Ecoadvisor model formulas

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Compilation command

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groff -e -ms formulas.ms -T pdf -K utf-8
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1. Activated sludge

1.1. Inputs

$$T, V_{p,} R_{s,} RAS, mass_{FeCl_3}$$

1.2. Volatile suspended solids (VSS)

$$Y_H = 0.45 \quad \text{(gVSS/gCOD)}$$

$$b_H = 0.24 \quad \text{(1/d)}$$

$$b_{HT} = b_H (1.029)^{(T-20)} \quad \text{(1/d)}$$

$$f_{X_{BH}} = \frac{Y_H \cdot R_s}{1 + b_{HT} \cdot R_s} \quad \text{(gVSS·d/gCOD)}$$

$$MX_{BH} = FS_{bi} \cdot f_{X_{BH}} \quad \text{(kgVSS)}$$

$$MX_{EH} = f_H \cdot b_{HT} \cdot R_s \cdot MX_{BH} \quad \text{(kgVSS)}$$

$$MX_I = FX_{ti} \cdot R_s \quad \text{(kgVSS)}$$

$$MX_V = MX_{BH} + MX_{EH} + MX_I \quad \text{(kgVSS)}$$

$$X_V = \frac{MX_V}{V_p} \quad \text{(kgVSS/m}^3\text{)}$$

1.3. Total inert solids (iSS)

$$f_{iOHO} = 0.15 \quad \text{(giSS/gVSS)}$$

$$MX_{IO} = FiSS \cdot R_s + f_{iOHO} \cdot MX_{BH} + F_{iSS\_precipitation} \cdot R_s \quad \text{(kgiSS)}$$

1.4. Total suspended solids (TSS)

$$MX_T = MX_V + MX_{IO} \quad \text{(kgTSS)}$$

$$X_T = \frac{MX_T}{V_p} \quad \text{(kgTSS/m}^3\text{)}$$

1.5. Nominal hydraulic retention time

$$HRT = \frac{V_p}{Q} \quad \text{(d)}$$

1.6. Wastage flowrate

$$Q_w = \frac{V_p}{R_s} \quad \text{(ML/d)}$$

1.7. Effluent flowrate

$$Q_e = Q - Q_w \quad \text{(ML/d)}$$

1.8. Nitrogen and Phosphorus required for sludge production

$$N_s = \frac{f_{N_{OHO}}(MX_{BH} + MX_{EH}) + f_{N_{UPO}} MX_I}{R_s \cdot Q} \quad \text{(mg/L)}$$

$$P_s = \frac{f_{P_{OHO}}(MX_{BH} + MX_{EH}) + f_{P_{UPO}} MX_I}{R_s \cdot Q} \quad \text{(mg/L)}$$

1.9. Effluent Ammonia concentration

$$N_{ae} = N_{ti} - N_s - N_{ouse} \quad \text{(mg/L)}$$

1.10. Effluent Orthophosphate concentration

$$P_{se} = P_{ti} - P_s - P_{ouse} - P_{precipitation} \quad \text{(mg/L)}$$

1.11. Wastage solids concentration

$$BPO_{was} = f_{cv_{BPO}}(1 - f_H) X_{BH} \quad \text{(mg/L)}$$

$$UPO_{was} = f_{cv_{UPO}}(f_H X_{BH} + X_{EH} + X_I) \quad \text{(mg/L)}$$

$$iSS_{was} = \frac{MX_{IO}}{V_p} \quad \text{(mg/L)}$$

1.12. Oxygen demand

$$FO_c = Y_H(1 - f_{cv_{OHO}}) + f_{cv_{OHO}}(1 - f_H)\cdot b_{HT} \cdot f_{X_{BH}} \qquad \text{(kgO/d)}$$

$$FO_n = 4.57 \cdot Q \cdot N_{ae} \qquad \text{(kgO/d)}$$

$$FO_t = FO_c + FO_n \qquad \text{(kgO/d)}$$

$$OUR = \frac{FO_t}{V_p} \qquad \text{(mgO/L·h)}$$

2. Nitrification

2.1. Inputs

$$SF,\ f_{xt,} DO,\ pH$$

2.2. Nitrifier kinetics

$$\mu_{Am} = 0.45 \qquad \text{(1/d)}$$

$$\mu_{AmT} = \mu_{Am}(1.123)^{T-20} \qquad \text{(1/d)}$$

$$K_O = 0.3 \qquad \text{(mgO/L)}$$

$$\mu_{AmO} = \mu_{AmT}\,\frac{DO}{K_O + DO} \qquad \text{(1/d)}$$

$$K_i = 1.13, K_{ii} = 0.3, K_{\max} = 9.5$$

$$\mu_{AmpH} = \mu_{AmO}(2.35)^{pH-7.2} K_i\,\frac{K_{\max} - pH}{K_{\max} + K_{ii} - pH} \qquad \text{(1/d)}$$

$$Y_A = 0.1 \qquad \text{(gVSS/gNH4)}$$

$$Y_{AT} = Y_A^{T-20} \qquad \text{(gVSS/gNH4)}$$

$$K_n = 1.0 \qquad \text{(mg/L)}$$

$$K_{nT} = K_n(1.123)^{T-20} \qquad \text{(mg/L)}$$

$$b_A = 0.04 \qquad \text{(1/d)}$$

$$b_{AT} = b_A(1.029)^{T-20} \qquad \text{(1/d)}$$

2.3. Maximum design unaerated sludge mass fraction

$$f_{xm} = 1 - SF\,\frac{b_{AT} + \frac{1}{R_s}}{\mu_{AmpH}} \qquad \text{(ø)}$$

2.4. Minimum sludge age for nitrification

$$R_{sm} = \frac{1}{\mu_{AmpH}(1 - f_{xt}) - b_{AT}} \qquad \text{(d)}$$

2.5. Effluent Ammonia concentration

$$N_{ae} = \frac{K_{nT}(b_{AT} + \frac{1}{R_s})}{\mu_{AmpH}(1 - f_{xt}) - b_{AT} - \frac{1}{R_s}} \qquad \text{(mg/L)}$$

2.6. Nitrification capacity

$$N_c = N_{ti} - N_s - (N_{ae} + N_{ouse}) \qquad \text{(mg/L)}$$

2.7. ANO biomass

$$f_{X_{BA}} = \frac{Y_{AT} R_s}{1 + b_{AT} \cdot R_s} \qquad \text{(gVSS·d/gNH4)}$$

$$MX_{BA} = Q \cdot N_c \cdot f_{X_{BA}} \qquad \text{(kgVSS)}$$

$$X_{BA} = \frac{MX_{BA}}{V_p} \qquad \text{(kgVSS/m}^3\text{)}$$

3. Denitrification

3.1. Inputs

$$IR, DO_{RAS,} alk_i$$

3.2. Denitrification kinetics

$$K_1^{20} = 0.72, K_2^{20} = 0.10, K_3^{20} = 0.10, K_4^{20} = 0.00 \qquad \text{(mgN/mgVSS·d)}$$

$$K_{1T} = K_1^{20}(1.200)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

$$K_{2T} = K_2^{20}(1.080)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

$$K_{3T} = K_3^{20}(1.029)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

$$K_{4T} = K_4^{20}(1.029)^{T-20} \qquad \text{(mgN/mgVSS·d)}$$

3.3. Denitrification potential

$$D_{p1RBSO} = \frac{S_{bsi}(1 - f_{cv}Y_H)}{2.86} \qquad \text{(mgN/L)}$$

$$D_{p1BPO} = K_{2T}\, f_{xt} S_{bi}\, f_{X_{BH}} \qquad \text{(mgN/L)}$$

$$D_{p1} = D_{p1RBSO} + D_{p1BPO} \qquad \text{(mgN/L)}$$

3.4. Optimum internal recirculation

$$a_{opt} = \frac{-B + \sqrt{B^2 + 4AC}}{2A} \qquad (ø)$$

where:

$$A = \frac{DO}{2.86}$$

$$B = N_c - D_{p1} + \frac{(1 + RAS) \cdot DO + RAS \cdot DO_{RAS}}{2.86}$$

$$C = (1 + RAS) \cdot (D_{p1} - \frac{RAS \cdot DO_{RAS}}{2.86}) - RAS \cdot N_c$$

3.5. Minimum effluent NOx concentration

$$N_{ne\_opt} = \frac{Nc}{a_{opt} + RAS + 1} \qquad \text{(mgN/L)}$$

3.6. Effluent nitrate

$if\,(a < a_{opt})$

$$N_{ne} = \frac{N_c}{a + RAS + 1} \qquad \text{(mgN/L)}$$

$if\,(a > a_{opt})$

$$N_{ne} = N_c - D_{p1} + \frac{a * DO + RAS * DO_{RAS}}{2.86} \qquad \text{(mgN/L)}$$

3.7. Nitrogen gas

$$FN_2 = Q(N_c - N_{ne}) \qquad \text{(kgN/d)}$$

3.8. Oxygen recovered by denitrification

$$FO_d = 2.86 \cdot Q \cdot (N_c - N_{ne}) \qquad \text{(kgO/d)}$$

$$FO_t = FO_c + FO_n - FO_d \qquad \text{(kgO/d)}$$

3.9. Effluent alkalinity

$$alk_e = alk_i + 3.57 \cdot (N_{obi} - (N_s - N_{oupi})) - 7.14 \cdot N_c + 2.86 \cdot (N_c - N_{ne}) \qquad \text{(mg/L)}$$