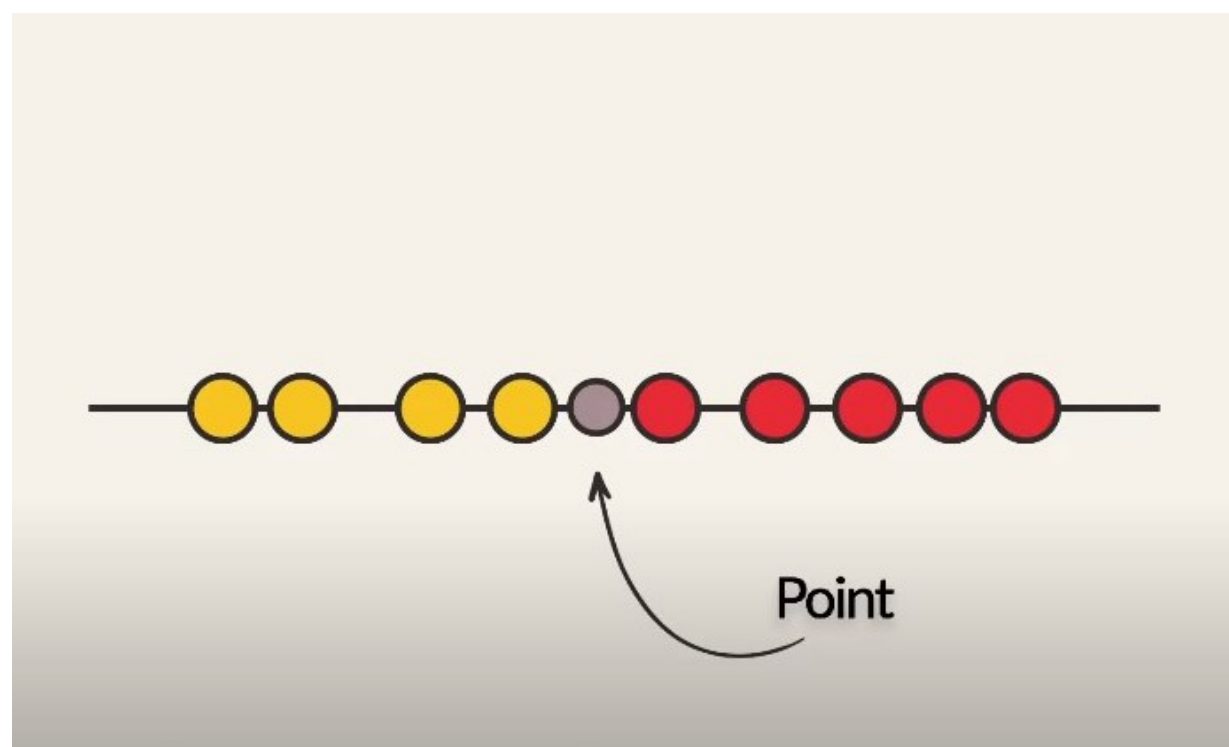


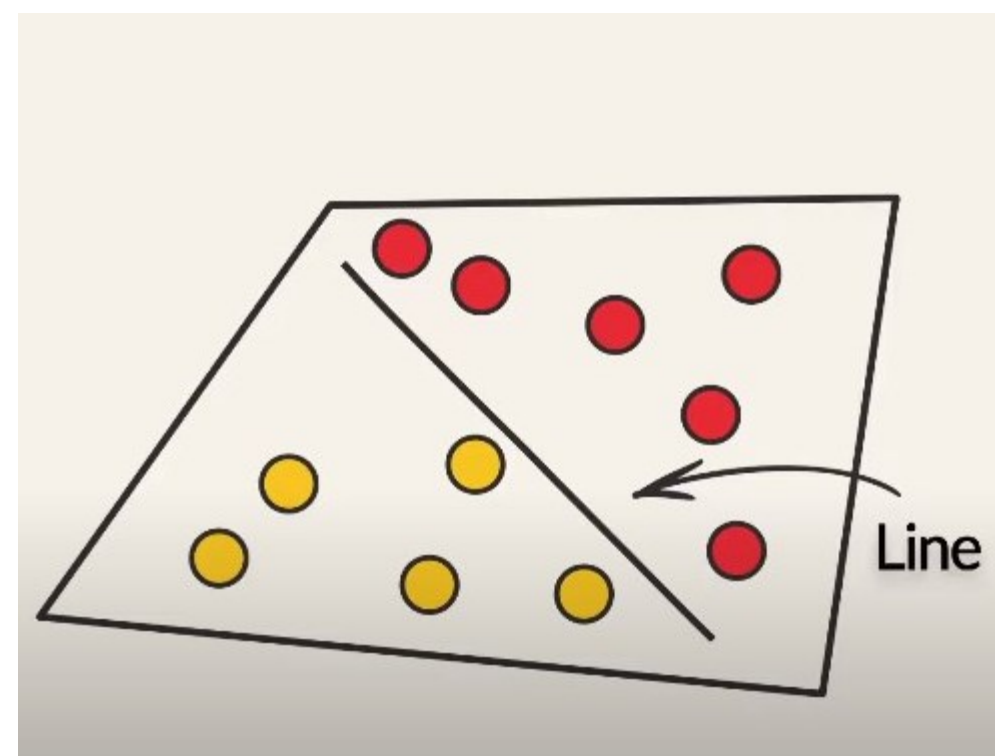
Support Vector Machine

Kanokkorn Pimcharoen

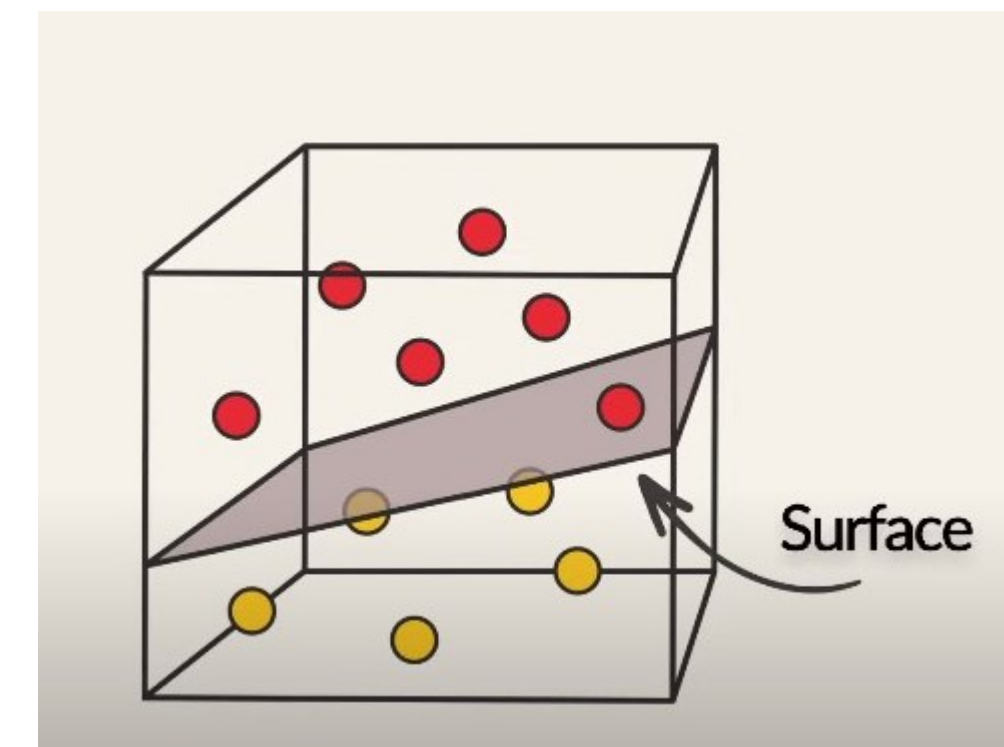
Separating Hyperplanes



1D Feature space



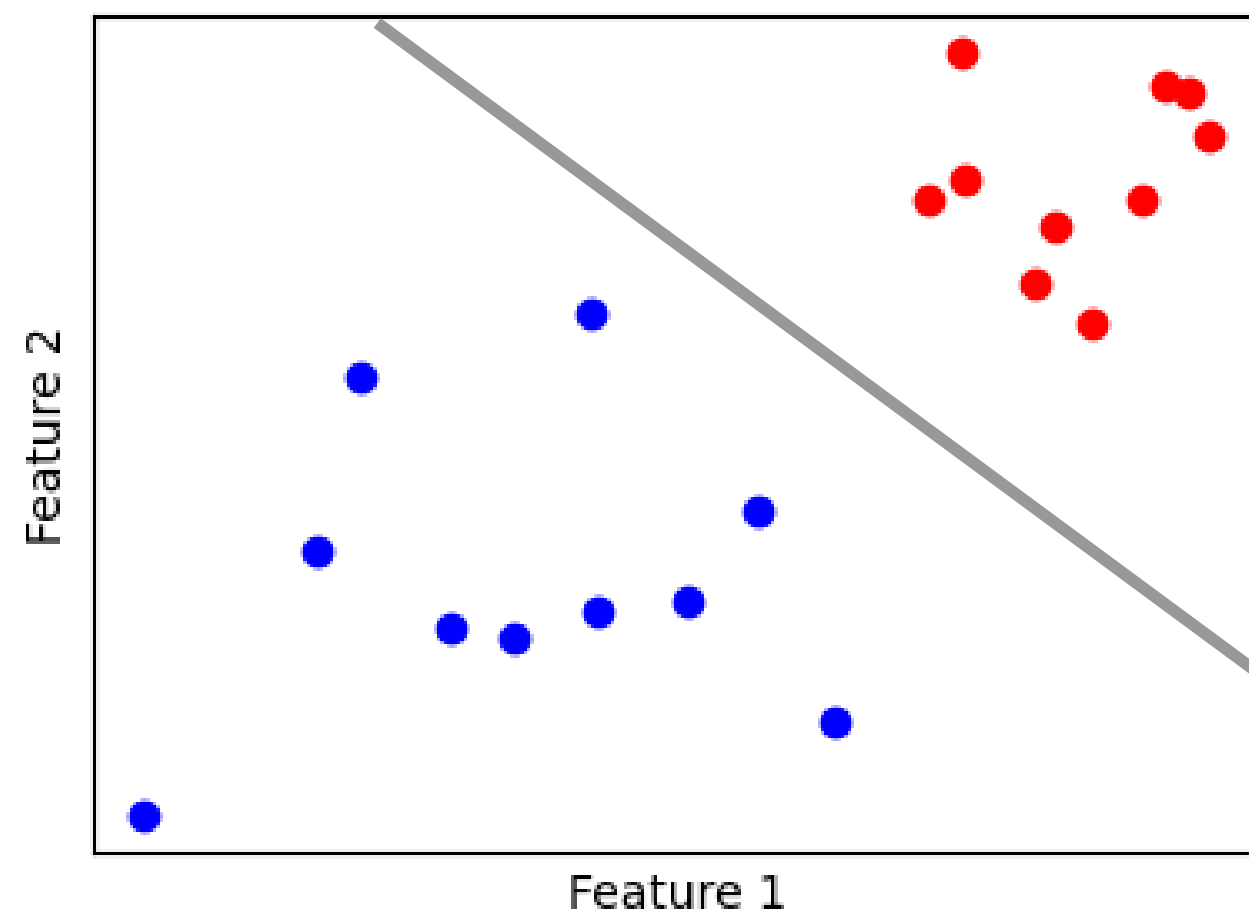
2D Feature space



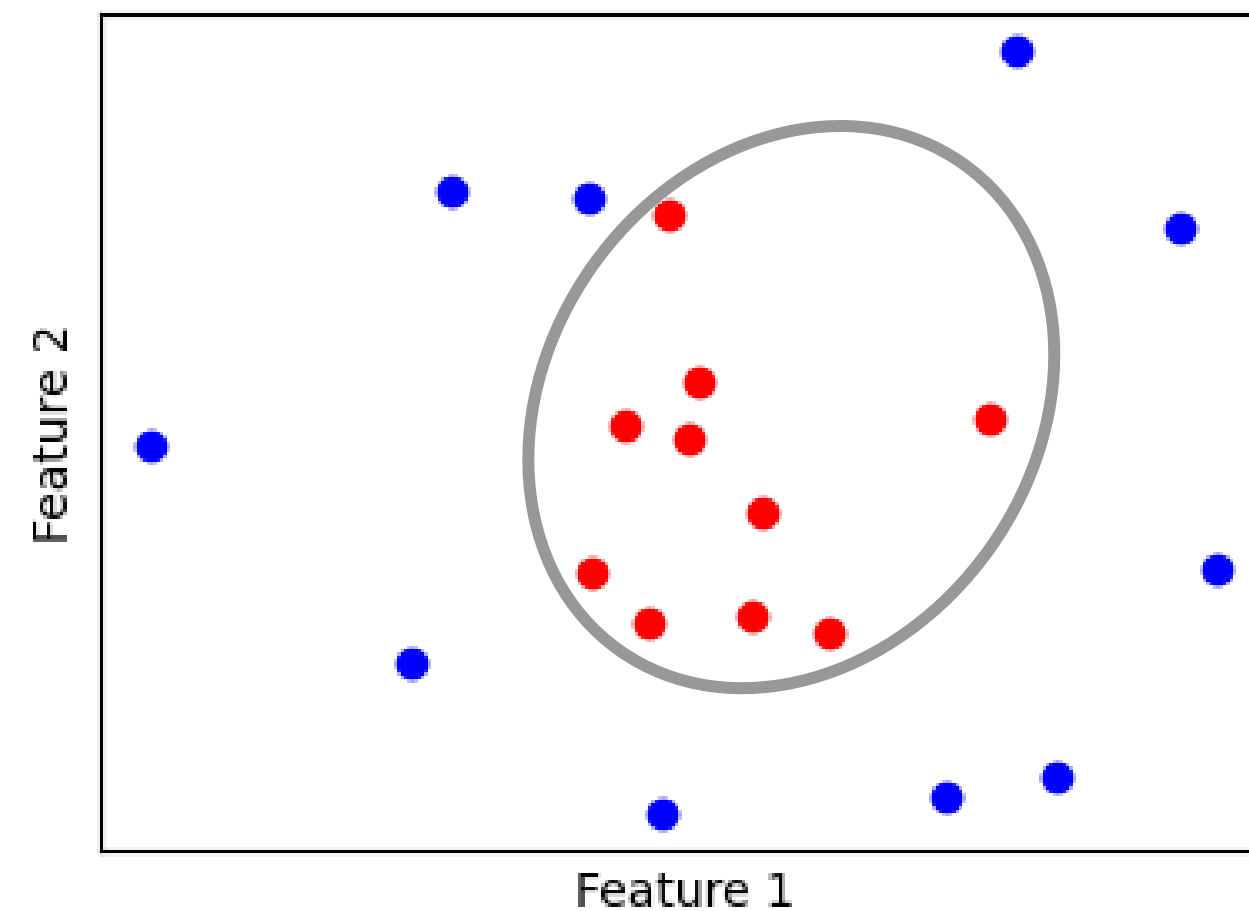
3D Feature space

Support Vector Machine

Linearly Separable

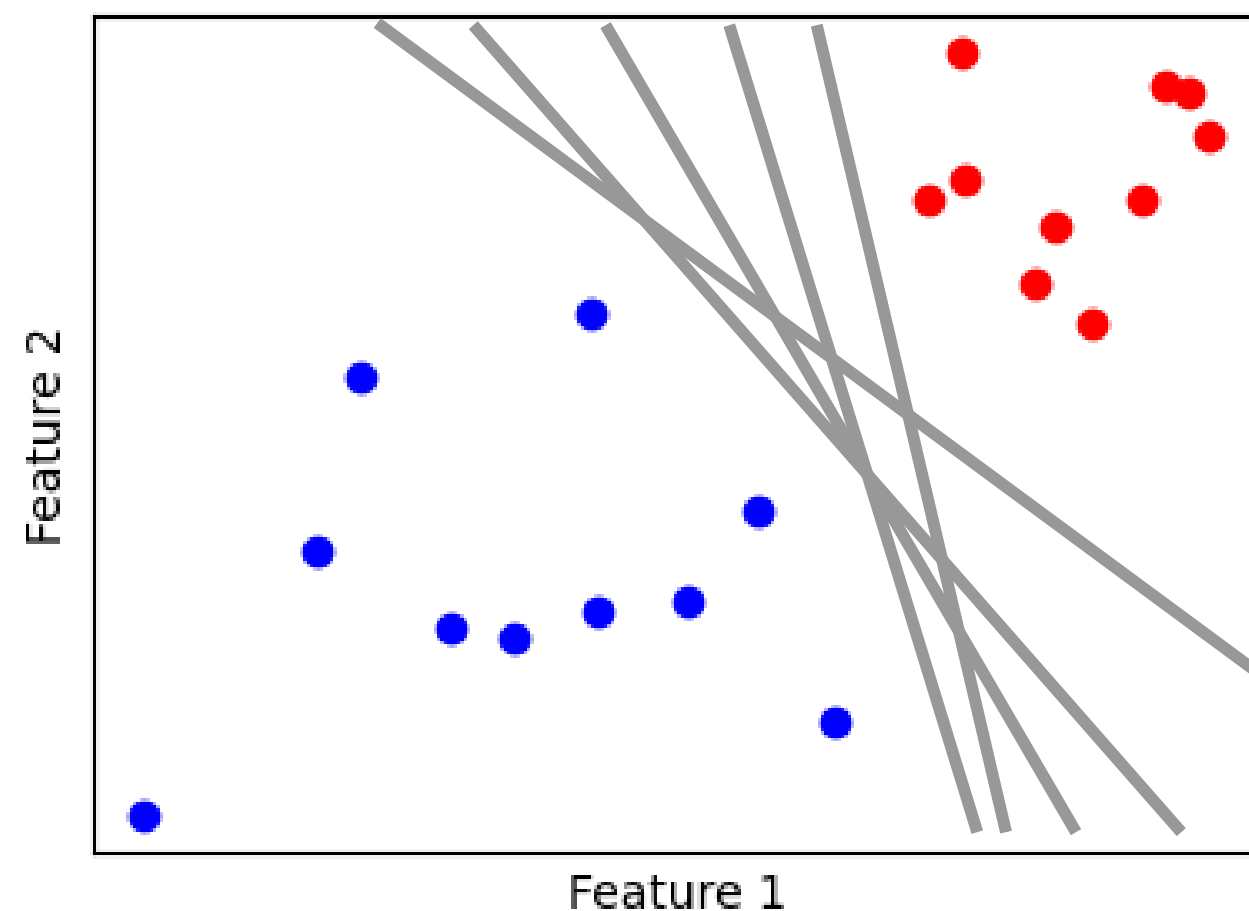


Non-Linearly Separable

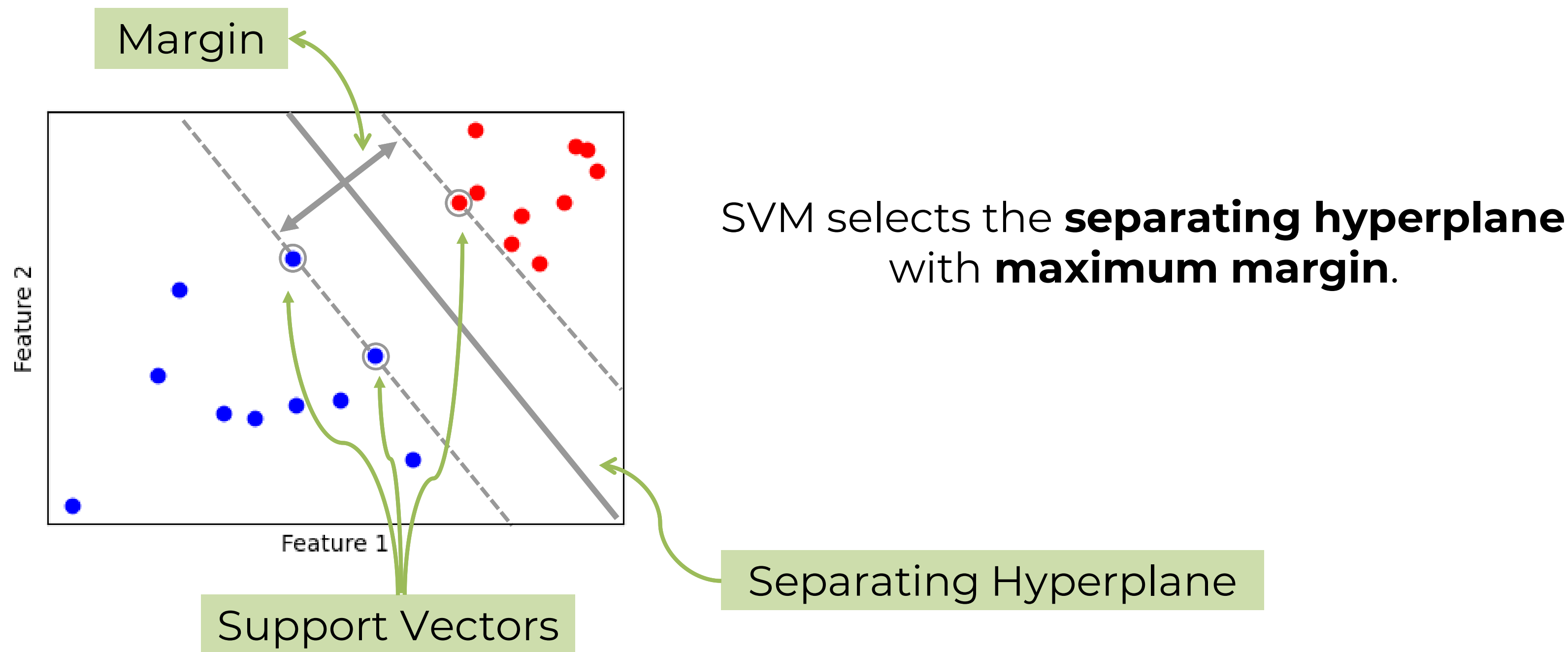


Support Vector Machine

Linearly Separable

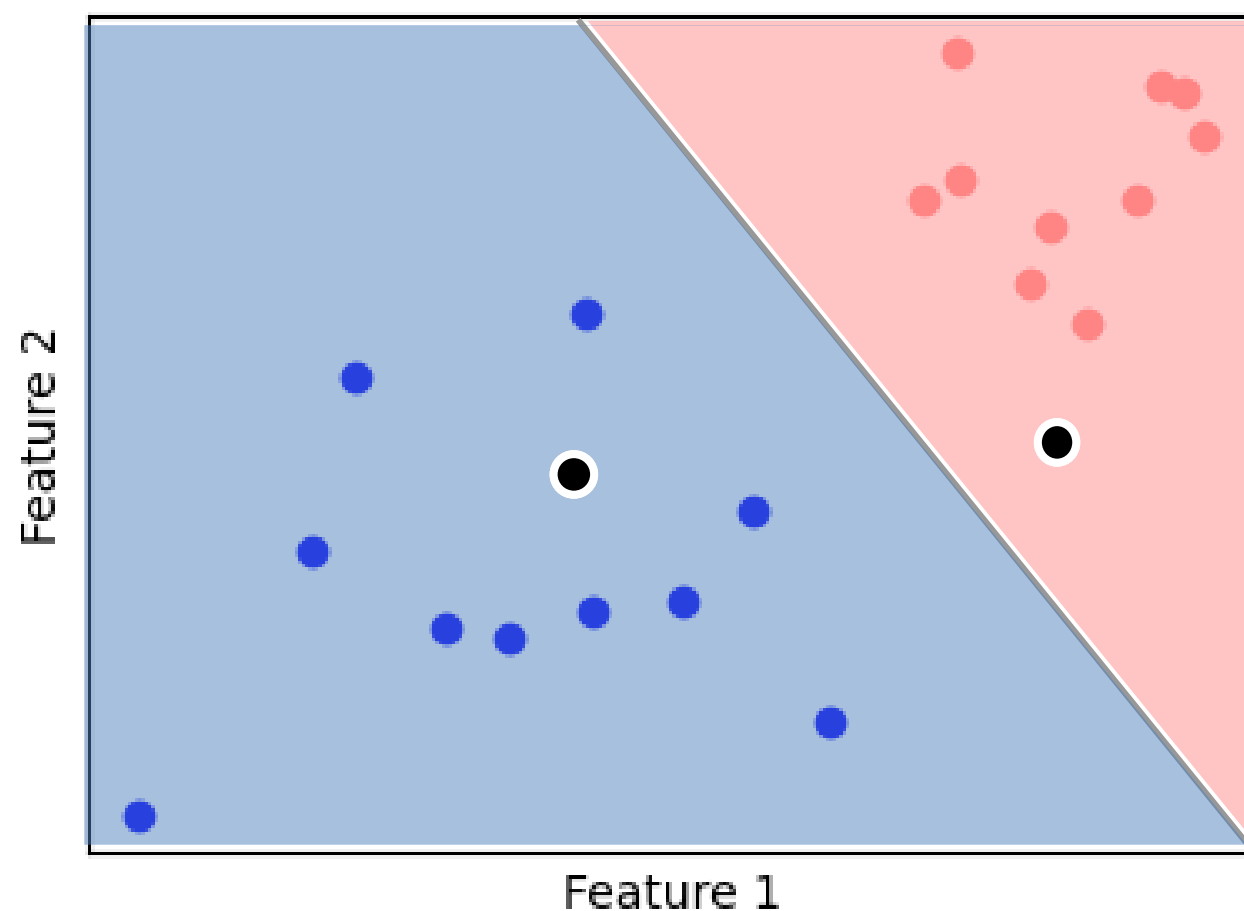


Support Vector Machine



Support Vector Machine

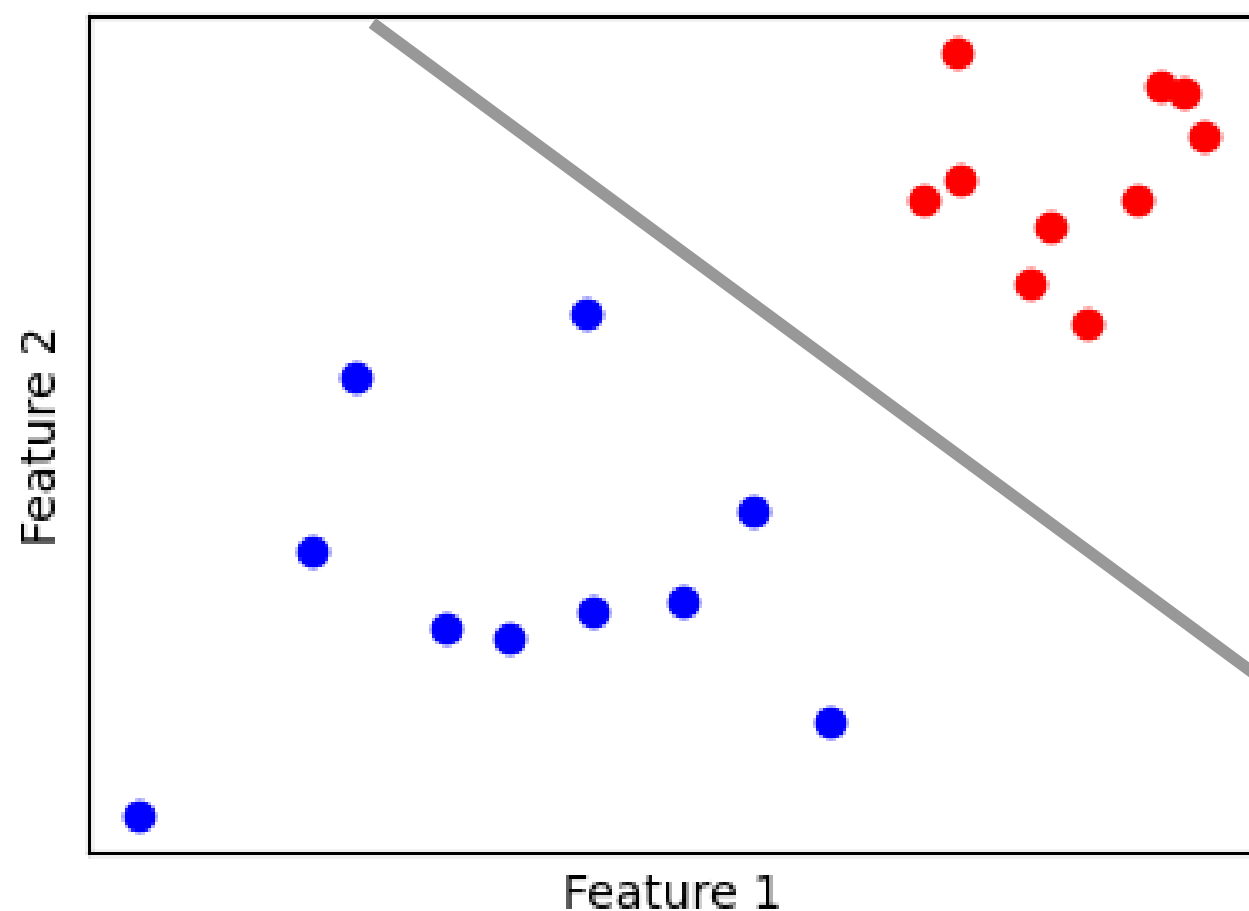
Decision Boundary



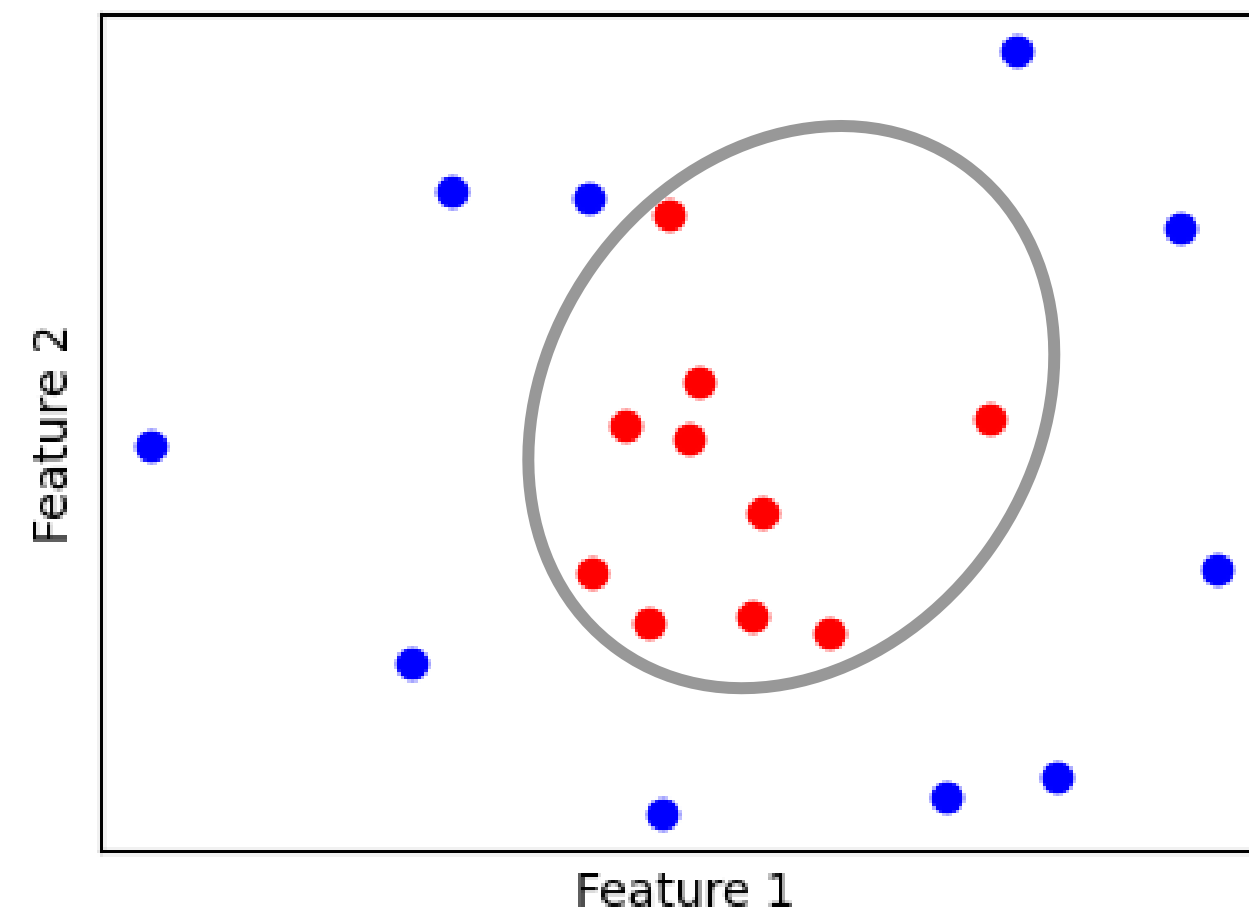
SVM selects the **separating hyperplane** with **maximum margin**.

Support Vector Machine

Linearly Separable ✓

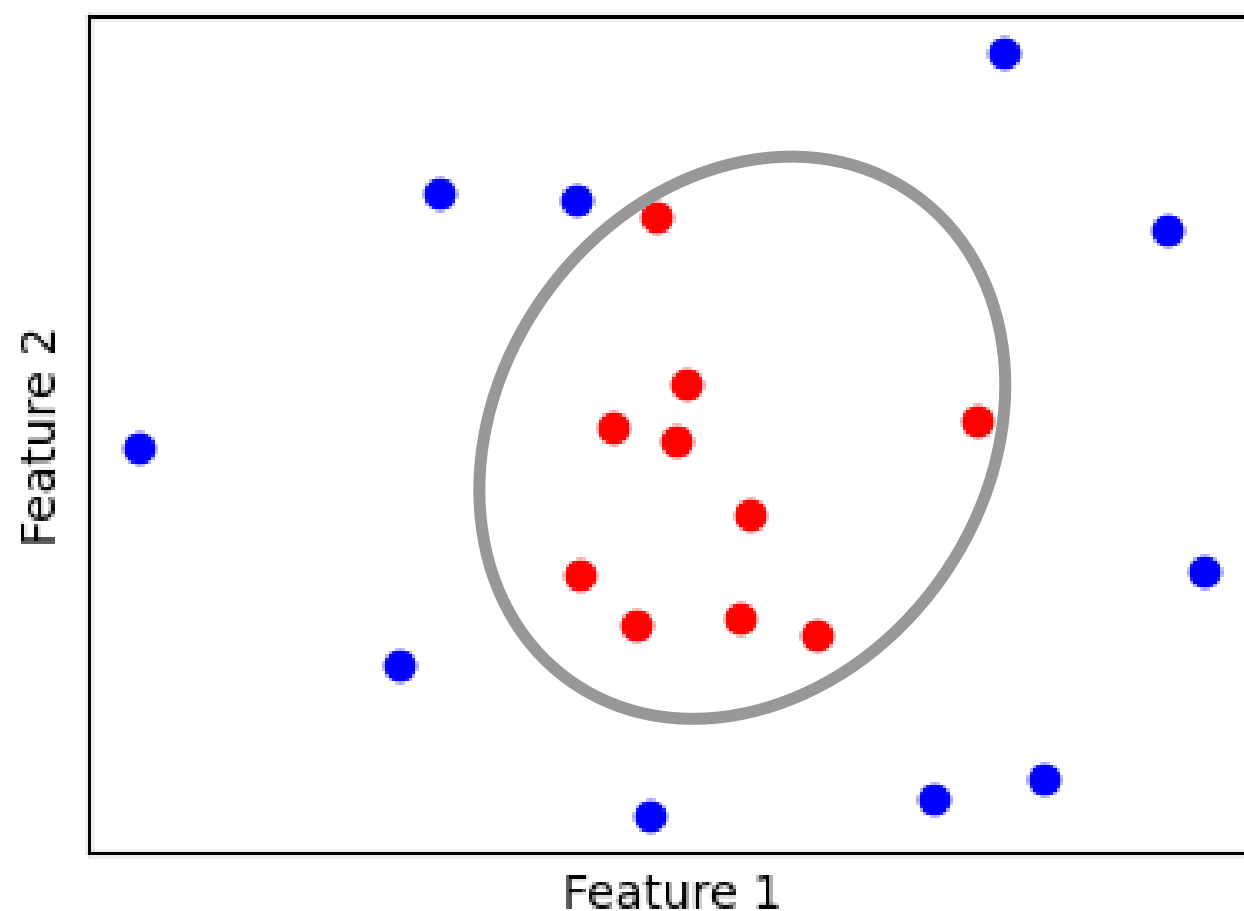


Non-Linearly Separable



Support Vector Machine

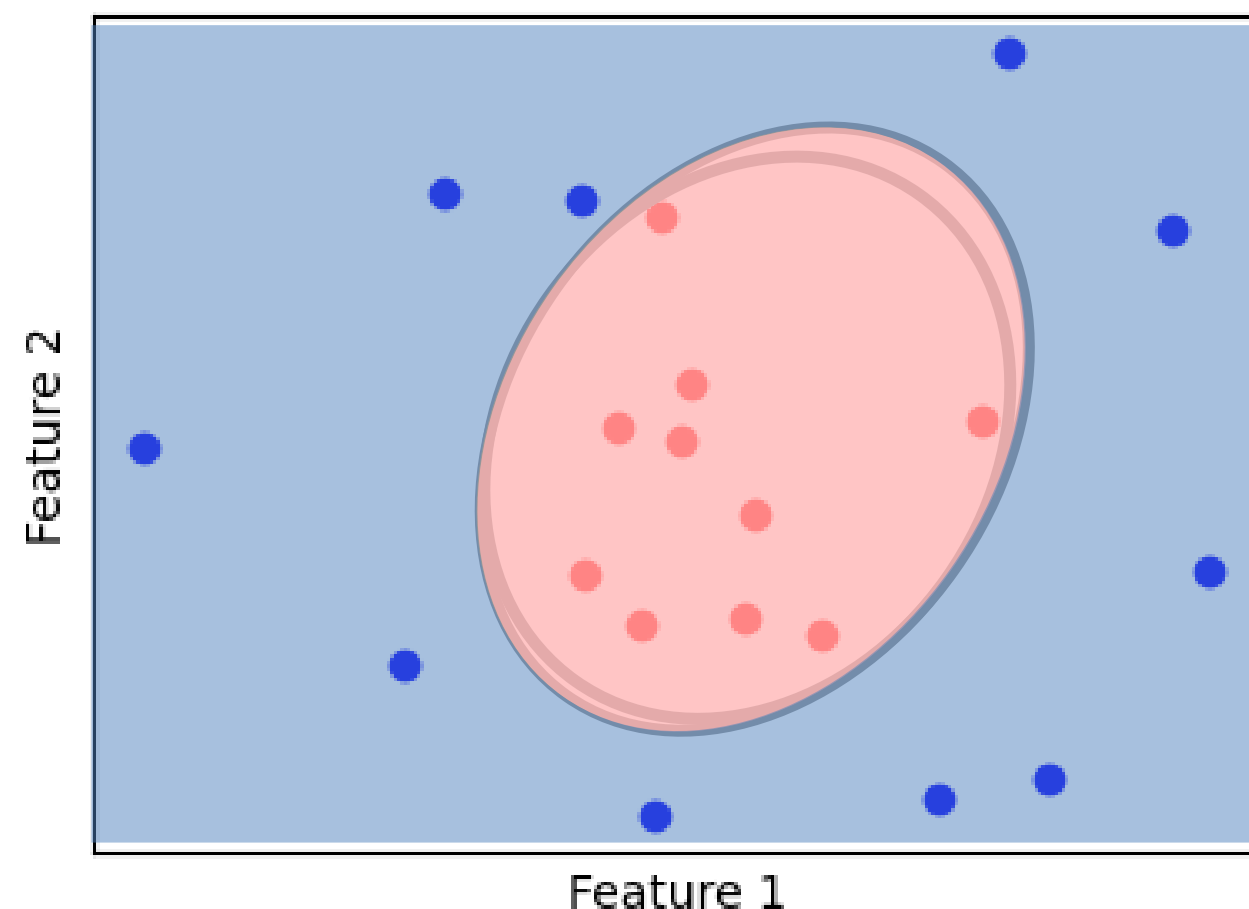
Non-Linearly Separable



SVM selects the **separating hyperplane** with **maximum margin**.

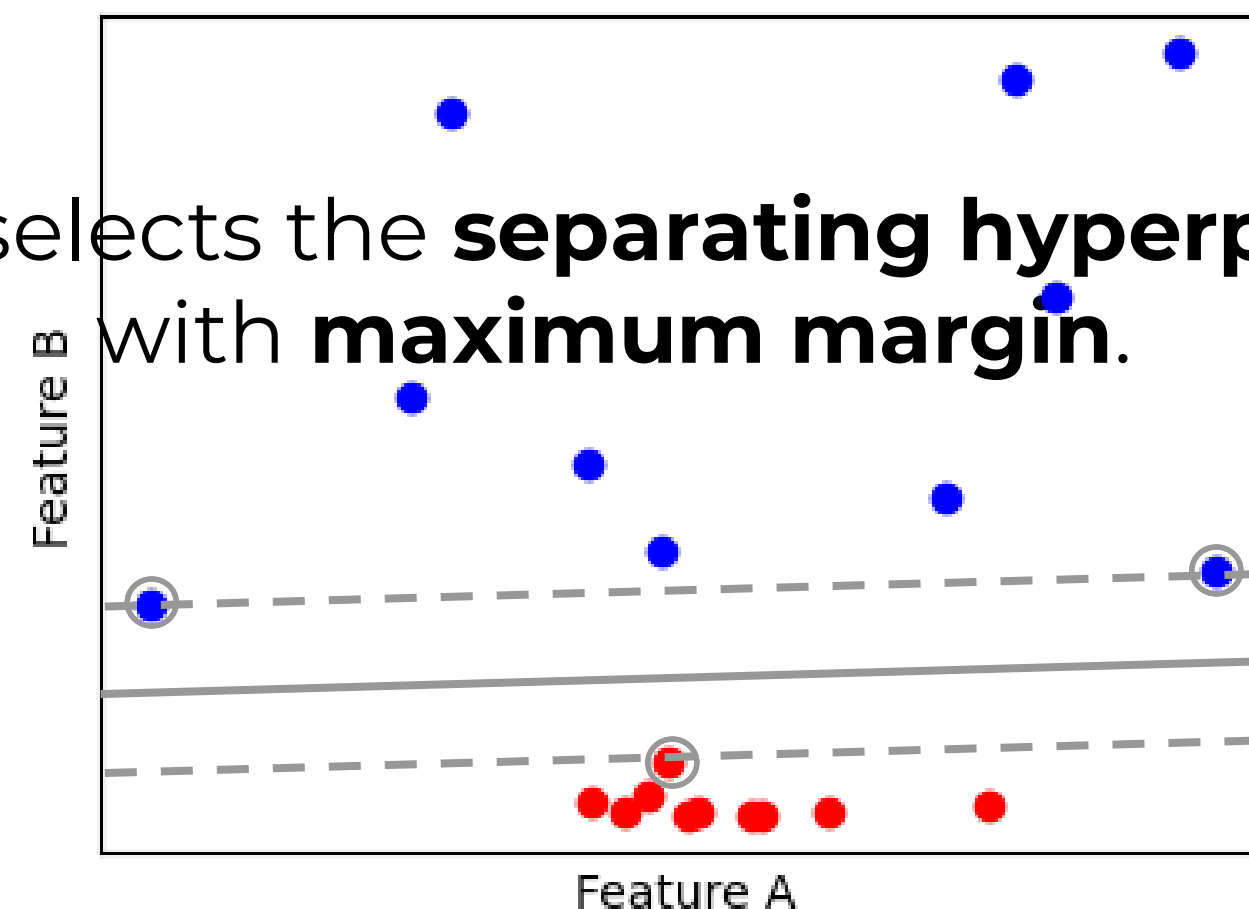
Support Vector Machine

Non-Linearly Separable



Non-Linear Decision Boundary

Linearly Separable



SVM selects the **separating hyperplane** with **maximum margin**.

Kernel

sklearn.svm.SVC

```
class sklearn.svm.SVC(*, C=1.0, kernel='rbf', degree=3, gamma='scale', coef0=0.0, shrinking=True,
probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1,
decision_function_shape='ovr', break_ties=False, random_state=None) ↑
```

[\[source\]](#)

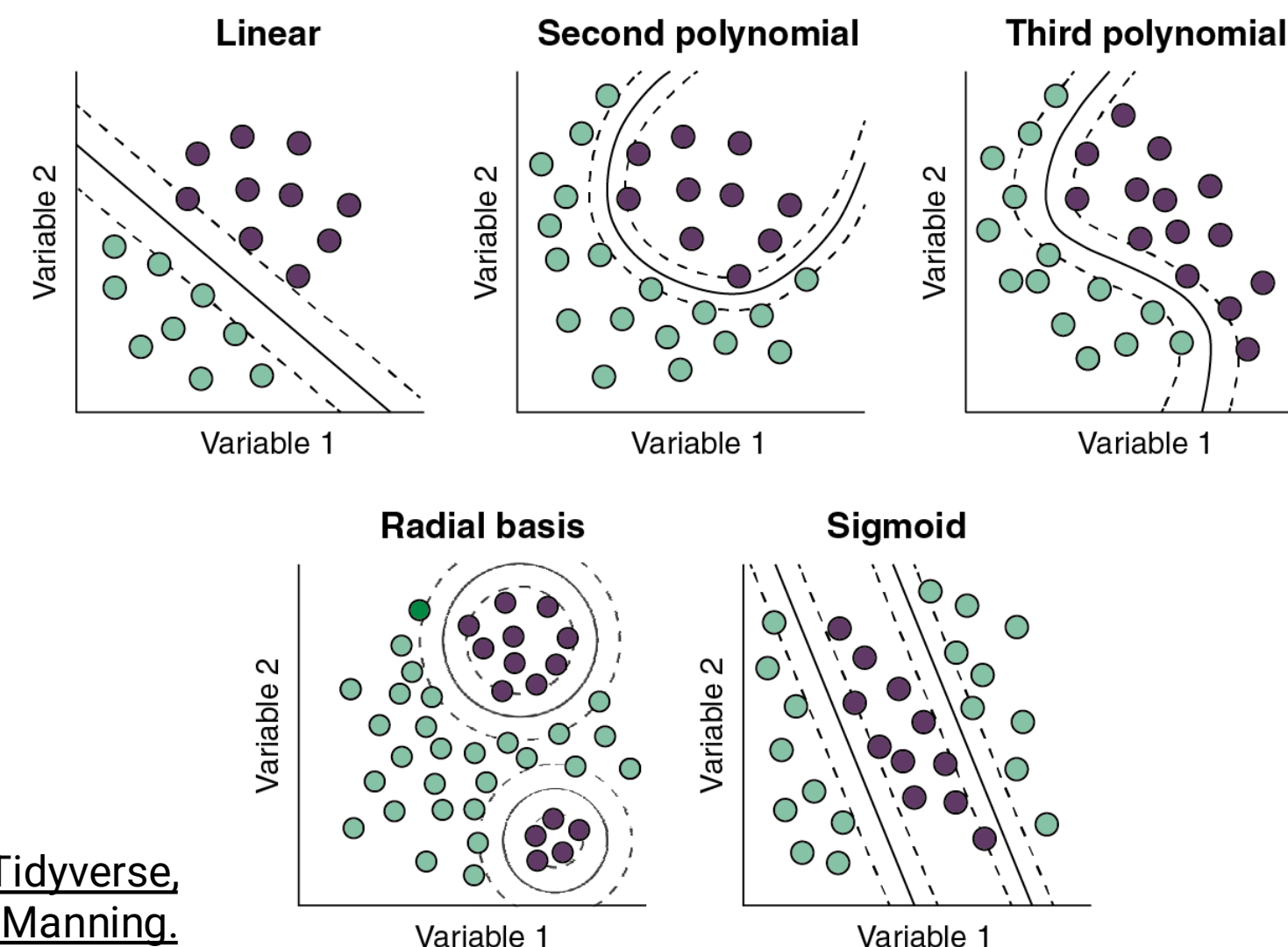
Parameters:

kernel : {'linear', 'poly', 'rbf', 'sigmoid', 'precomputed'} or callable, default='rbf'

Specifies the kernel type to be used in the algorithm. If none is given, 'rbf' will be used.

degree : int, default=3

Degree of the polynomial kernel function ('poly').



Rhys, H. (2020). Machine Learning with R, the Tidyverse, and Mlr. United States: Manning.

sklearn.svm.SVC

```
class sklearn.svm.SVC(*, C=1.0, kernel='rbf', degree=3, gamma='scale', coef0=0.0, shrinking=True,
probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1,
decision_function_shape='ovr', break_ties=False, random_state=None) ↑
```

[\[source\]](#)

Parameters:

C : float, default=1.0

Regularization parameter. The strength of the regularization is inversely proportional to C. Must be strictly positive. The penalty is a squared l2 penalty.

$$\mathcal{L}(x, y) + \lambda R(w) \longrightarrow C \mathcal{L}(x, y) + R(w)$$

Setting C to high value will reduce the effect of regularization

sklearn.svm.SVC

```
class sklearn.svm.SVC(*, C=1.0, kernel='rbf', degree=3, gamma='scale', coef0=0.0, shrinking=True,
probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1,
decision_function_shape='ovr', break_ties=False, random_state=None) ↑
```

[\[source\]](#)

Attributes:

coef_ : ndarray of shape (n_classes * (n_classes - 1) / 2, n_features)

Weights assigned to the features when `kernel="linear"`.

dual_coef_ : ndarray of shape (n_classes - 1, n_SV)

Dual coefficients of the support vector in the decision function

intercept_ : ndarray of shape (n_classes * (n_classes - 1) / 2,)

Constants in decision function.

support_ : ndarray of shape (n_SV)

Indices of support vectors.

support_vectors_ : ndarray of shape (n_SV, n_features)

Support vectors.

n_support_ : ndarray of shape (n_classes,), dtype=int32

Number of support vectors for each class.

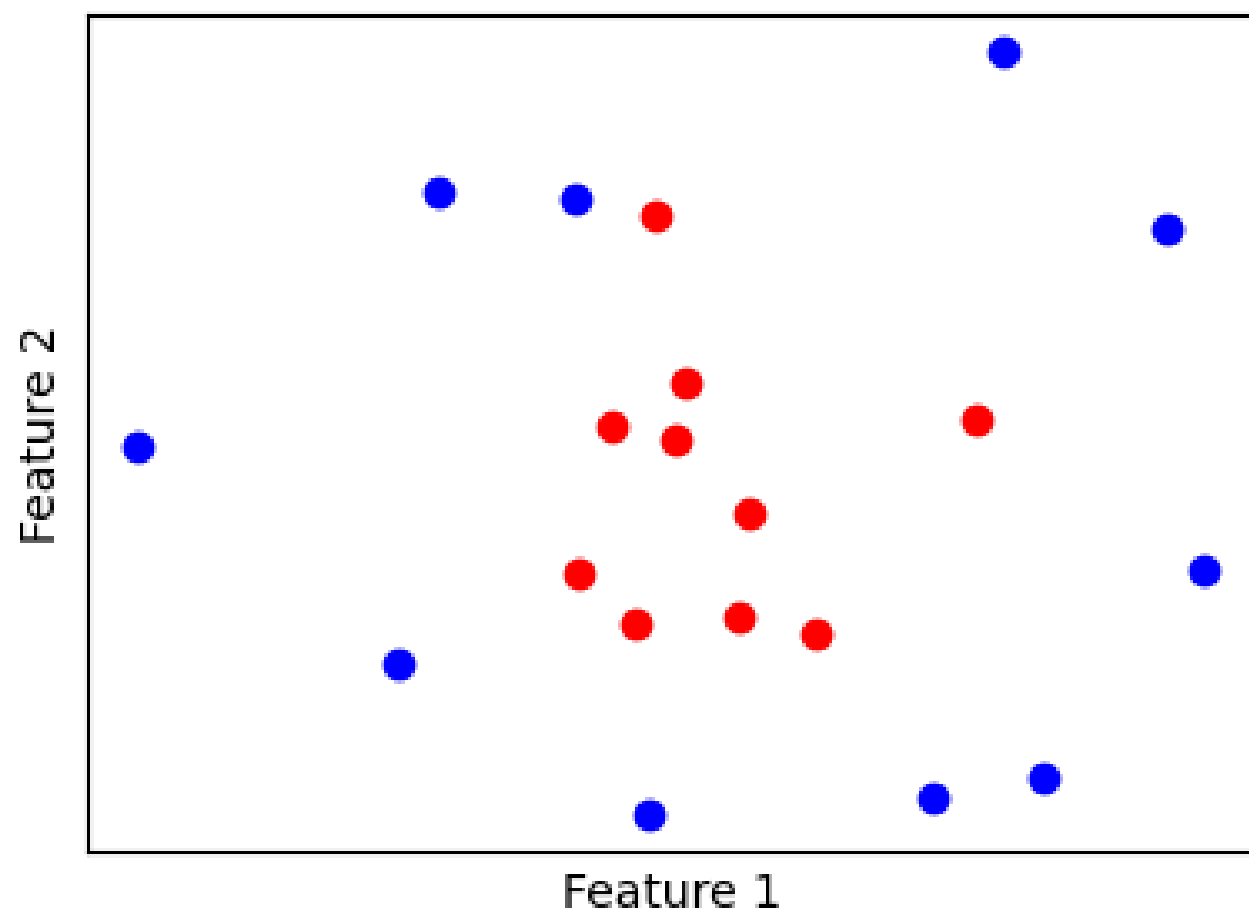
Decision Boundary

Support Vectors

Support Vector Machine

Dataset

$$(x_{1,1}, x_{1,2}, y_1), (x_{2,1}, x_{2,2}, y_2), (x_{3,1}, x_{3,2}, y_3), \dots, (x_{n,1}, x_{n,2}, y_n)$$



$$\mathbf{X} = \begin{bmatrix} x_{1,1} & x_{1,2} \\ x_{2,1} & x_{2,2} \\ x_{3,1} & x_{3,2} \\ \vdots & \vdots \\ x_{n,1} & x_{n,2} \end{bmatrix}$$

shape = (n, 2)

$$\mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_n \end{bmatrix}$$

shape = (n, 1)

```
# Import a necessary modules
from sklearn.svm import SVC
```

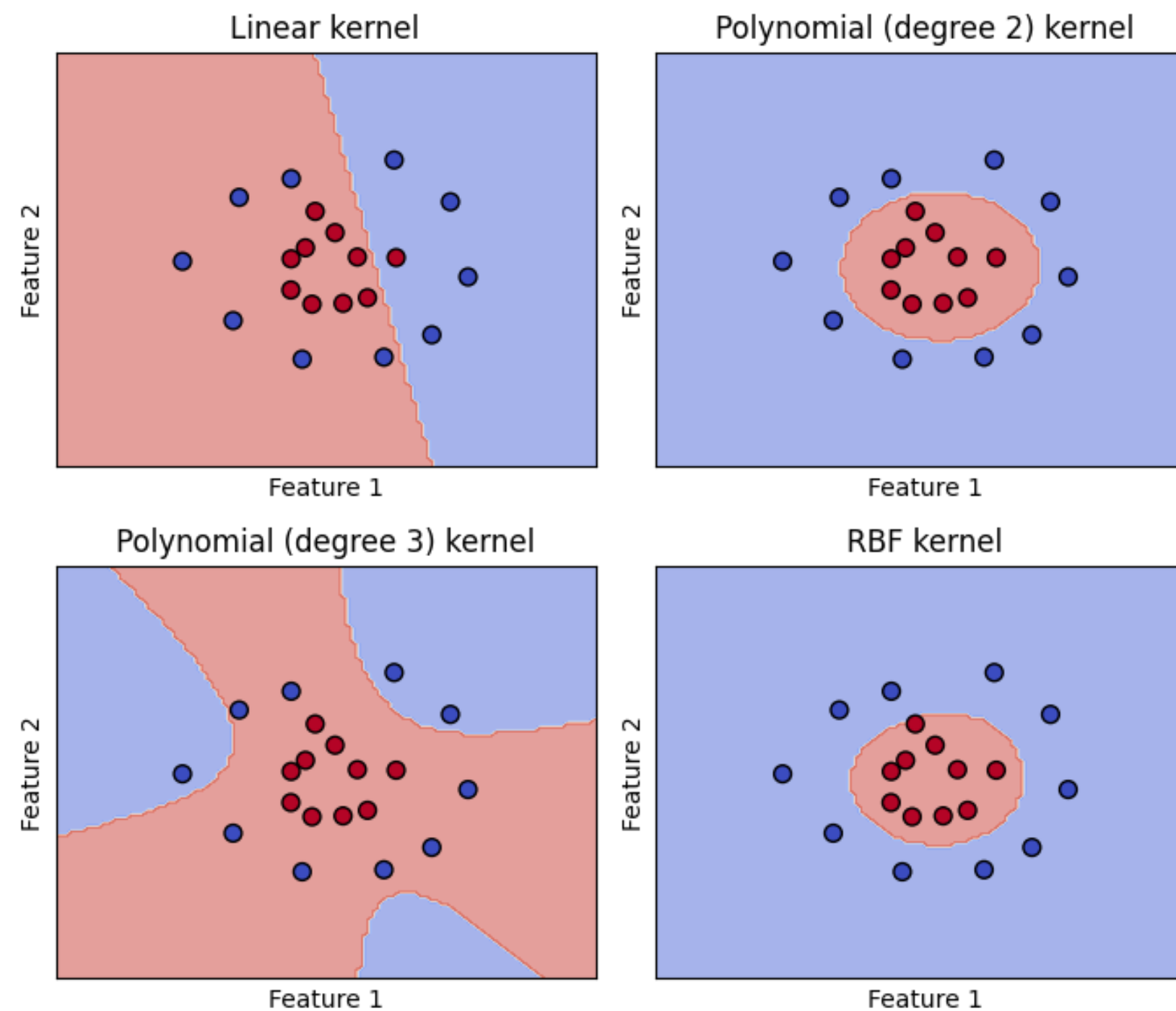
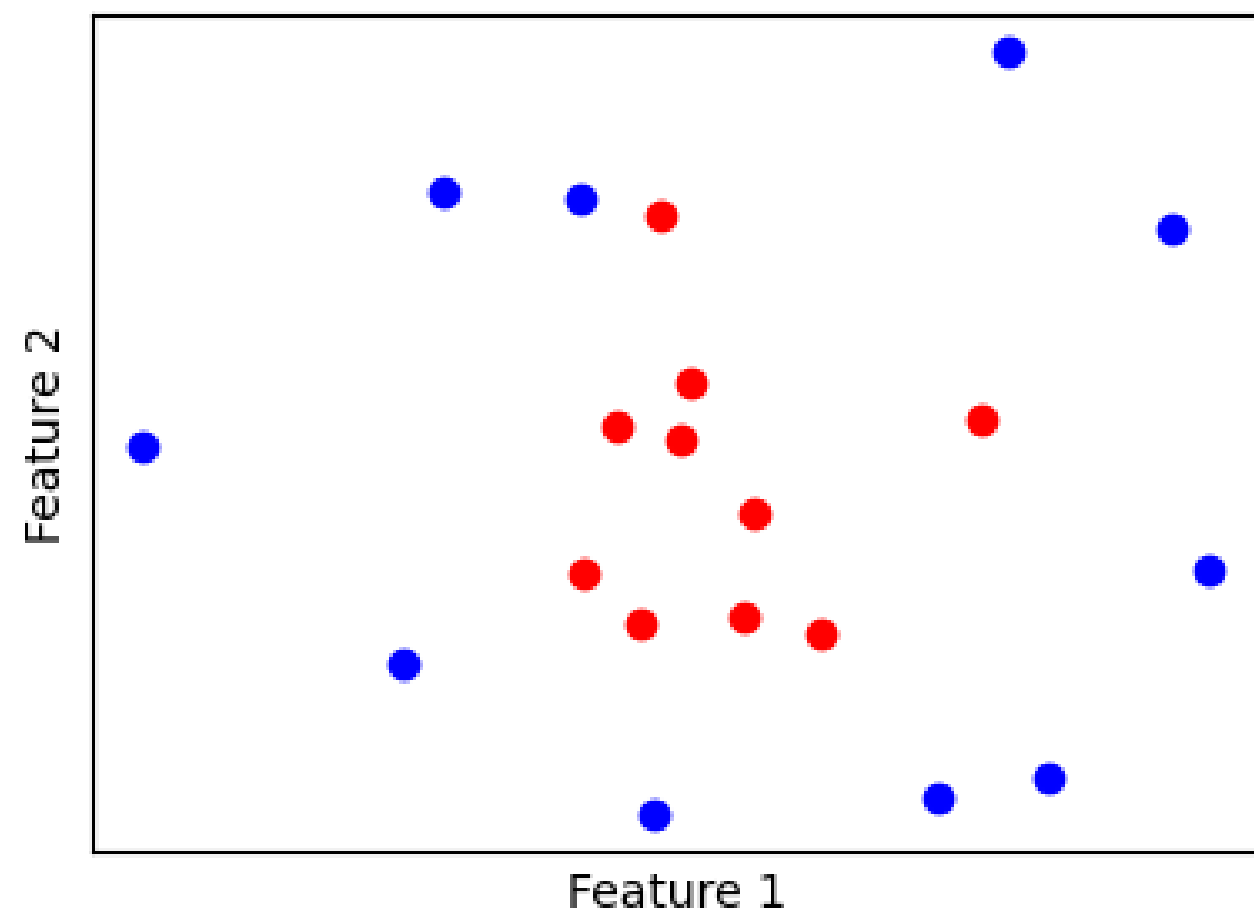
```
# Create the model with linear kernel
clf = SVC(kernel='linear')
```

```
# Train the model
clf.fit(X, y)
```

```
# Make prediction
y_pred = clf.predict(X_test)
```

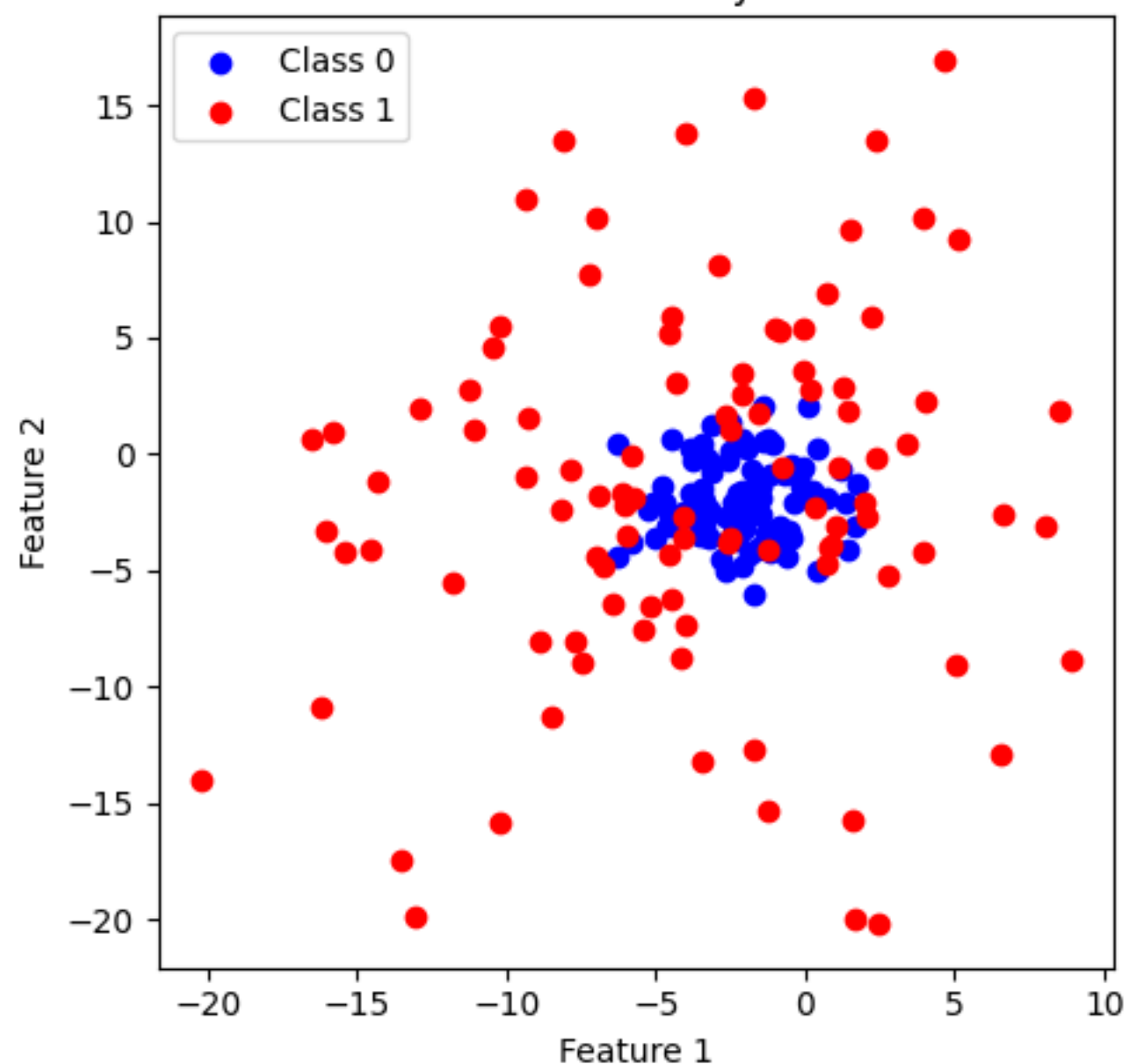
```
# Create the model with non-linear kernel
clf = SVC(kernel='poly', degree=2)
clf = SVC(kernel='rbf')
```

Support Vector Machine

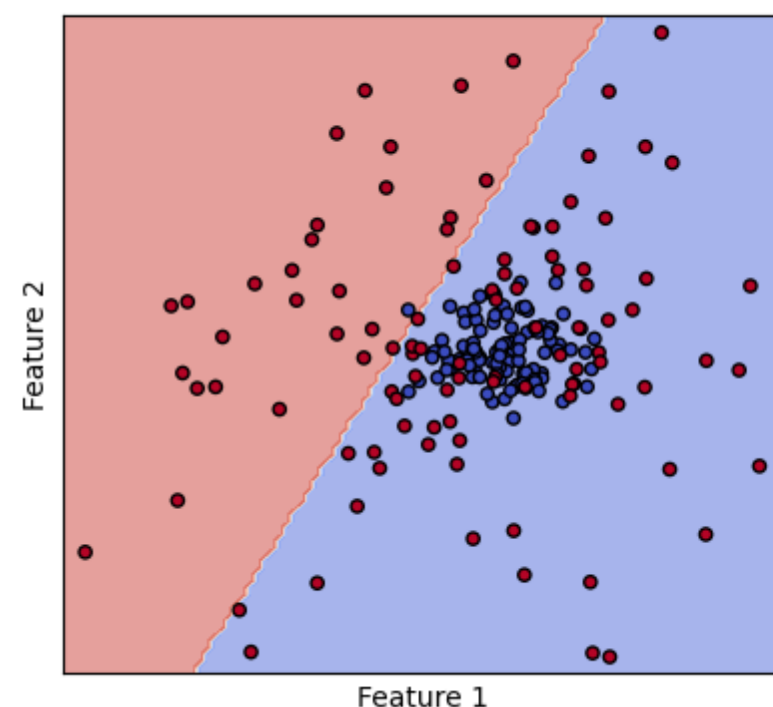


Support Vector Machine

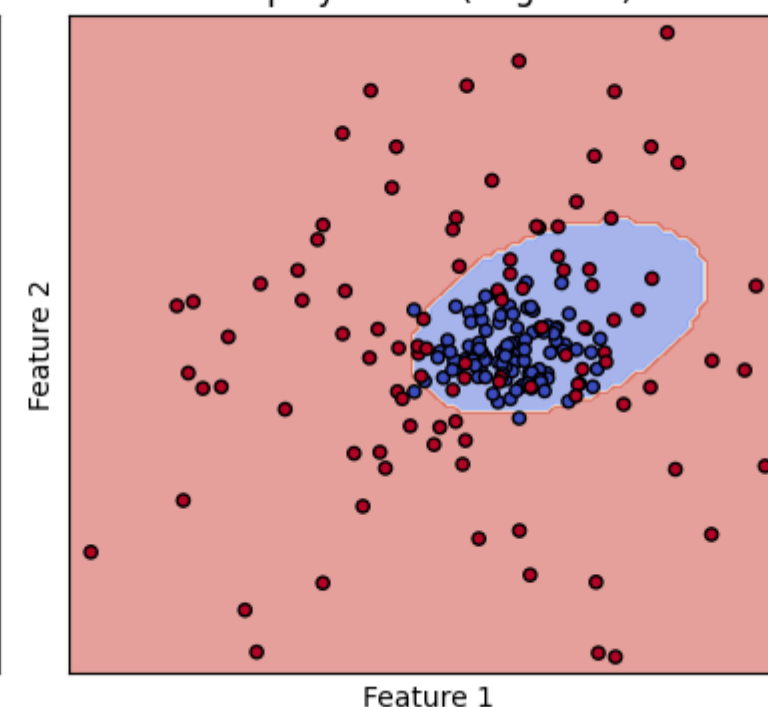
Simulated Data for Binary Classification



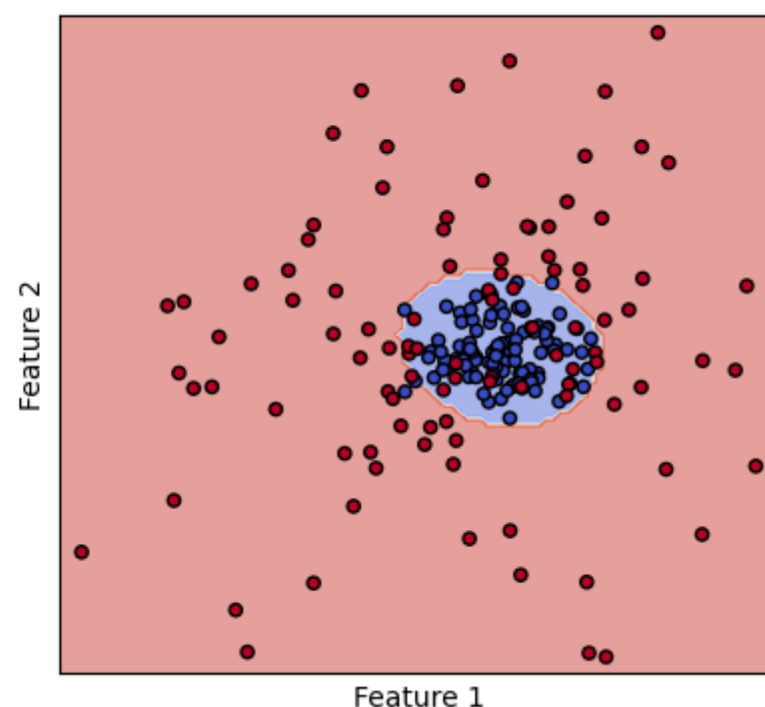
SVC with linear kernel



SVC with polynomial (degree 2) kernel



SVC with RBF kernel

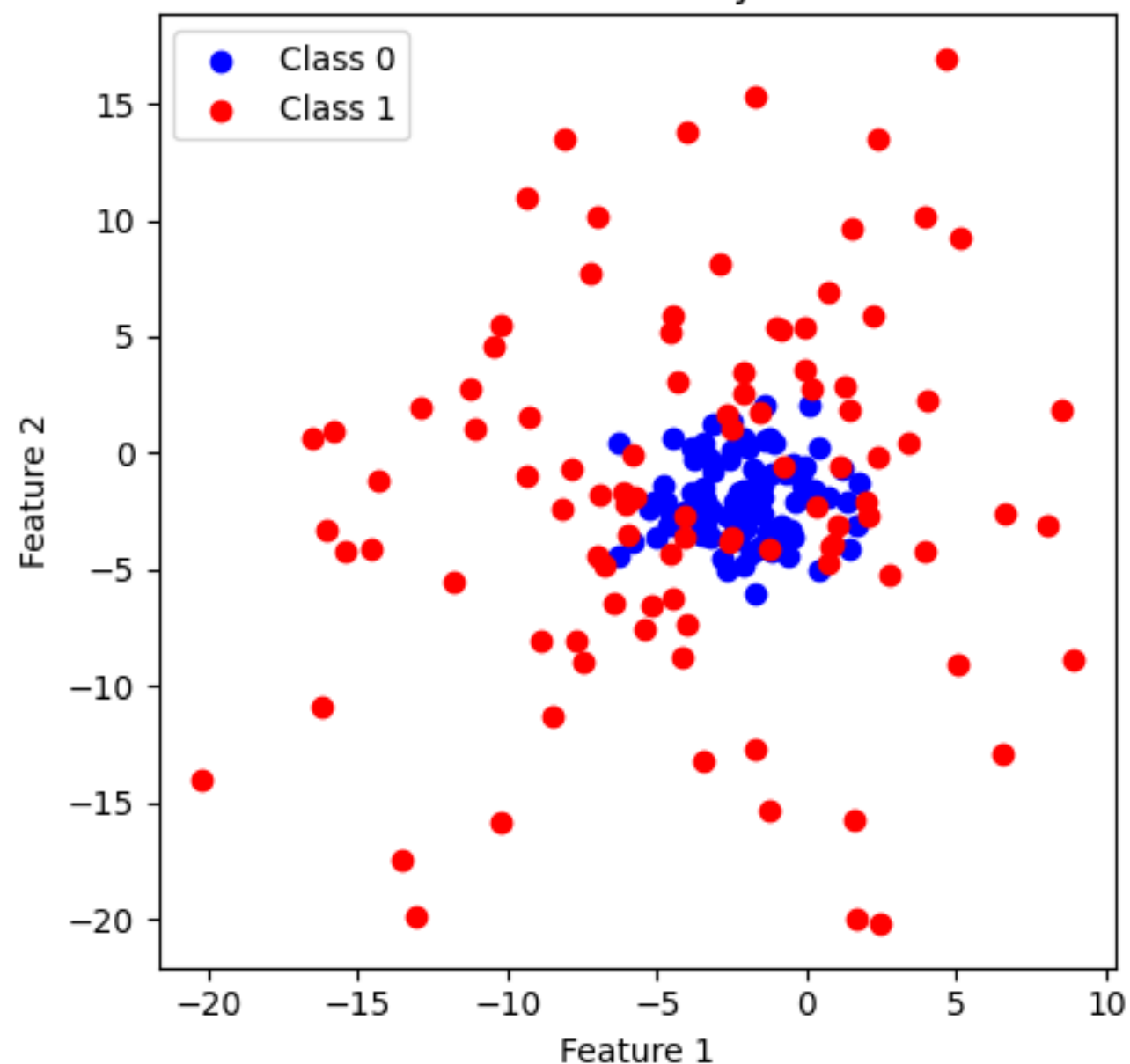


Linear kernels always yield linear decision boundary. For a non-linearly separable dataset, a non-linear kernel is preferred.

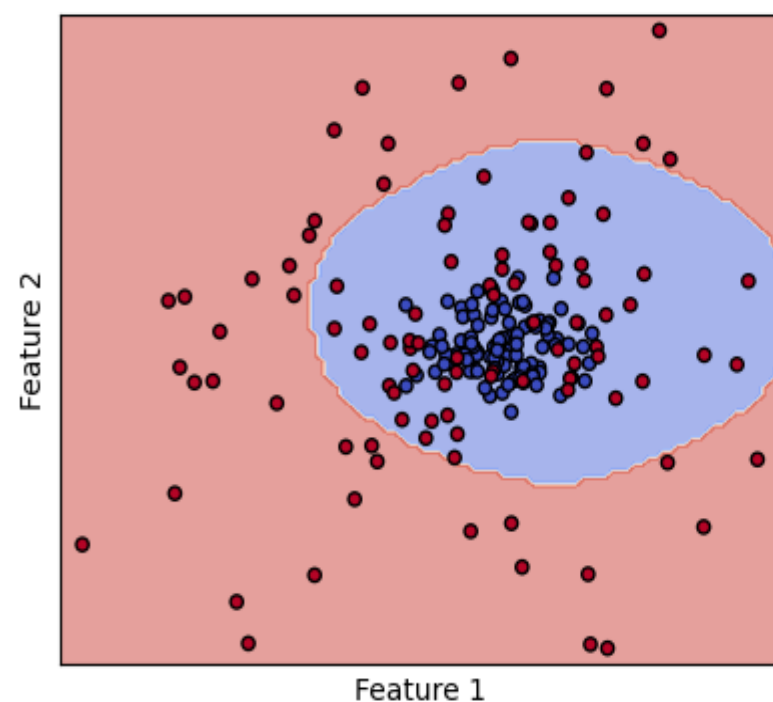
Thus, polynomial (degree 2) and RBF kernels can fit this dataset better than linear kernels.

Support Vector Machine

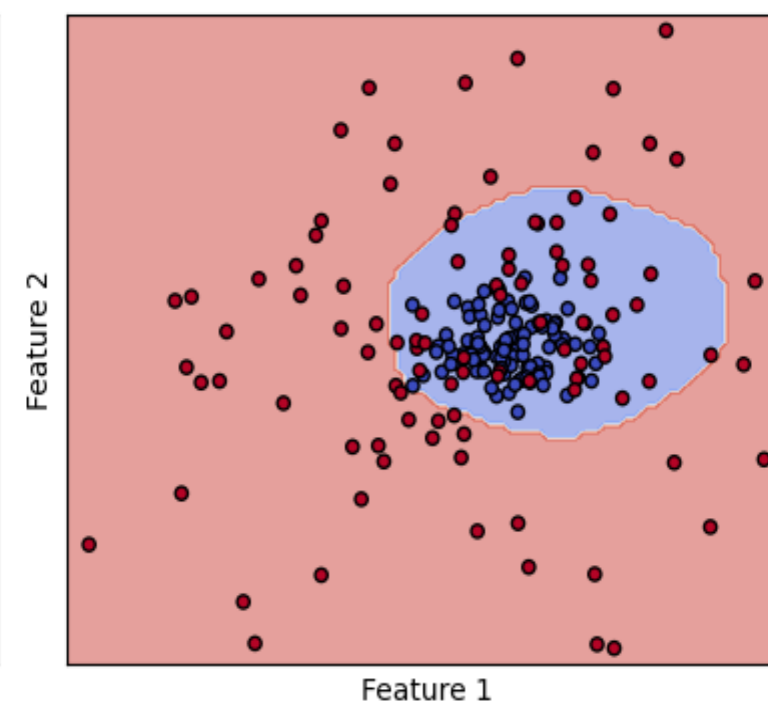
Simulated Data for Binary Classification



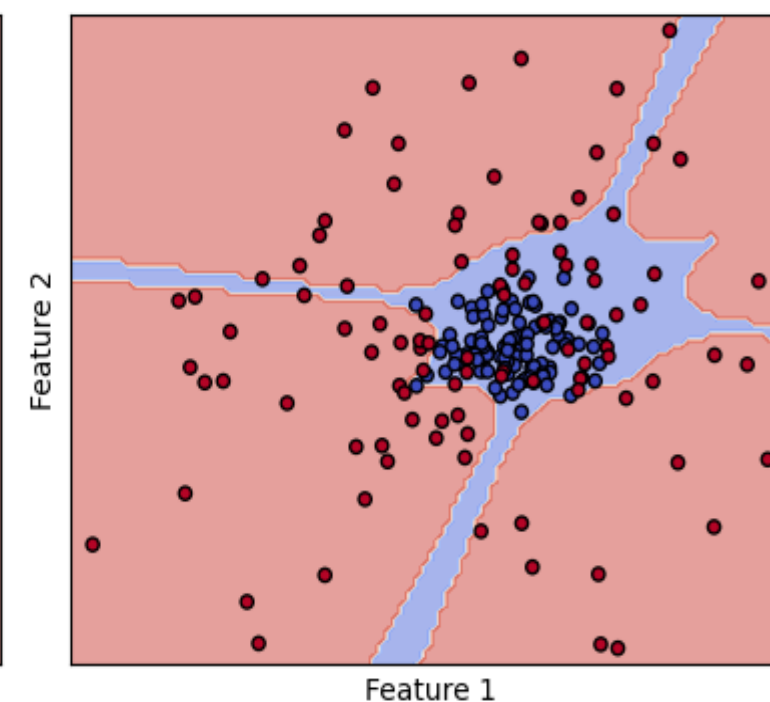
SVC with polynomial (degree 10) kernel,
 $C=10^{-3}$



SVC with polynomial (degree 10) kernel,
 $C=10^0$



SVC with polynomial (degree 10) kernel,
 $C=10^3$



$$C \mathcal{L}(x, y) + R(w)$$

- Too low $C \rightarrow$ regulation effect is strengthened. \rightarrow Underfitting
- Too high $C \rightarrow$ regulation effect is weakened. \rightarrow Overfitting