

# Knapsack and rounding

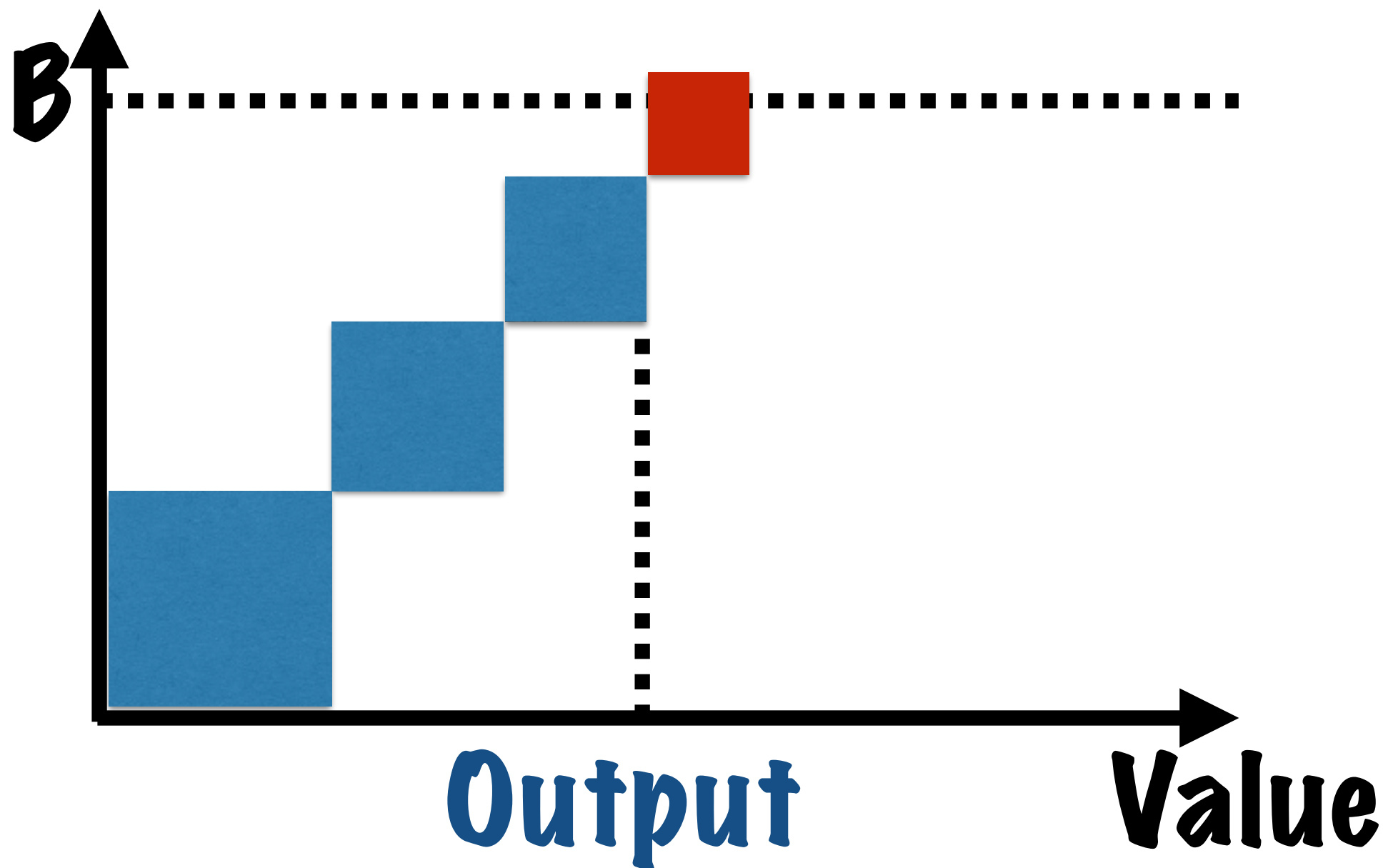


**A greedy algorithm  
for special case  $\text{size} = \text{value}$**

**Order items by decreasing value.**

**How good is that?**

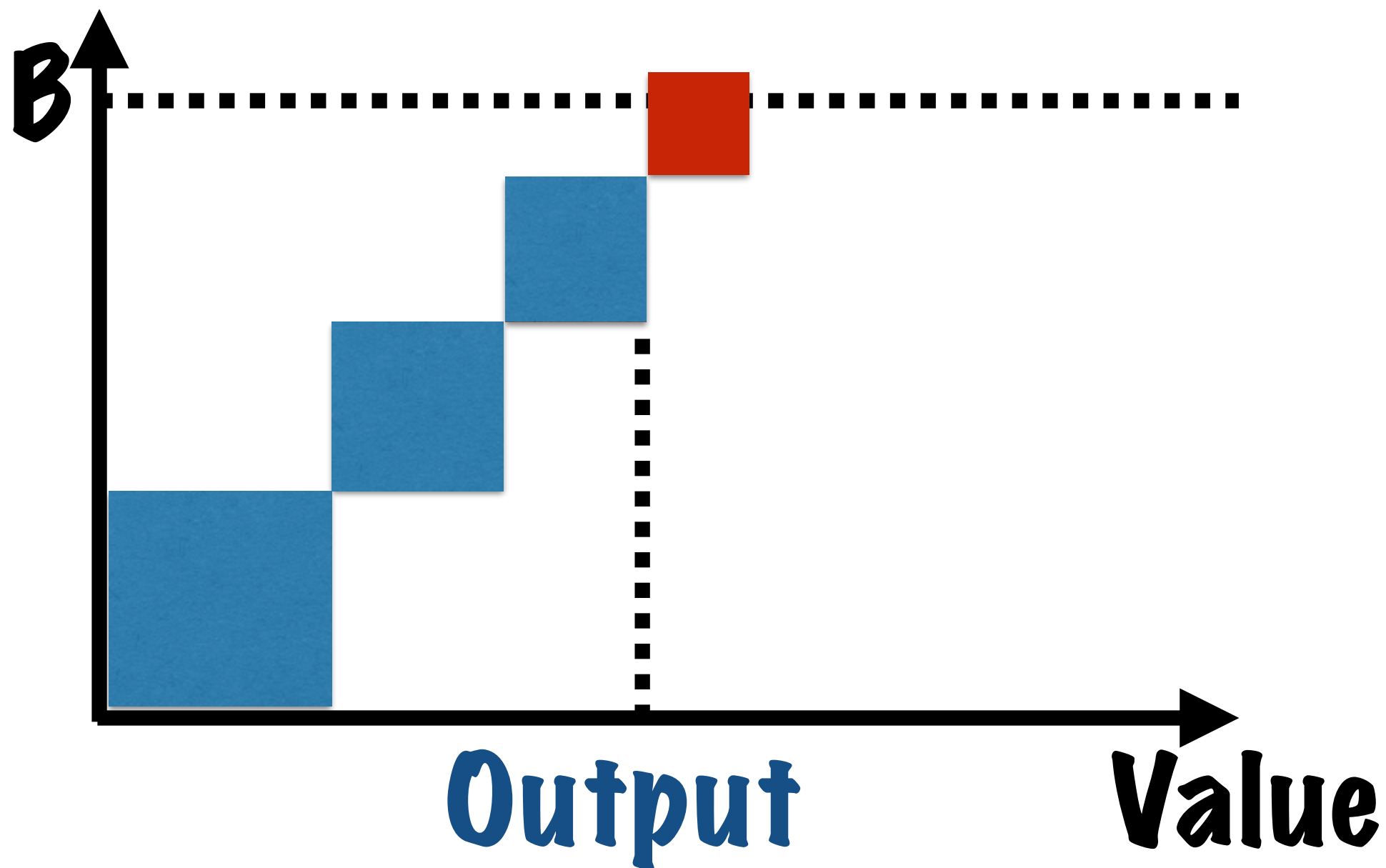
**Observe:**  $\text{OPT} \leq B$



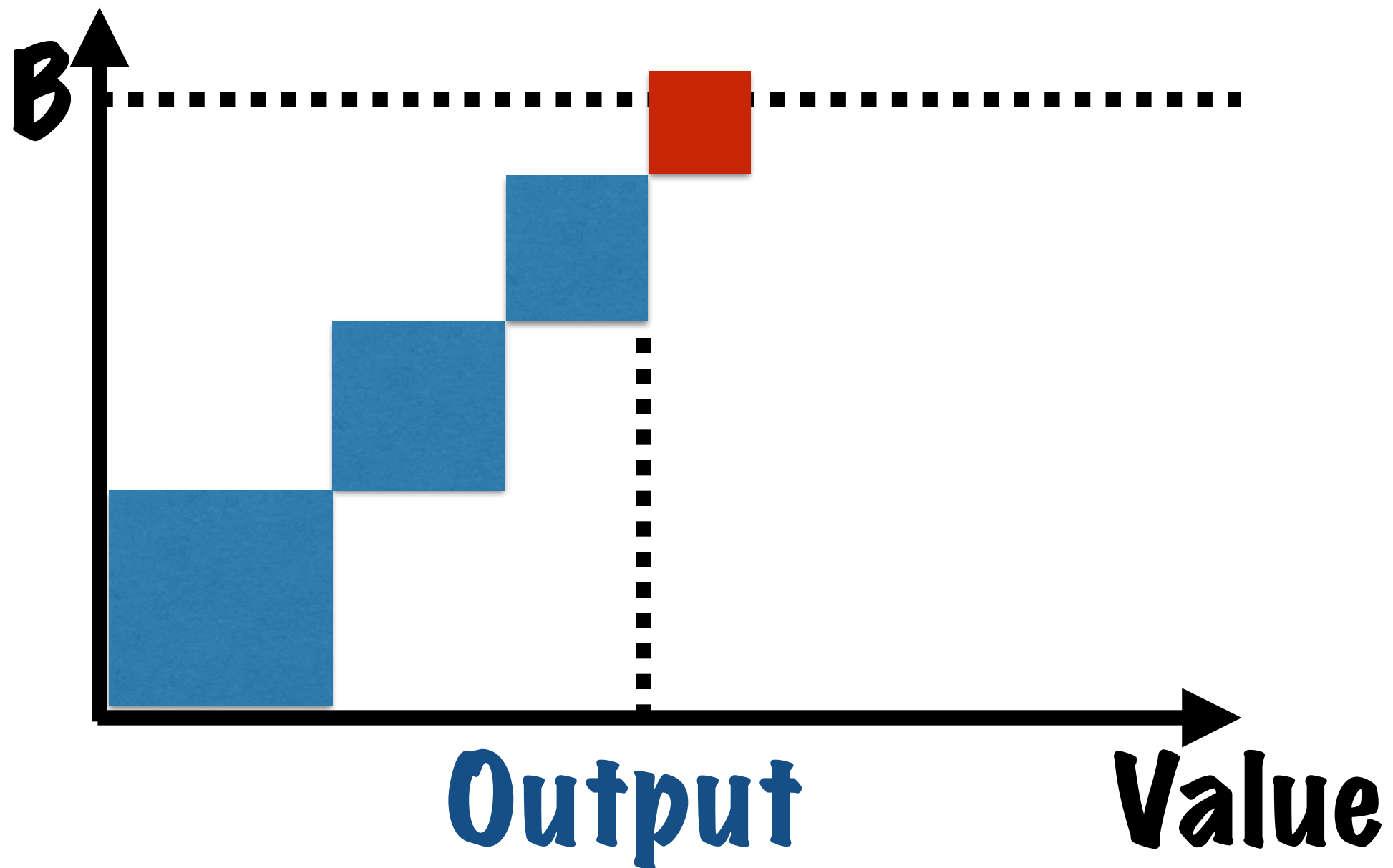
**Observe:  $\text{Output} + 1 \text{ item} > B$**

**Can assume:**

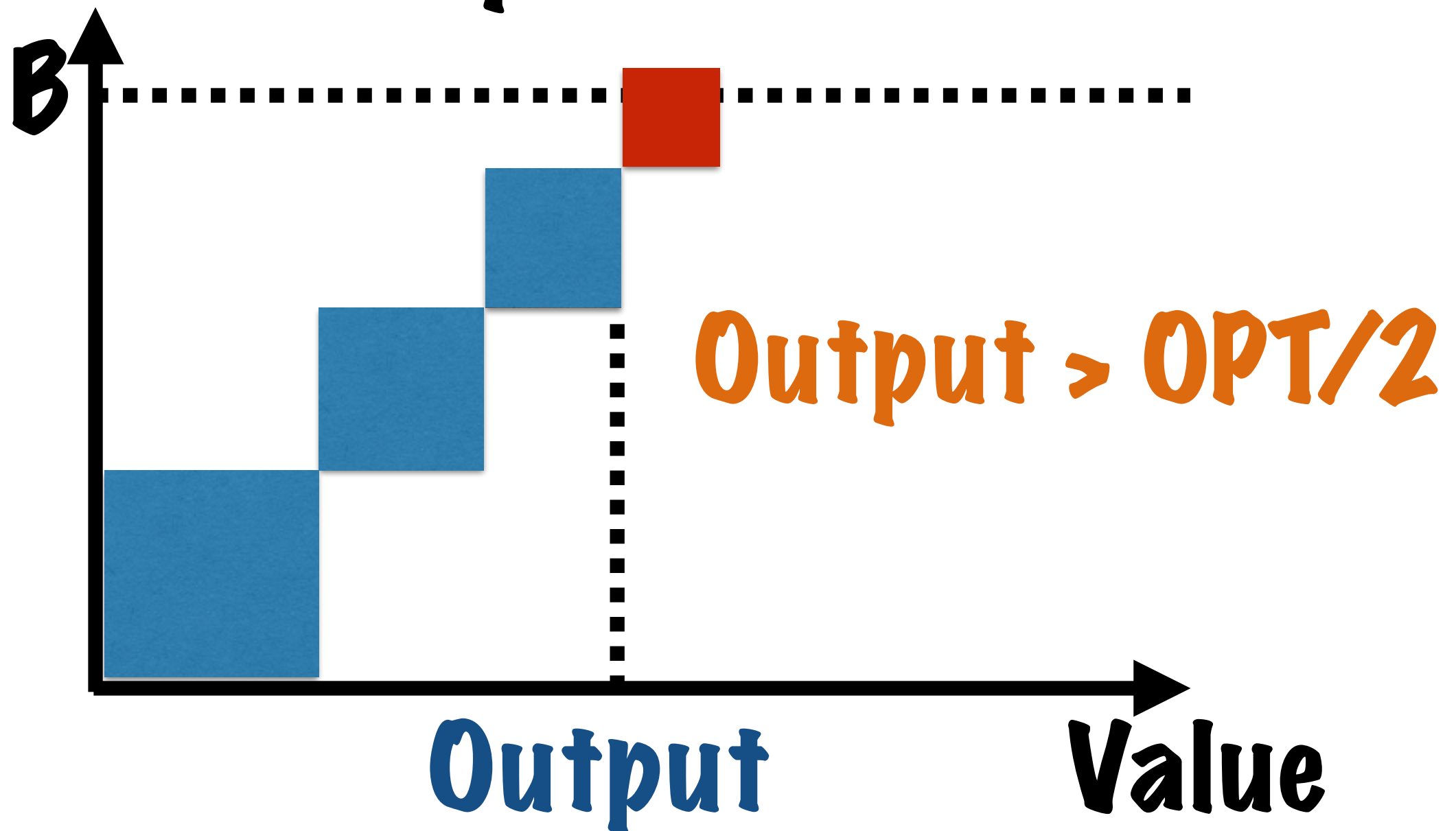
**Output has at least 1 item**



**Observe: first item in output  
is better than  
item not in output**



**Combine:  $\text{Output} + \text{red item} > B$**   
**First output item  $>$  red item**  
 **$\text{Output} > B/2$**



**Theorem:**  
in special case  $\text{size} = \text{value}$ ,  
greedy is a 2-approximation.

**Can we do better?**



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