

(c) Formulate gradient descent for the objective function f . The learning rate should be $\alpha = 0.4$ and the initial point $x^0 = (x^0, y^0) = (2, 2)$.

```
function objective_function(x,y):  
    return  $x^2 + y^2 + xy - 5x - 7y + 20$   
ffun
```

```
function partial_derivate_x(x,y):  
    return  $2x + y - 5$   
ffun
```

```
function partial_derivate_y(x,y):  
    return  $2y + x - 7$   
ffun
```

```
function gradient_descent(initial_x, initial_y, learning_rate, max_iterations)  
    x:=initial_x  
    y:=initial_y  
  
    for i from 1 to max_iterations  
        gradient_x:=partial_derivate_x(x,y)  
        gradient_y:=partial_derivate_y(x,y)  
  
        x:=x-learning_rate*gradient_x  
        y:=y-learning_rate*gradient_y  
    ffor  
ffun
```