

## Problem A. AK the Problems

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

**Suzukaze**, a Codefalsers who has the **master** title, is now competing in a contest on Codefalsers. He has solved all the problems except the last one and there are only ten minutes left. This is a crucial contest to **Suzukaze** so he is asking for your help. The problem statement follows:

Two players are given a forest(undirected acyclic graph) and decide to play a game on it. The first player plays first and they take alternating turns. In each turn, the current player can either 1) delete an edge or 2) delete a vertex and the edges on it. Whoever is unable to make a move, loses. Determine who wins if they both play optimally.

If **Suzukaze** solves this last problem and AK the problemset, he will achieve a new title - **grandmaster**. However, if he fails on this problem, he will lose all the ratings and stop competing in any contests. Can you help him solve this problem?

### Input

The first line contains two integers  $n$  and  $m$  ( $1 \leq n \leq 10^5, 0 \leq m \leq n - 1$ ), the number of vertices in the forest and the number of edges in the forest. The vertices in the forest are labeled from 1 to  $n$ .

In the following  $m$  lines, each of the lines contains 2 integers  $u, v$  ( $1 \leq u, v \leq n; u \neq v$ ), which means that there is an undirected edge connecting vertex  $u$  and vertex  $v$ .

It's guaranteed that the input data is a forest.

### Output

If the first player will win the game, output "Suzukaze becomes a grandmaster!"(without quotes). Otherwise, output "Suzukaze loses all his ratings!"(without quotes).

### Examples

stdin	stdout
8 6 1 2 2 3 4 5 5 6 6 7 7 8	Suzukaze loses all his ratings!
stdin	stdout
2 1 1 2	Suzukaze becomes a grandmaster!

## Problem B. Bigram Language Model

Input file: `stdin`  
Output file: `stdout`  
Time limit: 5 seconds  
Memory limit: 256 MB

In natural language processing, language models gives how likely a certain English sentence appear in a context (e.g. casual conversations, academic papers, or news websites) by assigning a probability distribution over all possible sentences. Bigram language model approaches this modeling problem by estimating the transition probabilities from previous word to next word. Formally,

$$P(S = w_1 w_2 \dots w_m) = P(w_1)P(w_2 | w_1) \dots P(w_m | w_{m-1})$$

We can estimate transition probabilities from word  $s$  to  $t$  from a corpus (a collection of sentences) collected from the context:

$$P(t | s) = \frac{c(s, t)}{\sum_{t' \in V} c(s, t')}$$

where  $V$  denotes the vocabulary (aka set of all words in the corpus), and  $c(s, t)$  denotes the total number of times that word  $t$  comes right after word  $s$  in the same sentence in the corpus.

**Suzukaze** has collected a corpus and is trying to compute the probability of some sentences. He needs your help to get some transition probabilities. Can you help him?

### Input

The first line contains an integer  $n$  ( $1 \leq n \leq 1000$ ), the number of sentences in the corpus.

In the following  $n$  lines, the  $i$ -th line starts with an integer  $m_i$  ( $1 \leq m_i \leq 100$ ), the number of words in the  $i$ -th sentence. It is then followed by  $m_i$  space-separated words.

The next line contains an integer  $q$  ( $1 \leq q \leq 10^4$ ), the number of queries.

In the following  $q$  lines, each line contains two space-separated words  $s$  and  $t$ , querying for the estimated transition probability from word  $s$  to  $t$ .

All words in the corpus and queries are no more than 10 characters long and contain lowercase letters only.

### Output

For each query, output a line containing the estimated transition probability for the queried word pair. Print the number as an irreducible fraction. (See example for details)

If you cannot estimate the transition probability from the corpus, print "Insufficient data" instead.

## Examples

stdin	stdout
5	1/1
7 get busy living or get busy dying	1/2
4 stay hungry stay foolish	1/1
6 whatever you do do it well	Insufficient data
6 everything you can imagine is real	1/2
5 the things you can find	1/3
8	2/3
get busy	0/1
busy living	
hungry stay	
foolish stay	
do do	
you do	
you can	
can do	

## Problem C. Corns

Input file: `stdin`  
Output file: `stdout`  
Time limit: 3 seconds  
Memory limit: 256 MB

**pittoresque** is a corn lover and he eats corns every day. One day he visited a new corn shop and decided to purchase some corns for his meal. **pittoresque** brought a  $W$  dollar bill with him and he always spends as much money as he can to buy corns. To be specific, **pittoresque** wants to choose some corns such that the sum of their price is no larger than  $W$ , and is maximum among all possible choices of corns.

### Input

The first line contains two integers  $n$  and  $W$  ( $1 \leq n \leq 2 \times 10^5$ ,  $1 \leq W \leq 2 \times 10^5$ ), the number of corns and the bill **pittoresque** brought.

In the following  $n$  lines, the  $i$ -th line contains a single integer  $p_i$  ( $1 \leq p_i \leq 2 \times 10^5$ ), the price of corn  $i$ .

It is guaranteed that  $\sum_i p_i \leq 2 * 10^5$ .

### Output

Output the maximum sum of price of corns that **pittoresque** can purchase.

### Examples

stdin	stdout
3 10 1 1 11	2

  

stdin	stdout
4 10 3 5 3 4	10

## Problem D. Diameter

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

**pittoresque** loves playing a game called Cover'em all. In this game, he is given some points on a 2-D grid, and he finds some straight segments that together cover all the points. Now after finishing finding the segments, **pittoresque** is bored and wants to find something interesting about the points. Specifically, he wants to know what's the maximum (square-euclidean) distance between two points among all pair of points in this grid.

Squared-euclidean distance between two points  $(x_1, y_1), (x_2, y_2)$  is defined as  $(x_1 - x_2)^2 + (y_1 - y_2)^2$

### Input

The first line contains two integers  $n$  and  $k$  ( $2 \leq n \leq 10^5$ ,  $1 \leq k \leq 500$ ), the number of points and the number of segments.

In the following  $k$  sections, the first line of each section contains a single integer  $m_i$  ( $1 \leq m_i$ ), the number of points on segment  $i$ . And the following  $m_i$  lines contains a pair of integer  $x_{ij}, y_{ij}$  ( $-10^9 \leq x_{ij}, y_{ij} \leq 10^9$ ). It is guaranteed that these points are on a common segment.

It is also guaranteed that  $\sum_{i=1}^k m_i = n$ . It is **NOT** guaranteed that the points are in order on a segment, and it is **NOT** guaranteed that the points don't collide with another.

### Output

Output the maximum *square*-euclidean distance among all pairs of points.

### Examples

stdin	stdout
5 2 3 1 2 2 3 3 4 2 1 0 10 0	85
stdin	stdout
4 1 4 1 2 2 3 3 4 4 5	18

## Problem E. Egma Game

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

As we all know, **TiChuot97** is *one of* the greatest professional gamers of all time. And, similar to other great gamers, he loves games, especially nim games. Today, he just found out an online nim game - Egma. As other nim games, Egma requires proficiency in computing mex values in order to master it. **TiChuot97** understands that, just like millions of other games he mastered, Egma requires practicing. This is where his best friend, **tourist**, comes in to help.

**tourist** has prepared a drill for **TiChuot97**'s practice. Initially, **TiChuot97** is given an array of size  $n$  of nonnegative integers  $a_1, a_2, \dots, a_n$ . Then, **tourist** will give **TiChuot97**  $q$  queries each consists of two numbers  $l, r$  ( $1 \leq l \leq r \leq n$ ) asking for the mex of  $\{a_l, a_{l+1}, \dots, a_r\}$ . Of course, **TiChuot97** finished this drill easily. However, he thinks that this challenge can improve, not only his mex-computing skill, but also his programming skill. Do you also want to give this challenge a try?

**Note:** Mex value of a set of nonnegative integers is defined to be the minimum nonnegative integer that does not belong to the set.

### Input

The first line contains an integer  $n$  ( $1 \leq n \leq 5 \times 10^5$ ), the length of the initial array. The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $0 \leq a_i \leq 10^9$ ). The third line contains an integers  $q$  ( $1 \leq q \leq 5 \times 10^5$ ), the number of queries. Each of the next  $q$  lines contain a pair  $l, r$  ( $1 \leq l \leq r \leq n$ ) describing a query.

### Output

For each query, output on one line the answer to such query.

### Examples

stdin	stdout
5	0
1 2 3 0 5	4
2	
1 3	
1 4	

## Problem F. Fruit on the Tree

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

“Triangoes”, a new type of fruit, are in triangular shapes and taste like mangoes. However, nobody in the world has ever seen “triangoes” since they always grow implicitly on the tree and hide in the triangles. Formally, a “triango” tree is an acyclic undirected connected graph with weighted edges and a “triango” is a set of three vertices on the “triango” tree such that the lengths of the three simple paths between each pair of these three vertices satisfy the triangle inequality; that is to say, they form a triangle.

After a long expedition, **Suzukaze** has eventually found a “triango” tree in his house. He needs your help to count the number of “triangoes” on the “triango” tree. Can you help him?

### Input

The first line contains an integer  $n$  ( $1 \leq n \leq 10^5$ ), the number of vertices on the “triango” tree. The vertices on the “triango” tree are labeled from 1 to  $n$ .

In the following  $n - 1$  lines, each of the lines contains 3 integers  $u, v, w$  ( $1 \leq u, v \leq n, u \neq v, 1 \leq w \leq 10^5$ ), which means that there is an undirected edge with weight  $w$  connecting vertex  $u$  and vertex  $v$ .

It’s guaranteed that the input data is an acyclic undirected connected graph.

### Output

Output an integer - the number of “triangoes” on the “triango” tree.

### Examples

stdin	stdout
7 1 2 1 1 3 1 2 4 1 2 5 1 3 6 1 3 7 1	8

## Problem G. Greenberg Mass Comparison

Input file: `stdin`  
Output file: `stdout`  
Time limit: 1 second  
Memory limit: 256 MB

Linguist Joseph Greenberg proposed the method of mass comparison for determining genetic relatedness between languages. In this method,  $N$  languages are categorized into one or more families. Formally, given a set of  $N$  different languages  $\mathcal{L} = \{L_1, \dots, L_N\}$ , a relation analysis is a set of families  $\mathcal{F}$ , satisfying the following properties:

- $\mathcal{F} = \{F_1, \dots, F_k\}$  for some  $k$
- For  $1 \leq i \leq k$ ,  $F_i \subseteq \mathcal{L}$  and  $F_i \neq \emptyset$
- For  $1 \leq i, j \leq k, i \neq j$ ,  $F_i \cap F_j = \emptyset$
- $\cup_{1 \leq i \leq k} F_i = \mathcal{L}$

Greenberg wants to know how many distinct relation analysis are there for  $N$  languages. Two relation analyses  $\mathcal{F}_1$  and  $\mathcal{F}_2$  are distinct if  $\mathcal{F}_1 \neq \mathcal{F}_2$ . Can you help him compute this number?

### Input

The first line of input contains a single integer  $T$  ( $1 \leq T \leq 100$ ), the number of test cases. In the following  $T$  lines, each line contains a single integer  $N$  ( $1 \leq N \leq 100$ ).

### Output

For each test case, output a line containing the answer for the queried  $N$ , modulo  $(10^9 + 7)$ .

### Examples

stdin	stdout
4	1
1	2
2	5
3	840750853
40	



## Problem H. Hamiltonian Farm

Input file: `stdin`  
Output file: `stdout`  
Time limit: 3 seconds  
Memory limit: 256 MB

Last year, your team failed on helping the Codefalsar **Suzukaze** AK the problemset. Therefore, **Suzukaze** decided to retire from competitive programming and became a farmer since he wants to own a farm as **pittoresque** does. **Suzukaze** is an orange-lover so he decided to plant only orange trees in his farm in spring. Winter is coming next week! **Suzukaze** is planning to walk inside his farm to harvest his favorite fruit. However, as a forgetful farmer, **Suzukaze** loses his memory about the configuration of his farm. Fortunately, as a careful programmer, **Suzukaze** stored the configuration of his farm in the computer as a function in case of he gets into this kind of desperate situation.

The farm can be modelled as a graph with  $n$  vertices where vertices are orange trees, and the edges in the graph can be derived from the function  $f$ :

$$f(i, j) = \begin{cases} 0 & i = j \\ ((ip)^{jq} \bmod (10^9 + 7)) \bmod 2 & i < j \\ 1 - f(j, i) & i > j \end{cases}$$

where  $i$  and  $j$  are the indices of the vertices ( $1 \leq i, j \leq n$ ),  $p$  and  $q$  are non-negative integers less than  $10^9 + 7$ . If  $f(i, j) = 1$ , there is a directed edge from  $i$  to  $j$ .

As a lazy farmer, **Suzukaze** wants to find a path that can visit each orange tree exactly once. Can you help him find this path in compensation for your failure last year?

### Input

The first line contains three integers  $n$ ,  $p$  and  $q$  ( $1 \leq n \leq 10^5$ ,  $0 \leq p, q < 10^9 + 7$ ,  $p$  and  $q$  can't be 0 at the same time), the number of orange trees and the parameters of the function. You may assume that the orange trees have indices  $1, \dots, n$ .

### Output

If the path exists, output the vertices on the path from the beginning vertex to the end vertex as the example shows. Any of the path that satisfies **Suzukaze**'s demand will be accepted. Otherwise, output -1, which means that you fail on **Suzukaze**'s request again.

### Examples

stdin	stdout
6 1 1	1 3 5 6 4 2

### Explanation

The path  $1 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$  satisfies **Suzukaze**'s demand in the example.

## Problem I. Innovative Alignment

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

**Stringers** can only read books if the  $i$ 'th word of consecutive sentences start at the same position. If this condition is not met, they cannot read their books, and get rather upset. Can you help the **Stringers** by aligning all the given words correctly?

### Input

The first line contains one integer  $n$  ( $1 \leq n \leq 10$ ), representing the number of sentences you will be given to align.

The next  $n$  lines that follow contain the sentences to align. Each sentence contains up to 10 words, and each word has up to 10 characters. The alphabet for this problem will only consist of uppercase and lowercase English letters.

### Output

Output the correct alignment of the input strings, such that the  $i$ 'th word of each sentence starts at the same index. Note that when aligning words, there is always a space between the longest  $i$ 'th word of any sentence and the first position of the alignment of the  $i + 1$ 'th words. Please take a look at the examples (specifically the second) below for clarification.

### Examples

stdin	stdout
2 Hello World UoI IPL	Hello World UoI IPL

  

stdin	stdout
3 Align my life plz CTCI sucks Welcome to check in	Align my life plz CTCI sucks Welcome to check in

### Explanation

In the second example, the most important thing to note is the space between the second 's' in 'sucks' and the first alignment position for 'life' and 'check' (i.e. you can think about the index of the second 's' in 'sucks' is 12 and the index of the beginning of 'life' and 'check' is 14).

## Problem J. Juicy

Input file: `stdin`  
Output file: `stdout`  
Time limit: 5 seconds  
Memory limit: 256 MB

Farmer **pittoresque** has a farm planted with two types of fruit, apples and bananas. Every fall, **pittoresque** needs to walk inside his farm to harvest these delicious fruits. However, as a banana-lover, **pittoresque** only cares about collecting bananas and doesn't care about how many apples he harvested.

The farm can be modelled as a graph where vertices are apple trees or banana trees, and there is an additional vertex indicating the entrance of the farm. To prepare for harvesting, **pittoresque** needs to build (bidirectional) roads throughout his farm between vertices. The roads must be built such that it is possible to reach every banana tree from the entrance. As a dedicated person, **pittoresque** gains some happiness during road building, despite spending some energy. Energy and happiness may be different for different roads. Nevertheless, **pittoresque** doesn't want to build roads that form a cycle, nor does he want to build roads that he cannot reach. Finally, **pittoresque** wants to maximize the ratio of sum of all happiness gained and sum of all energy consumed after he build the roads.

### Input

The first line contains two integers  $a$  and  $b$  ( $0 \leq a \leq 10$ ,  $1 \leq b \leq 100$ ), the number of apple trees and the number of banana trees. You may assume that the apple trees have index  $1, \dots, a$ , the banana trees have index  $a + 1, \dots, a + b$  and the entrance have index  $a + b + 1$ .

Next line contains a single integer  $m$ ,  $b \leq m \leq 1000$ , the number of roads that can be built.

Next  $m$  lines contain information about the roads that can be built. Each line contains four integers  $u, v, h, e$ ,  $1 \leq u, v \leq a + b + 1$ ,  $u \neq v$ ,  $0 \leq h \leq 10^6$ ,  $1 \leq e \leq 10^6$ . This means that if a road connecting  $u$  and  $v$  is built,  $e$  energy is consumed and  $h$  happiness is gained.

It is guaranteed that it is possible to reach every banana tree from the entrance. Between two vertices, multiple roads may exist.

### Output

The maximum ratio between sum of all happiness gained and sum of all energy consumed, among all configuration of road building that satisfy the aforementioned constraints, can be expressed as  $P/Q$ , where  $P$  and  $Q$  are integers and they are co-prime. For your convenience, you just need to output  $P \times Q$ .

## Examples

stdin	stdout
1 3 4 1 2 10 1 2 3 10 1 3 4 10 1 1 5 10 1	10

stdin	stdout
1 3 5 1 2 100000 1 2 3 0 20 3 4 1 1 4 5 1 1 2 5 1 400	2300046

## Problem K. Koolhash

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

**tourist** has thought of a new hashing function to store administrator records, and he's enlisted you to help him build it! His hash function  $\phi(n)$  will output a single integer, and needs the following pieces of information:  $l$ ,  $r$ , and  $N$ , where  $l$  represents the leftmost bit of  $n$ ,  $r$  represents the rightmost bit of  $n$ , and  $N$  represents the number of 1-bits in  $n$ .

There aren't too many administrator records, so for now let's assume an unsigned 32-bit number system. Your job is to provide **tourist** with the three components of his hashing function given the number of records  $k$ , and the unique identifier of each record  $n$ . And yes, please forget about the absurdity of his hashing algorithm. Unfortunately, **tourist** has never taken a formal CS class.

### Input

The first line contains the number of records  $k$ ,  $1 \leq k \leq 500$ .

Each of the next  $k$  lines contains an integer representing a record identifier  $n$ ,  $0 \leq n < 2^{31}$ .

You can assume all inputs are given in decimal, and you need to convert them into 32-bits unsigned integers to get  $l$ ,  $r$  and  $N$  for each  $n$ .

### Output

On each line, print three space-separated integers for every input record, denoting the leftmost bit  $l$  of  $n$ , the rightmost bit  $r$  of  $n$ , and number of 1-bits  $N$  of  $n$ , respectively.

For further clarification, see the explanation provided for the first example below.

### Examples

stdin	stdout
1 8	0 0 1

  

stdin	stdout
3 45 68 23	0 1 4 0 0 2 0 1 4

### Explanation

For the first example, 8 is represented as `0x00000008` (written in hexadecimal for simplicity). Thus, the left most bit is 0, the right most bit is 0, and the number of 1-bits is 1.

## Problem L. Larger-Smaller Country

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 MB

**TiChuot97** loves travelling. In fact, it's his 4<sub>th</sub> most favourite hobby. This time, **TiChuot97** decides to visit the Country of Larger-Smaller (or LS for short). LS consists of  $n$  cities numbered from 1 to  $n$ . Interestingly, city  $i$  is assigned a distinct value  $a_i$ . Moreover, these cities are of 2 types:

1. A city  $i$  of this type can only travel to another city  $j$  if  $a_i < a_j$ .
2. A city  $i$  of this type can only travel to another city  $j$  if  $a_i > a_j$ .

Since each city in LS has its own culture and is very interesting to see, **TiChuot97** wants to visit all the cities, each exactly once. His trip will start from city 1 and will end at city  $n$ . As a competitive programmer, **TiChuot97** always practices, even while travelling. This time, he wants to count the number of ways he can schedule his trip given the information above. Can you help him?

Since the answer can be large, you only need to output its remainder when divided by  $10^9 + 7$ .

### Input

The first line contains an integer  $n$  ( $1 \leq n \leq 5000$ ), the number of cities. The second line contains  $n$  distinct integers,  $a_1, a_2, \dots, a_n$ , denoting the values assigned to these cities ( $1 \leq a_i \leq 10^9$ ). The third line, contains  $n$  integers  $b_1, b_2, \dots, b_n$  where  $b_i$  denotes the type of the  $i$ <sub>th</sub> city ( $1 \leq b_i \leq 2$ ).

### Output

Output on 1 line an integer which is the desired value modulo  $10^9 + 7$ .

### Examples

stdin	stdout
4 2 3 4 1 1 2 2 1	1