

Lista de Exercícios 01 - Conversão de uma base qualquer para decimal (respostas)

1) Converter para decimal (ternário -> decimal):

$$\begin{aligned} 2102_3 &= 2 \times 3^3 + 1 \times 3^2 + 0 \times 3^1 + 2 \times 3^0 \\ &= 2 \times 27 + 1 \times 9 + 0 \times 3 + 2 \times 1 \\ &= 54 + 9 + 0 + 2 \\ &= 65 \end{aligned}$$

$$\begin{aligned} 212121_3 &= 2 \times 3^5 + 1 \times 3^4 + 2 \times 3^3 + 1 \times 3^2 + 2 \times 3^1 + 1 \times 3^0 \\ &= 2 \times 243 + 1 \times 81 + 2 \times 27 + 1 \times 9 + 2 \times 3 + 1 \times 1 \\ &= 486 + 81 + 54 + 9 + 6 + 1 \\ &= 637 \end{aligned}$$

$$\begin{aligned} 222_3 &= 2 \times 3^2 + 2 \times 3^1 + 2 \times 3^0 \\ &= 2 \times 9 + 2 \times 3 + 2 \times 1 \\ &= 18 + 6 + 2 \\ &= 26 \end{aligned}$$

$$1000_3 = 1 \times 3^3 = 1 \times 27 = 27$$

$$2222_3 = 2 \times 27 + 2 \times 9 + 2 \times 3 + 2 \times 1 = 54 + 18 + 6 + 2 = 80$$

$$10000_3 = 1 \times 3^4 = 1 \times 81 = 81$$

$$100000_3 = 1 \times 3^5 = 1 \times 243 = 243$$

Resumo (todas questões base 3):

Base ^Exp	3 ⁵	3 ⁴	3 ³	3 ²	3 ¹	3 ⁰	Cálculo	Resp.
Potência	243	81	27	9	3	1		
Exerc. 1			2	1	0	2	2x27+1x9+0x3+2x1	65
Exerc. 2	2	1	2	1	2	1	2x243+1x81+2x27+1x9+2x3+1x1	637
Exerc. 3				2	2	2	2x9+2x3+2x1	26
Exerc. 4			1	0	0	0	1x27	27
Exerc. 5			2	2	2	2	2x27+2x9+2x3+2x1	80
Exerc. 6		1	0	0	0	0	1x81	81
Exerc. 7	1	0	0	0	0	0	1x243	243

Converter para decimal (octal -> decimal):

$$\begin{aligned}
 12035_8 &= 1 \times 8^4 + 2 \times 8^3 + 0 \times 8^2 + 3 \times 8^1 + 5 \times 8^0 \\
 &= 1 \times 4096 + 2 \times 512 + 0 \times 64 + 3 \times 8 + 5 \times 1 \\
 &= 4096 + 1024 + 0 + 24 + 5 \\
 &= 5149
 \end{aligned}$$

$$\begin{aligned}
 2746_8 &= 2 \times 8^3 + 7 \times 8^2 + 4 \times 8^1 + 6 \times 8^0 \\
 &= 2 \times 512 + 7 \times 64 + 4 \times 8 + 6 \times 1 \\
 &= 1024 + 448 + 32 + 6 \\
 &= 1510
 \end{aligned}$$

$$\begin{aligned}
 37_8 &= 3 \times 8^1 + 7 \times 8^0 \\
 &= 3 \times 8 + 7 \times 1 \\
 &= 24 + 7 \\
 &= 31
 \end{aligned}$$

$$\begin{aligned}
 116_8 &= 1 \times 64 + 1 \times 8 + 6 \times 1 \\
 &= 64 + 8 + 6 = 78
 \end{aligned}$$

$$\begin{aligned}
 2537_8 &= 2 \times 512 + 5 \times 64 + 3 \times 8 + 7 \times 1 \\
 &= 1024 + 320 + 24 + 7 = 1375
 \end{aligned}$$

$$777_8 = 7 \times 64 + 7 \times 8 + 7 \times 1 = 448 + 56 + 7 = 511$$

$$1000_8 = 1 \times 8^3 = 1 \times 512 = 512$$

$$10000_8 = 1 \times 8^4 = 1 \times 4096 = 4096$$

Resumo (todas questões base 8):

Base^Exp	8 ⁵	8 ⁴	8 ³	8 ²	8 ¹	8 ⁰	Cálculo	Resp.
Potência	32768	4096	512	64	8	1		
Exerc. 1		1	2	0	3	5	1x4096+2x512+0x64+3x8+5x1	5149
Exerc. 2			2	7	4	6	2x512+7x64+4x8+6x1	1510
Exerc. 3					3	7	3x8+7x1	31
Exerc. 4				1	1	6	1x64+1x8+6x1	78
Exerc. 5			2	5	3	7	2x512+5x64+3x8+7x1	1375
Exerc. 6				7	7	7	7x64 + 7x8 + 7x1	511
Exerc. 7			1	0	0	0	1x512	512
Exerc. 8		1	0	0	0	0	1x4096	4096

Converter para decimal (binário -> decimal):

$$\begin{aligned}
 110101_2 &= 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\
 &= 1 \times 32 + 1 \times 16 + 0 \times 8 + 1 \times 4 + 0 \times 2 + 1 \times 1 \\
 &= 32 + 16 + 0 + 4 + 0 + 1 \\
 &= 53
 \end{aligned}$$

$$11111_2 = 16 + 8 + 4 + 2 + 1 = 31$$

$$101011_2 = 32 + 8 + 2 + 1 = 43$$

$$111111_2 = 32 + 16 + 8 + 4 + 2 + 1 = 63$$

$$1000000_2 = 64$$

$$1000001_2 = 64 + 1 = 65$$

$$1000011_2 = 64 + 2 + 1 = 67$$

Resumo (todas questões base 2):

Base ^{Exp}	2 ⁶	2 ⁵	2 ⁴	2 ³	2 ²	2 ¹	2 ⁰	Cálculo	Resp.
Potência	64	32	16	8	4	2	1		
Exerc. 1		1	1	0	1	0	1	32+16+4+1	53
Exerc. 2			1	1	1	1	1	16+8+4+2+1	31
Exerc. 3		1	0	1	0	1	1	32+8+2+1	43
Exerc. 4		1	1	1	1	1	1	32+16+8+4+2+1	63
Exerc. 5	1	0	0	0	0	0	0	64	64
Exerc. 6	1	0	0	0	0	0	1	64+1	65
Exerc. 7	1	0	0	0	0	1	1	64+2+1	67

Converter para decimal (hexadecimal -> decimal):

$$\begin{aligned}A8D_{16} &= A \times 16^2 + 8 \times 16^1 + D \times 16^0 \\&= 10 \times 256 + 8 \times 16 + 13 \times 1 \\&= 2560 + 128 + 13 \\&= 2701\end{aligned}$$

$$\begin{aligned}AB5C_{16} &= A \times 16^3 + B \times 16^2 + 5 \times 16^1 + C \times 16^0 \\&= 10 \times 4096 + 11 \times 256 + 5 \times 16 + 12 \times 1 \\&= 40960 + 2816 + 80 + 12 \\&= 43868\end{aligned}$$

$$2E_{16} = 2 \times 16 + E \times 1 = 32 + 14 \times 1 = 32 + 14 = 46$$

$$2F_{16} = 2 \times 16 + F \times 1 = 32 + 15 \times 1 = 32 + 15 = 47$$

$$30_{16} = 3 \times 16 + 0 \times 1 = 48 + 0 = 48$$

$$31_{16} = 3 \times 16 + 1 \times 1 = 48 + 1 = 49$$

$$F2D_{16} = 15 \times 256 + 2 \times 16 + 13 = 3840 + 32 + 13 = 3885$$

$$\begin{aligned}B3AC_{16} &= B \times 16^3 + 3 \times 16^2 + A \times 16^1 + C \times 16^0 \\&= 11 \times 4096 + 3 \times 256 + 10 \times 16 + 12 \times 1 \\&= 45056 + 768 + 160 + 12 \\&= 45996\end{aligned}$$

$$FF_{16} = 15 \times 16 + 15 = 240 + 15 = 255$$

$$100_{16} = 1 \times 16^2 = 1 \times 256 = 256$$

$$FFF_{16} = 15 \times 256 + 15 \times 16 + 15 = 3840 + 240 + 15 = 4095$$

$$1000_{16} = 1 \times 16^3 = 1 \times 4096 = 4096$$

Resumo (todas questões base 16):

Base^Exp	16^5	16^4	16^3	16^2	16^1	16^0	Cálculo	Resp.
Potência			4096	256	16	1		
Exerc. 1				A	8	D	$10 \times 256 + 8 \times 16 + 13 \times 1$	2701
Exerc. 2			A	B	5	C	$10 \times 4096 + 11 \times 256 + 5 \times 16 + 12 \times 1$	43868
Exerc. 3					2	E	$2 \times 16 + 14 \times 1$	46
Exerc. 4					2	F	$2 \times 16 + 15 \times 1$	47
Exerc. 5					3	0	3×16	48
Exerc. 6					3	1	$3 \times 16 + 1 \times 1$	49
Exerc. 7				F	2	D	$15 \times 256 + 2 \times 16 + 13 \times 1$	3885
Exerc. 8			B	3	A	C	$11 \times 4096 + 3 \times 256 + 10 \times 16 + 12 \times 1$	45996
Exerc. 9					F	F	$15 \times 16 + 15 \times 1$	255
Exerc. 10				1	0	0	1×256	256
Exerc. 11				F	F	F	$15 \times 256 + 15 \times 16 + 15 \times 1$	4095
Exerc. 12			1	0	0	0	1×4096	4096