



# Overview

- Introduction to Kinematics
- Joint Motor Control ([overview](#) + [tutorial](#))
- Cartesian Control ([theory](#) + [API](#) + [tutorial](#))
- Gaze Control ([theory](#) + [API](#) + [tutorial](#))
- Assignment



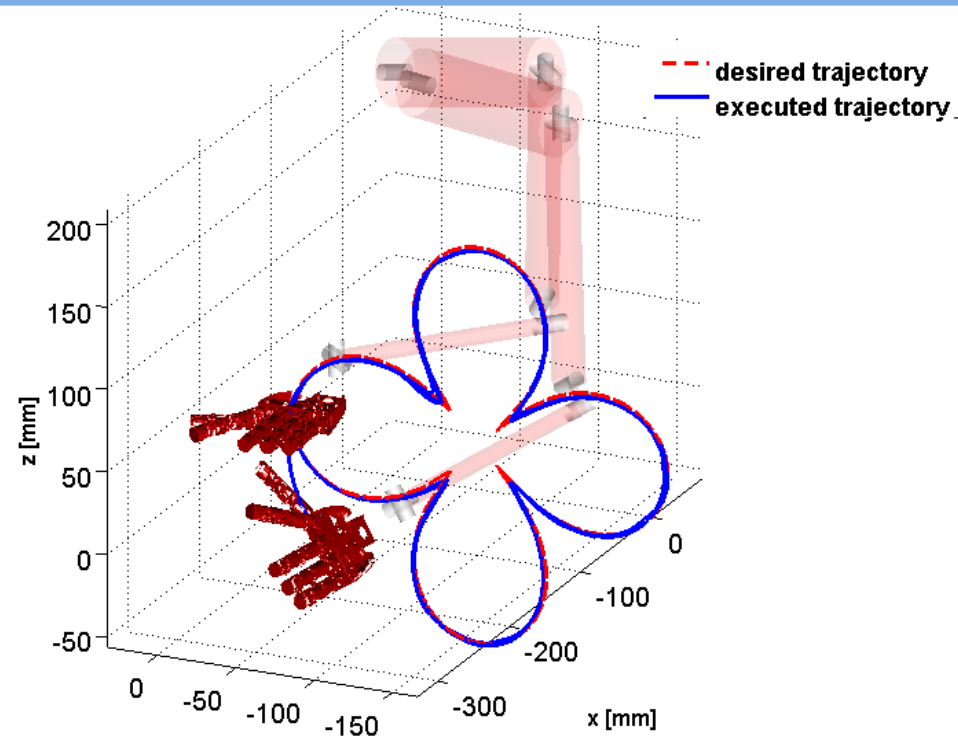
## Basic Kinematics (1/2)

Study of properties of motion (position, velocity, acceleration) without considering body inertias and forces

### The Problem

$$\begin{cases} \mathbf{x} = \mathbf{f}(\mathbf{q}) \\ \mathbf{q} \in \mathbb{R}^n \\ \mathbf{x} \in \mathbb{R}^6 \end{cases}$$

$$\mathbf{q} \stackrel{?}{=} \mathbf{f}^{-1}(\mathbf{x})$$





## Basic Kinematics (2/2)

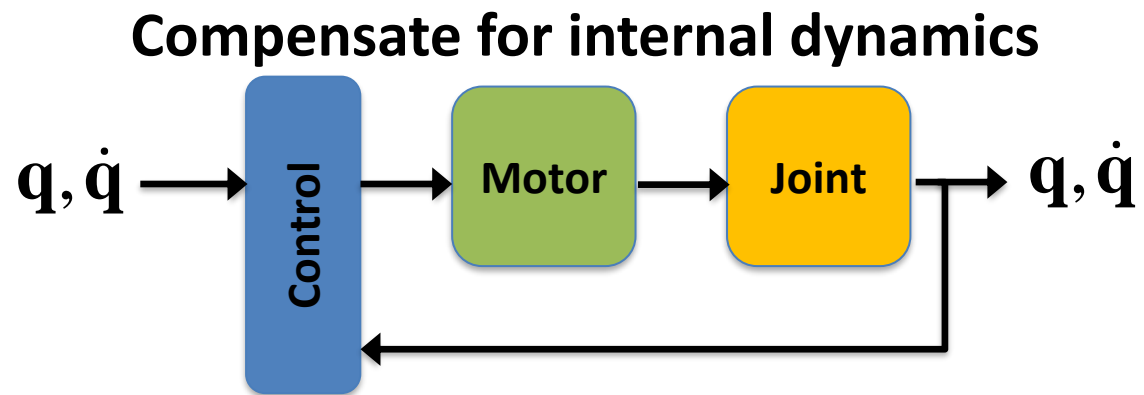
**Dynamics** – forces, torques, inertias, energy, contact with environment

$$\mathbf{B}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{C}(\mathbf{q}, \dot{\mathbf{q}})\dot{\mathbf{q}} + \mathbf{F}_v\dot{\mathbf{q}} + \mathbf{F}_s \operatorname{sgn}(\dot{\mathbf{q}}) + \mathbf{g}(\mathbf{q}) = \boldsymbol{\tau} - \mathbf{J}^T(\mathbf{q})\mathbf{h}_e$$

**VS.**

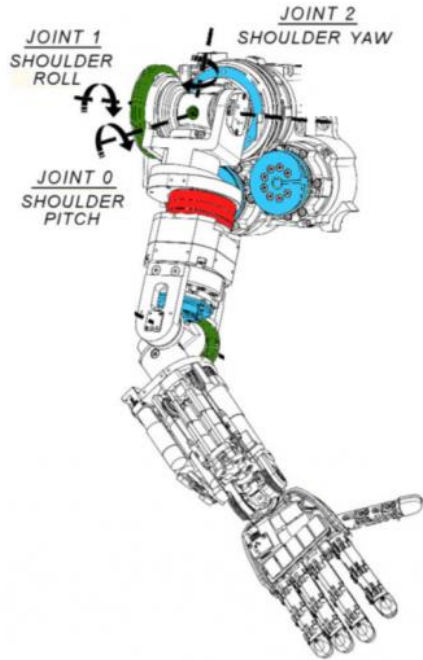
**Kinematics** – pure motion imposed to the manipulator's joints

$$\begin{cases} \dot{\mathbf{x}} = \mathbf{J}\dot{\mathbf{q}} \\ \mathbf{J} = \partial \mathbf{f} / \partial \mathbf{q} \end{cases}$$





# Joint Motor Control (1/4)

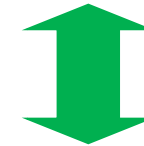


DC MOTORS



## USER CODE @ 100 Hz

```
ipos->positionMove(poss.data());  
while (norm(poss-encs)>1.0) {  
    Time::delay(0.1);  
    ienc->getEncoders(encs.data());  
    cout<<encs.toString()<<endl;  
}
```

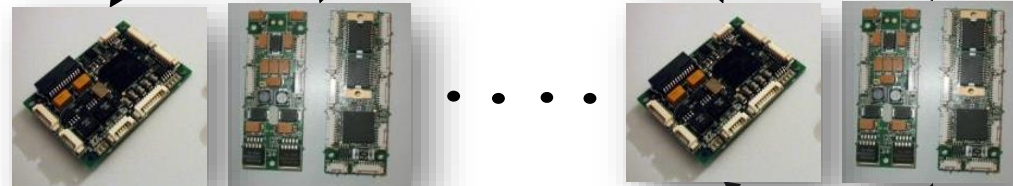


Gbit Ethernet

PC104

FIRMWARE @ 1 KHz

CONTROLLERS

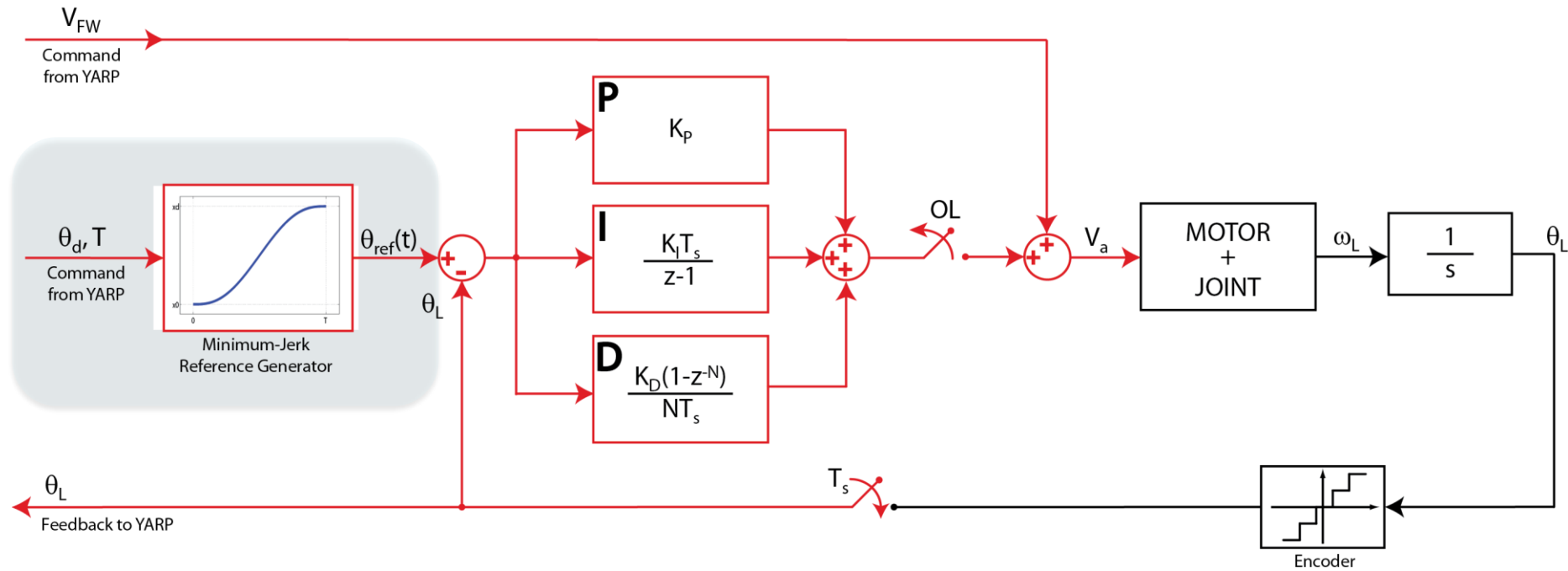


Sensors & Actuators



## Joint Motor Control (2/4)

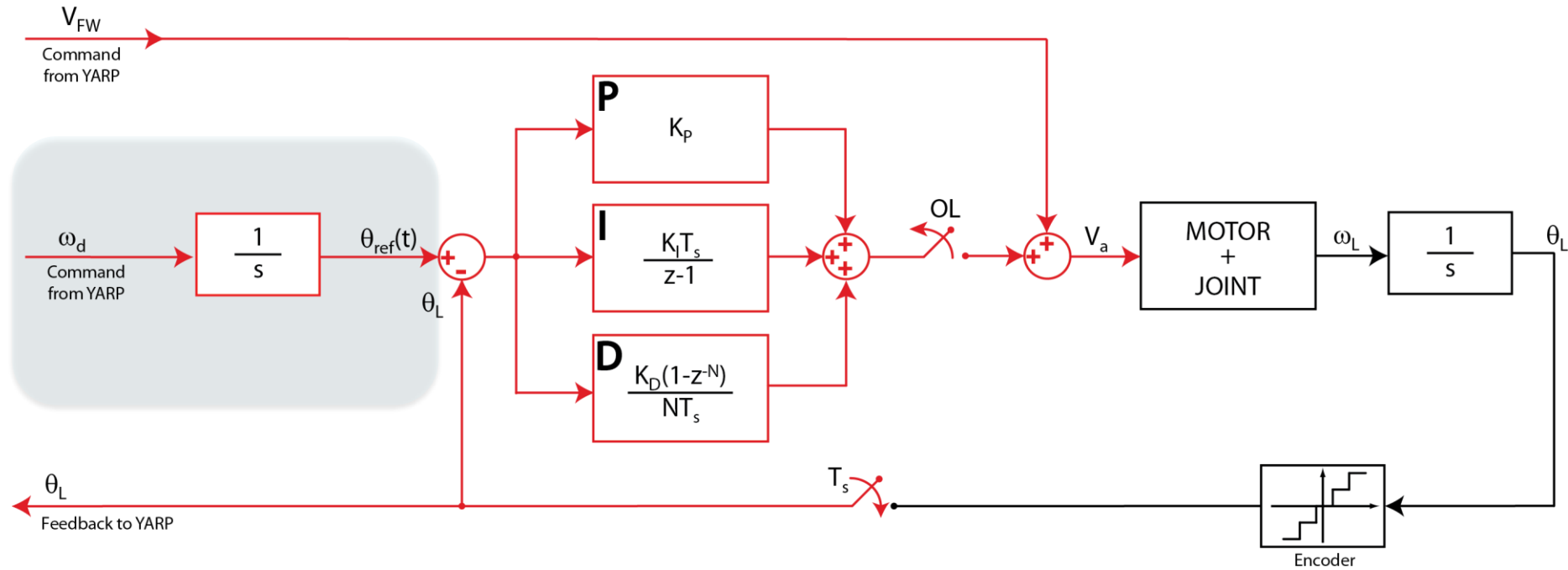
### Position Control





## Joint Motor Control (3/4)

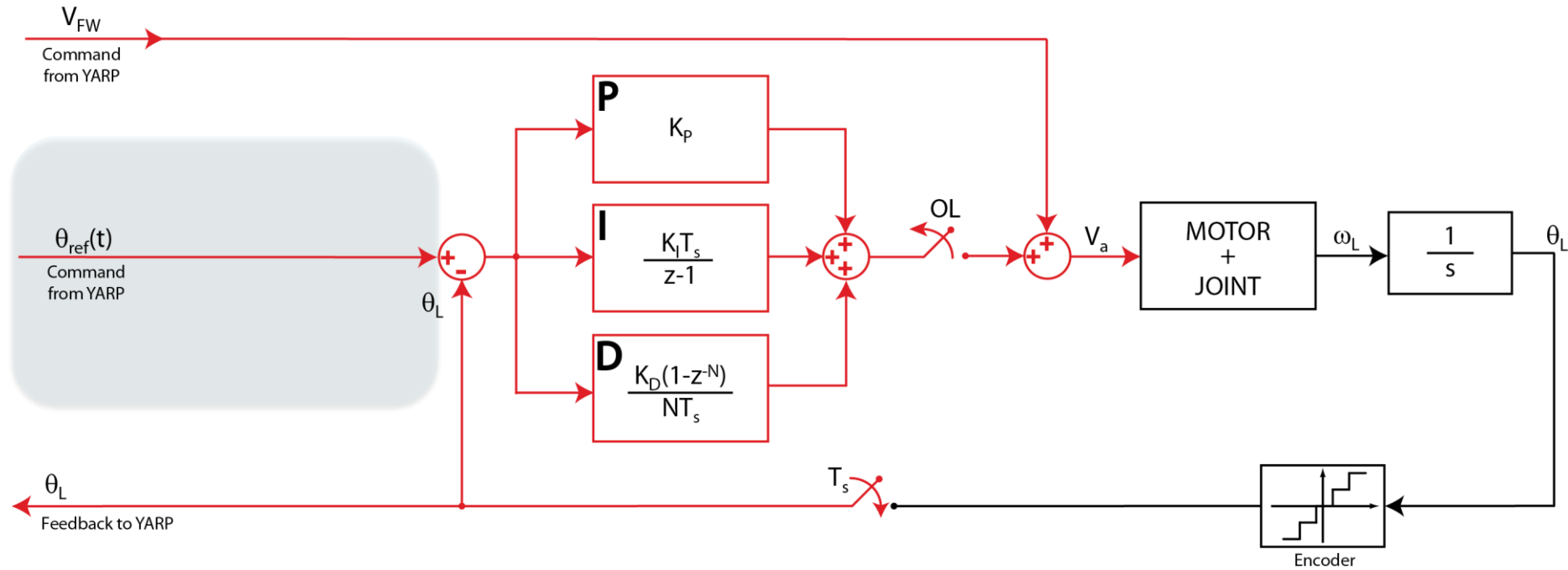
### Velocity Control





# Joint Motor Control (4/4)

## Position-Direct Control





# Tutorial Time !





# The Cartesian Controller (1/5)

## Operational (Cartesian) Space Control

You know  $\mathbf{x}$  (3D/6D points), you cannot control directly the motors, you have to solve the **Inverse Kinematics (IK) problem** beforehand.



very “robotic” movements:

- snap onset
- exponential decay

Jacobian Transpose

$$\dot{\mathbf{q}} = \mathbf{J}^T \mathbf{K} \mathbf{e}, \quad \mathbf{e} = \mathbf{x}_d - \mathbf{x}_e$$

Jacobian Pseudoinverse

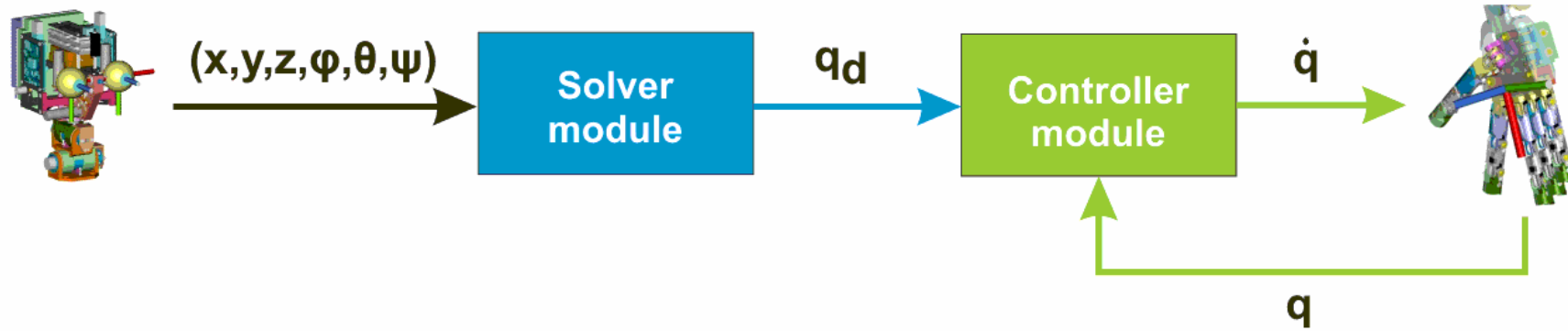
$$\dot{\mathbf{q}} = \mathbf{J}^\dagger \mathbf{K} \mathbf{e} + (\mathbf{I} - \mathbf{J}^\dagger \mathbf{J}) \dot{\mathbf{q}}_0, \quad \mathbf{J}^\dagger = \mathbf{J}^T (\mathbf{J} \mathbf{J}^T)^{-1}$$

Damped Least-Squares

$$\dot{\mathbf{q}} = \mathbf{J}^* \mathbf{K} \mathbf{e}, \quad \mathbf{J}^* = \mathbf{J}^T (\mathbf{J} \mathbf{J}^T + \lambda^2 \mathbf{I})^{-1}$$



## The Cartesian Controller (2/5)



nonlinear constrained optimization:

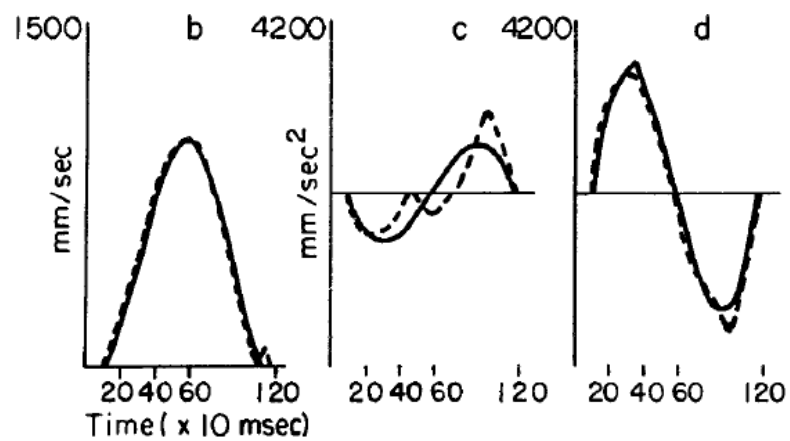
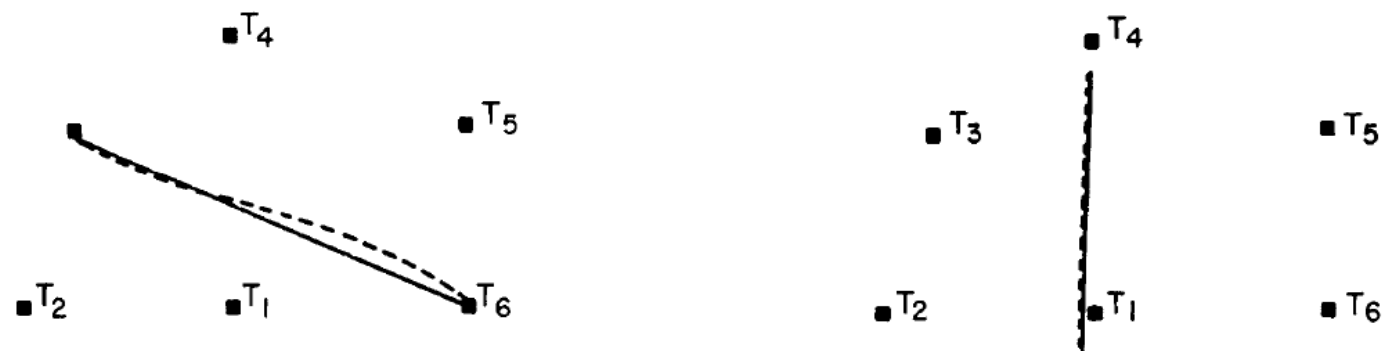
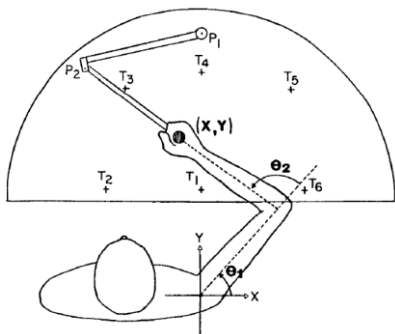
- fast
- scalable

human-like movements (min-jerk):

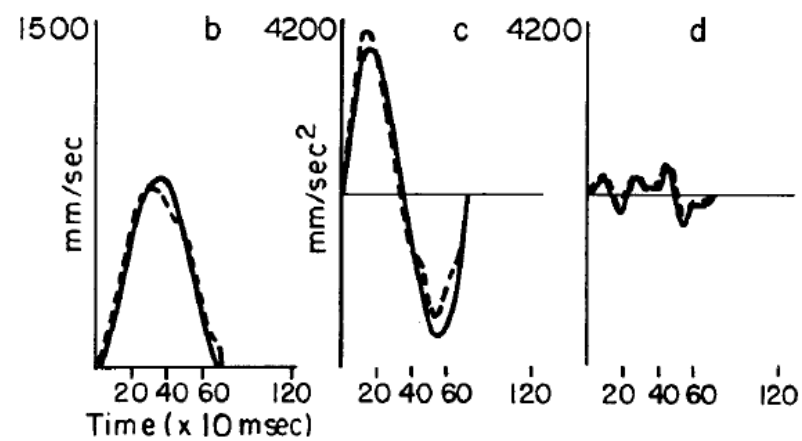
- bell-shape velocity profile
- quasi-straight path



## The Cartesian Controller (3/5)



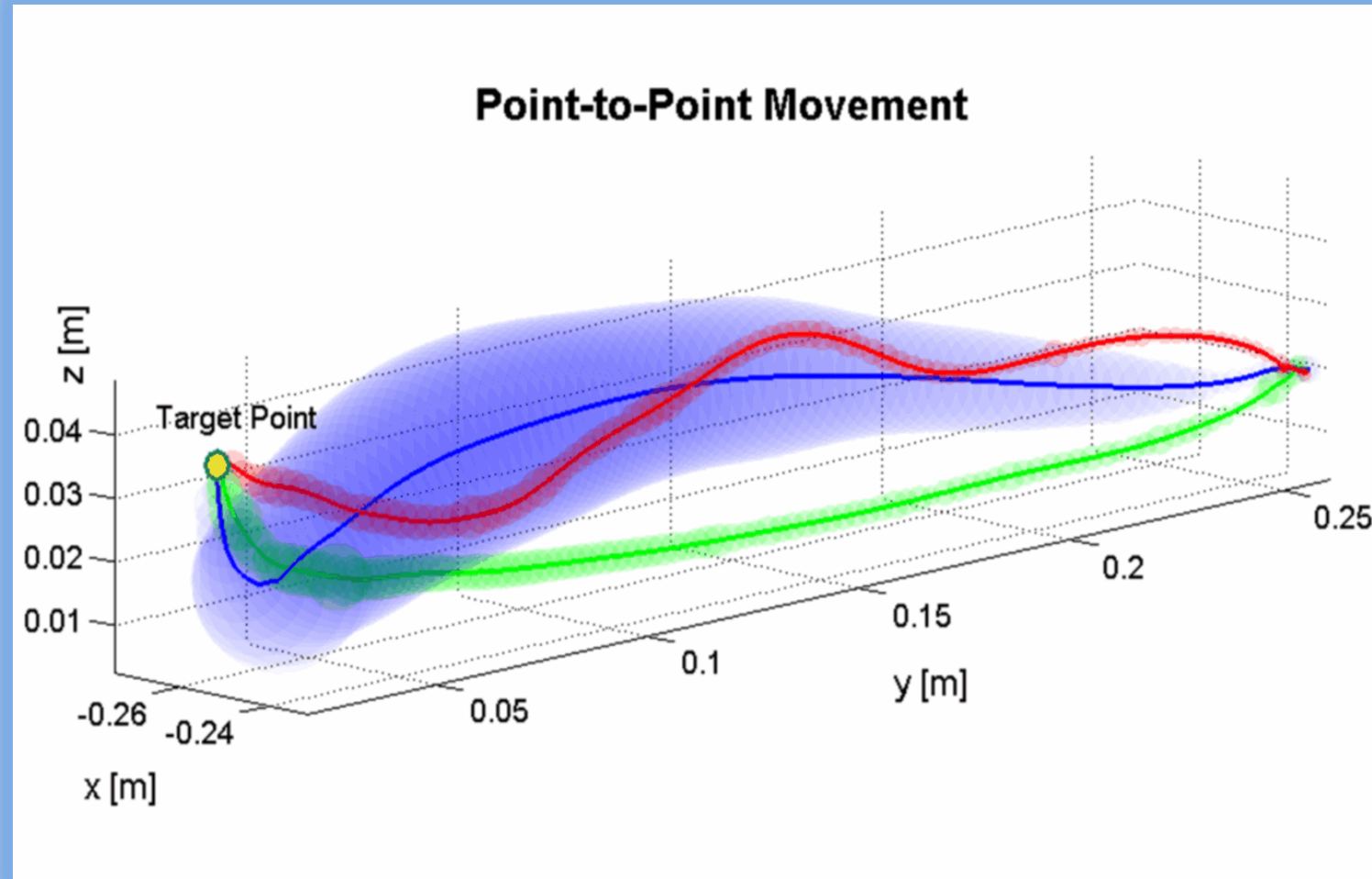
A



B



## The Cartesian Controller (4/5)



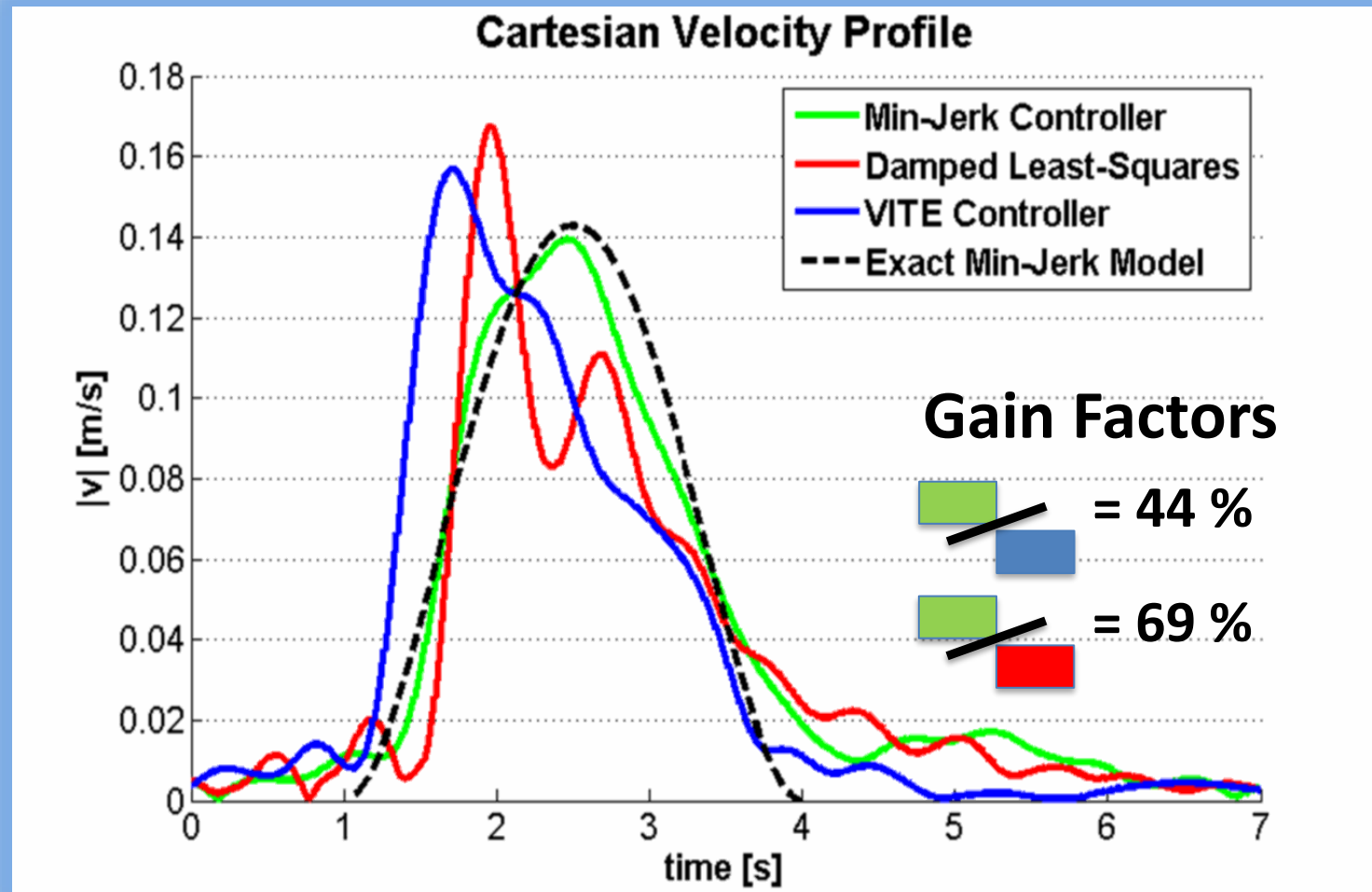
Min-Jerk

DLS

VITE



## The Cartesian Controller (5/5)



Min-Jerk

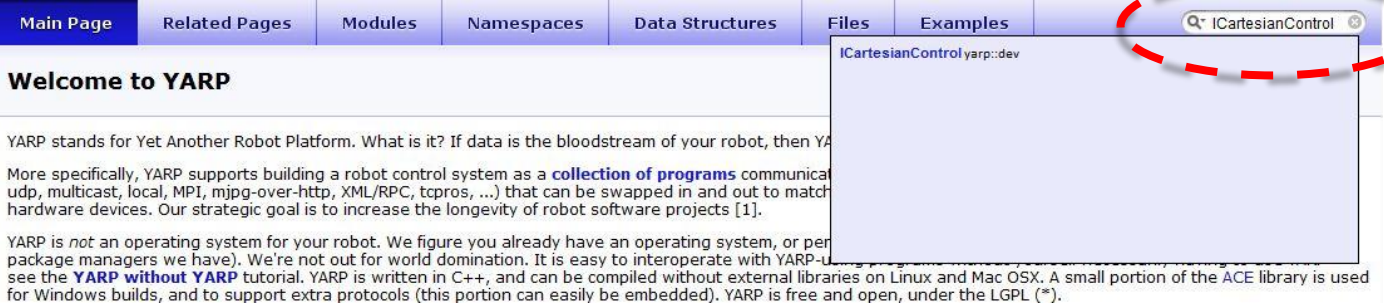
DLS

VITE



# Interfaces Documentation

In the search field: type **ICartesianControl/IGazeControl**



The screenshot shows the YARP documentation website. The top navigation bar includes links for Main Page, Related Pages, Modules, Namespaces, Data Structures, Files, and Examples. A search bar in the top right corner contains the text "ICartesianControl". Below the navigation bar, the main content area displays the "Welcome to YARP" message. To the right of the main content, a search results dropdown menu is visible, showing "ICartesianControl yarp::dev".

Public Member Functions

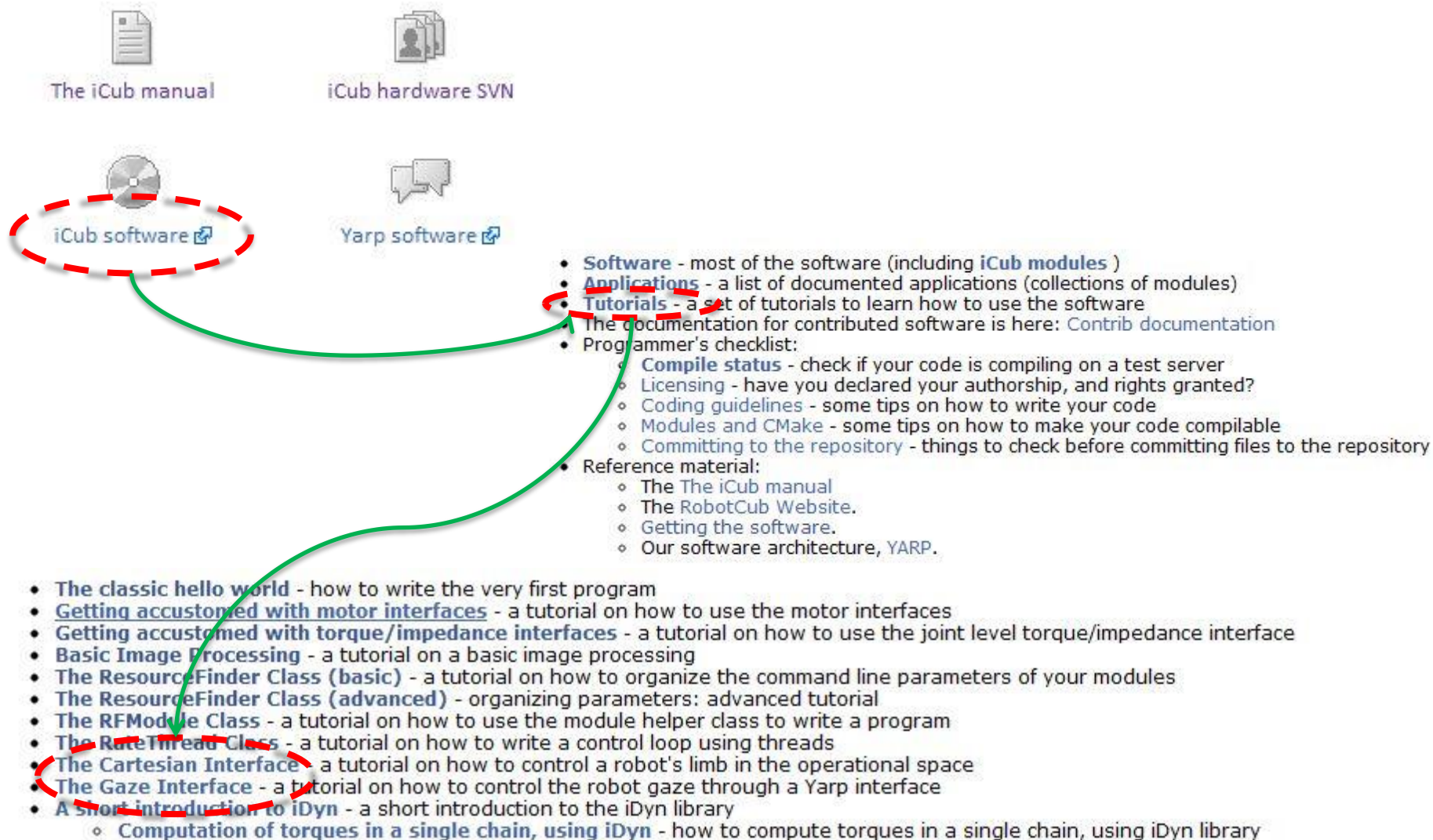
virtual	<code>~ICartesianControl ()</code>	Destructor.
virtual bool	<code>setTrackingMode (const bool f)=0</code>	Set the controller in tracking or non-tracking mode.
virtual bool	<code>getTrackingMode (bool *f)=0</code>	Get the current controller mode.
virtual bool	<code>getPose (yarp::sig::Vector &amp;x, yarp::sig::Vector &amp;o)=0</code>	Get the current pose of the end-effector.
virtual bool	<code>getPose (const int axis, yarp::sig::Vector &amp;x, yarp::sig::Vector &amp;o)=0</code>	Get the current pose of the specified link belonging to the kinematic chain.
virtual bool	<code>goToPose (const yarp::sig::Vector &amp;xd, const yarp::sig::Vector &amp;od, const double t=0.0)=0</code>	Move the end-effector to a specified pose (position and orientation) in cartesian space.
virtual bool	<code>goToPosition (const yarp::sig::Vector &amp;xd, const double t=0.0)=0</code>	Move the end-effector to a specified position in cartesian space, ignore the orientation.
virtual bool	<code>goToPoseSync (const yarp::sig::Vector &amp;xd, const yarp::sig::Vector &amp;od, const double t=0.0)=0</code>	Move the end-effector to a specified pose (position and orientation) in cartesian space.
virtual bool	<code>goToPositionSync (const yarp::sig::Vector &amp;xd, const double t=0.0)=0</code>	Move the end-effector to a specified position in cartesian space, ignore the orientation.
virtual bool	<code>getDesired (yarp::sig::Vector &amp;xdhat, yarp::sig::Vector &amp;odhat, yarp::sig::Vector &amp;qdhat)=0</code>	Get the actual desired pose and joints configuration as result of kinematic inversion.
virtual bool	<code>askForPose (const yarp::sig::Vector &amp;xd, const yarp::sig::Vector &amp;od, yarp::sig::Vector &amp;xdhat, yarp::sig::Vector &amp;odhat, yarp::sig::Vector &amp;qdhat)=0</code>	Ask for inverting a given pose without actually moving there.
virtual bool	<code>askForPose (const yarp::sig::Vector &amp;q0, const yarp::sig::Vector &amp;xd, const yarp::sig::Vector &amp;od, yarp::sig::Vector &amp;xdhat, yarp::sig::Vector &amp;odhat, yarp::sig::Vector &amp;qdhat)=0</code>	Ask for inverting a given pose without actually moving there.
virtual bool	<code>askForPosition (const yarp::sig::Vector &amp;xd, yarp::sig::Vector &amp;xdhat, yarp::sig::Vector &amp;odhat, yarp::sig::Vector &amp;qdhat)=0</code>	Ask for inverting a given position without actually moving there.

## Doxygen Documentation





# Interfaces Tutorials





## Cartesian Interface (1/8)

### OPENING THE CARTESIAN INTERFACE

```
#include <yarp/dev/all.h>
Property option;

option.put("device", "cartesiancontrollerclient");
option.put("remote", "/icub/cartesianController/right_arm");
option.put("local", "/client/right_arm");

PolyDriver clientCartCtrl(option);

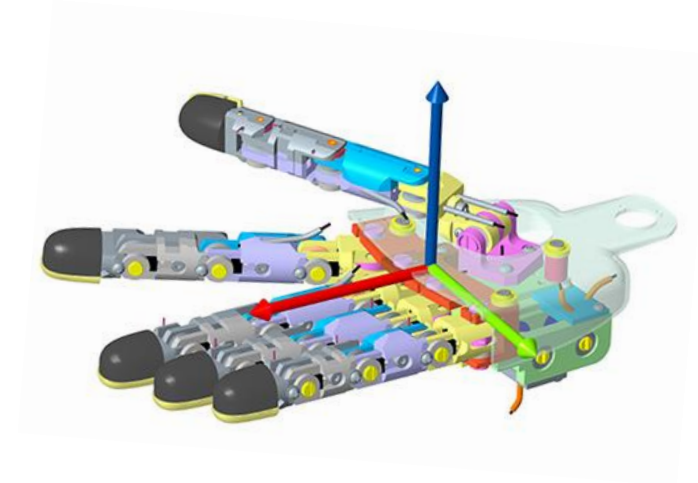
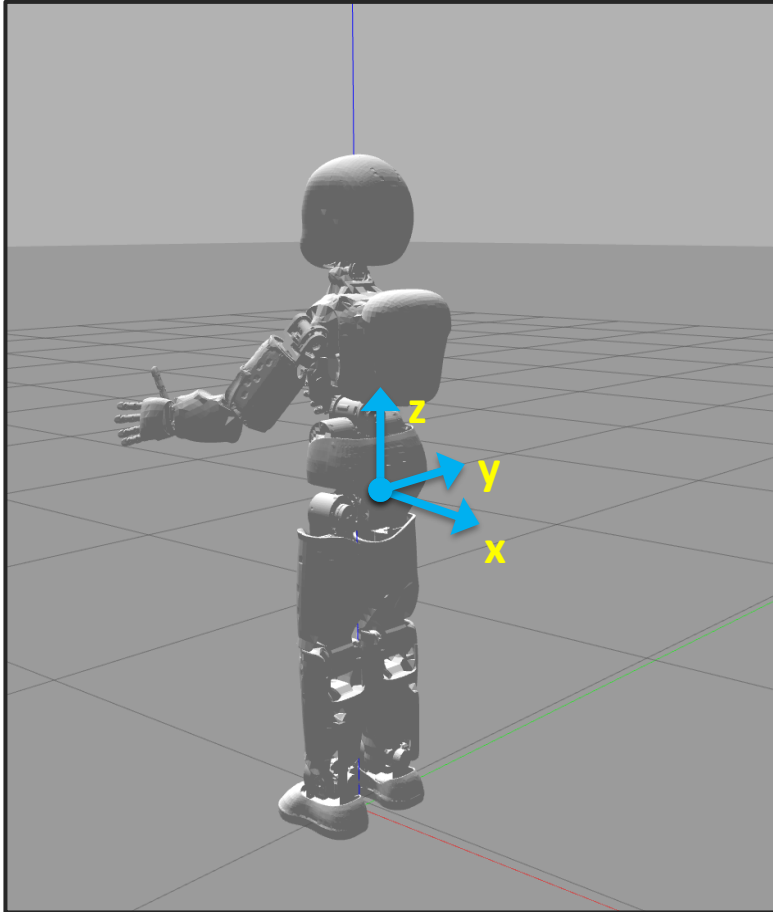
ICartesianControl *icart=NULL;
if (clientCartCtrl.isValid()) {
    clientCartCtrl.view(icart);
}
```





## Cartesian Interface (2/8)

### Coordinate Systems



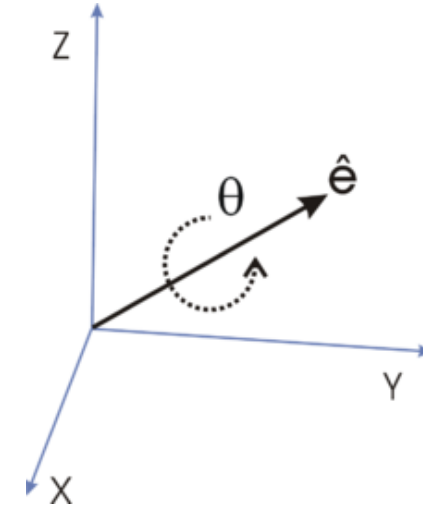


## Cartesian Interface (3/8)

Orientation: Axis-Angle

$$r = \begin{bmatrix} e_x & e_y & e_z & \theta \end{bmatrix}$$

$\underbrace{\hspace{1.5cm}}_{\|e\| = 1} \quad \underbrace{\hspace{1.5cm}}_{\text{rad}}$



### TARGET ORIENTATION through DIRECTION COSINE MATRIX

```
Matrix R(3,3);  
// pose x-axis  y-axis  z-axis  
R(0,0)= 0.0; R(0,1)= 1.0; R(0,2)= 0.0; // x-coordinate  
R(1,0)= 0.0; R(1,1)= 0.0; R(1,2)=-1.0; // y-coordinate  
R(2,0)=-1.0; R(2,1)= 0.0; R(2,2)= 0.0; // z-coordinate  
  
Vector o=ctrl::dcm2axis(R);
```



## Cartesian Interface (4/8)

### RETRIEVE CURRENT POSE

```
Vector x,o;  
icart->getPose(x,o);
```

### REACH FOR A TARGET POSE (SEND-AND-FORGET)

```
icart->goToPose(xd,od);  
icart->goToPosition(xd);
```

### REACH FOR A TARGET POSE (WAIT-FOR-REPLY)

```
icart->goToPoseSync(xd,od);  
icart->goToPositionSync(xd);
```

### REACH AND WAIT

```
icart->goToPoseSync(xd,od);  
icart->waitMotionDone();
```



## Cartesian Interface (5/8)

### ASK FOR A POSE (without moving)

```
Vector xdhat,odhat,qdhat;  
icart->askForPose(xd,xdhat,odhat,qdhat);
```

### MOVE FASTER/SLOWER

```
icart->setTrajTime(1.5); // point-to-point trajectory time
```

### REACH WITH GIVEN PRECISION

```
icart->setInTargetTol(0.001);
```

### KEEP THE POSE ONCE DONE

```
icart->setTrackingMode(true);
```



## Cartesian Interface (6/8)

### ENABLE/DISABLE DOF

```
Vector curDof;  
icart->getDOF(curDof); // [0 0 0 1 1 1 1 1 1 1]  
  
Vector newDof(3);  
newDof[0]=1; // torso pitch: 1 => enable  
newDof[1]=2; // torso roll: 2 => skip  
newDof[2]=1; // torso yaw: 1 => enable  
icart->setDOF(newDof, curDof);
```

### GIVE PRIORITY TO REACHING IN POSITION/ORIENTATION

```
icart->setPosePriority("position"); // default  
icart->setPosePriority("orientation");
```



## Cartesian Interface (7/8)

### CONTEXT SWITCH

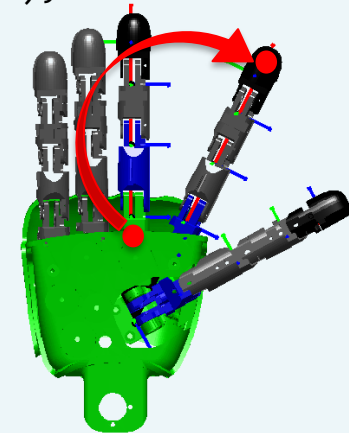
```
icart->setDOF(newDof1,curDof1);    // prepare the context  
icart->setTrackingMode(true);  
  
int context_0;  
icart->storeContext(&context_0);  // latch the context  
  
icart->setDOF(newDof2,curDof2);    // perform some actions  
icart->goToPose(x,o);  
  
icart->restoreContext(context_0);  // retrieve context_0  
icart->goToPose(x,o);              // perform with context_0
```



## Cartesian Interface (8/8)

### DEFINING A DIFFERENT EFFECTOR

```
iCubFinger finger("right_index");  
Vector encs; iencs->getEncoders(encs.data());  
Vector joints; finger.getChainJoints(encs,joints);  
Matrix tipFrame=finger.getH((M_PI/180.0)*joints);  
  
Vector tip_x=tipFrame.getCol(3);  
Vector tip_o=ctrl::dcm2axis(tipFrame);  
  
icart->attachTipFrame(tip_x,tip_o);  
  
icart->getPose(x,o);  
icart->goToPose(xd,od);  
  
icart->removeTipFrame();
```



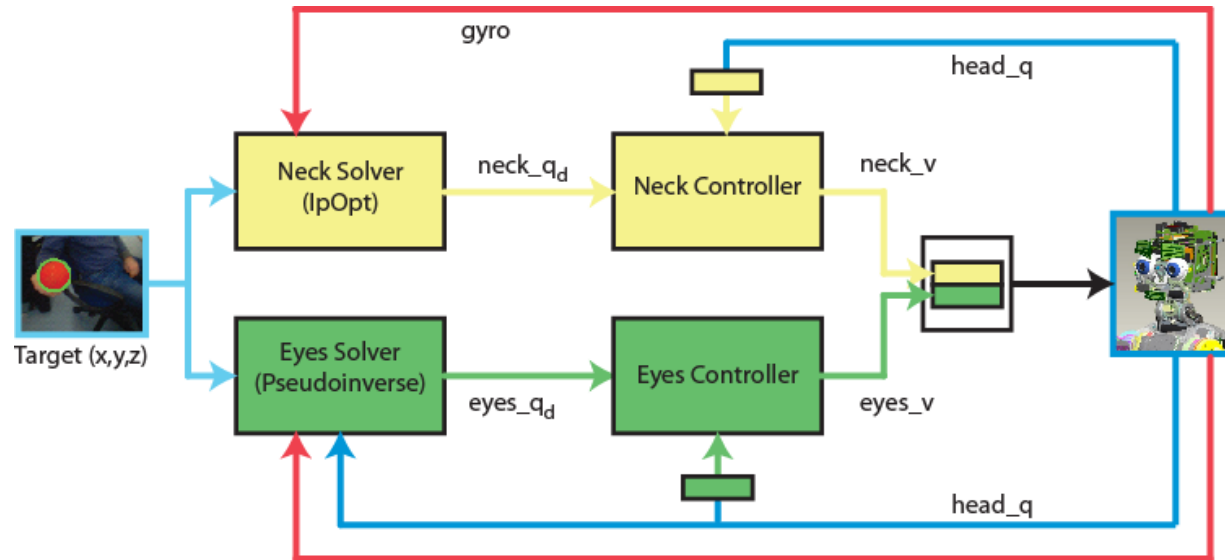
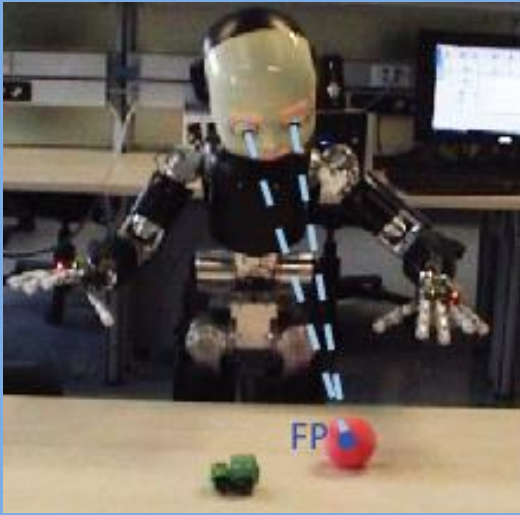


# Tutorial Time !





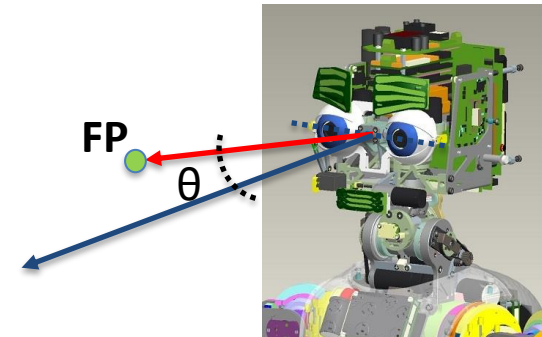
# The Gaze Controller (1/6)

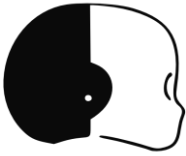


Yet another Cartesian Controller: reuse ideas ...

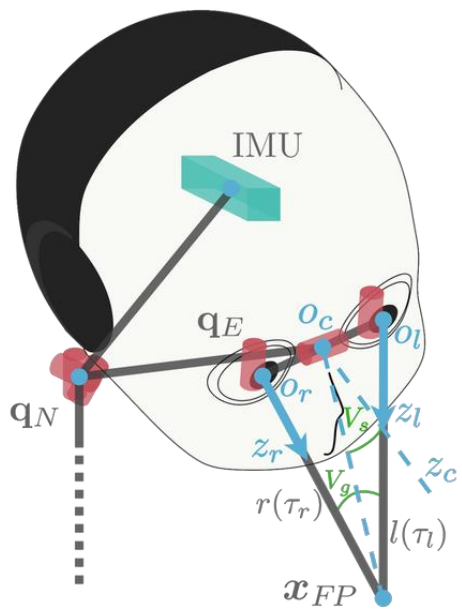
Then, apply easy transformations from Cartesian to ...

1. Egocentric angular space
2. Image planes (mono and stereo)





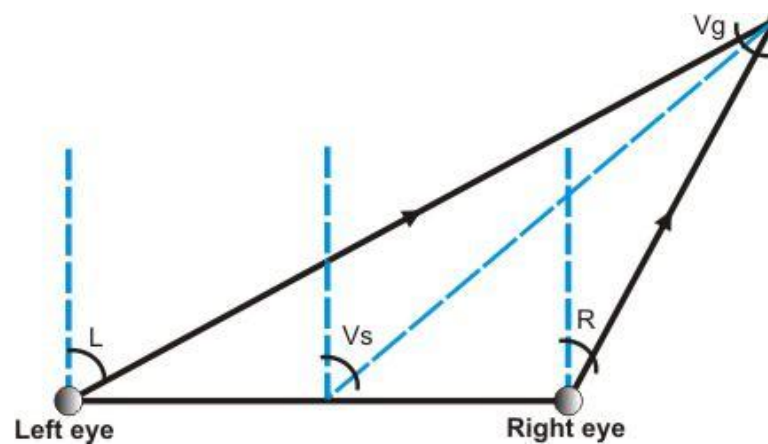
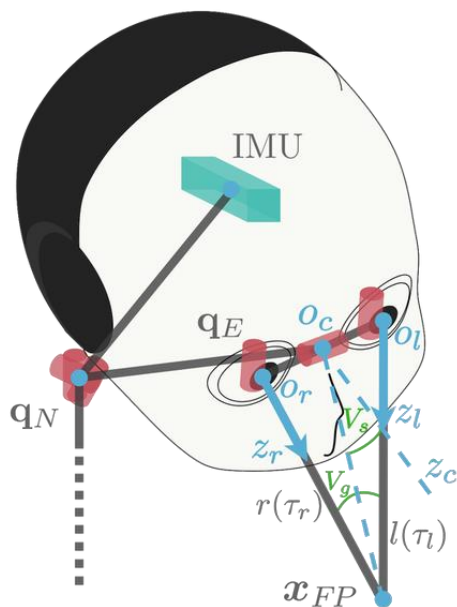
# The Gaze Controller (2/6)



Joint #	Part	Joint Name	Range	Unit
0	Neck	<b>Pitch</b>	+/-	[deg]
1	Neck	<b>Roll</b>	+/-	[deg]
2	Neck	<b>Yaw</b>	+/-	[deg]
3	Eyes	<b>Tilt</b>	+/-	[deg]
4	Eyes	<b>Version</b>	+/-	[deg]
5	Eyes	<b>Vergence</b>	$\geq 0$	[deg]



## The Gaze Controller (3/6)

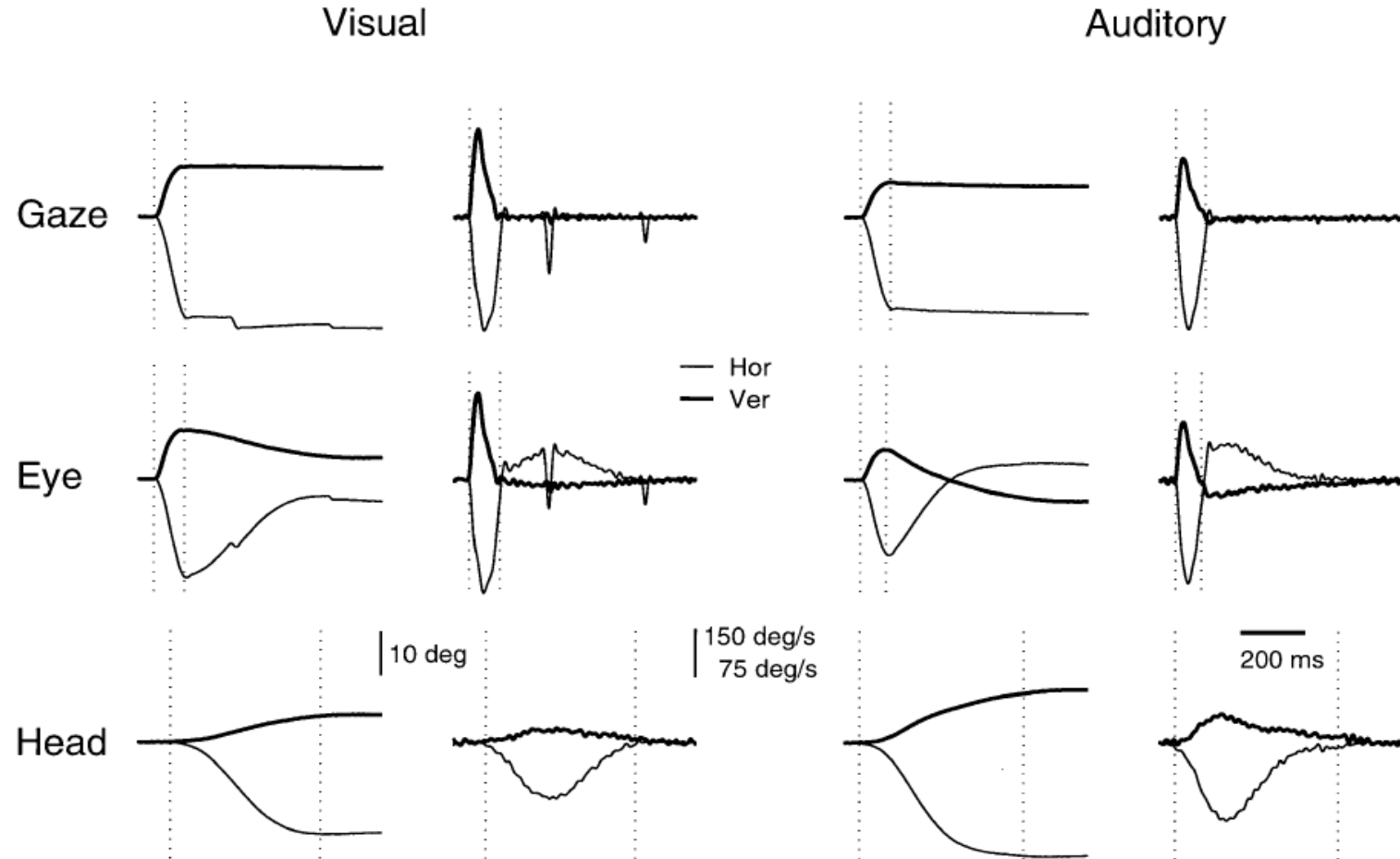


$$\begin{cases} V_g = L - R \\ V_s \approx (L + R)/2 \end{cases}$$



## The Gaze Controller (4/6)

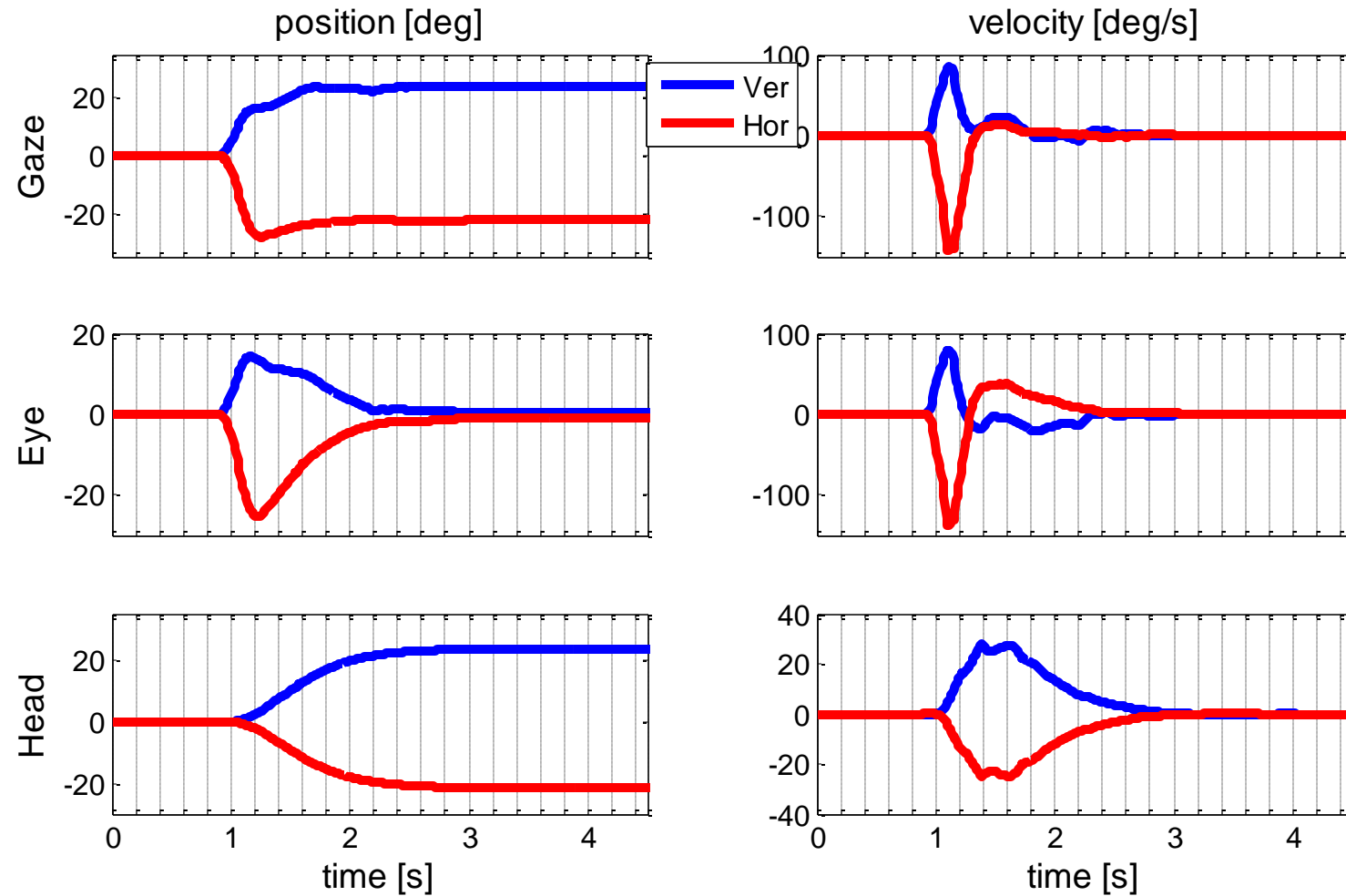
Studies on humans ...





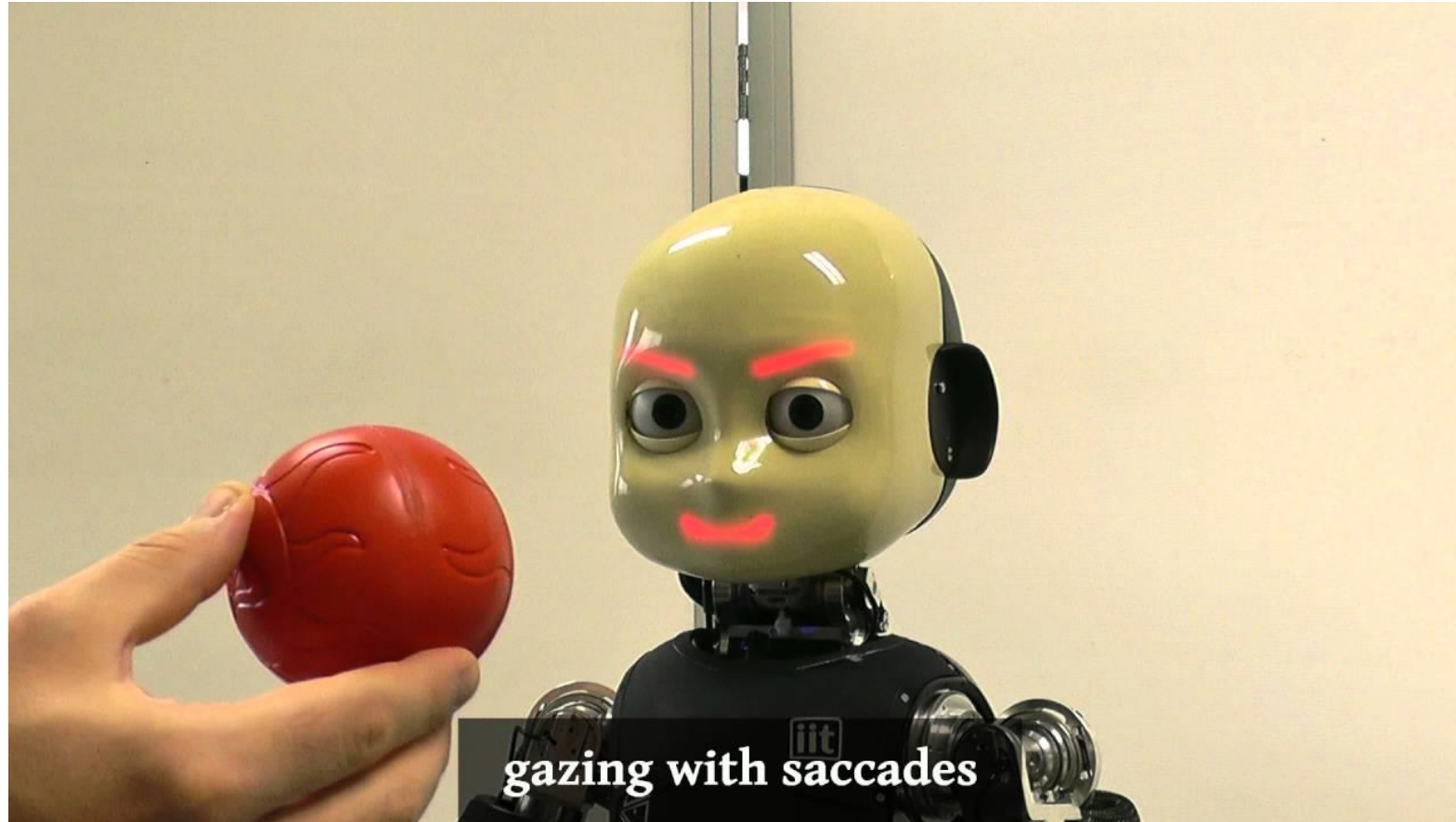
# The Gaze Controller (5/6)

Results on iCub ...





## The Gaze Controller (6/6)



<http://y2u.be/I4ZKfAvs1y0>



## Gaze Interface (1/6)

### OPENING THE GAZE INTERFACE

```
#include <yarp/dev/all.h>
Property option;

option.put("device", "gazecontrollerclient");
option.put("remote", "/iKinGazeCtrl");
option.put("local", "/client/gaze");

PolyDriver clientGazeCtrl(option);

IGazeControl *igaze=NULL;
if (clientGazeCtrl.isValid()) {
    clientGazeCtrl.view(igaze);
}
```



## Gaze Interface (2/6)

### GET CURRENT FIXATION POINT IN CARTESIAN DOMAIN

```
Vector x;  
igaze->getFixationPoint(x);
```

### GET CURRENT FIXATION POINT IN ANGULAR DOMAIN

```
Vector ang;  
igaze->getAngles(ang);  
// ang[0] => azimuth [deg]  
// ang[1] => elevation [deg]  
// ang[2] => vergence [deg]
```

### LOOK AT 3D POINT

```
igaze->lookAtFixationPoint(xd);
```

### ... IN ANGULAR DOMAIN

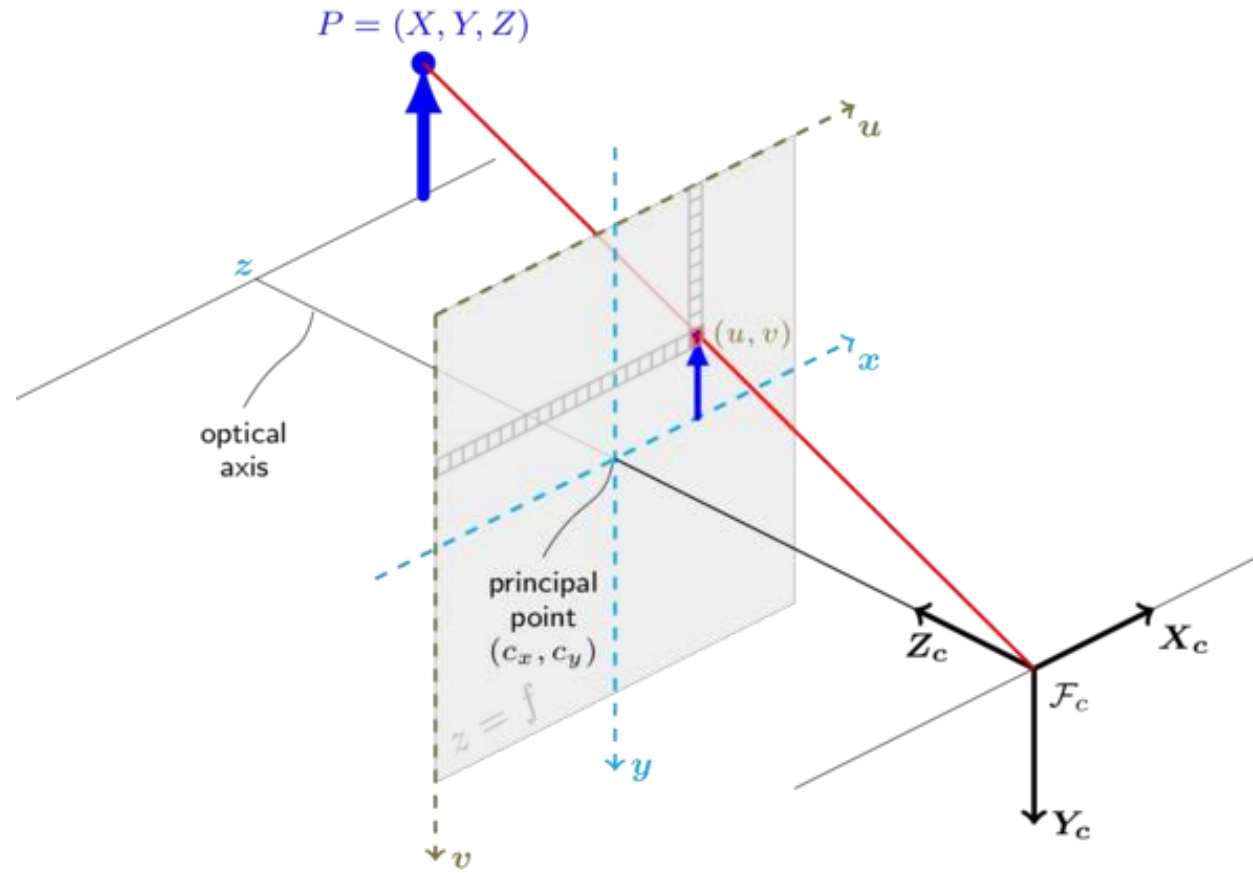
```
igaze->lookAtAbsAngles(ang);  
igaze->lookAtRelAngles(ang);
```





## Gaze Interface (3/6)

LOOK AT POINT IN IMAGE DOMAIN





## Gaze Interface (4/6)

### LOOK AT POINT IN IMAGE DOMAIN

```
int camSel=0; // 0 => left, 1 => right
Vector px(2);
px[0]=100;
px[1]=50;
double z=1.0;

igaze->lookAtMonoPixel(camSel,px,z);
```



### ... EQUIVALENT TO

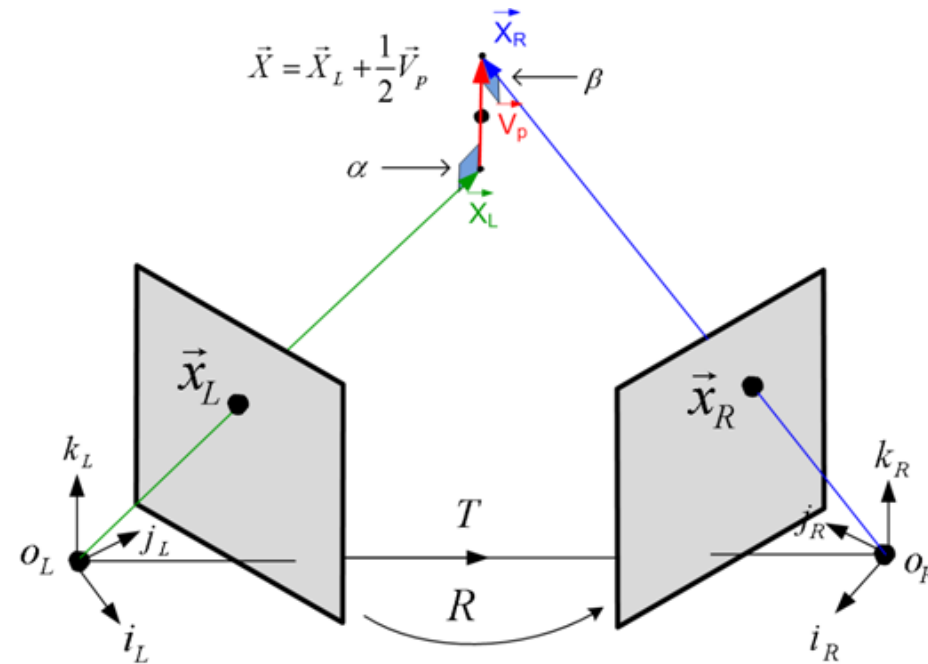
```
Vector x;
igaze->get3DPoint(camSel,px,z,x);
igaze->lookAtFixationPoint(x);
```



## Gaze Interface (5/6)

### GEOMETRY OF PIXELS

```
Vector x;  
igaze->get3DPointOnPlane(camSel,px,plane,x);  
igaze->get3DPointFromAngles(mode,ang,x);  
igaze->triangulate3DPoint(px1,pxr,x);
```





## Gaze Interface (6/6)

### GEOMETRY OF PIXELS

```
Vector x;  
igaze->get3DPointOnPlane(camSel,px,plane,x);  
igaze->get3DPointFromAngles(mode,ang,x);  
igaze->triangulate3DPoint(px1,pxr,x);
```





# Tutorial Time !