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A dynamic physicochemical model for chemical phosphorus removal



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ABSTRACT

A dynamic physico-chemical model for chemical phosphorus removal in wastewater is presented as a tool to optimize chemical dosing simultaneously while ensuring compliant effluent phosphorus concentration. This new model predicts the kinetic and stoichiometric variable processes of precipitation of hydrous ferric oxides (HFO), phosphates adsorption and co-precipitation. It is combined with chemical equilibrium and physical precipitation reactions in order to model observed bulk dynamics in terms of pH. The model is calibrated and validated based on previous studies and experimental data from Smith et al. (2008) and Szabo et al. (2008) as a first step for full-plant implementation. The simulation results show that the structure of the model describes adequately the mechanisms of adsorption and co-precipitation of phosphate species onto HFO and that the model is robust under various experimental conditions.

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1. Introduction

Phosphate adsorption

Achieving phosphorus removal from wastewater to very low levels is often performed by metal salt addition. Iron dosage leads to rapid hydrous ferric oxide (HFO, close to 2-line ferrihydrite) precipitation. Phosphorus may then be removed from

the bulk solution through different pathways: 1) adsorption of phosphates onto HFO by sharing an oxygen atom with iron; 2) co-precipitation of phosphate species into the HFO structure; 3) precipitation of ferric phosphate and 4) precipitation of mixed cation phosphates (Smith et al., 2008). The engineering stakes for this process consist of ensuring compliant effluent phosphorus concentrations, while at the same time saving

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chemicals and limiting chemical sludge production. Furthermore, high doses of metal salts cause bulk pH decrease by metal hydrolysis reactions and decrease the buffer capacity due to phosphate entrapment (<u>Caravelli et al.</u>, 2010) and carbon dioxide stripping.

Modelling is a commonly used engineering tool to handle such issues. However, metal salt precipitation such as iron dosing is not well described in current wastewater process models. Existing chemical phosphorus removal models are mainly focused on ferric phosphate precipitation (Fytianos et al., 1998). However, this pathway occurs only at acidic pH (below pH 5) as demonstrated by Smith et al. (2008) and based on literature solubility data (NIST, 2001). Luedecke et al. (1989) proposed an equilibrium model that includes acid/base reactions, hydrolysis of ferric ions and adsorption of phosphate on precipitates, considering an adsorption coefficient proportional to the ratio of the amount of adsorbed phosphates over the amount of adsorbent and the involved ions concentrations. However this ratio was adjusted to each experimental condition in a broad range (0.28–4.3 e^{-12} mol² L^{-2}), indicating that the adsorption process is not correctly described. This can be partly explained by the variation of adsorption capacity of ferric compounds due to aging process demonstrated by Smith et al. (2008) and Bligh and Waite (2010). Therefore a new model is required to predict HFO precipitation, pH modifications through chemical equilibrium and phosphates adsorption and co-precipitation onto/into HFO.

The combination of very fast (chemical equilibrium) and slow (kinetic precipitation/adsorption) reactions, variable molar ratios, multiple dosage points, the effect of mixing, colloidal material conversions and multiple precipitates requires a new modelling framework. This framework can then be applied to full plant process models to optimize doses and dosage locations and increase the safety of effluent compliance. Consequently, a dynamic physicochemical model for chemical phosphorus removal was developed and calibrated based on previous studies and experimental data from Smith et al. (2008) and Szabo et al. (2008) as a first step before full-

plant implementation. Furthermore, this study is focused on chemical phosphorus removal in aerobic plants and consequently on ferric iron (Fe³⁺) processes.

2. Model development

A fully kinetic framework was used during development to simplify the model structure, meaning that chemical equilibrium dissociation processes are modelled dynamically with very fast rates as described in Musvoto et al. (2000). Five process types were included in the model: 1) chemical equilibrium dissociation (CED) processes (6 CED processes) that include water dissociation, carbonate, and phosphate acidbase systems. These kinetics are based on Loewenthal et al. (1989) and Musvoto et al. (2000); 2) chemical ion paring (CIP) processes (11 CIP processes) for ions present in the system (Fe, Ca) with kinetics based on Loewenthal et al. (1989) and Musvoto et al. (2000); 3) physical mineral precipitation (PMP) process (2 PMP process: HFO and FePO4 precipitation) with kinetic rate expressions built as in Musvoto et al. (2000); 4) chemical surface complexation (CSC) onto HFO processes (8 CSC processes) and 5) HFO aging processes (4 HFO processes).

All the reactions considered in the model are listed in Table 1, and the model concepts are described in more details below. The state variables related to these reactions are expressed in mol $\rm L^{-1}$. The standardised notation from Corominas et al. (2010) has been used to name the state variables and parameters introduced in this model.

2.1. The physico-chemical model

The Gujer Matrix for the first two modules, namely the chemical equilibrium dissociation and chemical ion paring processes is presented in Appendix D. The kinetic rate expressions for chemical equilibrium dissociation are based on Musvoto et al. (2000), reverse and forward reactions being merged into a single process rate in order to reduce the number of modelled processes. The values of thermodynamic

Table 1 - Reactions considered in the kinetic pH model, chemical ion paring and precipitation model. 1) Chemical Equilibrium Dissociation 3) Physical Mineral Precipitation $H_2O \leftrightarrow H^+ + OH^-$ PMP 1 HFO_pre $Fe(OH)_{3,aq} \longleftrightarrow Fe(OH)_{3(s)}$ CED 01 H2O $Fe^{3+} + PO_4^{3-} \leftrightarrow FePO_4$ $H_2CO_3 \leftrightarrow H^+ + HCO_3$ CED_02_H2CO3 PMP_2_FePO4 $HCO_3 \leftrightarrow H^+ + CO_3^2$ CED 03 HCO3 CED 04 H3PO4 $H_3PO_4 \leftrightarrow H^+ + H_2PO_4^-$ 4) Chemical Surface Complexation $H_2PO_4^- \leftrightarrow H^+ + HPO_4^{-2}$ $HPO_4^{-2} \leftrightarrow H^+ + PO_4^{-3}$ CED 05 H2PO4 CSC 01 HFOH HPO4 adsorption of CED_06_HPO4 CSC 02 HFOH H2PO4 phosphates onto CSC 03 HFOH_H3PO4 2) Chemical Ion Paring $X_{HFO,H}$ $Ca^{2+} + OH^{-} \leftrightarrow CaOH^{+}$ Protonation of X_{HFO,H} CIP 01 CaOH CSC 04 HFOH H CIP 02 CaCO3 $Ca^{2+} + CO_3^{2-} \leftrightarrow CaCO_3$ CSC 05 HFOL HPO4 adsorption of $Ca^{2+} + HCO_3^- \leftrightarrow CaHCO_3^+$ CIP 03 CaHCO3 CSC_06_HFOL_H2PO4 phosphates onto $Ca^{2+} + PO_4^{3-} \leftrightarrow CaPO_4^{-}$ CIP 04 CaPO4 CSC 07 HFOL H3PO4 $X_{\text{HFO},L}$ Ca²⁺ + HPO₄²⁻ ↔ CaHPO₄ CIP 05 CaHPO4 CSC_08_HFOL_H Protonation of X_{HFO,L} $Ca^{2+} + H_2PO_4 \leftrightarrow CaH_2PO_4$ CIP_06_CaH2PO4 $Fe^{3+} + OH \leftrightarrow FeOH^{2-}$ CIP 07 FeOH 5) HFO aging processes $\text{FeOH}^{2+} + \text{OH}^{-} \leftrightarrow \text{Fe(OH)}_{2}^{+}$ CIP 08 FeOH2 HFO_1_aging_HFOH $X_{HFO,H} \rightarrow X_{HFO,L}$ CIP 09 FeOH3 $Fe(OH)_2^+ + OH^- \leftrightarrow Fe(OH)_{3(aq)}$ HFO_2_aging_HFOL $X_{HFO,L} \rightarrow X_{HFO,old}$ CIP 10 FeOH4 $Fe(OH)_2^+ + 2OH \leftrightarrow Fe(OH)_4^-$ HFO_3_aging_HFOH,b $X_{HFO,H,b} {\longrightarrow} X_{HFO,L,b}$ $Fe^{3+} + HPO_4^{2-} \leftrightarrow FeHPO_4^{+}$ $X_{HFO,L,b} \rightarrow X_{HFO,old}$ CIP_11_FeHPO4 HFO_4_aging_HFOL,b $Fe^{3+} + H_2PO_4 \leftrightarrow FeH_2PO_4$ CIP_12_FeH2PO4

constants (pKa) and their temperature correction coefficients are taken from the NIST database (National Institute of Standards and Technology (2001)).

The Davies equation is used for a non-iterative correction of ionic concentrations with ionic activities and ion pairing. This should ensure achievement of a pH error <5%, with an effluent ionic strength comprised between 0.001 and 0.1 mol L⁻¹, which correspond to weak industrial and all domestic wastewaters (Batstone et al., 2012).

The precipitation reactions are kinetically modelled following Koutsoukos et al. (1980) and Musvoto et al. (2000). To ensure good initial speciation of ionic species in the bulk and influent, concentrations are initialized to values obtained by species decomposition with the Phreeqc software (version 2.18.3, USGS, Reston, Virginia, USA) (Parkhurst et al., 1980) on the basis of experimental results of Szabo et al. (2008).

2.2. The hydrous ferric oxide model

The precipitation of amorphous hydrous ferric oxide (HFO, considered to be $Fe(OH)_{3(s)}$ by Smith et al. (2008)) provides a number of adsorption sites for ions on its surface, which allow both adsorption and co-precipitation of ions with HFO. The term of co-precipitation is defined by the International Union of pure and Applied Chemistry (IUPAC) as "the simultaneous precipitation of a normally soluble component with a macrocomponent from the same solution by the formation of mixed crystals, by adsorption, occlusion or mechanical entrapment" (McNaught and Wilkinson, 1997). The model concepts are developed on the basis of this definition, focussing only on phosphates adsorption and co-precipitation.

The model is based on the concept of reactive site density (named active site factor, ASF expressed as sites/mole of HFO), consisting of oxygen binding sites on HFO for which phosphate species and protons are competing. An equilibrium model has already been developed on this basis by Smith et al. (2008). The total number of available sites per unit of volume (SiteT in mol m⁻³) is defined as the product of the mean number of active site factors of HFO (iASF, HFO) and the amount of precipitated HFO (X_{HFO} in mol Fe L^{-1}). Each site has the ability to form bidentate and monodentate surface complexes with HPO_4^{2-} , $H_2PO_4^{-}$ and H_3PO_4 (MUSIC model, (Hiemstra and VanRiemsdijk, 1996)). Bidentate species means that phosphate species (H₂PO₄ or H₃PO₄) are bound to two sites owning two iron atoms. Four state variables are then introduced representing phosphate species or protons that are adsorbed on HFO: $X_{HFO,H}$, X_{HFO,H_2PO_4} , X_{HFO,H_3PO_4} , and X_{HFO,HPO_4} . These state variables are expressed in terms of mol Fe L^{-1} .

In the equilibrium model of Smith et al. (2008), each complexation reaction is associated with an equilibrium constant, which will define the proportion of each species adsorbed on HFO and their equilibrium with the bulk phase. These constants, as the i_{ASF,HFO} were determined heuristically to describe the experimental data. The mean number of active site factors of HFO (i_{ASF,HFO}) has been found to depend on mixing intensity and HFO aging (Smith et al., 2008; Szabo et al., 2008), and should then be recalibrated for each experimental condition in this model. Furthermore this equilibrium model was not designed to describe the experimental results observed by Szabo et al. (2008), such as kinetic behaviour of

phosphorus removal consisting of an initial fast removal followed by slow removal, and the influence of HFO aging (loss of active surface sites).

Consequently, the kinetic model developed in this study aims to overcome these limitations. The equilibrium model developed by Smith et al. (2008) is retained and kinetic rates toward the equilibrium state are added. It results in one HFO precipitation process, four HFO aging processes and eight chemical surface complexation processes (4 complexation processes on $X_{\rm HFO,H}$ and 4 complexation processes on $X_{\rm HFO,L}$). These processes are described in more detail below and in a Gujer matrix (Appendix A and B) for the stoichiometry and kinetics, and schematically synthesized on Fig. 1. The model has been checked for continuity following the methodology described in Hauduc et al. (2010).

2.2.1. HFO precipitation

Rose and Waite (2003) and Pham et al. (2006) invoke a surface-mediated precipitation phenomenon for ferrihydrite, with a solubility product varying with the precipitate surface area, which would then not fit with the approach of Koutsoukos et al. (1980). Furthermore they found experimental evidence of a kinetic dependence on $Fe(OH)_{3(aq)}$ concentration, which would be the dominant precursor for polymerization of ferrihydrite. They propose first order kinetics with respect to total iron (Fe_T , dissolved and precipitated) and to the $Fe(OH)_{3(aq)}$ concentration. The approach of Rose and Waite (2003) was chosen in this study and presented in Equation (1).

$$Rate_{PMP_{HFO},pre} = q_{PMP_{HFO}_{pre}} * S_{FeOH_3aq} * Fe_T * \left(\frac{S_{FeOH_3aq}}{S_{FeOH_3aq} + 10^{-10}} \right) \tag{1}$$

2.2.2. HFO aging

The ferrihydrite is considered to initially precipitate as X_{HFO,H} with a high adsorption capacity, which will flocculate in larger aggregates. The floc growth depends on the mixing intensity (mean shear rate expressed as G value in s⁻¹), the concentration of metal and on the collision efficiency of the flocs (<u>Duan and Gregory, 2003</u>). Indeed, a limiting floc size exists at which collision efficiency decrease and disruptive forces increase and lead to floc breakage (<u>Duan and Gregory, 2003</u>).

This phenomenon is usually modelled as aggregation and breakage processes (Elimelech et al., 1995; Jarvis et al., 2005; Thomas et al., 1999) by a population mass balance. This complex problem may be approximated, for example by discretization (Vanni, 2000). The population of X_{HFO} is then discretized into three classes: a HFO population with a high $i_{ASF,HFO}$ ($X_{HFO,H}$), a population with a low $i_{ASF,HFO}$ ($X_{HFO,L}$) and a population with no more adsorption capacity X_{HFO,old}. These three populations represent respectively: (1) fresh HFO with an open structure and easily accessible binding sites, (2) an older HFO type with a more compact structure and less accessible sites, which will be reached with a lower diffusion rate of ions, and (3) a very old population, which may be more crystallized. The related state variables are expressed in mol Fe L⁻¹, which is equivalent to the molar concentration of $Fe(OH)_{3(s)}$.

The aging mechanism leads to a loss of reactivity of the HFO, for which process the kinetic rate expression developed

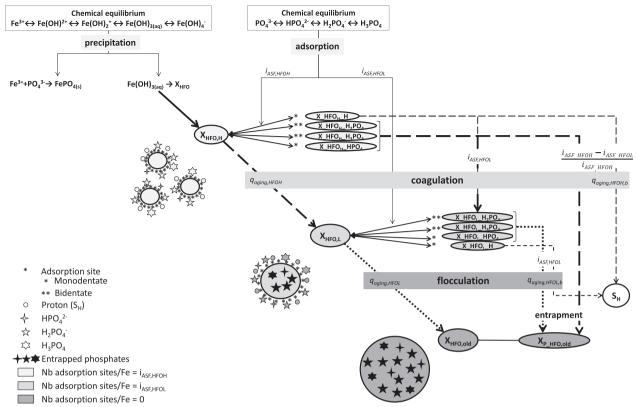


Fig. 1 - Description of adsorption and co-precipitation of phosphate on HFO modelling concepts.

by Bligh and Waite (2010) is chosen, with a general form presented in Equation (2), i being the considered population. As mentioned above, the coefficient q_{aging} in this study depends on the mixing intensity (G value). The exact form of the dependence will be studied and commented in the results section.

Rate =
$$q_{aging} * [X_{HFO,i}]^4 / [X_{HFO_T}]^2$$
 (2)

As flocs become older and larger, the importance of floc breakage increases over aggregation, resulting in a lower overall rate of floc growth (Jarvis et al., 2005). A reduction factor η_L is then introduced to lower the kinetic rate of $X_{HFO,L}$ aging compare to X_{HFO,H} aging process. Furthermore, the formation of complexes seems to suppress the hydrolysis and polymerization processes of HFO precipitation, which leads to smaller ferrihydrite particles (Galvez et al., 1999; Karlsson and Persson, 2012). The aging kinetic rates are then considered to be different for bounded HFO and free HFO, and two reduction factors are introduced to lower the kinetic rates of X_{HFOH,bT} (bounded X_{HFO,H}) and X_{HFOL,bT} (bounded X_{HFO,L}) aging processes, respectively $\eta_{b,H}$ and $\eta_{b,L}$ (A). This results into four processes of HFO aging to describe the coagulation of bounded and free fresh HFO and then their flocculation, leading to old HFO structure with no reactive sites $(X_{HFO.old})$.

Lijklema (1980) shows that desorption of phosphates due to pH changes (increase) are not completely reversible, and even less if the HFO is older. This is considered by modelling simultaneously with coagulation and flocculation, the

entrapment of phosphates that are already bounded on reactive sites into the structure of the HFO. These entrapped phosphates will not contribute to the equilibrium between adsorbed and free phosphates any more. Consequently the ratio P/Fe of the inactive HFO will evolve over time depending on the history of the HFO and its bounded phosphates. To count for entrapped phosphates, a state variable $X_{P_HFO,old}$ expressed in mol P L⁻¹ is then introduced.

2.2.3. Phosphates adsorption onto HFO

The state variables X_{HFOH_H} , $X_{HFOH_H_2PO_4}$, $X_{HFOH_H_3PO_4}$, and $X_{HFOH_HPO_4}$ and their equivalent for X_{HFOL} represent the ferrihydrite with bounded adsorption sites. They are expressed in term of mol Fe L^{-1} and their equivalent proton or phosphate contents is calculated from their stoichiometry (bidentate or monodentate complexes) and the $i_{ASF,HFO}$ of the considered population (see continuity matrix of Appendix A).

The kinetic rate expressions for complexation processes are developed based on Lagergren's kinetic equation (Lagergren, 1898), in the same way as chemical equilibrium kinetic rate equations. This equation for the liquid/solid adsorption system expresses the variation of component concentrations as a function of a driving force, being the difference between the amounts of the component that should be bound at equilibrium of the system, calculated based on equilibrium constants and the actual bounded component. An order of the reaction of one with respect to the driving force for monodentate species and of two for bidentate species is considered, in accordance with Qiu et al. (2009). The

Table 2	Table 2 $-$ Experimental condition of the selected datasets from Szabo et al. (2008).												
Dataset	Corres	ponding figure	Chemical	condition		Physical conditions							
#	This article	Szabo et al. (2008).	Fe/P dose [mol/mol]	$P_{\rm ini}$ [mg L^{-1}]	рН	Mixing G [s ⁻¹]	Aging [min]	Duration [min]					
Calibratio	n												
1	Fig. 3	Fig. 1	0.43-7.42	3.5	6.5	425	_	11					
2	Fig. 4	Fig. 16	1.8	4.1	6.5	4-371	_	11					
3	Fig. 5	Fig. 17	3	1	6.5	425	1-30	20					
Validation	n												
4	Fig. 6	Fig. 11	0.25-7	0.5-3	7	425	_	11					
5	Fig. 7	Fig. 8	1.5-3	3.75	3.5-10	425	_	11					
6	Fig. 8	Fig. 13	1-3	0-6	6.5	425	_	290					
7	Fig. 9	Fig. 15	1	3	7.5	2-425	_	100					

equilibrium constant determined experimentally by <u>Antelo</u> et al. (2010) for ferrihydrites are chosen as starting point.

The ferrihydrite flocs are porous and their adsorption sites are consequently not all equally accessible. Considering that the more accessible sites are bounded first, the subsequent decrease of the kinetic rate due to the decrease of accessibility of remaining sites have to be taken into account. A term $(SiteF/SiteT)^n$ is then introduced in the kinetic expression to moderate the kinetic constant, with n=2 for bidentate species and n=1 for monodentate species. This ratio represents the amount of free sites to the amount of total sites, its value being bounded between 0 and 1.

2.3. Model implementation and calibration

This model is implemented in Aquasim software (version 2.1g, EAWAG, Dübendorf, Switzerland) (Reichert, 1994).

The laboratory experiments from Szabo et al. (2008) provide a large number of results obtained under different conditions. These conditions may be categorized into two types: 1) the chemical conditions for which influence of iron dose, initial phosphorus concentration or pH have been tested; and 2) physical conditions for which influence of initial mixing intensity, aging processes (aggregation of flocs with time) and reaction duration (kinetic) have been investigated. Among the available results, three set of data have been chosen for calibration and four have been selected for validation of the model. The experimental conditions of these datasets are synthesized in Table 2.

The three datasets selected for calibration allow investigating all the experimental condition tested: Effect of dose and pH for dataset 1 (final pH being), effect of mixing for dataset 2 and effect of aging for dataset 3. The parameters considered in the model are listed in Table 3. As the uncertainties on the datasets cannot be evaluated (analytical uncertainties and sampling time), this calibration exercise does not aim to predict with accuracy all the values, but to determine a parameter set that describes all the selected datasets in order to validate the model structure. Each set of data leads to calibration of part of the parameters and the new parameter set is compared iteratively to other sets of data, as schematically represented in Fig. 2.

3. Results

3.1. Model calibration

The simulation of dataset #1 have reproduced the residual soluble phosphorus obtained after 11 minutes for different Fe/P ratio (0.43, 1.28, 2.54, 3.80 and 7.42) with initial pH of 6.5, initial phosphorus concentration of 3.5 mg L^{-1} and initial alkalinity of 125 mg CaCO3 $L^{-1}.$ The batch tests were performed first with a high stirring period of 1 minute at $G=425\,\mathrm{s^{-1}},$ followed by a gentle stirring period of 10 minutes. The experimental results and simulation results are shown in Fig. 3.

ASF values			Kinetic rate constants		
i _{ASF,HFOH}	1.53	Sites/mole of X _{HFO_H}	9 нғон,н	$1e^{-5}$	d^{-1}
i _{ASF,HFOL}	0.63	Sites/mole of X _{HFO_L}	$q_{HFOH,H_2PO_4}, q_{HFOH,H_2PO_4}$	$1.5e^{-6}$	$L \text{ mol}^{-1} \text{ d}^{-1}$
			Q нгон,нро ₄	$5e^{-4}$	d^{-1}
Equilibrium cons	tants (pK $values = -$	-log K)	Ч нгог,н	5e ⁻⁶	d^{-1}
	Initial ^a	Calibrated	q _{hfol.h₂po4} , q _{hfol.h₂po4}	$2e^{-8}$	$\mathrm{L}\mathrm{mol}^{-1}\mathrm{d}^{-1}$
pK _{HFO,H}	-8.7	-8.7	QHFOL,HPO ₄	5e ⁻⁵	d^{-1}
pK_{HFO,H_2PO_4}	-8.157	-8.193	q _{PMP,HFO,pre}	1e ¹⁰	$\rm L~mol^{-1}~d^{-1}$
pK _{HFO,H₃PO₄}	-10.339	-10.334	Aging parameters		
pK _{HFO,HPO4}	-7.265	-5.698	$\eta_{ m L}$	$2.5e^{-4}$	-
			$\eta_{b,H}$	1e ⁻⁵	-
			$\eta_{ m b,L}$	0.4	-

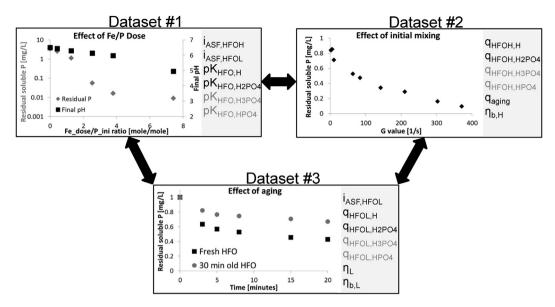


Fig. 2 — Calibration procedure and parameters identified with each dataset. Parameters in grey are not used in the simplified model.

This set of experiments allows calibration of equilibrium constants and i_{ASF,HFO} values (Table 3).

The simulation results are relatively close to experimental observations in terms of final phosphorus concentration with absolute percent errors between 4 and 32% (Table 4, left column). The final simulated pH values (squares on Fig. 3) are very close to the measured pH, with an error below 3%.

The previous batch tests were performed at high mixing intensity with a G value of $425 \, \mathrm{s}^{-1}$, which may not be the case at dosing point of wastewater treatment plants. For dataset #2 (Fig. 4), the influence of mixing intensity was investigated by Szabo et al. (2008) with 9 batch tests with varying intensity between 2 and 370 s^{-1} , which reveals lower removal capacity at lower G values after 10 minutes of reaction.

Because aging process depends on aggregation (coagulation and flocculation) which is influenced by mixing, a kinetic

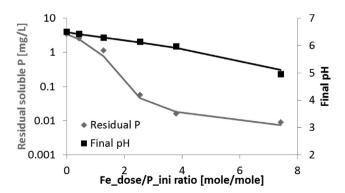


Fig. 3 – Dataset #1. Effect of initial Fe/P molar ratio on residual soluble phosphorus (diamonds) and on final pH (squares) of the batch: experimental results from Szabo et al. (2008) and simulation results (lines) (batch tests of 11 min, $P_{\rm ini}=3.5$ mg L^{-1} , $pH_{\rm ini}=6.5$, $Alk_{\rm ini}=125$ mg $CaCO_3$ L^{-1} , G=425 s $^{-1}$).

constant q_{aging} have been identified for each batch test and a function of G is calibrated on these values (Fig. 4 a). The determined expression is presented on Equation (3) and the associated simulation results are presented in Fig. 4b. The reduction factor $\eta_{b,H}$ to decrease the aging kinetic rate in case of bounded HFO is calibrated.

$$q_{aging} = 9.0e^7 \cdot \exp(-G/57.3) \tag{3}$$

The fitting of dataset #2 is very good for intermediate G value with an absolute percent error below 10% for G between

Table 4 – Quality criteria of model adjustment with all the chemical surface complexation (CSC) processes considered, or considering only proton and $\rm H_2PO_4^-$ chemical surface complexation processes.

Condition	Full model	Simplified model
Dataset#1 (Fig. 3) (Pe	ercent Error)	
Fe/P = 0.43	-4%	-4%
Fe/P = 1.28	-32%	-31%
Fe/P = 2.54	-20%	-19%
Fe/P = 3.80	12%	13%
Fe/P = 7.42	-27%	-18%
Dataset#2 (Fig. 4) (Pe	ercent Error)	
G = 371	114%	116%
G = 303	34%	35%
G = 211	-8%	-8%
G = 143	6%	6%
G = 84	5%	5%
G = 64	5%	6%
G = 10	2%	3%
G = 4	-12%	-12%
Dataset#3 (Fig. 5) (M	lean Percent Error)	
1 min old floc	-13%	-8%
5 min old floc	0%	4%
10 min old floc	-13%	-13%
30 min old floc	4%	7%

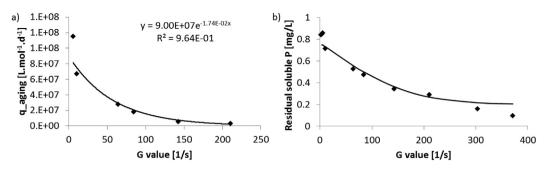


Fig. 4 – Dataset #2. Effect of G value (mixing intensity) on a) the value of the aging constant calibrated and b) on residual soluble phosphorus: experimental results from Szabo et al. (2008) (diamonds) and simulation results (line) (batch tests of 11 min, $P_{\rm ini} = 4.1$ mg/L, $Fe/P_{\rm ini} = 1.8$ mole/mole).

10 and 211 s⁻¹, slightly higher for G=2 (12%) and 34% and 114% for respectively G=303 and 371 s⁻¹ (Table 4, left column).

To analyse the influence of HFO age on removal capacity, Szabo et al. (2008) performed for dataset #3 a series of four batch tests where HFO are separately formed with a high initial stirring period of 1 minute at $G = 425 \, \mathrm{s}^{-1}$ and added to the phosphorus solution after 1, 5, 10 or 30 minutes. For each batch two samples are taken at 3 and 20 minutes after HFO addition. The simulation results obtained are presented in Fig. 5.

This data set allows identification of the reduction factors for aging processes of unbounded and bounded $X_{HFO,L}$ (respectively η_L and $\eta_{b,L}$), the phosphate adsorption rates on $X_{HFO,L}$ and the $i_{ASF,\ HFOL}$ value.

The simulated results show the same tendency as the experimental observation with a loss of removal capacity of the HFO after the same duration of contact with phosphorus solution. The adjustment of model to dataset is good, with a mean percent error below 13% for each condition (Table 4, left column).

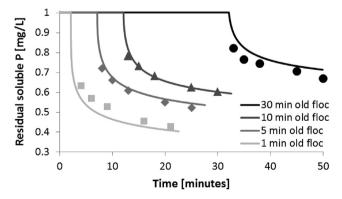


Fig. 5 — Dataset #3. Effect of HFO aging on residual soluble phosphorus: experimental results from Szabo et al. (2008) (points) and simulation results (lines). (batch tests with $P_{\rm ini}=1$ mg/L and Fe/ $P_{\rm ini}=3.0$ mole/mole, addition of preformed hydrous ferric oxides after 1, 5, 10 and 30 minutes; samples at 3 and 20 minutes after ferric chloride solution addition).

3.2. Model simplifications

The simulations reveal that $FePO_4$ does not precipitate under the tested conditions. The simplification of the model by inactivating $FePO_4$ precipitation process and associated ion paring processes (CIP_11 and 12) leads to exactly the same results.

The analyse of dynamics of iron forms reveals that Fe^{3+} , $FeOH^{2+}$ and $Fe(OH)_4^-$ concentrations reach very low concentration in less than 1 minute due to precipitation. The model have then been simplified to keep only $Fe(OH)_2^+$ and $Fe(OH)_{3(aq)}^+$ processes to correctly describe the pH and the precipitation of HFO (disabling CIP_7, 8, and 10). This leads to exactly the same results.

In the test pH range the dominant adsorbed phosphate is $H_2PO_4^-$ which represents more than 95% of the adsorbed phosphates species. The model is then tested with enabling only CSC_2, 4, 6 and 8 processes ($H_2PO_4^-$ and H^+ adsorption). The quality criteria of model adjustment are presented in Table 4, right column and show very similar results than with model considering adsorption of all phosphate species. Consequently, only CSC_2, 4, 6 and 8 processes ($H_2PO_4^-$ and H^+ adsorption) may be considered.

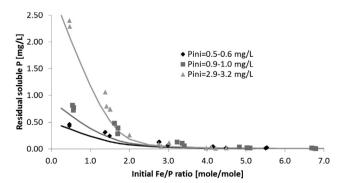


Fig. 6 — Dataset #4. Effect of initial Fe/P ratio and initial P concentration on residual soluble phosphorus: experimental results from Szabo et al. (2008) (points) and simulation results (lines) (batch tests of 11 min).

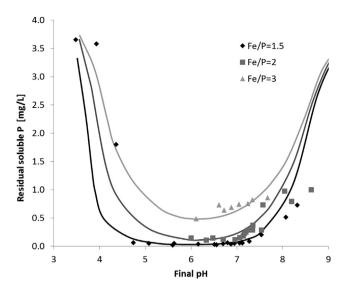


Fig. 7 – Dataset #5. Effect of pH and initial Fe/P ratio on residual soluble phosphorus: experimental results from Szabo et al. (2008) (points) and simulation results (lines) (batch tests of 11 min, $P_{\rm ini} = 3.75$ mg/L).

3.3. Model validation

The simplified model with determined parameter set is compared to independent datasets obtained under different conditions.

Datasets #4 and #5 (respectively represented on Fig. 6 and Fig. 7) allow validating the ability of the model to represent behaviour under different chemical conditions of initial phosphorus concentration, iron dose and pH. These datasets are globally well represented by the model, and the pH behaviour is well represented between pH 4.5 and 8 (Fig. 7).

Datasets #6 and #7 (respectively represented on Fig. 8 and Fig. 9) allow testing the ability of the model to simulate kinetic behaviour and the effect of various mixing conditions. The initial fast removal of phosphorus occurring in less than one minute (instantaneous phosphorus removal) is well represented for both datasets. However, the further removal (slow phosphorus removal) occurring in several hours is not accurately modelled, especially for dataset #6 (Fig. 8). The effect of the mixing intensity is well represented for $G=425\ s^{-1}$, less for $G=22.5\ s^{-1}$ and poorly for $G=2\ s^{-1}$.

4. Discussion

4.1. Prediction capabilities of the model

In this study the main operating parameters were considered through both chemical conditions (iron dose, initial phosphorus concentration or pH) and physical conditions (initial mixing intensity, aging processes due to aggregation of flocs with time and kinetic). For the first time a model is here proposed to describe the variation of adsorption capacity due simultaneously to precipitates aging, two different bounding sites capacities and entrapment.

The effect of Fe/P molar ratio is very well represented by all the simulations, either for simultaneous feeding or successive feeding thanks to the description of aging mechanism. Indeed the amount of phosphates removed by a given amount of iron will depend on the Fe/P dose, the initial phosphates concentration and on the number of adsorption sites which is related to floc size and depends on the age of the flocs and the mixing regime under which they have precipitated. In addition the model gives satisfying prediction for various residual phosphates concentrations from 0.01 to 3 mg P $\rm L^{-1}$ and in the range of pH 4.5 to 8.

The calibration of dataset #1 leads to the calibration of i_{ASF} values slightly higher than those determined by Smith et al. (2008) in the range of [0.2–1.18] Sites mol⁻¹. Those values should be confirmed with experiments under real activated sludge matrices, which organic matter may complex with HFO and leads to smaller ferrihydrite particles (Karlsson and Persson, 2012).

The loss of phosphate adsorption capacity of HFO flocs with time is well described by the model in a range of time from 5 to 30 minutes (Fig. 3). Effect of mixing intensity is also predicted by the model with satisfying results for G values in a range from 5 to 425 s⁻¹. The calibration of mixing intensity effect is very sensitive to parameter $\eta_{b,H}$, i.e. the reduction factor for the aging rate in case of bounded HFO (kinetic expression of HFO2 in A). This parameter allows a good spread of residual phosphorus values as function of G.

The q_{aging} function has been fitted based on dataset #2 with initial phosphorus concentration of 4.1 mg/L. However the model seems to underestimate the aging process in the case of a G of 2 s⁻¹ in dataset #7, for which initial phosphorus was 1 mg/L. This is logical as the rate q_{aging} was not correctly predicted for very low value of G with the exponential model

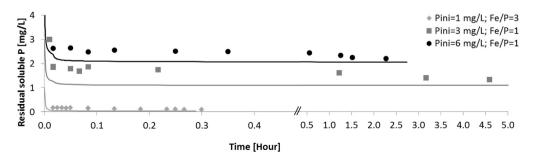


Fig. 8 – Dataset #6. Effect of initial phosphorus concentration on kinetics of residual soluble phosphorus: experimental results from Szabo et al. (2008) (points) and simulation results (lines).

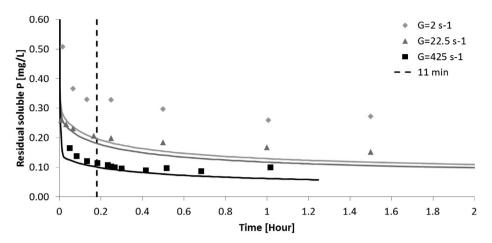


Fig. 9 – Dataset #7. Effect of initial mixing on kinetics of residual soluble phosphorus: experimental results from Szabo et al. (2008) (points) and simulation results (lines). (batch tests with $P_{\rm ini} = 1$ mg/L and Fe/ $P_{\rm ini} = 3.0$ mole/mole).

chosen (Fig. 4). Such a very slow mixing is relatively extreme. Therefore, this kinetic model of aging should be compared with further experimental results and full-scale mixing conditions which may greatly differ from jar-test conditions.

4.2. About model simplifications and further needs

The simulated amount of phosphorus precipitated in the form of FePO₄ is shown to be negligible (<10-12 mg P L⁻¹), which is consistent with the work of Smith et al. (2008) showing no FePO₄ precipitation above pH 5. This further indicates that the existing models based on precipitation in the form of FePO₄ are not suitable to describe the mechanisms observed.

The dominant simulated adsorbed phosphate is H₂PO₄ (>95% of the adsorbed phosphates species), which is consistent with experimental observations of Hiemstra and VanRiemsdijk (1996) who measured more than 85% of this surface species over pH range of 3.5-8. Antelo et al. (2010) shows no significant improvement in modelling HPO₄²⁻ species adsorption onto HFO, whereas Rahnemaie et al. (2007) choose to neglect H₃PO₄ adsorption, since its concentration is negligible above pH 4. Furthermore, the equilibrium constant pK_{HFO,HPO} (determined at -5.698 before simplification) takes a large range of values in literature, from 3.125 (Smith et al., 2008) to 15.255 (Rahnemaie et al., 2007). This reveals the uncertainty on this adsorption process. Consequently, the simplification of both HPO₄²⁻ and H₃PO₄ adsorption onto HFO in this study is consistent with previous work. The simplification of HPO₄²⁻ species by Antelo et al. (2010) leads the author to recalibrate the thermodynamic constant $pK_{\text{HFO},H_{7}\text{PO}_{4}}$ from -8.157 to -8.207, which value is very close to the one determined in this study (-8.193).

The model validation step demonstrates the validity of the simplified model in the range of pH 4.5 to 8. In this range of pH the iron forms $Fe(OH)_4^-$ and $Fe(OH)_3$ are predominant, and thus sufficient to correctly predict the HFO precipitation. In this range of pH, $FePO_4$ precipitation is also negligible, just as the H_3PO_4 adsorption onto HFO. However HPO_4^{2-} is one of the major phosphate ionic form in this range of pH (50% at pH 7.2

and major ionic for above). Consequently the simplifications made in this model by not considering its adsorption onto HFO do not depend only on the hypothesis made on the pH range applicability, but on the adsorption process itself. Indeed, Hiemstra and VanRiemsdijk (1996) specify that HPO $_4^{2-}$ species adsorption may become important at high pH and low P charge. The available datasets show the ability of the model to predict phosphates adsorption for initial phosphate concentration as low as 1 mg/L, but the applicability limit for lower initial phosphates concentration would require to be evaluated with additional experiments.

Above pH 7.5—8 the model results presented on Fig. 7 show significant differences with experimental data. At this pH other components of the tap water used for these experiments, such as calcium phosphate, may precipitate. This precipitates may have to be considered for model validation with real wastewater.

All the experimental observations revealed an initial fast removal of phosphorus occurring in less than one minute (instantaneous phosphorus removal), and a further removal (slow phosphorus removal) as observed by Szabo et al. (2008). The results demonstrate the ability of the model to correctly predict the initial fast removal process with aging but poorly the further slow removal. This behaviour of the model may be explained by the choice to represent the distribution of HFO flocs properties by only three classes ($X_{\rm HFO,IH}$, $X_{\rm HFO,L}$ and $X_{\rm HFO,old}$). The impact of this choice should be further investigated, especially in case of full scale results.

The calibration exercise on both influence of initial mixing rate and HFO aging evidenced a competition between adsorption and aging processes, to which parameters the model is very sensitive and impact both equilibrium and kinetic behaviour. Consequently, these processes should be carefully calibrated on full scale case study. At this stage it is not possible to say that the identification performed in this study will be directly applicable to full scale system. It is clear that the lab-scale conditions facilitate the homogeneity of the system. For industrial reactors performing such rapid processes a good

characterisation of hydrodynamics would be probably necessary in association with this model.

5. Conclusion

A new model has been developed to predict kinetically the precipitation of HFO, its aging processes and phosphates adsorption and co-precipitation mechanisms in the framework of chemical phosphorus removal in wastewater treatment plants. The simulation results showed that the structure of the model describes adequately the mechanisms of adsorption and co-precipitation of phosphates into/onto HFO and that the model is robust under various experimental conditions.

In this work, the model was validated with experiments carried out in tap water with low ammonium content and other component precipitations were not considered. For a validation with real wastewater, the physico-chemical model should be extended to take into account ammonia dissociation, calcium and magnesium ion pairing and precipitation processes. The influence of other parameters on chemical phosphate removal should also be investigated, such as the competition with carbonates, TSS and organics (COD). The

next step will be to implement this model in an activated sludge model and compare the results to pilot or full scale data to validate it under continuous condition. The behaviour of ferric iron (Fe³⁺) under anaerobic condition, and especially its reduction into ferrous iron (Fe²⁺) should also be studied and included in the model.

The model developed and validated could then be used in full scale wastewater treatment plant models to optimize chemical dosing simultaneously while ensuring compliant effluent phosphorus concentration. Optimization parameters could include quantity of chemicals, frequency, location(s), mixing intensity and sludge age.

Acknowledgements

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Appendix A. Stoichiometric and kinetic matrix of chemical surface complex formation processes. Processes in grey are not considered in the simplified model.

Units	HPO ₄ ²⁻ [mol P.L ⁻¹]	H ₂ PO ₄ - [mol P.L. ¹]	H ₃ PO ₄ [mol P.L ⁻¹]	H^+ [mol H.L. 1]	HFO (Fe(OH) _{3(aq)}) with high i _{ASE,HFO} [mol Fe.L. ¹]	Protonated X _{HFO,H} [mol Fe.L. ¹]	X _{HFO,H} bounded with HPO ₄ ²⁻ [mol Fe.L ⁻¹]	X _{HFO,H} bounded with H ₂ PO ⁴⁻ [mol Fe.L ⁻¹]	X _{HFO,H} bounded with H ₃ PO ₄ [mol Fe.L ⁻¹]	HFO (Fe(OH) _{3(aq)}) with low i _{ASF,HFO} [mol Fe,L ⁻¹]	Protonated X _{HFO,L} [mol Fe,L. ¹]	X _{HFO,L} bounded with HPO4 ² - [mol Fe.L ⁻¹]	X _{HFO,L} bounded with H ₂ PO ₄ - [mol Fe.L. ¹]	X _{HFO,L} bounded with H ₃ PO ₄ [mol Fe.L. ¹]	Inactive HFO (Fe(OH) ₃ (s)) [mol Fe.L. ¹]	Phosphorus entrapped into HFO structure [mol P.L. ¹]
					Х _{нғон,т}							X _{HFO}	L,T			
					X _{HI}	OHf,T		X _{HFOHb,T}		X _{HF}	OLf,T		X _{HFOLb,T}			
Name	S _{HPO4}	S _{H2PO4}	S _{H3PO4}	S_{H}		$X_{HFOH_{H}} \\$	X _{HFOH_{HPO4}}	$X_{HFOH_{H2PO4}}$	X _{HFOH_{H3PO4}}	X _{HFOL}	X _{HFOLH}	X _{HFOLHPO}	X _{HFOLH2PO4}	X _{HFOLH3PO4}	$X_{HFO_{old}}$	$X_{P_{HFO_{old}}}$
CSC1	-i _{ASFHFOR}				-1		1									
CSC2		-i _{ASFHFOH} /2			-1			1								
CSC3			$-i_{ASF_{HFOH}}/2$		-1				1							
CSC4				-i _{ASFHFO}	₄ -1	1										
CSC5	-i _{ASFHFOL}									-1		1				
CSC6		$-i_{ASF_{HFOL}}/2$								-1			1			
CSC7			$-i_{ASF_{HFOL}}/2$							-1				1		
CSC8				$-i_{ASF_{HFO}}$						-1	1					
	Continuity matrix															
P	1	1	1				$i_{ASF_{HFOH}}$	i _{ASFHFOH} /2	$i_{ASF_{HFOH}}/2$			i _{ASFHFOL}	$i_{ASF_{HFOL}}/2$	$i_{ASF_{HFOL}}/2$		1
Fe					1	1	1	1	1	1	1	1	1	1	1	
Н				1		$i_{ASF_{HFOH}}$					$i_{ASF_{HFOL}}$					
							Kinetio	rate expre	sions							
CSC1	Ads	sorption of S _{HP}	O4 on X _{HFOH}				$q_{HFOH_{HPO4}} *$	$\frac{SiteF_H}{SiteT_H + \varepsilon} *$	$\left(10^{-pK_{HFO_{HPO}}}\right)$	04 * S _{HPO4}	$* f_d * \frac{S}{Si}$	$\frac{SiteF_H}{teT_H + \varepsilon}$	$i_{ASF_{HFOH}} * \frac{X_H}{S}$	ron _{HPO4}		
CSC2	Ads	orption of S _{H2F}	on X _{HFOH}		$q_{HFOH_{H2PO4}}*\left(\frac{SiteF_{H}}{SiteT_{U}+\varepsilon}\right)^{2}*\left(10^{-pK_{HFOH_{H2PO4}}}*S_{H2PO4}*f_{m}*\left(\frac{SiteF_{H}}{SiteT_{U}+\varepsilon}\right)^{2}-\frac{i_{ASF_{HFOH}}*X_{HFOH_{H2PO4}}}{SiteT_{U}+\varepsilon}\right)^{2}$											
CSC3	Ads	orption of S _{H3P}	o ₀₄ on X _{HFOH}			q_H	$FOH_{H3PO4} * \left(\frac{1}{S} \right)$	$\frac{SiteF_H}{iteT_H + \varepsilon}$ ² *	$\left(10^{-pK_{HFO_{H3}}}\right)$	8P04 * S _{H31}	$v_{O4} * \left(\frac{S}{Sit}\right)$	$\frac{(iteF_H}{eT_H + \varepsilon})^2$	i _{ASFHFOH} * X SiteT _F	$\left(\frac{HFOH_{H3PO4}}{H+\varepsilon}\right)^{2}$		
CSC4	A	dsorption of S _H	on X _{HFOH}				q_{HFOH_H}	* $\frac{SiteF_H}{SiteT_{} + \varepsilon}$	* (10 ^{-pK} _{HFO} _H	$*S_H * f_m$	* SiteI	$\frac{T_H}{+ \epsilon} - i_{ASF_H}$	$X_{HFOI} * \frac{X_{HFOI}}{SiteT}$	H _H + s		
CSC5	Ads	sorption of S _{HP}	O4 on X _{HFOL}				q _{HFOL_{HPO4} *}	$\frac{SiteF_L}{SiteT_L + \varepsilon} *$	$\left(10^{-pK_{HFO_{HPO}}}\right)$	04 * S _{HPO4}	$* f_d * \frac{1}{Sit}$	$\frac{SiteF_L}{teT_L + e} - i$	$X_{ASF_{HFOL}} * \frac{X_{HI}}{Site}$	$\frac{FOL_{HPO4}}{eT_L + e}$		
CSC6	Ads	orption of S _{H2F}	on X _{HFOL}			q_{HFG}	$OL_{H2PO4} * \left(\frac{S}{Sit}\right)$	$\frac{iteF_L}{eT_L + \varepsilon}$) ² * $\left(\frac{eT_L + \varepsilon}{eT_L + \varepsilon}\right)^2$	$10^{-pK_{HFO_{H2PO}}}$	4 * S _{H2PO}	$1 * f_m * \left(\frac{1}{2}\right)$	$\frac{SiteF_L}{SiteT_L + \varepsilon}$	$-\frac{i_{ASF_{HFOL}} *}{Site}$	$\left(\frac{X_{HFOL_{H2PO4}}}{T_L + \varepsilon}\right)^2$		
CSC7	Ads	orption of S _{H3F}	on X _{HFOL}			q_{I}	$q_{HFOL_{H3PO4}}*\left(\frac{SiteF_L}{SiteT_L+\varepsilon}\right)^2*\left(10^{-pK_{HFO_{H3PO4}}}*S_{H3PO4}*\left(\frac{SiteF_L}{SiteT_L+\varepsilon}\right)^2 - \frac{i_{ASF_{HFOL}}*X_{HFOL_{H3PO4}}}{SiteT_L+\varepsilon}\right)^2$									
CSC8	A	dsorption of S _F	on X _{HFOL}						* (10 ^{-pK_{HFO}}							

Appendix B. Stoichiometric and kineticmatrix of HFO aging processes.

Name S	н Хнгон	X _{HFOHH}	X _{HFOH_{HPO4}}	X _{HFOH_{H2PO4}}	X _{HFOH_{H3PO4}}	X _{HFOL}	X_{HFOL_H}	X _{HFOLHPO4}	X _{HFOLH2PO4}	X _{HFOLH3PO4}	$X_{HFO_{old}}$	$X_{P_{HFO_{old}}}$
HFO1	$\frac{-X_{HFOH}}{X_{HFOHf_T}}$ +	$\frac{-X_{HFOH_H}}{X_{HFOH_{f_T}} + \varepsilon}$				$\frac{X_{HFOH}}{X_{HFOHf_T} + \varepsilon}$	$\frac{X_{HFOH_H}}{X_{HFOHf_T} + \varepsilon}$					
HFO2						$\frac{-X_{HFOL}}{X_{HFOLf_T} + \varepsilon}$	$\frac{-X_{HFOL_H}}{X_{HFOLf_T} + \varepsilon}$				$\frac{X_{HFOL} + X_{HFOL_H}}{X_{HFOLf_T} + \varepsilon}$	
нгоз			$\frac{-X_{HFOH_{HPO4}}}{X_{HFOHb_T} + \varepsilon}$	$\frac{-X_{HFOH_{H2PO4}}}{X_{HFOHb_T} + \varepsilon}$	$\frac{-X_{HFOH_{H3PO4}}}{X_{HFOHb_T} + \varepsilon}$,	$\frac{X_{HFOH_{HPO4}}}{X_{HFOHb_T} + \varepsilon}$	$\frac{X_{HFOH_{H2PO4}}}{X_{HFOHb_T} + \varepsilon}$	$\frac{X_{HFOH_{H3PO4}}}{X_{HFOHb_T} + \varepsilon}$		С
HFO4					·			$\frac{-X_{HFOL_{HPO4}}}{X_{HFOLb_T} + \varepsilon}$	$\frac{-X_{HFOL_{H2PO4}}}{X_{HFOLb_T} + \varepsilon}$	$\frac{-X_{HFOL_{H3PO4}}}{X_{HFOLb_T} + \varepsilon}$	D	Е
$A = \left(\frac{i_{ASF}}{}\right)$	$ \begin{aligned} & \text{with} \\ & \text{A} = \left(\frac{i_{ASF}_{HFOH} - i_{ASF}_{HFOL}}{i_{ASF}_{HFOH}} * \left(i_{ASF}_{HFOH} + \frac{x_{HFOH}_{H}}{x_{HFOH}_{T} + \varepsilon}\right)\right) \\ & \text{B} = \left(i_{ASF}_{HFOL} * \frac{x_{HFOL}}{x_{HFOL}} * x_{H$											
				1	Kin	etic rate expr	essions					
HFO1	Aging of	X _{HFOH,fT} (unbound	ed X _{HFOH})				q_{aging}	$*X_{HFOHf_T}*\frac{X}{X_H^2}$	$\frac{1}{HFOH_T}$			
HFO2	Aging of	X _{HFOL,fT} (unbound	ed X _{HFOL})				$\eta_L * q_{agi}$	ng * X _{HFOLfT} *	$\frac{X_{HFOL_T}^3}{X_{HFO_T}^2 + \varepsilon}$			
нгоз	Aging of	X _{HFOH,bT} (bounde	d X _{HFOH})	$q_{aging} * X_{HFOH_T} * \frac{X_{HFOH_T}^3}{X_{HFO_T}^2 + \varepsilon}$ $\eta_L * q_{aging} * X_{HFOH_T} * \frac{X_{HFOL_T}^3}{X_{HFO_T}^2 + \varepsilon}$ $\eta_{b,h} * q_{aging} * X_{HFOH_T} * \frac{X_{HFOH_T}^3}{X_{HFO_T}^2 + \varepsilon}$ $\eta_{b,h} * q_{aging} * X_{HFOH_T} * \frac{X_{HFOH_T}^3}{X_{HFO_T}^2 + \varepsilon}$ $\eta_L * \eta_{b,L} * q_{aging} * X_{HFOL_D} * \frac{X_{HFOL_T}^3}{X_{HFO_T}^2 + \varepsilon}$								
HFO4	Aging o	X _{HFOL,bT} (bounde	d X _{HFOL})	$\eta_L * \eta_{b,L} * q_{aging} * X_{HFOL_T} \frac{X_{HFOL_T}^3}{X_{hro}^3 + \varepsilon}$								

Appendix C. List of calculated variables.

Name	Expression	Units
SiteT _H	$(X_{HFOH} + X_{HFOH_{H}} + X_{HFOH_{H_2PO_4}} + X_{HFOH_{H_2PO_4}} + X_{HFOH_{HPO_4}}) * i_{ASF_{HFOH}}$	mol sites L ⁻¹
$SiteT_L$	$(X_{HFOL} + X_{HFOL_H} + X_{HFOL_{HoPOs}} + X_{HFOL_{HoPOs}} + X_{HFOL_{HPOs}} + X_{HFOL_{HPOs}}) * i_{ASF_{HFOL}}$	$ m mol~sites~L^{-1}$
SiteF _H	$(X_{HFOH} + X_{HFOH_H}) * i_{ASF_{HFOH}}$	$ m mol~sites~L^{-1}$
SiteF _L	$(X_{HFOL} + X_{HFOL_H}) * i_{ASF_{HFOL}}$	$ m mol~sites~L^{-1}$
Fe _T	$S_{FeT} + X_{HFOH_{\mathtt{T}}} + X_{HFOH_{\mathtt{T}}}$	$ m mol~Fe~L^{-1}$
ε	Small number to avoid numerical problems with fractions (10^{-16})	_
f_m , f_d	Correction factors for ionic activities of mono- and divalent ions using	_
	Davies equation	

Appendix D. Physico-chemical model.

Table D.1 - Stoichiometric and kinetic matrix of chemical equilibrium dissociation, chemical ion paring and physical mineral precipitation processes. Processes in grey are not considered in the simplified model.

Name)3aq .L.¹]	2 <i>P04</i> .L ^{.1}]	,T.,]	'P04 .L.']	OH -T:-	P04 .L.']	'a .L.']	23 .L. ¹]	2 <i>P0</i> 4	'P04 .L.¹]	2H2 .L.']	Н3аq .L⁻¹]	2H4 .L. ¹]	OH -T-	'e .L. ¹]	C03	P04 .L. ¹]	P04 .L.¹]	.03 .L. ⁻¹]	0.04 .L. ¹]	Ч .L. ⁻¹]	H.T.	04 .L. ¹]	P04 .L.']	(0.H
[Units]	Scacosaq [mol.L ⁻¹]	Scan2PC [mol.L. ⁻¹]	S_{CaHCO}	S_{CaHPO}	S_{CaOH}	S_{CaPO4}^{CaPO4}	S_{Ca}^{-1}	S_{CO3} [mol.L. ¹	Srenzpo [mol.L.1	S_{FeHPO}	S _{FeOH2} [mol.L. ¹]	S_{FeOH3a} [mol.L. $^{ ext{-}1}$]	S_{FeOH4} [mol.L. ¹]	S_{FeOH}	S_{Fe} [mol.L ⁻¹]	S_{H2CO3}^{CO3}	SH2PO4 [mol.L. ¹]	S_{H3PO4}^{C}	S_{HCO3} [mol.L ⁻¹]	S_{HPO4}^{2}	S_H^{-1}	S _{OH}	S_{PO4} [mol.L.1	X_{FePO4} [mol.L.1]	X_{HFOH} [mol.L.']
CED_01																					1	1			
CED_02																-1			1		1				
CED_03								1											-1		1				
CED_04																	1	-1			1				
CED_05																	-1			1	1				
CED_06																				-1	1		1		
CIP_01					1		-1															-1			
CIP_02 CIP_03	I		1				-1 -1	-1																	_
CIP_03			1			1	-1												-1				-1		_
CIP_04				1		- 1	-1													-1			-1		_
CIP 06		1		1			-1										-1			-1					
CIP 07							-							1	-1							-1			
CIP 08											1			-1								-1			
CIP 09											-1	1										-1			
CIP 10												-1	1									-1			
CIP_11										1					-1					-1					
CIP_12									1						-1		-1								
PMP_1												-1													1
PMP_2															-1								-1	1	
	-	ı					-	•	•		inetic	rate ex	pressi	ons		•	·-								
CED_01	L_H2O					CEDH2O *						CIP_0	5_CaE	IPO4	Table Canada										
CED_02_	H2CO3	q_{CI}	ED _{H2CO3}	* (10 ^{-p}	K _{CED} _{H2C}	03 * (1/	$(f_m^2) * .$	S_{H2CO3}	$- S_H *$	S_{HCO3})		CIP_0	6_CaH	2PO4							_{2PO4})				
CED_03	_HCO3					гсоз * (1						CIP	_07_Fe	ОН							$_n/f_d)*$				
CED_04_	H3PO4					94 * (1/						CIP_	08_Fe0	OH2		q_c	IP _{FeOH2}	* (10 ⁻¹	oK _{CIP FeO}	$H^2 * f_d$	$*S_{FeOH}$	* S _{OH} -	- S _{FeOH}	2)	
CED_05_	H2PO4	q_C	ED _{H2PO4}	* (10-	$pK_{CED_{H2}}$	P04 * (1	$/f_d) * S$	H2PO4	$-S_{H} * S$	S_{HPO4}		CIP_	09_Fe0	OH3		q_{CIP}	FeOH3 *	(10^{-pK_0})	CIP _{FeOH3}	* f _m ² *	S_{FeOH2}	$*S_{OH}$ -	- S _{FeOH}	3aq)	
CED_06	_HPO4	q_{CEI}				* (f _d /()	CIP_	10_Fe0	OH4		q	CIP _{FeOH}	* (10	pK _{CIPFeC}	он4 * S _F	eOH3aq	* S _{OH} —	S_{FeOH4}	.)	
CIP_01_	CaOH		q_{CIP_C}	аон * ($10^{-pK_{CI}}$	^Р СаОН * _.	$f_d * S_{Ca}$	$*S_{OH}$	— S _{саон}	1)		CIP_1	11_FeH	PO4	q	CIP _{FeHP}	* (10	$-pK_{CIP_F}$	eHPO4 *	$(f_t * f_d)$	$/f_{m}) * S$	S _{HPO4} *	$S_{Fe} - S$	FeHP04)
CIP_02_	CaCO3	(ЯсіР _{Сасо}	* (10	-pK _{CIP} _{Co}	$t^{cos} * f_d$	$^{2}*S_{Ca}$	* S _{co3}	- Scace	заа (CIP_1	2_FeH	2PO4							$/f_d) * S$				
CIP_03_C	CaHCO3	q	CIPCaHCO	* (10	-pK _{CIPC}	ансоз * ј	$f_d * S_{Ca}$	* S _{HCO}	$_3 - S_{Ca}$	нсоз)		PMP_	1_HFC	_pre			q_{PMF}	'нго _{рге} *	S_{FeOH3}	aq * Fe	$T * \left(\frac{1}{S_F}\right)$	S _{FeOH36} :eOH3aq	$\left(\frac{q}{+\varepsilon}\right)$		
CIP_04_	CaPO4	q_{CIP}	CaPO4 *	(10 ^{-pK}	CIP _{CaPO4}	* (f _d *	f_t/f_m)	* S _{Ca} *	S_{PO4} —	S_{CaPO4})	PMP	_2_Fel	204		q_{Pl}	MP _{FePO4]}	* (()	$c_t^2 * S_{F\epsilon}$, * S _{PO4}	$)^{\frac{1}{2}} - (1$	$0^{-pK_{PM}}$	P_{FePO4}	2)2	

Table D.2 — Physico	-chemical model par	ameter values.				
		K) corrected with temperature $exp(-\Delta/R*(1/T-1/298.15)))$	Kinetic rate constants (from Musvoto al. (2000))			
	pK (25 °C)	Δ (kJ mol^{-1})		$(L \text{ mol}^{-1} \text{ d}^{-1})$		
pK_CED_H ₂ CO ₃	6.352	9.16	q_CED_H ₂ CO ₃	8.64E + 11		
pK_CED_H ₂ O	13.997	55.81	$q_CED_H_2O$	8.64E + 14		
pK_CED_H ₂ PO ₄	7.198	3	$q_CED_H_2PO_4$	8.64E + 16		
pK_CED_H ₃ PO ₄	2.148	-7.9	$q_CED_H_3PO_4$	8.64E + 12		
pK_CED_HCO ₃	10.329	14.6	q_CED_HCO ₃	8.64E + 14		
pK_CED_HPO ₄	12.375	15	$q_CED_HPO_4$	8.64E + 19		
pK_CIP_CaCO ₃	-3.2	16	q_CIP_CaCO₃	8.64E + 11		
pK_CIP_CaH ₂ PO ₄	-1.35	-24	q_CIP_CaH ₂ PO ₄	8.64E + 11		
pK_CIP_CaHCO ₃	-1.27	-9.2	q_CIP_CaHCO₃	8.64E + 11		
pK_CIP_CaHPO ₄	-2.66	-18	q_CIP_CaHPO ₄	8.64E + 11		
pK_CIP_CaOH	-1.3	8.3	q_CIP_CaOH	8.64E + 11		
pK_CIP_CaPO ₄	-6.46	12.9704	q_CIP_CaPO ₄	8.64E + 11		
pK_CIP_FeH ₂ PO ₄	-4.2785	-12.6	q_CIP_FeH ₂ PO ₄	8.64E + 11		
pK_CIP_FeHPO ₄	-9.917	-45.5432	q_CIP_FeHPO ₄	8.64E + 11		

Table D.2 — (continu	ued)					
	nts (pK values = $-\log 1$ tabase): $-\log(10^{-pK_{25^{\circ}C}}*$	Kinetic rate constants (from Musvoto et al. (2000))				
	pK (25 °C)	Δ (kJ mol $^{-1}$)		$(L \text{ mol}^{-1} \text{ d}^{-1})$		
pK_CIP_FeOH	-11.81	-14	q_CIP_FeOH	8.64E + 11		
pK_CIP_FeOH ₂	-11.59	-41.81	q_CIP_FeOH ₂	8.64E + 11		
pK_CIP_FeOH ₃	-6.031	-184.994	q_CIP_FeOH₃	8.64E + 11		
pK_CIP_FeOH ₄	-4.969	-167.43	q_CIP_FeOH ₄	8.64E + 11		
Equilibrium constants	for precipitation process	ses (pK values = -log K)	Kinetic rate constants for precipitation processes (Calibrated)			
pK_PMP_FePO ₄	26.4	Smith et al., 2008 (I = 0.02 M)	q_PMP_FePO ₄ _pre	100,000		
pK_PMP_HFO	15.4	Smith et al., 2008 (I = 0.02 M)	q_PMP_HFO_pre	1E + 10		

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