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Wien, am 8. Juli 2024

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# 1 Introduction

Research questions:

- Which criteria can distinguish between unactivated, activated and pre-activated cells?
- Do different types of activated cells exist? How are they different?
- With which frequencies does the Calcium concentration repeat after activation?
- Is there a difference in frequencies between mouse and human cells?



## 2 Optimization Algorithm

An optimization problem is any problem where a function  $f : X \rightarrow Y$  is given, and we search for the point  $x \in X$  such that  $f(x)$  is minimal. Obviously the minimum must not exist, as the example  $f : (0, 1] \rightarrow \mathbb{R}, x \mapsto x$  demonstrates. Investigating conditions on  $X, Y$  and  $f$  such that a minimum exists is mathematically interesting. However, when implementing an optimization algorithm the true minimum can often not be found and is instead replaced by a sufficiently good approximation.

First we want to first think about some variations of the problem.

In the case of a problem with additional conditions  $P$  the minimum must satisfy we can consider at the subset  $M := \{x \in X : P(x)\} \subseteq X$ . By finding the minimum of  $f : M \rightarrow Y$  the problem is solved. Once again such a minimum must not exist, even if one is present in  $X$ .

In the example dealt with in this work we are given some data points  $((x_k, y_k))_{k \in \{1, 2, \dots, n\}}$  and want to find a close approximation in the form of a function  $g(x, a_1, a_2, \dots, a_m)$  where for every  $a = (a_1, \dots, a_m)$  we have a function  $g_a(x) : \mathbb{R} \rightarrow \mathbb{R}, x \mapsto g(x, a_1, \dots, a_m)$ . Searching for a good approximation can be reformulated as searching for the minimum of  $r(a) := \sum_{k=1}^n |g_a(x_k) - b_k|^2$  or any other error function.

### 2.1 Algorithm Name

algorithm description

pseudo code for algorithm

[proof of convergence, if applicable]



## 3 T Cells, Calcium Concentration

Lymphocytes form a key component of the immune system. T cells are a type of lymphocyte and are responsible for responding to viruses, fungi, allergens and tumours. Different subtypes of t cells exist, that perform various responsibilities. They are transported throughout the body via the lymphatic system and blood.[KCF18]

Precursor cells are formed in the bone marrow. Once they are transported to the thymus they undergo maturation and selection to become t cells. Each cell forms receptors, called t cell receptors (TCR), that respond to one particular out of many ( $10^6$ – $10^9$ ) possible short pieces of proteins, called peptides. These peptides are attached to the major histocompatibility complex (MHC) present on antigens and antigen presenting cells (APC). Important aspects of the selection are ensuring that the t cells react to foreign peptides, but not to those present on the body's own cells.[AH24]

In positive selection cells in the thymus present peptides on their MHC. If a t cell is unable to bind, it will undergo apoptosis, a type of cell death. T cells which were able to bind receive survival signals. Negative selection verifies that t cells will not attack the body's own cells. This is done by only selecting t cells which only bind moderately to the peptides presented, as a strong bond suggests that these t cells would have a high likelihood of being reactive to own cells.[Hag18] If a t cell passed both the positive and negative selection it is transported to the periphery.

There are multiple types of peripheral t cells. Native t cells respond to new antigens. Cytotoxic t cells kill cells which present peptides on their MHC compatible with the t cells TCR. Helper T cells activate other parts of the immune response. Memory t cells shorten the reaction time when the same antigen is encountered again at a later point in time. Suppressor t cells moderate the immune response.[Gan97]

### 3.1 Components of a T Cell

T cell components relevant in activation and subsequent changes in intracellular  $\text{Ca}^{2+}$  are listed below and schematically shown in figure 3.1.

- **T cell receptor (TCR):** Receptor on the cell surface that can recognize peptides. By the simultaneous triggering of the TCR and co-stimulator signalling is induced that leads to activation.
- **Co-stimulator:** A stimulation of co-stimulatory molecules is necessary in order for signalling to occur as part of activation.
- **Endoplasmic reticulum (ER):** A series of connected sacs in the cytoplasm that is attached to the nucleus. Important functions are folding, modification and transportation of proteins.[Rog24]

- **Ca<sup>2+</sup> permeable ion channel on the ER:** There are several Ca<sup>2+</sup> channels present on the ER. Some receptors are responsible for releasing Ca<sup>2+</sup> into the cytoplasm, when the intracellular Ca<sup>2+</sup> concentration is low. [SB16]
- **Ca<sup>2+</sup> storage in the ER:** Ca<sup>2+</sup> is stored in the ER and can be released by Ca<sup>2+</sup> permeable ion channels on the ER.
- **Cytoplasm:** The semi-fluid substance enclosed in the plasm membrane. It contains organelles, ions, proteins and molecules.
- **Stromal interaction molecule (STIM):** If the Ca<sup>2+</sup> storage in the ER is depleted STIM proteins cluster where the ER is in the vicinity of the plasm membrane and assembles CRAC, which then leads to uptake in extracellular Ca<sup>2+</sup>. [SB16]
- **Plasm membrane:** A semipermeable structure forming the wall of the cell made up of lipids and proteins. Ion channels and transport proteins allow certain substances to move through.[Gan12]
- **Ca<sup>2+</sup> release activated Ca<sup>2+</sup> channel (CRAC):** Opened after a decrease in ER stored Ca<sup>2+</sup> is sensed by STIM, these channels intake Ca<sup>2+</sup> from outside the cell.[SI13]
- **Cytoskeleton:** A system of fibres within the cell, that allows it to change shape and move.[Gan12]
- **Nucleus:** An organelle that stores most of the DNA, controls cell growth and cell division. A double membrane separates it from the cytoplasm.[CA22]

Relevant components of APC are the

- **Major histocompatibility complex (MHC)**, which can present peptides, and the
- **Co-stimulator**, which can form a bond with the co-stimulator on a t cell.

Both are present on the surface of the APC.

## 3.2 Activation

Activation is necessary for t cells to divide and perform their functions.[Gan97]

When a native t cell encounters a peptide on an APC that is compatible, a bond is formed between the TCR on the t cell and the peptide-MHC complex on the APC. This recognition can be triggered by less than ten molecules of foreign substance and is therefore described as near perfect. Sufficiently long contact is necessary between the APC and the t cell in order for the t cell to activate. The role of contact time in t cell activation is modelled by Morgan et al..[ML23].

The presence of co-stimulatory molecules is needed for proper activation. The bond between the co-stimulatory molecules on the t cell and APC plays a role in signalling. Ca<sup>2+</sup> signals play a vital part in t cell activation.

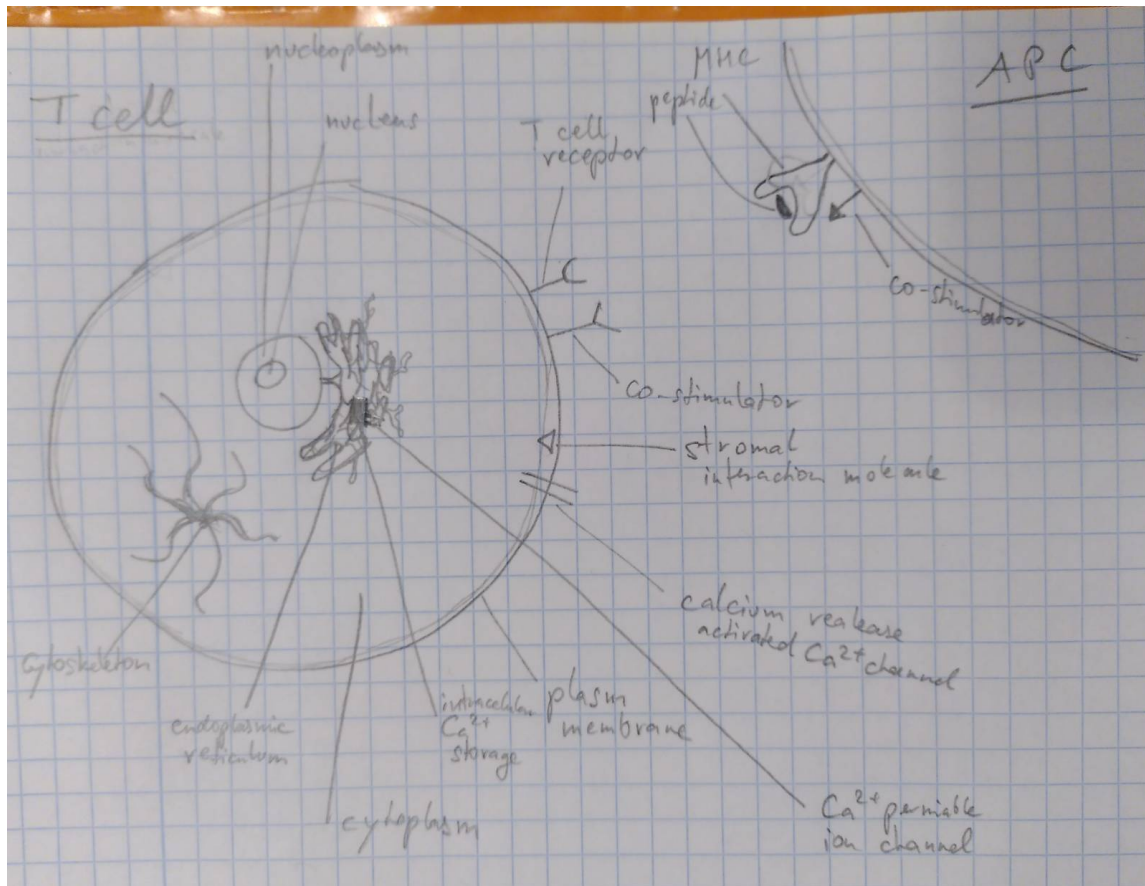


Figure 3.1: Schematic view of a t cell and antigen presenting cell, with all relevant components.

An increase of  $\text{Ca}^{2+}$  in t cells during activation is caused by the stimulation of  $\text{Ca}^{2+}$  permeable ion channel receptors on the ER membrane.  $\text{Ca}^{2+}$  is released from the ER into the cytoplasm. Additionally, this decrease in  $\text{Ca}^{2+}$  is sensed by STIM, which leads to an influx of  $\text{Ca}^{2+}$  through plasma membrane CRAC channels.[SKJ09]

As the intracellular  $\text{Ca}^{2+}$  concentration is dependent on the interaction between  $\text{Ca}^{2+}$  sources and sinks, a variety of different forms in  $\text{Ca}^{2+}$  concentration have been observed. Examples are infrequent spikes, sustained oscillations and plateaus.[Lew01]

Intercellular  $\text{Ca}^{2+}$  increase together with other signals lead to a redistribution of receptors, signalling molecules and organelles.[JRB14]



## 4 Data

From section 3.2, we gather that analysing the intracellular  $\text{Ca}^{2+}$  concentration gives us good insight in whether and when a cell activates. Additionally, it can be measured relatively easily by the method described in this chapter.

### 4.1 Structure of Data

The data matrix has a row per tracked cell and frame. The information stored for each cell and frame combination is described in detail in table 4.1.

Name	Data Type	Description
x	float64	Position of cell in pixels along the horizontal axis
y	float64	Position of cell in pixels along the vertical axis
frame	int32	Number of frame, with frame rate of 1 frame per second
mass short	float64	Brightness of cell in 340nm channel
bg short	float64	Background in 340nm channel
mass long	float64	Brightness of cell in 380nm channel
bg long	float64	Background in 380nm channel
ratio	float64	Calculated as mass short divided by mass long
particle	int32	Identification for each particle

Table 4.1: Description and data type of all columns present in the data matrix.

One recording can have between 500 and 10000 cells and is between 700 and 1000 frames long, which corresponds to between about 11 and 17 minutes. The ratio is typically between 0 and 5.

### 4.2 How it was generated

Four recordings were generated, with two each from human and mouse cells. Per cell type a positive and negative control was measured. In a positive control the conditions are such, that in theory every cell should activate, while in negative control the conditions are such, that none should activate. Due to stress on the cells and other factors a few cells will not follow theory.

#### 4.2.1 Jurkat Cells, 5c.c7 primary mouse T cells and Fura-2

The prototypical cell line to study T cell signalling is the Jurkat cell line.[ML23] It was obtained from the blood of a boy with T cell leukaemia.[SSB77] Different cell lines within

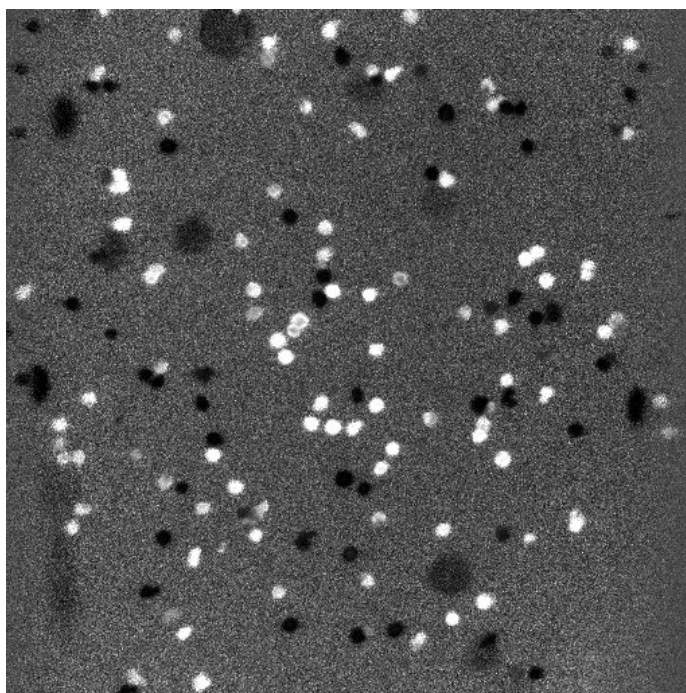


Figure 4.1: Single frame showing the ratio of the 340nm and 380nm images from a recording of human Jurkat cells. Activated cells appear lighter, unactivated cells darker than the background. Big dark circles are out of focus cells that have not yet settled on to the plate.

the Jurkat family are described by Abraham and Weiss.[[AW04](#)] They provide a timeline of discoveries linked to Jurkat cells and t cell receptor signalling.

Another type of T cells used in signalling studies are gathered from mice. [Additional information]

In order to be able to measure the intracellular  $\text{Ca}^{2+}$  concentration of cells they can be labelled with Fura-2. This method provides a way to record the  $\text{Ca}^{2+}$  concentration of multiple cells over a time period.[[MMS17](#)] Challenges encountered when using Fura-2 on certain cell types are described by Roe, Lemasters and Herman along with their respective solutions.[[RLH90](#)]

#### 4.2.2 Measuring Calcium Concentration

After the cells have been labelled with Fura-2, a recording of up to 15 to 20 minute can be generated. To achieve this the cells and stimulant are photographed at both 340nm and 380nm wavelength once per second. The resolution of the images are 1.6 $\mu\text{m}$  per pixel. By calculating the ratio of the two images at each point the  $\text{Ca}^{2+}$  concentration can be observed. An exemplary resulting image showing the ratio is shown in figure [4.1](#). The T cells appear a lighter shade than the background when activated and darker when not activated.

To activate the cells in the duration of the recording they are transferred to a plate

covered with replicas of the MHC-peptide complex normally present on APCs. This plate is then recorded as described above. For a negative control the plate is not covered with peptides, while for the positive control the peptide covering on the plate is very dense. Recordings of different densities in peptides lead to activation of a percentage of t cells.

### 4.2.3 Processing

To track single t cells moving around during the video the sum of the 340nm and 380nm image of each second is calculated. This image provides the basis for separating t cells from the background. On this image all t cells will appear similarly light in colour. Therefore, it is used to track the movement of cells. Each cell is numbered, such that the same cell will have the same number during the video. For some cells the trajectory tracking is not perfect, resulting in a split of the numbering into multiple numbers for the same cell. The position and shade during both 340nm and 380nm as well as the ratio of each particle and each frame is then recorded into the data structure used in this work. The first roughly 50 frames at the start of the recording are discarded due to the video being out of focus. Additionally, cells only appearing in fewer than 300 frames are discarded as they most likely represent trajectories incorrectly tracked or split. The resulting data is then stored in a matrix structured as described in table 4.1.



## 5 Results



## **6 Conclusion**





# Bibliography

- [AH24] K Maude Ashby and Kristin A Hogquist. “A guide to thymic selection of T cells”. In: *Nature Reviews Immunology* 24.2 (2024), pp. 103–117.
- [AW04] Robert T Abraham and Arthur Weiss. “Jurkat T cells and development of the T-cell receptor signalling paradigm”. In: *Nature reviews immunology* 4.4 (2004), pp. 301–308.
- [CA22] Geoffrey M Cooper and Kenneth Adams. “The Nucleus”. eng. In: *The cell: a molecular approach*. 19. edition. Oxford University Press, 2022, pp. 336–364. ISBN: 9780197583722.
- [Gan12] William F. Ganong. “Overview of Cellular Physiology in Medical Physiology”. eng. In: *Review of medical physiology*. 24. edition. Stamford, Conn: McGraw-Hill, 2012, pp. 35–66. ISBN: 9780071780032.
- [Gan97] William F. Ganong. “Circulating Body Fluids”. eng. In: *Review of medical physiology*. 18. ed. Stamford, Conn: Appleton & Lange, 1997, pp. 486–488. ISBN: 9780838584439.
- [Hag18] Kimberly Hagel. *Positive and Negative Selection of T Cells*. 2018. URL: <https://immunobites.com/2018/08/20/positive-and-negative-selection-of-t-cells/> (visited on 06/21/2024).
- [JRB14] Noah Joseph, Barak Reicher, and Mira Barda-Saad. “The calcium feedback loop and T cell activation: how cytoskeleton networks control intracellular calcium flux”. In: *Biochimica et Biophysica Acta (BBA)-Biomembranes* 1838.2 (2014), pp. 557–568.
- [KCF18] Brahma V Kumar, Thomas J Connors, and Donna L Farber. “Human T cell development, localization, and function throughout life”. In: *Immunity* 48.2 (2018), pp. 202–213.
- [Lew01] Richard S Lewis. “Calcium Signaling Mechanisms in T Lymphocytes”. In: *Annual Review of Immunology* 19. Volume 19, 2001 (2001), pp. 497–521. ISSN: 1545-3278. DOI: <https://doi.org/10.1146/annurev.immunol.19.1.497>. URL: <https://www.annualreviews.org/content/journals/10.1146/annurev.immunol.19.1.497>.
- [ML23] Jonathan Morgan and Alan E Lindsay. “Modulation of antigen discrimination by duration of immune contacts in a kinetic proofreading model of T cell activation with extreme statistics”. In: *PLOS Computational Biology* 19.8 (2023), e1011216.

- [MMS17] Magdiel Martínez, Namyr A Martínez, and Walter I Silva. “Measurement of the intracellular calcium concentration with Fura-2 AM using a fluorescence plate reader”. In: *Bio-protocol* 7.14 (2017), e2411–e2411.
- [RLH90] MW Roe, JJ Lemasters, and B Herman. “Assessment of Fura-2 for measurements of cytosolic free calcium”. In: *Cell calcium* 11.2-3 (1990), pp. 63–73.
- [Rog24] Kara Rogers. *endoplasmic reticulum*. 2024. URL: <https://www.britannica.com/science/endoplasmic-reticulum> (visited on 06/23/2024).
- [SB16] Dianne S. Schwarz and Michael D. Blower. “The endoplasmic reticulum: structure, function and response to cellular signaling”. In: *Cellular and Molecular Life Sciences* 73 (2016), pp. 79–94. DOI: <https://doi.org/10.1007/s00018-015-2052-6>. URL: <https://www.ncbi.nlm.nih.gov/pmc/articles/PMC4700099/>.
- [SI13] Peter B Stathopoulos and Mitsuhiro Ikura. “Structural aspects of calcium-release activated calcium channel function”. In: *Channels* 7.5 (2013). PMID: 24213636, pp. 344–353. DOI: [10.4161/chan.26734](https://doi.org/10.4161/chan.26734). eprint: <https://doi.org/10.4161/chan.26734>. URL: <https://doi.org/10.4161/chan.26734>.
- [SKJ09] Jennifer E Smith-Garvin, Gary A Koretzky, and Martha S Jordan. “T cell activation”. In: *Annual review of immunology* 27 (2009), pp. 591–619.
- [SSB77] Ulrich Schneider, Hans-Ulrich Schwenk, and Georg Bornkamm. “Characterization of EBV-genome negative “null” and “T” cell lines derived from children with acute lymphoblastic leukemia and leukemic transformed non-Hodgkin lymphoma”. In: *International journal of cancer* 19.5 (1977), pp. 621–626.