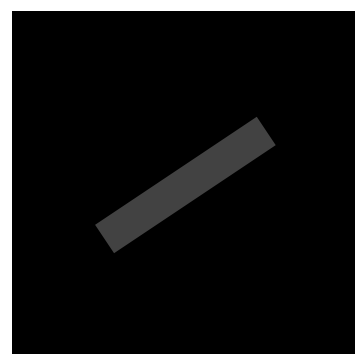


# Simple Linear Models

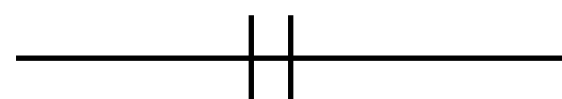
Itthi Chatnuntawech

# Spike Count Prediction

Contrast 1



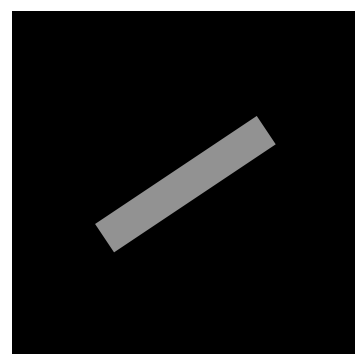
spike trains



spike count

2

Contrast 2



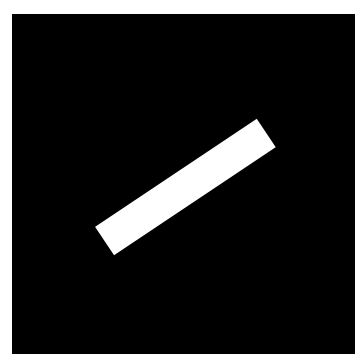
9

⋮

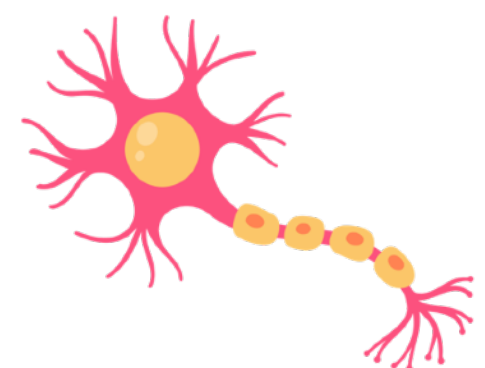
⋮

⋮

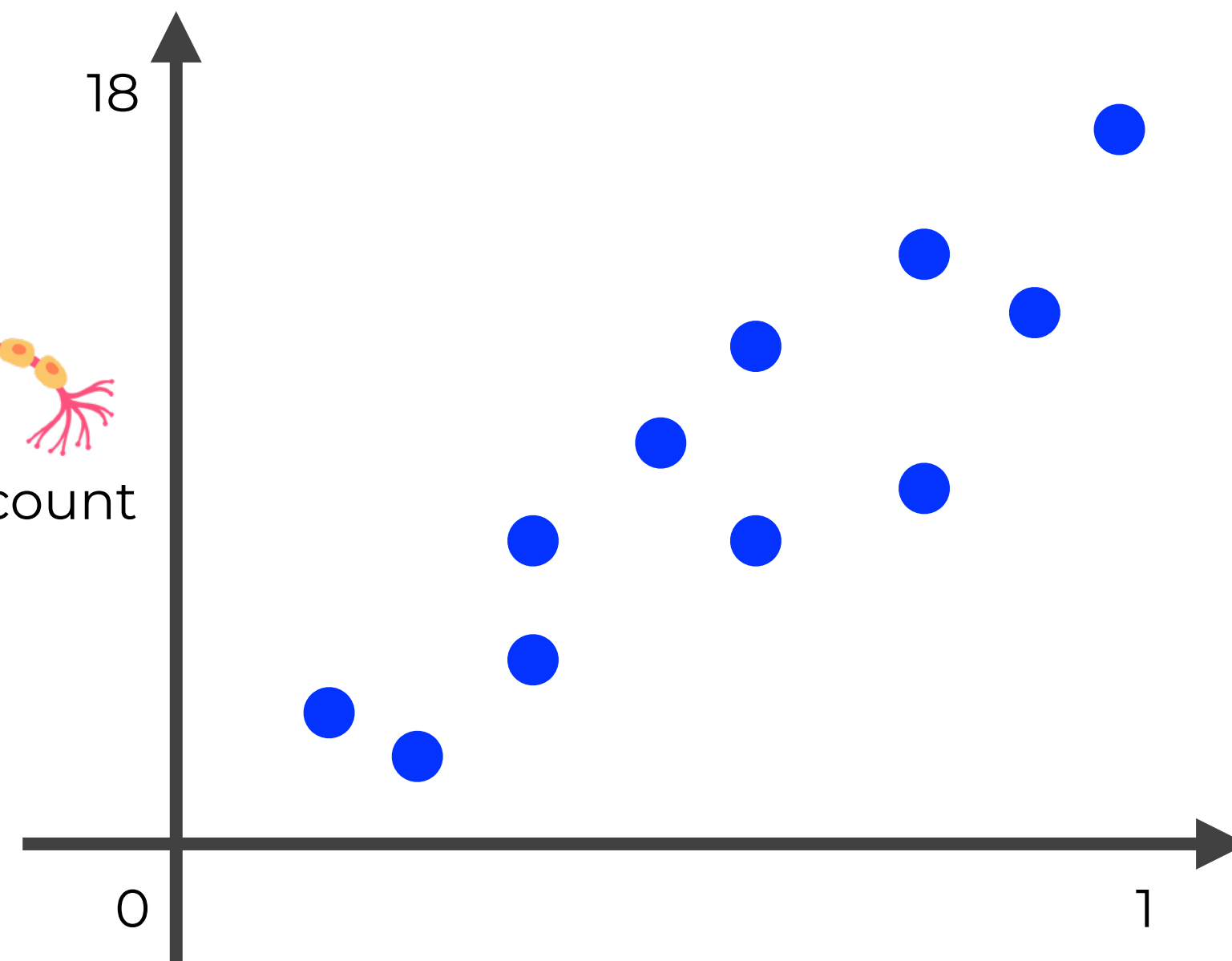
Contrast n



18



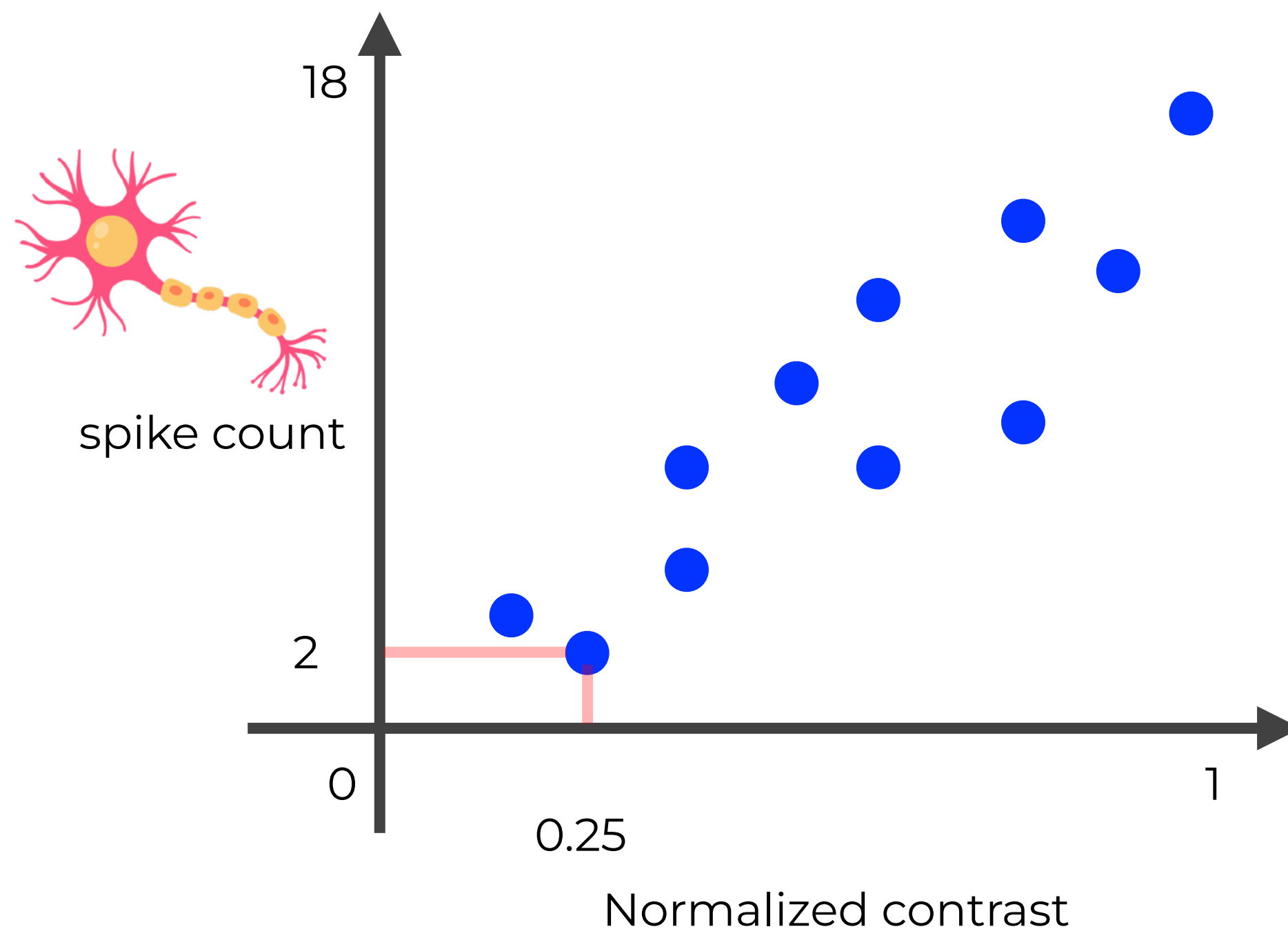
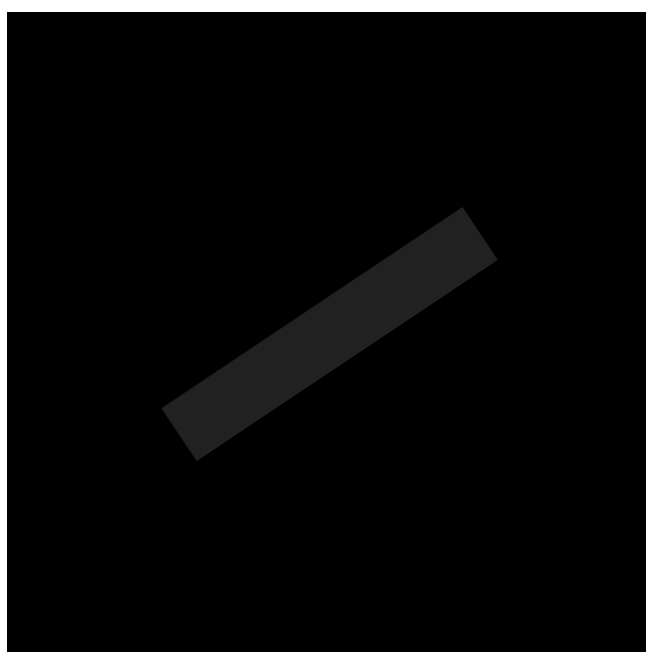
spike count



Normalized contrast

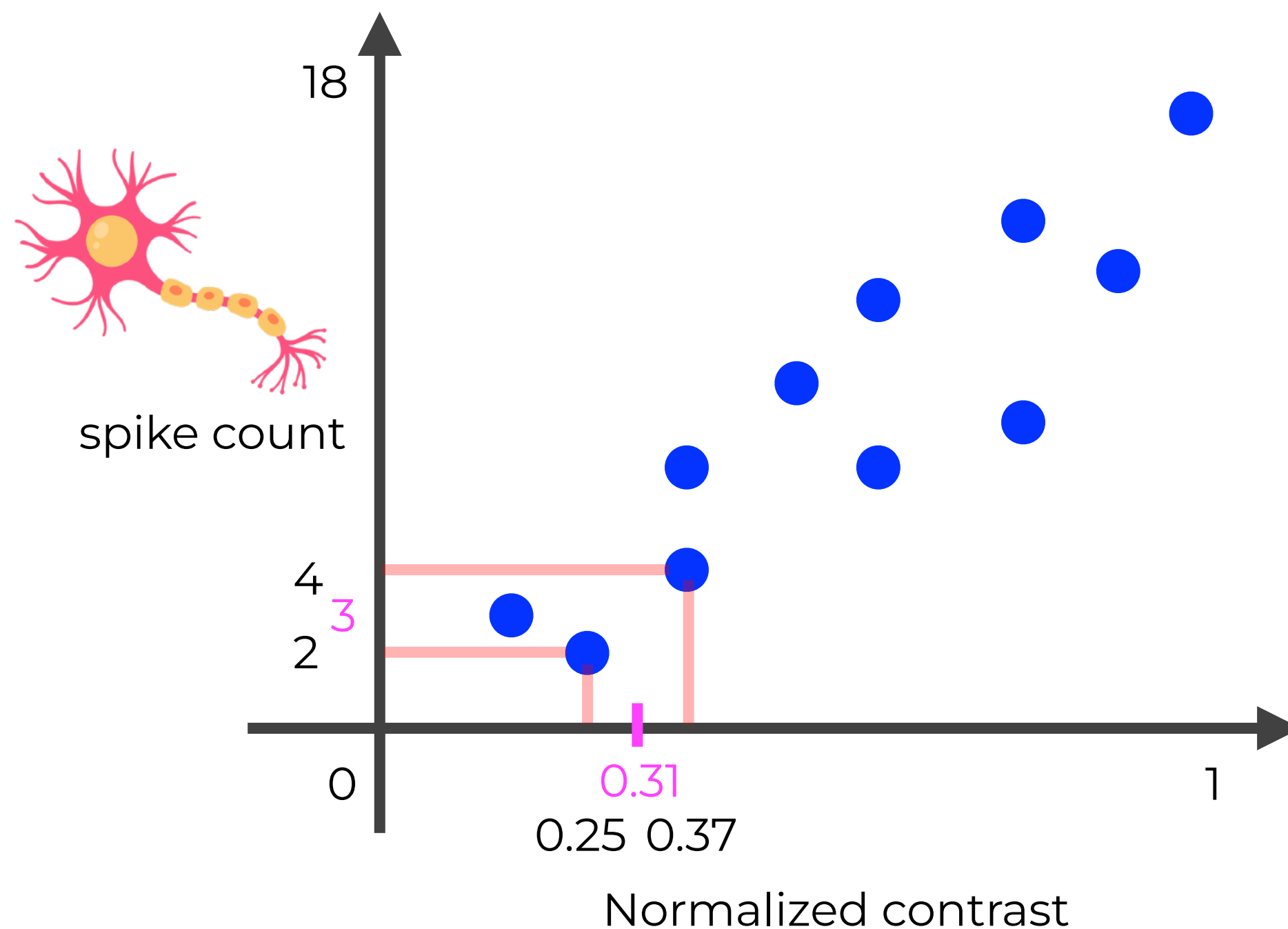
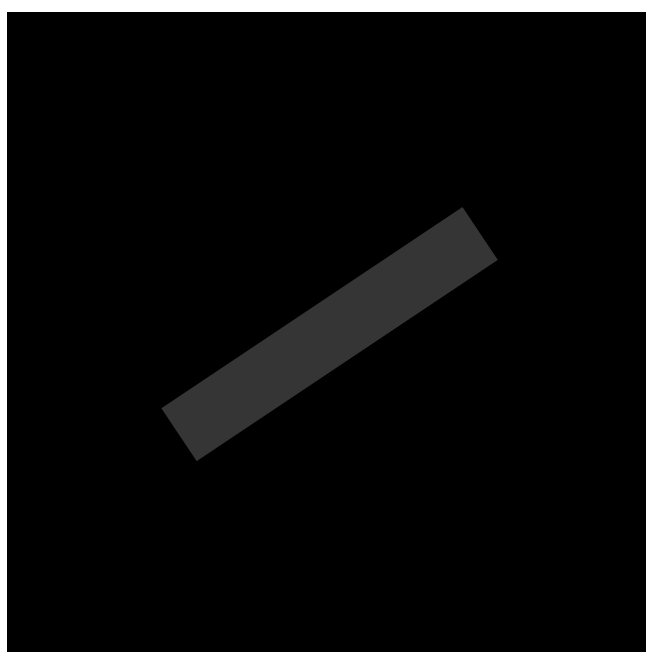
# Spike Count Prediction

Normalized contrast = 0.25



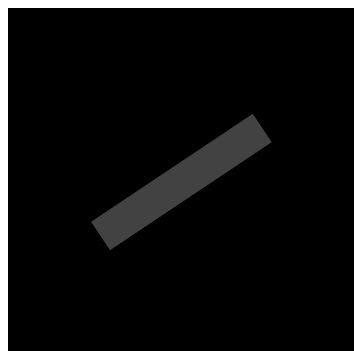
# Spike Count Prediction

Normalized contrast = 0.31

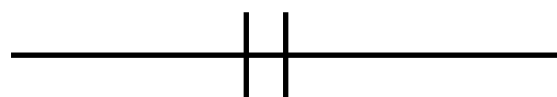


# Spike Count Prediction

Contrast 1



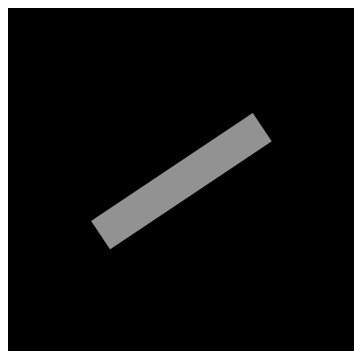
spike trains



spike count

2

Contrast 2



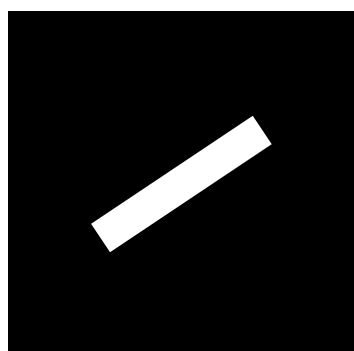
9

⋮

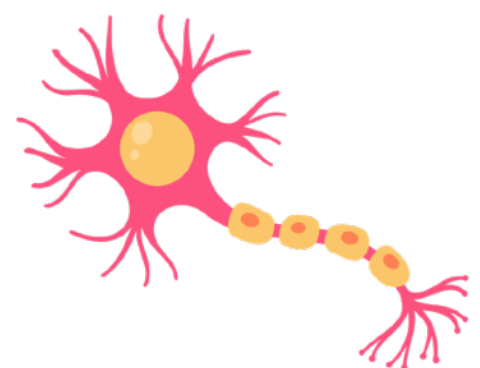
⋮

⋮

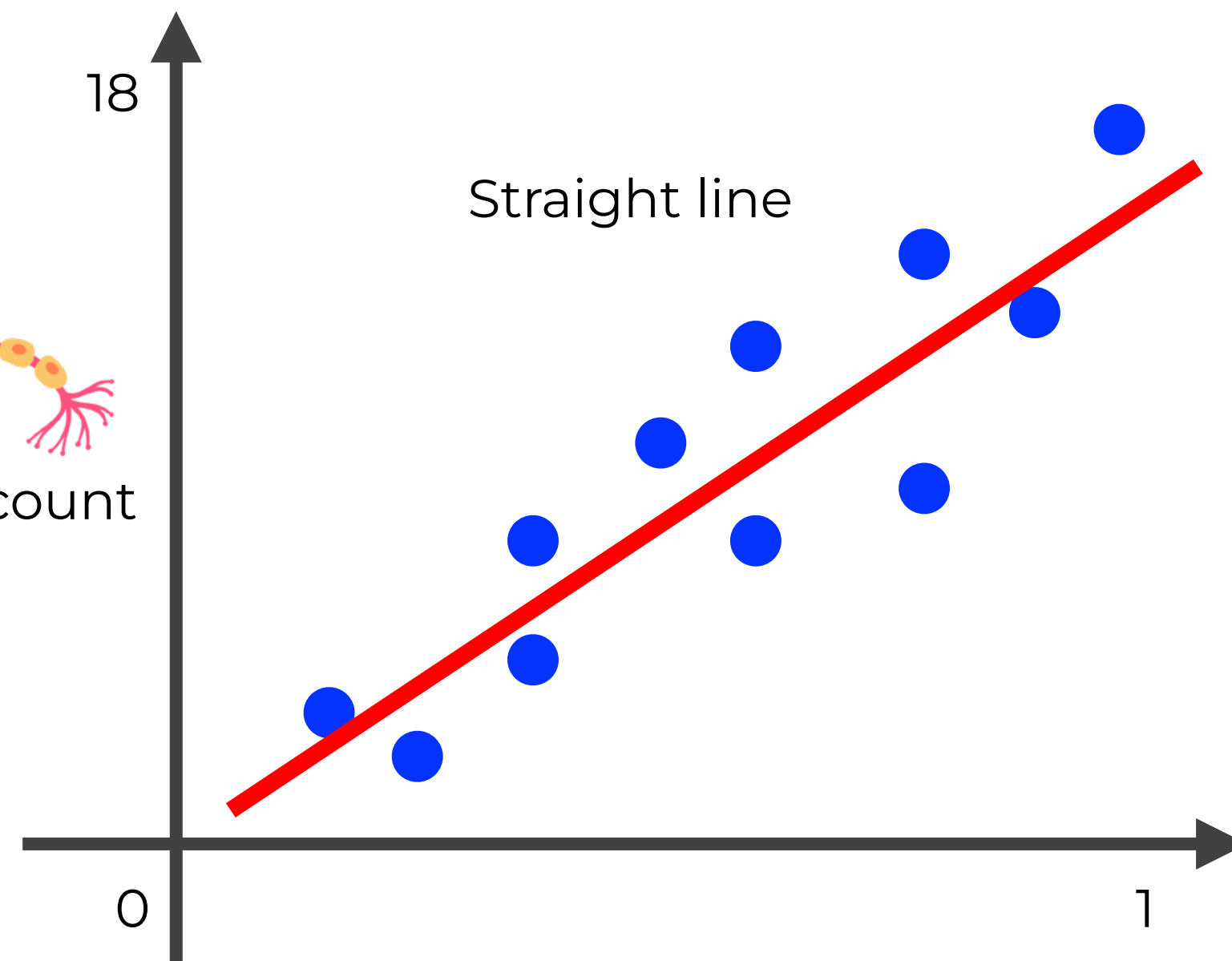
Contrast n



18



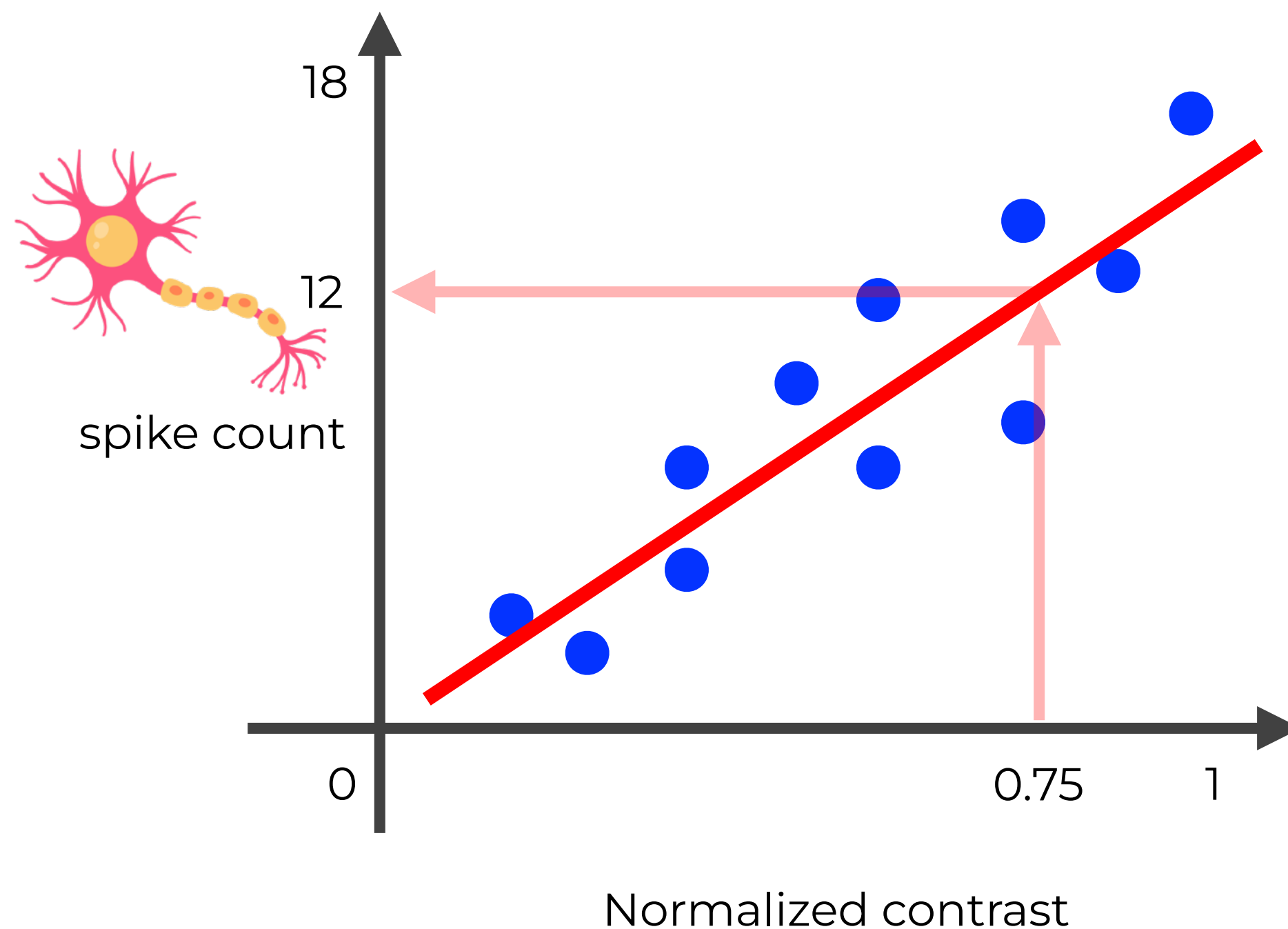
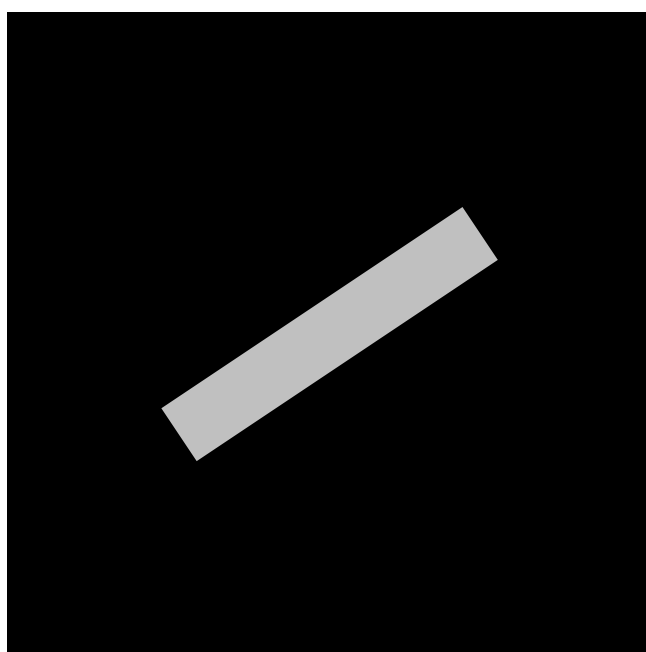
spike count



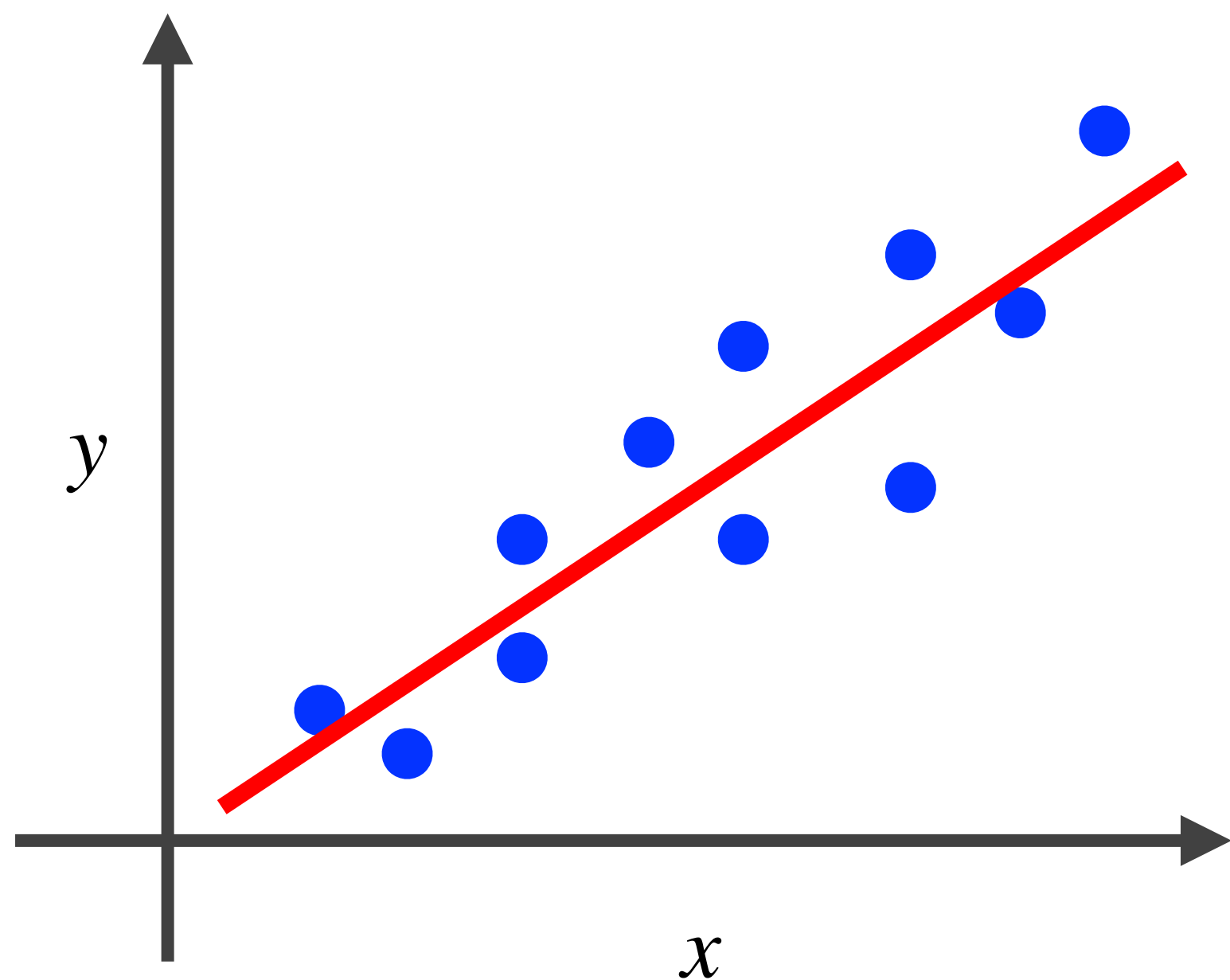
Normalized contrast

# Spike Count Prediction

Normalized contrast = 0.75



# Linear Model



$$y = mx + c$$

$m$ : slope

$c$ : y-intercept

2 parameters

$$y = w_0 + w_1x$$

$w_1$ : slope

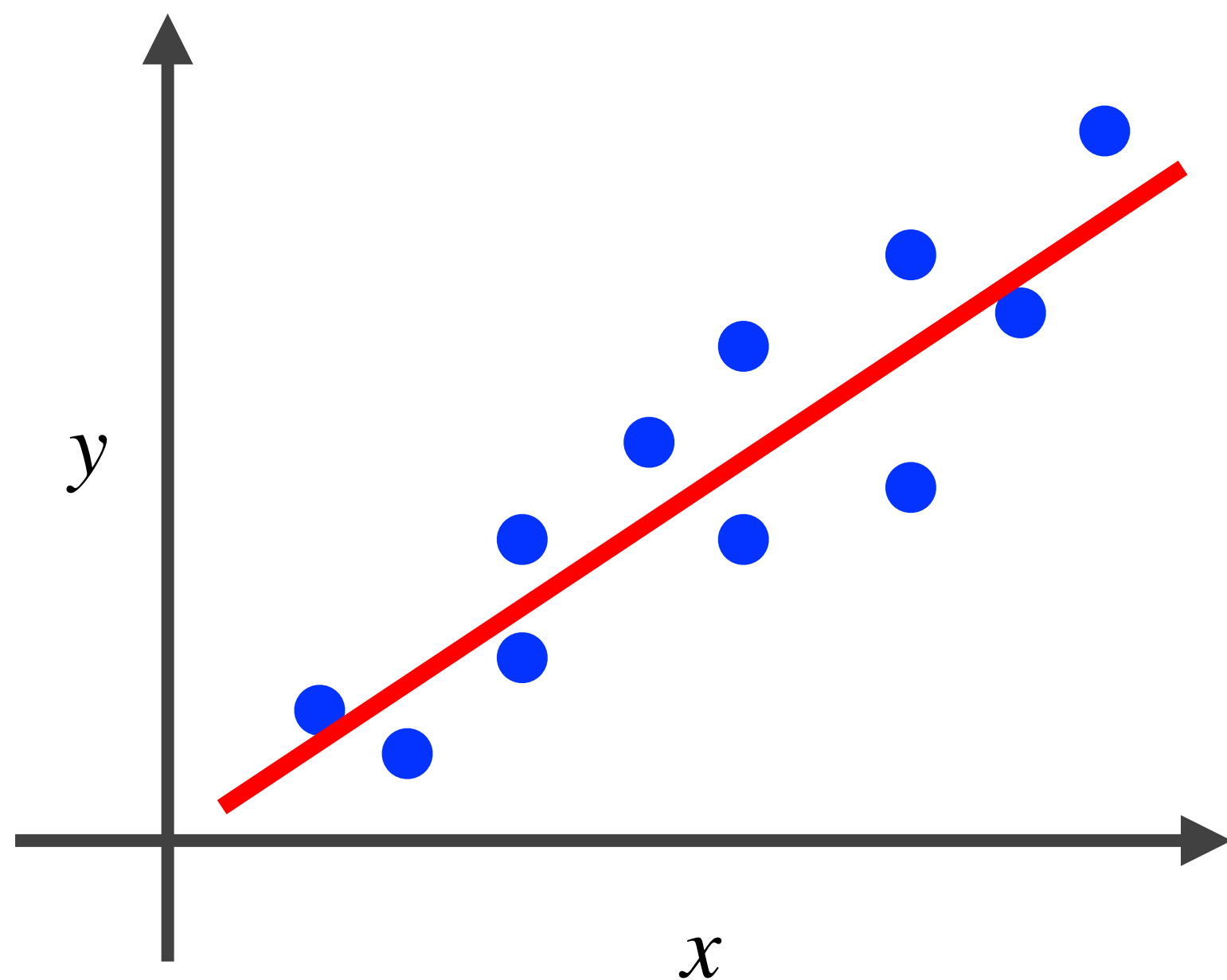
$w_0$ : y-intercept

2 parameters

Higher dimensions

$$y = w_0 + w_1x_1 + w_2x_2 + w_3x_3 + \dots + w_px_p$$

# Linear Model



$$y = w_0 + w_1x$$

$w_1$ : slope

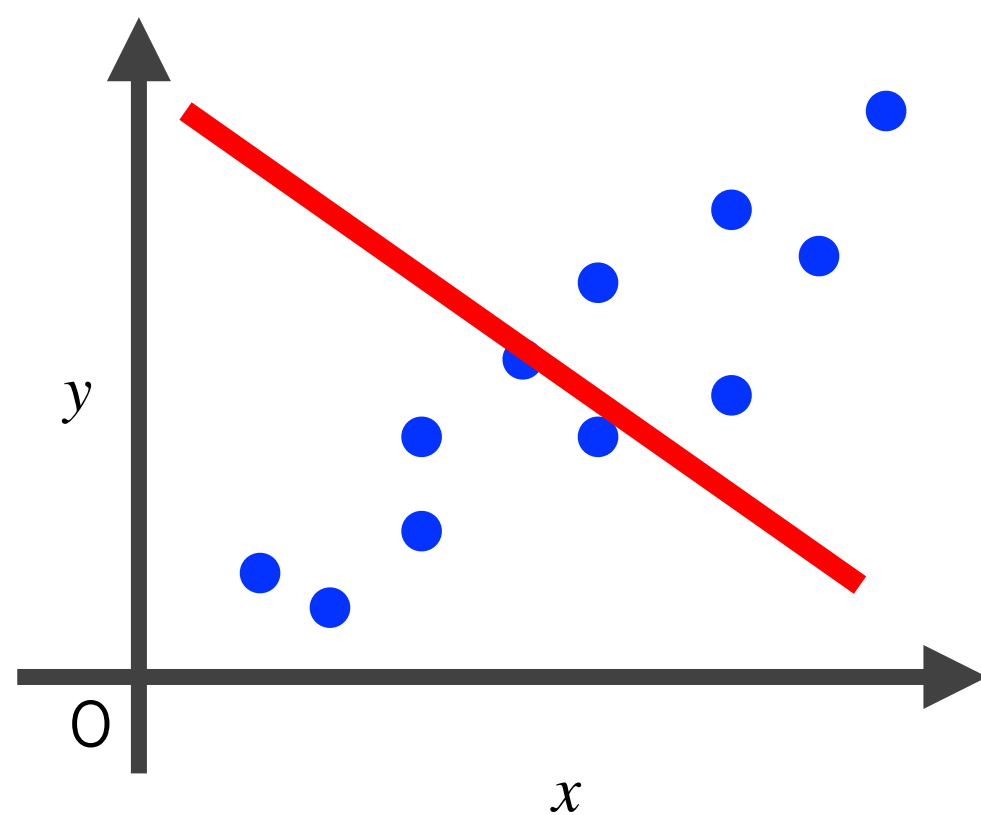
$w_0$ : y-intercept

2 parameters



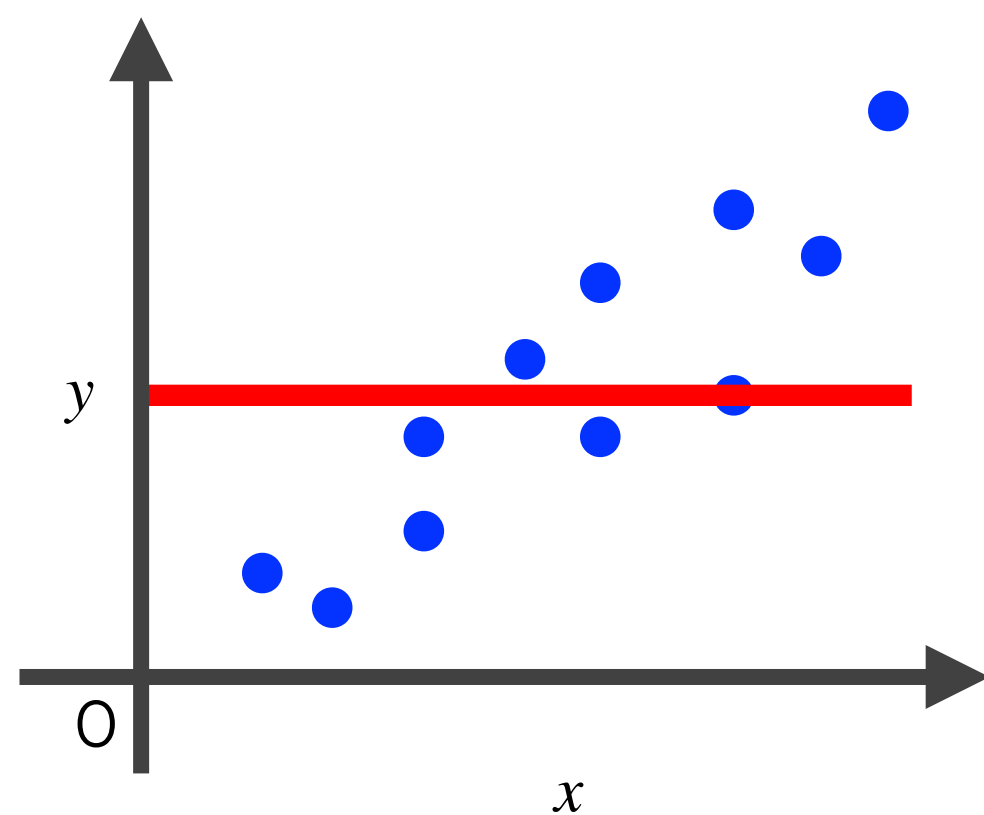
# Linear Model

$$y = w_0 + w_1x$$



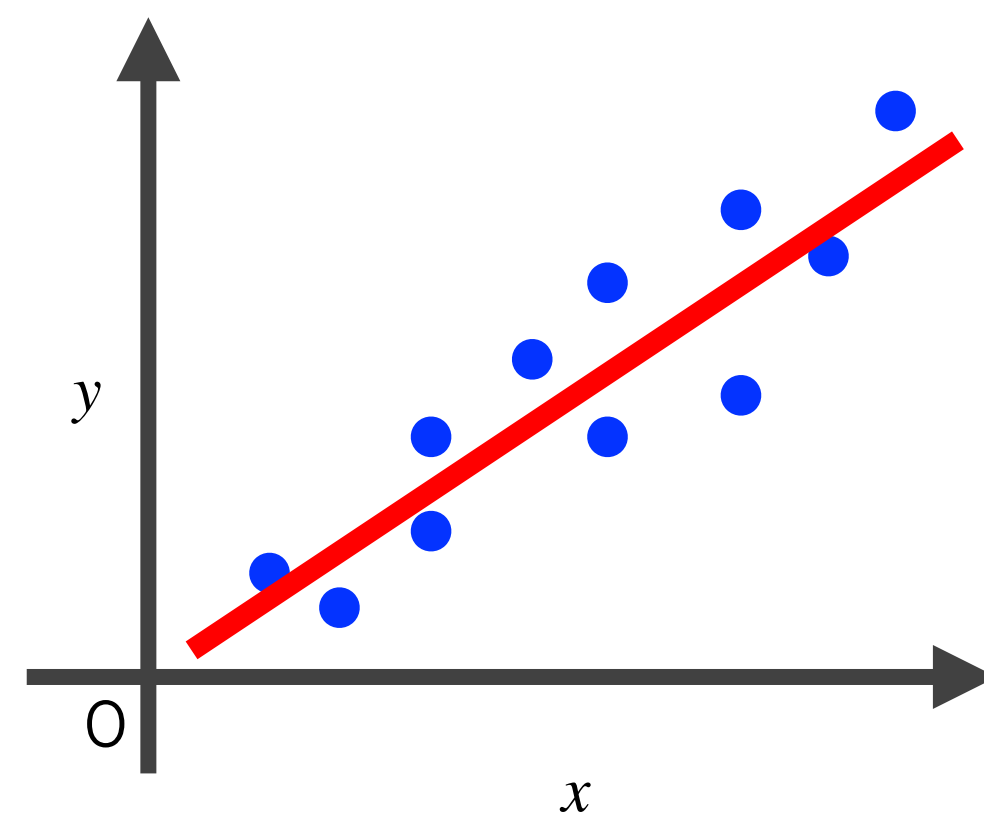
$$w_1 < 0$$

$$w_0 > 0$$



$$w_1 = 0$$

$$w_0 > 0$$

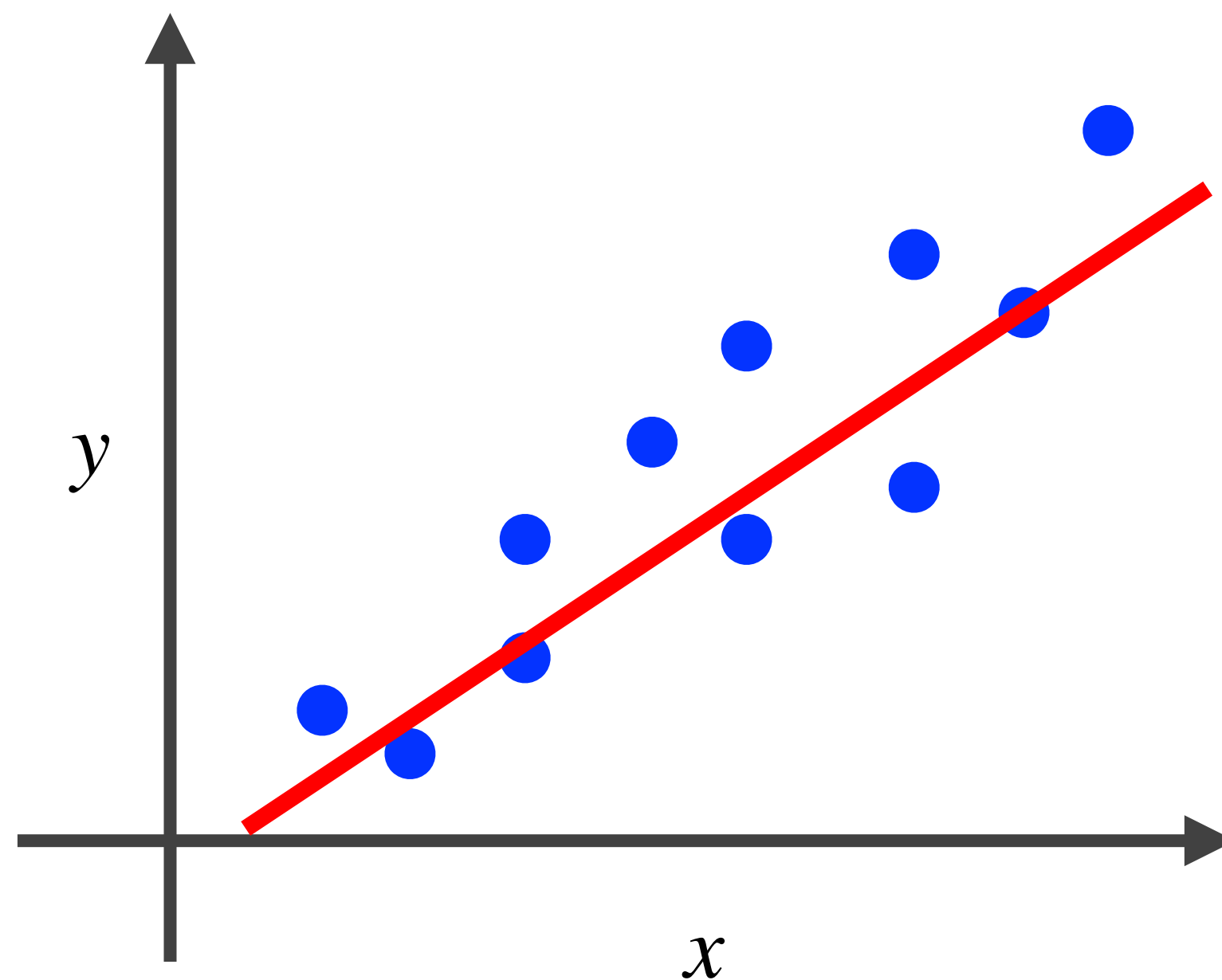


$$w_1 > 0$$

$$w_0 \approx 0$$

# Linear Model

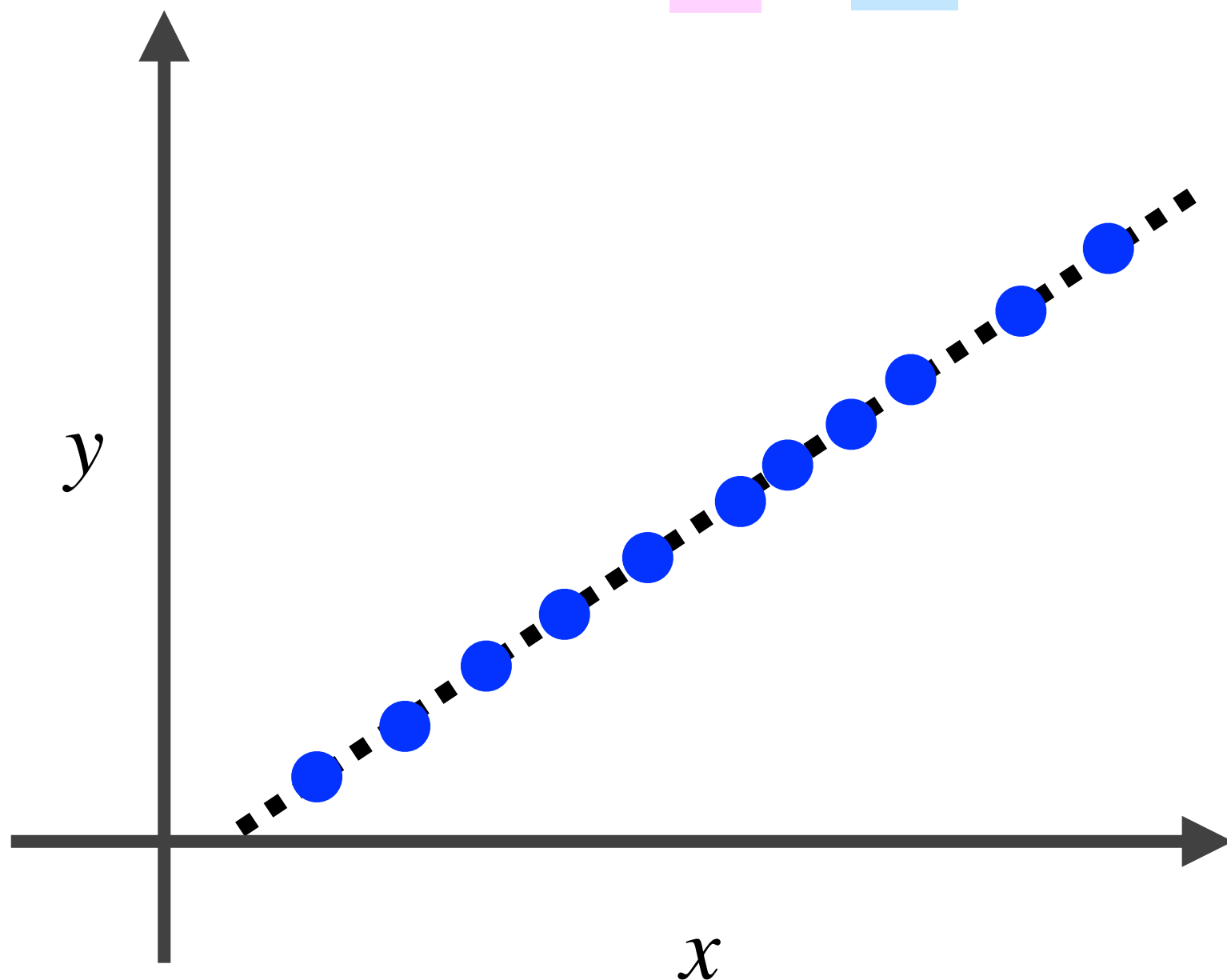
$$y = w_0 + w_1x$$



# Signal and Noise

Underlying relationship

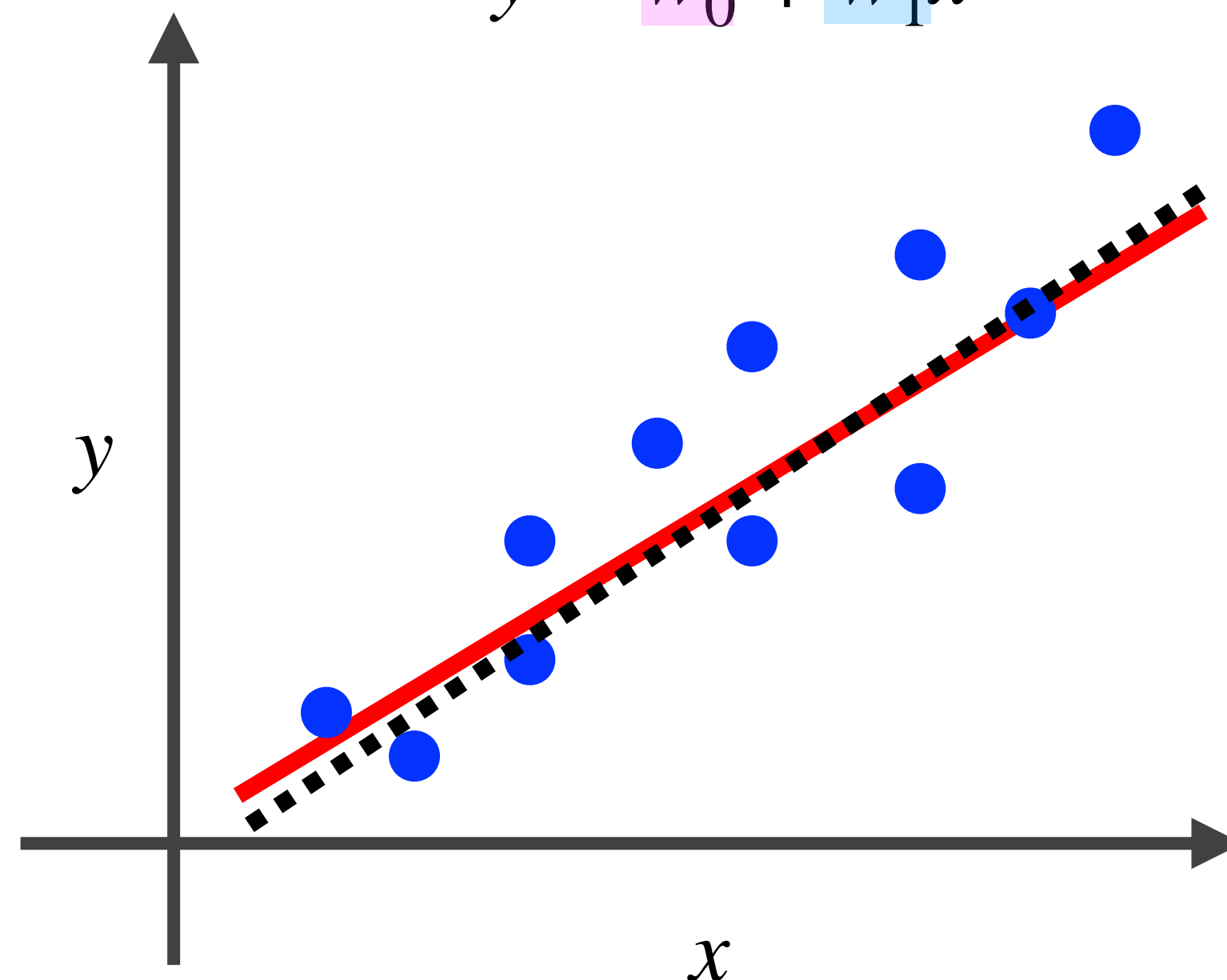
$$y = w_0 + w_1 x$$



Observed data

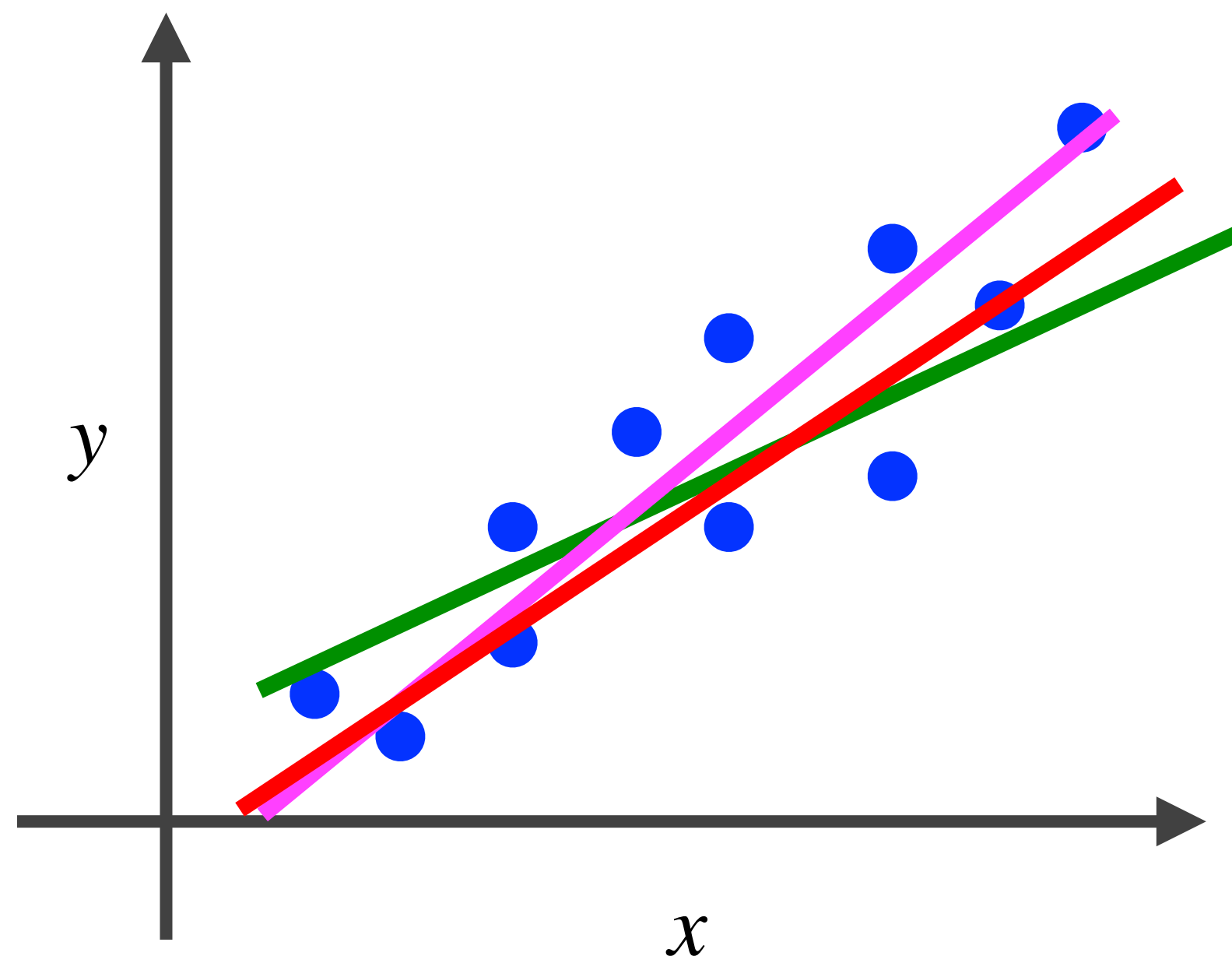
$$y = w_0 + w_1 x + \text{noise}$$

$$\hat{y} = \hat{w}_0 + \hat{w}_1 x$$



# Linear Model

$$\hat{y} = \hat{w}_0 + \hat{w}_1 x$$



Which one is the best?