

ANAL

7.) ges: $\sqrt[6]{1}$ in Polarkoordinaten und Real- und Imaginär Schreibweise

$$1+0i = (1, 0) \quad \sqrt[6]{1} = (1, \frac{2\pi}{6} \cdot k) \quad k \in \mathbb{Z}$$

$$\Rightarrow (1, 0), (1, \frac{\pi}{3}), (1, \frac{2\pi}{3}), (1, \pi), (1, \frac{4\pi}{3}), (1, \frac{5\pi}{3}) \text{ Lösungen in}$$

Polarkoordinaten

$$(1, 0) = 1$$

$$(1, \frac{\pi}{3}) = \frac{1}{2} + i \frac{\sqrt{3}}{2}$$

$$(1, \frac{2\pi}{3}) = -\frac{1}{2} + i \frac{\sqrt{3}}{2}$$

$$(1, \pi) = -1$$

$$(1, \frac{4\pi}{3}) = -\frac{1}{2} - i \frac{\sqrt{3}}{2}$$

$$(1, \frac{5\pi}{3}) = \frac{1}{2} - i \frac{\sqrt{3}}{2}$$

$$w = r \cdot (\cos(t) + i \sin(t))$$

$$\frac{1}{2} + i \frac{\sqrt{3}}{2} = 1 \cdot (\cos(\frac{\pi}{3}) + i \sin(\frac{\pi}{3}))$$

$$\Rightarrow \cos(\frac{\pi}{3}) = \frac{1}{2} \quad \sin(\frac{\pi}{3}) = \frac{\sqrt{3}}{2}$$