A Study of Undefined Behavior Across Foreign Function Boundaries in Rust Libraries Appendix

July 26, 2024

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1 Results

Table 1: Download counts for each crate where a bug was found, sorted by "All-Time". The mean download count per day is aggregated across the 6 months between March 20th and September 20th, 2023.

Crate	Version	Mean 🕻 / Day	♣ All-Time	Last Updated	Bug IDs
flate2	1.0.27	136,292	82,637,795	2023-08-15	38
foreign-types	0.5.0	88,416	64,223,888	2019-10-13	33
bzip2	0.4.4	23,862	13,447,830	2023-01-05	34
zmq	0.10.0	1,594	1,824,174	2022-11-04	19
lcms2	6.0.0	363	158,000	2023-09-02	42, 43, 10
dec	0.4.8	237	118,377	2022-02-05	41, 22, 46, 47
tectonic engine bibtex	0.2.1	32	15,680	2023-06-15	27
special-fun	0.2.0	28	15,176	2019-03-15	9
littlefs2	0.4.0	40	14,288	2023-02-07	35, 36
librsync	0.2.3	3	12,350	2023-03-10	39
libhydrogen	0.4.1	23	12,264	2021-05-16	20
bad64	0.6.0	10	6,071	2021-12-22	26
fluidlite	0.2.1	6	5,768	2021-08-21	17
sgp4-rs	0.4.0	10	5,680	2023-07-19	28
minimap2-sys	$0.1.16^{1}$	15	3,782	2023-09-12	45
minimp3 ex-sys	0.1.1	14	3,192	2020-12-19	16
libcmark-sys	0.1.0	1	2,396	2017-11-30	12
dec-number-sys	0.0.25	8	1,400	2022-11-28	23, 32, 7
xxhrs	2.0.0	3	1,390	2020-09-15	48
tetsy-secp256k1	0.7.0	3	1,202	2021-02-19	29
bchlib	0.2.1	1	739	2019-05-27	11
tree-sitter-svelte	0.10.2	2	718	2022-04-15	14
everrs	0.2.1	2	650	2020-04-12	4
x42ltc-sys	0.0.5	1	648	2020-09-05	15
quickjs_regex	0.2.3	3	637	2021-11-30	5, 24, 24
crypto_pimitives	0.1.1	2	535	2019-11-17	21
klu-rs	0.4.0	2	530	2022-09-15	44
ytnef	0.2.0	6	521	2021-11-14	18
tinyspline-sys	0.2.0	1	441	2020-06-09	13
ms5837	0.2.1	2	377	2022-07-30	31
spritz_cipher	0.1.0	1	324	2019-10-16	8
mseed	0.5.0	4	318	2023-08-24	25
jh-rs	0.1.0	1	206	2021-01-31	1
lsmlite-rs	0.1.0	2	52	2023-07-17	30

 $^{^{1}0.1.16 +} minimap 2.2.26$

Table 2: Unique bugs detected by our tool, sorted Miri's error label ("Error Category") and our additional classification ("Error Type"). A "-" indicates that our classification is the same as Miri's label. When a commit is listed in the last column, it indicates that the bug has been fixed. If multiple commits were used to fix a bug, we provide the last commit in the series.

ID	Crate	Version	Error Category	Error Type	Fix	Error	Issue(s)	Pull(s)	Commit(s)
1	jh-rs	0.1.0	Alignment	Invalid Transmutation	Rust	Rust	#1		
2	quickjs_regex	0.2.3	Cross-Language Free	ı	LLVM	Rust	#2		
က	tree-sitter	0.20.3	Dangling Int Pointer	Null Pointer Dereference	LLVM	Γ	8#		4676cd4
4	everrs	0.2.1	Incorrect Binding	Incorrect Integer Width	Binding	Binding	#1		
ಬ	quickjs_regex	0.2.3	Incorrect Binding	Incorrect Integer Width	Binding	Binding		#1	
9	secp256k1	0.28.0	Incorrect Binding	Incorrect Integer Width	Binding	Binding	699#	029#	60a5e36
7	dec-number-sys	0.0.25	Incorrect Binding	Missing Return Type	Binding	Binding		#2	
∞	spritz_cipher	0.1.0	Incorrect Binding	Missing Return Type	Binding	Binding		#1	
6	special-fun	0.2.0	Incorrect Binding	Missing Return Type	Binding	Binding	#14	#13	ded37f8
10	lcms2	6.0.0	Invalid Enum Tag	Logical Error	Rust	Rust			85218b6
11	bchlib	0.2.1	Memory Leaked	Missing C Destructor	Rust	Rust	#1		
12	libcmark-sys	0.1.0	Memory Leaked	Missing C Destructor	Rust	Rust	#3		
13	tinyspline-sys	0.2.0	Memory Leaked	Missing C Destructor	Rust	Rust	#1		
14	tree-sitter-svelte	0.10.2	Memory Leaked	Missing C Destructor	Rust	Rust	#46		
15	x42ltc-sys	0.0.5	Memory Leaked	Missing C Destructor	Rust	Rust	#1	#2	1c594f2
16	minimp3_ex-sys	0.1.1	Memory Leaked	Missing C Destructor	Rust	Rust		42	33bea0d
17	fluidlite	0.2.1	Memory Leaked	Missing from Raw	Rust	Rust	#15		
18	ytnef	0.2.0	Memory Leaked	Missing from Raw	Rust	Rust	#1		
19	bmz	0.10.0	Memory Leaked	Missing from Raw	Rust	Rust	#387	#388	
20	libhydrogen	0.4.1	Memory Leaked	Missing from Raw	Rust	Rust	#11		bddff45
21	crypto_pimitives	0.1.1	Out of Bounds Access	1	LLVM	Rust	#1		
22	dec	0.4.8	Out of Bounds Access	1	LLVM	LLVM	92#		
23	dec-number-sys	0.0.25	Out of Bounds Access	1	LLVM	LLVM	92#		
24	quickjs_regex	0.2.3	Out of Bounds Access	1	LLVM	Rust		#1	
25	mseed	0.5.0	Out of Bounds Access	1	$\Gamma\Gamma\Lambda$ M	Rust			0cfede1
26	bad64	0.6.0	Out of Bounds Access	1	LLVM	$\Gamma\Gamma$			6dbd961
27	tectonic_engine_bibtex	0.2.1	Tree Borrows	Freeing Through &mut T	TLVM	Rust		#1129	c64e524
28	sgp4-rs	0.4.0	Tree Borrows	Incorrect Integer Width	LLVM	Binding	#29		
56	tetsy-secp256k1	0.7.0	Tree Borrows	Incorrect const	LLVM	Rust	#3		
30	lsmlite-rs	0.1.0	Tree Borrows	Incorrect const	LLVM	Binding		#2	2e0cf90
31	ms5837	0.2.1	Tree Borrows	Incorrect const	TLVM	Rust		#26	7be 05 c 1
32	dec-number-sys	0.0.25	Tree Borrows	Incorrect const	$\Gamma\Gamma\Lambda$ M	Binding	#1	#2	4a12cce
33	foreign-types	0.5.0	Tree Borrows	Phantom UnsafeCell <t></t>	$\Gamma\Gamma\Lambda$ M	Rust	#24		
34	bzip2	0.4.4	Tree Borrows	Sharing &mut T	TLVM	Rust	#94		
35	littlefs2	0.4.0	Tree Borrows	Sharing &mut T	$_{ m LLVM}$	Rust		#54	
								Continued	Continued on next page

Table 2 – continued from previous page

			Table 1	table 1 communed from providing page	,				
ID	Crate	Version	Error Category	Error Type	Fix	Error	$_{ m Issue(s)}$	Pull(s)	Commit(s)
36	littlefs2	0.4.0	Tree Borrows	Sharing &mut T	TLVM	Rust		#24	
37	Buds	0.2.0-alpha.2	Tree Borrows	Sharing &mut T	Rust	Rust	#11	#12	
38	flate2	1.0.27	Tree Borrows	Sharing &mut T	LLVM	Rust	#392	#394	0a584f4
39	librsync	0.2.3	Tree Borrows	&⊤ as *mut ⊤	Rust	Rust	#23		
40	blitsort-sys	0.1.0	Tree Borrows	&⊤ as *mut ⊤	TLVM	Rust	#1	#2	
41	dec	0.4.8	Tree Borrows	&T as *mut T	LLVM	Rust	#74	#2	ece7d84
42	lcms2	0.0.9	Tree Borrows	&⊤ as *mut ⊤	TLVM	Rust		#18	28626ed
43	lcms2	0.0.9	Tree Borrows	&⊤ as *mut ⊤	TLVM	Rust			5d3b648
44	klu-rs	0.4.0	Tree Borrows	&T as *mut T	LLVM	Rust		#1	c5e89d1
45	minimap2-sys	$0.1.16^{2}$	Uninitialized Memory	Erroneous Failure	Rust	Rust			2ac2a6d
46	dec	0.4.8	Uninitialized Memory	Incomplete Initialization	Rust	Rust	92#	22#	3545623
47	dec	0.4.8	Uninitialized Memory	Incomplete Initialization	LLVM	Rust	92#	22#	3545623
48	xxhrs	2.0.0	Uninitialized Memory	Uninitialized Padding	Rust	Rust		#10	def77e5

Table 3: Test results across each of the three evaluation modes. In the "Zeroed" mode, all stack and heap memory from LLVM is zero-initialized. In the "Uninitialized" mode, LLVM is allowed to read uninitialized bytes without throwing an error.

	Zeroed	ed	Uninitialized	dized
Error Type	Stacked Borrows Tree Borrows	Tree Borrows	Stacked Borrows Tree Borrows	Tree Borrows
Borrowing Violation	2.7% (245)	2% (184)	2.7%~(245)	2% (183)
Using Uninitialized Memory	2.2% (197)	2.2% (202)	2.2% (200)	2.2% (205)
Other Error	5.4% (495)	5.5% (501)	5.2% (479)	5.4% (490)
Passed	18.7% (1706)	18.9% (1724)	18.6% (1695)	18.7% (1710)
Timeout	9.7% (890)	10.6% (968)	9.6% (873)	10.4% (953)
Unsupported Operation	61.3% (5597)	60.8% (5551)	61.8% (5638)	61.2% (5589)

 2 +minimap2.2.26

2 Semantics

Rust LLVM

2.1 Domains

 $b \in \text{BYTES} \qquad \qquad (bytes) \\ m, n \in \mathbb{N} \cup \{0\} \qquad \qquad (sizes) \\ \ell \in \text{Locations} : \mathcal{P}(\text{Bytes}) \qquad \qquad (heap \ locations) \\ t \in \text{Tags} \qquad \qquad (access \ tags)$

2.2 Type Syntax

$$\tau ::= \operatorname{int}(n) \mid \operatorname{ptr} \mid \overline{\tau} \qquad (LLVM \ types)
\tau ::= \operatorname{int}(n) \mid *\tau \mid \tau^{p} \qquad (Rust \ types)
\tau^{p} ::= \overline{\langle \tau, n \rangle}^{m} \qquad (Rust \ products)
\tau ::= \tau \mid \tau \qquad (Types)$$

2.3 Value Syntax

$$v_b ::= \overline{b} \mid \langle \ell, \varrho \rangle$$
 (Base Values)
 $v ::= v_b \mid \langle \overline{v} \rangle$ (LLVM Values)
 $v ::= v_b$ (Rust Values)
 $\varrho ::= t \mid * \mid \cdot$ (Provenance)

2.4 Environments

 $\mu \in \text{Mem} : \text{Loc} \to (\text{Bytes} \times \text{Tag})$ (memory) $\sigma \in \text{TagSet} : \mathcal{P}(\text{Tag})$ (exposed tags)

2.5 Conversion

```
\mu; \sigma \vdash \mathbf{v} : \mathbf{\tau} \iff \mathbf{v} : \mathbf{\tau} \dashv \mu'; \sigma'
```

$$\begin{aligned} & \text{C-Pointer} \\ & \frac{\text{C-Int}}{\mu; \sigma \vdash \langle \ell, \varrho \rangle : \tau \leftrightsquigarrow \langle \ell, \varrho \rangle : \mathsf{ptr} \dashv \mu; \sigma} & \frac{\text{C-Int}}{\mu; \sigma \vdash \overline{b}^n} : \mathsf{int}(n) \leftrightsquigarrow \overline{b}^n : \mathsf{int}(n) \dashv \mu; \sigma \\ & \frac{\text{C-Product}}{\mathsf{fields}(\langle \ell, \varrho \rangle : \overline{\tau^p}^n) = \overline{v : \tau^p}^n}{\forall i \in [1, n]. \ \mu_{i-1}; \sigma_{i-1} \vdash v : \tau^p \leftrightsquigarrow v : \tau_i \dashv \mu_i; \sigma_i} \\ & \frac{\forall i \in [1, n]. \ \mu_{i-1}; \sigma_{i-1} \vdash v : \tau^p \leftrightsquigarrow v : \tau_i \dashv \mu_i; \sigma_i}{\mu_0, \sigma_0 \vdash \langle \ell, \varrho \rangle : \overline{\tau^p}^n \leftrightsquigarrow \langle \overline{v} \rangle : \overline{\tau}^n \dashv \mu_n; \sigma_n} \end{aligned}$$

[&]quot;Under the store μ and tag set σ , Rust values v of type τ and LLVM values v of type τ are interconvertible, producing the updated store μ' and tag set σ' ."

$$\mu; \sigma \vdash \mathbf{v} : \mathbf{\tau} \leadsto \mathbf{v} : \mathbf{\tau} \dashv \mu; \sigma'$$

"Under the store μ and tag set σ , Rust values v of type τ can be converted to LLVM values v of type τ , producing the updated tag set σ' "

$$\begin{split} & \text{C-PointerToInt} \\ & \underline{\ell \triangleq \overline{b}} \quad \text{expose}(\sigma, \varrho) = \sigma' \\ & \underline{\mu; \sigma \vdash \langle \ell, \varrho \rangle : *\tau \leadsto \overline{b} : \text{int}(n_{ptr}) \dashv \mu; \sigma'} \end{split}$$

$$\begin{array}{ll} \text{C-FieldToScalar} & \text{C-ProductToInt} \\ \mu; \sigma \vdash \mathsf{read}(\ell, \pmb{\tau}) = v_b \dashv \sigma'' & \mathsf{sizeof}(\pmb{\tau}^{\pmb{p}}) = q \\ \underline{\mu; \sigma'' \vdash v_b : \pmb{\tau} \leadsto v_b : \tau \dashv \mu; \sigma'} & \underline{\mu; \sigma \vdash \mathsf{read}(\ell, \mathsf{int}(q)) = \bar{b} \dashv \sigma'} \\ \underline{\mu; \sigma \vdash \langle \ell, \varrho \rangle : \langle \tau, 0 \rangle \leadsto v_b : \tau \dashv \mu; \sigma'} & \underline{\mu; \sigma \vdash \langle \ell, \varrho \rangle : \tau^p \leadsto \bar{b} : \mathsf{int}(q) \dashv \mu; \sigma'} \\ \end{array}$$

C-PRODUCTTOINT sizeof
$$(\tau^p) = q$$

$$\mu; \sigma \vdash \text{read}(\ell, \text{int}(q)) = \bar{b} \dashv \sigma'$$

$$\mu; \sigma \vdash \langle \ell, \rho \rangle : \tau^p \leadsto \bar{b} : \text{int}(q) \dashv \mu; \sigma'$$

$$\mu; \sigma \vdash \mathbf{v} : \mathbf{\tau} \leadsto \mathbf{v} : \mathbf{\tau} \dashv \mu; \sigma'$$

"Under the store μ and tag set σ , LLVM values \mathbf{v} of type τ can be converted to Rust values \mathbf{v} of type τ , producing the updated store μ' "

$$\begin{split} & \frac{\text{C-PointerFromInt}}{\ell \triangleq \overline{b}} \\ & \frac{\ell \triangleq \overline{b}}{\mu; \sigma \vdash \langle \ell, * \rangle : *\tau \iff \overline{b} : \text{int}(n_{ptr}) \dashv \mu; \sigma} \end{split}$$

C-FIELDFROMSCALAR
$$\mu'' \vdash \mathsf{write}(\ell, v_b) \dashv \mu'$$

$$\mu; \sigma \vdash v_b : \tau \leadsto v_b : \tau \dashv \mu''; \sigma$$

$$\mu; \sigma \vdash \langle \ell, \varrho \rangle : \langle \tau, 0 \rangle \leadsto v_b : \tau \dashv \mu'; \sigma$$

$$\begin{array}{ll} \mu'' \vdash \mathsf{write}(\ell, v_b) \dashv \mu' & \text{C-ProductFromInt} \\ \mu; \sigma \vdash v_b : \underline{\tau} \leadsto v_b : \underline{\tau} \dashv \mu''; \sigma & \text{sizeof}(\underline{\tau}^p) = q \quad \mu \vdash \mathsf{write}(\ell, \overline{b}) \dashv \mu' \\ \mu; \sigma \vdash \langle \ell, \varrho \rangle : \langle \tau, 0 \rangle \leadsto v_b : \underline{\tau} \dashv \mu'; \sigma & \mu; \sigma \vdash \langle \ell, \varrho \rangle : \underline{\tau}^p \leadsto \overline{b} : \mathsf{int}(q) \dashv \mu'; \sigma \end{array}$$

2.6 Store Operations

$$\mu(\ell) = \langle b, \varrho \rangle$$

"The store μ maps the location ℓ to the byte b with provenance ρ ."

Store
$$\ell \mapsto \langle b, \varrho \rangle \in \mu$$
 $\mu(\ell) = \langle b, \varrho \rangle$

$$\mu(\ell,m) = \overline{\langle b,\varrho\rangle}^m$$

"Reading a value of size m from location ℓ produces a list of m pairs of bytes and provenance values."

Store-Slice
$$\frac{\mu(\ell), \dots, \mu(\ell+m-1) = \overline{\langle b, \varrho \rangle}^m}{\mu(\ell, m) = \overline{\langle b, \varrho \rangle}^m}$$

$$\operatorname{expose}(\sigma,\varrho) = \sigma'$$

"Exposing the tag ρ produces the updated tag set σ' ."

$$\begin{array}{ll} \text{Ex-Tag} & \text{Ex-Null} & \text{Ex-Wild} \\ \text{expose}(\sigma,t) = \sigma \cup \{t\} & \text{expose}(\sigma,\cdot) = \sigma & \text{expose}(\sigma,*) = \sigma \end{array}$$

$$\mu \vdash \mathsf{write}(\ell, v) \dashv \mu'$$

"Writing the value v to the store μ at location ℓ produces the updated store μ' ."

$$\begin{aligned} & \text{W-Bytes} \\ & \ell \in \text{dom}(\mu_0) \\ & \underbrace{\forall i \in [0, n-1].\mu_{i+1} = \mu_i [\ell + i \mapsto \langle b_i, \cdot \rangle]}_{\mu_0 \vdash \text{write}(\ell, \overline{b}^n) \dashv \mu_n} \end{aligned} \end{aligned} \qquad \begin{aligned} & \text{W-Ptr} \\ & \ell \in \text{dom}(\mu_0) \quad \ell \triangleq \overline{b}^{n_{ptr}} \\ & \underbrace{\forall i \in [0, n_{ptr} - 1].\mu_{i+1} = \mu_i [\ell + i \mapsto \langle b_i, \varrho \rangle]}_{\mu_0 \vdash \text{write}(\ell, \langle \ell, \varrho \rangle) \dashv \mu_n} \end{aligned}$$

$$\mu; \sigma \vdash \mathsf{read}(\ell, \tau) = v \dashv \sigma'$$

"Reading a rust value v of type τ from the store μ at location ℓ produces the updated tag set σ' ."

$$\begin{array}{ll} \text{R-Int} & \text{R-Ptr} \\ \mu[\ell,n] = \overline{\langle b,\varrho\rangle}^n & \mu[\ell,n_{ptr}] = \overline{\langle b,\varrho\rangle}^{n_{ptr}} \\ \forall i \in [1,n]. \\ \exp(\sigma_{i-1},\varrho_i) = \sigma_i \\ \mu;\sigma_0 \vdash \operatorname{read}(\ell,\operatorname{int}(n)) = \overline{b}^n \dashv \sigma_n & \ell' \triangleq \overline{b}^{n_{ptr}} & \forall i \in [1,n_{ptr}].\varrho_i = \varrho' \\ \mu;\sigma \vdash \operatorname{read}(\ell,*\tau) = \langle \ell',\varrho'\rangle \dashv \sigma \end{array}$$

2.7 Metafunctions

 $\operatorname{sizeof}(\tau) = n$

"The type τ has size n."

$$\begin{array}{ll} \text{TS-Int} & \text{TS-R-Ptr} & \text{TS-L-Ptr} \\ \text{sizeof}(\text{int}(n)) = n & \text{sizeof}(*\tau) = n_{ptr} & \text{sizeof}(\text{ptr}) = n_{ptr} \\ \\ \text{TS-R-Field} & \text{TS-R-Prod} \\ \text{sizeof}(\tau) + m = n \\ \text{sizeof}(\langle \tau, m \rangle) = n & \\ \hline \text{sizeof}(\overline{\tau^p}^m) = n & \\ \hline \end{array} \qquad \begin{array}{l} \text{TS-L-Prod} \\ \frac{\sum_{i=1}^m (\text{sizeof}(\tau_i)) = n}{\text{sizeof}(\overline{\tau^p}^m) = n} & \\ \hline \end{array}$$

$scalar(\tau)$

$$\operatorname{scalar}(\operatorname{int}(n))$$
 $\operatorname{scalar}(*\tau)$ $\operatorname{scalar}(\operatorname{ptr})$

$$\mathsf{fields}(v: \tau^p) = \overline{v: \tau}$$

$$\frac{\forall i \in [1,n].o_i = \Sigma_{j=1}^{i-1}(\mathsf{sizeof}(\pmb{\tau^p}_j))}{\mathsf{fields}(\langle \ell,\varrho \rangle : \overline{\tau^p}^n) = \overline{\langle \ell + o_i,\varrho \rangle : \underline{\tau^p}_i}^n}$$

 $homogeneous(\tau)$

$$\frac{\exists \pmb{\tau}. \forall \langle \pmb{\tau}', n \rangle \in \pmb{\tau}^p. n = 0 \land \pmb{\tau}' = \pmb{\tau} \land \mathsf{homogeneous}(\pmb{\tau})}{\mathsf{homogeneous}(\pmb{\tau}^p)}$$

[&]quot;The type τ is a scalar."

[&]quot;The rust product value $v:\tau^p$ can be represented as a list of field values $v:\tau$ "

[&]quot;The type τ is a homogeneous aggregate."

$$\mathsf{equivalent}(\tau) = \tau'$$

"The type τ is equivalent to the type τ "

$$\mathsf{equivalent}(\tau_b) = \tau_b \qquad \qquad \mathsf{equivalent}(*\tau) = \mathsf{ptr} \qquad \qquad \mathsf{equivalent}(\mathsf{ptr}) = *\tau$$

2.8 Well-formedness

 $\vdash v : \tau$

"The typed value $v : \tau$ is well-formed."

2.9 Proofs

Lemma 2.9.1 (Canonical Forms). For all values v, if $\vdash v : \tau$, then

- 1. If $v \triangleq \overline{b}^n$, then $\tau \triangleq \operatorname{int}(n)$.
- 2. If $v \triangleq \langle \ell, \varrho \rangle$, then τ is either $*\tau$ or τ^p in Rust, or ptr in LLVM.
- 3. If $v \triangleq \langle \overline{v}^n \rangle$ then τ is an LLVM product type $\overline{\tau}^n$

Proof. By inspection of $\vdash v : \tau$.

Lemma 2.9.2 (Compatible Forms). For all Rust typed values $v : \tau$ and LLVM typed values $v : \tau$, if $\mu; \sigma \vdash v : \tau \leadsto v : \tau \dashv \mu; \sigma'$ then $v : \tau$ determines the possible forms of $v : \tau$.

- 1. If $\mathbf{v}: \boldsymbol{\tau} \triangleq \overline{b}^n : \operatorname{int}(n)$, then $\mathbf{v}: \boldsymbol{\tau} \triangleq \mathbf{v}: \boldsymbol{\tau}$
- 2. If $\mathbf{v}: \mathbf{\tau} \triangleq \langle \ell, \varrho \rangle : \mathbf{\tau}$, then $\mathbf{v}: \mathbf{\tau}$ is either:
 - (a) An opaque pointer of the form $\langle \ell, \varrho \rangle$: ptr.
 - (b) An integer of the form $\overline{b}^n : int(n)$.
 - (c) An LLVM product type $\langle \overline{v} \rangle : \overline{\tau}$.

Similarly, if μ ; $\sigma \vdash \mathbf{v} : \mathbf{\tau} \leftrightarrow \mathbf{v} : \mathbf{\tau} \dashv \mu'$; σ

then the form of $v:\tau$ determines the possible forms of $v:\tau$.

- 1. If $v : \tau \triangleq \overline{b}^n : \mathsf{int}(n)$, then $v : \tau$ is either:
 - (a) An integer value of the same form.
 - (b) A pointer value of the form $\langle \ell, * \rangle : *\tau$
 - (c) A Rust product value $\langle \ell, \varrho \rangle : \tau^p$ stored at some valid location ℓ .
- 2. If $v : \tau \triangleq \langle \ell, \varrho \rangle$: ptr, then $v : \tau$ is either:
 - (a) A Rust product value $\langle \ell, \varrho \rangle : \tau^p$ for some τ^p
 - (b) A Rust pointer value $\langle \ell, \varrho \rangle : *\tau$ for some τ .
- 3. If $v: \tau \triangleq \langle \overline{\tau} \rangle : \overline{\tau}$ then $v: \tau$ must be a Rust product value $\langle \ell, \varrho \rangle : \tau^p$ for some τ^p .

Proof. By Lemma 2.9.1 and inspection of the syntax for the value conversion judgement.

Lemma 2.9.3. For all well-formed, typed scalar values $v:\tau$ and all valid heap locations ℓ , we have:

$$\mu \vdash \mathsf{write}(\ell, v) \dashv \mu' \quad \Rightarrow \quad \mu'; \sigma \vdash \mathsf{read}(\ell, \tau) = v \dashv \sigma'$$

Proof. By inversion, guided by the structure of $v:\tau$. Since $v:\tau$ is a well-formed, scalar-typed value, we have $\vdash v:\tau$ and $\mathsf{scalar}(\tau)$. It follows that v is either a byte string \overline{b} or a pointer $\langle \ell',\varrho \rangle$ to some location ℓ with some provenance ϱ .

Case 1: $v \triangleq \overline{b}^n$

By Lemma 2.9.1 we have that $\tau \triangleq \operatorname{int}(n)$. By inversion of W-BYTES and for $i \in [0, n-1]$, the store μ' maps each location $\ell + i$ to the tuple $\langle b_{i+1}, \cdot \rangle$. By STORE and STORE-LIST, we have that

$$\mu'(\ell), \dots, \mu'(\ell+n-1) = \mu'(\ell,n) = \overline{\langle b, \cdot \rangle}^n$$

Exposing the null provenance of each byte leave σ unchanged (Ex-Null). We can now apply R-Int to read the original value \bar{b} back from the store.

Case 2: $v \triangleq \langle \ell, \varrho \rangle$

By Lemma 2.9.1 and since $\operatorname{scalar}(\tau)$, we have that τ is either $*\tau$ of ptr. Each are treated equivalently. We can implicitly convert the location ℓ into the byte string, \overline{b}_{ptr}^n , so we proceed as in the first case. However, instead of the null provenance, we have:

$$\mu'(\ell, n_{ptr}) = \overline{\langle b, \varrho \rangle}^{n_{ptr}}$$

Each ϱ_i is equivalent to the provenance ϱ of the pointer value. Now, we can apply R-PTR to reach our goal by reading the original value $\langle \ell, \varrho \rangle$ back from the store.

Theorem 2.9.1 (Conversion is semi-functional). For all well-typed values $v : \tau$ and $v : \tau$, there exists some heaps μ, μ' and tag sets σ, σ' such that

$$\mu; \sigma \vdash \mathbf{v} : \mathbf{\tau} \leadsto \mathbf{v} : \mathbf{\tau} \dashv \mu' \sigma \Rightarrow \mu'; \sigma \vdash \mathbf{v} : \mathbf{\tau} \leadsto \mathbf{v} : \mathbf{\tau} \dashv \mu' \sigma'$$

Converting an LLVM value to Rust may affect the heap, but it will not change the tag set. Likewise, converting a Rust value to LLVM may affect the tag set but it will not change the contents of the heap.

Case 1: $v : \tau \triangleq \overline{b} : \tau$

By Lemma 2.9.2, $v:\tau$ can take one of the following forms:

Subcase 1: $\mathbf{v}: \boldsymbol{\tau} \triangleq \bar{b}: \tau_b$

Both typed values are interconvertible by C-Int.

Subcase 2: $\mathbf{v} : \boldsymbol{\tau} \triangleq \langle \ell, * \rangle : \boldsymbol{\tau}$

By inversion of C-PtrfromInt, we have $\ell \triangleq \overline{b}$. We can now apply C-PtrtoInt to achieve our goal.

Subcase 3: $\mathbf{v} : \mathbf{\tau} \triangleq \langle \ell, * \rangle : \langle \mathbf{\tau}, 0 \rangle$ and scalar($\mathbf{\tau}$)

By inversion of C-FIELDFROMSCALAR, we have:

$$\mu; \sigma \vdash v_b : \tau \leadsto v_b : \tau \dashv \mu''; \sigma$$
 $\mu'' \vdash \mathsf{write}(\ell, \overline{b}) \dashv \mu'$ scalar (τ)

By the induction hypothesis and Lemma 2.9.3, we have:

$$\mu'\sigma \vdash \mathsf{read}(\ell, \tau) \dashv \mu'; \sigma'' \qquad \mu'; \sigma'' \vdash \tau \leadsto v_b \dashv \mu'; \sigma'$$

Now we can apply C-FIELDToSCALAR to reach our goal.

Subcase 4: $\mathbf{v}: \boldsymbol{\tau} \triangleq \langle \ell, * \rangle : \boldsymbol{\tau}^{\mathbf{p}}$

By inversion of C-PRODFROMINT, we have:

$$sizeof(\tau^p) = q \qquad \mu \dashv write(\ell, \bar{b}, \dashv)\mu'$$

By Lemma 2.9.3, we have:

$$\mu'\sigma \vdash \operatorname{read}(\ell, \tau) \dashv \mu'; \sigma'$$

We can apply C-ProdToInt to reach our goal.

Case 2: $v : \tau \triangleq \langle \ell, \varrho \rangle$: ptr

By Lemma 2.9.2, $\mathbf{v}: \boldsymbol{\tau}$ must take the following forms:

Subcase 1: $\mathbf{v} : \mathbf{\tau} \triangleq \langle \ell, \varrho \rangle : *\mathbf{\tau}$ for some $\mathbf{\tau}$

Both typed values are interconvertible by C-PointerFromPointer and C-AnyToPointer.

Subcase 2: $\mathbf{v}: \boldsymbol{\tau} \triangleq \langle \ell, \rho \rangle : \langle \boldsymbol{\tau}, 0 \rangle$ for some $\boldsymbol{\tau}$

Equivalent to Case 1, Subcase 3.

Case 3: $v : \tau \triangleq \langle \overline{v} \rangle : \overline{\tau}$

By Lemma 2.9.2, $v:\tau$ must be equivalent to $\langle \ell,\varrho\rangle:\tau^p$ for some τ^p , which is interconvertible by C-PRODUCT and the induction hypothesis.

Theorem 2.9.2 (Equal size is required). Value conversion will succeed if and only if Rust and LLVM values have the same size. For all well-typed values $v : \tau$ and $v : \tau$, if there exists some heaps μ, μ' and tag sets σ, σ' such that either

$$\mu; \sigma \vdash \mathbf{v} : \mathbf{\tau} \leadsto \mathbf{v} : \mathbf{\tau} \dashv \mu'; \sigma$$
 or $\mu; \sigma \vdash \mathbf{v} : \mathbf{\tau} \leadsto \mathbf{v} : \mathbf{\tau} \dashv \mu; \sigma'$

Then either $sizeof(\tau) = sizeof(\tau)$ or $\tau = ptr$. That is, conversion will get "stuck" (which is reported as undefined behavior) if the types on either side of the boundary have unequal size, unless the LLVM type is an opaque pointer.

Proof. By induction on value conversion. Cases in either direction are equivalent; here, we consider the forwards case (\leadsto) of a Rust value $\boldsymbol{v}:\boldsymbol{\tau}$ being converted into an LLVM value. By Lemma 2.9.2, if the Rust value is an integer such that $\boldsymbol{v}:\boldsymbol{\tau}\triangleq\bar{b}:\tau_b$, then the LLVM value has the same type, so size is preserved. The remaining cases involve products and pointers, where the Rust value takes the form $\langle \ell, \rho \rangle$ for some $\boldsymbol{\tau}$.

Case 1: $\tau \triangleq *\tau$

Then the the LLVM value is either an opaque pointer (C-POINTER) or an integer with a size equal to the size of a pointer (C-POINTERTOINT).

Case 2: $\tau \triangleq \langle \tau^p, 0 \rangle$

By inversion of FIELDTOSCALAR, the induction hypothesis, and TS-R-FIELD.

Case 3: $\tau \triangleq \tau^p, \tau : v \triangleq \overline{b} : int(q)$

By inversion of C-Product ToInt we have $sizeof(\tau^p) = q$, which is equal to the size of the value read from memory.

Case 4: $\tau \triangleq \tau^p, \tau : v \triangleq \langle \overline{v} \rangle : \overline{\tau}$

By inversion of C-Product and the induction hypothesis, size is preserved for each field, so size is preserved for the entire product.

2.10 Parameter Passing

Algorithm 1: Converting a list of LLVM arguments to Rust arguments.

```
// A list of typed values provided by Rust
R \leftarrow [\overline{\mathbf{v}, \mathbf{\tau}}^n];
// A list of LLVM types.
L \leftarrow [\overline{\tau}^n];
// A calling convention; either 'static' or 'variable'.
C \leftarrow c;
// The list of converted arguments
A \leftarrow [];
// The initial store and tag set.
\mathcal{S} \leftarrow \mu; \sigma;
while R is not empty do
     v_i : \tau_i \leftarrow \mathsf{next}(R);
    if L is not empty then
         \tau_j \leftarrow \mathsf{next}(L);
          if sizeof(\tau_i) = sizeof(\tau_j) then
               \mathcal{S} \leftarrow \mathcal{S}' where \mathcal{S} \vdash v_i : \tau_i \leadsto v_j : \tau_j \dashv \mathcal{S}';
               A \leftarrow A ++ [v_j : \tau_j];
               continue
          else
               /* We only expand homogeneous aggregates when converting from Rust; in
                    the other direction, we skip directly to an error.
               if \tau \triangleq \overline{\tau^p}^n and homogeneous(\tau) then
                    if len(L) \ge n + len(R) then
                         R \leftarrow R ++ [\mathsf{fields}(\boldsymbol{v}_i : \boldsymbol{\tau}_i)];
                         continue
                    end
               end
         end
     else
         if L is empty and C = \text{variable } and \operatorname{scalar}(\tau_i) \operatorname{then}
           L \leftarrow L ++ [\text{equivalent}(\tau_i)]; \text{ continue}
         end
     end
     error()
\mathbf{end}
```