

## Ecoadvisor model formulas

*Institut Català de Recerca de l'Aigua (ICRA)*

### Compilation command

```
groff -e -t -ms formulas.ms -T pdf -K utf-8
```

## 1. State Variables

### 1.1. Inputs

$$Q \quad (\text{ML/d})$$

$$S_{VFA}, S_{FBSO}, X_{BPO}, X_{UPO}, S_{USO}, X_{iSS}, S_{FSA}, S_{OP}, S_{NOx} \quad (\text{mg/L})$$

### 1.2. Total chemical oxygen demand (COD = $S_t$ )

$$(\text{mg/L})$$

where:

$$S_{bs} = S_{VFA} + S_{FBSO} \quad (\text{mg/L})$$

$$S_t = S_b + S_u$$

$$S_t = S_s + S_p$$

### 1.3. Mass ratios for COD, N, P and C

State Variable	COD ( $f_{cv}$ )	N ( $f_N$ )	P ( $f_P$ )	C ( $f_C$ )
$S_{VFA}$	1.0667	0.0000	0.0000	0.400
$S_{FBSO}$	1.4200	0.0464	0.0118	0.471
$X_{BPO}$	1.5230	0.0323	0.0072	0.498
$X_{UPO}$	1.4810	0.1000	0.0250	0.518
$S_{USO}$	1.4930	0.0366	0.0000	0.498

### 1.4. Total Kjehdahl Nitrogen (TKN)

$$TKN = N_t = N_o + S_{FSA} \quad (\text{mg/L})$$

where:

$$\begin{aligned}
 N_o &= N_{obs} + N_{obp} + N_{ous} + N_{oup} \\
 N_{obs} &= S_{VFA} \frac{f_{N_{VFA}}}{f_{cv_{VFA}}} + S_{FBSO} \frac{f_{N_{FBSO}}}{f_{cv_{FBSO}}} \\
 N_{obp} &= X_{BPO} \frac{f_{N_{BPO}}}{f_{cv_{BPO}}} \\
 N_{ous} &= S_{USO} \frac{f_{N_{USO}}}{f_{cv_{USO}}} \\
 N_{oup} &= S_{UPO} \frac{f_{N_{UPO}}}{f_{cv_{UPO}}}
 \end{aligned}$$

### 1.5. Total Phosphorus (TP)

$$TP = P_t = P_o + S_{OP} \quad (\text{mg/L})$$

where:

$$\begin{aligned}
 P_o &= P_{obs} + P_{obp} + P_{ous} + P_{oup} \\
 P_{obs} &= S_{VFA} \frac{f_{P_{VFA}}}{f_{cv_{VFA}}} + S_{FBSO} \frac{f_{P_{FBSO}}}{f_{cv_{FBSO}}} \\
 P_{obp} &= X_{BPO} \frac{f_{P_{BPO}}}{f_{cv_{BPO}}} \\
 P_{ous} &= S_{USO} \frac{f_{P_{USO}}}{f_{cv_{USO}}} \\
 P_{oup} &= S_{UPO} \frac{f_{P_{UPO}}}{f_{cv_{UPO}}}
 \end{aligned}$$

### 1.6. Total Organic Carbon (TOC)

$$TOC = C_t = C_{obs} + C_{obp} + C_{ous} + C_{oup} \quad (\text{mg/L})$$

where:

$$\begin{aligned}
 C_{obs} &= S_{VFA} \frac{f_{C_{VFA}}}{f_{cv_{VFA}}} + S_{FBSO} \frac{f_{C_{FBSO}}}{f_{cv_{FBSO}}} \\
 C_{obp} &= X_{BPO} \frac{f_{C_{BPO}}}{f_{cv_{BPO}}} \\
 C_{ous} &= S_{USO} \frac{f_{C_{USO}}}{f_{cv_{USO}}} \\
 C_{oup} &= S_{UPO} \frac{f_{C_{UPO}}}{f_{cv_{UPO}}}
 \end{aligned}$$

## 2. Activated sludge

### 2.1. Inputs

$$T, V_p, R_s, RAS, mass_{FeCl_3}$$

### 2.2. Volatile suspended solids (VSS)

$$Y_H = 0.45 \quad (\text{gVSS/gCOD})$$

$$b_H = 0.24 \quad (1/\text{d})$$

$$b_{HT} = b_H(1.029)^{(T-20)} \quad (1/\text{d})$$

$$f_{X_{BH}} = \frac{Y_H \cdot R_s}{1 + b_{HT} \cdot R_s} \quad (\text{gVSS} \cdot \text{d/gCOD})$$

$$MX_{BH} = FS_{bi} \cdot f_{X_{BH}} \quad (\text{kgVSS})$$

$$MX_{EH} = f_H \cdot b_{HT} \cdot R_s \cdot MX_{BH} \quad (\text{kgVSS})$$

$$MX_I = FX_{ii} \cdot R_s \quad (\text{kgVSS})$$

$$MX_V = MX_{BH} + MX_{EH} + MX_I \quad (\text{kgVSS})$$

$$X_V = \frac{MX_V}{V_p} \quad (\text{kgVSS/m}^3)$$

### 2.3. Total inert solids (iSS)

$$f_{iOHO} = 0.15 \quad (\text{giSS/gVSS})$$

$$MX_{IO} = FiSS \cdot R_s + f_{iOHO} \cdot MX_{BH} + F_{iSS\_precipitation} \cdot R_s \quad (\text{kgiSS})$$

### 2.4. Total suspended solids (TSS)

$$MX_T = MX_V + MX_{IO} \quad (\text{kgTSS})$$

$$X_T = \frac{MX_T}{V_p} \quad (\text{kgTSS/m}^3)$$

### 2.5. Nominal hydraulic retention time

$$HRT = \frac{V_p}{Q} \quad (\text{d})$$

## 2.6. Wastage flowrate

$$Q_w = \frac{V_p}{R_s} \quad (\text{ML/d})$$

## 2.7. Effluent flowrate

$$Q_e = Q - Q_w \quad (\text{ML/d})$$

## 2.8. Nitrogen and Phosphorus required for sludge production

$$N_s = \frac{f_{N_{OHO}}(MX_{BH} + MX_{EH}) + f_{N_{UPO}}MX_I}{R_s \cdot Q} \quad (\text{mg/L})$$

$$P_s = \frac{f_{P_{OHO}}(MX_{BH} + MX_{EH}) + f_{P_{UPO}}MX_I}{R_s \cdot Q} \quad (\text{mg/L})$$

## 2.9. Effluent Ammonia concentration

$$N_{ae} = N_{ti} - N_s - N_{ouse} \quad (\text{mg/L})$$

## 2.10. Effluent Orthophosphate concentration

$$P_{se} = P_{ti} - P_s - P_{ouse} - P_{precipitation} \quad (\text{mg/L})$$

## 2.11. Wastage solids concentration

$$BPO_{was} = f_{cv_{BPO}}(1 - f_H)X_{BH} \quad (\text{mg/L})$$

$$UPO_{was} = f_{cv_{UPO}}(f_H X_{BH} + X_{EH} + X_I) \quad (\text{mg/L})$$

$$iSS_{was} = \frac{MX_{IO}}{V_p} \quad (\text{mg/L})$$

## 2.12. Oxygen demand

$$FO_c = Y_H(1 - f_{cv_{OHO}}) + f_{cv_{OHO}}(1 - f_H) \cdot b_{HT} \cdot f_{X_{BH}} \quad (\text{kgO/d})$$

$$FO_n = 4.57 \cdot Q \cdot N_{ae} \quad (\text{kgO/d})$$

$$FO_t = FO_c + FO_n \quad (\text{kgO/d})$$

$$OUR = \frac{FO_t}{V_p} \quad (\text{mgO/L} \cdot \text{h})$$

### 3. Nitrification

#### 3.1. Inputs

$$SF, f_{xt}, DO, pH$$

#### 3.2. Nitrifier kinetics

$$\mu_{Am} = 0.45 \quad (1/d)$$

$$\mu_{AmT} = \mu_{Am}(1.123)^{T-20} \quad (1/d)$$

$$K_O = 0.3 \quad (\text{mgO/L})$$

$$\mu_{AmO} = \mu_{AmT} \frac{DO}{K_O + DO} \quad (1/d)$$

$$K_i = 1.13, K_{ii} = 0.3, K_{\max} = 9.5$$

$$\mu_{AmpH} = \mu_{AmO}(2.35)^{pH-7.2} K_i \frac{K_{\max} - pH}{K_{\max} + K_{ii} - pH} \quad (1/d)$$

$$Y_A = 0.1 \quad (\text{gVSS/gNH}_4)$$

$$Y_{AT} = Y_A^{T-20} \quad (\text{gVSS/gNH}_4)$$

$$K_n = 1.0 \quad (\text{mg/L})$$

$$K_{nT} = K_n(1.123)^{T-20} \quad (\text{mg/L})$$

$$b_A = 0.04 \quad (1/d)$$

$$b_{AT} = b_A(1.029)^{T-20} \quad (1/d)$$

#### 3.3. Maximum design unaerated sludge mass fraction

$$f_{xm} = 1 - SF \frac{b_{AT} + \frac{1}{R_s}}{\mu_{AmpH}} \quad (\emptyset)$$

#### 3.4. Minimum sludge age for nitrification

$$R_{sm} = \frac{1}{\mu_{AmpH}(1 - f_{xt}) - b_{AT}} \quad (d)$$

### 3.5. Effluent Ammonia concentration

$$N_{ae} = \frac{K_{nT}(b_{AT} + \frac{1}{R_s})}{\mu_{AmpH}(1 - f_{xt}) - b_{AT} - \frac{1}{R_s}} \quad (\text{mg/L})$$

### 3.6. Nitrification capacity

$$N_c = N_{ti} - N_s - (N_{ae} + N_{ouse}) \quad (\text{mg/L})$$

### 3.7. ANO biomass

$$f_{X_{BA}} = \frac{Y_{AT}R_s}{1 + b_{AT} \cdot R_s} \quad (\text{gVSS} \cdot \text{d/gNH}_4)$$

$$MX_{BA} = Q \cdot N_c \cdot f_{X_{BA}} \quad (\text{kgVSS})$$

$$X_{BA} = \frac{MX_{BA}}{V_p} \quad (\text{kgVSS/m}^3)$$

## 4. Denitrification

### 4.1. Inputs

$$IR, DO_{RAS}, alk_i$$

### 4.2. Denitrification kinetics

$$K_1^{20} = 0.72, K_2^{20} = 0.10, K_3^{20} = 0.10, K_4^{20} = 0.00 \quad (\text{mgN/mgVSS}\cdot\text{d})$$

$$K_{1T} = K_1^{20}(1.200)^{T-20} \quad (\text{mgN/mgVSS}\cdot\text{d})$$

$$K_{2T} = K_2^{20}(1.080)^{T-20} \quad (\text{mgN/mgVSS}\cdot\text{d})$$

$$K_{3T} = K_3^{20}(1.029)^{T-20} \quad (\text{mgN/mgVSS}\cdot\text{d})$$

$$K_{4T} = K_4^{20}(1.029)^{T-20} \quad (\text{mgN/mgVSS}\cdot\text{d})$$

### 4.3. Denitrification potential

$$D_{p1RBSO} = \frac{S_{bsl}(1 - f_{cv}Y_H)}{2.86} \quad (\text{mgN/L})$$

$$D_{p1BPO} = K_{2T}f_{xt}S_{bi}f_{X_{BH}} \quad (\text{mgN/L})$$

$$D_{p1} = D_{p1RBSO} + D_{p1BPO} \quad (\text{mgN/L})$$

### 4.4. Optimum internal recirculation

$$a_{opt} = \frac{-B + \sqrt{B^2 + 4AC}}{2A} \quad (\emptyset)$$

where:

$$A = \frac{DO}{2.86}$$

$$B = N_c - D_{p1} + \frac{(1 + RAS) \cdot DO + RAS \cdot DO_{RAS}}{2.86}$$

$$C = (1 + RAS) \cdot (D_{p1} - \frac{RAS \cdot DO_{RAS}}{2.86}) - RAS \cdot N_c$$

#### 4.5. Minimum effluent NOx concentration

$$N_{ne\_opt} = \frac{N_c}{a_{opt} + RAS + 1} \quad (\text{mgN/L})$$

#### 4.6. Effluent nitrate

*if* ( $a < a_{opt}$ )

$$N_{ne} = \frac{N_c}{a + RAS + 1} \quad (\text{mgN/L})$$

*if* ( $a > a_{opt}$ )

$$N_{ne} = N_c - D_{p1} + \frac{a * DO + RAS * DO_{RAS}}{2.86} \quad (\text{mgN/L})$$

#### 4.7. Nitrogen gas

$$FN_2 = Q(N_c - N_{ne}) \quad (\text{kgN/d})$$

#### 4.8. Oxygen recovered by denitrification

$$FO_d = 2.86 \cdot Q \cdot (N_c - N_{ne}) \quad (\text{kgO/d})$$

$$FO_t = FO_c + FO_n - FO_d \quad (\text{kgO/d})$$

#### 4.9. Effluent alkalinity

$$alk_e = alk_i + 3.57 \cdot (N_{obi} - (N_s - N_{oupi})) - 7.14 \cdot N_c + 2.86 \cdot (N_c - N_{ne}) \quad (\text{mg/L})$$