

(c) Formulate gradient descent for the objective function  $f$ . The learning rate should be  $\alpha=0.4$  and the initial point  $x^0=(x^0, y^0)=(2, 2)$ .

```
function objective_function(x,y):  
    return x2+y2+xy-5x-7y+20  
ffun  
  
function partial_derivate_x(x,y):  
    return 2x+y-5  
ffun  
  
function partial_derivate_y(x,y):  
    return 2y+x-7  
ffun  
  
function gradient_descent(initial_x, initial_y, learning_rate, max_iterations)  
    x:=initial_x  
    y:=initial_y  
  
    for i from 1 to max_iterations  
        gradient_x:=partial_derivate_x(x,y)  
        gradient_y:=partial_derivate_y(x,y)  
  
        x:= x - learning_rate * gradient_x  
        y:= y - learning_rate * gradient_y  
    ffor  
ffun
```