

# Visual Representation Learning Does Not Generalize Strongly Within the Same Domain

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## Motivation

### Question:

Can neural networks generalize factors of variation?  
Do neural networks learn underlying mechanisms?

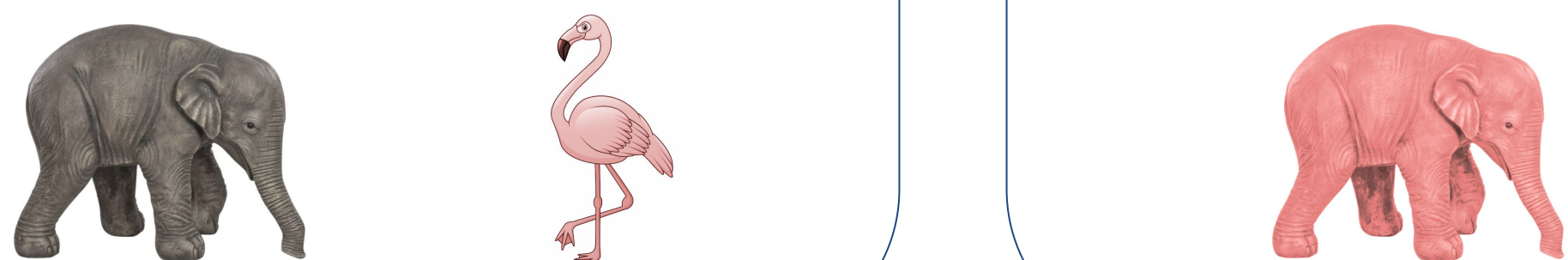
### Extrapolation:



### Interpolation:

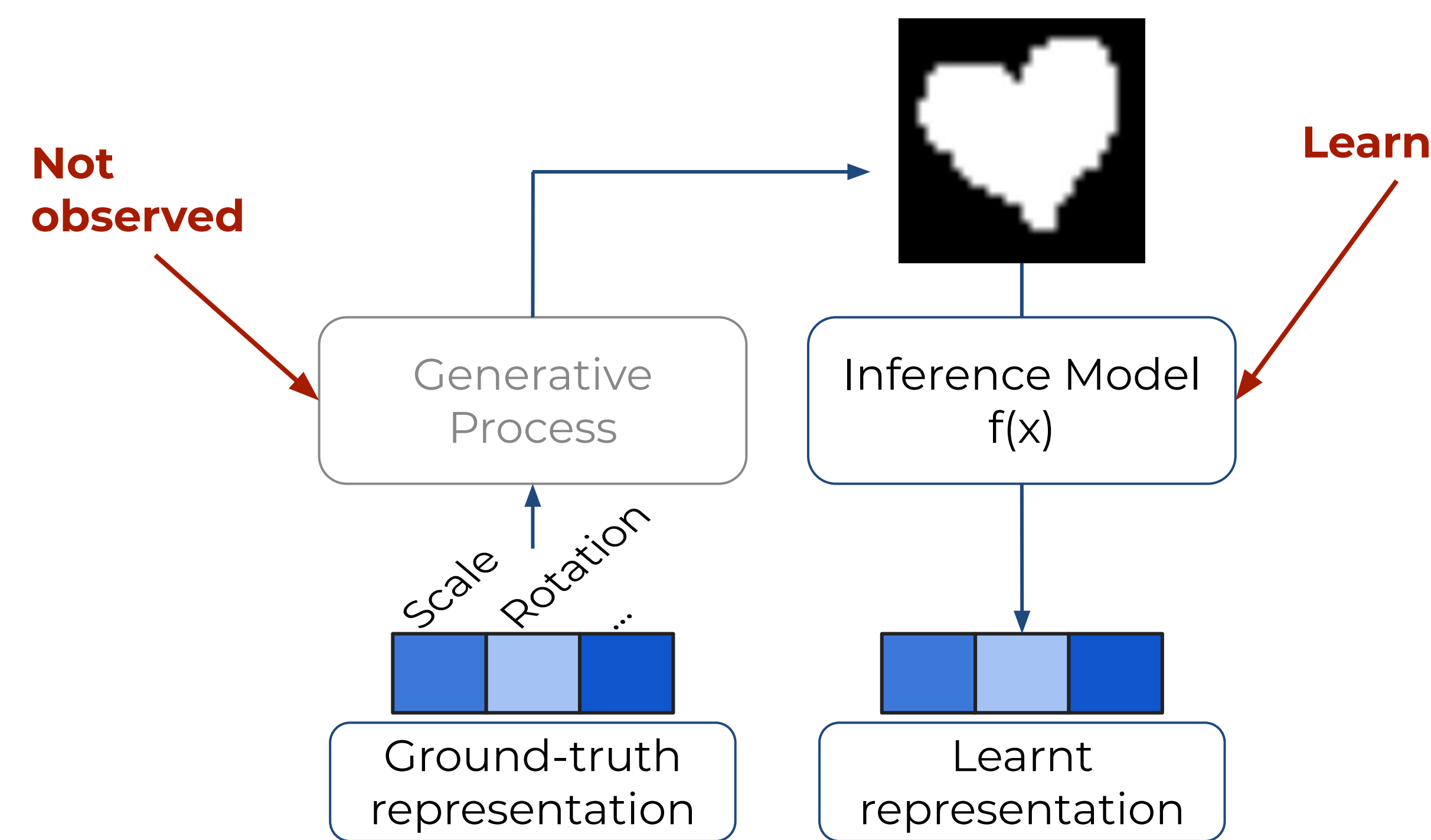


### Composition:



**Goal:** Test whether models learn the underlying mechanisms of a scene.

## Problem Setting



## Datasets

MPI3D [8]



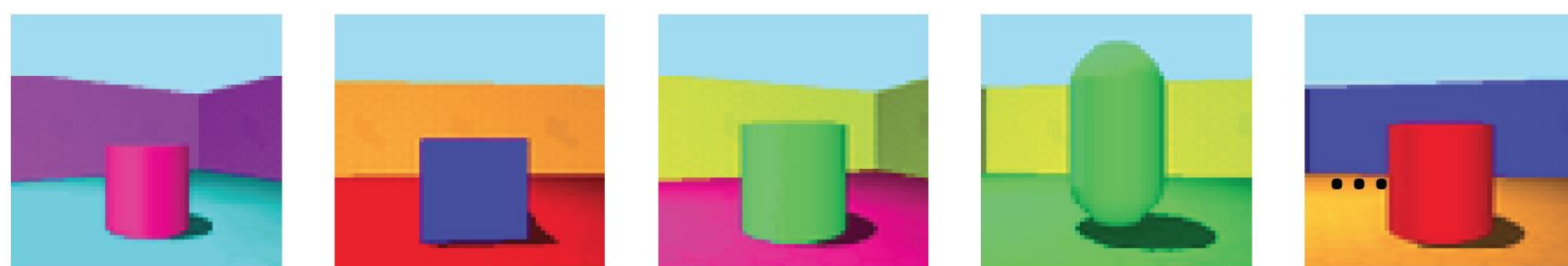
Color, shape, camera-elevation, size,

dSprites [6]



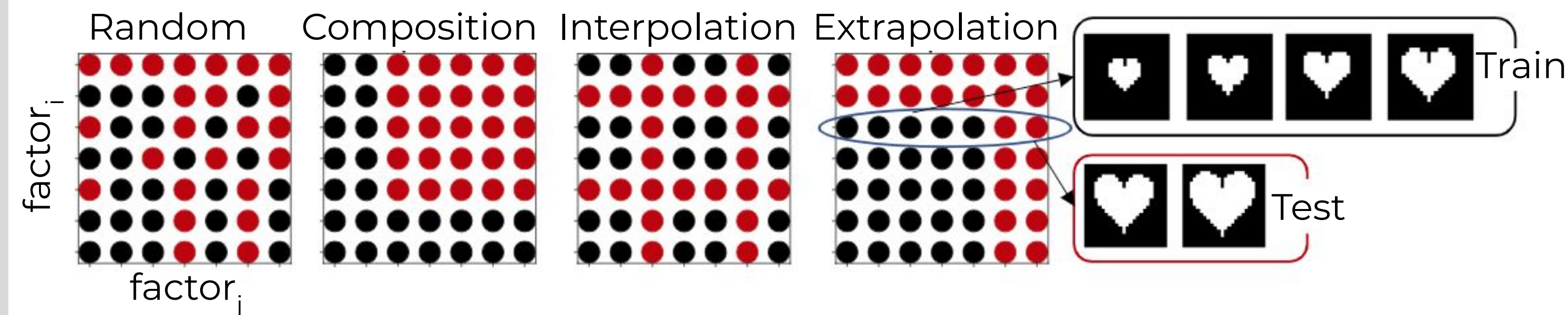
Shape, size, position, orientation

Shapes3D [7]



Bg/floor/object-color, shape, camera-azimut

## Setup



**Factors of variation:** Size, color, ...

**Test-train-split:** split all factors except shape: ~30%(train) : ~70%(test) samples

**Training:** Sample from the generative process on the training data in any way.

**Un-/ weakly supervised:** VAE, Ada-GVAE, SlowVAE, PCL

**Fully Supervised:** MLP, CNN, CoordConv, SetEncoder, Equivariant, ...

**Transfer Learning:** RN50 on IN-21k, RN101 on IN21-k, DenseNet on IN1-k

## Evaluation

**Regression of factors of variation:**

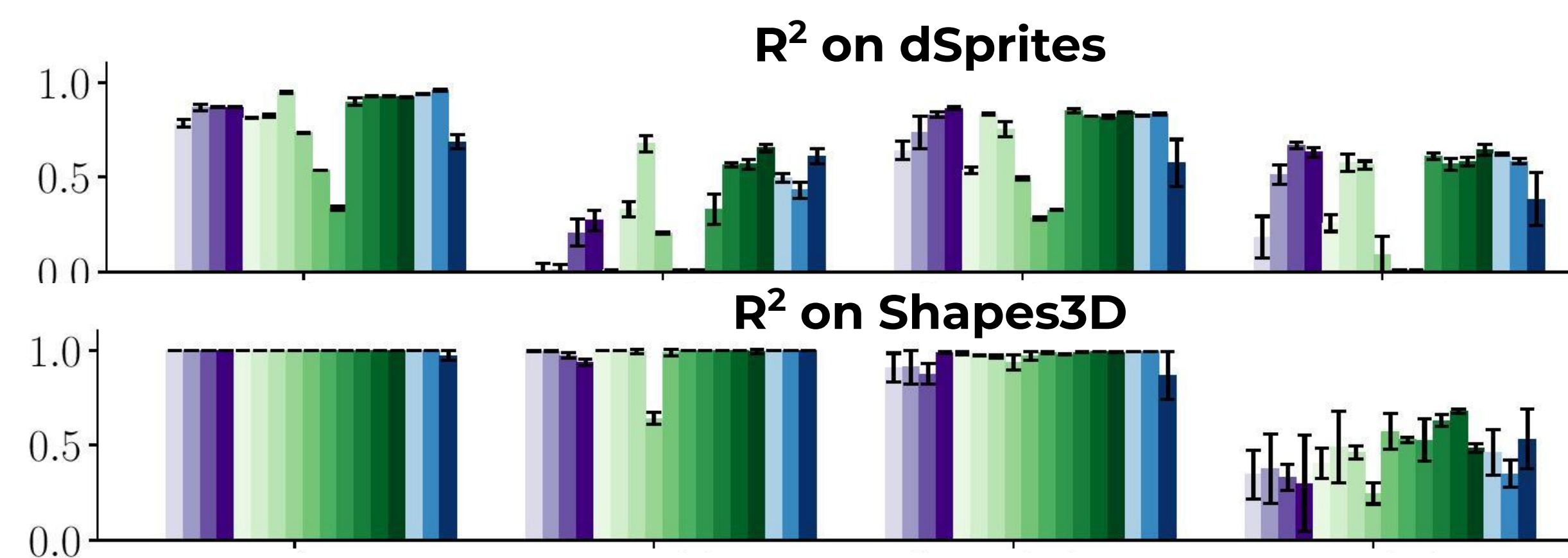
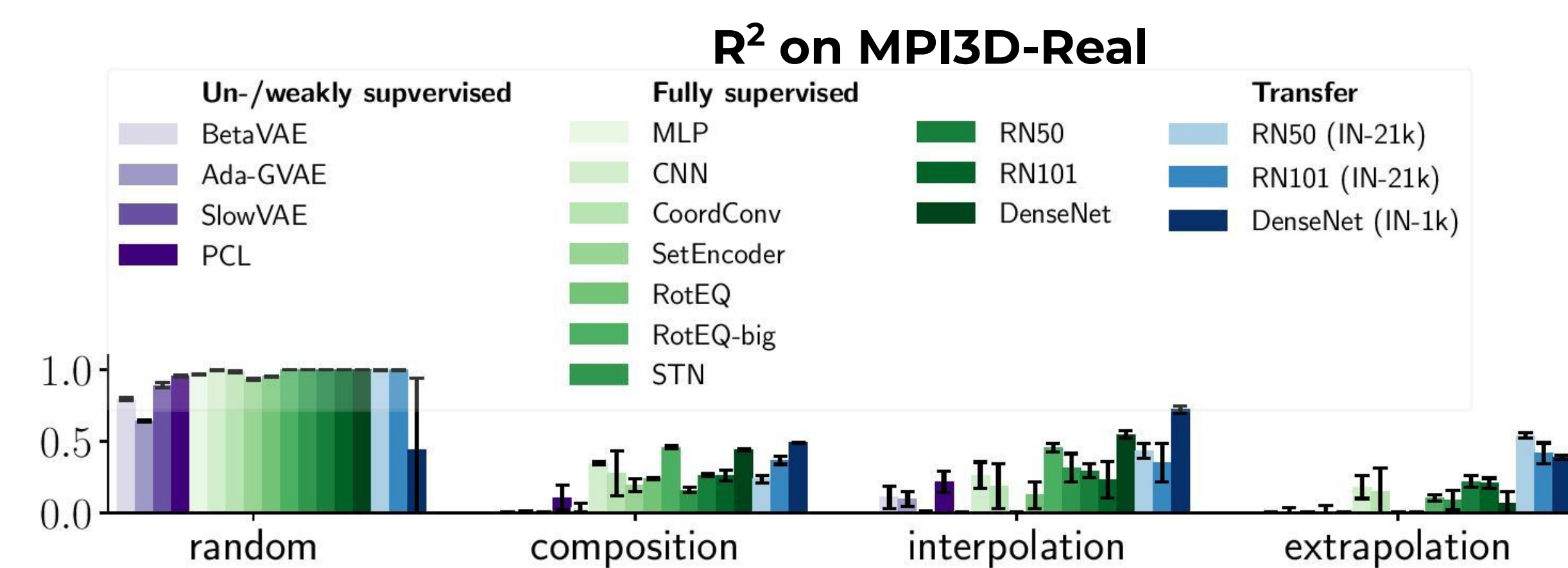
$$R_i^2 = 1 - \frac{\text{MSE}_i}{\sigma_i^2} \quad \text{MSE}_j = \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim p_{\text{te}}} \left[ (\mathbf{y}_j - f_j(\mathbf{x}))^2 \right]$$

$R^2 = 1$  → perfect regression, 100% variance explained

$R^2 = 0$  → e.g. always predicting the mean

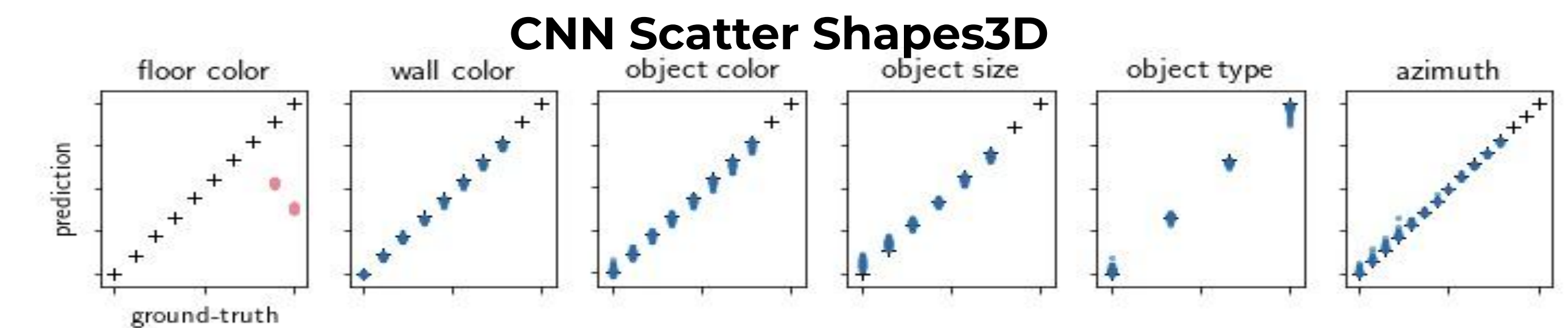
$R^2 < 0$  → worse than predicting the mean

## Results - All Models



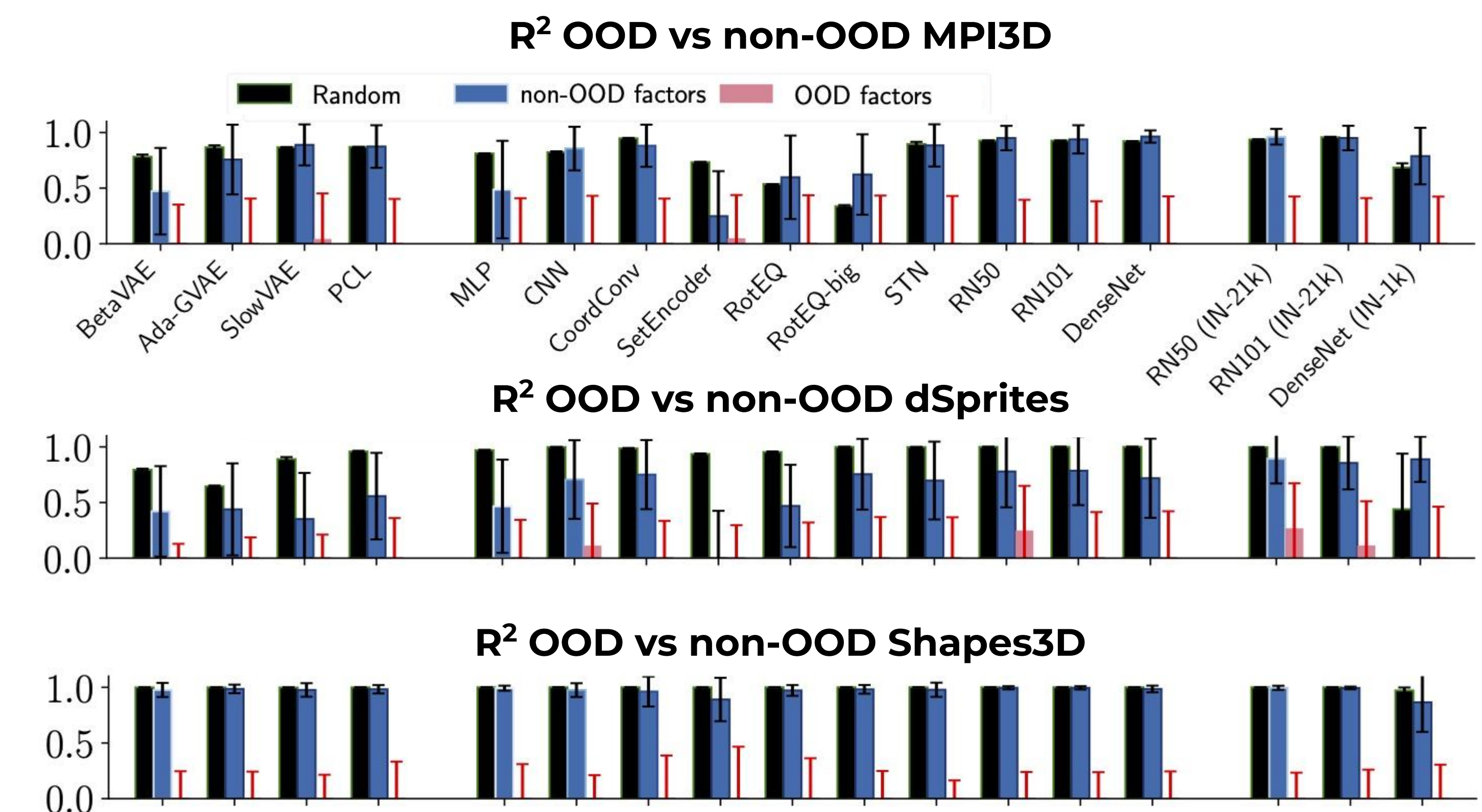
- On realistic dataset (MPI3D): Models do **not** learn underlying mechanism
- Shapes3D color composition/ interpolation works fairly well
- Extrapolation most difficult → investigate further

## Extrapolation - Qualitative



- OOD factors different behavior on non-OOD vs OOD factors
- OOD factors tend towards the mean

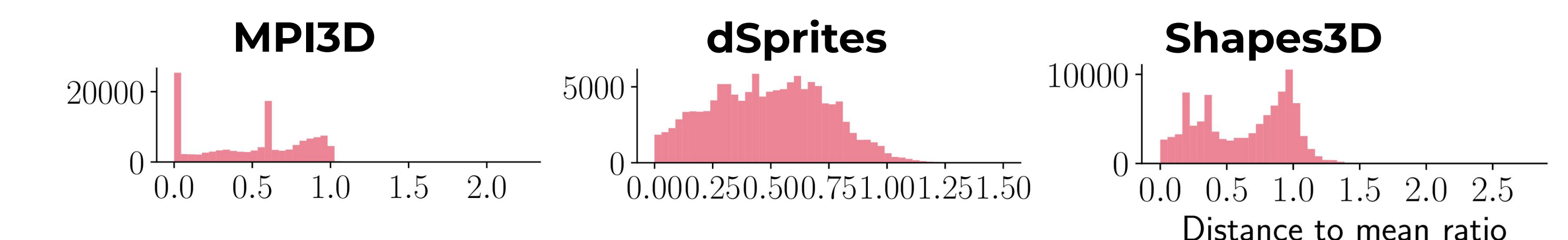
## Extrapolation - Error Analysis



- OOD factors  $R^2$  low → Models do not extrapolate
- non-OOD  $R^2$  better → Models are surprisingly modular

## Extrapolation Towards the Mean

$$\frac{|f(\mathbf{x}^i)_j - \bar{\mathbf{y}}_j|}{|\mathbf{y}^i_j - \bar{\mathbf{y}}_j|} \quad \begin{array}{l} \text{if in } [0, 1] \rightarrow \text{prediction closer to mean than ground-truth} \\ \text{if } > 1 \rightarrow \text{further away from mean} \end{array}$$



Values mostly in [0,1] → Models tend to extrapolate towards the mean

## Conclusions

- In more difficult settings, our tested ML models are unable to generalize and do not learn the underlying model.
- Models are surprisingly modular and tend to extrapolate towards the mean.
- On the non-artificial MPI3D we found transfer learning to be most helpful.

## References

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