Faulty LED seven-edge digit recognition

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Original problem

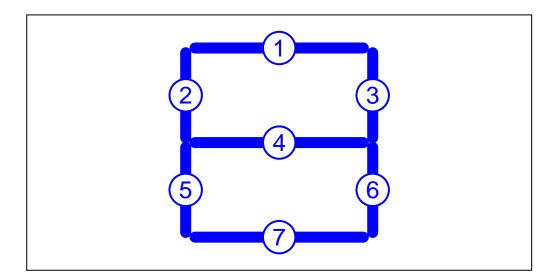
The problem involves representations of digits by seven LED lights which are selectively lit to form each digit. It is described in the book: Leo Breiman, Jerome Friedman, R.A. Olshen and Charles J. Stone (1984) Classification and Regression Trees (BFOS), p. 43-49.

Digits.plot.r contains auxiliary functions for visualizing them.

```
source("Digits.plot.r")
```

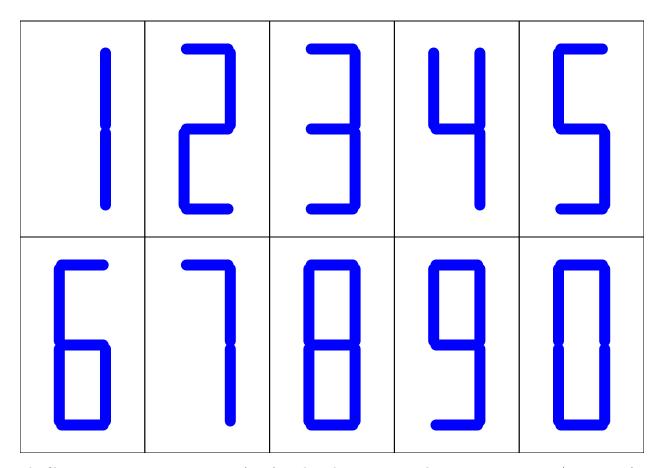
The figure below shows the numbering of the seven edges used to form the digits

```
options(repr.plot.width=4,repr.plot.height=4)
plot.digits.matrix.with.segment.indexes()
```



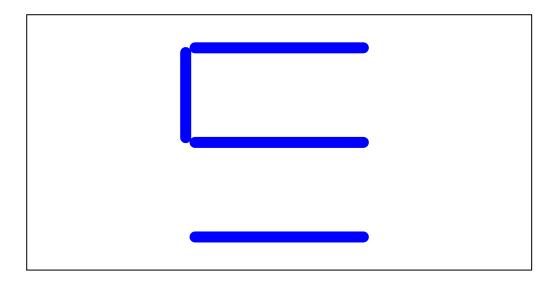
Here we see the ten digits, represented by the seven edges.

```
options(repr.plot.width=7.0,repr.plot.height=2.5)
show.all.digits()
```



The file digits.csv contains 500 sets (rows), each with seven ones and zeros, representing ON/OFF status for each of the seven edges, numbered as above, plus a label, the intended digit. Most rows, however, contain faulty edges, set ON when they should be OFF and vice-versa. For instance, the following picture shows a faulty '5' where the sixth edge failed to light on.

```
options(repr.plot.width=2.5,repr.plot.height=3.0)
v<-as.logical(c(1,1,0,1,0,0,1))
plot.faulty.digit(v)</pre>
```



Each row in digits.csv contains an additional variable, DIGIT, with the name of the intended digit.

```
digits.data<-read.csv("digits.csv")</pre>
str(digits.data)
## 'data.frame':
                   500 obs. of 8 variables:
## $ digit: Factor w/ 10 levels "eight", "five", ...: 6 5 3 9 1 5 2 7 9 1 ...
## $ x1
         : int 1001001111...
          : int 0011101001...
## $ x2
## $ x3
          : int 1 1 1 1 1 1 0 0 1 1 ...
                 0 0 1 1 1 0 1 1 1 1 ...
## $ x4
          : int
##
   $ x5
                 0 0 0 1 1 0 0 1 1 0 ...
          : int
## $ x6
          : int
                1 1 1 0 1 1 1 1 0 1 ...
          : int 0000101111...
## $ x7
levels(digits.data$digit)
## [1] "eight" "five" "four" "nine" "one"
                                                              "three" "two"
                                               "seven" "six"
## [10] "zero"
Better with shorter (and equal length) names for levels
#install.packages("dplyr", dependencies=TRUE, repos="https://cloud.r-project.org")
require(dplyr)
## Loading required package: dplyr
## Attaching package: 'dplyr'
```

```
## The following objects are masked from 'package:stats':
##
       filter, lag
##
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
digits.data$digit<-recode(digits.data$digit, "one"="1", "two"="2",
          "three"="3", "four"="4", "five"="5", "six"="6", "seven"="7",
          "eight"="8", "nine"="9", "zero"="0")
str(digits.data)
## 'data.frame':
                    500 obs. of 8 variables:
   $ digit: Factor w/ 10 levels "8", "5", "4", "9",...: 6 5 3 9 1 5 2 7 9 1 ...
           : int 1001001111...
##
   $ x1
                  0 0 1 1 1 0 1 0 0 1 ...
##
   $ x2
           : int
##
  $ x3
           : int
                 1 1 1 1 1 1 0 0 1 1 ...
##
  $ x4
           : int
                  0 0 1 1 1 0 1 1 1 1 ...
                  0 0 0 1 1 0 0 1 1 0 ...
##
   $ x5
           : int
##
   $ x6
                 1 1 1 0 1 1 1 1 0 1 ...
           : int
   $ x7
           : int
                  0 0 0 0 1 0 1 1 1 1 ...
table(digits.data$digit)
##
   8
      5 4 9 1 7 6 3 2 0
## 58 54 52 55 43 48 50 55 43 42
```

Generating more data

Possibly the digits.csv dataset is extracted from the collection of datasets in the *Splus* program. In the BFOS book they mention an (unpublished, I believe) training dataset with 200 observations and a test sample of 5000. The generator program by David W. Aha, in C, can be found at the UCI Machine Learning repository.

A better alternative is the rdigitsBFOS() function from the gencve package, which generates digits with a given flipping probability alpha (that is, the probability of one of the seven LEDs changing its correct status to the opposite one). As a bonus the function computes the Bayes optimal missclassification rate, which can be used to have an objective lower bound for the quality of any classification method.

```
#install.packages("gencve", dependencies=TRUE, repos="https://cloud.r-project.org")
require(gencve)
```

Loading required package: gencve