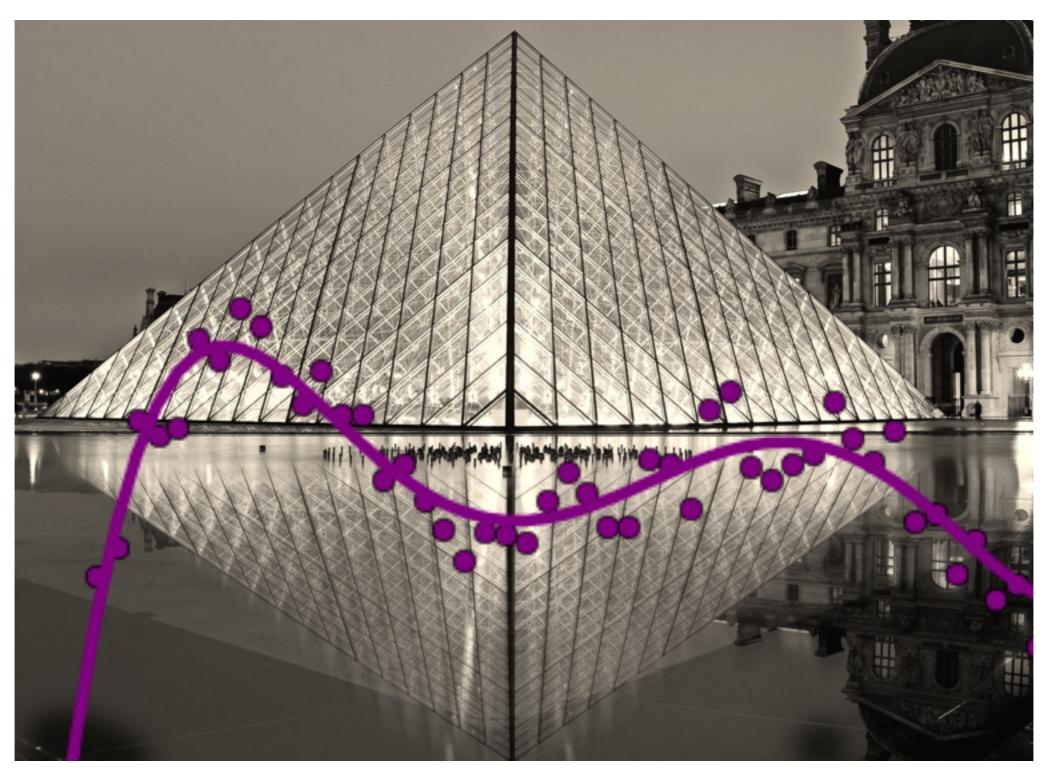
Approximation Algorithms



Combinatorial optimization: Scheduling classes

Planning delivery routes for trucks

Most are NP-hard

Le Diplôme de l'ENS - Spécialité Informatique

Emploi du Temps 2015-2016 - 1ère année (L3 informatique) 1er semestre

Lundi				Mardi			Mercredi		Jeudi			Vendredi		
		TD proba 1	Syst emes Dyna miques		Algèbre 1	Proba 2		Logique		TD Topo 1	EDP cours	Structures et Algorithmes Aléatoires (A Bouillard)		TD Logiqu
		Topo 1	miques			Logique	Topo 1	Algèbre 2		TD Algèbre 1		8h30-12h15 Cours et TD		
_angages de				Système		TD Statis-			Langages		TD EDP	Début : Algorithmique	et	
orogrammatio et compilatio JC Filliatre) 13h15-15h15 cours salle W Début : 28 se	n	TD Algèbre 1	TD proba 2	Digital (J. Vuillemin) 13h15- 17h cours TD	TD Proba 1	tiques	Algèbre 1 Proba 1	Statis- tiques	formels (D. Vergnaud) 13h15- 17h cours	Proba 1	TD Syst emes	programmatio (C Mathieu) 13h15-15h15 cours salle UV Début :	n	Proba
15h15-17h00 TD 1 compil salle Info 4	TD 2 Algo salle W		Algèbre 2	(peut-etre2) salle UV Début : 29-sept	TD Topo 1	Model lisation et Simula tion	Thé d	u DMA	TD salle R Début :	GL	Dyna miques	15h15-17h00 TD 1 Algo salle W	TD 2 Compil salle Info 4	TD Algèbi 2
•		GT	TD Logique			Numé rique	17h00	-19h00			ı			





Dealing with NP-hard problems

- · Give up?
 · Roll up our sleeves?
- · Try something, hoping for luck?
- · Do a rough but good enough job

In polynomial time, we find a solution whose value is provably within a "small" factor of the optimal solution

Designing approximation algorithms

- Real-life problems are too complex
 Study idealized problems
- · Theorems: new algorithmic and structural insights



The interface with real life

Real life Distilling Theory for basic problems

A course with two parts Approximation algorithms, Part I

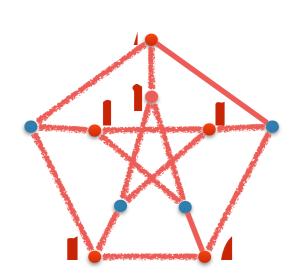
Vertex cover

Knapsack

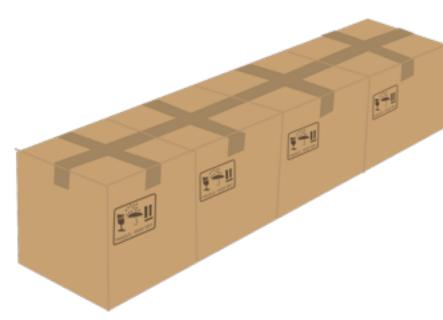
Bin packing

Set cover

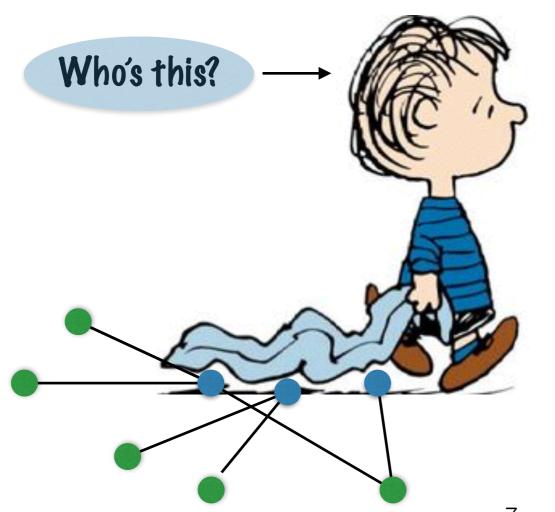
Multiway cut







Approximation algorithms, vertex cover, and linear programming





$$\min c_1 x_1 + c_2 x_2 + \dots + c_n x_n$$

such that

$$\begin{cases} a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n & \ge b_1 \\ a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n & \ge b_2 \end{cases}$$

. . .

$$a_{m1}x_1 + a_{m2}x_2 + \dots + a_{mn}x_n \ge b_m$$

 $\forall i: 0 \le x_i \le 1$

 $\forall i: x_i \text{ real number}$

Teaching staff behind the scenes

- · Vincent Cohen-Addad
- · Frederik Mallmann-Trenn

· Victor Verdugo



Film director: Nordine Méziane Cameraman: Jovanny Parvedy