Ecoadvisor model formulas

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Compilation command (bash)

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groff -e -t -ms formulas.ms -T pdf -K utf-8
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1. State Variables

1.1. Inputs

$$Q \qquad \text{(ML/d)}$$

$$S_{VFA}, S_{FBSO}, X_{BPO}, X_{UPO}, S_{USO}, X_{iSS}, S_{FSA}, S_{OP}, S_{NOx} \qquad \text{(mg/L)}$$

1.2. Total chemical oxygen demand (COD = S_t)

$$S_t = S_{VFA} + S_{FBSO} + X_{BPO} + X_{UPO} + S_{USO} \qquad \text{(mg/L)}$$

also:

$$\begin{aligned}
S_t &= S_b + S_u = S_s + S_p = S_{bs} + S_{bp} + S_{up} + S_{us} \\
S_b &= S_{bs} + S_{bp} \\
S_u &= S_{us} + S_{up} \\
S_s &= S_{bs} + S_{us} \\
S_p &= S_{bp} + S_{up} \\
S_{bs} &= S_{VFA} + S_{FBSO} \\
S_{bp} &= X_{BPO} \\
S_{up} &= X_{UPO} \\
S_{us} &= S_{USO}
\end{aligned}$$

1.3. Mass ratios for COD, N, P and C

State Variable	COD (f_{cv})	N (f_N)	P (f_P)	C (f_C)
S_{VFA}	1.0667	0.0000	0.0000	0.400
S_{FBSO}	1.4200	0.0464	0.0118	0.471
X_{BPO}	1.5230	0.0323	0.0072	0.498
X_{UPO}	1.4810	0.1000	0.0250	0.518
S_{USO}	1.4930	0.0366	0.0000	0.498
OHO	1.4810	0.1000	0.0250	0.518
ANO	1.4810	0.1000	0.0250	0.518
PAO	1.4810	0.1000	0.0250	0.518

1.4. Total Kjeldahl Nitrogen (TKN = N_t)

$$N_t = N_o + S_{FSA} \qquad \text{(mg/L)}$$

where:

$$\begin{aligned}
N_o &= N_{obs} + N_{obp} + N_{ous} + N_{oup} \\
N_{obs} &= S_{VFA}\,\frac{f_{N_{VFA}}}{f_{cv_{VFA}}} + S_{FBSO}\,\frac{f_{N_{FBSO}}}{f_{cv_{FBSO}}} \\
N_{obp} &= X_{BPO}\,\frac{f_{N_{BPO}}}{f_{cv_{BPO}}} \\
N_{ous} &= S_{USO}\,\frac{f_{N_{USO}}}{f_{cv_{USO}}} \\
N_{oup} &= X_{UPO}\,\frac{f_{N_{UPO}}}{f_{cv_{UPO}}}
\end{aligned}$$

1.5. Total Phosphorus (TP = P_t)

$$P_t = P_o + S_{OP} \qquad \text{(mg/L)}$$

where:

$$P_o = P_{obs} + P_{obp} + P_{ous} + P_{oup}$$
$$P_{obs} = S_{VFA}\frac{f_{P_{VFA}}}{f_{cv_{VFA}}} + S_{FBSO}\frac{f_{P_{FBSO}}}{f_{cv_{FBSO}}}$$
$$P_{obp} = X_{BPO}\frac{f_{P_{BPO}}}{f_{cv_{BPO}}}$$
$$P_{ous} = S_{USO}\frac{f_{P_{USO}}}{f_{cv_{USO}}}$$
$$P_{oup} = X_{UPO}\frac{f_{P_{UPO}}}{f_{cv_{UPO}}}$$

1.6. Total Organic Carbon (TOC =C_t)

$$C_t = C_{obs} + C_{obp} + C_{ous} + C_{oup} \qquad \text{(mg/L)}$$

where:

$$C_{obs} = S_{VFA}\frac{f_{C_{VFA}}}{f_{cv_{VFA}}} + S_{FBSO}\frac{f_{C_{FBSO}}}{f_{cv_{FBSO}}}$$
$$C_{obp} = X_{BPO}\frac{f_{C_{BPO}}}{f_{cv_{BPO}}}$$
$$C_{ous} = S_{USO}\frac{f_{C_{USO}}}{f_{cv_{USO}}}$$
$$C_{oup} = X_{UPO}\frac{f_{C_{UPO}}}{f_{cv_{UPO}}}$$

1.7. Total suspended solids (TSS = X_T)

$$X_T = X_V + X_{iSS} \qquad \text{(mg/L)}$$

where:

$$X_V = \frac{X_{BPO}}{f_{cv_{BPO}}} + \frac{X_{UPO}}{f_{cv_{UPO}}}$$

2. Activated sludge

2.1. Inputs

$$T, V_p, R_s, RAS, mass_{FeCl_3}$$

2.2. Volatile suspended solids (VSS)

$$Y_H = 0.45 \qquad \text{(gVSS/gCOD)}$$

$$b_H = 0.24 \qquad \text{(1/d)}$$

$$b_{HT} = b_H(1.029)^{T-20} \qquad \text{(1/d)}$$

$$f_{X_{BH}} = \frac{Y_H \cdot R_s}{1 + b_{HT} \cdot R_s} \qquad \text{(gVSS·d/gCOD)}$$

$$k_{vT} = 0.007 \cdot (1.035)^{T-20} \qquad \text{(L/mgVSS·d)}$$

$$S_{nd} = \frac{1}{f_{X_{BH}} k_{vT}} \qquad \text{(mg/L)}$$

$$FdS_{bi} = FS_{bi} - Q \cdot S_{nd} \qquad \text{(mg/L)}$$

$$MX_{BH} = FdS_{bi} \cdot f_{X_{BH}} \qquad \text{(kgVSS)}$$

$$MX_{EH} = f_H \cdot b_{HT} \cdot R_s \cdot MX_{BH} \qquad \text{(kgVSS)}$$

$$MX_I = FX_{Ti} \cdot R_s \qquad \text{(kgVSS)}$$

$$MX_V = MX_{BH} + MX_{EH} + MX_I \qquad \text{(kgVSS)}$$

$$X_V = \frac{MX_V}{V_p} \qquad \text{(kgVSS/m}^3\text{)}$$

2.3. Total inert solids (iSS)

$$f_{iOHO} = 0.15 \qquad \text{(giSS/gVSS)}$$

$$MX_{IO} = FiSS \cdot R_s + f_{iOHO} \cdot MX_{BH} + F_{iSS\_precipitation} \cdot R_s \qquad \text{(kgiSS)}$$

2.4. Total suspended solids (TSS)

$$MX_T = MX_V + MX_{IO} \qquad \text{(kgTSS)}$$

$$X_T = \frac{MX_T}{V_p} \qquad \text{(kgTSS/m}^3\text{)}$$

2.5. Nominal hydraulic retention time

$$HRT = \frac{V_p}{Q} \qquad \text{(d)}$$

2.6. Wastage flowrate

$$Q_w = \frac{V_p}{R_s} \qquad \text{(ML/d)}$$

2.7. Effluent flowrate

$$Q_e = Q - Q_w \qquad \text{(ML/d)}$$

2.8. Nitrogen and Phosphorus required for sludge production

$$N_s = \frac{f_{N_{OHO}}(MX_{BH} + MX_{EH}) + f_{N_{UPO}} MX_I}{R_s \cdot Q} \qquad \text{(mg/L)}$$

$$P_s = \frac{f_{P_{OHO}}(MX_{BH} + MX_{EH}) + f_{P_{UPO}} MX_I}{R_s \cdot Q} \qquad \text{(mg/L)}$$

2.9. Effluent Ammonia concentration

$$N_{ae} = N_{ti} - N_s - N_{ouse} \qquad \text{(mg/L)}$$

2.10. Effluent Orthophosphate concentration

$$P_{se} = P_{ti} - P_s - P_{ouse} - P_{precipitation} \qquad \text{(mg/L)}$$

2.11. Wastage solids concentration

$$BPO_{was} = f_{cv_{BPO}}(1 - f_H)X_{BH} \qquad \text{(mg/L)}$$

$$UPO_{was} = f_{cv_{UPO}}(f_H X_{BH} + X_{EH} + X_I) \qquad \text{(mg/L)}$$

$$iSS_{was} = \frac{MX_{IO}}{V_p} \qquad \text{(mg/L)}$$

2.12. Oxygen demand

$$FO_c = Y_H(1 - f_{cv_{OHO}}) + f_{cv_{OHO}}(1 - f_H) \cdot b_{HT} \cdot f_{X_{BH}} \qquad \text{(kgO/d)}$$

$$FO_n = 4.57 \cdot Q \cdot N_{ae} \qquad \text{(kgO/d)}$$

$$FO_t = FO_c + FO_n \qquad \text{(kgO/d)}$$

$$OUR = \frac{FO_t}{V_p} \qquad \text{(mgO/L·h)}$$

3. Nitrification

3.1. Inputs

$$SF,\ f_{xt},DO,\ pH$$

3.2. Nitrifier kinetics

$$\mu_{Am} = 0.45 \qquad \text{(1/d)}$$

$$\mu_{AmT} = \mu_{Am}(1.123)^{T-20} \qquad \text{(1/d)}$$

$$K_O = 0.3 \qquad \text{(mgO/L)}$$

$$\mu_{AmO} = \mu_{AmT}\frac{DO}{K_O + DO} \qquad \text{(1/d)}$$

$$K_i = 1.13, K_{ii} = 0.3, K_{\max} = 9.5$$

$$\mu_{AmpH} = \mu_{AmO}(2.35)^{pH-7.2}K_i\frac{K_{\max} - pH}{K_{\max} + K_{ii} - pH} \qquad \text{(1/d)}$$

$$Y_A = 0.1 \qquad \text{(gVSS/gNH4)}$$

$$Y_{AT} = Y_A^{T-20} \qquad \text{(gVSS/gNH4)}$$

$$K_n = 1.0 \qquad \text{(mg/L)}$$

$$K_{nT} = K_n(1.123)^{T-20} \qquad \text{(mg/L)}$$

$$b_A = 0.04 \qquad \text{(1/d)}$$

$$b_{AT} = b_A(1.029)^{T-20} \qquad \text{(1/d)}$$

3.3. Maximum design unaerated sludge mass fraction

$$f_{xm} = 1 - SF\frac{b_{AT} + \frac{1}{R_s}}{\mu_{AmpH}} \qquad \text{(ø)}$$

3.4. Minimum sludge age for nitrification

$$R_{sm} = \frac{1}{\mu_{AmpH}(1 - f_{xt}) - b_{AT}} \qquad \text{(d)}$$

3.5. Effluent Ammonia concentration

$$N_{ae} = \frac{K_{nT}(b_{AT} + \frac{1}{R_s})}{\mu_{AmpH}(1 - f_{xt}) - b_{AT} - \frac{1}{R_s}} \qquad \text{(mg/L)}$$

3.6. Nitrification capacity

$$N_c = N_{ti} - N_s - (N_{ae} + N_{ouse}) \qquad \text{(mg/L)}$$

3.7. ANO biomass

$$f_{X_{BA}} = \frac{Y_{AT} R_s}{1 + b_{AT} \cdot R_s} \qquad \text{(gVSS·d/gNH4)}$$

$$MX_{BA} = Q \cdot N_c \cdot f_{X_{BA}} \qquad \text{(kgVSS)}$$

$$X_{BA} = \frac{MX_{BA}}{V_p} \qquad \text{(kgVSS/m}^3\text{)}$$

4. Denitrification

4.1. Inputs

$$IR, DO_{RAS}, alk_i$$

4.2. Denitrification kinetics

$$K_1^{20} = 0.72, K_2^{20} = 0.10, K_3^{20} = 0.10, K_4^{20} = 0.00 \qquad \text{(mgN/mgVSS·d)}$$

$$K_{1T} = K_1^{20}(1.200)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

$$K_{2T} = K_2^{20}(1.080)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

$$K_{3T} = K_3^{20}(1.029)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

$$K_{4T} = K_4^{20}(1.029)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

4.3. Denitrification potential

$$D_{p1RBSO} = \frac{S_{bsi}(1 - f_{cv}Y_H)}{2.86} \qquad \text{(mgN/L)}$$

$$D_{p1BPO} = K_{2T}\, f_{xt}(S_{bi} - S_{nd})\, f_{X_{BH}} \qquad \text{(mgN/L)}$$

$$D_{p1} = D_{p1RBSO} + D_{p1BPO} \qquad \text{(mgN/L)}$$

4.4. Optimum internal recirculation

$$a_{opt} = \frac{-B + \sqrt{B^2 + 4AC}}{2A} \qquad (\text{ø})$$

where:

$$A = \frac{DO}{2.86}$$
$$B = N_c - D_{p1} + \frac{(1 + RAS)\cdot DO + RAS\cdot DO_{RAS}}{2.86}$$
$$C = (1 + RAS)\cdot(D_{p1} - \frac{RAS\cdot DO_{RAS}}{2.86}) - RAS\cdot N_c$$

4.5. Minimum (optimum) effluent nitrate concentration

$$N_{ne\_opt} = \frac{N_c}{a_{opt} + RAS + 1} \qquad \text{(mgN/L)}$$

4.6. Effluent nitrate (N_{ne})

$if\,(a < a_{opt})$

$$N_{ne} = \frac{N_c}{a + RAS + 1} \qquad \text{(mgN/L)}$$

$if\,(a > a_{opt})$

$$N_{ne} = N_c - D_{p1} + \frac{a \cdot DO + RAS \cdot DO_{RAS}}{2.86} \qquad \text{(mgN/L)}$$

4.7. Nitrogen gas production (FN_2)

$$FN_2 = Q(N_c - N_{ne}) \qquad \text{(kgN/d)}$$

4.8. Oxygen recovered by denitrification

$$FO_d = 2.86 \cdot Q \cdot (N_c - N_{ne}) \qquad \text{(kgO/d)}$$

$$FO_t = FO_c + FO_n - FO_d \qquad \text{(kgO/d)}$$

4.9. Effluent alkalinity

$$alk_e = alk_i + 3.57 \cdot (N_{obi} - (N_s - N_{oupi})) - 7.14 \cdot N_c + 2.86 \cdot (N_c - N_{ne}) \qquad \text{(mg/L)}$$