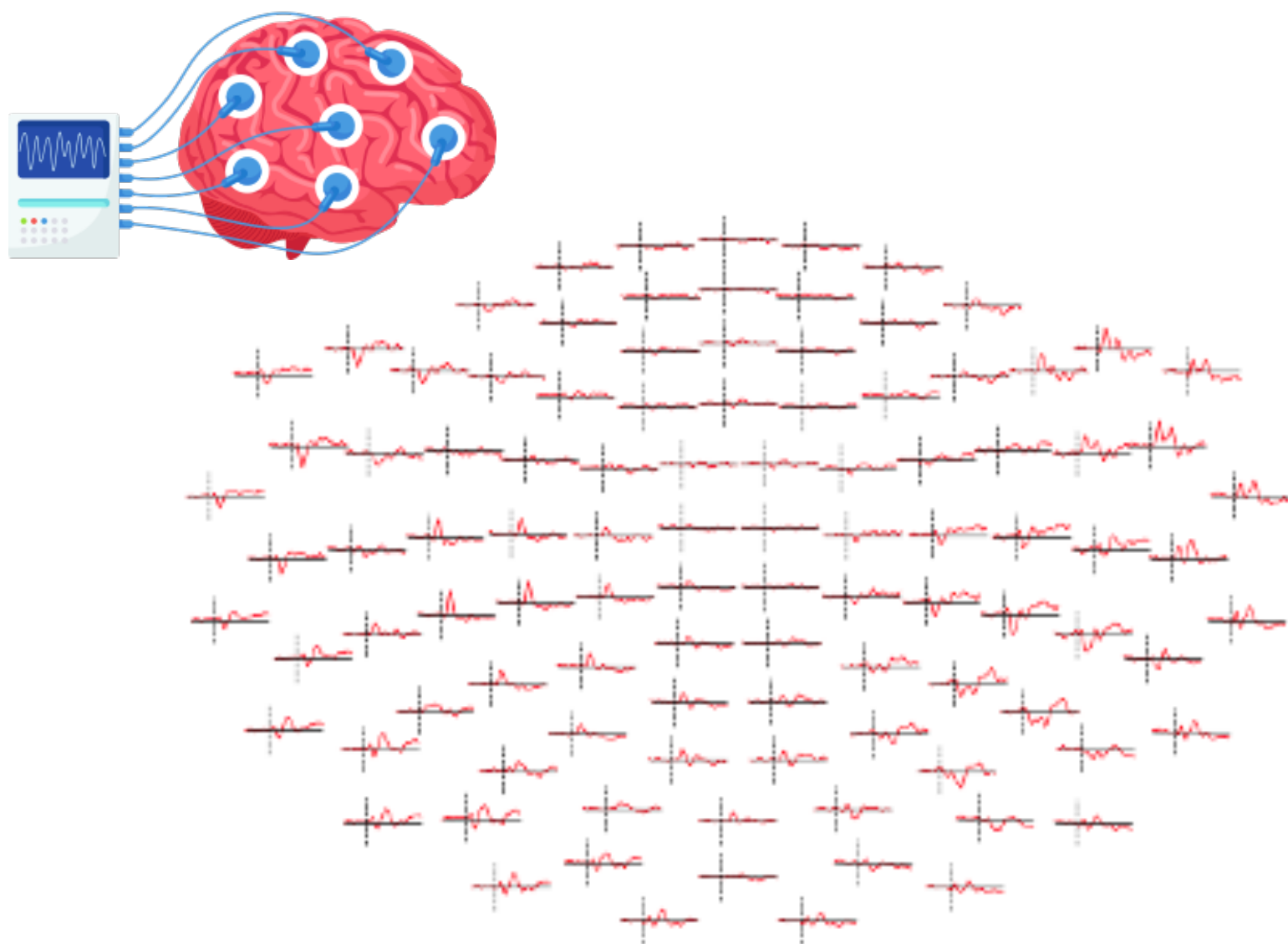


# Signals and Sampling

Itthi Chatnuntaweck

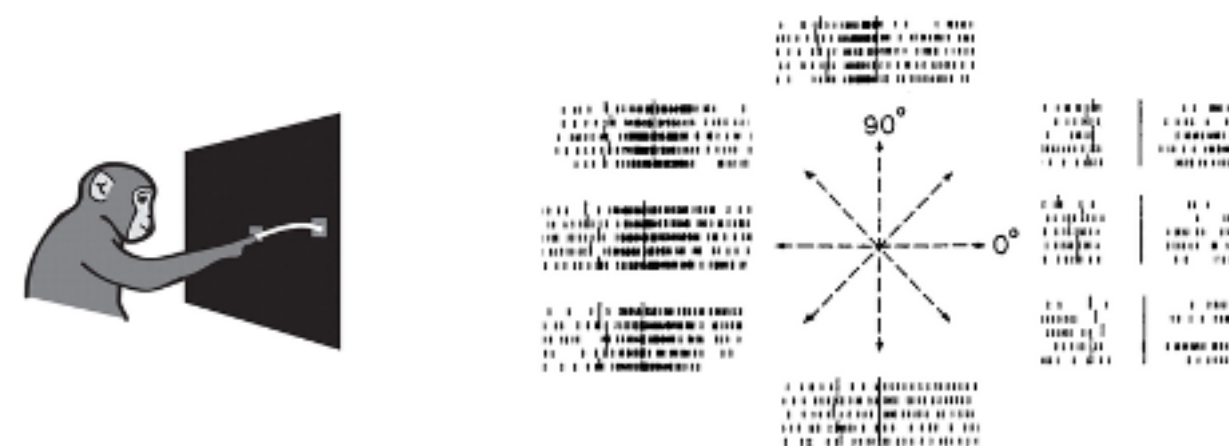
# Signals

## EEG



MNE's overview of MEG/EEG analysis with MNE-Python

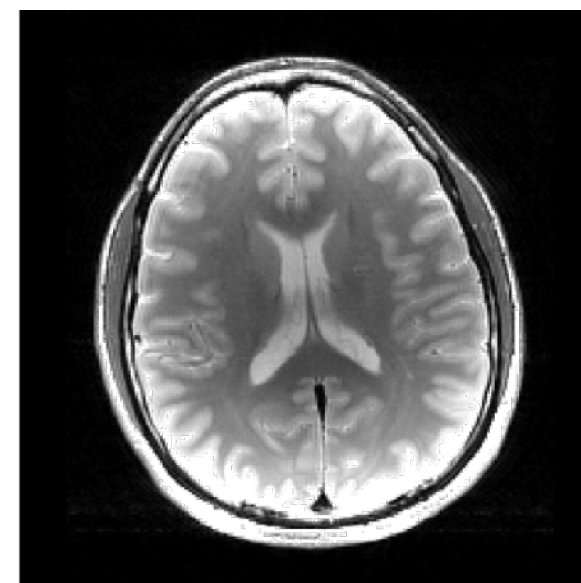
## Neural Spiking



Dayan P and Abbott LF. MIT Press (2005)

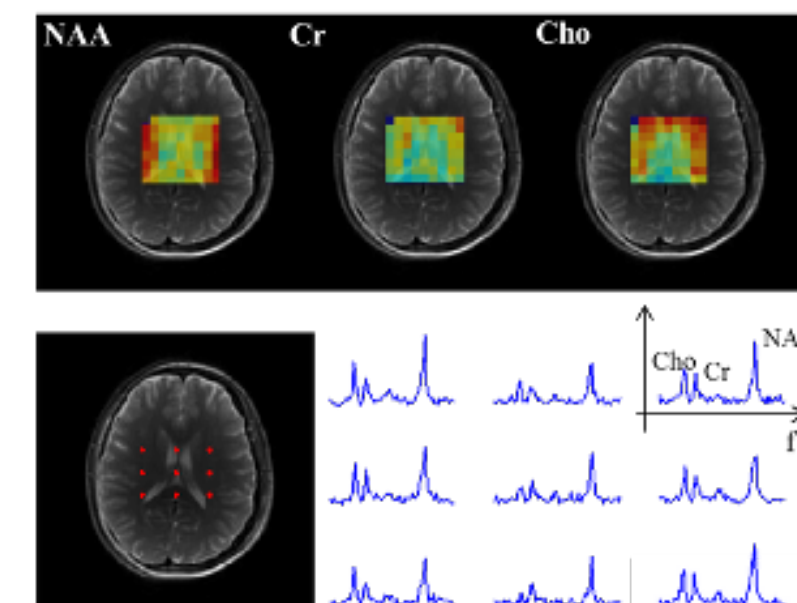
Chestek CA et al. JNeurosci (2007)

## MRI



Chatnuntawech et al. MRI (2016)

## MRSI

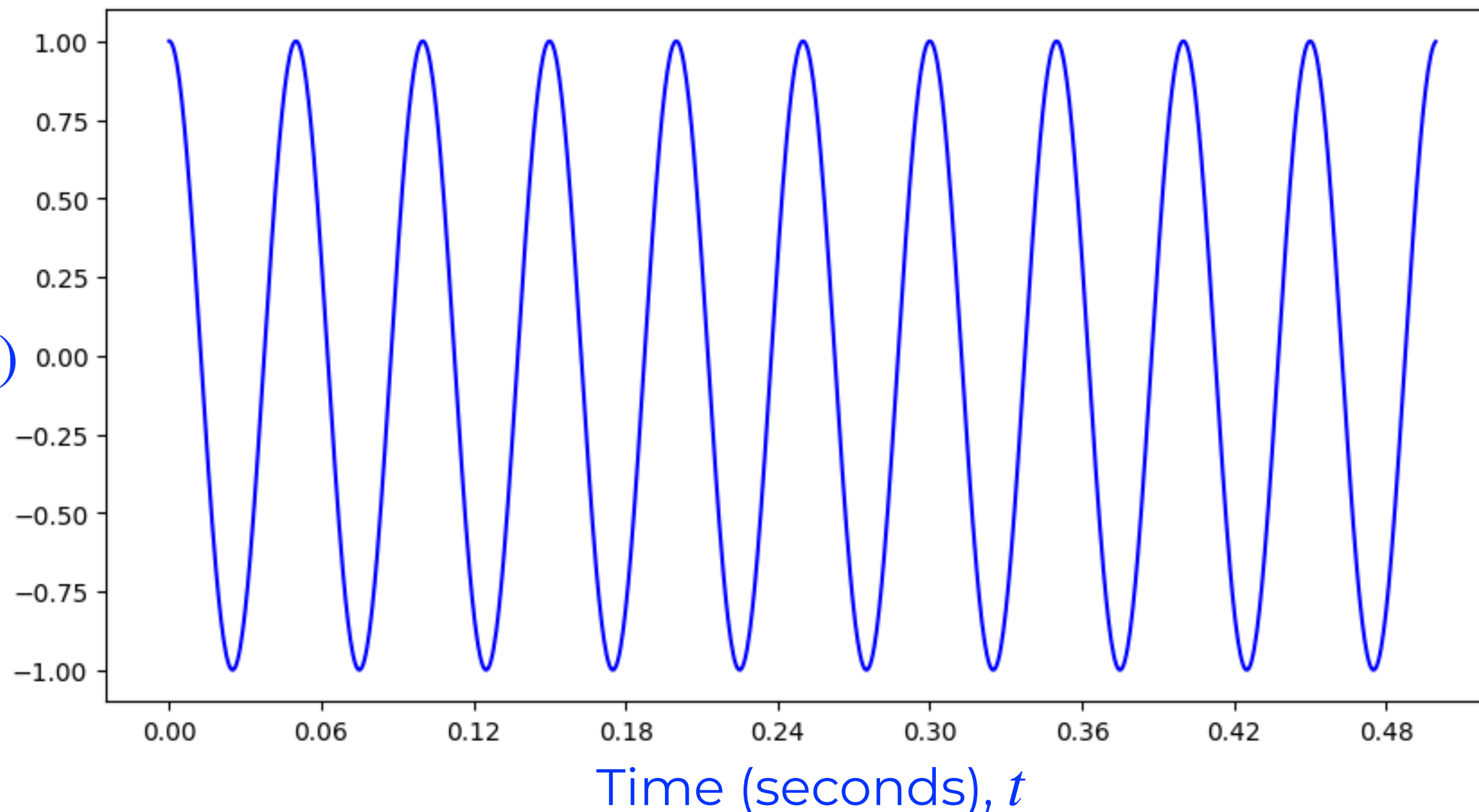


Chatnuntawech et al. MRM (2015)

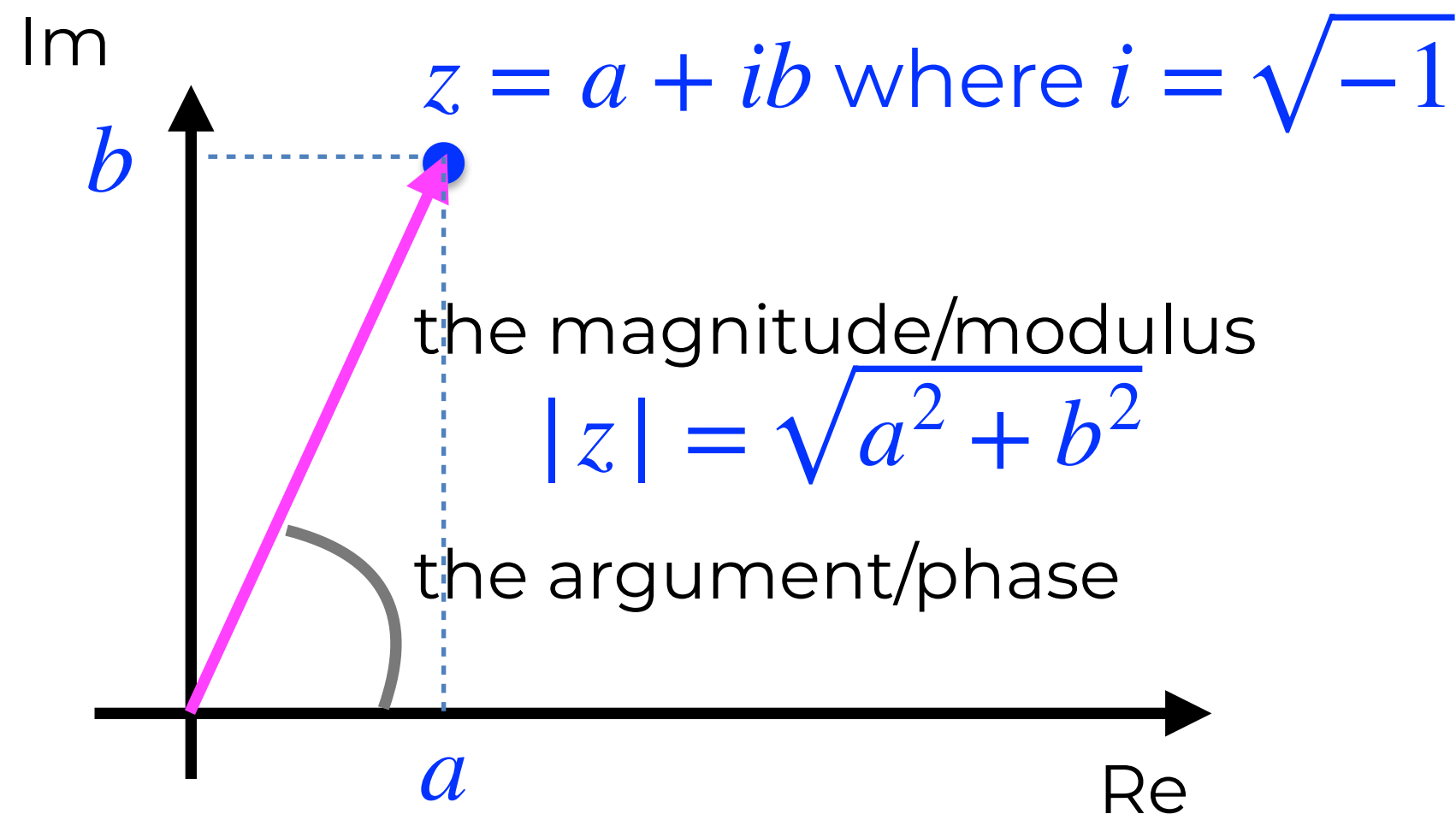
# Signals

Signal - A function of one or more independent variables  
real-valued signal

$$x(t) = \cos(2\pi \times 20t)$$



# Complex-valued Signals



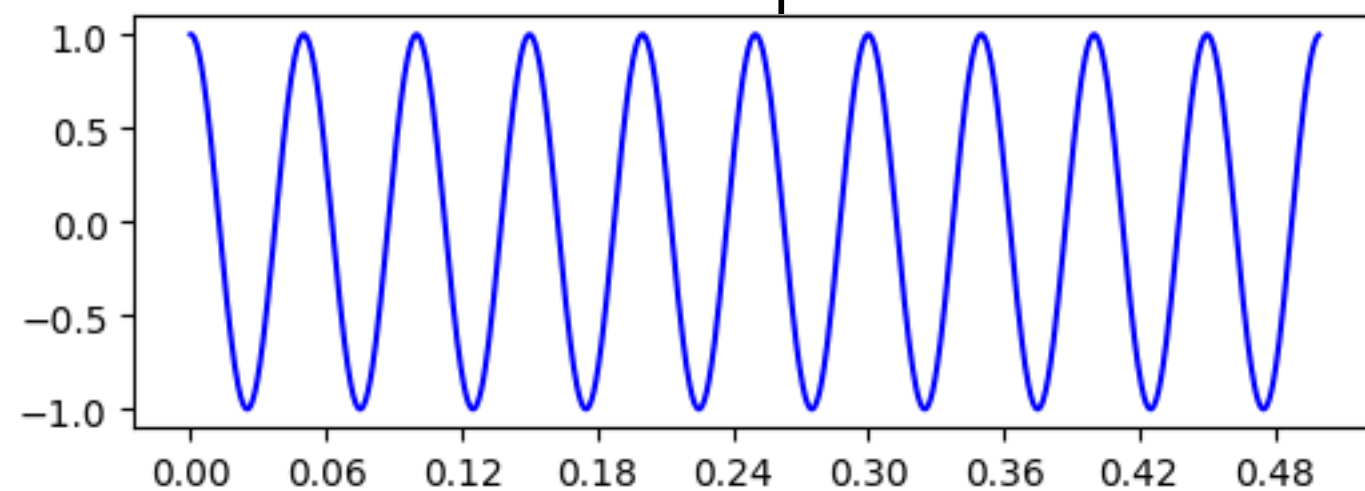
$$z = a + jb \text{ where } j = \sqrt{-1}$$

Electrical and control system engineers use  $j$  instead of  $i$

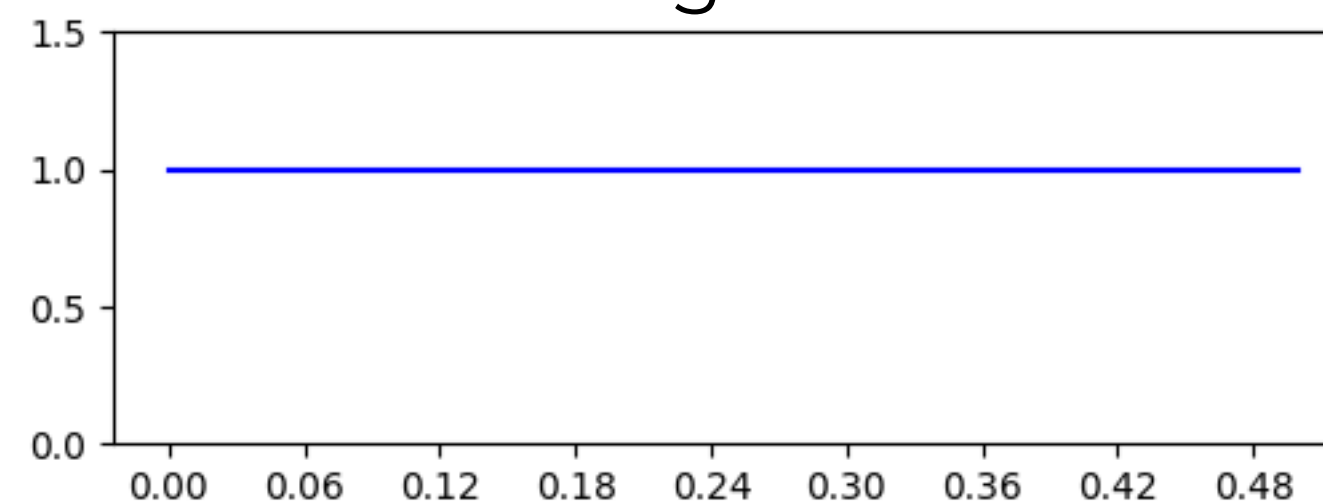
# Complex-valued Signals

$$x(t) = e^{j2\pi \times 20t} = \cos(2\pi \times 20t) + j \sin(2\pi \times 20t)$$

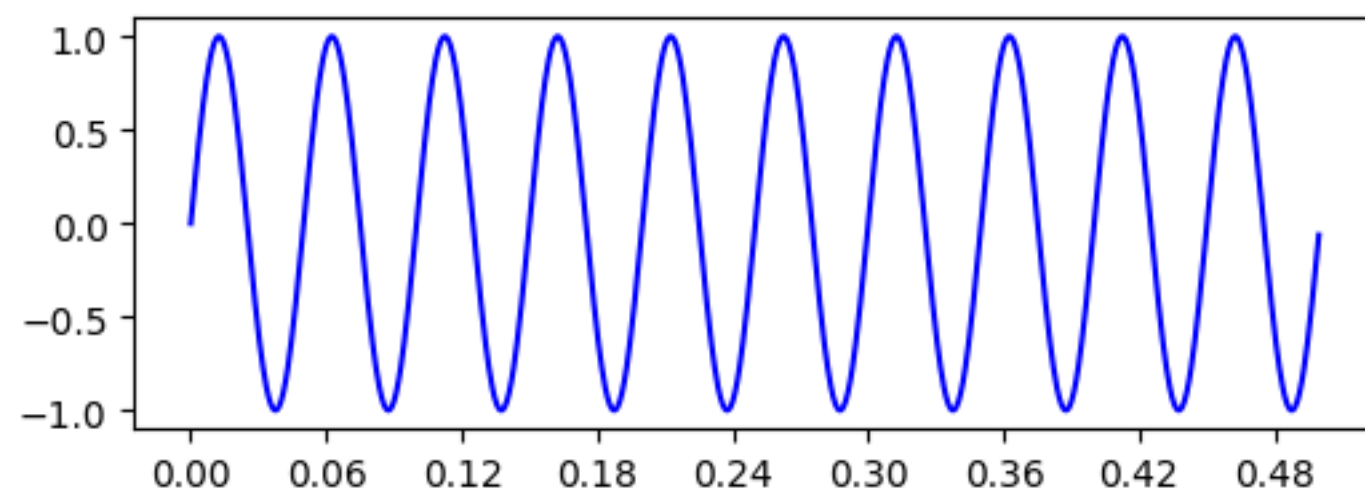
real part



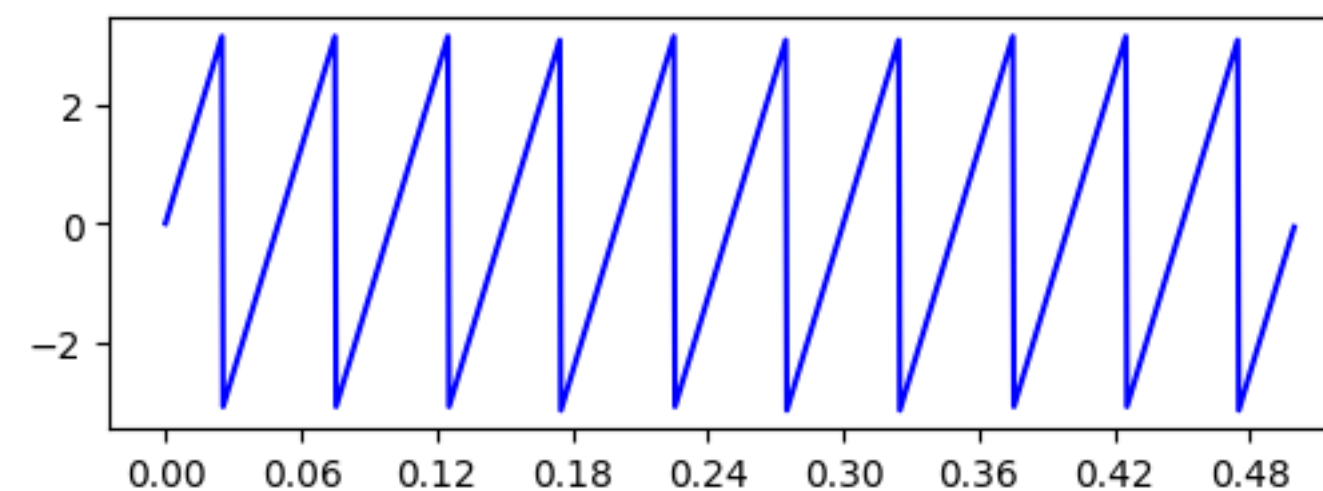
magnitude



imaginary part

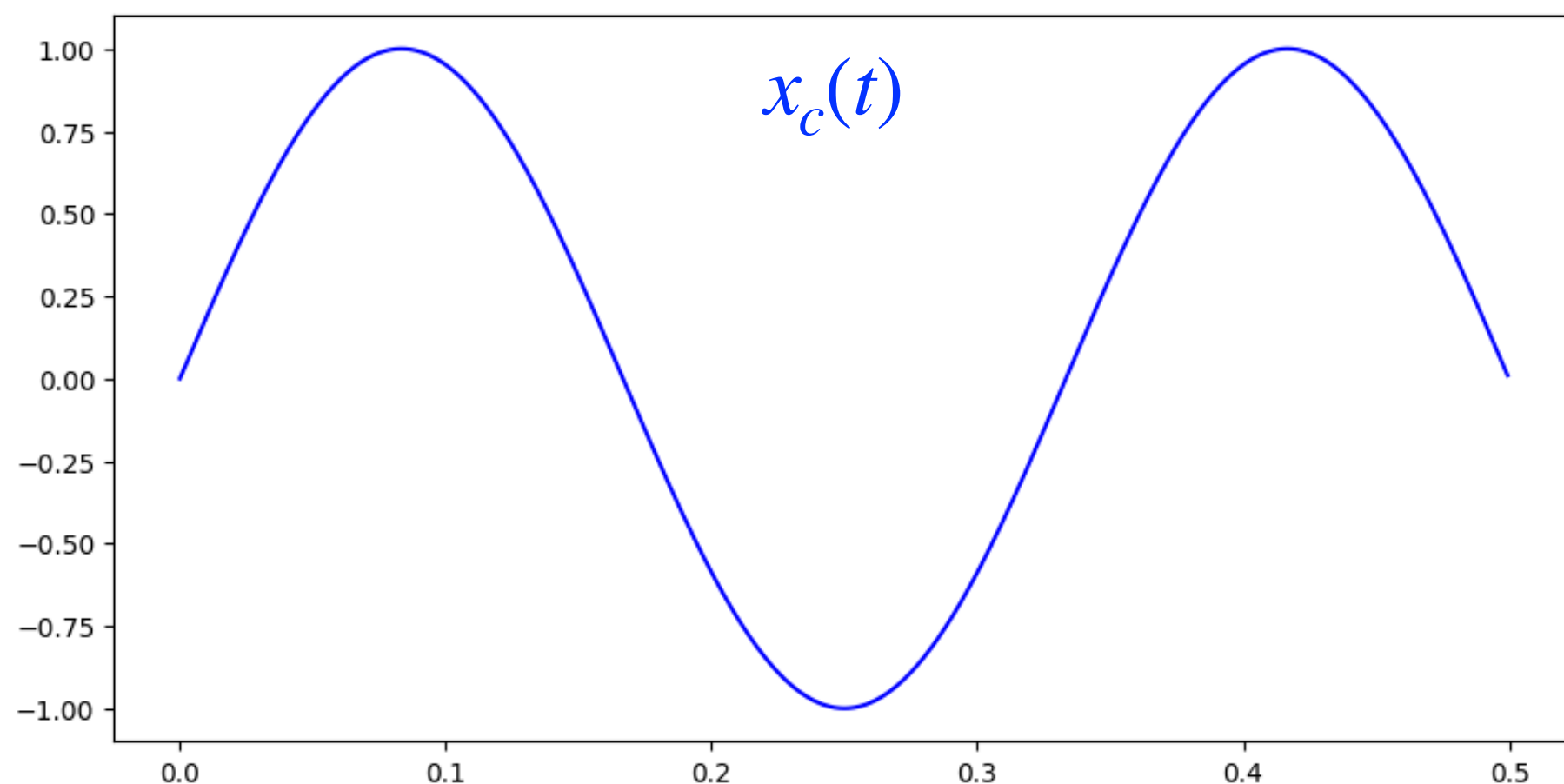


phase



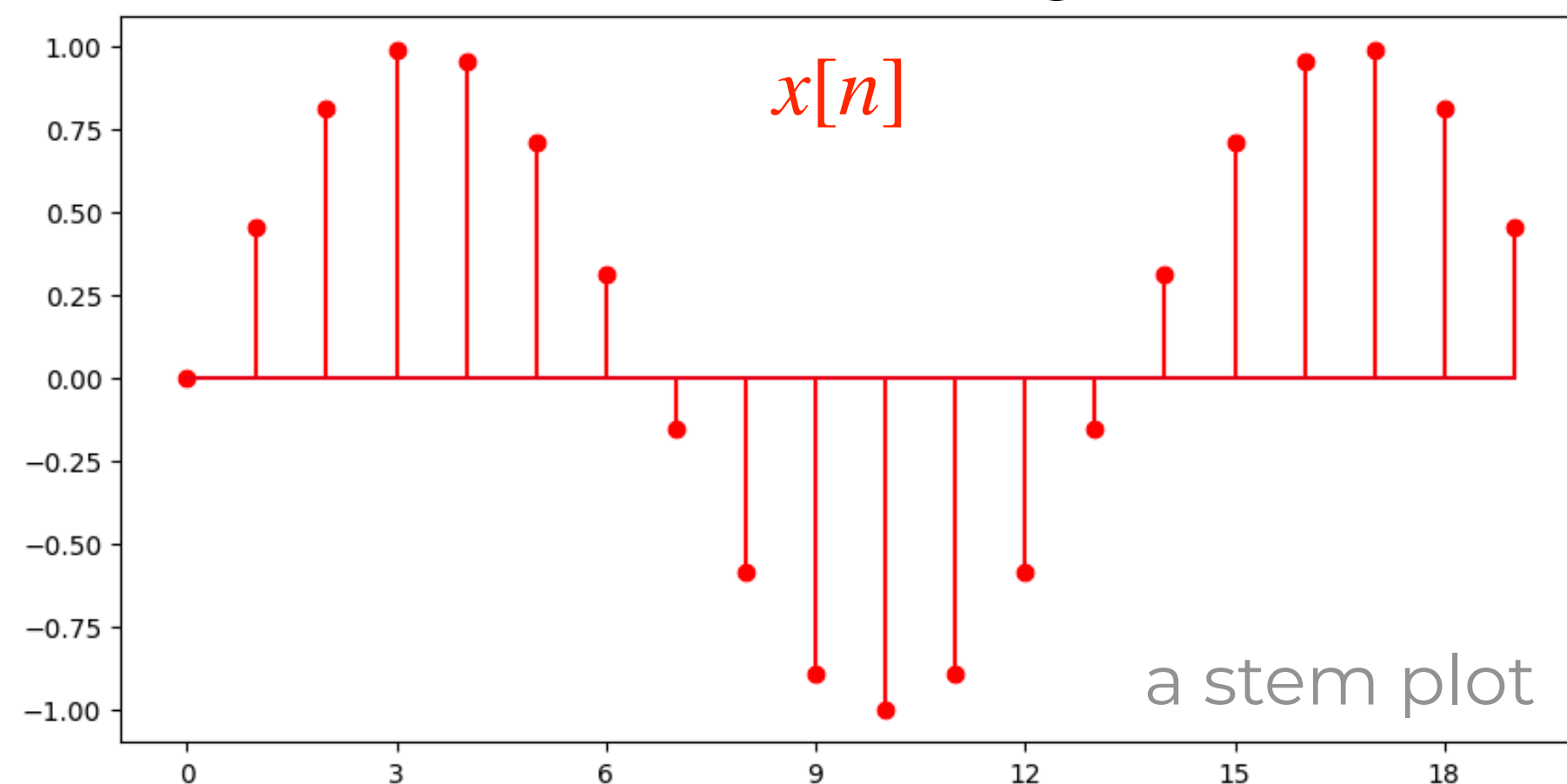
# Continuous- and Discrete-Time Signals

continuous-time signal



continuous independent variable,  $t$

discrete-time signal



integer variable,  $n$

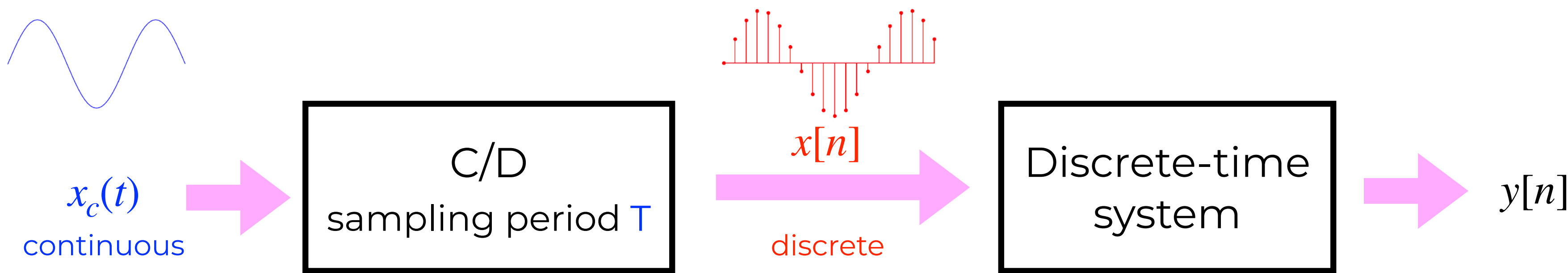
$[0, 0.4540, 0.8090, \dots, 0.8090, 0.4540]$

a sequence of 20 numbers in this case



# Discrete-Time Signal Processing

Many applications make use of discrete-time technology to process signals that started out as continuous-time signals.



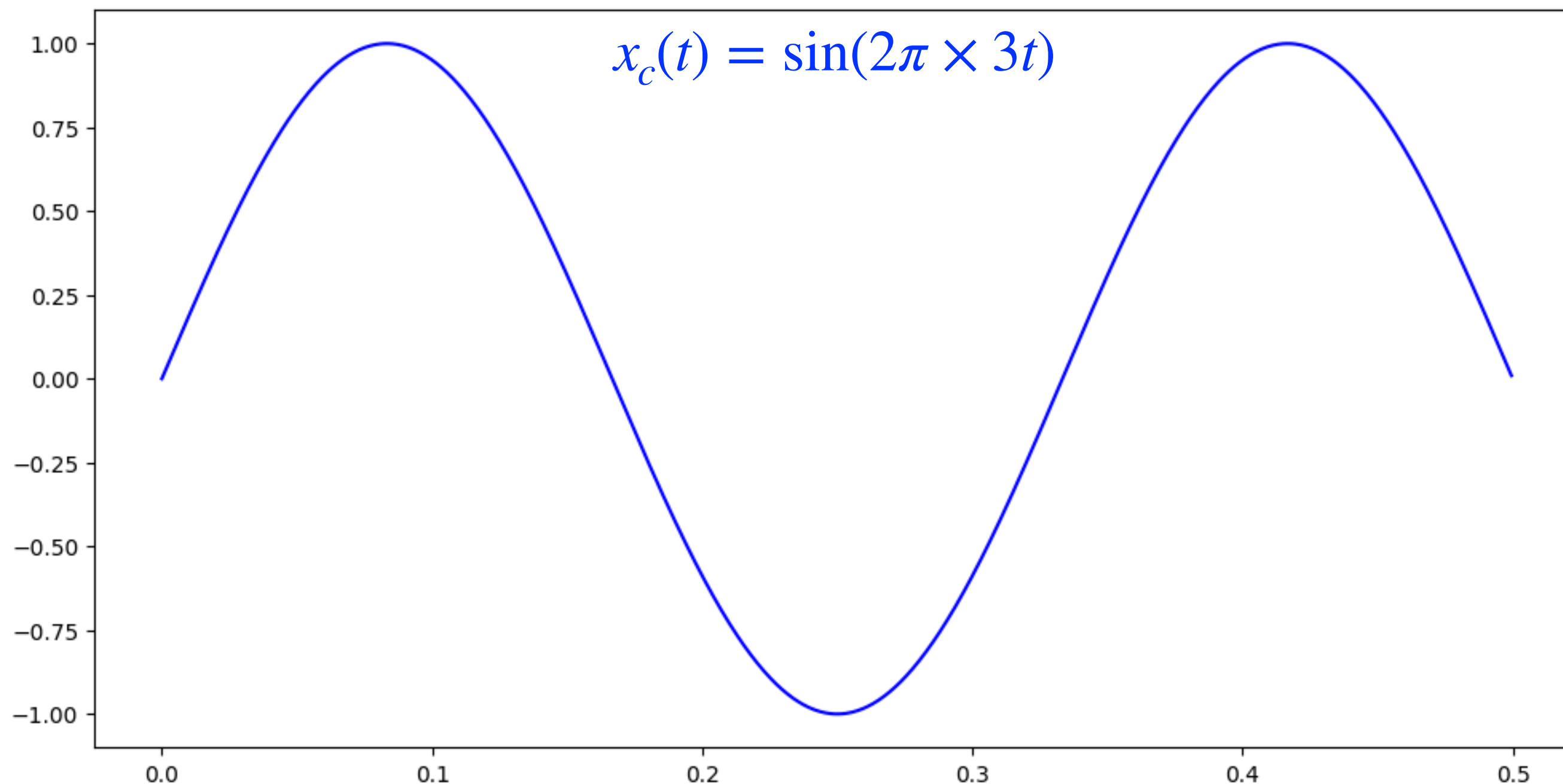
In many contexts, discrete-time signal processing is

- More flexible
- Less expensive
- Programmable
- Easily reproducible

Oppenheim, Alan V. Discrete-time signal processing. Pearson Education India, 1999.

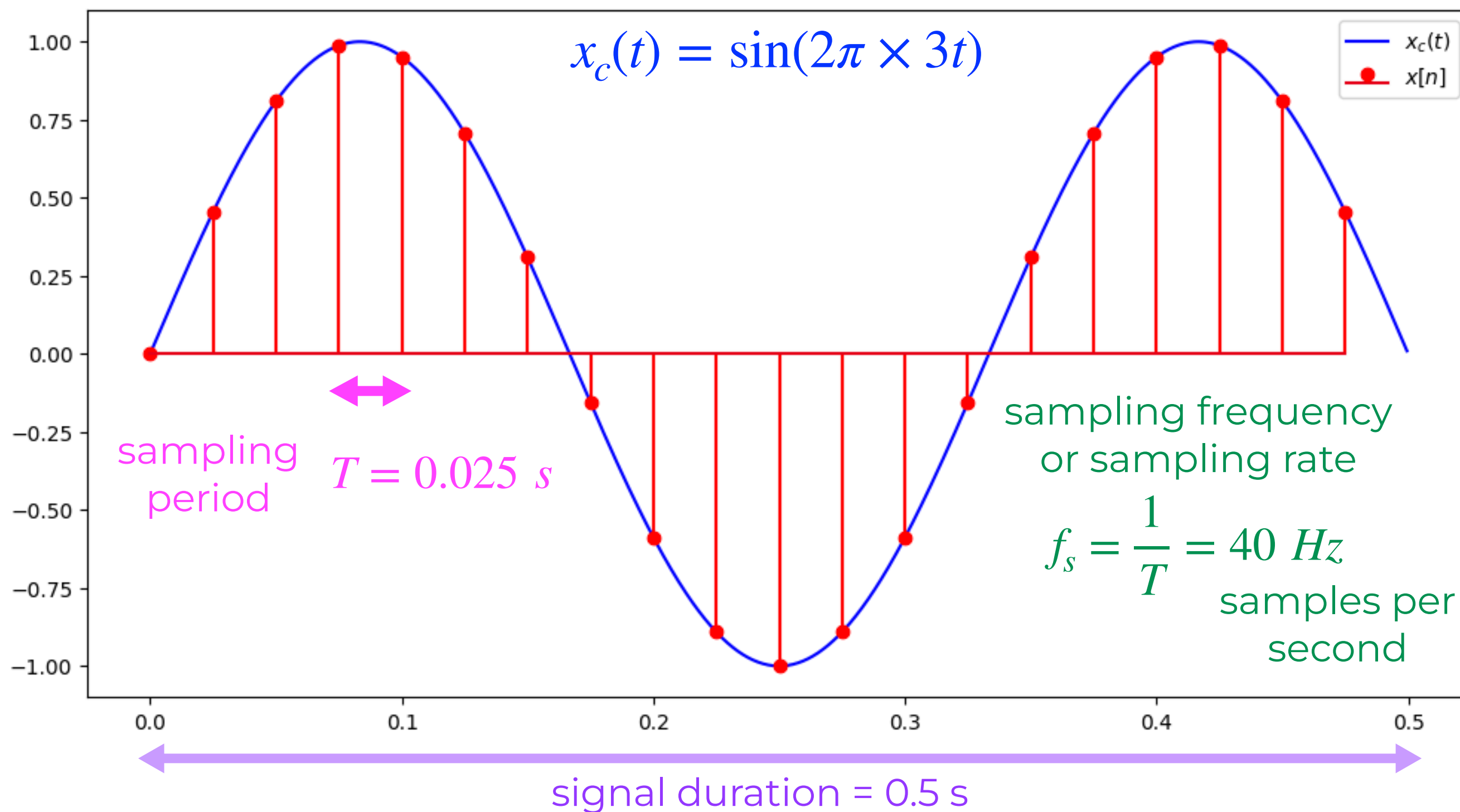
Oppenheim, Alan V., et al. Signals and systems. Vol. 2. Upper Saddle River, NJ: Prentice hall, 1997.

# Sampling of Continuous-Time Signals

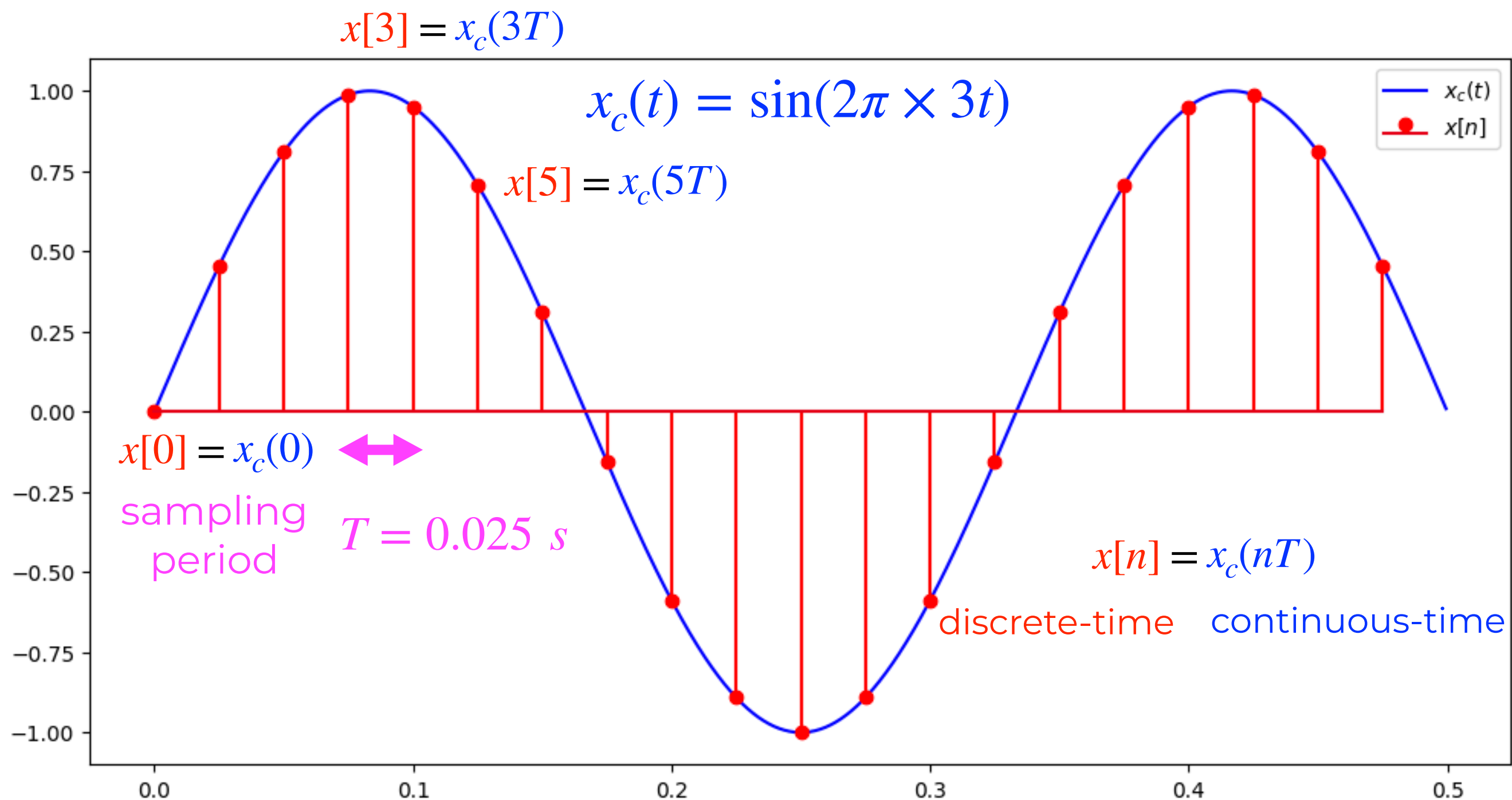




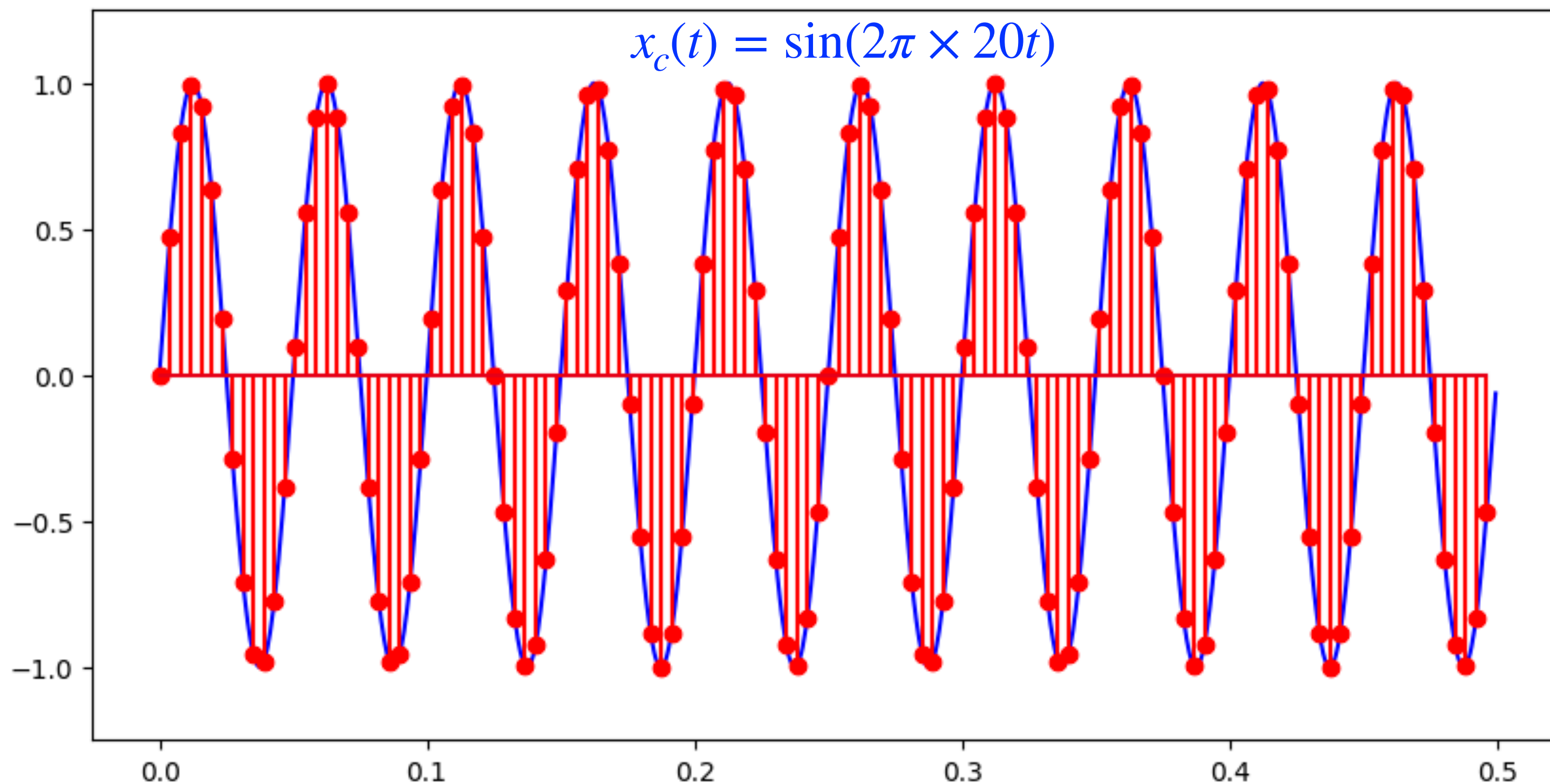
# Sampling of Continuous-Time Signals



# Sampling of Continuous-Time Signals

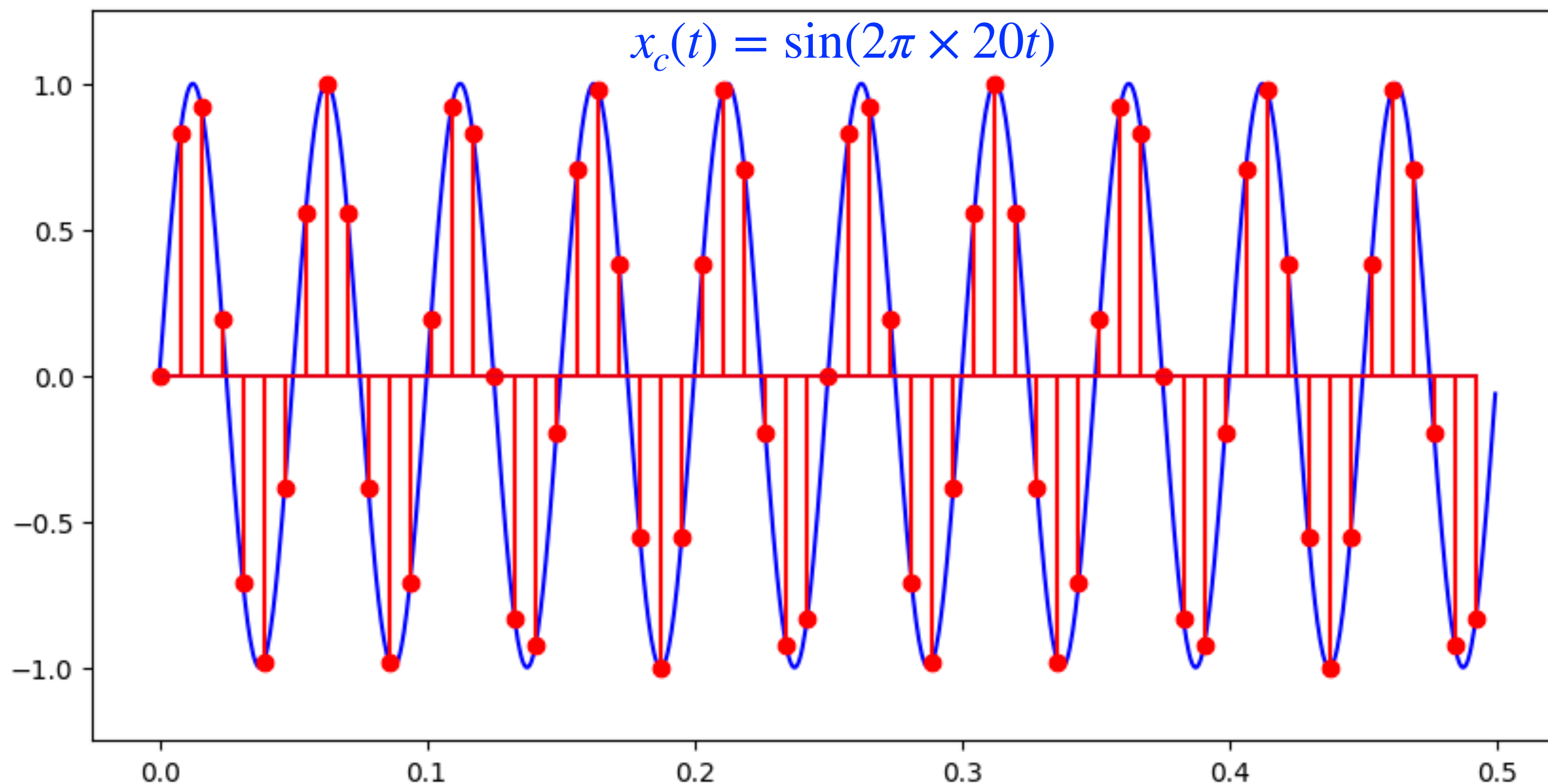


# Sampling Rate



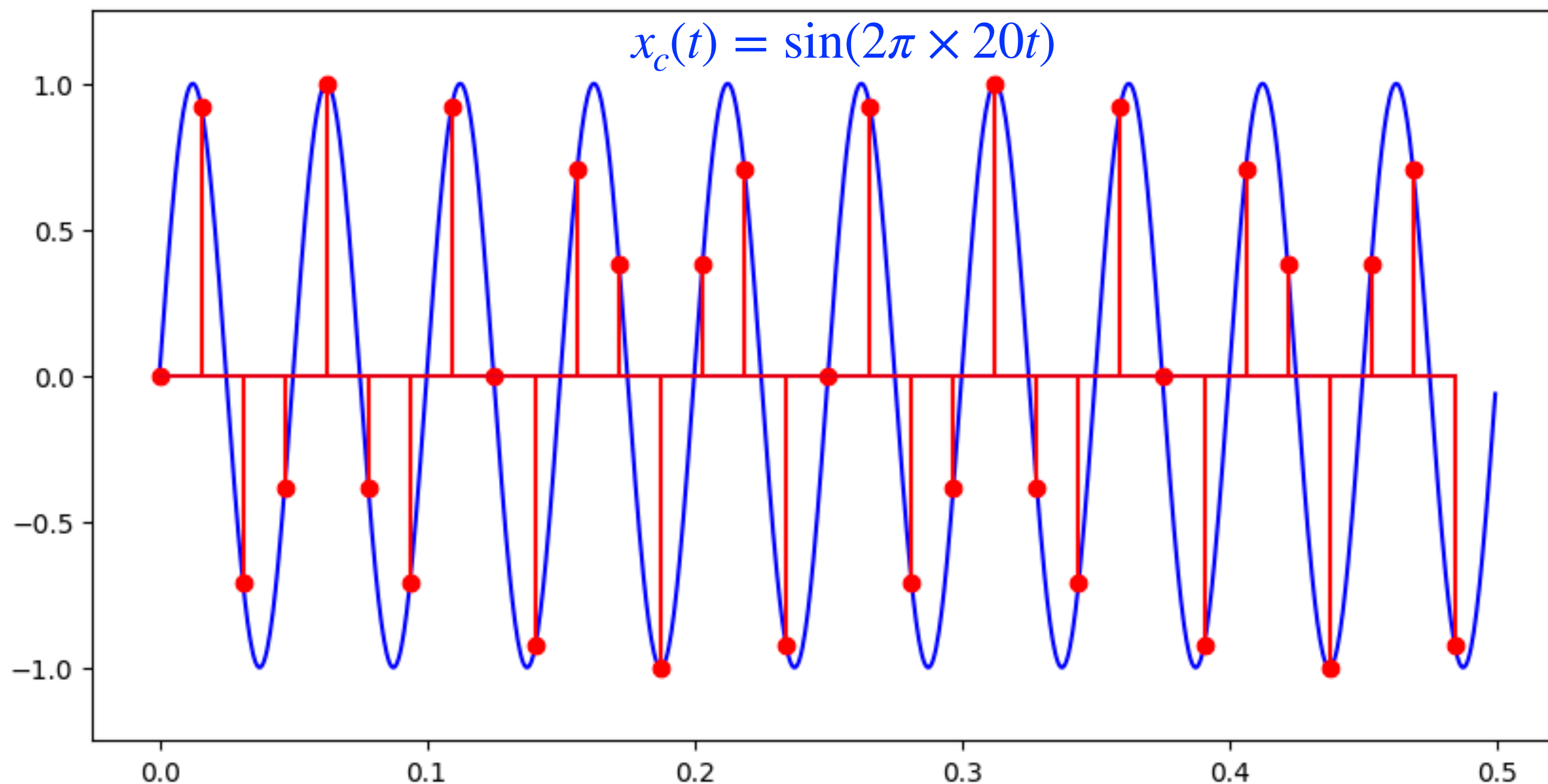
$f_s = 256 \text{ Hz}$   
 $T = 0.004 \text{ s}$   
128 samples

# Sampling Rate



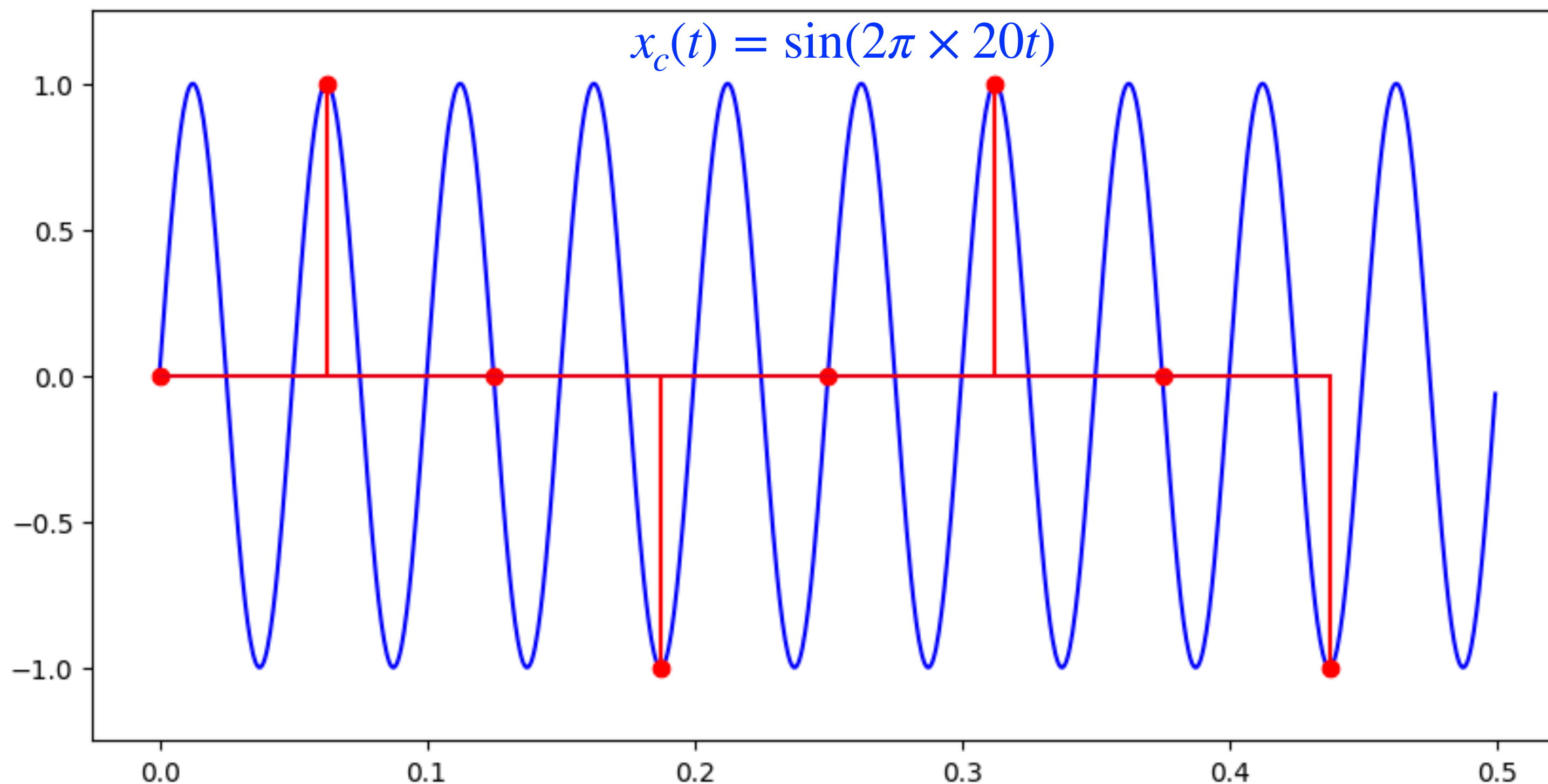
$f_s = 128 \text{ Hz}$   
 $T = 0.008 \text{ s}$   
 64 samples

# Sampling Rate



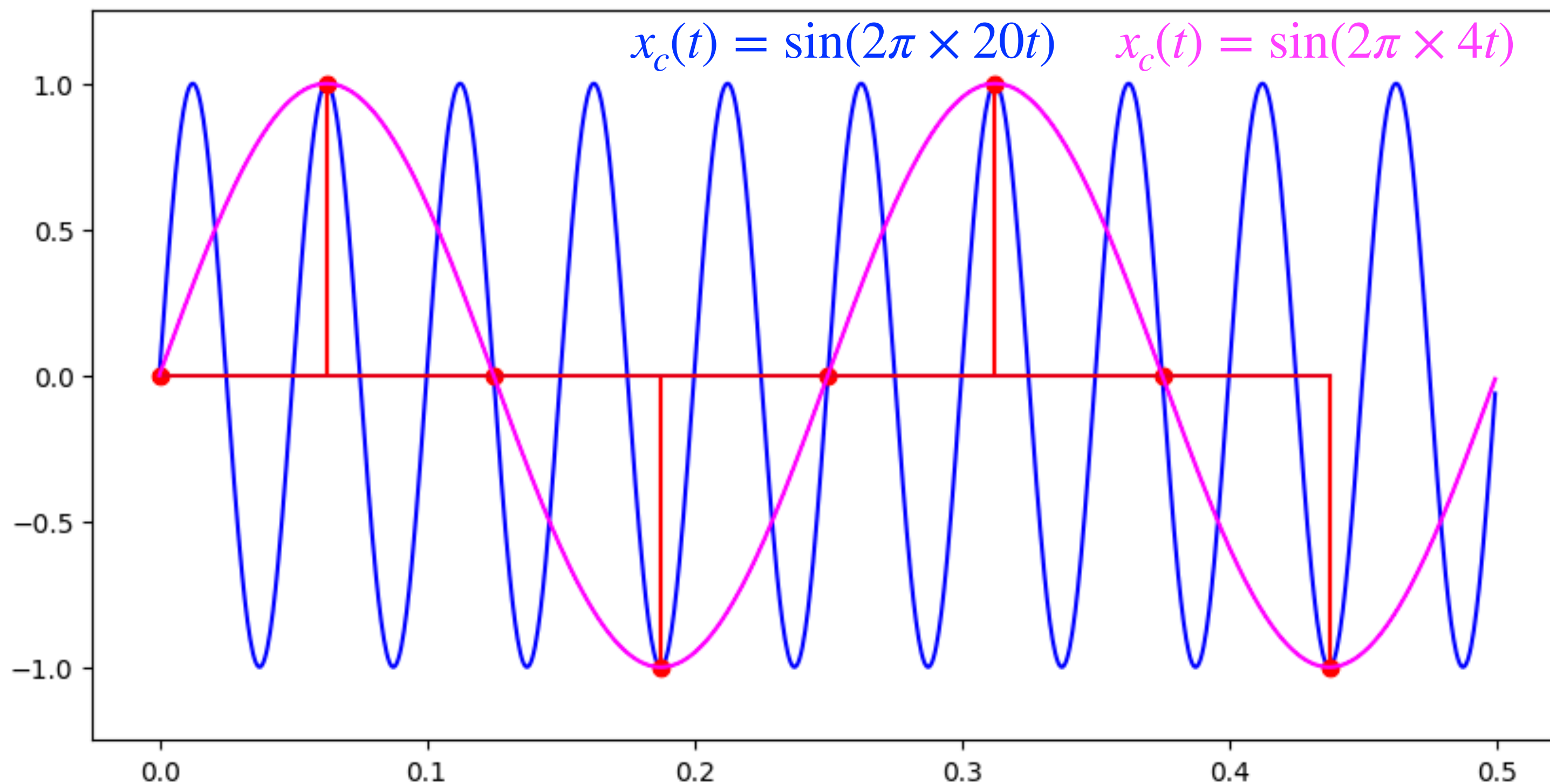
$f_s = 64 \text{ Hz}$   
 $T = 0.016 \text{ s}$   
 32 samples

# Sampling Rate



$f_s = 16 \text{ Hz}$   
 $T = 0.00625 \text{ s}$   
 8 samples

# Sampling Rate



$f_s = 16 \text{ Hz}$   
 $T = 0.00625 \text{ s}$   
 8 samples



# The Sampling Theorem

## Communication in the Presence of Noise\*

CLAUDE E. SHANNON†, MEMBER, IRE

**THEOREM 1:** *If a function  $f(t)$  contains no frequencies higher than  $W$  cps, it is completely determined by giving its ordinates at a series of points spaced  $1/2W$  seconds apart.*

If a function  $x_c(t)$  contains no frequencies higher than  $W$  Hz, then it can be completely determined from  $x[n] = x_c(nT)$  if  $T < \frac{1}{2W}$ .

$$f_s = \frac{1}{T} > 2W$$

The Nyquist rate -  $2W$

The Nyquist frequency -  $W$

