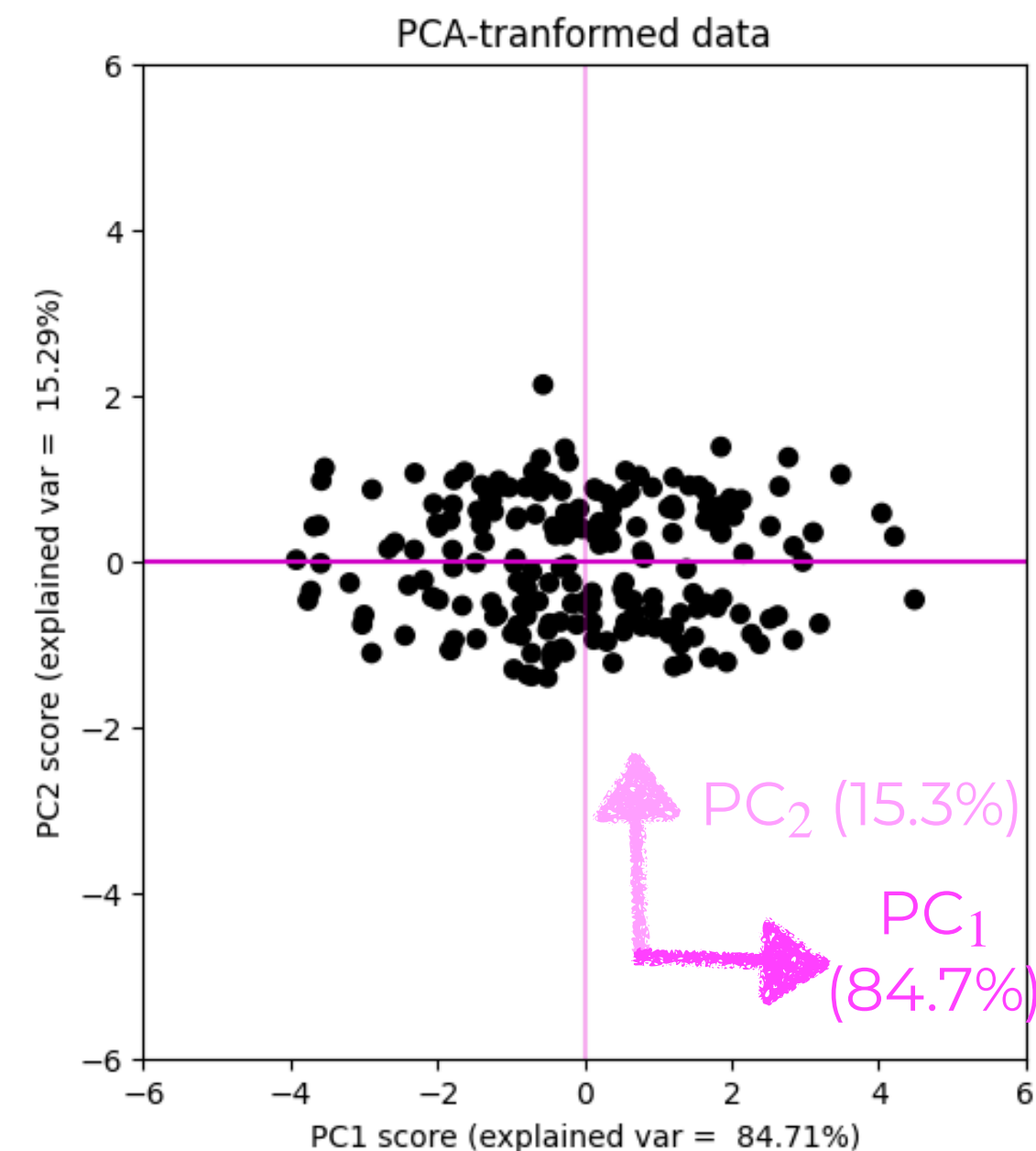
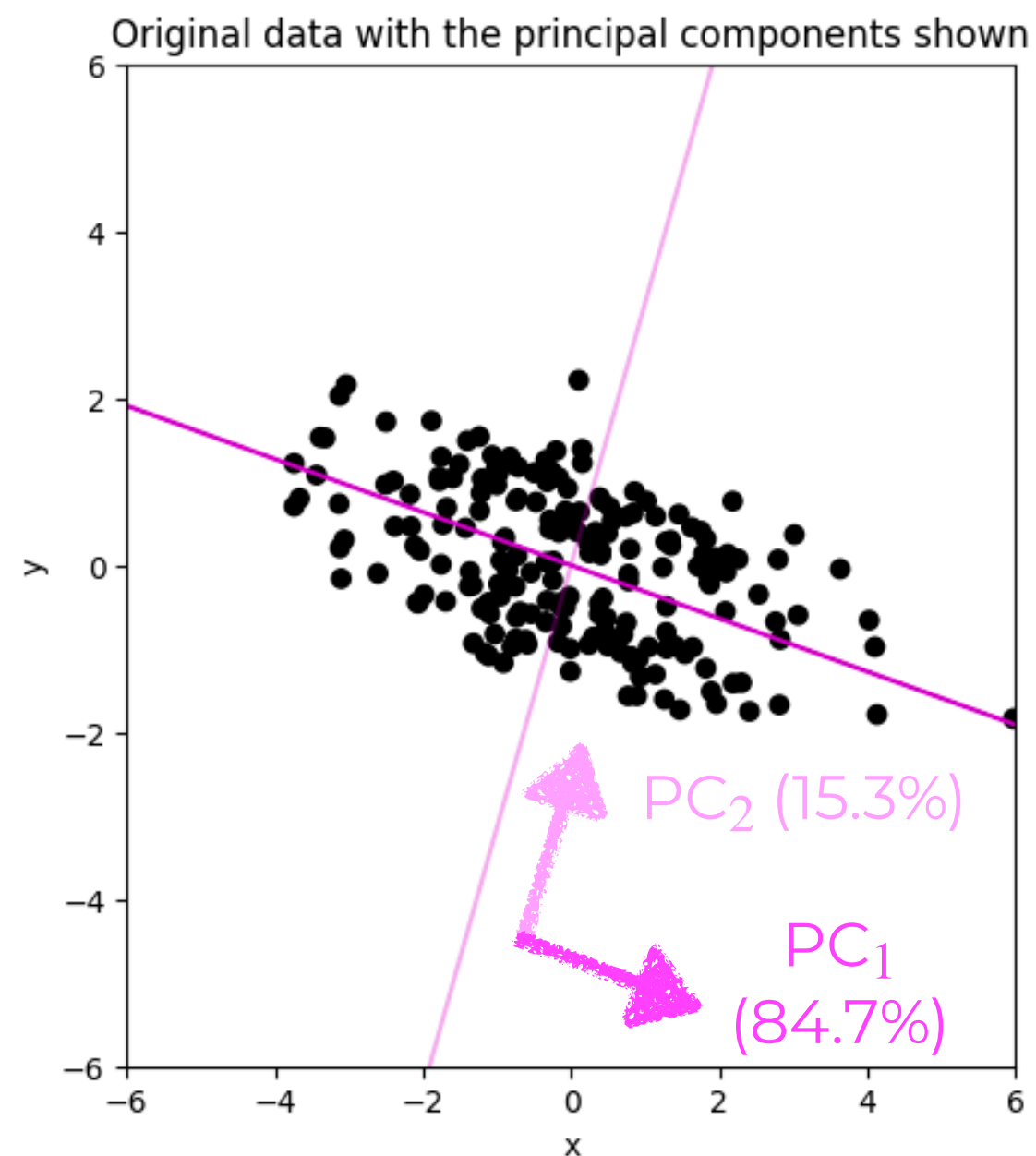
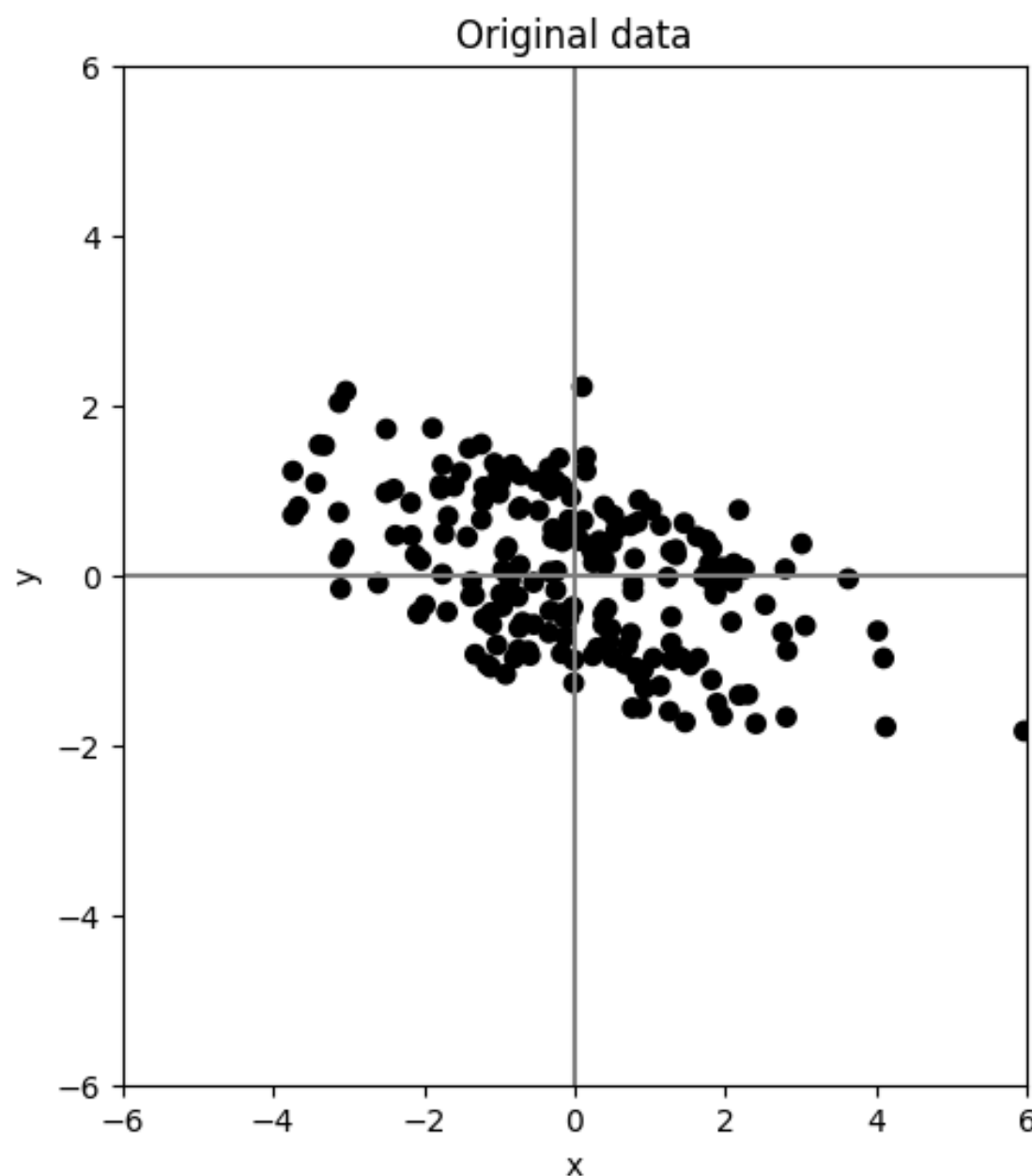


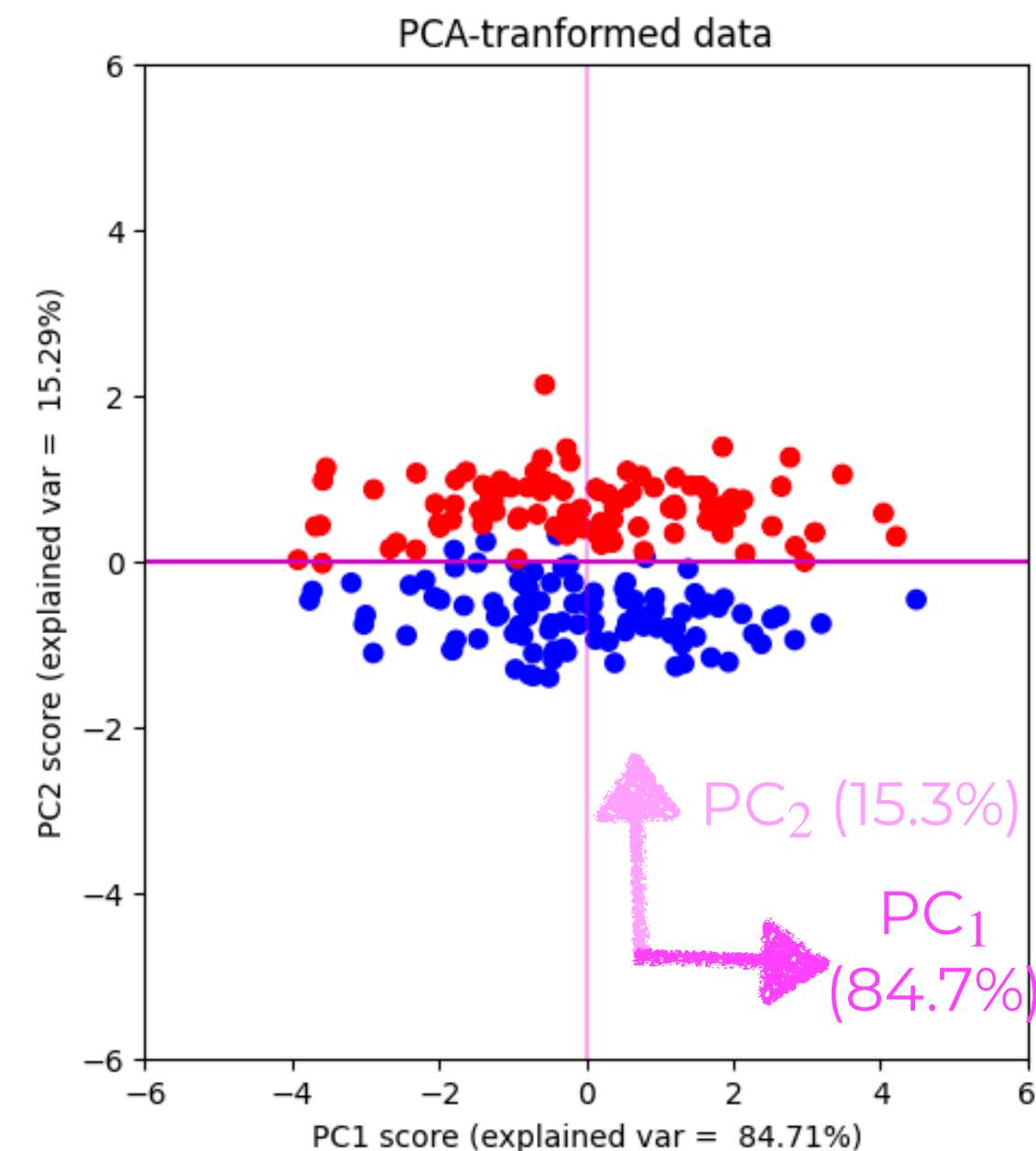
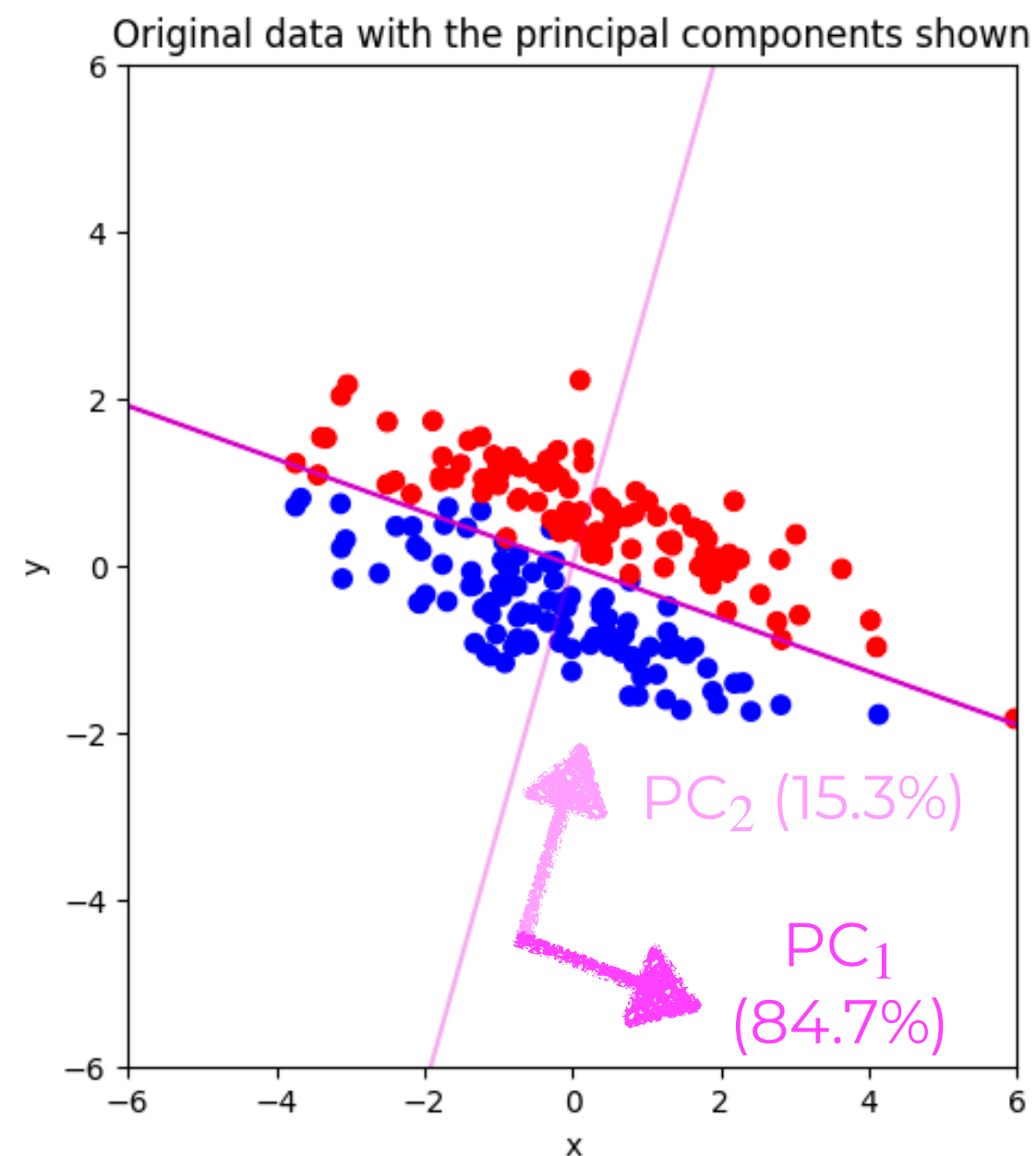
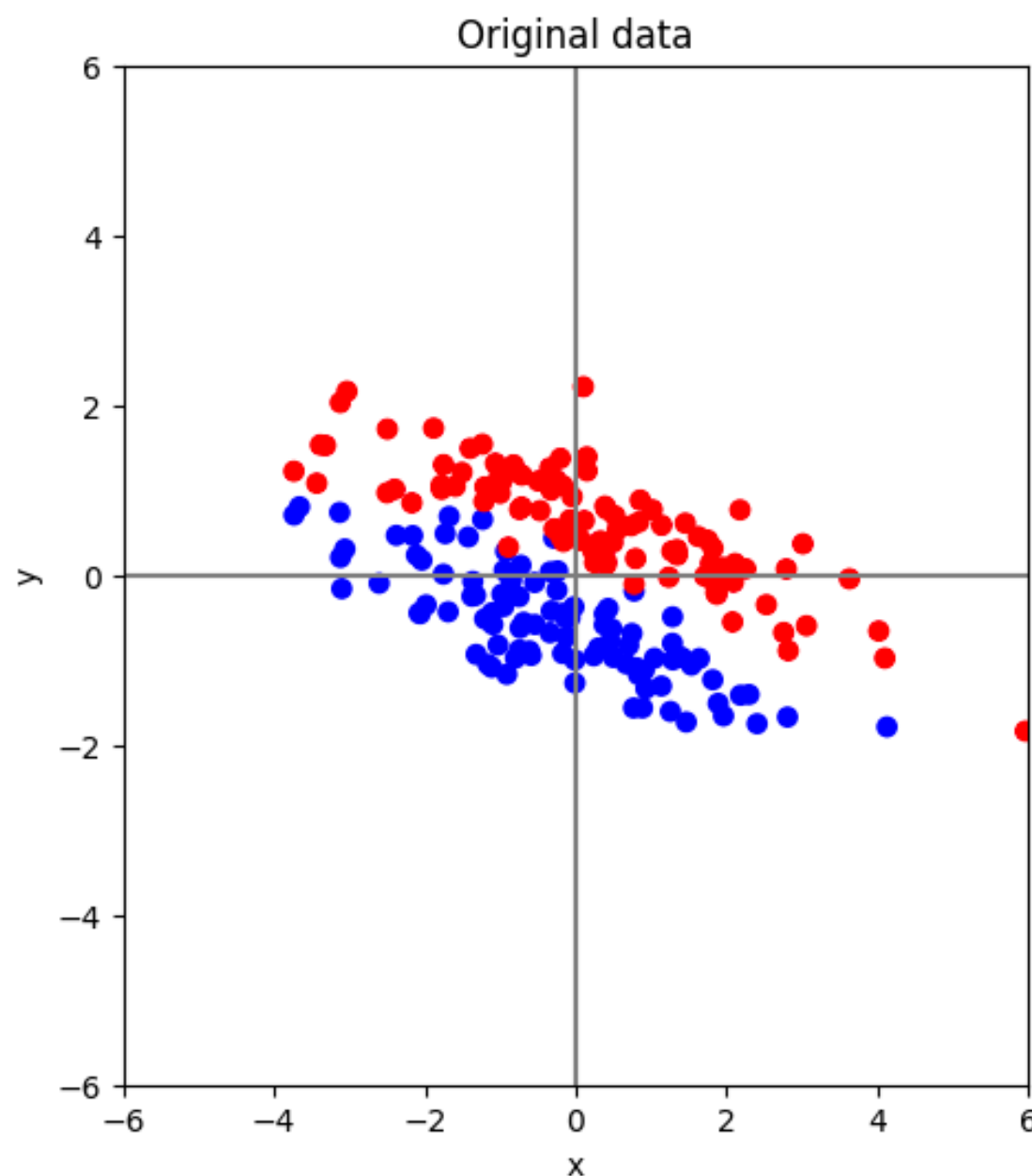
Nonlinear Dimensionality Reduction

Itthi Chatnuntawech

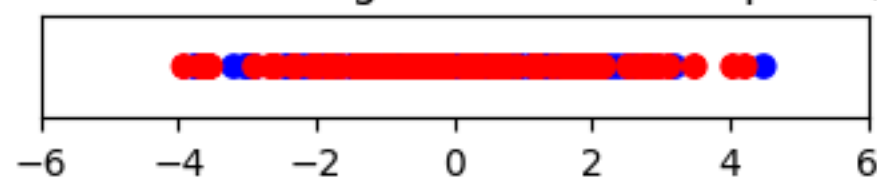
PCA Example



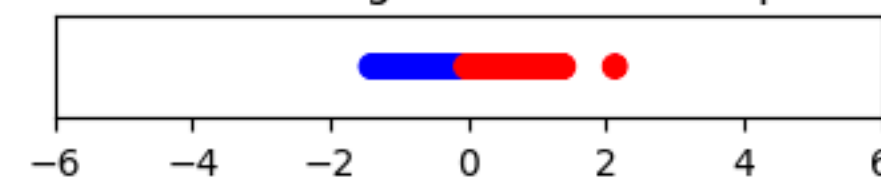
PCA Example



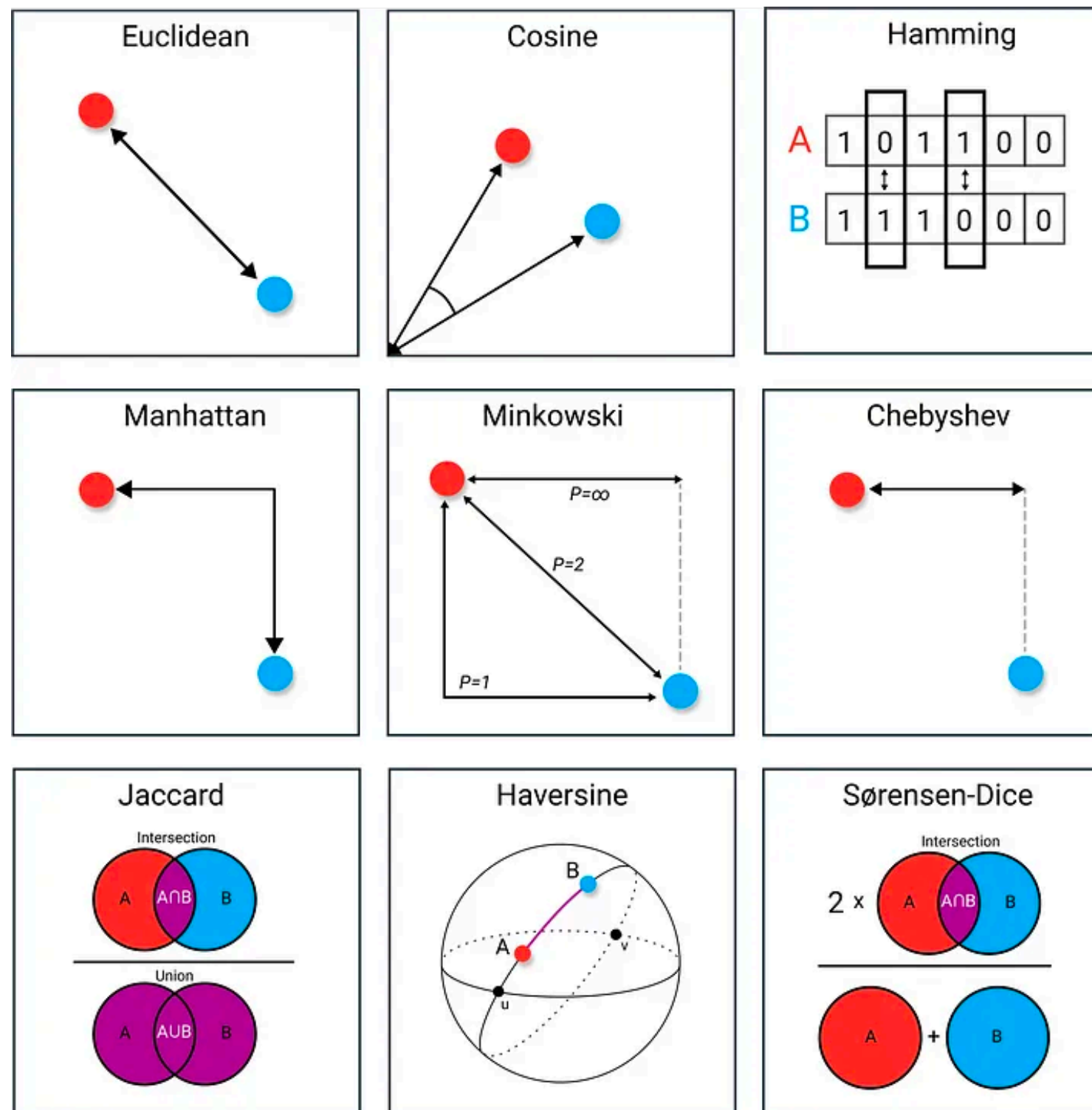
Data in the resulting 1-dimensional space (PC1)



Data in the resulting 1-dimensional space (PC2)

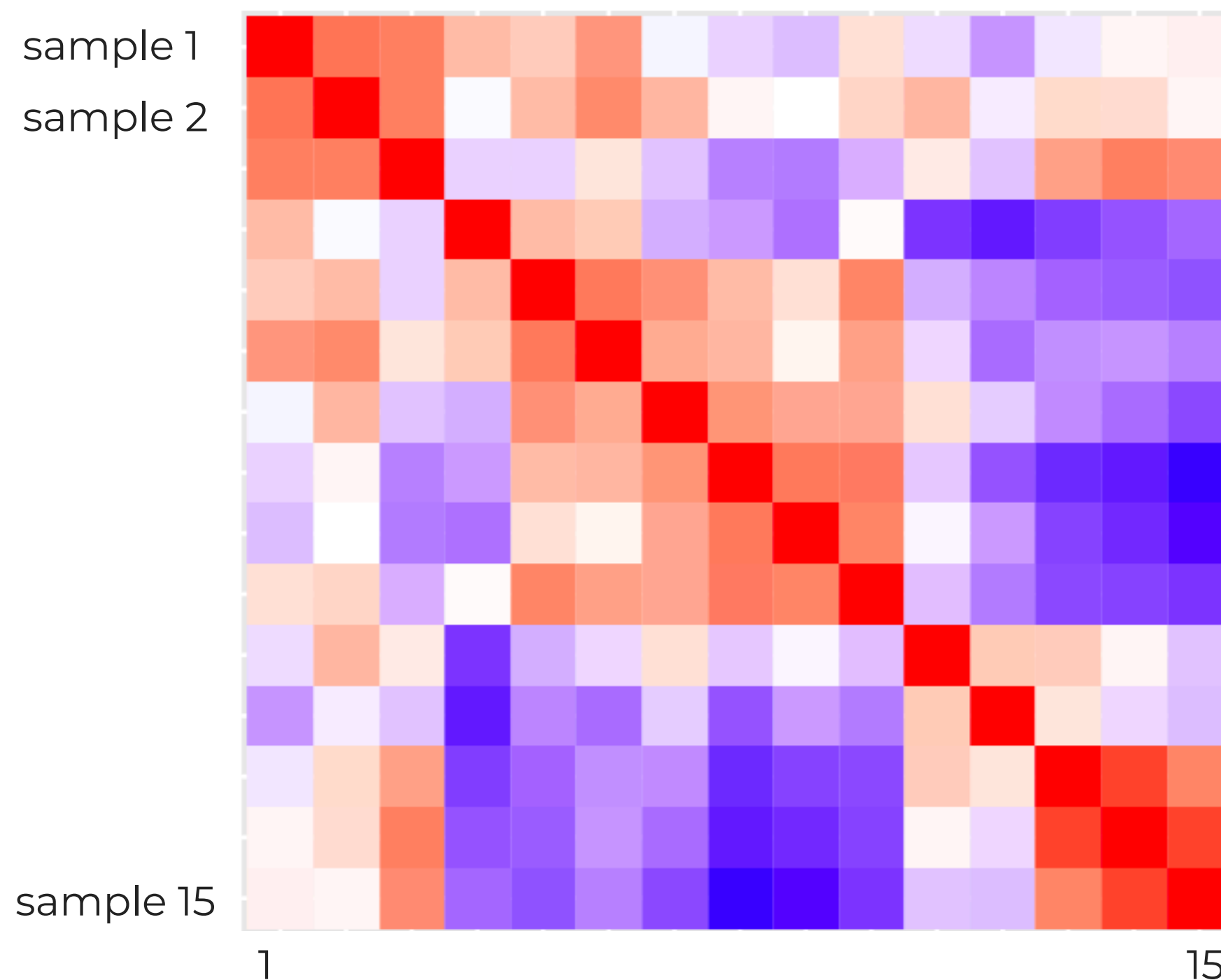


Distance Measures



<https://towardsdatascience.com/9-distance-measures-in-data-science-918109d069fa>

Pairwise Distance Matrix



The element at row i and column j represents the distance between sample i and sample j

$$D_{ij} = D_{ji}$$

$$D_{ii} = 0$$

Modified from <https://www.datanovia.com/en/lessons/clustering-distance-measures/>

Generalized Multi-Dimensional Scaling (MDS)

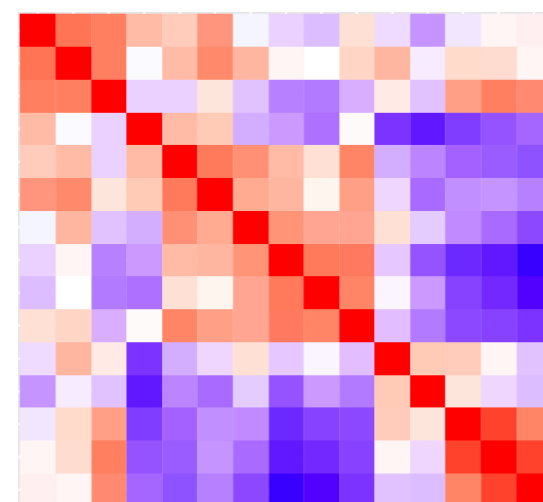
High-dimensional feature space

features

samples



pairwise distance matrix
created using any types
of distance

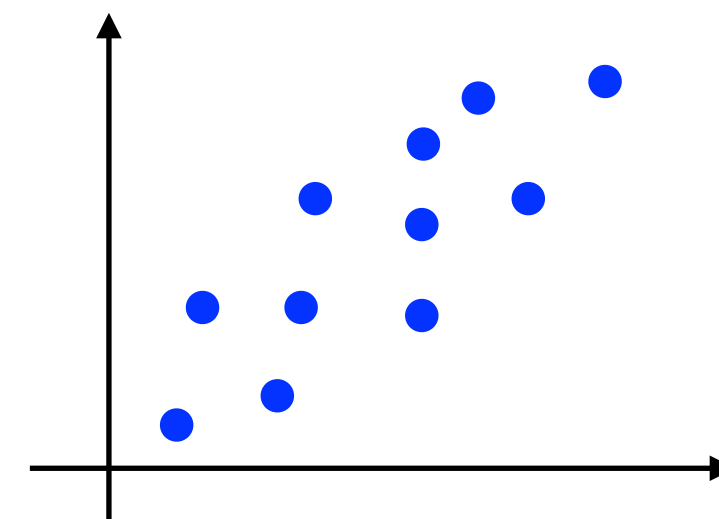
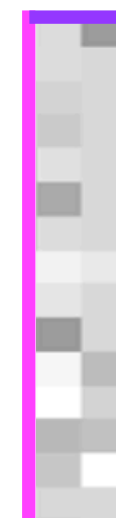


\approx

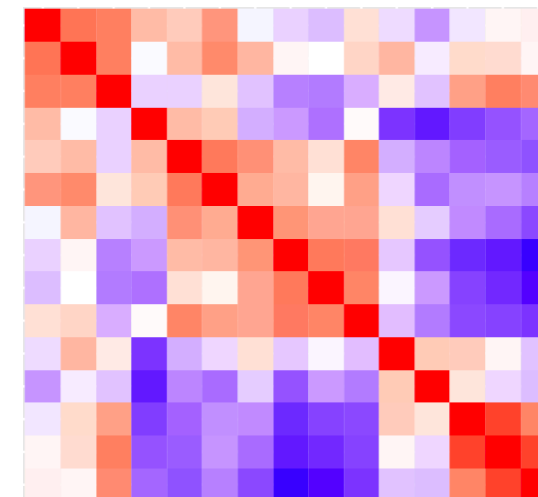
Low-dimensional space

new features

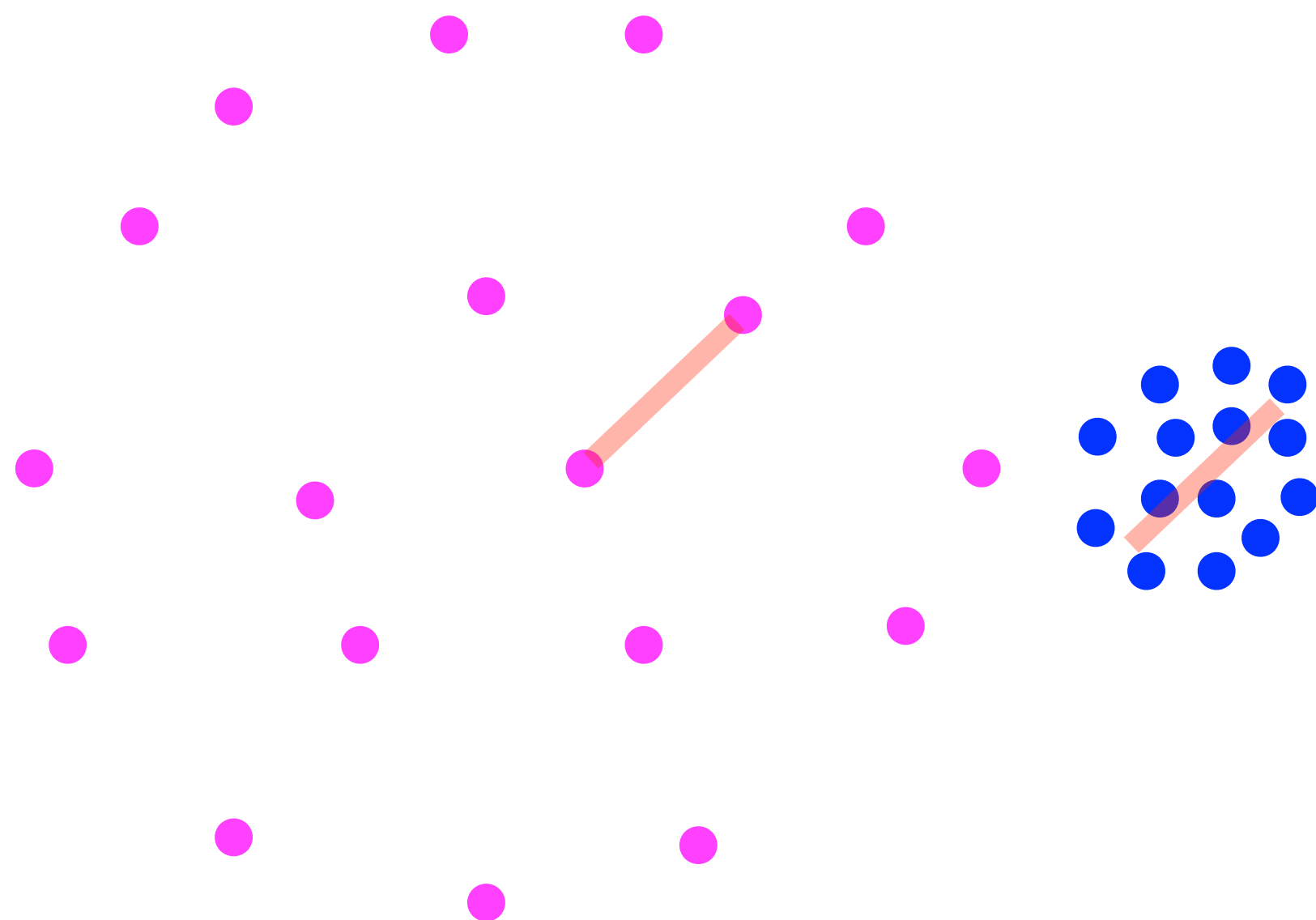
samples



pairwise distance matrix
created using any types
of distance



Beyond MDS



Should we use distance metrics that take into account data density?

Popular Nonlinear Dimensionality Reduction Methods

t-distributed Stochastic Neighbor Embedding (t-SNE)

sklearn.manifold.TSNE

```
class sklearn.manifold.TSNE(n_components=2, *, perplexity=30.0, early_exaggeration=12.0, learning_rate='auto',
n_iter=1000, n_iter_without_progress=300, min_grad_norm=1e-07, metric='euclidean', metric_params=None, init='pca',
verbose=0, random_state=None, method='barnes_hut', angle=0.5, n_jobs=None) \[source\]
```

Uniform Manifold Approximation and Projection (UMAP)

```
class umap.umap_.UMAP(n_neighbors=15, n_components=2, metric='euclidean', metric_kwds=None,
output_metric='euclidean', output_metric_kwds=None, n_epochs=None, learning_rate=1.0, init='spectral',
min_dist=0.1, spread=1.0, low_memory=True, n_jobs=-1, set_op_mix_ratio=1.0, local_connectivity=1.0,
repulsion_strength=1.0, negative_sample_rate=5, transform_queue_size=4.0, a=None, b=None,
random_state=None, angular_rp_forest=False, target_n_neighbors=-1, target_metric='categorical',
target_metric_kwds=None, target_weight=0.5, transform_seed=42, transform_mode='embedding',
force_approximation_algorithm=False, verbose=False, unique=False, densmap=False, dens_lambda=2.0,
dens_frac=0.3, dens_var_shift=0.1, output_dens=False, disconnection_distance=None) \[source\]
```

