

LINAG 08

3.3.2. α) $\begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \mapsto \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} \quad \begin{pmatrix} 2 \\ 3 \\ 4 \end{pmatrix} \mapsto \begin{pmatrix} 5 \\ 3 \\ 1 \end{pmatrix} \quad \begin{pmatrix} 2 \\ 4 \\ 5 \end{pmatrix} \mapsto \begin{pmatrix} 3 \\ 2 \\ 2 \end{pmatrix}$

$$\begin{pmatrix} 1 & 2 & 2 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \\ 3 & 5 & 3 \\ 2 & 3 & 2 \\ 1 & 1 & 2 \end{pmatrix} \xrightarrow{\substack{-I \quad -I}} \begin{pmatrix} 1 & 1 & 1 \\ 2 & 1 & 2 \\ 3 & 1 & 2 \\ 3 & 2 & 0 \\ 2 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix} \xrightarrow{\substack{-III \quad -II}} \begin{pmatrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \\ 3 & 2 & -2 \\ 2 & 1 & -1 \\ 0 & 0 & 1 \end{pmatrix} \xrightarrow{\substack{-III \quad -I}} \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \\ 3 & 4 & -5 \\ 2 & 2 & -3 \\ 0 & -1 & 1 \end{pmatrix} \xrightarrow{\substack{II \quad III \quad I}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 4 & -5 & 3 \\ 2 & -3 & 2 \\ -1 & 1 & 0 \end{pmatrix}$$

$$\Rightarrow A = \begin{pmatrix} 4 & -5 & 3 \\ 2 & -3 & 2 \\ -1 & 1 & 0 \end{pmatrix}$$

β) $\begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \mapsto \begin{pmatrix} 2 \\ 1 \\ 2 \end{pmatrix} \quad \begin{pmatrix} 2 \\ 3 \\ 4 \end{pmatrix} \mapsto \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix} \quad \begin{pmatrix} 2 \\ 4 \\ 5 \end{pmatrix} \mapsto \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$

$$\begin{pmatrix} 1 & 2 & 2 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \\ 2 & 3 & 1 \\ 1 & 0 & 0 \\ 2 & 0 & 0 \end{pmatrix} \xrightarrow{\substack{-I \quad -II}} \begin{pmatrix} 1 & 1 & 0 \\ 2 & 1 & 1 \\ 3 & 1 & 1 \\ 2 & 1 & -2 \\ 1 & -1 & 0 \\ 2 & -2 & 0 \end{pmatrix} \xrightarrow{\substack{-3III \quad -III}} \begin{pmatrix} 1 & 1 & 0 \\ -1 & 0 & 1 \\ 0 & 0 & 1 \\ 8 & 3 & -2 \\ 1 & -1 & 0 \\ 2 & -2 & 0 \end{pmatrix} \xrightarrow{-II} \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 1 \\ 0 & 0 & 1 \\ 5 & 3 & -2 \\ 2 & -1 & 0 \\ 4 & -2 & 0 \end{pmatrix} \xrightarrow{\substack{(-I) \quad +I}} \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \\ -5 & 3 & 3 \\ -2 & -1 & 2 \\ -4 & -2 & 4 \end{pmatrix} \xrightarrow{\substack{II \quad I \quad III}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 3 & -5 & 3 \\ -1 & -2 & 2 \\ -2 & -4 & 4 \end{pmatrix}$$

$$\Rightarrow A = \begin{pmatrix} 3 & -5 & 3 \\ -1 & -2 & 2 \\ -2 & -4 & 4 \end{pmatrix}$$