Control Challenges: Solutions

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1 Introduction

1.1 What is this?

This is a collection of write ups on how to solve the various problems presented by Github user "Janismac".

$$\dot{x} = \mathbb{A}x + \mathbb{B}u$$

2 Block With Friction

Position Control with friction. Using Pole Placement + PD.

2.1 State Space representation

We can convert the set of ODE into a state space representation. The final bode plot of the block position is:

```
using DiscretePIDs, ControlSystems, Plots, LinearAlgebra
# System parameters
Ts = 0.02 # sampling time
Tf = 2.5; #final simulation time
g = 9.81 \#gravity
\alpha = 0.0 \# slope
\mu = 1.0 \# friction coefficient
x_0 = -2.0 # starting position
dx_0 = 0.0 \# starting velocity
\tau = 20.0 \text{ # torque constant}
# State Space Matrix
A = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}
    0 - \mu 1
    0 0 -τ
] * 1.0;
B = [0]
    \tau] * 1.0;
C = [1 \ 0 \ 0]
    0 1 0] * 1.0
sys = ss(A, B, C, 0) # Continuous
bodeplot(tf(sys))
```

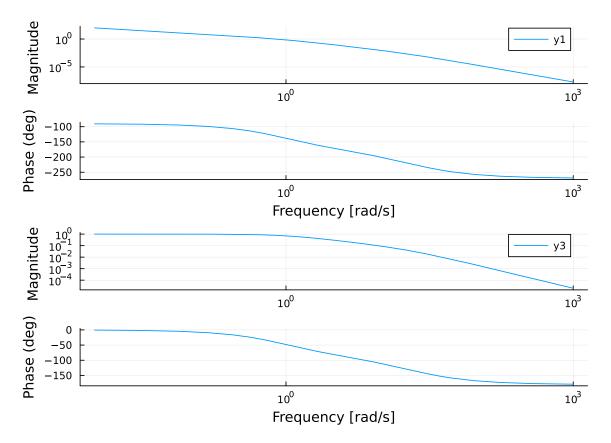


Figure 2.1: Starting Bode Plot

It has the shape we expect from a motor + friction. Slow pole for the mass + friction and a faster pole for the current & inductance.

Numerically they are:

```
display(eigvals(A)) # -20 , -1, 0
display(pzmap(tf(sys)))
```

-20.0 -1.0 0.0 (a) Starting PZ map Pole-zero map

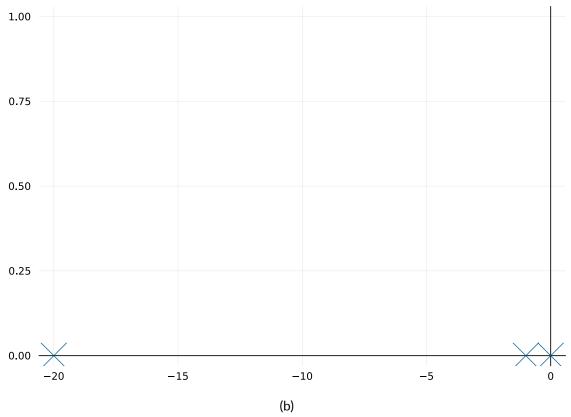


Figure 2.2

In Figure 2.2 we see that we start with all the pole in the left-half plane, which is good.

2.2 Pole Placement

3-element Vector{Float64}:

We can design a controller with pole placement.

For some reason pole placement doesn't work for the observer, I use a Kalman Filter with random fast values.

```
observability(A, C).isobservable & controllability(A, B).iscontrollable; #OK

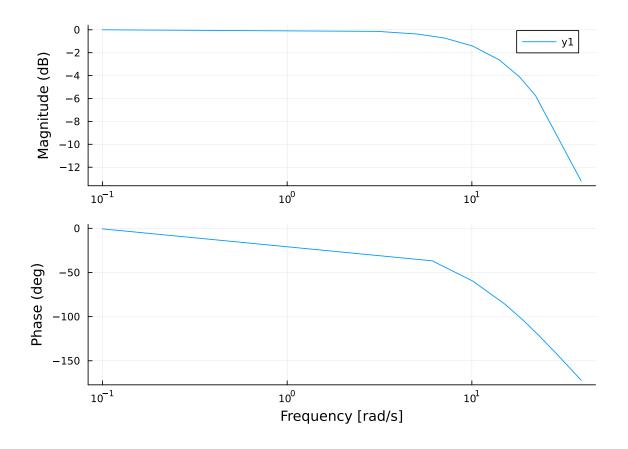
D = 0.01;
pp = 15;
poles_cont = -2.0 * [pp + D, pp - D, pp];
L = real(place(sys, poles_cont, :c));

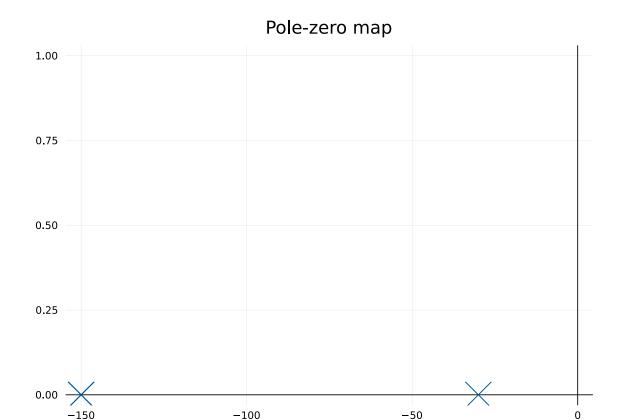
poles_obs = poles_cont * 5.0;
K = place(1.0 * A', 1.0 * C', poles_obs)'
cont = observer_controller(sys, L, K; direct=false);
```

We can check the effect of the new controller on the loop

```
closedLoop = feedback(sys * cont)
print(poles(closedLoop));
setPlotScale("dB")
display(bodeplot(closedLoop[1, 1], 0.1:40))
display(pzmap(closedLoop))
```

```
ComplexF64[-29.980000105166976 + 0.0im, -29.999999789554334 + 0.0im, -
30.020000105278555 + 0.0im, -150.00000000000000 + 0.0im, -150.0999999988327 + 0.0
149.9000000010167 + 0.0im]
```





We can compare this to the open-loop response in Figure 2.1. We can see that we achieve unitary gain throughout the whole low-frequency range.

We can convert the pole placement controller into the standard PD gain form.

```
K = L[1];
Ti = 0;
Td = L[2] / L[1];
pid = DiscretePID(; K, Ts, Ti, Td);
```

2.3 Simulation

We can simulate this with a motor that only outputs the position:

```
sysreal = ss(A, B, [1 0 0], 0)
ctrl = function (x, t)
   y = (sysreal.C*x)[] # measurement
   d = 0 * [1.0] # disturbance
   r = 2 * (t ≥ 1) # reference
   # u = pid(r, y) # control signal
```

```
# u + d # Plant input is control signal + disturbance
# u =1
e = x - [r; 0; 0]
e[3] = 0 # torque not observable, just ignore it in the final feedback
u = -L * e + d
u = [maximum([-20 minimum([20 u])])]
end
t = 0:Ts:Tf

res = lsim(sysreal, ctrl, t)
plot(res, plotu=true, plotx=true, ploty=false);
ylabel!("u", sp=1);
ylabel!("x", sp=2);
ylabel!("v", sp=3);
ylabel!("T", sp=4);
```

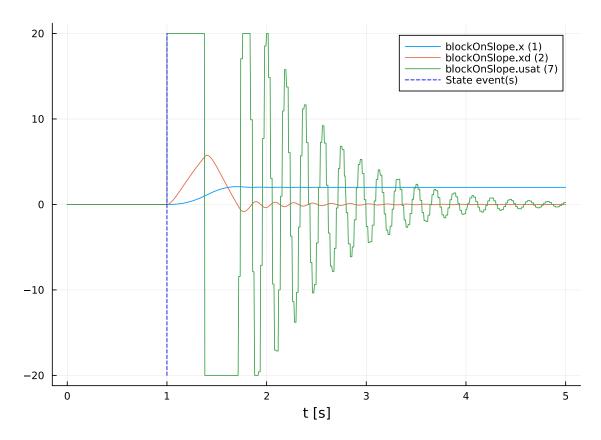
For more stats:

```
si = stepinfo(res);
plot(si);
title!("Step Response");
```

We can also simulate it in a SIMULINK-like environment:

```
using FMI, DifferentialEquations
fmu = loadFMU(abspath("../modelica/ControlChallenges/ControlChallenges.BlockOnSlope
simData = simulateME(fmu, (0.0, 5.0);
    recordValues=["blockOnSlope.x", "blockOnSlope.xd", "blockOnSlope.usat"]);
unloadFMU(fmu);
plot(simData, states=false, timeEvents=false)
```

```
Simulating ME-FMU ... 0%| | ETA: N/ASimulating ME-FMU ... 100%| | ETA:
```



There is a slight difference between the lsim simulation and the FMU simulation. I need to recheck some stuff.