# Operating manual and detailed algorithms for conducting stochastic future projections with R packages of 'ssfuture'

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May 30, 2011

#### 1 Introduction

Stock Synthesis (SS) is currently one of the most commonly used software for stock assessment. The software provides statistical framework for calibration of a population dynamics model using a diversity of fishery and survey data (Methot, 2005). SS can also provide outlooks for future population dynamics with deterministic projections from the estimated parameters during the stock assessment period. In the future projection phase, SS provide averages of future statistics such as spawning biomass (SSB) and standard deviations of the future statistics. The standard deviations are estimated by Hessian-matrix under normal approximation (Maunder et al., 2006) or by MCMC. Therefore, the estimated future statistics (such as future SSB) in SS are assumed to distribute normally, and not reflect future stochastic uncertainty.

On the other hand, stochastic future projections are sometimes important for evaluating current stock status and future management procedures. Simulation-based reference points of  $F_{ssb}$  (Conser et al. 2006; Ichinokawa et al., 2010) are used as an interim reference point for this stock for North Pacific albacore stock. Future stochastic projections for the stock assessment of Pacific bluefin tuna in ISC have been conducted with specific software coded by R (cf. Ichinokawa et al., 2008). Suites of reference points are also produced with this software (cf. Kai et al. 2010).

This appendix made detailed description on algorithms to conduct stochastic future projections and reference points from outputs by Stock Synthesis with the R-code.

### 2 Population dynamics

#### 2.1 Definition of parameters and dimension for population dynamics

Table 1 shows definition of parameters used in this document. Basically, parameters estimated during the stock assessment phase are expressed by lower cases; those during future projection phase are by upper cases. For example, numbers at age a ( $0 \le a \le Amax$ ) and time t at the bth bootstrap run during the stock assessment period is expressed as  $n_{a,t}^b$ , while those in the future projection period are expressed by  $N_{a,t}^{b,k}$ . The superscript of b, representing the bth bootstrap results, can range from 0 to the number of bootstrap iterations of  $X_b$ . The 0th iteration represents maximum likelihood estimation.

Since multiple season per year can be assumed in SS, estimated parameters in SS include the dimension of season ( $0 \le s \le nseason$ ). However, because description of the additional dimension make the R-code complicated, population dynamics used in the future projections didn't include the dimension of season. Instead, the time series is expanded by year and season to use year interval of i = 1/nseason. For example, time series from 1952 to 2006 with 4 seasons can be expressed by t = 1952, 1952.25, 1952.5, ..., 2005.5, 2005.75, and age classes from 0 to 20 years old are by a = 0, 0.25, 0.5, ..., 19.5, 19.75. Then, estimates in SS of  $n_{a,s,t}$  (numbers at age at the beginning of the

Table 1: Parameters used in this document

Parameter	Description
$n_{a,t}^b, N_{a,t}^{k,b}$	Population numbers at beginning of season
$n_{a,t}^b, N_{a,t}^{k,b}$ $f_{a,t}^b, F_{a,t}^{k,b}$	Instantaneous rate of fishing mortality during the stock assessment period (lower
	case) and future projection period (upper case)
$c_{a,t}^b, C_{a,t}^{k,b}$	Catch at age during the stock assessment period (lower case) and future projection
	period (upper case)
$M_a$	Instantaneous rate of natural mortality (/yr)
$w_a$	Weight at age at the beginning of season
$w_{af}$	Weight at age by fleet at the beginning of season
$Q_a$	Maturity rates at age
Fcur <sub>a</sub>	Current F, which is produced by averaging a current F period
PFcur <sub>af</sub>	Partial F corresponding with Fcur <sub>a</sub> . $\sum_{k=1}^{nfleet} PFcur_{af} = Fcur = a$
$b_t^b,\!B_t^b$	Stock biomass at the beginning of the year
$ssb_t^b$ , $SSB_t^b$	SSB spawning stock biomass at the beginning of the spawning season
$PTC_t^b, TC_t^b$	Total catch by fleet, and total catch in weight
$t_1, t_2$	Generic parameters specifying a range of time period from $t_1$ to $t_2$ (Table 2)
nseason	Number of seasons per year (inherited from SS)
nfleet	Number of fisheries (inherited from SS)
i	Time interval = $1/qt$
$A_{min},A_{max}$	Minimum and maximum age considered in the stock assessment model and future
	projection. Plus groups are included in the age of $A_{max}$ . Recruitments are assumed
	to occur at $a = 0$ .
$X_s$	Number of stochastic simulations. $k = 1, 2,, X_s$ .
$X_b$	Number of bootstrap iterations. $b = 0, 1, 2,, X_s$ . The 0th iteration represents
	point estimates.

time time interval t),  $c_{a,s,t}$  (catch at age of age a during the time interval t), and  $c_{a,s,t,f}$  (partial catch at age by fisheries) are rewritten as the following equations.

$$n_{a+(s-1)/qt,t+(s-1)/qt} = \begin{cases} n_{a,s,t} & \text{if } n_{a,s,t} > 0\\ NA & \text{if } n_{a,s,t} = 0 \end{cases}$$
 (1)

$$c_{a+(s-1)/qt,t+(s-1)/qt} = \begin{cases} c_{a,s,t} & \text{if } n_{a,s,t} > 0 \text{ and } a < A_{max} \\ \frac{1}{nseason} \sum_{s=1}^{nseason} c_{a,s,t} & \text{if } n_{a,s,t} > 0 \text{ and } a = A_{max} \\ NA & \text{if } n_{a,s,t} = 0 \end{cases}$$
 (2)

$$n_{a+(s-1)/qt,t+(s-1)/qt} = \begin{cases} n_{a,s,t} & \text{if } n_{a,s,t} > 0 \\ \text{NA} & \text{if } n_{a,s,t} = 0 \end{cases}$$

$$c_{a+(s-1)/qt,t+(s-1)/qt} = \begin{cases} c_{a,s,t} & \text{if } n_{a,s,t} > 0 \text{ and } a < A_{max} \\ \frac{1}{nseason} \sum_{s=1}^{nseason} c_{a,s,t} & \text{if } n_{a,s,t} > 0 \text{ and } a = A_{max} \\ \text{NA} & \text{if } n_{a,s,t} = 0 \end{cases}$$

$$c_{a+(s-1)/qt,t+(s-1)/qt,f} = \begin{cases} c_{a,s,t,f} & \text{if } n_{a,s,t} > 0 \text{ and } a < A_{max} \\ \frac{1}{nseason} \sum_{s=1}^{nseason} c_{a,s,t,f} & \text{if } n_{a,s,t} > 0 \text{ and } a < A_{max} \\ \text{NA} & \text{if } n_{a,s,t} = 0 \end{cases}$$

$$(1)$$

'NA' stands for a blank element, where corresponding population does not exist. Also, since all elements of  $n_{a,t}$ ,  $c_{a,t}$ ,  $c_{a,t}$ , can't be filled with the above equation, remaining elements are filled by 'NA'. Those blank columns expressed by 'NA' are ignored int the following calculations. Note that, in the case of catch at age, catch of terminal ages are assumed to be an average through the season.

#### 2.2 Current F

Current F (Fcur<sub>a</sub>) is defined from the parameters estimated in the stock assessment period, numbers at age  $(n_{a,t}^b)$  and catch at age  $(c_{a,t}^b)$ . First,  $f_{a,t}^b$  is estimated by solving the following catch equation.

$$c_{a,t}^b = \frac{f_{a,t}}{f_{a,t} + M_a} (1 - \exp(-f_{a,t} - M_a)) n_{a,t}$$
(4)

Given the time range representative to 'current' as  $t_1 \le t < t_2$ , the current F of Fcur<sub>a</sub> is calculated by averaging F at age during the time range. In averaging F at age through the current F period, two options can be selected: simple or geometric average. In using simple average, the following equation is used.

$$Fcur_a = \frac{1}{\text{number of years}} \sum_{t_1 \le t < t_2} f_{a,t}$$
 (5)

Otherwise, geometric mean can also be available.

$$Fcur_{a} = \exp\left(\sum_{t=1}^{t_{1} \le t \le t_{2}} \log f_{a,t} \frac{1}{\text{number of years}}\right)$$
 (6)

Current F by fleet (Fcur<sub>a,f</sub>) is also calculated as following equations using partial catch at age ( $c_{a,t,f}$ ).

$$Fcur_{a,f} = Fcur_a PFcur_{a,f}$$
 (7)

where

$$PFcur_{a,f} = \frac{1}{\text{number of years}} \sum_{t_1 \le t \le t_1} \frac{c_{a,t,f}}{c_{a,t}}$$
 (8)

The parameter of PFcur $_{a,f}$  is partial catch ratio assumed in the current F, which is utilized in calculating partial catch in weight by fleet in future. Note that the PFcur $_{a,f}$  is calculated by using simple average, even though the option of 'geometric mean' is used. This is because zero partial fishing mortality appears frequently, which cause inability to calculate geometric mean.

#### 2.3 Population dynamics in future

Numbers at age  $N_{a,y}^{k,b}$  in the future period  $(t_1 \le t \le t_2)$  are calculated as the following equations.

$$N_{a,t_1}^{k,b} = \begin{cases} R_t^{k,b} & a = 0 \text{ and } t = \text{recruitment timing} \\ 0 & a = 0 \text{ and } t \neq \text{recruitment timing} \end{cases}$$

$$N_{a,t_1}^{k,b} = \begin{cases} R_t^{k,b} & a = 0 \text{ and } t = \text{recruitment timing} \\ 0 & a = 0 \text{ and } t \neq \text{recruitment timing} \\ 0 & a = 0 \text{ and } t \neq \text{recruitment timing} \\ N_{a-i,t-i}^{k,b} \exp(-F_{a-i} + -M_{a-i}) & 0 < a < A_{max} \\ N_{a-i,t-i}^{k,b} \exp(-F_{a-i} + -M_{a-i}) + N_{a,t-i}^{k,b} \exp(-F_a + -M_a) & a = A_{max} \end{cases}$$
Extrem recruitment of  $R$  and  $S$  being weathlite at each of  $F$ , and determined by artical according of  $S$ .

Future recruitment of  $R_t$  and fishing mortality at age of  $F_a$  are determined by optional scenarios of recruitment (see section 3) and harvesting (see section 4).

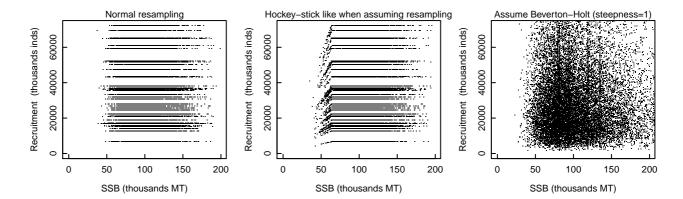


Figure 1: Examples of future recruitment scenarios. Left panel: simple re-sampling of past recruitments during 1965–2008. Middle panel: assuming hockey-stick type recruitments based on re-sampling of past recruitments. In this example, the threshold of SSB is set to be lower 20% of the historically observed SSB. Right panel: beverton-Holt spawner-recruitment relationship and lognormal error. Parameters of the S-R curve are inherited from the estimates in SS. In this example, steepness is fixed as 1 in SS.

Future statistics of total biomass  $(B_t^{k,b})$  and SSB  $(SSB_t^{k,b})$  are calculated.

$$B_{y}^{k,b} = \sum_{a=0}^{A_{max}} w_{a} N_{a,t}^{k,b} \tag{11}$$

$$SSB_{y}^{k,b} = \sum_{a=0}^{A_{max}} w_{a} Q_{a} N_{a,t}^{k,b}$$
 (12)

weight at age,  $w_a$ , is derived from SS results (column specified by 'Wt\_Beg'). Total catch (TC<sub>t</sub><sup>k,b</sup>, in weight) and total partial catch by fisheries (PTC<sub>t</sub><sup>k,b</sup>, in weight) are also calculated.

$$TC_{t}^{k,b} = \sum_{f=1}^{nfleet} PTC_{t,f}^{k,b} = \sum_{f=1}^{nfleet} w_{a,f} \sum_{a=0}^{A_{max}} \frac{F_{a}PFcur_{a,f}}{F_{a} + M_{a}} (1 - exp(-F_{a} + M_{a})) N_{a,t}^{k,b}$$
(13)

Fishery specific weight at age  $(w_{af})$  is used in calculating TC and PTC. The parameter of  $w_{af}$  is derived from SS results (column specified by 'Selwt' in Report.sso).

### 3 Recruitment scenarios

Following scenarios are available for future recruitments.

#### 3.1 Simple resampling (REC.resample)

This scenario assumes future recruitments as random re-samplings from recruitments estimated in the stock assessment periods specified by  $t_1 \le t \le t_2$ .

$$R_t^{k,b} = \begin{cases} \text{random draw from} & n_{0,t_1 \le t \le t_2} \\ 0 & t \ne \text{recruitment timing} \end{cases}$$
 (14)

Followings are required configurations in using this recruitment scenario.

REC.resample	
year.lim(=NULL)	Give a vector with 2 elements of $t_1$ and $t_2$
qt(=1)	Assumed number of seasons per year (be consistent with SS configuration).
recruit.qt(=1)	Season when recruitments occur (be consistent with SS configuration). Currently, multiple recruitments per year can't be assumed with this R-code.

#### 3.2 Beverton-Holt S-R relation + stochastic error (REC.beverton.ss)

Future recruitment is assumed to occur according to the Beverton-Holt relationship with stochastic error of random lognormal or random resampling of past deviances of recruitment logRdev during a certain year range specified by year.lim  $(t_1 \le t \le t_2)$ . The parameters of the stock-recruitment relationship  $(h, S_0, R_0)$  and  $\sigma R$  is basically derived from SS output.

If option of resample=FALSE,

$$R_t^{k,b} = \begin{cases} \hat{R}_t \exp\left(N(-\sigma^2/2, \sigma^2)\right) & t = \text{recruitment timing} \\ 0 & t \neq \text{recruitment timing} \end{cases}$$
(15)

If option of resample=TRUE,

$$R_t^{k,b} = \begin{cases} \hat{R}_t \exp\left(-\sigma^2/2 + \text{random draw from} & logRdev_{t_1 \le t \le t_2}\right) & t = \text{recruitment timing} \\ 0 & t \ne \text{recruitment timing} \end{cases}$$
(17)

where

$$\hat{R}_t = \frac{4hR_0 SSB_t}{S_0(1-h) + SSB_t(5h-1)}$$
(18)

REC.beverton.ss	
recruit.qt(=1)	Season when recruitments occur (be consistent with SS config-
	uration). Currently, multiple recruitments per year can't be as-
	sumed with this R-code.
resampled(=FALSE)	Type of stochastic error. If resampled=TRUE, randomly resam-
	ple recruitment deviation. If resampled=FALSE, random log-
	normal error is assumed.
year.lim(=NULL)	Give a vector with 2 elements of $t_1$ and $t_2$ when
	resampled=TRUE.
(steepness, R0, Rsigma, B0)	If those parameters are explicitly given, those parameters are
	used instead of parameters assumed in SS.

#### 3.3 Assume empirical spawner-recruit relationship (REC.twophase)

This option is only for testing the effects of empirical spawner-recruit relationship observed in the Pacific bluefin tuna.

#### 3.4 Options applied to all recruitment scenarios

In addition, hockey-stick type recruitments can be assumed for the all recruitment scenarios. The parameter of  $SSB_{threshold}$  should be specified with this option.

$$R'_{t} = \begin{cases} R_{t} \frac{\text{SSB}_{t}}{\text{SSB}_{threshold}} & \text{SSB}_{t} \leq \text{SSB}_{threshold} \\ R_{t} & \text{SSB}_{t} > \text{SSB}_{threshold} \end{cases}$$

$$(19)$$

### 4 Harvesting scenarios

#### 4.1 Constant F (MP.CESqt3)

 $F_a$  is given by Fcur<sub>a</sub> scaled by a multiplier,  $F_{multi}$ , determined by the optional settings described below.

$F_a = F_{multi} *$	Fcur <sub>a</sub>	(20)
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MP.CESqt3	
Fcur1(=NULL)	Give a vector with 2 elements of $t_1$ and $t_2$ . The parameter of Fcur <sub>a</sub>
	is calculated with this time duration. Fcur1 is used before the year to start regulation.
Fcur2(=NULL)	Give a vector with 2 elements of $t_1$ and $t_2$ . The parameter of Fcur <sub>a</sub>
	is calculated with this time duration. Fcur1 is used after the year to start regulation.
start.regulation(=2011)	Start year for regulation (switch F vectors from Fcur1 to Fcur2).
CES.multi(=1)	Simple multiplier to $F_a$ (both for Fcur1 and Fcur2).
gm(=FALSE)	Use geometric mean (TRUE) or simple average (FALSE) for calculating $Fcur_a$ .
CES.plus(=0)	Simple additional F to $F_a$ .
CES.multi.year(=NULL)	Multiple vectors when changing multipliers to $F_a$ by year. Even
	though the population dynamic consider season, this vector is given
	by year.
catch.capping(=NULL)	Set upper limit of annual partial catch (MT) by fleet. 'NULL' is
	not to use this option. If using this option, provide a list to specify
	target fisheries, upper limit of catch and reset timing.

#### **4.2** Constant catch by season (MP.CHSfleet)

 $F_a$  is given by  $Fcur_a = PFcur_{af}$  scaled by a multiplier determined by solving catch equation (eq. 13) to archieve given future catches in weight by season.

MP.CHSfleet		
CHS.qt (=NULL)	Give a vector with nsesaon elements assigning catch in weight per	
	quarter.	
Fcur1(=NULL)	Give a vector with 2 elements of $t_1$ and $t_2$ . The parameter of	
	$Fcur_a and PFcur_{af}$ is calculated with this time duration. Fcur1 is used	
	before the year to start regulation. In constant catch scenario, the	
	estimated $Fcur_a and PFcur_{af}$ is scaled to adjust constant catch.	
Fcur2(=NULL)	Give a vector with 2 elements of $t_1$ and $t_2$ . The parameter of	
	Fcur <sub>a</sub> is calculated with this time duration. Fcur1 is used after the	
	year to start regulation. In constant catch scenario, the estimated	
	$Fcur_a and PFcur_{af}$ is scaled to adjust constant catch.	
start.regulation(=2011)	Start year for regulation (switch F vectors from Fcur1 to Fcur2).	
gm(=FALSE)	Use geometric mean (TRUE) or simple average (FALSE) for calcu-	
	lating Fcur <sub>a</sub> .	

#### 4.3 Hybrid scenario by year (MP.hybrid)

If you want to change harvesting scenario by year, you can use this option. With this option, harvesting scenarios can be switched among years. For this scenario, MP arguments is to be 'MP.hybrid', and provide lists of mp.arguments where harvesting scenario and appied year range is specified.

#### 4.4 Scenarios not implemented

Constant catch by quarter and fleet

### 5 Calculation of reference points

#### 5.1 $F_{ssb}$

 $F_{ssb}$  is based on the probability that future SSB will fall below a given threshold of SSB<sub>threshold</sub> at one or more years, during the assumed projection period ( $t_1 \le t \le t_2$ ). The probability can be calculated from results of the stochastic projections.

$$\Pr\left[SSB_{future}^{k,b} < SSB_{threshold}^{b}|F\right] = \frac{1}{X_b X_s} \sum_{k=1}^{X_b X_s} \|\min\left(SSB_{t_1 \le t \le t_2}^{k,b}\right) < SSB_{threshold}^{b}\|$$
(21)

, where the double bracket  $\parallel$  indicates a logical test with outcome 0 (if false) or 1 (if true). Note that the probability is different from the probability that SSB at nearly equilibrium year, SSB<sub>equilibrium</sub>, falls below the SSB<sub>threshold</sub> as follows.

$$\Pr\left[SSB_{equilibrium} < SSB_{threshold}|F\right] = \frac{1}{X_b X_s} \sum_{k=1}^{X_b X_s} \|\min\left(SSB_{equilibrium}^k\right) < SSB_{threshold}\|$$
 (22)

The F-based reference point of  $F_{ssb}$  is determined by letting the probability,  $Pr\left[SSB_{future} < SSB_{threshold}|F\right]$  be equal to a given probability,  $Pr_{threshold}$ . So, for the calculation of  $F_{ssb}$ ,  $SSB_{threshold}$ ,  $Pr_{threshold}$  and projection range of  $t_1$  and  $t_2$  should be specified.

The parameter of  $SSB_{threshold}$  is originally proposed to be  $\min(ssb_{t1 \le t \le t2})$ , or average of ten historical lowest (ATHL) of  $ssb_{t1 \le t \le t2}$ . Currently it is not determined whether the threshold level should depend on bootstrap iteration (using  $\min(ssb_{t1 \le t \le t2}^b)$ ), or not (using point estimates of  $\min(ssb_{t1 \le t \le t2}^0)$ ).

#### Suites of other reference points

Other reference points based on SPR and YPR are calculated from the following functions. It is noteworthy that the oldest age in estimating SPR and YPR is extended to  $3A_{max}$ . However, weight at age at the ages older than  $A_{max}$  is simply equal to  $w_{A_{max}}$ ,  $w_{A_{max},f}$ .

$$N_a = \begin{cases} 1 & a = 0 \\ N_{a-i} \exp(-F_{a-i} - M_{a-i}) & a > 0 \end{cases}$$
 (23)

$$C_a = \frac{F_a}{F_a + M_a} (1 - \exp(-F_a - M_a)) N_a$$

$$C_{af} = C_a \text{PFcur}_{a,f}$$
(24)

$$C_{af} = C_a PFcur_{a,f}$$
 (25)

$$SPR = \sum_{a=0}^{3A_{max}} N_a w_a Q_a$$
 (26)

$$YPR = \sum_{a=1}^{3A_{max}} \sum_{f=1}^{nfleet} C_{af} w_{af}$$
 (27)

### Test runs for comparing SS deterministic future projection

#### Validation of the R-code with deterministic run of future projections by SS

Average numbers at age (Fig. 2) and partial catch by fisheries (Fig. 3) estimated from stochastic future projections implemented by the R-code are compared with those calculated by deterministic projections implemented by SS. Those runs follow the setting of run 0, except for time period of current F. This run (run 1) used F in 2008 as current F, instead of average F during 20006-2008 in the base case.

While average numbers at age (Fig. 2) are almost identical between the two results from the R-code and SS, partial catch by fisheries and estimated SSB in weight (Fig. 3) are slightly different especially in the catch by fleet 6 and SSB. The differences of the partial catch are caused by different assumptions of annual partial F by fleet between SS and this R-code. There are no clear description on the way to assume future partial F in SS, so that the R could not trace every procedures in SS. The difference in SSB is may because SS (>3.10a) calculate weight at terminal age from initial numbers at age older than the terminal age with assumption of M=0.2, but it shouln't cause the differences. Details in future projection by SS should be asked to Dr. Methot. In near future, the R-code should be modified to follow the way to calculate weight at terminal age as used in SS.

## Practical codes for implementing future projections

#### 7.1 **Examples**

In starting future projection with this package, configuration list can be created by the function of 'create.defconf'. You can get default configulation list with this function interactively as following. This function shows all available options for future MP and recruitment scenario. Then copy and paste the resultant description for specifying configuration to your editor for editing specification as you like. Wrapper function to do future projection is 'do.projection.ss'.

```
R> create.defconf()
available option of MP: (1) MP.CESqt3 (constant F, and able to set upper limit of catch by fleet)
                        (2) MP.CESqt4 (constant F, and able to set constant catch by a specified fle
```

```
(3) MP.CHSfleet (constant quarterly catch)
                        (4) MP.CHS (prototype of MP.CHSfleet, not quarterly catch)
Please select 1-4 [default: 1]: 1
available option of R.fun: (1) REC.resample (Resampling of past recruitment)
                           (2) REC.beverton.ss (inherit Beverton-Holt S-R relation assumed in SS)
                           (3) REC.twophase (If SSB > historical median, resample R > R[SSB > histor
Please select 1-4 [default: 1]: 2
\# <- Copy and paste from here
config.tmp <- list(boot=c(1,300),</pre>
                                      # specification of bootstrap from and to
                   pred.year=30,
                                      # Projection year
                                      # N of simulations
                   N=20,
                   record.NAA=FALSE, # Is detailed results such as NAA produced?
                   initial.year=2008, # initial year of projection
                   ex.ssb=0,
                                      # Below this number, the population is considered to extinct
                   gm=TRUE,
                                      # Calculate selectivity by geometric or arithmetic mean
                   qt=4,
                                      # Number of season per year
                   MP="MP.CESqt3",
                                      # Function for future harvesting
                   args.mp=list(CES0=NULL,CES.multi=1, # Options for future harvesting
                                    start.regulation=2000,
                                    Fyear1=c(2004,2006), Fyear2=c(2004,2006)),
                                          # Function for future recruitment
                   Rec.fun="REC.ss2",
                                                    # Options for future recruitment,
                   args.R=list(recruit.qt=2),
                   HSlimit.tmp=NULL # Is hockey-stick option used? If yes, input vectors of SSB bre
                      # <- Copy and paste to here
R> config.tmp <- 'XXX'</pre>
R> do.projection.ss(mcore=1,bootfiles=c('Report_b01.sso', 'Report_b02.sso'),
                    faafiles=NULL,config.list=config.tmp)
```

do.projection.ss	
mcore (=1)	Number of CPU core used for this projection for parallel computing.
	Library of snow and snowfall is needed if mcore¿1.
bootfiles(=NULL)	Report files (Report.sso) of SS output.
faafiles(=NULL)	R object saved by the function of 'save'. This should be return value of
	calFAA.ss('Report.sso'). If this is NULL, calFAA.ss is conducted inside
	this function.
config.list(=NULL)	Configuration list for specifying future projection scenario.

#### 8 References

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Ichinokawa, M., Takeuchi, Y., Conser, R., Piner, K., and Aires-da-Silva, A. 2008. Future projections from the current stock status estimated by Stock Synthesis II for Pacific bluefin tuna. ISC/08/PBF-WG-1/15. p. 37.

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Maunder, M.N., Harley, S.J., and Hampton, J. 2006. Including parameter uncertainty in forward projections of computationally intensive statistical population dynamic models. IJ 63: 969-979.

Methot, R.D., and Fisheries, N. 2005. Technical description of the Stock Synthesis II assessment program. Version 1.17. Seattle, WA.

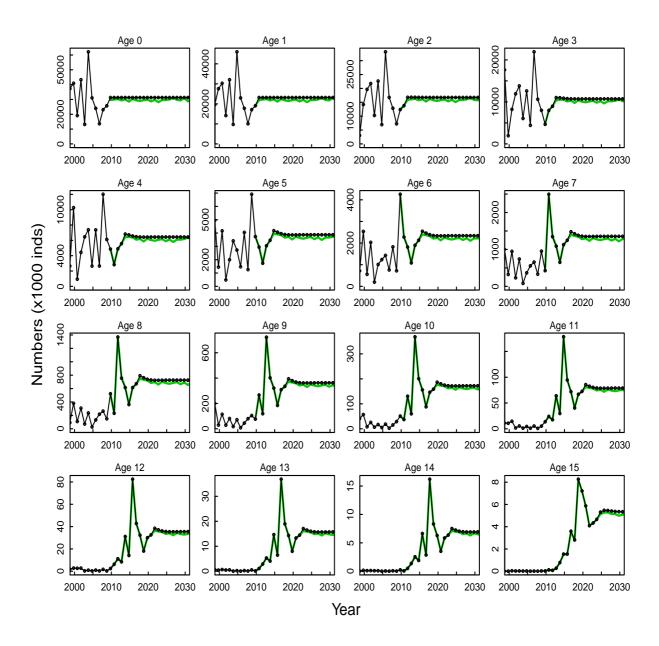


Figure 2: Comparison of numbers at age generated from stochastic projections by the R-code (average values, thick green lines) with those from a deterministic run by SS (lines with circles).

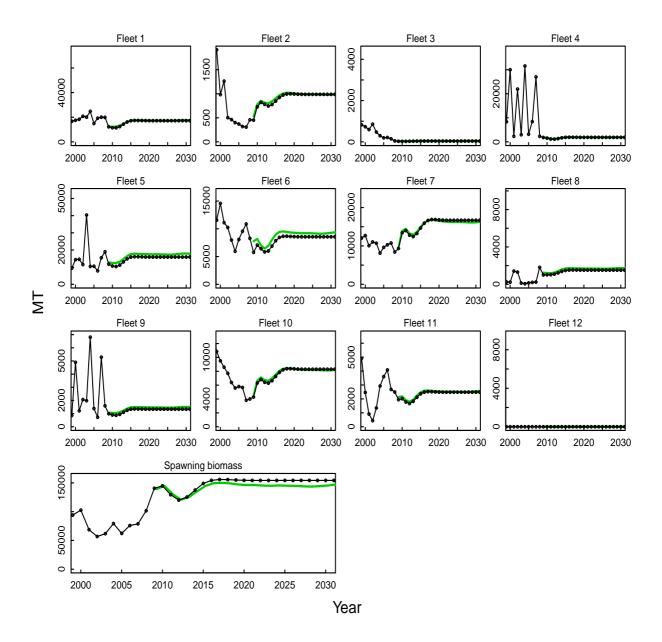


Figure 3: Comparison of catch in weight (MT) by fleets (figures titled by F1 to F12) and spawning biomass (MT) generated from stochastic projections by the R-code (thick lines) with those from a deterministic run by SS (lines with circles).