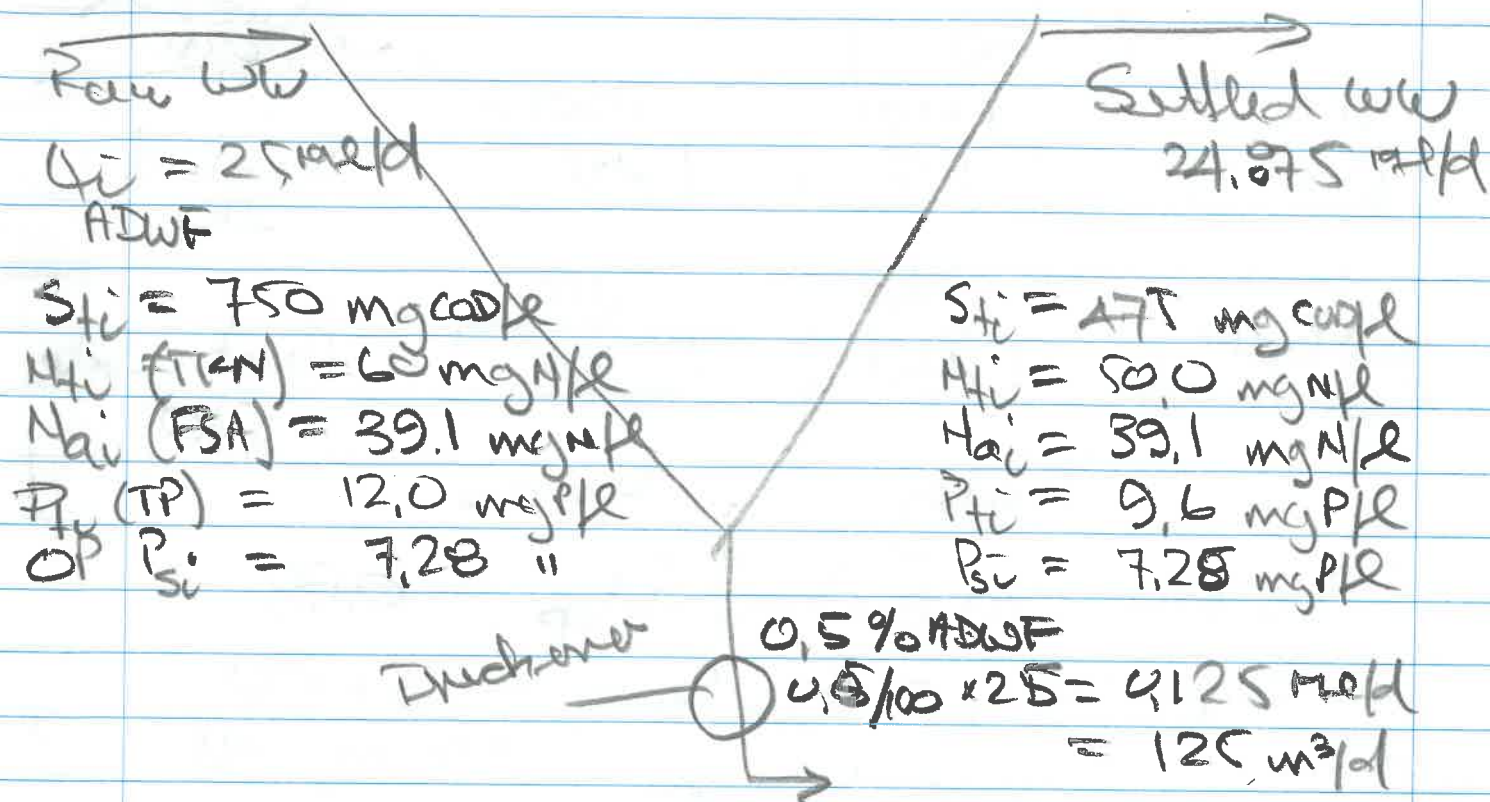


# IHE- Module 5 2018

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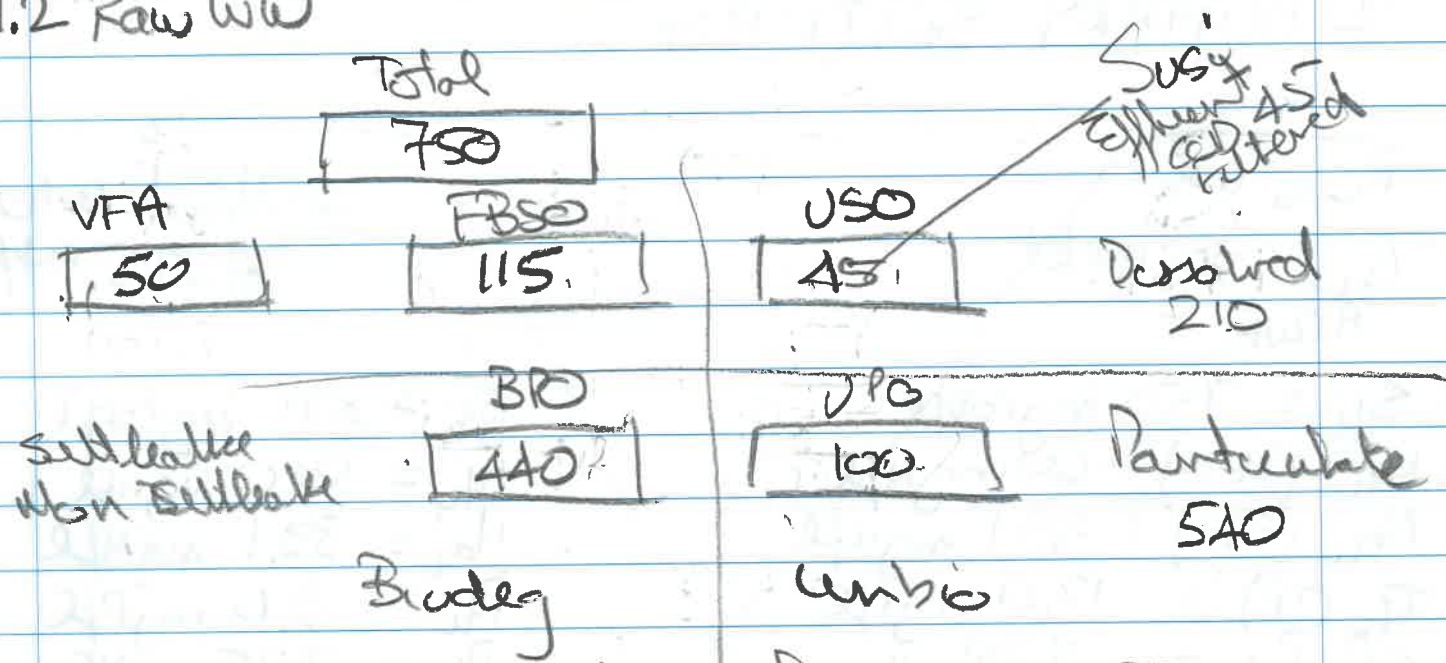
## 1 PRIMARY SETTLING



TOC  $C_{ti} = 250.8 \text{ mg/l}$   $C_{ti} = 158.8 \text{ mg/l}$   
 $T_{\text{SuspS}} = 416 \text{ mg TSuspS/l}$   $T_{\text{SuspS}} = 189 \text{ mg TSuspS/l}$   
 $I_{\text{SuspS}} = 60 \text{ mg ISuspS/l}$   $I_{\text{SuspS}} = 15 \text{ mg ISuspS/l}$

	Raw WW 25 m³/d		Settled WW 24.875		Primary Sludge 4.125 m³/d	
Flow	Conc mg/l	Flux kg/d	Conc mg/l	Flux kg/d	Conc mg/l	Flux kg/d
COD	750	18750	475	11816	55475	6934
TKN	60.0	1501	50.0	1244.8	2050.1	256.3
FSA	39.1	977.5	39.1	972.5	39.1	4.9
TP	12.0	300.97	9.6	238.92	488.37	61.05
OP	7.28		7.28		7.28	
TOC	250.8	16270.0	158.8	3949.7	18553.0	2319.1
TSuspS	416	10410.6	189	4706.0	45637.7	5704.7
ISuspS	60	1500	15	373.1	9015.0	1126.9
VSuspS	356	8900.6	174	4320.0	36622.3	4577.8

# Q1.2 Raw WW



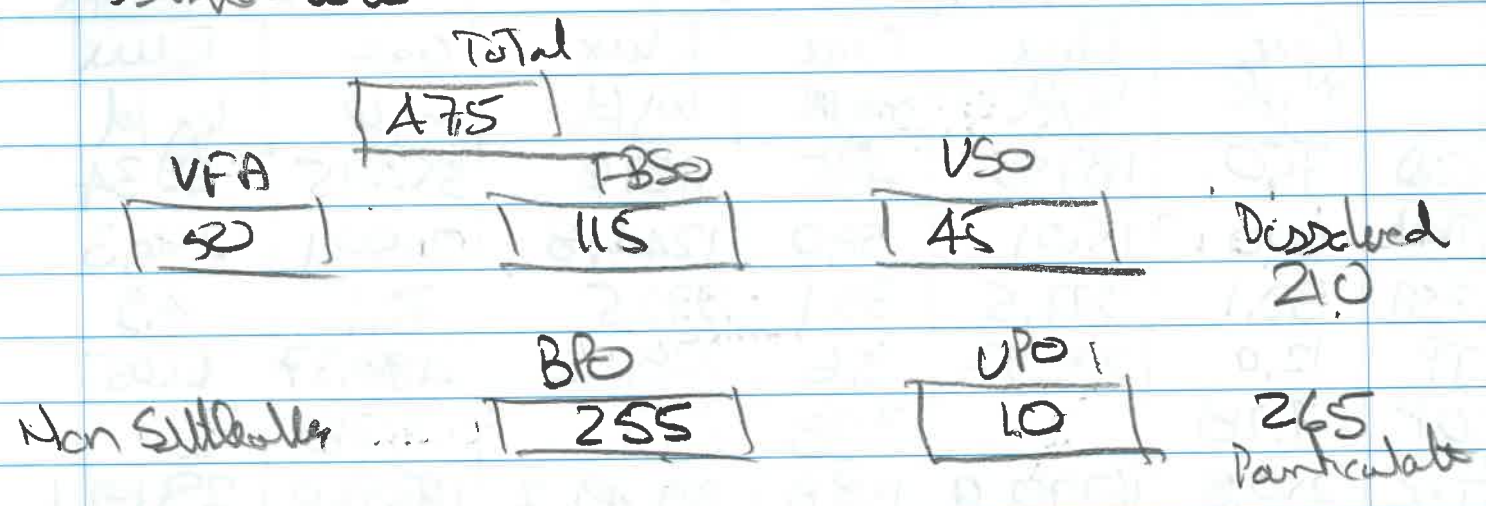
Raw WW UPO fraction  $f_{sup} = 0.133$

$$Sup_i (UPO) = f_{sup} St_i = 0.133 \times 750 = 100 \text{ mg COD/l}$$

$$Susi (USE) = f_{sus} = \frac{45}{750} = 0.06$$

$$VSS \text{ of the UPO} = \frac{COD \text{ of UPO}}{f_{cv}} = \frac{100}{1.481} = 67.5 \text{ mg VSS/l}$$

## Settled WW COD



$f_{sup} \text{ Settled} = 0.021$

$$Sup_i = f_{sup} St_i = 0.021 \times 475 = 10 \text{ mg COD/l}$$

NL 09h30



Raw WW TKN

	TKN	
	60.0	
FSA		
133.1		

Organic
20.9

Tillhard  
Effluent  
TKN = 1.48  
FSN = 0.38  
org N = 1.10

FBSO	4.9	VSO
3.8		1.1

Desired  
44.0

BPO	VPO
9.25	6.75

Particulate  
16.0

Biolog

unbiol

$$f_{n \text{ VPO}} = \frac{1}{VSS} \text{ ratio} = 0.10 \text{ mg N / mg VSS}$$

$$N_{\text{oupi}} = f_n \frac{\text{Supc}}{f_{cv}}$$

$$= 0.10 \times \frac{100}{1.48} = 6.75 \text{ mg N / l}$$

Raw WW

VSS 356

288.5
BPO

6.75
VPO

Particulate

COD 540

440

100

Settleable  
9.168 settled

Settled WW TKN

52.0
------

FSA
39.1

44.0

FBSO
3.8

VSO
1.1

Desired

16.0

5.33
------

0.67
VPO

Particulate

$$N_{\text{oupi}} = \frac{\text{Supc}}{f_{cv}} f_n = \frac{10}{1.48} \times 0.10 = 0.67$$

Raw WW TP

TP  
12.00

Effluent Filtered A  
TP = 7.55  
OP = 7.55  
wsg = 0

4.72

OP  
7.28

8.23

FBSO

0.95

USO

0.0

0.95 Dissolved

3.77

2.07  
BPO

1.17  
UPB

Particulate

$$P_{\text{oupi}} = \frac{\text{Supi}}{f_{\text{cu}}} f_p = \frac{100}{1.451} 0.025 = 1.7 \text{ mg P/l}$$

Settled TP

9.60

2.32 wsg P

7.28

8.23

0.95

0.95

0.0

Dissolved

1.37

1.20

1.37

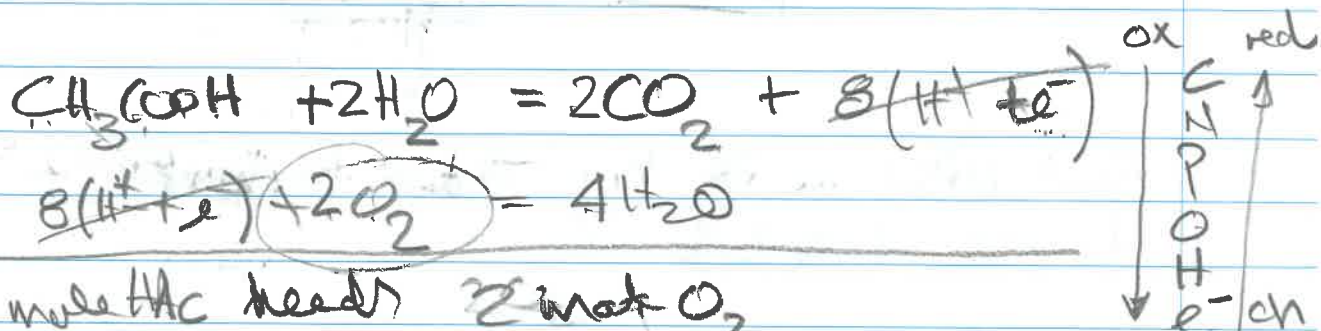
0.17

Particulate

$$P_{\text{oupi}} = f_{\text{pup}} \frac{\text{Supi}}{f_{\text{cu}}} = 0.025 \times \frac{10}{1.45} = 0.17$$



VFA 118.75*	FBSO 38.1	USO 15.0*	71.9* Dissolved
	143.9 BPO	35.0 UPD	178.9 Particulate



$$2 \times 32 = 64 \text{ g O}_2$$

60 g HAc needs 64 g O<sub>2</sub> or COD

1 g HAc needs  $\frac{64}{60} = 1.067 \text{ g O}_2 \text{ or COD}$

50 mg COD/l HAc  $\therefore$  mass =  $\frac{50}{1.067} = 46.8 \text{ g HAc/l}$

$$\frac{50}{64} = 0.78 \text{ mmol HAc/l}$$

TOC: HAc has 2 mol C/mol

$\therefore$  has  $2 \times 12 = 24 \text{ g C/mol}$

$$\therefore \text{TOC} = 0.78 \times 24 = 18.75 \text{ mg C/l}$$

$$C_{\text{org}} = f_c \frac{S_{\text{up}}}{f_{\text{c, up}}} = 0.518 \times \frac{100}{143.1} = 35 \text{ mg C/l}$$

Settled WW TOC

	Total 158.8		
VFA 187.5	38.1	15.0	71.9
	83.4	3.5	86.9

$$C_{\text{org}} = f_{\text{c, up}} \frac{S_{\text{up}}}{f_{\text{c, up}}} = 0.518 \times \frac{10}{143.1}$$

COD PS

6

		55475			
VFA		FBS		USO	
50		115		45	20 Dissolved
		BPO		UPO	
		37255		18010	55265 Particulate

Find UPO in PS by mass balance - see in table of 9.1.1

$$Q_{PS} \text{ Supi}_{PS} = Q_{inflow} \text{ Supi}_{Partic} - Q_{Settled} \text{ Supi}_{Settled}$$

$$0.125 \times \text{Supi}_{PS} = 25 \times 100 - 24.875 \times 10$$

$$\text{Supi}_{PS} = 18010 \text{ mg/l}$$

$$\text{Unbio fraction of the PS} = \frac{18010 + 45}{55475} = 0.325 = 32.5\%$$

$$\text{So PS is } 100 - 32.5 = 67.5\% \text{ Bio}$$

TKN of PS

20501

Flow Table

FSA		FSP		USO	
39.1	44.0	38		10.1	44.0

2006.1

790.0

1216.1

$$N_{\text{Supi PS}} = f_{NUB} \frac{\text{Supi PS}}{f_{NUB}} = 0.10 \frac{18010}{1481} = 1216.1 \text{ mg N/l}$$

1/10h 30 ML



TP of PS

TP  
488.4

Flux Table

7

481.1

OP

7.28 | 823 | 995 | 90

480.13

176.1

304.1

Particulate

Coups

$$= f_{\text{Sup PS}} \frac{\text{Sup PS}}{f_{\text{CV PS}}} = 4025 \frac{18010}{1.481}$$

TOC of PS

18553

Flux Table

18.8 | 71.9 | 32.1 | 15.0

1848.1

12121.8

6299.2

BPO

VPO

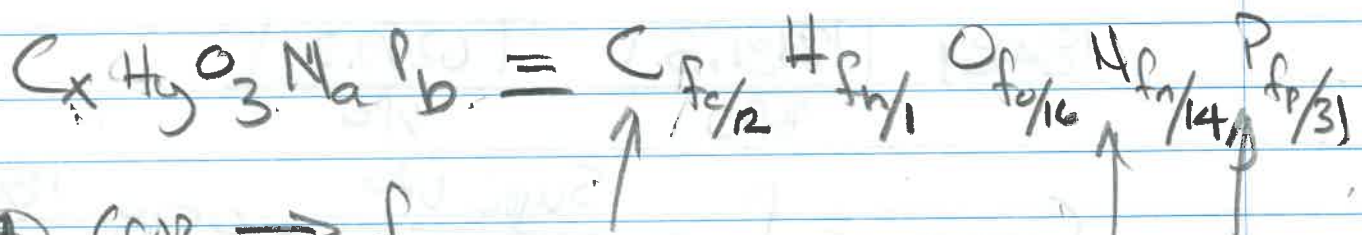
$$\text{Coups} = f_{\text{CVB}} \frac{\text{Supi VPO}}{f_{\text{CV VPO}}} = 4518 \frac{18010}{1.481}$$

$$= 6299.2 \text{ mg C/hr}$$

Q1.4 Primary Sludge	UPO + BRO	Final Value	
		UPO	BRO
COD		18010	37255
VSS	36622.3	12160.7	24461.6
DOC		1299.2	12181.9
org N		1216.1	790.0
org P		304.0	176.0
$f_{cv}$		1.481	1.523
$f_e$		0.518	0.498
$f_n$		0.100	0.0323
$f_p$		0.025	0.0072

$$VSS_{UPO} = \frac{COD_{UPO}}{f_{cvUR}} = \frac{18010}{1.481} = 12160.7$$

$$VSS_{BRO} = 36622.3 - 12160.7 = 24461.6$$



(4) COD  $\rightarrow f_o$

mass balance  $f_n + f_o + f_e + f_n + f_p = 1$  (5)



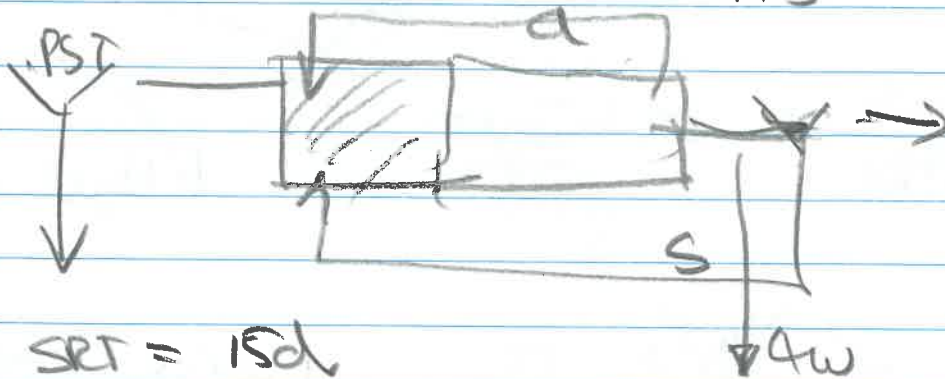
Q2 Activated Sludge PLU  
 Saturated WW T = 16°C

9

$$X_t = TSS = 4.5 \text{ g TSS/l}$$

$$f_{slus} = \frac{\text{USO COD}}{\text{Total COD}} = 4095; \frac{45}{475}$$

$$f_{slup} = \frac{\text{UPO COD}}{\text{Total COD}} = \frac{10}{475} = 4021$$



Flux Table

$$2.1 \text{ Fluxes COD} = Q_i S_{Fi} = 24,875 \times 475 = F_{Si} = 11816 \text{ kg COD/d}$$

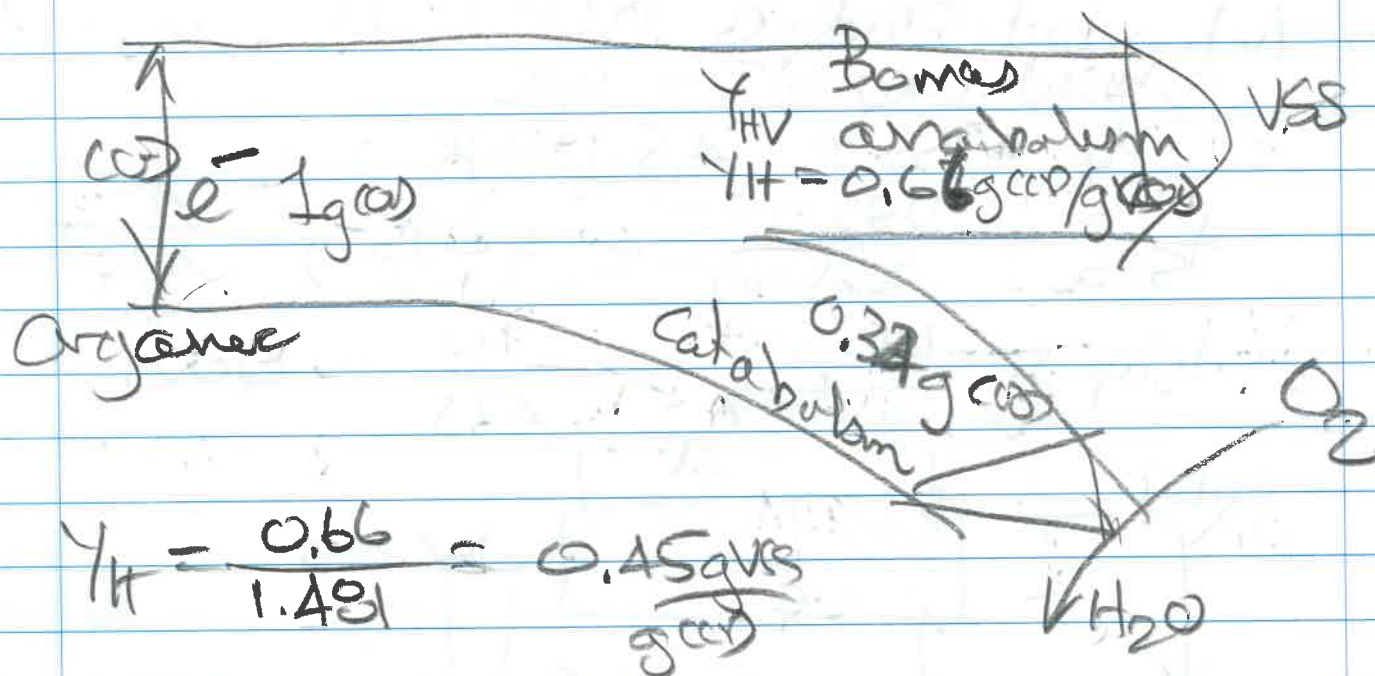
$$F_{Si} = B_{iO} \text{ COD} = F_{Si} (1 - f_{slus} - f_{slup}) = 11816 (1 - 0.095 - 0.021) = 10448 \text{ kg COD/d}$$

$$\begin{aligned} \text{Flux UPO in VSS} &= F_{X_{Ti}} = Q_i \text{ UPO COD conc Supl} \\ &= 24,875 \times 10 / f_{XV} \\ &= \frac{11816 \times 0.021}{1.481} = 1681 \text{ kg VSS/d} \end{aligned}$$

$$\begin{aligned} \text{Flux ISS} &= Q_i X_{Ti} = 24,875 \times 15 \\ &= 373 \text{ kg ISS/d} \end{aligned}$$

$$2.2 \text{ } 16^\circ\text{C } b_{H16} = b_{H20} (1.029)^{16-20} = 0.24 (1.029)^{16-20} = 0.214 / \text{d}$$

$$\frac{Y_{HV} R_s^{\text{SET}}}{1 + b_{HT} R_s} = \frac{0.45 \text{ g VSS/g COD } 15\text{d}}{1 + 0.214 / \text{d} \times 15\text{d}} = 1.603 \frac{\text{g VSS/d}}{\text{g COD}}$$



$$Y_H = \frac{0.66}{1.481} = 0.45 \frac{\text{g VSS}}{\text{g COD}}$$

$$MX_{BH} = \frac{Y_{HV} R_s}{1 + b_{HV} R_s} \quad F_{S_{in}} = 1.603 \times 10448 = 16747 \text{ kg VSS}$$

$$\frac{k_{gVSS,d}}{k_{gCOD}} = \frac{k_{gCOD}}{d} = k_{gVSS}$$

$$MX_{EB} = f_{BH} \cdot b_{BH} R_s \cdot MX_{BH}$$

$$= 0.20 \times 0.214 \times 15 \times 16747$$

$$= 10775 \text{ kg VSS}$$

$$MX_I (UPD) = F_{X_{Ii}} R_s = 168 \frac{\text{kg VSS}}{d} \times 15d$$

$$= 2519 \text{ kg VSS}$$

$$MX_V (VSS) = MX_{BH} + MX_{EB} + MX_I$$

$$= 16747 + 10775 + 2519$$

$$= 30021 \text{ kg VSS}$$

$$MX_{Ii} = F_{X_{Ii}} R_s + f_{Ii} \cdot MX_{BH}$$

$$= 373 \times 15 + 0.15 \times 16747$$

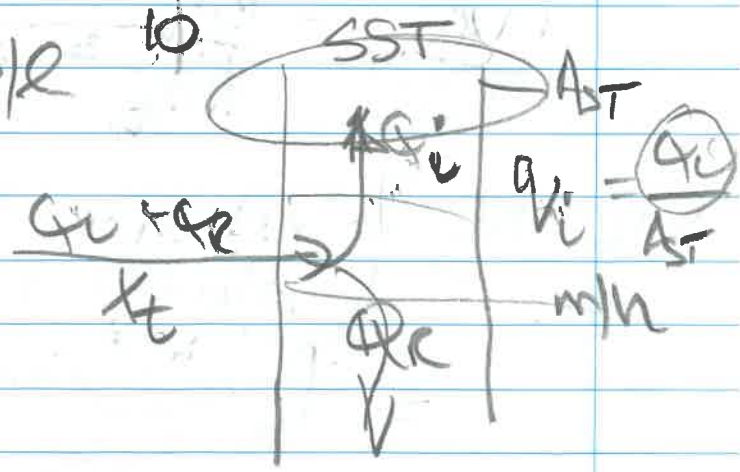
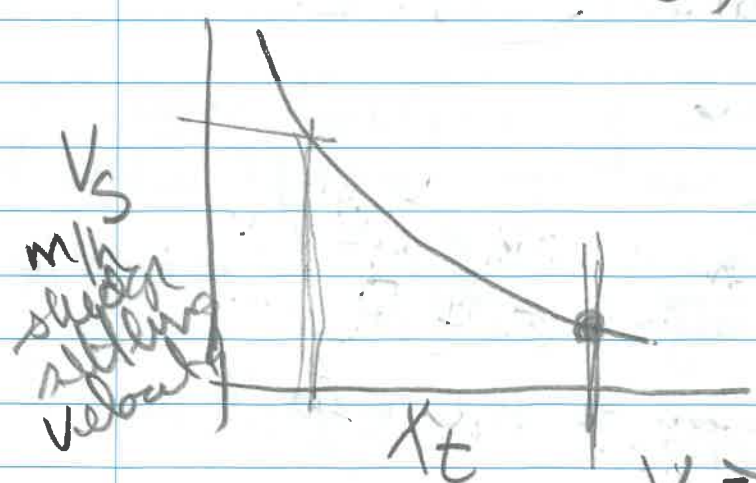
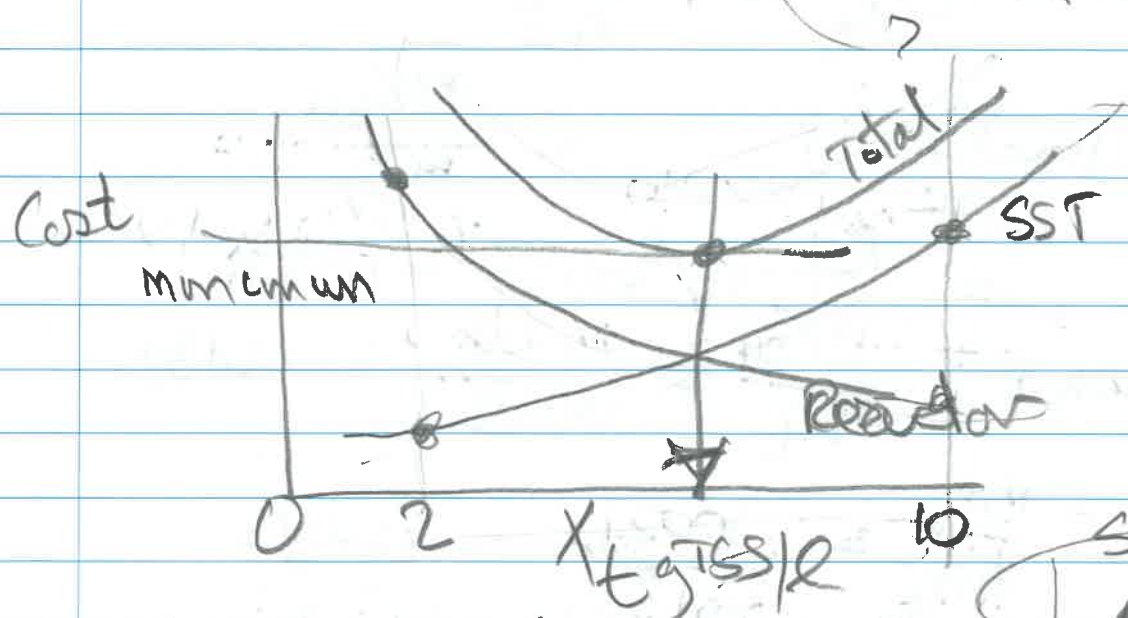


$$= 5597 + 2512 = 8109 \text{ kg ISS.}$$

$$MX_L = VSS + ISS = \mu X_V + \mu X_{TO} \\ = 30021 + 8109 = 38135 \text{ kg ISS.}$$

2.3 
$$V_p = \frac{MX_L}{X_t} = \frac{38135 \text{ kg ISS}}{4.5 \text{ g/m}^3} = 8473 \text{ m}^3$$
  
 $\approx 8.473 \text{ ML}$

$$HRT = \frac{V}{Q_i} = \frac{8.473}{24.875} = 0.34 \text{ d} \\ = 8.14 \text{ h}$$



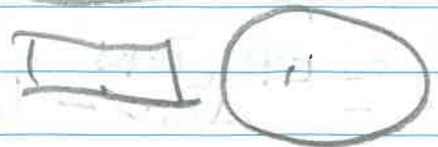
$$V_s \geq q_i = \frac{Q_i}{A_{ST}}$$

12h35 ML

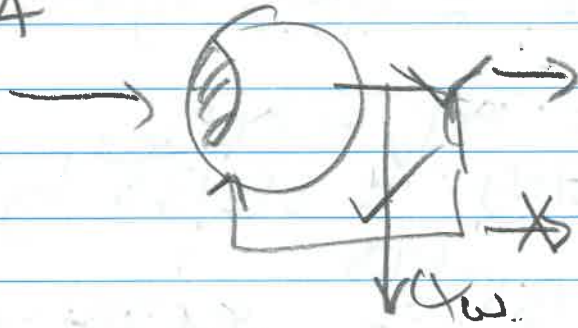
Low  $X_t$  2



High  $X_t$  10



Q2.4



$$R_s = SRT =$$

$$\frac{MX_t \log_{10} TS}{FX_t \log_{10} TS}$$

$$FX_t = \frac{MX_t}{R_s}$$

$$= \frac{38135}{15} = 2542 \log_{10} TS/d$$

$$Q_w = \frac{V}{R_s} = \frac{8473}{15} = 565 \text{ m}^3/d$$

$$Q_w = FX_t / X_t = \frac{2542}{4.5} = 565 \text{ m}^3/d$$

Q2.5 Active fraction  $f_{active} = \frac{MX_{BH}}{MX_V} =$

$$= 16747 / 30021 = 0.558$$

$$f_{active} = \frac{MX_{BH}}{MX_t} = \frac{16747}{38135} = 0.439$$

$$\frac{VSS}{TSS} = \frac{MX_V}{MX_t} = \frac{30021}{38135} = 0.787$$

Q2.6  $M_s$  = nitrogen conc in influent required for sludge production  $\text{mgN/l influent}$

$$= f_n \frac{MX_V}{R_s \phi_i} \cdot \frac{\text{mgN}}{\text{mgVSS}} \cdot \frac{\text{kg VSS}}{\text{d}^2 \text{H/d}} = \text{mgN/l}$$

$$= 0.10 \frac{30021}{15 \times 24.875} = 8.0 \text{ mgN/l influent}$$

Effluent TKN =  $N_e$  no nitrification

$$= N_i - N_s = 50 - 8.0$$

no nitrification = 42.0  $\text{mgN/l}$

$$\text{Effluent FSA (Nbe)} = \text{Effluent TKN} - N_{onVSS} = 42.0 - 1.1 = 40.9 \text{ mgN/l}$$



$$\text{Influent FSA} = 39.1 \text{ mg N/l}$$

$$\text{So effluent FSA} = 40.9 \text{ mg N/l}$$

go to TKN block diagram.

$$39.1 + 3.8 + 5.33 - \underbrace{(8.0 - 0.67)}_{\substack{\text{N}_s - \text{N}_{\text{orgi}} \\ \text{N taken up to} \\ \text{FSA produced} \\ \text{CH}_2\text{O} + \text{End Residue}}} = 40.9!$$

FSA      FBSO      BPO      organic from influent

Q27 Oxygen Demand

$$FO_c \text{ kg/d} = F_{Sbi} \left\{ \begin{array}{l} \text{calculate} \\ (1 - f_{cv}) Y_{Hv} \\ \text{growth} \end{array} \right. + f_{cv} (1 - f_H) b_{HT} \left\{ \frac{Y_{Hv} R_s}{1 + b_{HT} R_s} \right\}$$

$$= 10448 \left\{ (1 - 1.481 \times 0.45) + 1.481 (1 - 0.2) 0.214 \times 1.603 \right\}$$

$$= 7732 \text{ kg/d organic removal.}$$

$FO_n$  for complete nitrification. ce.

all FSA  $\rightarrow \text{NO}_3^-$

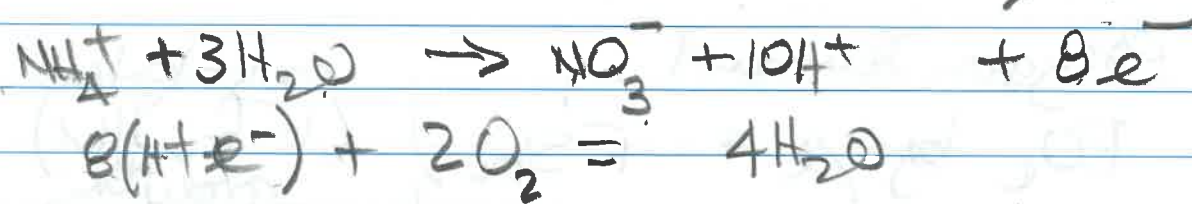
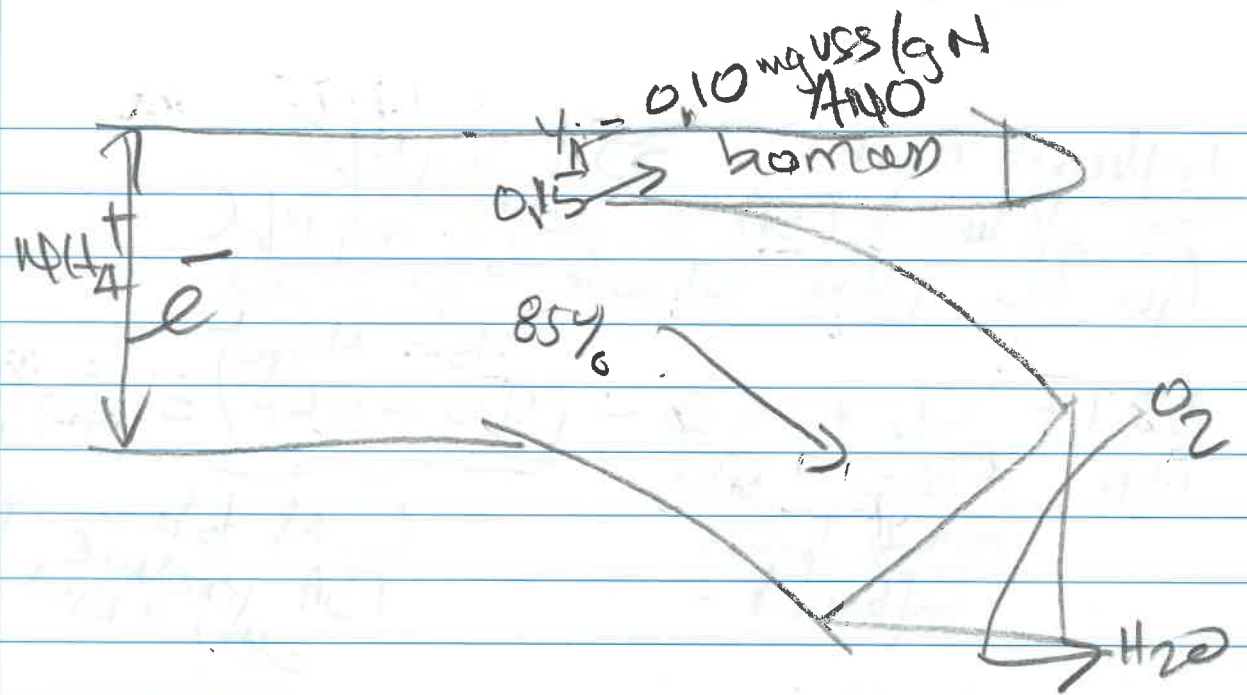
$$= 4.57 \text{ kg; effluent FSA} \xrightarrow{40.9 \text{ mg N/l}}$$

$$= 4649 \text{ kg/d}$$

$$FO_t = FO_c + FO_n = 7732 + 4649 = 12381 \text{ kg/d}$$

$$OUR = \frac{FO_t \cdot 10^6}{V_{\text{reactor}} \cdot 24 \times 10^3} = \frac{12381}{8472 \times 24 \times 10^3} \frac{\text{mgo}}{\text{L.h}} =$$

1A



1 mole FSA as N needs 64g O (2x32)  
 1g N needs  $\frac{64}{14} = 4.57 \text{ g O/g N}$

Q2.8  $\text{C}_5\text{H}_7\text{O}_2\text{N}_{0.9}\text{P}_{0.11}$  biomass

$$f_p = \frac{0.1 \times 31}{12 \times 5 + 7 + 2 \times 16 + 0.9 \times 14 + 0.1 \times 31} = \frac{3.1}{114.7}$$

$$= 4027 \text{ g P/g VSS} \quad \text{ck but we use } 0.025 \text{ g P/g VSS.}$$

$$P_s = f_p \frac{MX}{P_s \phi_c} = 4025 \frac{30021}{15 \times 24.875}$$

$$= 20 \text{ mg P/l} \quad (\text{notice } \frac{1}{4} \text{ of } M_s!)$$

$\frac{1}{4}$  of  $f_m$

$$P_{te} = P_{ti} - P_s = 9.6 - 20 = 7.6 \text{ mg TP-P/l}$$

$$P_{se} \text{ OP in effluent} = P_{te} - P_{in VSO}$$

$$= 7.6 - 0 \quad (\text{from block diagram})$$

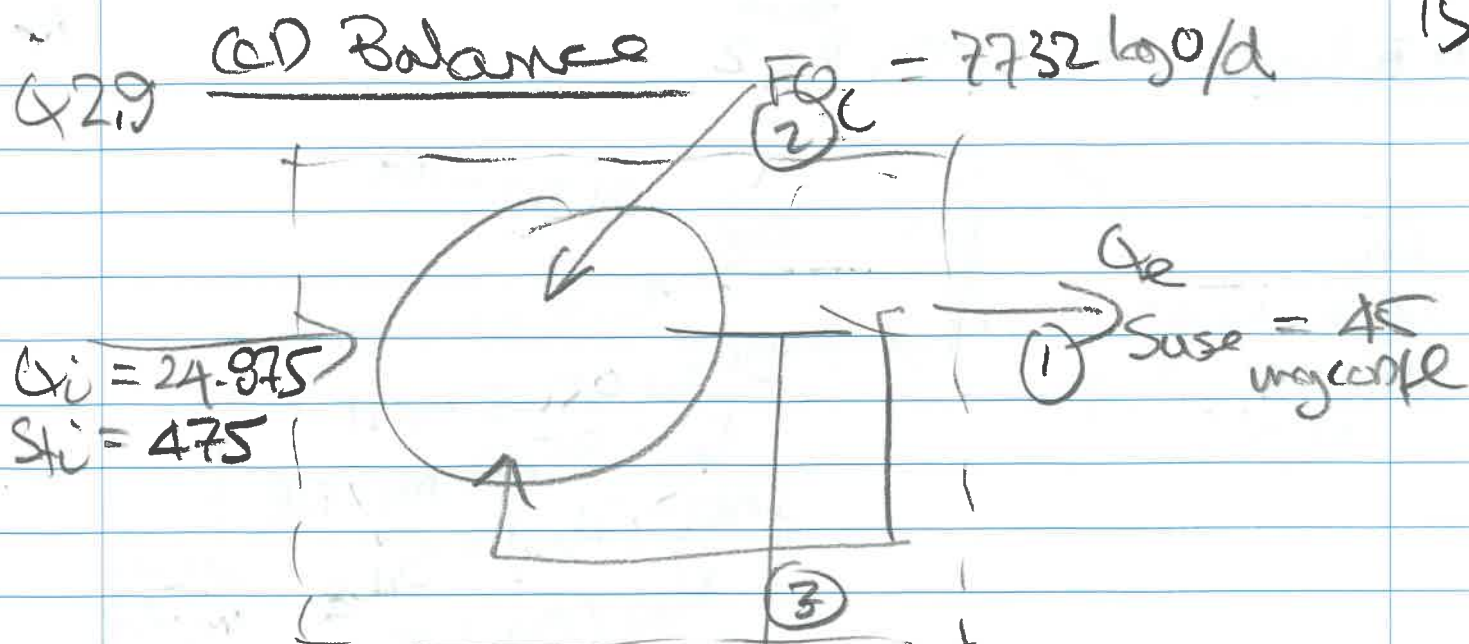
$$P_{se} = 7.6 \text{ mg OP-P/l}$$



Q29

COD Balance

15



$$\begin{aligned} \text{COD in} &= Q_i S_i \\ &= 24.875 \times 475 \\ &= 11816 \text{ kg COD/d} \end{aligned}$$

$$\begin{aligned} Q_w &= 565 \text{ m}^3/\text{d} \\ X_t &= 4500 \text{ mg TSS/l} \\ X_v &= \frac{VSS}{TSS} \times 4500 \\ &= \frac{0.787}{1.5} \times 4500 \\ &= 2352 \text{ mg VSS/l} \end{aligned}$$

$$\begin{aligned} \text{(1) Effluent COD} &= Q_e S_{use} = (Q_i - Q_w) S_{use} \\ &= (24.875 - 0.565) \times 45 \\ &= 24.310 \times 45 = 1094 \text{ kg COD/d} \end{aligned}$$

$$\text{(2) } FOC = 7732 \text{ kg O/d} \approx \text{kg COD/d}$$

$$\begin{aligned} \text{(3) Waste flow:} &= Q_w (S_{use} + f_v X_v) \\ &= 0.565 (45 + 1.481 \times 2352) \\ &= 2986 \text{ kg COD/d} \end{aligned}$$

$$\begin{aligned} \text{Total COD out} &= \text{(1)} + \text{(2)} + \text{(3)} \\ &= 1094 + 7732 + 2986 \\ &= 11815 \text{ kg COD/d} \end{aligned}$$

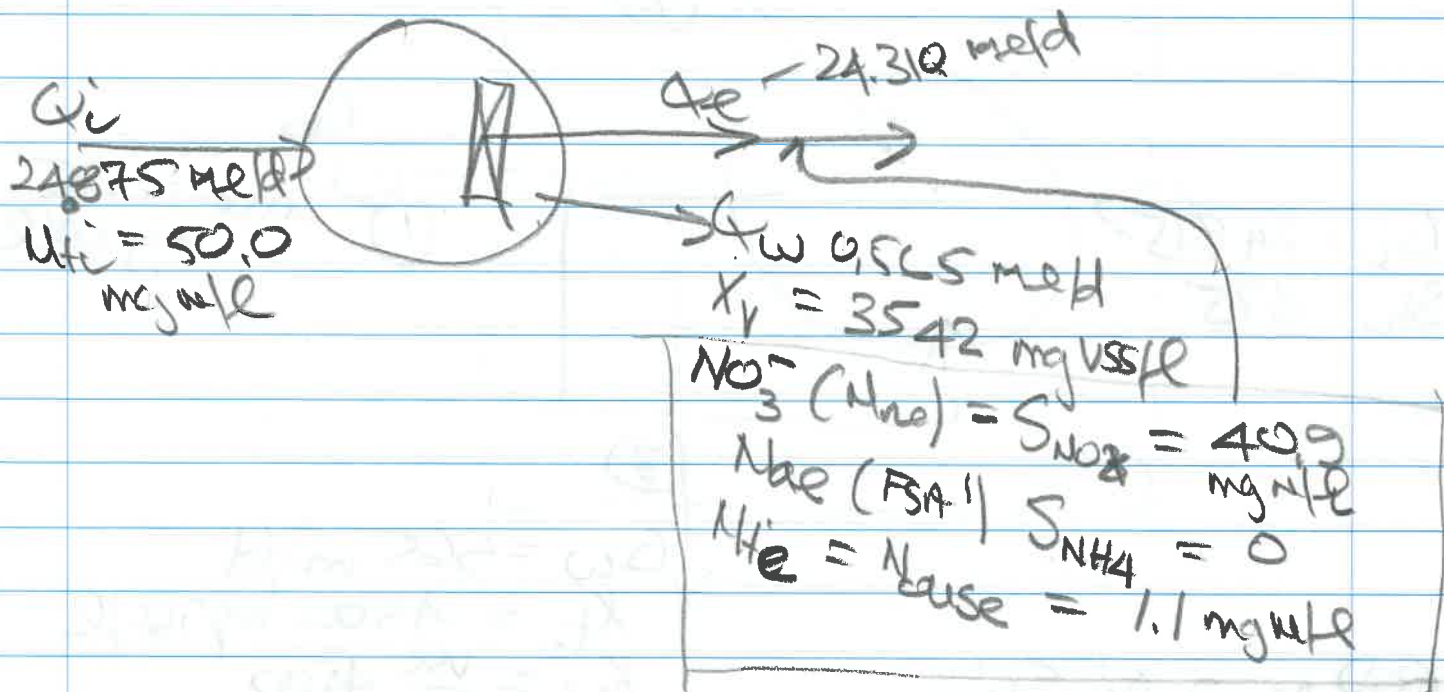
$$\begin{aligned} \text{COD balance \%} &= \frac{\text{COD out}}{\text{COD in}} \times 100 = \frac{11815}{11816} \times 100 \\ &= 99.99\% \quad \text{Error} \sim 0.01\% \end{aligned}$$

$$\text{Acceptable error} < \pm 0.1\% = \frac{1}{1000}$$

12h 30 min  
Error/day

N Balance 27/2/18 <sup>Start</sup> Day 2

16



$$Q_i N_{Ti} = ? Q_w (X_v f_n + \underbrace{N_{Te}}_{\text{TKN}} + \underbrace{N_{ne}}_{\text{NO}_3}) + Q_e (\underbrace{N_{Te}}_{\text{TKN}} + \underbrace{N_{ne}}_{\text{NO}_3})$$

$$24,875 \times 50 = ? 0.565 (3542 \times 0.1 + 1.1 + 40.9) + 24.31 (1.1 + 40.9)$$

$$1244.9 \text{ kg N/d} = ? 223.8 + 1021.0 = 1244.8 \text{ kg N/d}$$

$$\text{N balance \%} = \frac{N_{\text{out}}}{N_{\text{in}}} \times 100 = \frac{1244.8}{1244.9} \times 100 = 100.0 < 0.1\% \checkmark$$

P Balance

$$Q_i P_{Ti} = ? Q_w (X_v f_p + P_{Te}) + Q_e (P_{Te})$$

$$P_{Te} = \underbrace{P_{\text{ouse}}}_{0.0} + \text{OP} \quad P_{se} = S_{\text{PA}}$$

$$24,875 \times 9.6 = ? 0.565 (3542 \times 0.025 + 7.6) + 24.31 \times 7.6$$

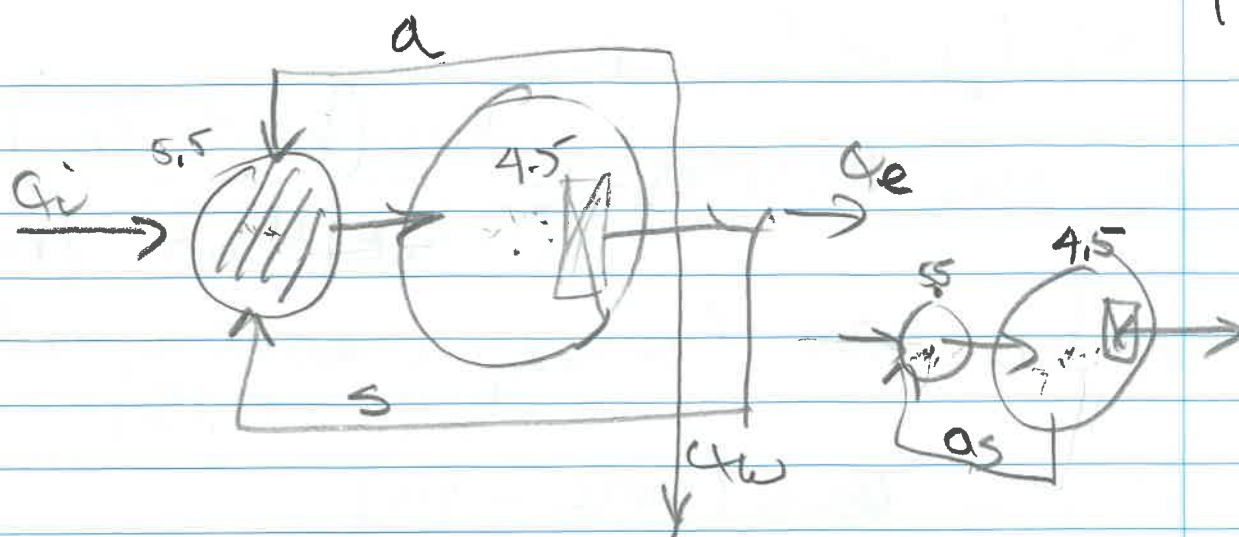
$$238.8 = ? 54.3 + 184.5 = 238.8 \text{ kg P/d}$$

P balance = 100%



Q3

17



$$\mu_{Am20} \text{ ANO} = 0.45/d \quad 4.3 \text{ to } 0.8/d$$

$$\mu_{Am16} = \mu_{Am20} (1.123)^{T-20}$$

$$= 0.45 (1.123)^{16-20} = 0.283/d$$

$$K_{nt16} = K_{nt20} (1.123)^{16-20} = 0.63 \text{ mg FSA-N/l}$$

$$b_{AT16} = b_{AT20} (1.029)^{16-20} = 0.036/d$$

$$\text{L } 404/d$$

$$\text{Safety factor} = SF = 1.25$$

$f_{2m}$  = mass unreacted sludge mass fraction

$$= 1 - \frac{SF (b_{AT} + 1/P_s)}{\mu_{AmT}}$$

#####

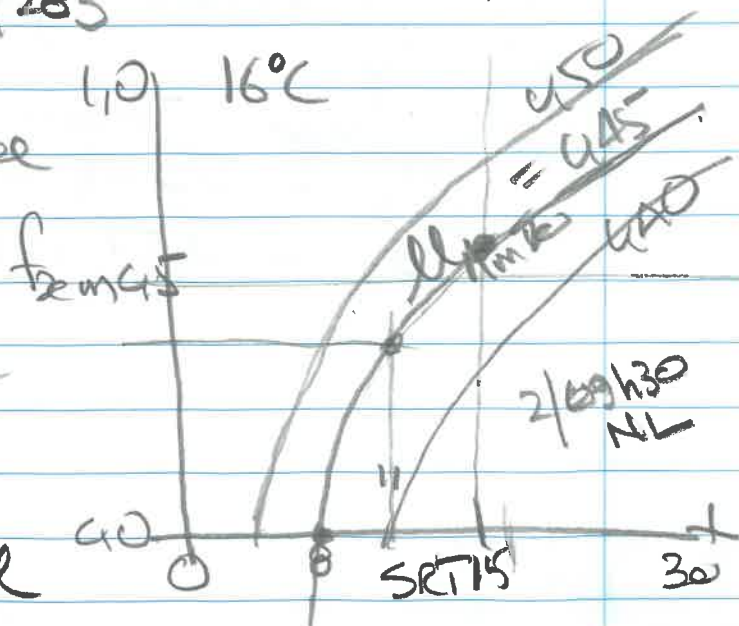
$$= 1 - \frac{1.25 (0.036 + 1/15)}{0.283} = 0.548$$

$$MX_L = 38135 \log TSS$$

So 54.8% of  $MX_L$  can be unreacted and still nitify well.

$$N_{ae} (FSA \text{ eff}) = \frac{K_{nt}}{SF - 1}$$

$$f_{act} = f_{2m} = \frac{0.63}{1.25 - 1} = 2.52 \text{ mg FSA-N/l}$$



If  $f_{act} < f_{crit}$  then

$$N_{ae} (EFF/FSA) = \frac{K_{NT} (b_{NT} + 1/R_s)}{(1 - f_{act}) \mu_{AMT} - (b_{NT} + 1/R_s)}$$

$f_{act} = 0.39$  (in 4 anaerobic reactor  
 $f_{act} = 0.15$ )

$$= \frac{0.63 (4036 + 1/15)}{(1 - 0.39) 0.283 - (0.036 + 1/15)}$$

$$= 0.91 \text{ mg FSA-N/l}$$

Effluent TKN =

$$N_{te} = N_{ae} + \frac{Q_{orgH}}{N_{biom}}$$

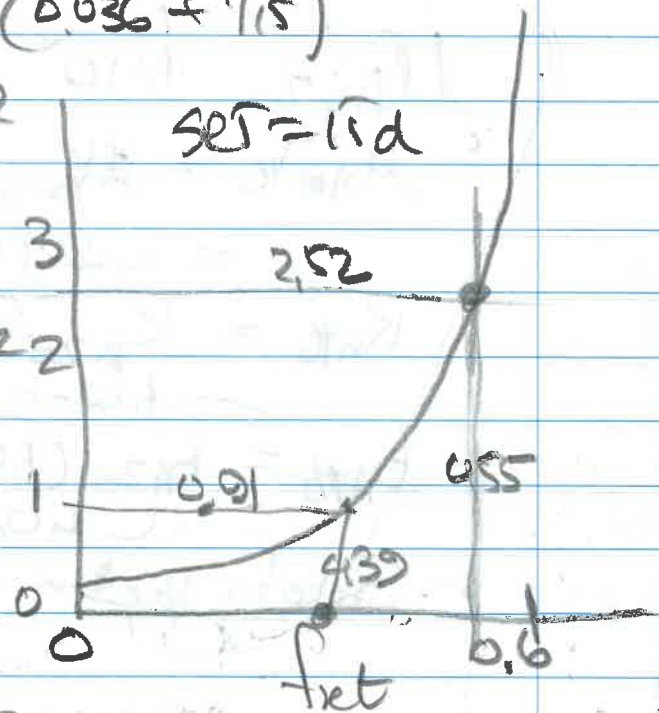
$$0.91 + 1.1 = 2.0 \text{ mg TKN-N/l}$$

Nitrification Capacity

$$N_c = N_{ti} - N_s - N_{te}$$

$$= 50.0 - 8.0 - 2.0$$

$$= 40.0 \text{ mg } NO_3\text{-N/l}$$



$$FO_n = 4.57 \times Q_i \times N_c = 4.57 \times 24,875 \times 40$$

$$= 4547 \text{ kg/d}$$

$f_{act} = f_{crit}$  Then  $N_{te} = 2.52 + 1.1 = 3.62 \text{ mg N/l}$

$$N_c = 50 - 8 - 3.62 = 38.4$$

$$FO_n = 4.57 \times 24,875 \times 38.4 =$$

less



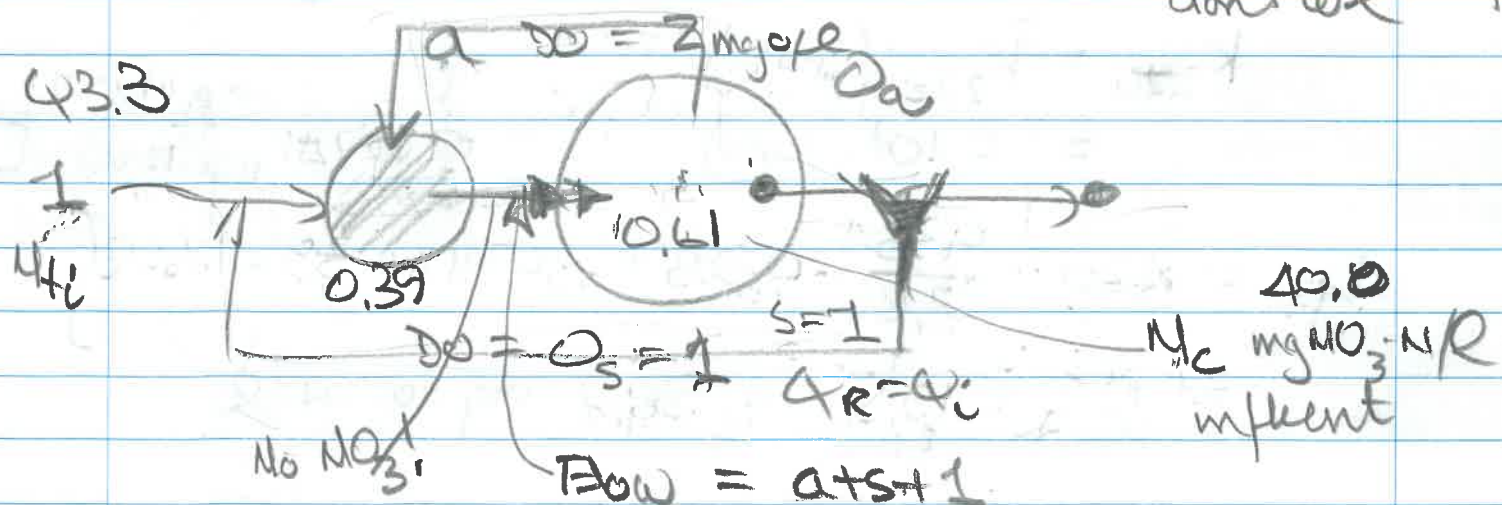
Q3.2 Reacting Biodeg COD fraction with respect to the unreacted Biodeg COD

$$f_{sb's} = \frac{\text{VFA} + \text{FBSO}}{\text{VFA} + \text{FBSO} + \text{BPO}} = \frac{50 + 115}{50 + 115 + 285} = 0.393$$

$$f_{sb's} \neq f_{s'bs} = \frac{\text{VFA} + \text{FBSO}}{\text{VFA} + \text{FBSO} + \text{BPO} + \text{URD} + \text{USD}}$$

$$f_{s'bs} = \frac{50 + 115}{475} = 0.347 \quad \text{don't use}$$

Q3.3

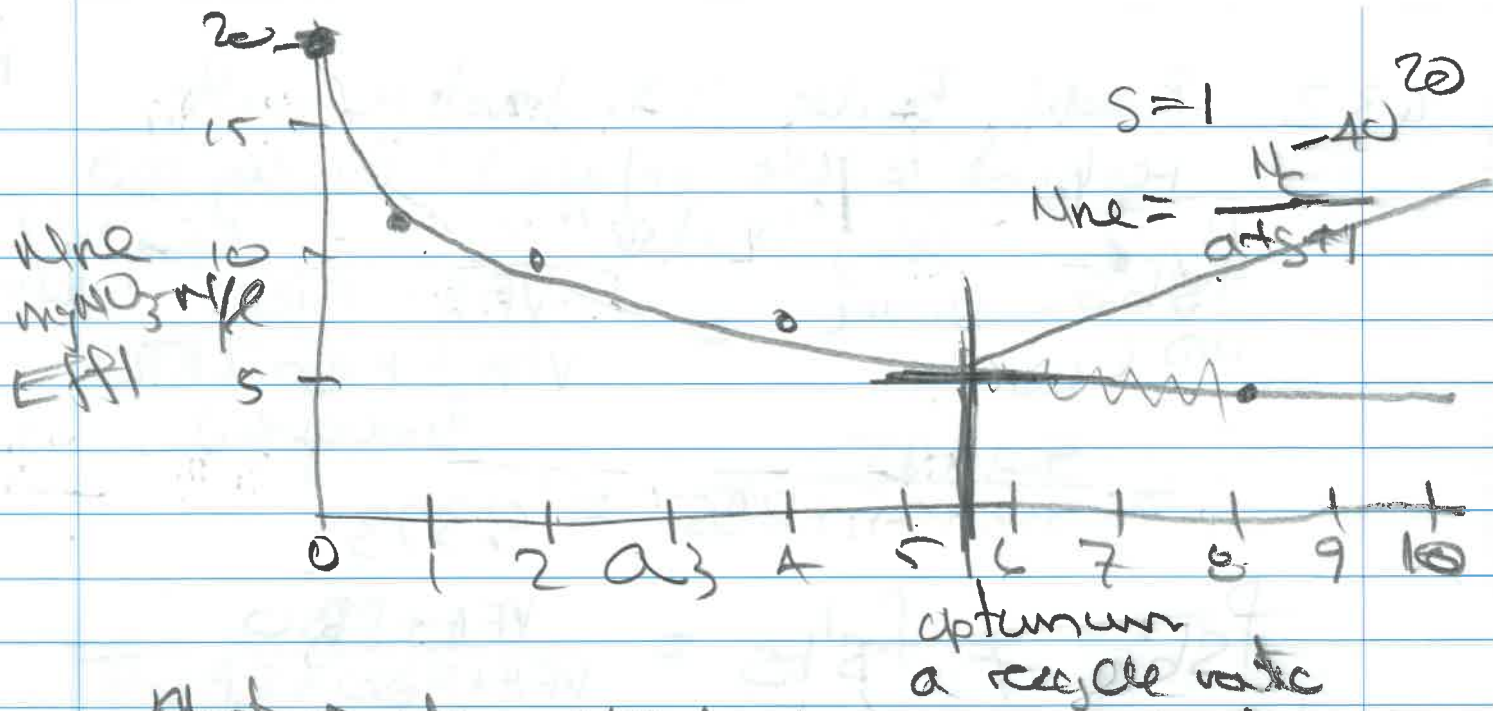


$$\text{Nitrate in anoxic} = \frac{N_c \cdot 1}{Q + S + 1}$$

$$\text{Nitrate load on anoxic} = \frac{N_c}{Q + S + 1} + \frac{Q_r}{2.86} + S \left\{ \frac{N_c}{Q + S + 1} + \frac{Q_r}{2.86} \right\}$$

But Anoxic has a certain denitrification potential  $D_{p1}$  (primary anoxic).

$$N_{re} = \frac{N_c}{Q + S + 1} \quad \text{on condition that } NO_3 \text{ from anoxic is zero!}$$



$D_{p1}$  is when  $\text{NO}_3$  load on aerobic =  $D_{p1}$

$$D_{p1} = S_{bi} \left\{ \frac{(1 - F_{av} Y_{Hv})}{2.86} f_{Sb's} + K_{21} f_{Sb's} \frac{Y_{Hv} R_s}{1 + K_{21} R_s} \right\}$$

RBCUD                      BRO

$$K_{210} = K_{220} (1.08)^{T-20}$$

$$= 0.104 (1.08)^{16-20} = 0.0741 \frac{\text{mg NO}_3\text{-N}}{\text{mg O}_2 \text{ used, d}}$$

$$D_{p1} = 420 \left\{ \frac{4.334}{2.86} 0.393 + 0.0741 \times 4.39 \times 1.603 \right\}$$

$$= 19.2 + 19.5 = 38.7 \text{ mg NO}_3\text{-N/l}$$

RBCUD                      BRO

$$D_{p1} = \text{nitrate load}$$

$$= a \left\{ \frac{N_c}{a+S+1} + \frac{O_a}{2.86} \right\} + S \left\{ \frac{N_c}{a+S+1} + \frac{O_a}{2.86} \right\}$$

only unknown is  $a$  so solve for  $a$

$$a_{opt} = \frac{-B + \sqrt{B^2 + 4AC}}{2A} \quad \text{not error}$$

$$A = \frac{O_a}{2.86}; B = N_c - D_{p1} + \frac{(1+S)O_a + S O_s}{2.86}$$

$$C = (1+S) \left\{ D_{p1} - \frac{S O_s}{2.86} \right\} - S N_c$$