sub>2</sub>, P<sub>1</sub> and P<sub>3</sub> are in hold and wait condition  
 but P<sub>4</sub>, P<sub>2</sub> are not in hold and wait. so  
 after some time it ~~is~~ P<sub>2</sub>, P<sub>4</sub> will be released

### Observation

- if RAG containing No cycles then "no deadlock"
- if RAG contains cycles:
  - if there is only one instance for resource type then there is a deadlock (necessary and sufficient conditions to fall deadlock)
  - if there are several instances for resource type then there is a possibility of deadlock (it is necessary but not sufficient conditions).

Possibility → may (or) may not

Methods for handling of deadlock

① Deadlock prevention :-  
→ Disatisfying the one of necessary and sufficient conditions of deadlock

Mutual exclusion: If cannot be ~~deadlock~~ satisfied since every resource access must be the mutually exclusive

Hold & wait: Disatisfying the hold and wait means either hold the resources or wait for the resources but not both at a time

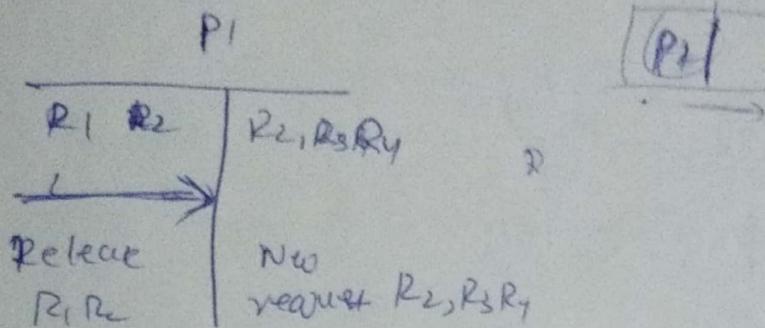
Condition to disatisfy hold and wait:

- I) \* Take all required resources before beginning of execution
- \* so that while executing it can process cannot request resources

Limitation (or condition)

- \* Resources not properly utilized and process get starved

2) You can make new request for the resource -  
by releasing held resources



### Limitation:

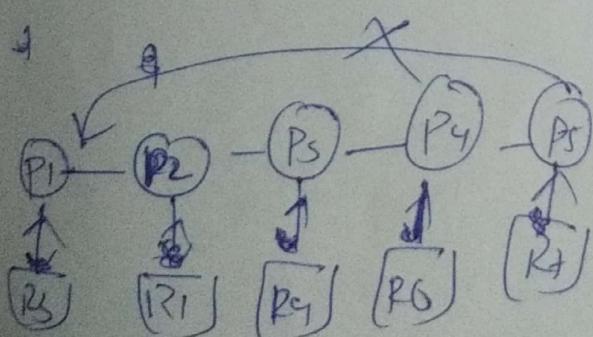
Current process will get starved if  $R_2, R_3, R_4$  all not available are busy with other process

### Circular wait:

→ Disallowing the circular wait by breaking the cycle

\* All resources in the system uniquely identified by the id or number

\* never allow process to ~~make request to lower~~ request number resources than the last one requested and allocated



→ Don't allow process  $P_5$

to request  $R_5$  because it have number 1 id

$$R_1 = 10$$

$$R_2 = 15$$

$$R_3 = 5$$

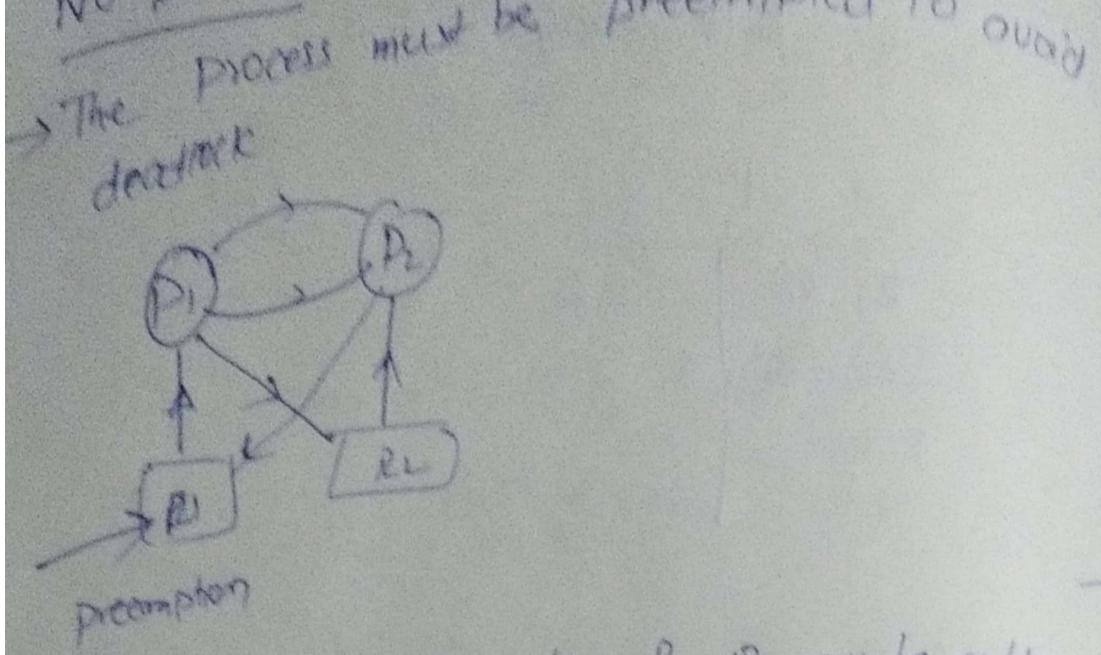
$$R_4 = 20$$

$$R_5 = 30$$

$$R_6 = 35$$

$$R_7 = 40$$

$$R_8 = 45$$



when you apply preemption  $R_1, R_1$  will be allocated to  $P_2$  and after some time  $P_2$  will release  $R_2$  and  $R_1$  is again can be used by  $P_1$

NOTE :

→ Deadlock prevention is more restrictive than

Deadlock avoidance

because in deadlock prevention we are restricting

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## II. Deadlock avoidance :-

- It is a simple to implement.
- It works on the state of the system.
- It need a priori information about
- process' ~~request~~ request for resources i.e. processes must declare their maximum demand of resource.

### System States :-

- ① Safe state [no deadlock]
- ② unsafe state [leads to deadlock]  
↓  
It ~~is~~ possibility to deadlock

### Safe State :-

A state is a safe if the system can allocate resources to each (upto its maximum) in some order and avoid the deadlock

(Or)

A state is safe only if there exist a safe sequence:

### Safe Sequence :-

A sequence of processes  $(P_1, P_2, P_3, \dots, P_m)$  is a safe sequence for the current allocation state if for each  $P_i$ , the resource that  $P_i$  can still request can be

satisfied currently available resources +  
The Resources held by all  $P_j$  (Pending Pro)

→ "Deadlock avoidance algorithm" uses

"Resource allocation Graph" for single instances.

→ Deadlock avoidance uses "Banker's algorithm" for multiple instances

### Banker's Algorithm

$\langle P_0, P_1, P_2 \dots P_m \rangle$

$m$  - Resources

$\langle R_0, R_1, R_2 \dots R_n \rangle$

① Maximum  $[1 \dots n, 1 \dots m]_{n \times m}$

$$\max [i, j] = k$$

$(P_i) \rightarrow k(R_j)$

process  $P_i$  requires  $k$  copies (instances) of Resource of  $R_j$  type

process  $P_i$  its peak demand of  $k$  copies of Resource  $R_j$  type

(2) Allocation  $[1 \dots n, 1 \dots m]_{n \times m}$

Allocation  $[i, j] = (=)$   $(P_i) \leftarrow o[R_j]$

a. copies ~~o~~ instances of  $R_j$  type is allocated  
to process  $P_i$

$$o \leq k$$

(3) Need  $[1 \dots n, 1 \dots m]_{n \times m}$

Need  $[i, j]$

$(P_i)' \xrightarrow{\text{Need}} b[R_j]$

→ process  $P_i$  remaining need Resource  $R_j$  type  
~~b~~  $\rightarrow$  'b' copies of Resource  $R_j$  type

$$b = k - o$$

(4) Request  $[1 \dots n, 1 \dots m]_{n \times m}$

Request  $[i, j]$

$(P_i) \xrightarrow{\text{Request}} c[R_j]$

process  $P_i$  Request  $\leq$  copies of  
Resource  $R_j$  type at time  $t$

$$c \leq b$$

Total [ $1 \dots m$ ]

$\text{Total}[j] = d$

There are  $d$  copies of Resource type  $j$

Available [ $1 \dots m$ ]

$\text{Available}[j] = e$

~~Ans~~ There are  $e$  copies of Resource  $R_j$  type still available at time  $t$ .

C1

Let us consider 5 process  $n = \{P_1, P_2, P_3, P_4, P_5\}$

$m = 1$ ,  $R = 29$  (Total)

Q  $m = 1$  (Resource type = 1)

$R > 29$  ( 29 copies )

Pid	max Demand	Allocation	Need	available
$P_1$	10	5	5	① 3 ② $1+3=4$ ③ $4-3=1$
$P_2$	5	2	3	④ $1+5=6$ ⑤ $6-5=1$
$P_3$	17	8	9	⑥ $1+10=11$ ⑦ $11-9=2$
$P_4$	3	1	2	⑧ $2+17=19$ ⑨ $19-10=9$
$P_5$	<u>20</u>	<u>10</u>	<u>10</u>	⑩ $9+20=29$ R
	<u>55</u>	<u>26</u>		

$$< P_4 - P_2 + P_1 - P_3 - P_5 >$$

Available = Total - Allocation

need = demand - Allocation

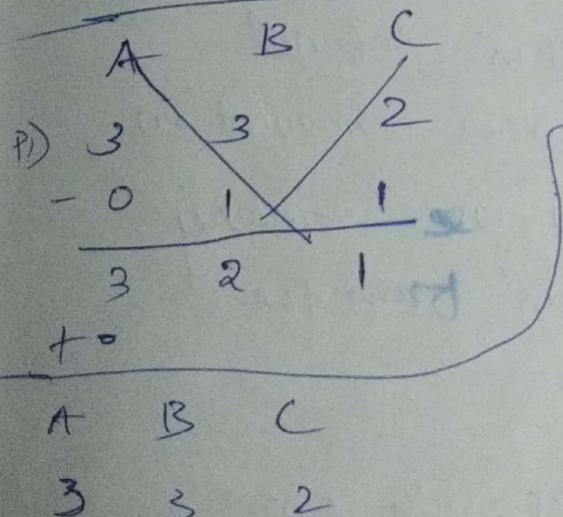
shortcut:

available = available  
+ allocation

Consider 5 process  $n=5$ ,  $m=3 \{A, B, C\} \{10, 5, 7\}$

Pid	mandemand of each type resource			current allocation	need
	A	B	C		
P0	7	5	3	0 1 0	7 4 3
P1	3	2	2	2 0 0	1 2 2
P2	9	0	2	3 0 2	6 0 0
P3	2	2	2	2 1 1	0 1 1
P4	4	3	3	8 0 0 2	4 3 3 4
				7 2 5	

Availability



$$= \begin{cases} 10 - 7 = 3 = A \\ 5 - 2 = 3 = B \\ 7 - 5 = 2 = C \end{cases}$$

P1-P3

③

shortcut  
- available

= available + allocation

+ 2 0 0 → Allocation of P1

~~6~~

5 3 2

+ 2 1 1 → Allocation of P3

~~2~~

743  
002 — allocation of P<sub>1</sub>

745  
302 — allocation of P<sub>2</sub>

1047  
510 — allocation of P<sub>3</sub>  
1057 = R (in) vestu

→ if we able to get the sequence

it is not deadlock so it is ~~not~~ safe

### Deadlock Detection and Recovery :

+ Allow the system to enter deadlock  
lock if it is enters use  
the detection algorithm to find  
processes and resources involved in  
deadlock and then use recovery  
scheme to recover from the  
deadlock state.

→ deadlock detection with single  
instances of resources apply  
"Wait for graph"

→ for multiple instances use the Banker's algorithm,

→ 'Wait for graph' is constructed from the resource allocation graph by applying transitive rule

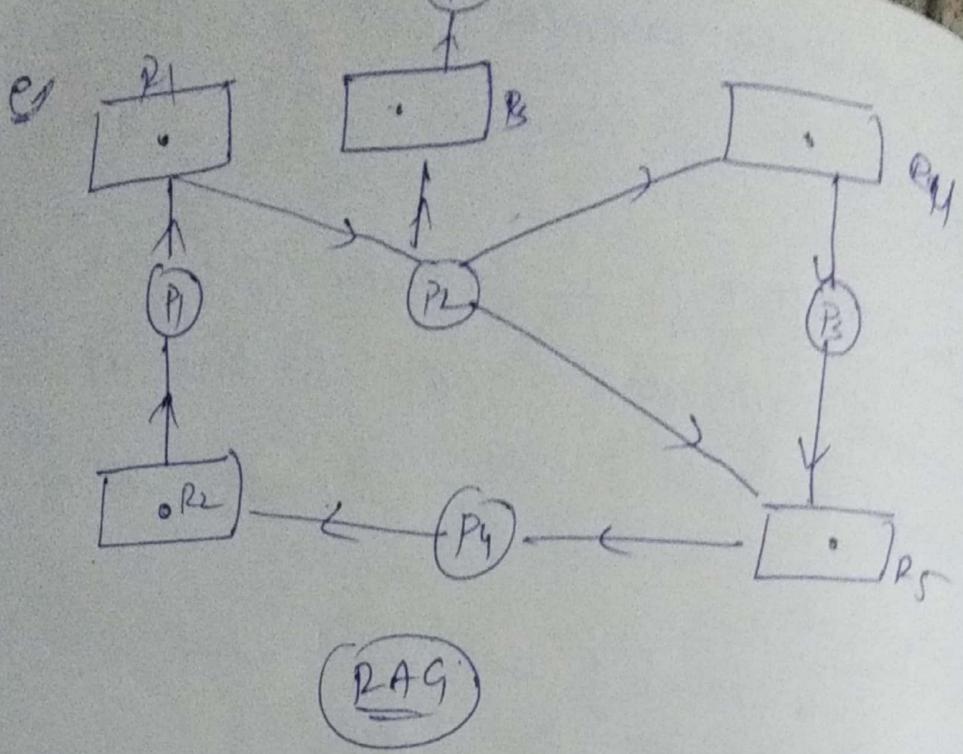
Transitive rule

$$\text{If } a \xrightarrow{r_b} b \text{ & } b \xrightarrow{r_c} c = a \xrightarrow{r_c} c$$

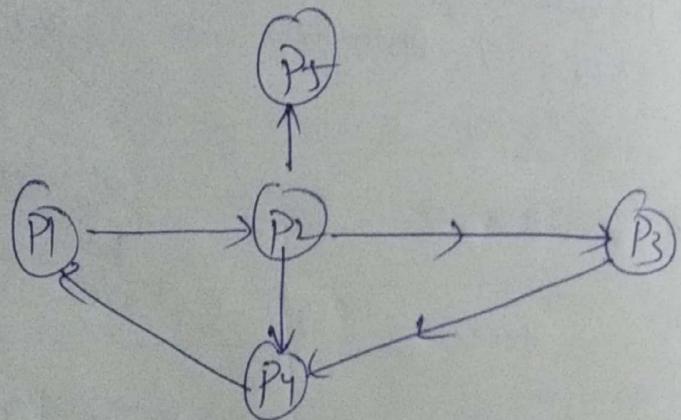
$$a^{rc} \text{ & } b^{rc} = a^{rc}$$

→ Wait for graph is a graph showing the dependencies between the processes waiting for 1-another  $\Leftrightarrow$  1 another

→ After drawing wait for graph take largest side and the processes which induced in the largest side those process only will be running in Deadlock



wait for graph



now take largest size

$$\boxed{P_1 - P_2 - P_3 - P_4 - P_1}$$

now only  $P_1 - P_2 - P_3 - P_4 - P_1$  are in

deadlock and  $P_5$  is not instead it

for multiple instances

$N=5$ ;  $(P_0, P_1 \dots P_4)$ ,  $m=3$   $(A, B, C) \rightarrow (7, 2, 6)$

PID	Allocation			Request			available
	A	B	C	A	B	C	
P <sub>0</sub>	0	1	0	0	0	0	1 A B C
P <sub>1</sub>	2	0	0	2	0	2	0 0 0
P <sub>2</sub>	3	0	3	0	0	0	3 0 3
P <sub>3</sub>	2	1	1	1	0	0	$\begin{array}{ c c c } \hline 3 & 1 & 3 \\ \hline 2 & 0 & 0 \\ \hline \hline 5 & 1 & 3 \\ \hline + & 2 & 1 & 1 \\ \hline \end{array}$
P <sub>4</sub>	0	0	2	0	0	2	$\begin{array}{ c c c } \hline 7 & 2 & 9 \\ \hline 0 & 0 & 2 \\ \hline \hline 7 & 2 & 6 \\ \hline \end{array}$
	<u>7 2 6</u>						

④  $P_2 - P_0 - P_1 - P_3 - P_4 \rightarrow$  Safe state

$$\boxed{\text{available} = \text{available} + \text{Allocation}}$$

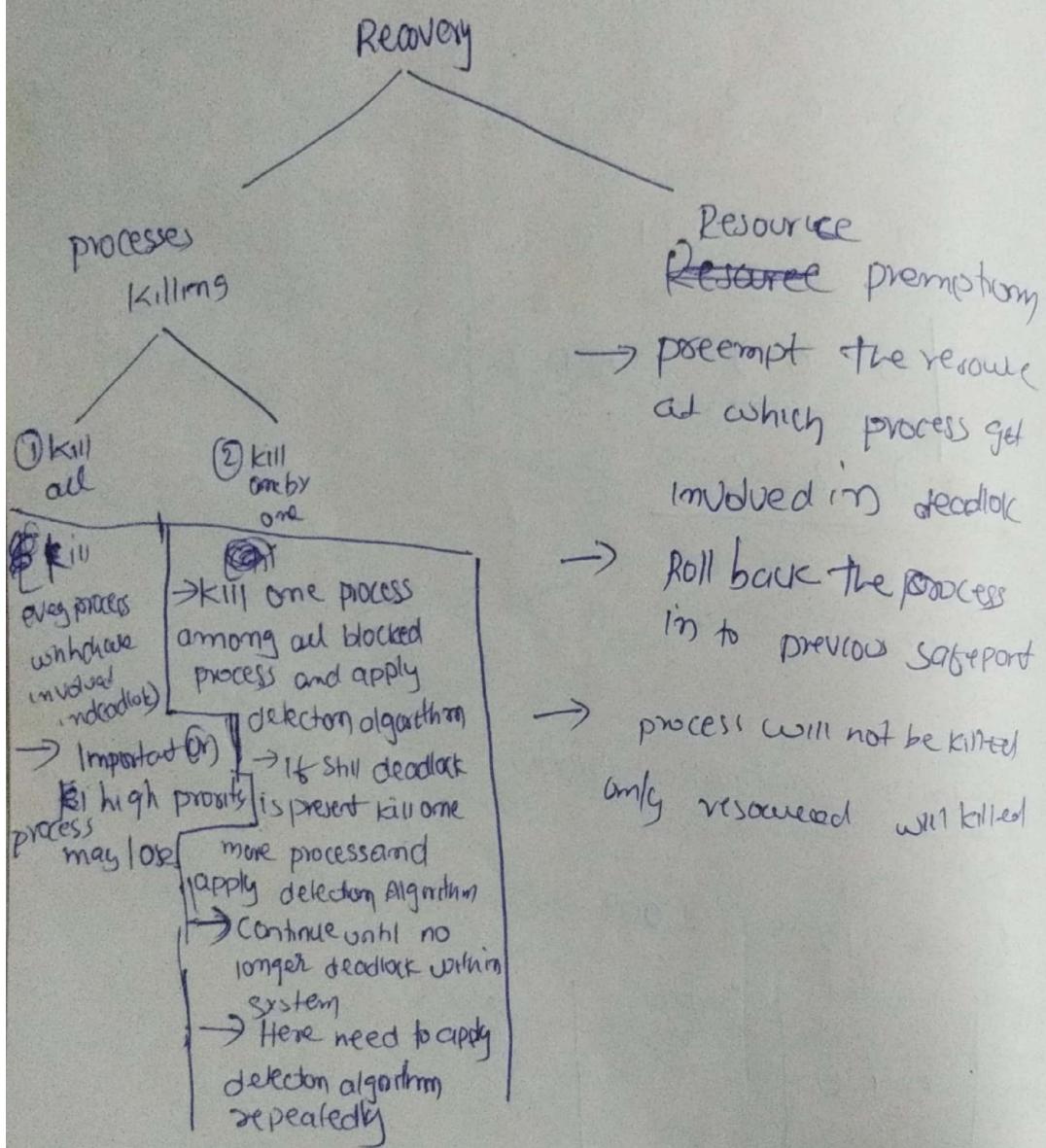
SUPD

~~t<sub>3</sub>~~  $\rightarrow P_2 \rightarrow \text{dead} \rightarrow \text{requested}$

PID	Allocation			Request			available (0 0 0)
	A	B	C	A	B	C	
P <sub>0</sub>	0	1	0	0	0	0	x
P <sub>1</sub>	2	0	0	2	0	2	
P <sub>2</sub>	3	0	3	0	0	1	
P <sub>3</sub>	2	1	1	1	0	0	
P <sub>4</sub>	0	0	2	0	0	2	

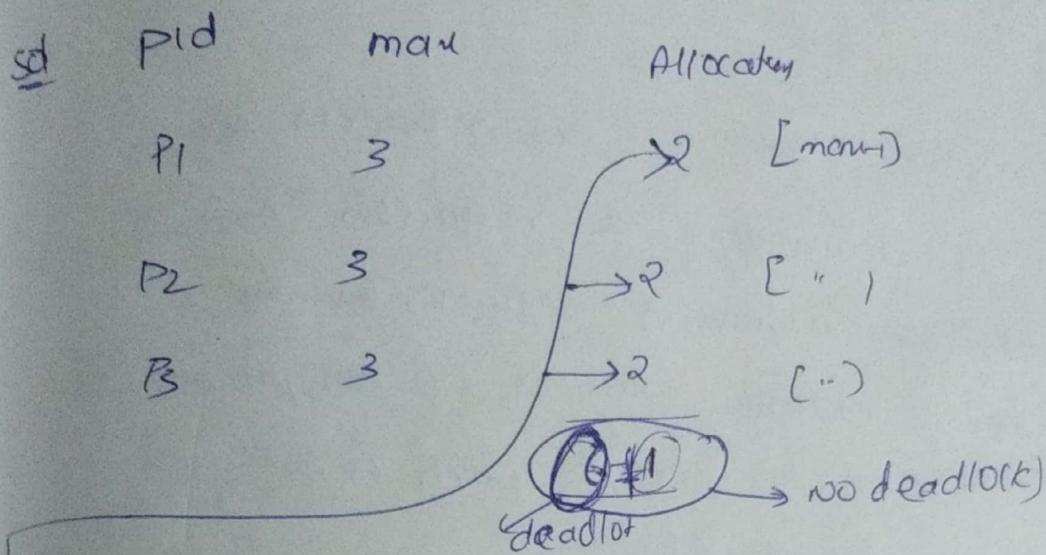
$P_1, P_2, P_3, P_4$  are in deadlock  
 $P_0$  is not in deadlock

### Recovery of deadlock:



Deadlock →

Q) Consider System with 3 processes each processes demanding minimum 3 tapes drives. what is the minimum no of resources 'R' that will not entering in to deadlock states.



→ when allocation vector is not given, allocate the Resources to the process with its

mandemand - 1) and now add 1 extra

Resource so that system will not

entering in to deadlock.

If you take

Allocation
1
2
2

Then also  
there is  
deadlock.  
so give more resource

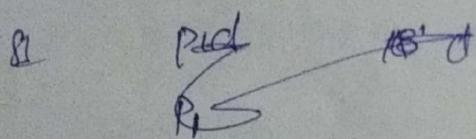
Allocation
2
2
2

→ Q1

→ The minimum no of resources Required to avoid deadlock in the system = 7

→ The maximum no of resources Required to cause the deadlock will be 6

(Q) Consider system with "n" processes each process demanding 2 resources. Assume that system having resources. Given = 6  
What is maximum number of processes can be in a system which is not leading to deadlock.



$$\text{Given} = R=6$$

$$n=?$$

Pid	max	Allocat	Left
1	2	2	$n=2$
2	2	2	

Pid	max	Allocation	Left
1	2	2	$n=3$
2	2	2	
3	2	2	

Let  $n=4$

$R=2$

pid	max	Allocation	
1	2	1	
2	2	1	
3	2	1	
4	2	1	

$4+1$       no deadlock

Let  $n=5$

$R=1$

pid	max	Allocation	
1	2	1	
2	2	1	
3	2	1	
4	2	1	
5	2	1	

$5+1$       no deadlock

for  $n=6$

→ There will be a deadlock  
Because  $R=2$   $R$  will become  $0$

~~then~~ The max no of process that can make will not lead to deadlock with 6 Resources are 5

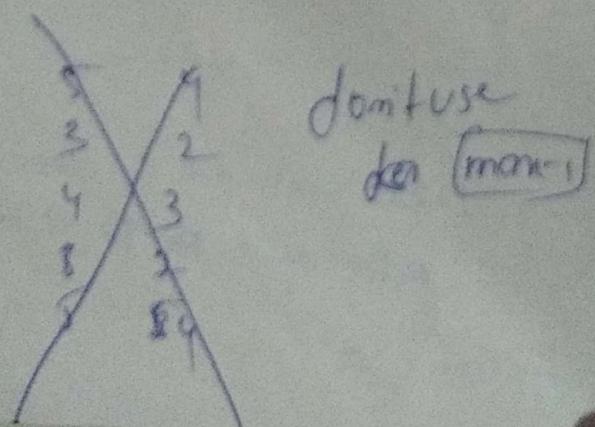
→ The minimum no of process that will ~~not~~ lead to deadlock with 6 Resources = 6

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Q) Consider 5 process, the claim vector, allocation vector has follows

pid	(Demand)	
	Claim	Allocation
1	5	3
2	3	2
3	4	2
4	8	
5	5	3

What will be minimum resource R so that system enters in to deadlock



Pid	claims	Allocation	Need	available
1	5	3	2	1
2	3	2	1	3
3	4	2	2	6
4	8	4	4	10
5	5	3	2	15

min no of enough

~~no~~ R=15^ to avoid deadlock

→ mark no of resources to go in deadlock = 14

→ Take initial value in available = min value  
in the need

### Deadlock Ignorance

~~if~~ just ignore it deadlock

comes and ~~the~~ system will crash

## Memory management :

\* It deals with main memory i.e. with RAM

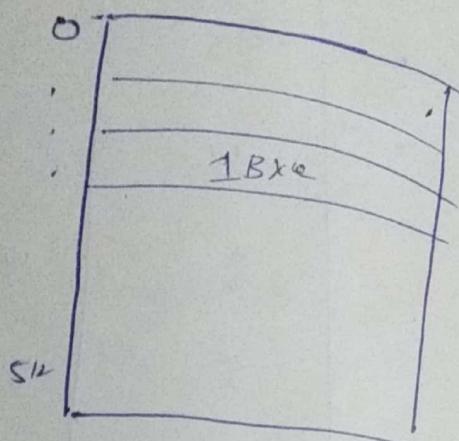
\* Ram (m) mm

is one dimensional  
large size array which  
contains set of locations,

set of words,  
set of bytes

000000000

11111111



$$\textcircled{1} \quad N = \text{no of words/bytes}$$

$$\textcircled{2} \quad m = \text{length of word}$$

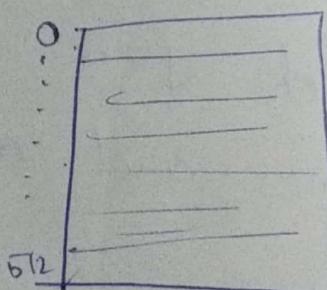
$$\textcircled{3} \quad n = \text{no of required bits required to address a word/location}$$

from above diagram

$$w = 512$$

$$m = 8 \text{ bit}$$

$$n = 9 \text{ bit}$$



\* Design Relation

$$\textcircled{1} \quad N = 2^n$$

$$\textcircled{2} \quad n = \log_2 N$$

$$\textcircled{3} \quad \text{memory size} \quad N \times m \quad (\text{Byte/1bit})$$

$$= 2^n \times m$$

$N = 128K$  words

$m = 16$  bits

$m = 16$  bits  
 $2B \times K$

0 words

words in memory =  $128K$  words

$$bytes = 128K \times 2B = 256KB$$

$$bits = 256KB \times 8 \text{ bits} = 2^8 \times 2^{10} \times 2^3 \text{ bits}$$

$2^{21}$  bits

$$\Phi 2^3 = 8$$

$$2^5 = 32$$

$$2^7 = 128$$

$$2^9 = 512$$

$$2^{10} = 1024B = 1KB \cong 10B$$

$$2^{11} = 2048B = 2KB$$

$$2^{12} = 4096B = 4KB$$

$$2^{13} = 8192B = 8KB$$

$$2^{14} = 16384B = 16KB$$

$$2^{17} = 2^7 \cdot 2^{10} = 128KB$$

$$2^{19} = 512KB$$

$$2^{20} = 2^{10} \cdot 2^{10} = 1mB \cong 10^6 B$$

$$2^{21} = 2mB$$

$$2^{23} = 8 \text{ MB}$$

$$2^{28} = 256 \text{ MB}$$

$$2^{30} = 1 \text{ GB} \approx 10 \text{ Bytes}$$

$$2^{33} = 8 \text{ GB}$$

$$2^{39} = 512 \text{ GB}$$

$$n = 27 \text{ bits}$$

$$m = 32 \text{ bits}$$

$$\textcircled{1} \text{ words } (N) = 2^n = 2^{27} \text{ words}$$

$$= 12.8 \text{ M word}$$

$$\boxed{n = 27 \text{ bits}}$$

$$\textcircled{2} \quad \text{Bytes} = 12.8 \text{ M words}$$

$$= 12.8 \text{ M} \times 8 \text{ bytes} \quad \begin{matrix} \text{Length of} \\ \text{word} = 32 \end{matrix}$$

$$\boxed{n = 29} = 512 \text{ MB}$$

$$\begin{matrix} \text{Length of} \\ \text{word} = 32 \end{matrix}$$

$$= 4 \text{ bytes}$$

$$\textcircled{3} \quad \text{bits} = 512 \text{ M} \times 8 \text{ bits}$$

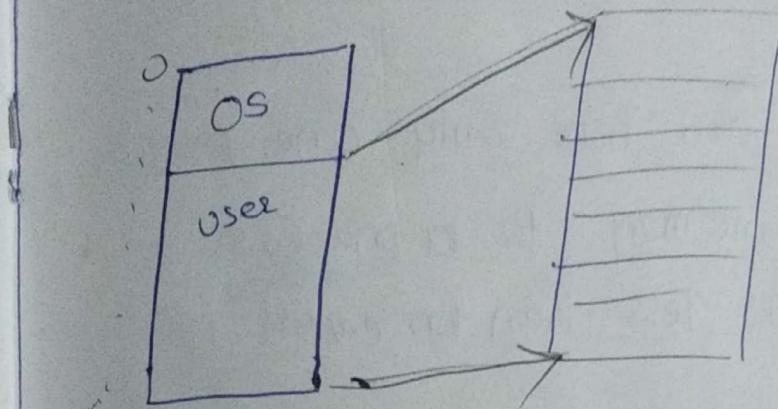
$$\approx 2^9 \cdot 2^{20} \cdot 2^3 \cdot \text{bits} = 2^{32} = \underline{\underline{49 \text{ bits}}}$$

$$\begin{matrix} n = 32 \text{ bits} \\ \text{Length of} \\ \text{word} = 32 \end{matrix}$$

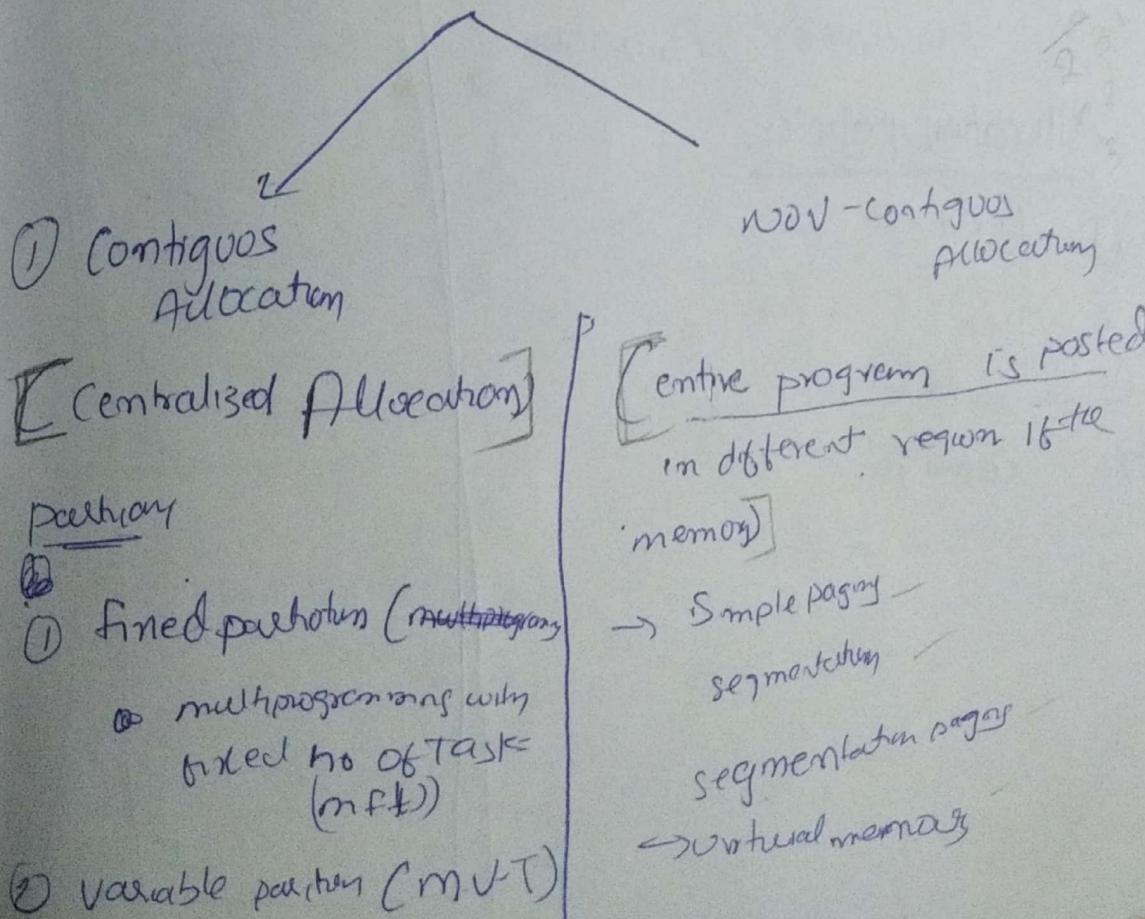
## \* Memory management techniques

\* Generally main memory divided in 2 parts

- 1) OS Resident
- 2) User space



- User area of the memory further division takes place to accommodate several processes
- These division is carried out by the operating system dynamically is known memory management



# I. Contiguous Allocation

## ① fixed Partition (M.FT)

(M.FT = Multiprogramming with fixed no of tasks)

→ MM is divided into equal (or) unequal sized partitions.

→ Each partition can hold only one program.

→ Allocate the memory ~~to~~ a process whose size is less than (or) equal to partition size.

Let consider process Request

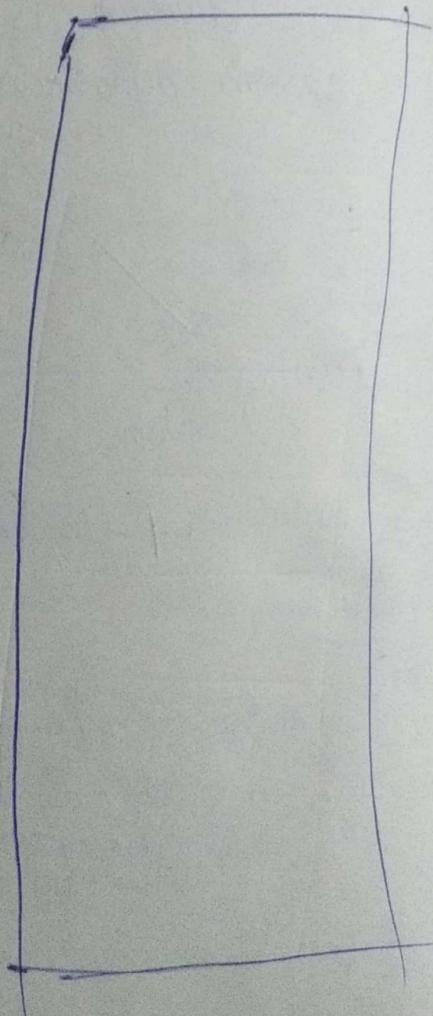
P<sub>1</sub>: 120KB, P<sub>2</sub>: 200KB

P<sub>3</sub>: 160KB, P<sub>4</sub>: 220KB

P<sub>5</sub>: 140KB / P<sub>6</sub>: 250KB

Allocation policies.

- ① first fit
- ② best fit
- ③ next fit
- ④ worst fit

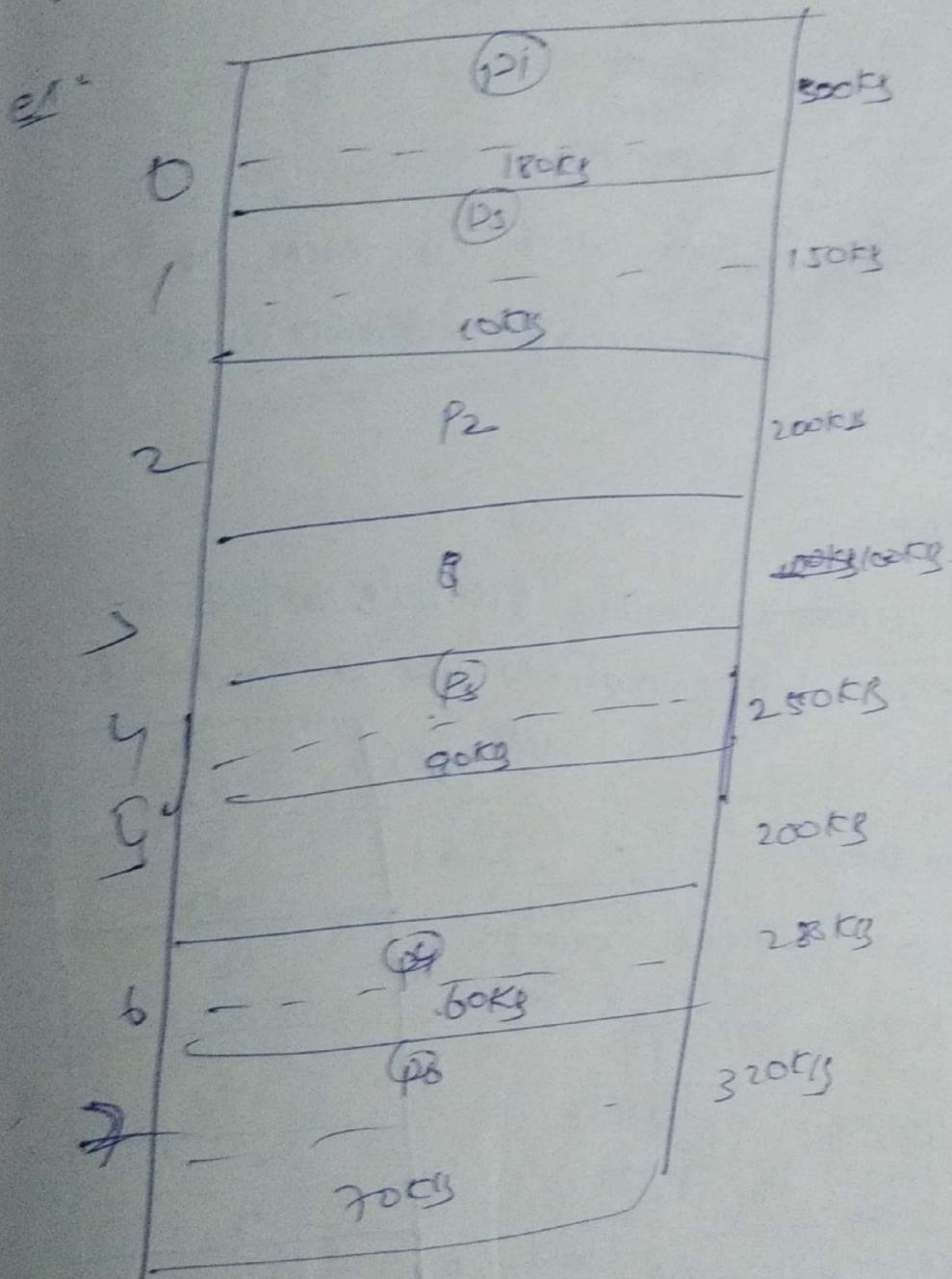


Enqueue

If allocate the partition with that free hole con free block that is big enough.

(Or)

→ If scan the memory from beginning allocate for free block that is large enough.



$$I.F.C \text{ (internal fragmentation)} = 180 - 140 = 40\%$$

$$60\text{K} + 20\text{K}$$

$$\boxed{410\text{KB}}$$

Q It percentage in memory

$$= \frac{410}{1000} \times 100$$

$$\begin{aligned} & 300 + 150 \\ & + 200 + 100 \\ & + 250 + 200 \\ & + 280 + 320 \end{aligned}$$

~~first fit~~ performs better in terms of time  
~~first fit~~ gives worst performance in terms of space

①

Bestfit:

→ It allocates smallest free hole or free block that is big enough to accommodate a process.

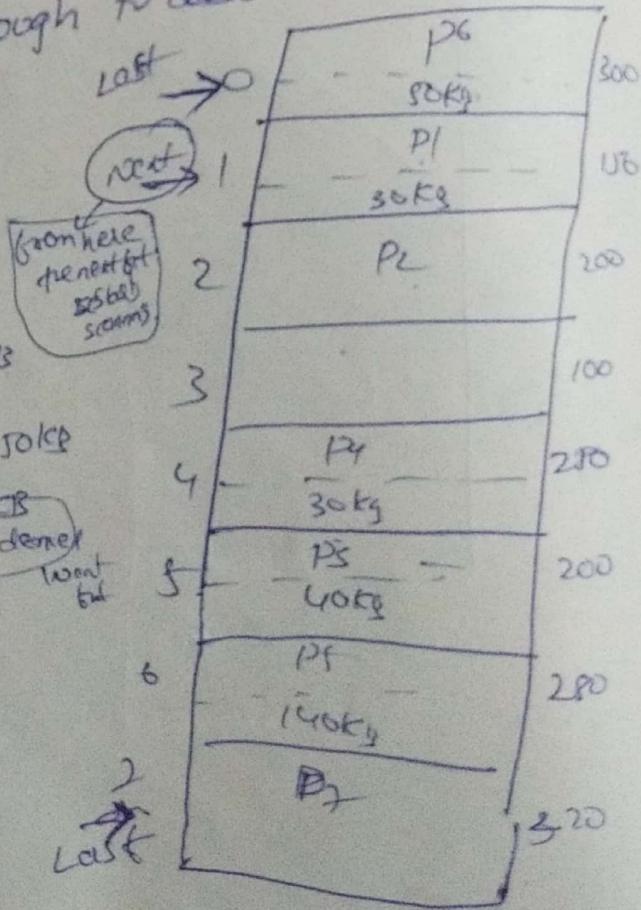
Process Details

P1: 120KB, P2: 200KB  
 P3: 160KB, P4: 220KB

P5: 140KB, P6: 250KB  
 P7: 120KB, P8: 180KB

I.F. 50K + 30K + 30K  
 + 40K + 140K

$$= 290\text{KB}$$



~~It gives better performance in terms of space~~

~~It takes more time to process~~

Next fit :-

It is same as a first fit except it scans the memory from next to last ~~pos~~ placement was made

worst fit:

~~It allocates largest position that is big enough to accommodate a process~~

P<sub>1</sub>: 120KB, P<sub>2</sub>: 200KB

P<sub>3</sub>: 160KB, P<sub>4</sub>: 220KB

P<sub>5</sub>: 140KB, P<sub>6</sub>: 150KB

$$I_6 = 100 + 60 + 30$$

$$+ 50 + 120 + 200$$

$$= 560KB$$

→ ~~worst fit will have more fit~~

	PC	
0	100KB	300 KB
1		150KB
2	60KB	200
3		100
4	36KB	250
5	56KB	200
6	120KB	280
	100 KB	320

## Performance of fixed partition

- 1) Best fit performs better in terms of space
- 2) Internal fragmentation is present
- 3) ~~No External fragmentation~~
- 4) Degree of multiprogramming is restricted by no of partitions

Degree of multiprogramming = No of  
fixed partitions

- 5) Maximum process size is proportional to maximum size partition size

~~The~~ i.e. The maximum process can be stored in, ~~whose~~ ~~process~~ whose program size is equal to largest partition in fixed ~~use~~ partition.

## Variable Partitioning :

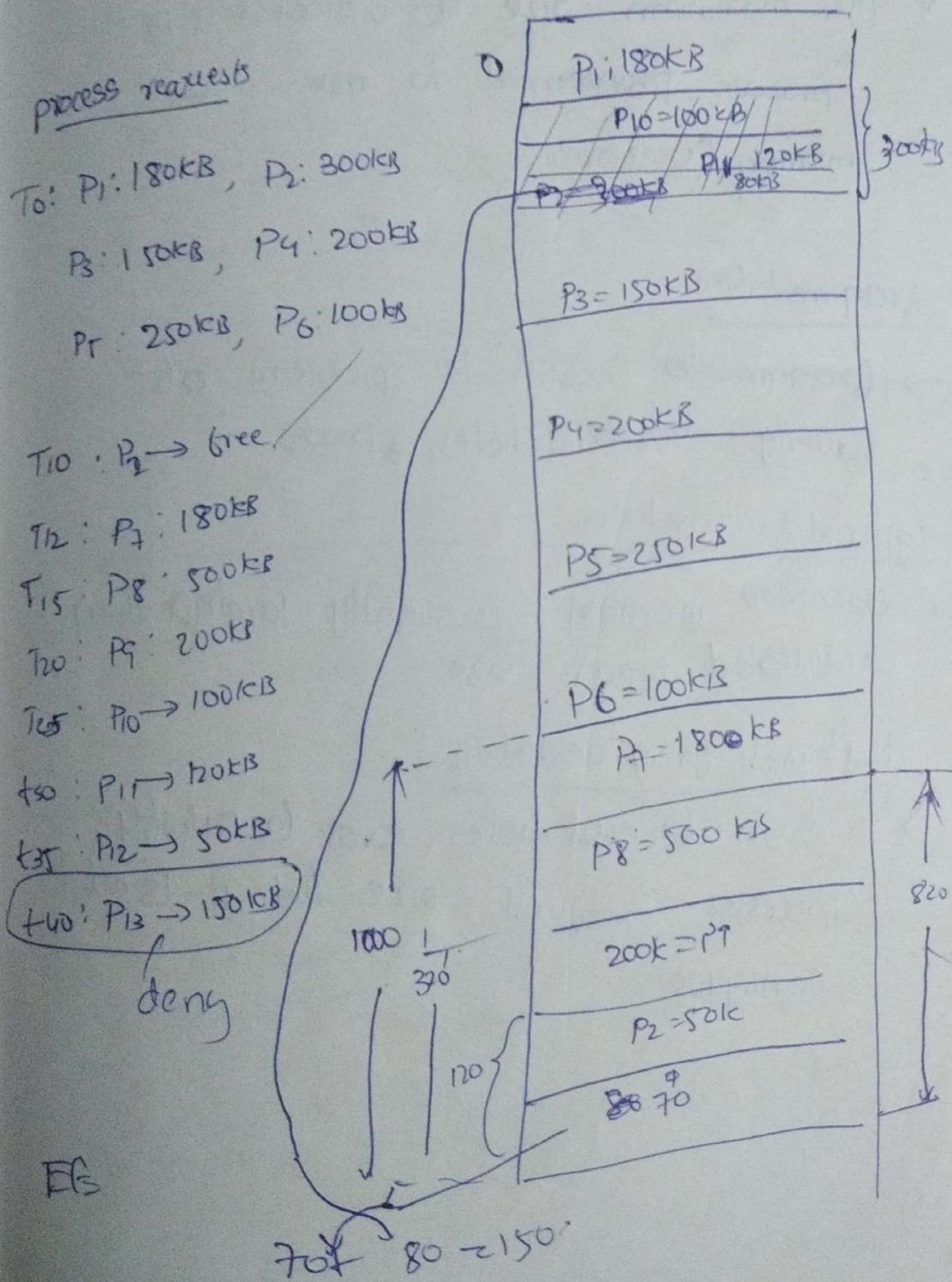
→ It is also referred as multiprogramming with variable hoof factors

→ It is also referred as dynamic contiguous allocation method

→ Here partitions are variable size  
and variable members

→ Allocate the memory exactly as  
much process is requires

→ Here ~~first fit~~ worst fit allocation  
will perform better



## Performance of variable partition

- 1) No internal fragmentation
- 2) External fragmentation is (✓)
- 3) Degree of multiprogramming  
↳ flexible
- 4) The maximum size of a process is proportional to user memory (User area)

## fragmentation

① → fragmentation refers to problem of having scattered holes (parts)

### internal fragmentation:

② → allocated memory is slightly larger than requested process size

### External fragmentation

→ sum of all holes exist to satisfy processes request size but it is not contiguous

## Solution of external fragmentation

- ① Compaction (Joining the free spaces or) by ~~PCP~~ C.P.
- ② Non-contiguous allocation (ovable compaction)

### Compaction :

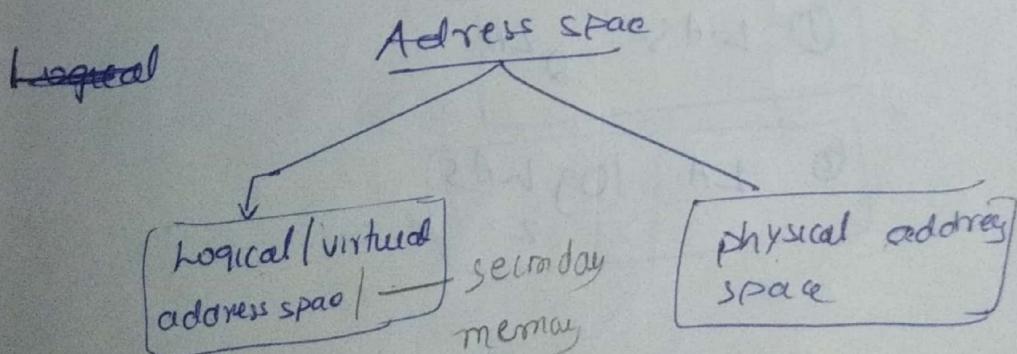
→ combining of all free holes into single big hole at the end part of memory

→ In order to implement compaction hardware support is highly needed i.e. reallocation → changing addresses dynamically.

### Non-Contiguous Allocation :-

#### Address Space :-

→ set of locations / words / set of addresses



Logical address space :- collect of / set of

Logic addresses

→ program size is nothing but logical addresses

physical address space  
and absolute address  
address in memory (MMI)

logical Address :-

- Logical address<sup>which</sup> is generated by CPU.  
→ it is a reference to a memory location,  
→ independent of current assignment of  
data to a memory location.  
→ must be translated into physical address

$nA = 10 \text{ bits}$

<0000 000000

:

<1111111>

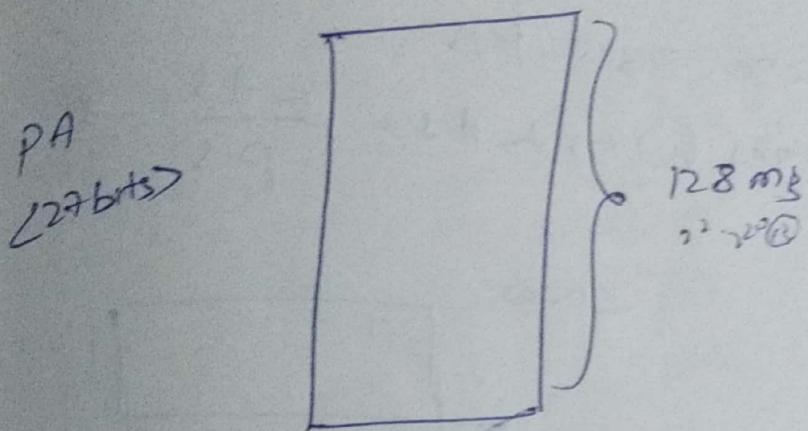
LAS  
1024b

① LAS =  $\frac{LA}{2}$

② LA =  $2^{\log_2 LAS}$

PA  
 Physical address is ~~a~~ which is seen  
 by the memory unit. It is also referred  
absolute address  $\Rightarrow$  actual locations in the  
 memory

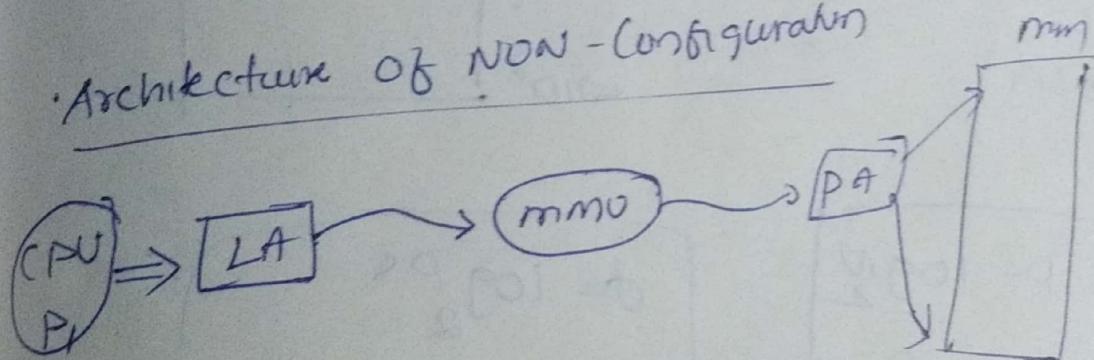
$$MM = PAS$$



$$\textcircled{1} \ PA.S = 2^{PA}$$

$$\textcircled{2} \ PA = \log_2 PAS$$

### Architecture of Non-Configurable



Simple Paging  $\hookrightarrow$  implemented by

① organisation of LAS

② " of PAS

③ " of mmu

④ Address Translation (LA to PA)

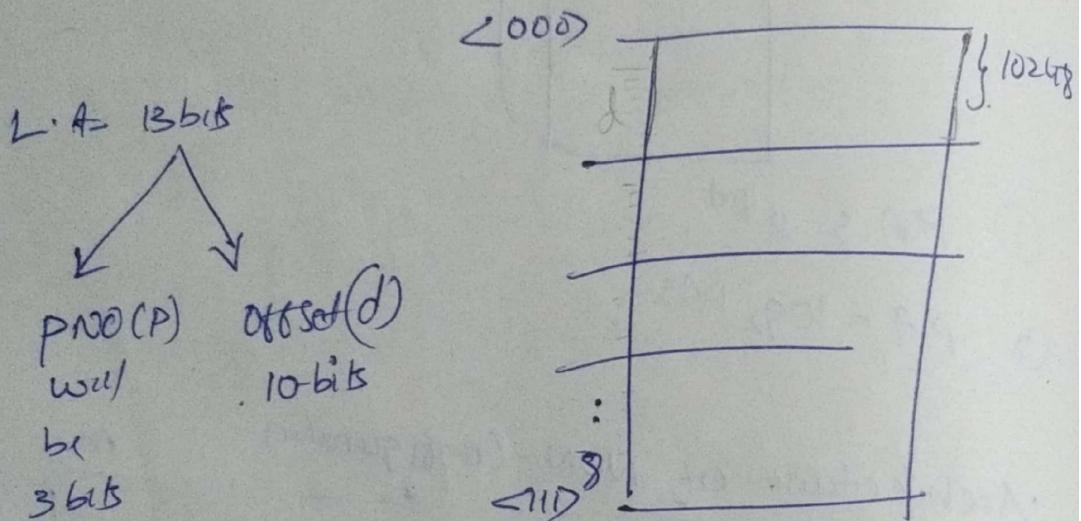
## ① Organization of L.A.S.

→ Divide the L.A.S / Virtual Address space program address space into equal sized units one called **Pages**

Net L.A.S = 8KB, L.A = 13 bits

Net page size = 1KB

$$\# \text{ of pages } (N) \text{ in L.A.S} = \frac{\text{L.A.S}}{\text{P.S}} = \frac{8\text{KB}}{1\text{KB}}$$



$$P = \log_2 N$$

$$N = 2^P$$

P = no. bits to address space  
N = no. of pages

$$d = \log_2 P.S$$

$$P.S = 2^{10} \text{ bytes}$$

$$P.S = 2^d \text{ Bytes}$$

P.S = Page size

d = no. of ~~bits~~ to address a word/Byte/Byte in a page

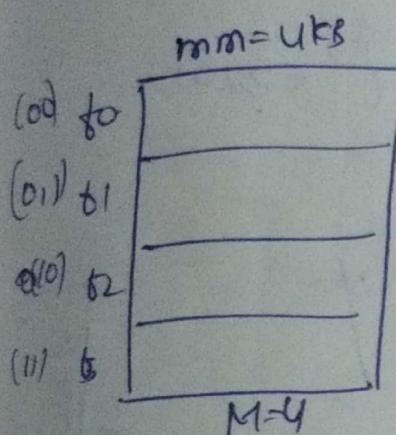
### ② Organization

→ Complete main memory is divided into equal size page frames / frames, where these size being equal to frame size.

Let P.A.S = 4KB, & Let frame size = 1KB

→ No of frames ( $M$ ) in Physical Address space

$$= \frac{P.A.S}{\text{Page size}} = \frac{4KB}{1KB} = 4$$



$$\begin{aligned} P.A &= 12 \text{ bits} = 4 \times 2^3 \\ &= 2^2 \times 2^{10} \text{ bits} \\ &= 12 \text{ bits} \end{aligned}$$

↓      ↓

frame no (f bits)      offset (d bits)

(6 bits)      (6 bits)

(2 bits)      (2 bits)

→ frame no (f bits) depend  $f = \log_2 M$

$$M = 2^f$$

→ offset (d bits) depends on  $= \log_2 P.S$

### ③ organization of memory management unit

→ organizing the page table is called 'memory management unit'

→ page table is organized into series of entries where no of entries in the page table is equal to no of entries in virtual address space

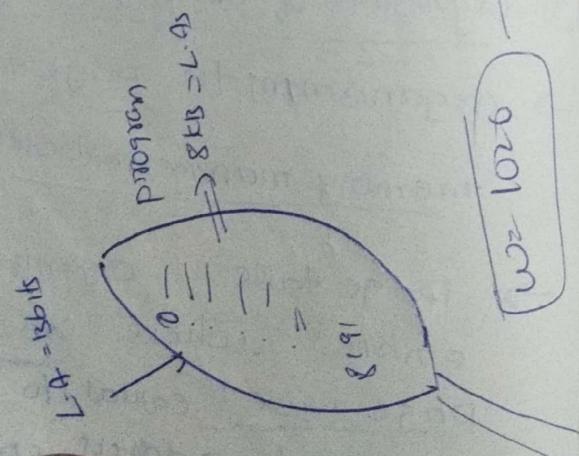
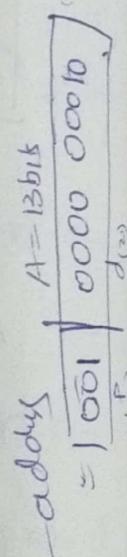
- page table entry contains essentially frame number of physical address space
- every process has its own page table
- page tables are kept in main memory (it is pure overhead) (kept in frames)
  - ↳ burden
- page table size is measured in to scores of entries multiplies by entry size
  - ↳ no of entries

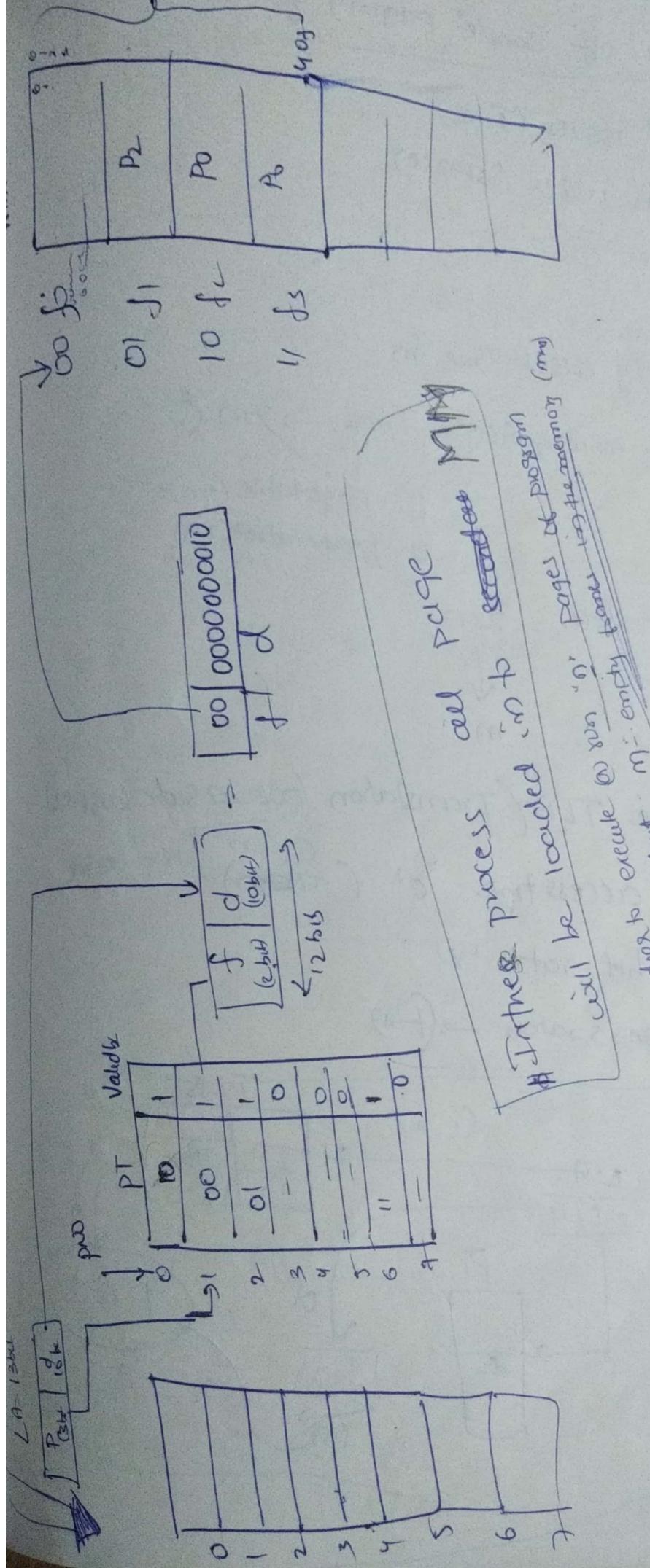
$$P.T \text{ size} = N * e \text{ Bytes} \quad [e \geq 2^8]$$

<u>N</u> = page size no of pages
<u>e</u> = no of entries

#### ④ Address translation:

- Converting from logical address to physical address





## Performance of simple paging :-

- ① temporal issues (Time)
- ② spatial issues (space)

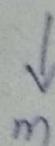
### Time

Non memory access time  $m$ :

effective memory Access Time  $\rightarrow 2m$

- ① page-table ( $m$ ) -
- ② front-toe ( $m$ ) -

To reduce  $2m$

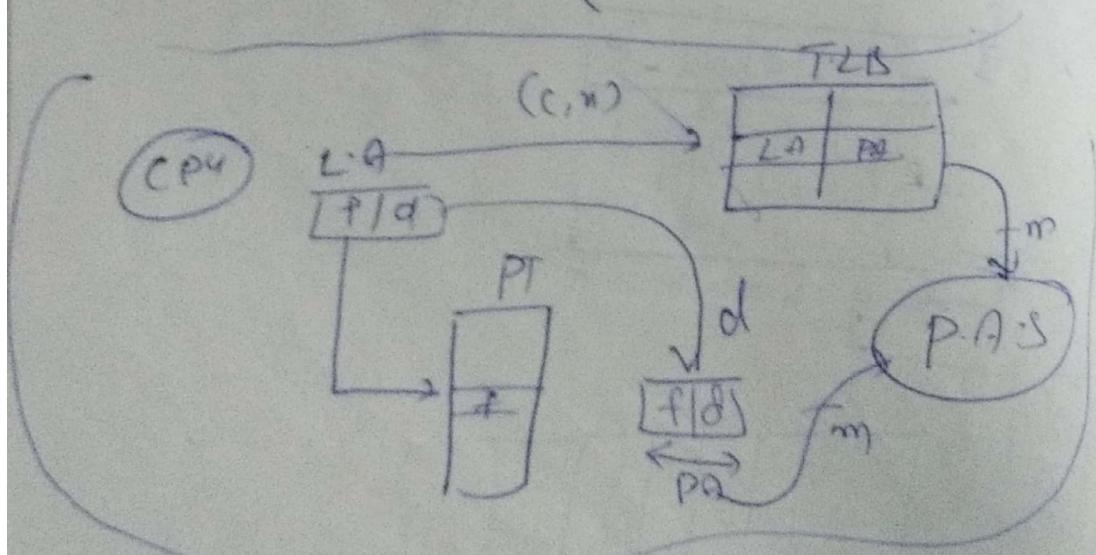


use the TLB (Translation look aside buffer)

$\rightarrow$  TLB access time ' $c$ ' (~~com~~ <sup>Cdes</sup>) very less

$\rightarrow$  TLB hit ratio ' $x$ '

$\rightarrow$  TLB miss ration  $\rightarrow (1-x)$



Example  
Block access with TLB with small pages -

A by accessing TLB

$$26.8 \text{ ms} + (1-1) \left( C + 2m \right)$$

↓  
miss rate

for page fault

if  $m = 100\text{ns}$

~~C = 100 ns~~

$m = 90\%$

$$\text{Time} = 90\% (10 + 100) + 10\% (C + 2m)$$

$$= 99 \text{ ns} + 200 \text{ ns} - [120 \text{ ns}]$$

Simple Paging without TLB used then the

Effective access time would be



number  
offset

Consider logical address 22 bit, physical address 18 bit, page size 2KB, page table entry

= 2 bits, what is the logical address space, physical address space, capital(N), M, f (frame number)

p (page number), d and page table size?

Note: page table entry(f) =  $2^b \times R$

frame	object/present	protection
		bit

A) Logical Address

$$= \frac{2^{18} B}{2^{10} B} = 2^{22} B$$

(~~4096~~)

256 kB

B) physical Address ~~of~~ space

$$= 2^{18} B$$

256 kB

c) N (No of pages) =

~~no of~~ Logical  
address space  
page size

$$= \frac{128 \text{ kB}}{2 \text{ kB}} = \frac{128 \text{ kB}}{2 \text{ KB}}$$

$$= \frac{2^{22} B}{2^{11} B}$$

2<sup>11</sup>

2 KB pages

d) M (No of frames) =

$$\frac{\text{PAS}}{\text{framesize}} = \frac{128}{2 \text{ KB}}$$

= 128

Here framesize = pagesize

A) Logical Address

$$= \frac{2^{18} B}{2^{10} B} = 2^{22} B \\ = 4 MB$$

(~~256KB~~)

256KB

B) physical Address ~~Space~~

$$= 2^{18} B \\ = 256 KB$$

c) N (No of pages) =  $\frac{\text{no of logical address space}}{\text{page size}}$

$$= \frac{128}{2 KB} = \frac{64}{1 KB}$$

$$= \frac{128}{2 KB} = \frac{2^2 \times 2^{10} \times 2^{10} B}{2 KB}$$

$$= \frac{2^{22} B}{2^{11} B}$$

= 2<sup>11</sup>

= 2<sup>11</sup> pages

d) M (No of frames) =

$$\frac{PAS}{\text{framesize}} = \frac{256 KB}{2 KB}$$

$$= 128$$

Here framesize = pagesize

$$f(b) = \log_2 M = \log_2 128 = 7$$

number of bits required  
to address 128 numbers (or)  
 $128 = 2^7 \rightarrow 7$

7 bits are reallocated to address size

$P_{bit} \log_2 N = 11 \text{ bits}$

$d_{bit} = \log_2 P_S = \log_2 2KB = \log_2 2^11 = 11 \text{ bits}$

Page Table Size = ~~No of entries~~  $\times$  ~~No of pages~~  
 $= 2^{11} \times 2^11$  (given)  
 $= 4KB$

$$\frac{512}{2^{11}} = \frac{3}{2^{11}}$$

Consider system with 512 frames, logical address = 22 bits, page size 4KB, find out logical address space PAS.

1 frame = size 4KB

$$L_{AS} = 2^{22} \text{ 4MB}$$

$$PAS = 2^{22}$$

$$M = 512$$

$$N = \frac{8^9}{4KB} = \frac{4MB}{4KB} = 112$$

$$= 112$$

$$L_{AS} = 2^{22} = 4MB$$

PAS:

$$M = 2^f$$

$$= 512 = 2^9$$

$$2^9 = 2^f$$

$$[f=9]$$

$$PAS = 2^9 = 512B$$

[f = no of bits]

[M = no of frame]

(address).  $\log_2$

$$P = 10$$

$$P = M = \frac{2^{22}}{4KB}$$

$$\frac{2^{22}}{2}$$

~~size of pages~~

(D) P.A [f/d]

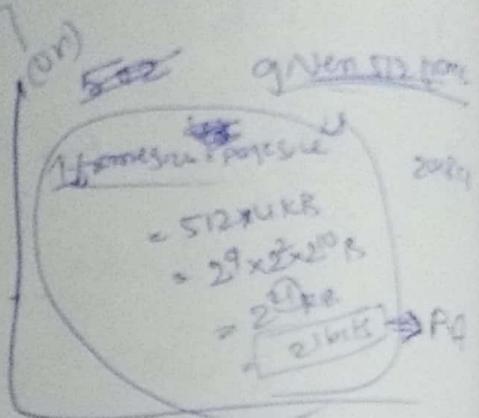
$$f = \log_2 M = \log_2 512 = 9 \text{ bits}$$

$$d = \log_2 P.S = \log_2 4KB = 12 \text{ bits}$$

M → total no. of frames

(E) P.A - f/d  
- (9+12) bits  
= 21 bits

(F) P.A\_3 = 2^21 = 2MB



(G) N =  $\frac{UMB}{4KB} = 1K \times L$

(H) P =  $\log_2 N = \log_2 k = 10 \text{ bits}$

(I) page Table size =  $N \times 2B$   
=  $1K \times 2B$   
=  $2KB$

e ~ ~~size of frame~~ + other info  
(Valid bit, protection bit,

dirty, ref bit)

$e = f + other$   
 $e = 9 \text{ bits} \leq 2B$

## (2) spatial issues (space)

let  $\text{L.A} = 32\text{bit}$ ,  $\text{L.A.S} = 4\text{GB}$   
page size =  $4\text{KB}$

$$\text{# of pages } N = \frac{4\text{GB}}{4\text{KB}} = 1\text{M} \quad 2\text{ (or)}$$

let  $C = 2B$

$$\begin{aligned}\text{page-table size} &= N \times C \\ &= 1\text{M} \times 2B \\ &= 2\text{MB}\end{aligned}$$

When you

\* Increase the page size that will reduce pagetable size

\* But internal fragmentation will be increases

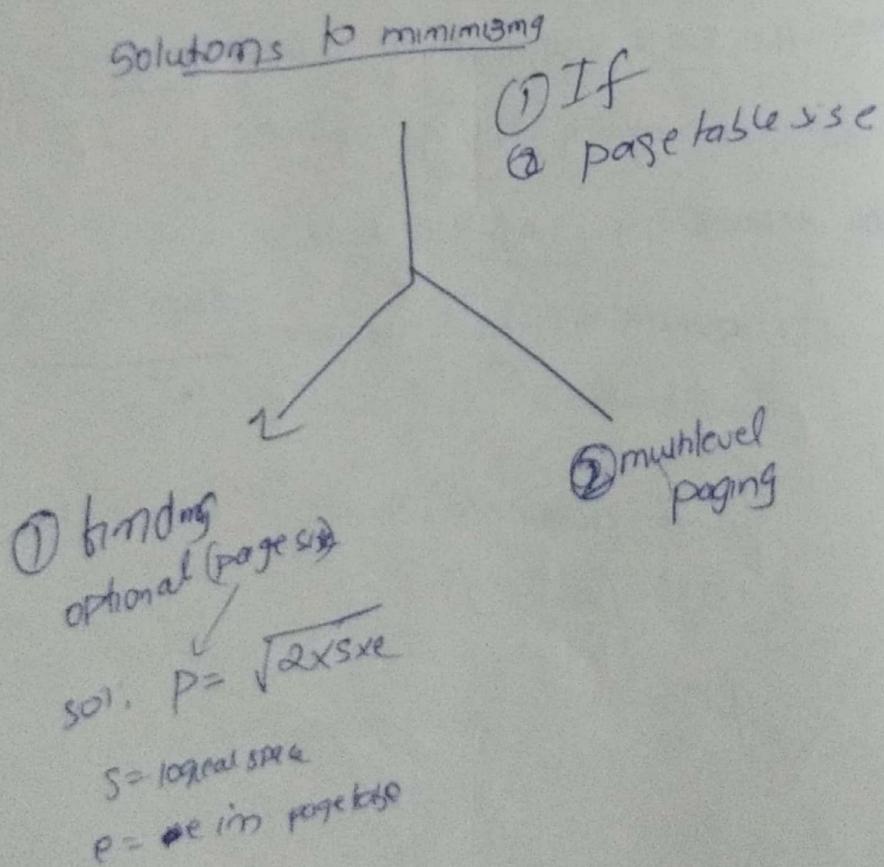
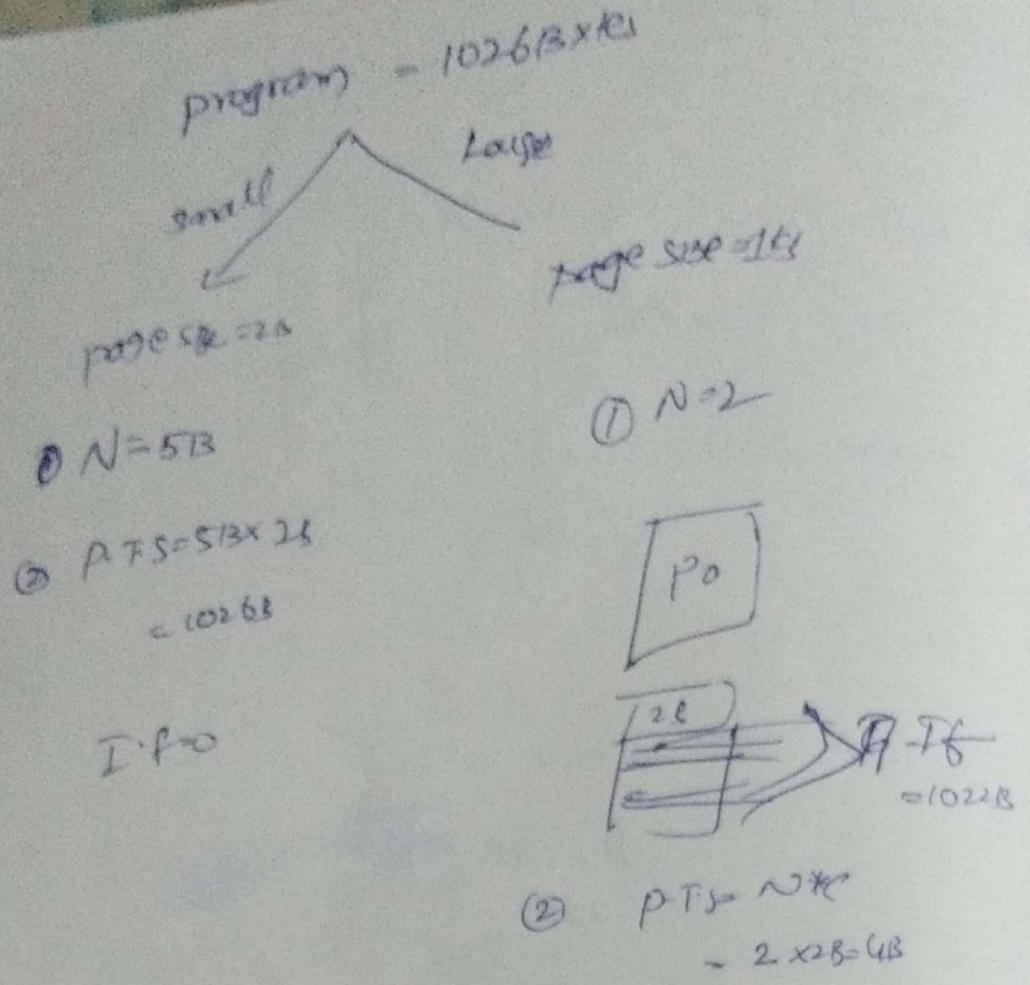
\* When you decrease the pagesize it will reduce

internal fragmentation but increase pagetable

increase —

~~Note~~ = internal fragmentation will be only  
in the last page

4



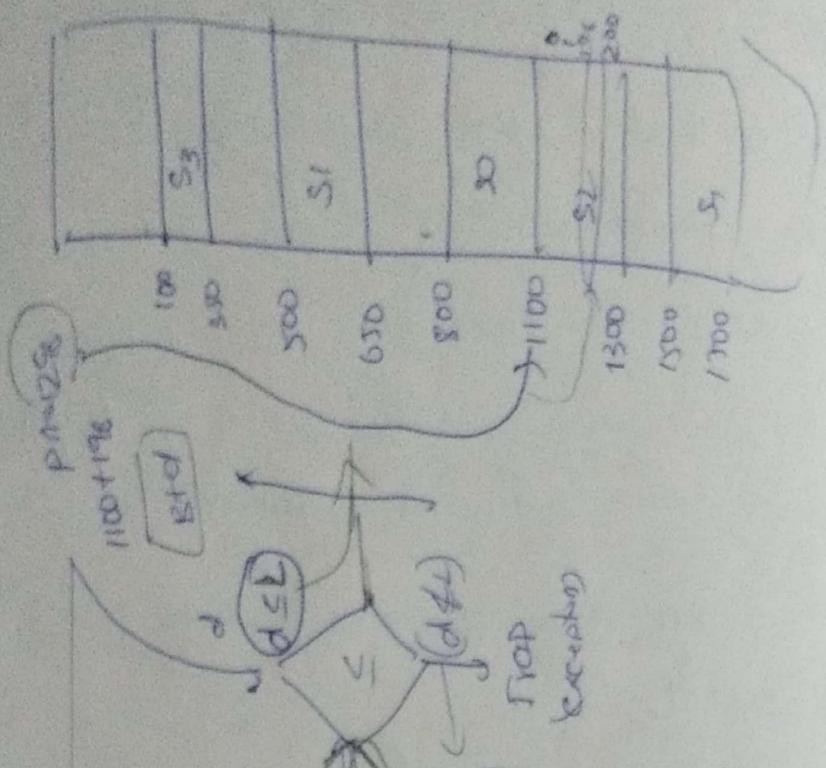
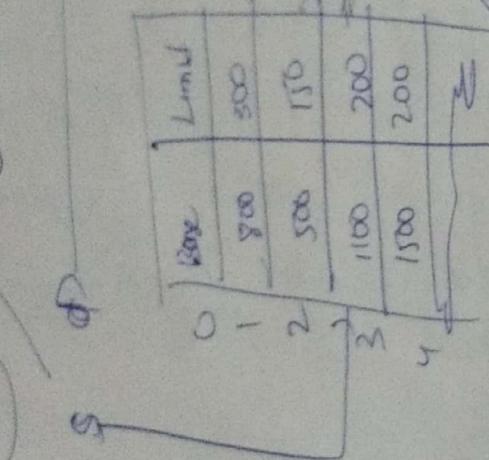
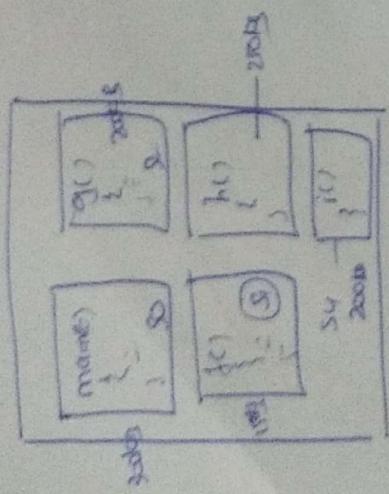
## SEGMENTATION

Logical address space is divided into Logical  
~~chunks~~ chunks Representing function,  
procedure, method, routine and datastructure are  
known as segments.

- Each segment may be variable size.
- Memory References are translated into physical Address space through segment table.
- Memory Reference contains segment number and offset
- Segmentation will handle
  - (1) Growing data structure
  - (2) Segmentation supports Reusability
- Segments of Logical address space can be independently Re-compiled and Re-linked

# SS segmentation

CPU → IA ① <2, 1968



② <3, 256 → X  
⑤ <0, 2967 ✓

Diff segments size are function size because all functions divided into the segments

### Performance of Segmentation:

#### (1) Temporal issues:

$$mn \rightarrow m$$

Effective memory access time  $\rightarrow 2m$

- (1) ~~Segment~~ Segment Table
- (2) ~~Index~~ offset

To reduce  $2m \rightarrow m$ .

\* TLB can be used to reduce memory access time  $2m \rightarrow m$

#### (2) Special issues

- (1) No internal fragmentation
- (2) External fragmentation

### Virtual memory:

\* Virtual memory gives an illusion to the programmer that a huge amount of memory is available greater than ~~more~~ available physical memory.

→ Virtual memory concept is implemented

by "Demand Paging"

→ mapping of logical address space to secondary storage device like disk and loading pages of process in to memory on demand basis is known as demand "Paging".

→ In Demand Paging all pages of process need not be loaded in to memory at a time (or) during execution. The disk load those pages which are required to compute immediately.

→ Demand paging needs I/O operation

→ It allows more processes can user to run  
(Degree of multiprogramming increases)

→ It improves CPU utilization and throughput.

→ Demand paging ~~uses~~ Lazy Swapper  
(Lazy pager)

→ Demand paging can be  
① pure demand paging  
② pre-fetched ,

pure demand:

→ no pages of a process are loaded into memory i.e start the program execution with empty frames

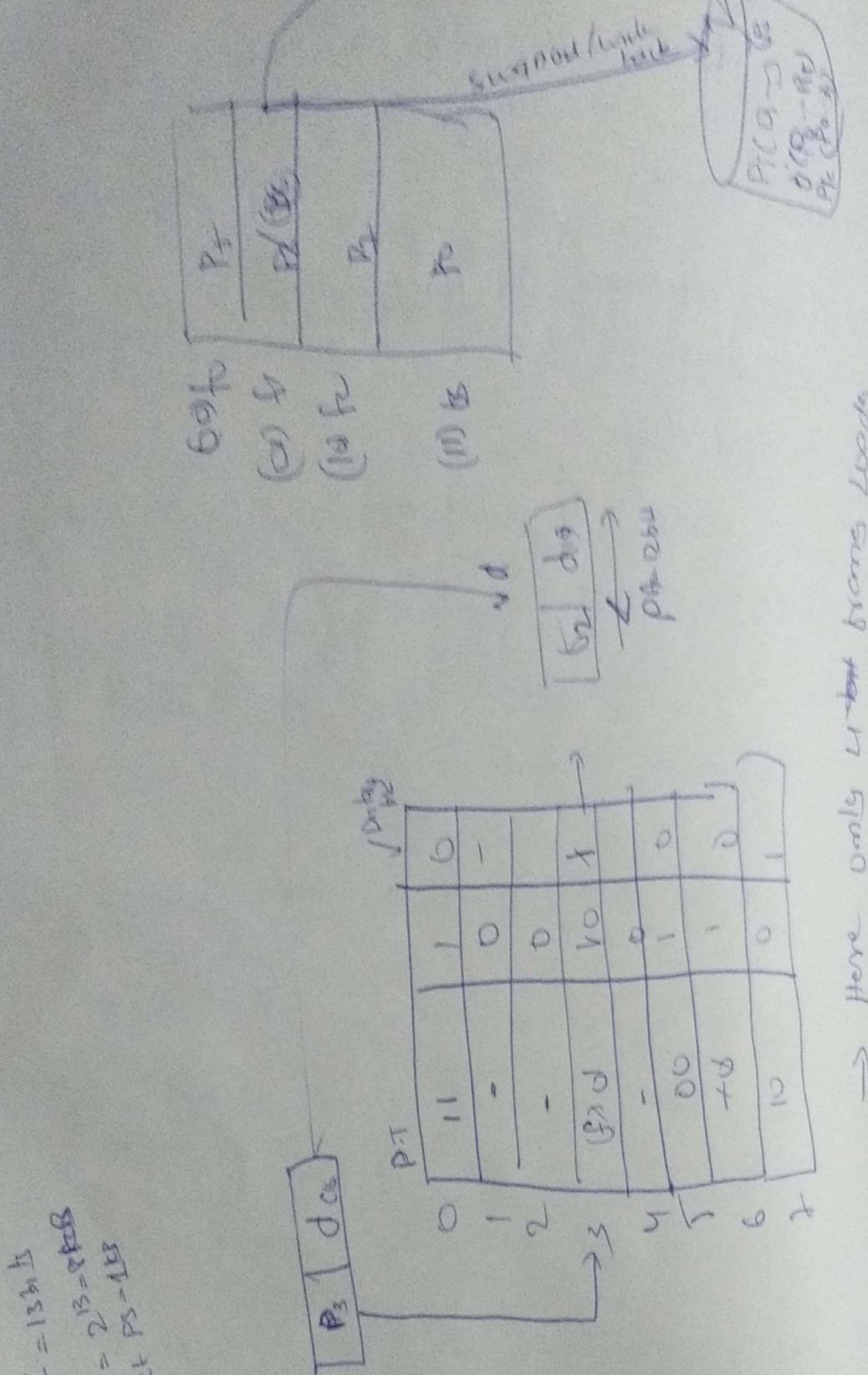
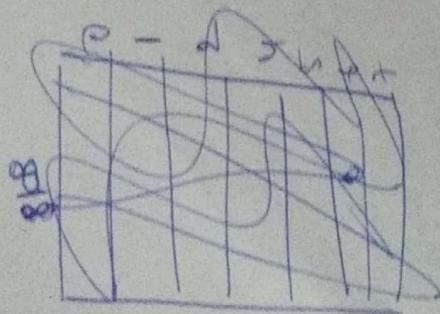
→ first reference is pagefault for 1st reference

pagefault

pre-fetched demand

4 some pages of a process loaded into memory  
Before Runtime

$$\begin{aligned} L.A.S &= 133.5 \\ L.A.S &= 2^{13} - 133 \\ \text{Let } P_3 &= 133 \end{aligned}$$



The difference here is that the only required page will be kept in memory where in simple pages all to page size will be loaded in to memory.

### Performance of Virtual memory

Let  $m \rightarrow m'$

$P \rightarrow$  page fault rate.

$(1-P)$  hit rate

$S \rightarrow$  ~~PFST~~ postfault service

$$\text{Emat} = \frac{(1-P) \times m + P \times S}{m}$$

### Page Replacement Algorithms

→ It occurs when there is no free frame in mm to bring requested page

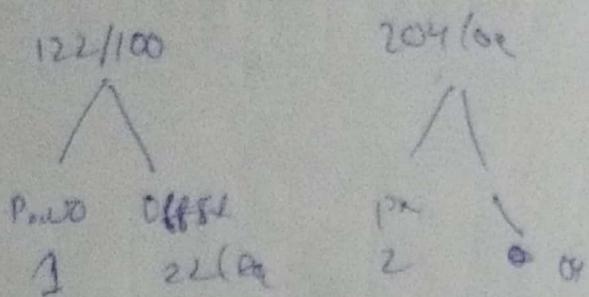
→ The page replacement algorithm minimizes the no of page faults

### Reference String

Set of successively used pages that are referred in the given list of logical address space

Ref. String: { 122, 204, 039, ~~56~~, 274, 396,  
457, 124, 094, 512 }

page size = 100 words



{ 1, 2, 0, 5, 2, 3, 4, 1, 0, 5 }  
or { 1, 2, 0, 4, 5, }

Algorithm:

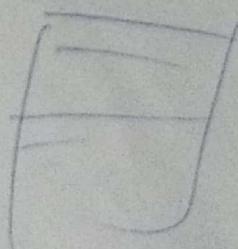
FIFO

Criteria:

It chooses the page replacement based on the arrival time of page

Consider 3 free frames initially

(3)



~~Off. Stamps~~ { } 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1

list { } 20

Unique { } 0, 1, 2, 3, 4, 7

= 6 - total size  
pages

Note if  $n$  pages ~~trans~~ for  $n$  frames  
 $n$  pagefault will occur

- if  $n$  pages for  $n >$  frames ( $n-1$  max)  
more than  $n$  pagefault will occur

e.g. 6 pages (above) if 6 frames free  
6 pagefaults will occur

→ But allocated only 3 frames so the  
pagefaults will more than 6

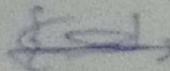
4 frames							
	0	3	0	4	2	3	0
1	2	2	2	2	2	1	2
1	1	1	1	1	1	1	0
0	0	0	0	4	4	4	4
7	7	7	7	3	3	3	3
*	*	*	*	*	*	*	*
*	*	*	*	*	*	*	*

1	2	0	1	7	0	1	
1	1	1	1	1	1	1	
0	0	0	0	0	0	0	
4	4	4	4	7	7	7	
5	2	2	2	2	2	2	
*	*	*	*	*	*	*	
*	*	*	*	*	*	*	

for strong

7 01 203 04 2  
21 20 17 01 303

2	0	3	0	4	2	3	0	3	0	4	2
1	1	1	1	0	0	0	3	3	3	3	3
0	0	0	0	3	3	3	2	2	2	2	3
2	+	X	1	2	2	4	4	4	0	0	4
0	3	9	6	3	1	2	1	0	1	*	*
3	3	2	2	2	1	1	1	1	1	*	*
0	0	0	0	0	0	0	0	0	0	*	*
4	4	4	4	3	4	2	2	2	2	*	*



b160 and b bits based algorithm suffers from the problem of Belady's anomaly  
(162,3,4,1,3,5,12,3,4)H

Belady's anomaly

- with increase in no of frames to a process  
the page fault rate logically should decrease  
but for few reference string contain  
increase in no of frames to a  
~~process~~ process. The page fault rate will also  
increase is called Belady's anomaly

### optimal replacement

- \* DR chooses the page for replacement which  
is not required longest period of time in the  
future

\* { 7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,  
1,7,0 }  
# # # # # # # # # # # # # # # # # #

Q3f

0	7	2	7
1	0	4	0
2	1	3	1

- 1) no of PF = 9  
2) No of hits = 11  
3) Hit Ratio =  $\frac{11}{20} \times 100$   
4) Status: { 7,0,1 }

\* If is not suitable to implement practical cases since predicting the future reference string is difficult

\* It is a bench mark tool ( ) which is used to compare all Algorithms with their optimality.

LRU (Least Recently Used)

→ If chooses the page for replacement based on usage

{ 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 17  
 . . . . . . . . . . . . . . . . . .  
 H H H H H H H H H H H H H H H H H H

X	2 4 X 1
0 0	3 0
1	8 X +

① no of hits = 8 —

② no of faults = 12 —

DISK

## Scheduling Algorithms :-

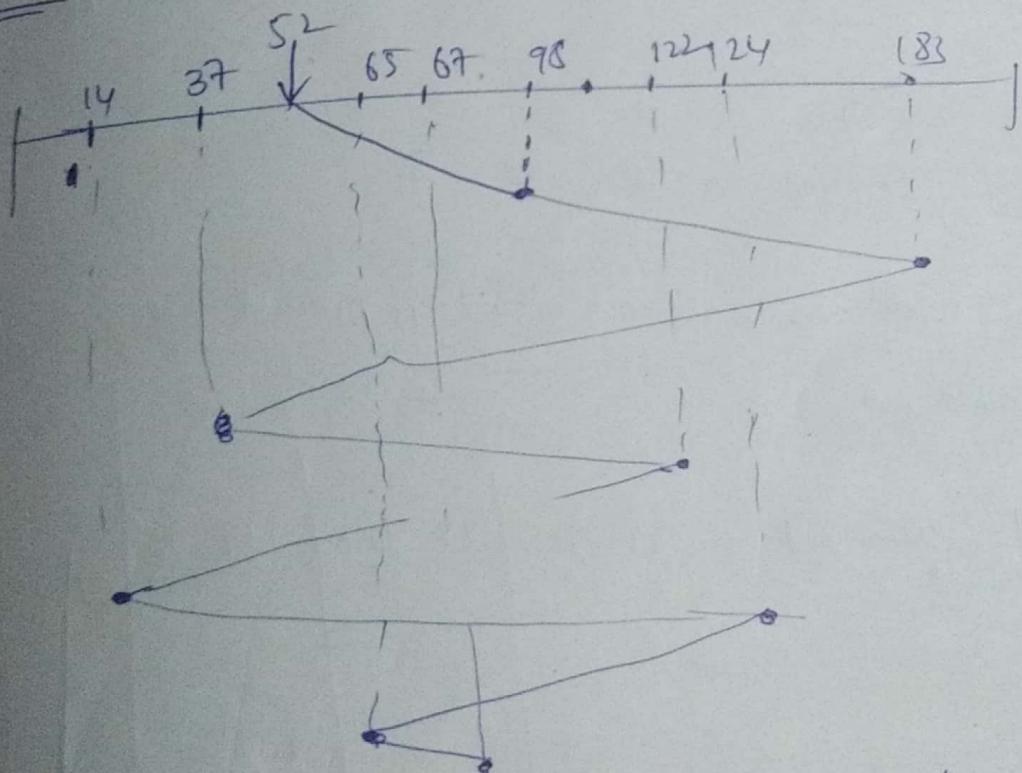
when more than one request comes to the disk we need to apply some algorithms to minimize no of seeks

Let us consider Disk has 200 cylinder which are numbered from (0 to 199). And disk requests are

98, 183, 37, 122, 14, 124, 65, 67

Current header position at cylinder no 52

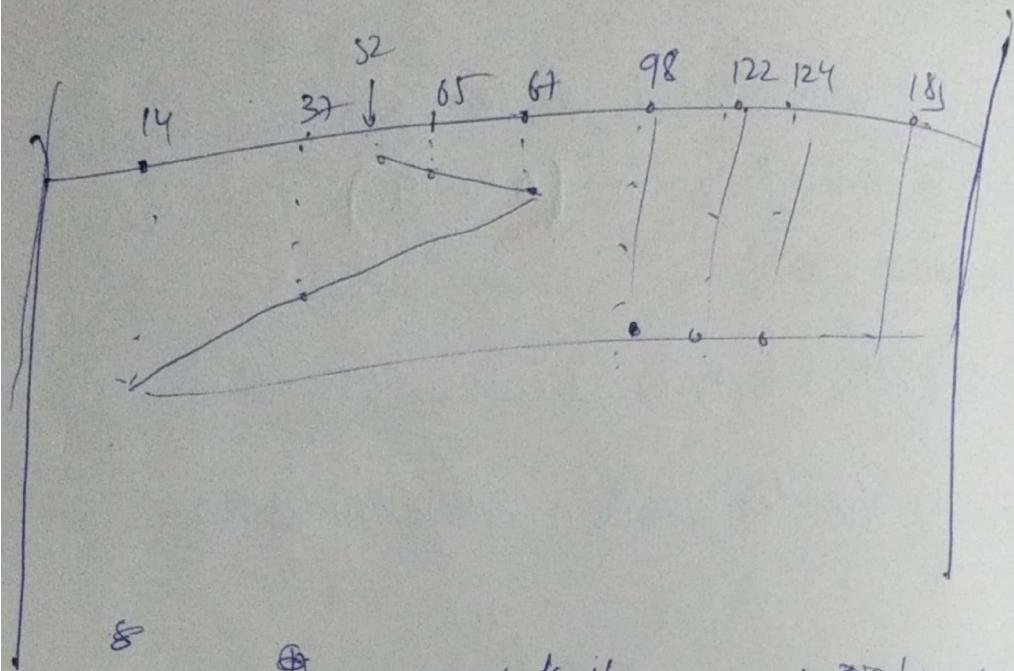
FCFS



$$\begin{aligned}
 \text{Seeks} = & |52 - 183| + |183 - 37| + |37 - 65| \\
 & + |65 - 67| + |67 - 98| \\
 & + |98 - 122| + |122 - 124| \\
 & + |124 - 65| + |65 - 67| \\
 = & 131 + 146 +
 \end{aligned}$$

SSTF (shortest seek Time first)

98, 183, 37, 65, 14, 124, 65, 67

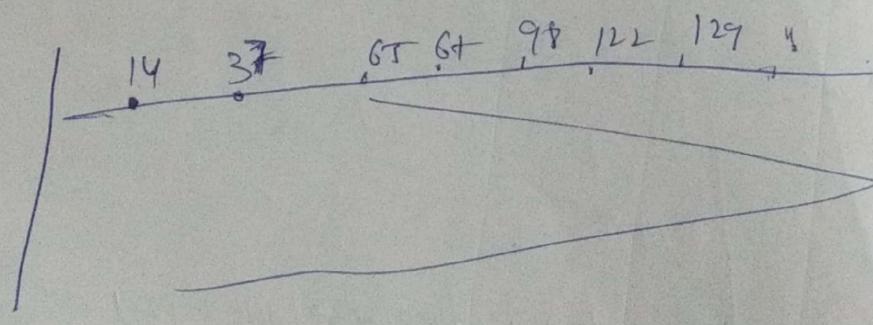


It serves nearest to it  
+ Not implementable

= 237

SCAN Considered as elevator

- Useful when heavy load is present
- gives ~~goes~~ goes



→ example: how to know whether to go

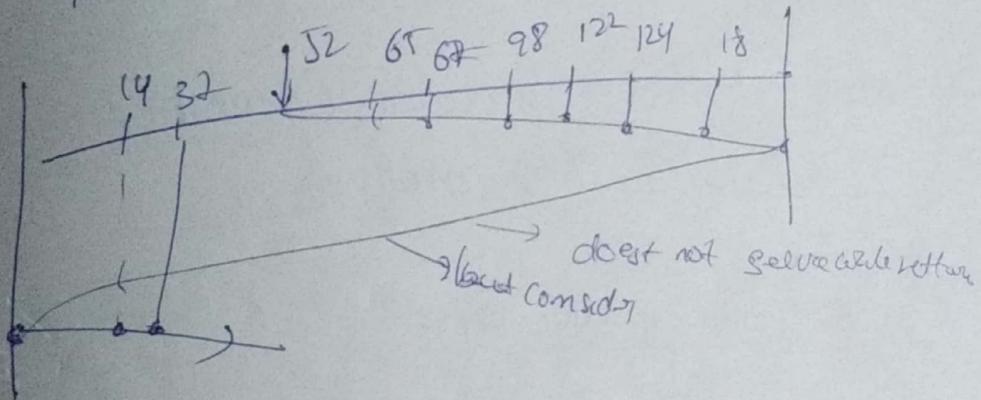
left or right side

Look  
does not go to complete end. ~~is~~ remaining  
will work as SCAN

Look is more than better than SCAN  
→ It ~~also~~ also useful for heavy loaded system

C-SCAN (Circular SCAN)

C-SCAN does not service while returning but  
touches the ends



$$(52-199) + (197-01) + (383-0-32) \\ = 383$$

$$\begin{array}{r} 199 \\ 183 \\ \hline 16 \end{array}$$

C-Look:  
It will not go to end

## file allocation methods / Disk space Allocation

1st disk size = 64MB

Disk block size = 1KB

Disk block address = 16-bit

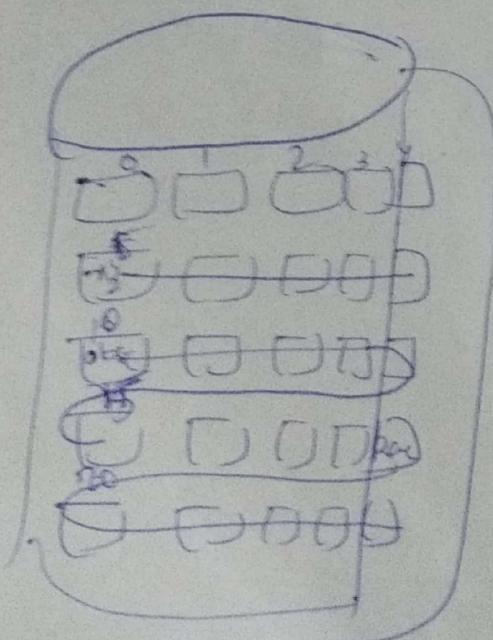
No. of disk blocks =  $\frac{64MB}{1KB} = 64k$

### Types of Allocation methods

- (A) Contiguous Allocation method
- (B) Non-contiguous Allocation (Linked Allocation)
- (C) Indexed Allocation method.

### Contiguous memory allocation:

→ contiguous free blocks are assigned for requested file size

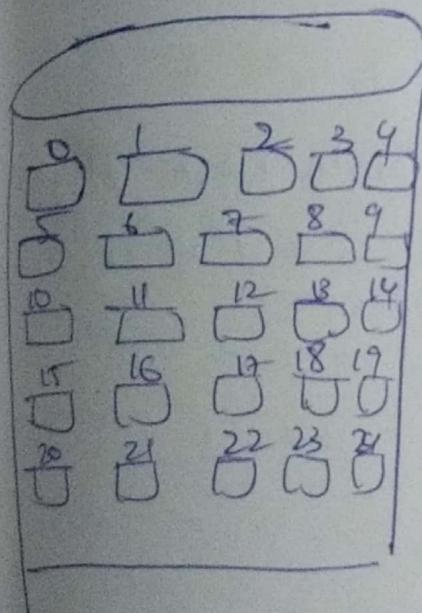


filename	start block	nof blocks
abc	10	7
xyzde	5	5
Random	19	6
Raw	X	C

~~If we can a~~ → ~~size and~~  
performance

- Internal fragmentation is present
- External fragmentation is present
- Increasing file size → ~~fragmentation may not~~  
→ Type of access ~~block~~ not trouble
- Sequential access
- Random access (base + number of blocks to be accessed)

### Linked allocation:



Size	filename	Start DBA	end DBA
1	abc.c	10	11
2	xyz.def	21	23
3	row	0	6

1 - { (0, 1, 13, 9, 3, 2)}

2 - { 21, 17, 23, 19 }

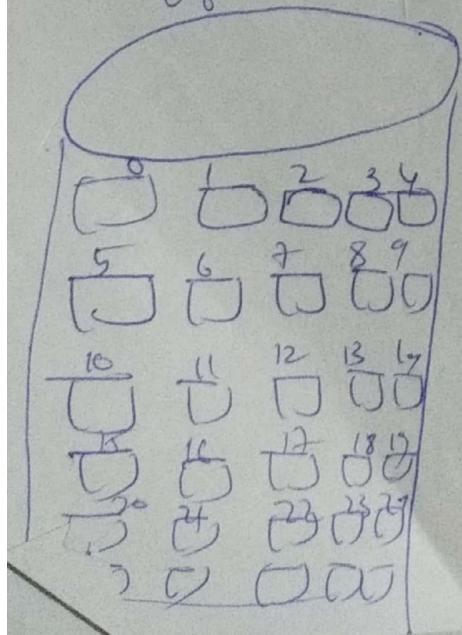
3. { 0, 6, 11, 8, 7 }

### Performance

- i) Internal fragmentation (✓)
- ii) external fragmentation (✗)
- iii) Increasing the file size flexible
- iv) Type of access segmented
- v) if datablock consist 'n' elements. (n)
- vi) if datablock consists of ~~elements~~ used to store data and ~~elements~~ elements used to store pointer to next datablock
- vii) memory leakage which it will break

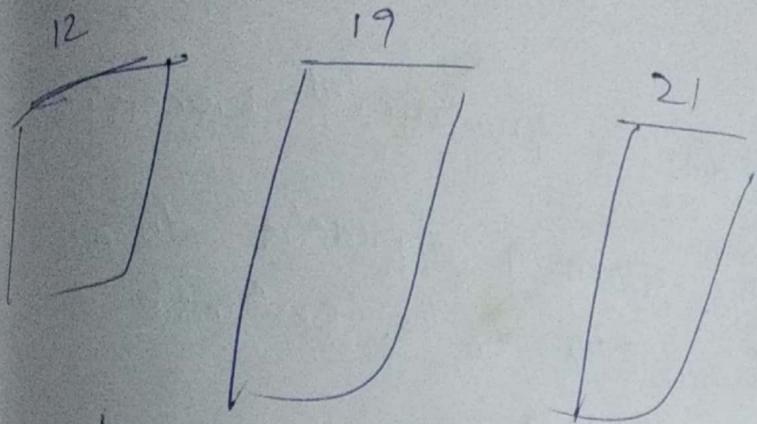
### Indexed Allocation

→ If file contains in data block Then  
 (nH) datablocks need to be used i.e  
 for each file there must be one index  
 block which contains list of addresses  
 of data blocks



SD	file	Index Block
1	abc-c	12
2	xyz-abc	19
3	kmkl	20

1024 size 512x512 ~ 6KB fat 64 6+1



Performance

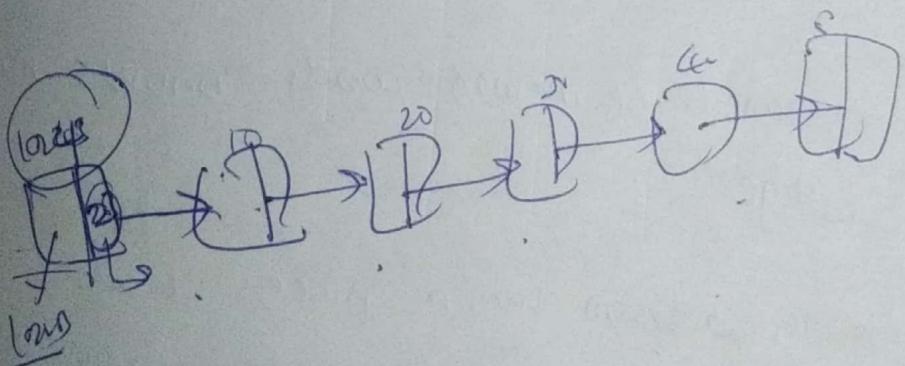
+ IF → ✓

+ EIF → ✗

Increasing file size → can be more

type of access

⇒ sequential and Random



→ The term page traffic describes the movement of page in and out of memory

→ blocked is not a fundamental process state.

→ Which of the following approaches do not require knowledge of the system?

- A. deadlock detection
- B. deadlock prevention
- C. deadlock avoidance

D. None

→ Blocking factor of a file is

- the number of logical records more than physical records

→ fragmentation is

fragments of memory words unused in a page

→ Consider a system has  $P$  processes. Each process needs a minimum of  $m$  resources and total of  $T$  resources available. What condition must hold to ~~make~~ make the system deadlock free

Q)  $\sum_{i=1}^P m_i \leq T$

~~Ques~~ a) ~~Explain what is the~~  
~~function~~ number of process that can be  
~~held~~ held in ready and blocked state ans

→ A Computer has 6 core drive with a  
process capacity for two. Each process  
may need two drives. If initially  
maximum value of n = 10 then  
deadlock free = 3

→ In which of following, ready to execute  
process must be present in P-M

- a - multiprogramming
- b - multiprogramming
- c - multitasking
- d - All

→ Threading implies excessive page I/O

3) Consider the following state

S1 The OS is designed to monitorize the  
resource utilization

S2 The control program manager for system  
program

OS file and S2 file

- starvation can be avoided by using first come first serve instead of SJT
- variable portion memory management technique with compaction results in reduction of fragmentation

- - 1. Deadlock state is unsafe
  - 2. unsafe state must lead to deadlock situation
  - 3. deadlock state is a subset of unsafe state

- loader performs the necessary relocation of the address and physically loads the executable code in memory

- A system has 3 processes sharing 4 resources. If each process needs a maximum of 2 units then deadlock never occur

- n processes share m resource of the same type. The maximum need of each process doesn't exceed n and sum of all ~~need~~ their maximum needs is always less than m. In this setup deadlock never occur

→ The main function of shared memory is  
Interprocess communication

→ What happens if a program address space  
does not end on a page boundary

Internal fragmentation (loss of memory)

→ A semaphore. count of negative n means  
( $s = -n$ ) that the queue contains n waiting  
processes

Important points

→ Response time are more predictable in preemptive  
systems than in non preemptive systems

→ Realtime systems generally use ~~non~~ preemptive  
cpu scheduling

\* The LRU algorithm

A pages out pages that have been used recently

B pages out pages that have not been recently  
used

C pages out pages that have been atleast  
used recently

→ The function perform by paging software are  
management of the physical address

→ A Loader creates a Load module