

# Master Thesis

## *Methods for modular soundness checker of feature model evolution plans*

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# **Master Thesis**

*Methods for modular soundness checker of  
feature model evolution plans*

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# Abstract

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# Preface

# **Part I**

## **Introduction**

Giving the thesis a purpose (not how, but why) Mention problems in industry practice (mention software product lines) Say what software product lines are for, not technicalities, why they exist Talk about why planning is difficult, when the project size is increasing -¿ Changing the plan is even more difficult, and there is a lack of automated tools for checking that the changes don't break anything Drawing a picture of the domain and the problem My thesis is addressing these challenges by looking at these research questions or goals Last part of introduction: research questions/goals (base structure of thesis on this) - 3 is a good number They are general. What, how, (never why) In this thesis, I will address these questions through these activities ...(will not tackle everything, so make the purpose clear) Start broader, chunk down to more detail Can take the goals up again in the following sections (mention the research questions when tackling them) How the sensor should read my master's thesis. How will she know what my contribution is, where it comes in. "In chapter 2 I will give the background, limited to the scope of my thesis". Make it clear that I'm not trying to cover everything, and give the logic/structure of the thesis.

**TODO: Reread essay and identify useful parts**

# Chapter 1

## Background

Software product lines, previous publication (pinpoint what can be improved), SOS rules and operational semantics, and what is modular analysis Background should not contain many of my results, but rather retelling what software product lines are, what operational semantics are, existing technologies What is the difficulty of doing analysis on it? Just explaining the structures does not convey why it is worth spending time to solve the problems. Hint at what is coming, that this is something I will tackle in the contribution. Can't be technical in the introduction, the background is where I introduce the terms and definitions and technical details. And the implications of these details. Explain what I mean by "modularity", explain why the previous work is not modular. What do I assume, and what do I focus on

# **Part II**

## **The project**

Help the reader distinguish the plan and the change of plan (maybe in background). Make an illustration that can help convey the terminology (when I say this word, I'm in this level, etc.) Forskerlinjen is part of the story and research work. Can include what we did earlier, since the thesis is based on this work. Focus on the operations. Not necessary to have the rules here, but can refer to the paper. Can use it to explain what it means to be paradox-free. Can say what the plan looks like and what a sound plan is, and refer the reader to the paper for more details. Then say in this project I will look at modular modifications of a plan (the previous work does not tackle plan change). Since it is already published, the sensor does not need to evaluate that part, only the continuation which is this thesis. However, the previous work is a necessary part of the story of this thesis.

**TODO: Need to structure the project part more finely**

# Chapter 2

## Definitions and semantics

TODO: Explain why it's non-trivial, why it may be difficult to do it manually, why we need to restrict the scope etc. Why simple lookup is not enough.

### 2.1 Definitions

#### 2.1.1 Temporal feature model

A temporal feature model is defined as a triple  $(\text{NAMES}, \text{FEATURES}, \text{GROUPS})$  where  $\text{NAMES}$ ,  $\text{FEATURES}$ , and  $\text{GROUPS}$  are all maps. The reason for this choice is efficiency and modularity. As mentioned in **TODO: motivation or background or something**, the goal of this thesis is to minimize the scope of the plan to check for paradoxes, as a change rarely affects more than a small part of the plan. It would then be a mistake to represent a plan as a sequence of trees associated with time points, or an initial model followed by a sequence of operations as described in “Consistency-preserving evolution planning on feature models” (Motzfeldt et al. 2020). To add a new feature to the plan, both representations would require us to look through the entire plan to check that the feature ID is fresh.

To add or rename a feature, a soundness checker must verify that no other feature is using the name during the affected part of the plan. We therefore include the  $\text{NAMES}$  map in the representation for efficient verification of aforementioned issue. A feature or group ID may not already be in use when we add it, so the  $\text{FEATURES}$  and  $\text{GROUPS}$  maps support efficient lookup for IDs. The rest of this section gives more detailed explanations of temporal feature models.

#### 2.1.2 Maps

In general, a map is a set of entries on the form  $[k \mapsto v]$ , where each key  $k$  uniquely defines a value  $v$ . Looking up a value at the key  $k$  in map  $\text{MAP}$



looks like this:

$$\text{MAP}[k]$$

This query would give us  $v$  if  $[k \mapsto v] \in \text{MAP}$ . If we wish to assign a value  $v'$  to key  $k$ , this is the syntax:

$$\text{MAP}[k] \leftarrow v'$$

This also works if  $k$  is not already in the map. We assume  $O(1)$  for lookup and insertion. For maps with set values, we define an additional operator  $\stackrel{\cup}{\leftarrow}$ . If  $\text{MAP}[k] = S$  then

$$\text{MAP}[k] \stackrel{\cup}{\leftarrow} v = \text{MAP}[k] \leftarrow S \cup \{v\}$$

To remove a mapping with key  $k$ , we use  $\text{MAP} \setminus k$ . For maps with set values, we additionally define  $\setminus^v$ , where  $v$  is some value. Let  $\text{MAP}$  be a map with set values containing the mapping  $[k \mapsto \{v\} \cup S]$ . Then  $\setminus^v$  is defined as follows:

$$\text{MAP} \setminus^v k = \begin{cases} \text{MAP} \setminus k & \text{if } S = \emptyset \\ \text{MAP}[k] \leftarrow S & \text{if } |S| > 0 \end{cases}$$

That is, if removing  $v$  leaves only the empty set at  $\text{MAP}[k]$ , we remove the mapping. Otherwise, we only remove  $v$  from the set of values associated with  $k$ .

### 2.1.3 Intervals

To define the map values, we must first define an interval. We use the familiar mathematical notation  $[t_{\text{start}}, t_{\text{end}})$  for the intervals, where  $t_{\text{start}}$  and  $t_{\text{end}}$  denote points in time. The intervals are left-closed and right-open, meaning that  $t_{\text{start}}$  is included in the interval, and all time points until but not including  $t_{\text{end}}$ . We say that an interval  $[t_{\text{start}}, t_{\text{end}})$  *contains* the time point  $t_k$  if  $t_{\text{start}} \leq t_k < t_{\text{end}}$ . Two intervals  $[t_n, t_m)$  and  $[t_i, t_j)$  *overlap* if there exists a time point  $t_k$  with  $t_n \leq t_k < t_m$  and  $t_i \leq t_k < t_j$ , i.e. a time point contained by both intervals.

For intervals  $[t_{\text{start}}, t_{\text{end}})$  with unknown bounds, we may restrict the bounds to  $t_l$  and  $t_r$  by writing  $\langle [t_{\text{start}}, t_{\text{end}}) \rangle_{t_l}^{t_r}$ . We then get the interval  $[\max(t_{\text{start}}, t_l), \min(t_{\text{end}}, t_r))$ .

### 2.1.4 Interval maps

An interval map is a map where the key is an interval (section 2.1.3). To look up values, one can either give an interval or a time point as key. Both will return sets of values. For instance, if an interval map  $I$  contains the

$$\begin{aligned}
&I[t_1] \\
&I[t_3] \\
&I[[t_1, t_5]] \\
&I[[t_2, t_4]]
\end{aligned}$$

Figure 2.1: Interval map example

mapping  $[[t_1, t_5) \mapsto v]$ , all of the queries in Figure 2.1 will return  $\{v\}$  (assuming that  $t_1 < t_2 < \dots < t_5$ ):

$IM[t_n]_{\leq}$  returns the set of keys containing time point  $t_n$ . For interval maps with non-overlapping keys, the resulting set will contain at most one element. For interval maps with set values, we define an additional function  $IM[t_n]_{\leq}^v$  where  $v$  is some value, returning the set of the keys containing  $t_n$  and associated with a set containing  $v$ .

We furthermore define function  $IM[t_n, t_m)_{\approx}$  which returns all the interval keys in the map  $IM$  overlapping the interval  $[t_n, t_m)$ .

### 2.1.5 Interval sets

An interval set is a set of intervals with a few custom predicates and operations. Given an interval set  $IS$ ,  $[t_n, t_m) \in IS$  if  $[t_n, t_m)$  is a member of the set, which is the expected semantics of  $\in$ . We define a similar predicate  $\in_{\leq}$  such that  $[t_n, t_m) \in_{\leq} IS$  iff there exists some interval  $[t_i, t_j) \in IS$  with  $t_i \leq t_n \leq t_m \leq t_j$ , i.e. an interval in  $IS$  which contains  $[t_n, t_m)$ . We further define the predicate  $\in_{\approx}$  such that  $[t_n, t_m) \in_{\approx} IS$  iff there exists some interval  $[t_i, t_j) \in IS$  with  $[t_n, t_m)$  overlapping  $[t_i, t_j)$ .

Notice that  $\in \subseteq \in_{\leq} \subseteq \in_{\approx}$ , which means that if  $[t_n, t_m) \in IS$  then also  $[t_n, t_m) \in_{\leq} IS$ , and  $[t_n, t_m) \in_{\approx} IS$ .

$IS[t_n]_{\leq}$  returns the subset of  $IS$  containing  $t_n$ .

### 2.1.6 Mapping names

The **NAMES** map has entries of the form  $[\mathbf{name} \mapsto \text{interval map}]$ . Assuming  $[\mathbf{name} \mapsto IM] \in \mathbf{NAMES}$ , the interval map  $IM$  contains mappings on the form  $[[t_{\text{start}}, t_{\text{end}}) \mapsto \text{featureID}]$ , where  $\text{featureID}$  is the ID of some feature in the temporal feature model. This should be interpreted as “The name  $\mathbf{name}$  belongs to the feature with ID  $\text{featureID}$  from  $t_{\text{start}}$  to  $t_{\text{end}}$ ”. Looking up a name which does not exist will return an empty map  $\emptyset$ .

This map is mainly used when adding features or changing names. The new name and the scope of the change is then looked up in the **NAMES** map to verify that no other feature shares the name.

### 2.1.7 Mapping features

The FEATURES map has entries of the form  $[\text{featureID} \mapsto \text{feature entry}]$ . Since several pieces of information are crucial to the analysis of a feature, it is not enough to have a simple mapping as we have for names. A feature has a name, a type, a parent group, and zero or more child groups. Furthermore, a feature may be removed and re-added during the course of the plan, so we also need information about when the feature exists. This information is collected into a 5-tuple  $(F_e, F_n, F_t, F_p, F_c)$ , where  $F_e$  is an interval set denoting when the feature exists,  $F_n$  is an interval map with name values,  $F_t$  is an interval map with the feature's variation types,  $F_p$  is an interval map with group ID values, and  $F_c$  is an interval map where the values are sets containing group IDs, the interval keys possibly overlapping.

Looking up a feature which does not exist returns an empty feature  $(\emptyset, \emptyset, \emptyset, \emptyset, \emptyset)$ . This lets us treat an unsuccessful lookup the same way as a successful one.

The root ID is constant for a temporal feature model. We assume that it has been computed and is stored in the variable `rootID`.

The reasoning behind the choice of interval sets and maps here is in large part the temporal scope; for instance, when a feature is removed, we can easily look up the temporal scope in the  $F_c$  map (child groups) to verify that removing the feature leaves no group without a parent.

### 2.1.8 Mapping groups

The GROUPS map has entries of the form  $[\text{groupID} \mapsto \text{group entry}]$ . A group has a type, a parent feature, and zero or more child features. It may also be removed and re-added. These can all be defined in terms of intervals and collected into a 4-tuple similarly to the feature entries  $(G_e, G_t, G_p, G_c)$ , where  $G_e$  is an interval set denoting when the group exists,  $G_t$  is a map with the group's types,  $G_p$  is a map with feature IDs, and  $G_c$  is a map with feature ID values, the interval keys possibly overlapping.

Looking up a group which does not exist in the map returns an empty group  $(\emptyset, \emptyset, \emptyset, \emptyset)$ .

### 2.1.9 Example evolution plan

A small example of a temporal feature model can be found in Figure 2.2 on the following page. It contains three features and one group, and describes a temporal feature model for a washing machine. The washing machine always has a washer, and a dryer is added at  $t_5$ . It is clear from this example that the representation is better suited for manipulating the structure than reading it.

$$\begin{aligned}
& (\{ [\text{Washing Machine} \mapsto [ [t_0, \infty) \mapsto 0 ] ] \\
& , [\text{Washer} \mapsto [ [t_0, \infty) \mapsto 1 ] ] \\
& , [\text{Dryer} \mapsto [ [t_5, \infty) \mapsto 2 ] ] \} \\
\\
& , \{ [0 \mapsto (\{ [t_0, \infty) \}, \\
& \quad \{ [ [t_0, \infty) \mapsto \text{Washing Machine} ] \}, \\
& \quad \{ [ [t_0, \infty) \mapsto \text{MANDATORY} ] \}, \\
& \quad \emptyset, \\
& \quad \{ [ [t_0, \infty) \mapsto 10 ] \} ) ] \\
& , [1 \mapsto (\{ [t_0, \infty) \}, \\
& \quad \{ [ [t_0, \infty) \mapsto \text{Washer} ] \}, \\
& \quad \{ [ [t_0, \infty) \mapsto \text{MANDATORY} ] \}, \\
& \quad \{ [ [t_0, \infty) \mapsto 10 ] \}, \\
& \quad \emptyset ) ] \\
& , [2 \mapsto (\{ [t_5, \infty) \}, \\
& \quad \{ [ [t_5, \infty) \mapsto \text{Dryer} ] \}, \\
& \quad \{ [ [t_5, \infty) \mapsto \text{OPTIONAL} ] \}, \\
& \quad \{ [ [t_5, \infty) \mapsto 10 ] \}, \\
& \quad \emptyset ) ] \} \\
\\
& , \{ [10 \mapsto (\{ [t_0, \infty) \}, \\
& \quad \{ [ [t_0, \infty) \mapsto \text{AND} ] \}, \\
& \quad \{ [ [t_0, \infty) \mapsto 0 ] \}, \\
& \quad \{ [ [t_0, \infty) \mapsto 1 ], [ [t_5, \infty) \mapsto 2 ] \} ) ] \\
& \} )
\end{aligned}$$

Figure 2.2: Small temporal feature model

### 2.1.10 Operations

We define *operations* to alter the temporal feature model. A software product line may grow very large, and the plans even larger. Since different factors may influence the plan, it is necessary to be able to change the plan accordingly. If the plan is indeed extremely large, and since feature models have strict structure constraints, it is also necessary to check *automatically* that the changes do not compromise the structure. Due to the size and complexity of the problem, it is not enough to let a human verify a change.

- **addFeature(featureID, parentGroupID, name, featureType)** from  $t_n$  to  $t_m$   
Adds feature with id featureID, name name, and feature variation type featureType to the group with id parentGroupID in the interval  $[t_n, t_m)$ . featureID must be fresh, and the name cannot belong to any other feature in the model during the interval. The parent group must exist during the interval, and the types of the feature and the parent group must be compatible. If the feature has type MANDATORY, then the parent group must have type AND.
- **addGroup(groupID, parentFeatureID, groupType)** from  $t_n$  to  $t_m$   
Adds group with id groupID and type groupType to the feature with id parentFeatureID during the interval  $[t_n, t_m)$ . The group ID must be fresh, and the parent feature must exist during the interval.
- **removeFeature(featureID)** at time  $t_n$   
Removes the feature with ID featureID from the feature model at  $t_n$  (does not affect possible reintroductions). The FEATURES map in the original plan must contain a mapping  $[featureID \mapsto (EXISTENCE, \dots)]$  such that  $[t_i, t_j) \in EXISTENCE$  with  $t_i \leq t_n \leq t_j$ . The feature must not have any child groups during  $[t_n, t_j)$ . After removing the feature, all interval mappings should be updated from  $[t_i, t_j)$  to  $[t_i, t_n)$ .
- **removeGroup(groupID)** at time  $t_n$   
Removes the group with ID groupID from the feature model at  $t_n$  (does not affect possible reintroductions). The GROUPS map in the original plan must contain a mapping  $[groupID \mapsto (EXISTENCE, \dots)]$  such that  $[t_i, t_j) \in EXISTENCE$  with  $t_i \leq t_n \leq t_j$ . The group must not have any child features during  $[t_n, t_j)$ . After removing the group, all interval mappings should be updated from  $[t_i, t_j)$  to  $[t_i, t_n)$ .
- **moveFeature(featureID, targetGroupID)** at  $t_n$   
Moves the feature with id featureID to the group with ID targetGroupID. The move cannot be done if it introduces a cycle;

that is, if the target group is in the feature's subtree. The feature's subtree is moved along with it. Parent group and child feature mappings are updated accordingly.

- **moveGroup(groupID, targetFeatureID)**  
Moves the group with id groupID to the feature with ID targetFeatureID. Very similar to **moveFeature**.
- **changeFeatureVariationType(featureID, newType)**  
Changes the feature variation type of the feature with ID featureID to newType. If the new type is MANDATORY, the parent group type must be AND.
- **changeGroupVariationType(groupID, newType)**  
Changes the group variation type of the group with ID groupID to newType. If the new type is OR or ALTERNATIVE, make sure that no child feature has type MANDATORY.
- **changeFeatureName(featureID, name)**  
Changes the name of the feature with ID featureID to name. No other feature may have the same name.

TODO: Look at possibilities for changing intervals; extending, restricting, and moving. This would be equivalent to removing/moving operations in the summer project semantics.

## 2.2 Define the scope

What is the scope?

Given a sound plan P and an operation associated with a timepoint O, the scope is the part of P that *may be affected* by adding O. The scope must be defined in two dimensions:

### Time

Which timepoints of the plan may be affected by the change?

### Space

Which parts of the feature model may be affected within the time scope?

## Operation scopes

We define the *minimal* scope for each operation.

- **addFeature**(featureID, parentGroupID, name, featureType) from  $t_n$  to  $t_m$

**TODO: Give an argument why the parent group is the spatial scope of this rule** When we add a feature from  $t_n$  to  $t_m$ , it is quite obvious that the scope in time will be  $[t_n, t_m)$ , since this is the interval in which the feature will exist. The spatial scope must be only the parent group: If the group type changes to a conflicting one, the operation is unsound. If the parent group is removed, we have an orphaned feature, which is also illegal. But what about the name? If we only stored name information inside features, we would have to check every feature in the whole interval for this change. However, since we store information about names in a separate map, we can look up the name and check that it is not in use during the interval.

**TODO: Consider moving last part to data structure definitions**

- **addGroup**(groupID, parentFeatureID, groupType) from  $t_n$  to  $t_m$   
The scopes are very similar in this and the preceding rule. The scope in time is  $[t_n, t_m)$ , and the scope in space is the parent feature, for which the only conflicting event is removal – the types of a group and its parent never conflict.

- **removeFeature**(featureID) at  $t_n$

**TODO: Explain why the temporal scope is the way it is** If the original interval containing  $t_n$  in which the feature exists inside the feature model is  $[t_m, t_k)$ , then the temporal scope is  $[t_n, t_k)$  - from the feature is removed until it would have been removed anyway  
**TODO: rephrase.** Since the feature is removed at  $t_k$  in the original plan, and the original plan is sound as we assume, removing the feature earlier may only affect the plan in the interval between these two time points.

The spatial scope must be the feature's subtree. If the feature has or will have a child group during the interval, then it cannot be removed. Otherwise, there are no conflicts.

- **removeGroup**(groupID) at  $t_n$   
Extremely similar to **removeFeature**.

- **moveFeature**(featureID, targetGroupID) at  $t_n$

If  $t_m$  is the time at which the feature is next moved in the original plan, the temporal scope is  $[t_n, t_m)$ , since this operation only affects the plan within this interval.

The spatial scope is discussed in more detail in the **move feature algo**. This scope is the largest and hardest to define, because we have

to detect cycles. The scope is defined by the feature and its ancestors, as well as target group and its ancestors, which may change during the intervals. It is not necessary to look at all ancestors, only the ones which feature and targetGroup do not have in common. As usual, conflicting types and removal must be considered in addition to cycles.

- **moveGroup**(groupID, targetFeatureID) at  $t_n$   
See moveFeature. Very similar.
- **changeFeatureVariationType**(featureID, newType) at  $t_n$   
Temporal scope:  $[t_n, t_m)$  if  $t_m$  is the next time point at which the feature's type changes or when feature is (next) removed.  
Spatial scope: The only possibly conflicting thing in the feature model is the parent group's type. At no point must the feature have type 'mandatory' and the parent group have type 'alternative' or 'or'. Thus, the spatial scope is the parent group.
- **changeGroupVariationType**(groupID, newType) at  $t_n$  Temporal scope: Same as previous.  
The spatial scope are the group's child features; the possible conflict is the same as with changeFeatureType.
- **changeFeatureName**(featureID, name) at  $t_n$  Temporal scope: Same as previous.  
Spatial scope: The name. If it already exists within the feature model during the interval, then the change is invalid.

**TODO: deal with batch operations/reverting a change:** It is currently impossible to *extend* an interval; If a feature exists during  $[t_3, t_5)$ , it is impossible to change the plan such that it exists during  $[t_3, t_6)$  instead. Don't really know how to fix that, except maybe adding an operation. In Figure 2.2 on page 10, if we try to change the name of feature 1 to Dryer at  $t_2$ , intending to change it back before Dryer is added, then these semantics will reject the first change, as two features will have the name Dryer during  $[t_5, \infty)$ . The paradox would be righted once we add that the name will change back to Washer at  $t_4$ . There are workarounds for this, for instance changing the name of feature 2 to some temporary placeholder, making the changes to feature 1, and then changing feature 2 back. This, however, seems too cumbersome. Hopefully this use case is not common enough that most users will suffer for it, but it is definitely an example of the semantics being too strict.



## 2.3 SOS rules

TODO: Consider having two rules for each operation; one for validating and one for updating. Alternatively use functions on the right-hand side of  $\longrightarrow$ .

TODO: Remember premises = above the line

TODO: Repeat definition of syntax/motivate use of weird constructs

SOS rules TODO: explain what SOS rules are used for

The rules are on the form

(Rule-Label)

$$\frac{\text{Premises}}{S \longrightarrow S'}$$

where  $S$  is the state, and  $S'$  is the new state after the rule is applied. The rule can only be applied if all the premises hold. In this thesis, the state is always on the form **operation**  $\triangleright$  (NAMES, FEATURES, GROUPS), where **operation** denotes the change we intend to make to the temporal feature model (NAMES, FEATURES, GROUPS). The new state is always on the form (NAMES', FEATURES', GROUPS'), where the maps have been updated according to the semantics of the operation. The premises ensure that an operation can only be applied if some conditions hold; for instance the **Add-Feature** rule 2.3 contains premises verifying that the feature does not already exist when we wish to add it.

### 2.3.1 Add feature rule

(Add-Feature)

$$\begin{array}{c} [t_n, t_m) \not\subseteq F_e \quad [t_n, t_m) \in \leq G_e \quad \text{NAMES}[\text{name}][t_n, t_m) = \emptyset \\ \text{FEATURES}[\text{fid}] = (F_e, F_n, F_t, F_p, F_c) \\ \text{GROUPS}[\text{parentGroupID}] = (G_e, G_t, G_p, G_c) \\ \forall \text{gt} \in G_t[t_n, t_m) (\text{compatibleTypes}(\text{gt}, \text{type})) \end{array}$$


---


$$\begin{array}{c} \text{addFeature}(\text{fid}, \text{name}, \text{type}, \text{parentGroupID}) \text{ at } [t_n, t_m) \triangleright \\ (\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\ \longrightarrow \\ (\text{NAMES}[\text{name}][t_n, t_m) \leftarrow \text{fid}, \\ \text{FEATURES}[\text{fid}] \leftarrow \text{setFeatureAttributes}(\text{FEATURES}[\text{fid}], [t_n, t_m), \text{name}, \text{type}, \text{parentGroupID}), \\ \text{GROUPS}[\text{parentGroupID}] \leftarrow \text{addChildFeature}(\text{GROUPS}[\text{parentGroupID}], [t_n, t_m), \text{fid})) \end{array}$$

Figure 2.3

Figure 2.3 describes the semantics of the **addFeature** operation. To add a feature during the interval  $[t_n, t_m)$ , its ID cannot exist during the

```

compatibleTypes(AND, _) = True
compatibleTypes(_, optional) = False
compatibleTypes(_, _) = True

```

Figure 2.4

```

setFeatureAttributes(( $F_e, F_n, F_t, F_p, F_c$ ), [ $t_{start}, t_{end}$ ], name, type
                    , parentGroupID)
= (  $F_e \cup [t_{start}, t_{end}]$ 
    ,  $F_n[t_{start}, t_{end}] \leftarrow \text{name}$ 
    ,  $F_t[t_{start}, t_{end}] \leftarrow \text{type}$ 
    ,  $F_p[t_{start}, t_{end}] \leftarrow \text{parentGroupID}$ 
    ,  $F_c$  )

```

Figure 2.5

interval  $([t_n, t_m] \not\subseteq F_e)$ . The parent feature must exist  $([t_n, t_m] \in_{\leq} G_e)$ , and the types it has during the interval must be compatible with the type of the added feature  $(\forall \text{gt} \in G_t[t_n, t_m] (\text{compatibleTypes}(\text{gt}, \text{type})))$ . The name of the feature must not be in use during the interval  $(\text{NAMES}[\text{name}][t_n, t_m] = \emptyset)$ . Notice that the default value in the FEATURES map lets us treat a failed lookup as a feature, thus allowing us to express the semantics of adding a feature using only one rule.

To make the rule tidier, we use three helper functions: `compatibleTypes` (Figure 2.4), `setFeatureAttributes` (Figure 2.5), and `addChildFeature` (Figure 2.6).

### 2.3.2 Add group rule

The rule in figure 2.7 describes the conditions which must be in place to add a (pre-existing or fresh) group to the FMEP during an interval  $[t_n, t_m]$ . The group must not already exist in the plan during the interval  $[t_n, t_m] \not\subseteq G_e$ , and the parent feature must exist for the duration of the interval  $[t_n, t_m] \in_{\leq} F_e$ . The group ID is added to the parent feature's map of child groups with the interval as key, and the attributes specified are added to the group entry in the GROUPS map.

```

addChildFeature(( $G_e, G_t, G_p, G_c$ ), [ $t_{start}, t_{end}$ ], fid)
= (  $G_e, G_t, G_p, G_c[t_{start}, t_{end}] \stackrel{\cup}{\leftarrow} \text{fid}$  )

```

Figure 2.6

$$\begin{array}{c}
\textbf{(Add-Group)} \\
\frac{
\begin{array}{l}
[t_n, t_m] \notin G_e \quad [t_n, t_m] \in F_e \\
\text{GROUPS}[\text{groupID}] = (G_e, G_t, G_p, G_c) \\
\text{FEATURES}[\text{parentFeatureID}] = (F_e, F_n, F_t, F_p, F_c)
\end{array}
}{
\begin{array}{l}
\text{addGroup}(\text{groupID}, \text{type}, \text{parentFeatureID}) \text{ at } [t_n, t_m] \triangleright \\
(\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
\longrightarrow \\
(\text{NAMES}, \\
\text{FEATURES}[\text{parentFeatureID}] \leftarrow (F_e, F_n, F_t, F_p, F_c \cup \{[t_n, t_m] \mapsto \text{groupID}\}), \\
\text{GROUPS}[\text{groupID}] \leftarrow \text{setGroupAttributes}(\text{GROUPS}[\text{groupID}], \text{type}, \text{parentFeatureID}))
\end{array}
}
\end{array}$$

Figure 2.7

$$\begin{aligned}
& \text{setGroupAttributes}((G_e, G_t, G_p, G_c), [t_{start}, t_{end}], \text{type} \\
& \quad , \text{parentFeatureID}) \\
& = ( G_e \cup [t_{start}, t_{end}) \\
& \quad , G_t[t_{start}, t_{end}) \leftarrow \text{type} \\
& \quad , G_p[t_{start}, t_{end}) \leftarrow \text{parentFeatureID} \\
& \quad , G_c)
\end{aligned}$$

Figure 2.8

$$\begin{aligned}
& \text{addChildGroup}((F_e, F_n, F_t, F_p, F_c), [t_{start}, t_{end}], \text{gid}) \\
& = (F_e, F_n, F_t, F_p, F_c[t_{start}, t_{end}) \overset{\cup}{\leftarrow} \text{gid})
\end{aligned}$$

Figure 2.9

**(Remove-Feature)**

$$\begin{array}{c}
F_e[t_n]_{\leq} = \{[t_{e_1}, t_{e_2}]\} \quad F_c[t_n, t_{e_2}] = \emptyset \\
F_n[t_n, t_{e_2}] = \{\text{name}\} \quad F_t[t_n, t_{e_2}] = \{\text{type}\} \quad F_p[t_n, t_{e_2}] = \{\text{parentGoupID}\} \\
\text{FEATURES}[\text{featureID}] = (F_e, F_n, F_t, F_p, F_c) \\
\text{GROUPS}[\text{parentGroupID}] = (G_e, G_t, G_p, G_c) \\
\hline
\text{removeFeature}(\text{featureID}) \text{ at } t_n \triangleright \\
(\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
\longrightarrow \\
(\text{NAMES}[\text{name}] \leftarrow \text{clampInterval}(\text{NAMES}[\text{name}], t_n), \\
\text{FEATURES}[\text{featureID}] \leftarrow \text{clampFeature}(\text{FEATURES}[\text{featureID}], t_n), \\
\text{GROUPS}[\text{parentGroupID}] \leftarrow \text{removeFeatureAt}(\text{GROUPS}[\text{parentGroupID}], \text{featureID}, t_n))
\end{array}$$

Figure 2.10

### 2.3.3 Remove feature rule

Figure 2.10 shows the semantics of removing a feature with ID `featureID` at time  $t_n$ . We find the time point when the feature was to be removed in the original plan by looking up the interval containing  $t_n$  in the feature's EXISTENCE set  $[t_{e_1}, t_{e_2}]$ . The interval in which the new plan is different from the original is then  $[t_n, t_{e_2}]$ . We verify that the feature does not have any child groups during the affected interval ( $F_c[t_n, t_{e_2}] = \emptyset$ ). We furthermore check that the feature has only a single name, type, and parent during the interval. This means that the original plan did not change the feature's name, type, or parent during this time. If these conditions all hold, we update the temporal feature model by clamping all the relevant intervals to  $t_n$ , i.e. shortening them to end at  $t_n$ .

### 2.3.4 Remove group rule

The **Remove-Group** rule in figure 2.18 describes the semantics of removing a group in a temporal feature model. The temporal scope is identified as the existence interval containing the time point for removal. In that interval, the group may not have any children, and there cannot be plans to change the type or move the group within the interval. We check the latter by looking up the type and parent feature during the interval; if the set contains only one type/parent feature then the type and parent feature do not change.

We use the `clampInterval` (figure 2.11 on the following page), `clampIntervalValue` (figure 2.12 on the next page), and `clampGroup` (figure 2.15 on the following page) helper functions to update the temporal feature model. The `clampInterval` function takes an interval map with non-overlapping keys and a time point  $t_c$ , and updates the interval key

```

clampInterval(MAP,  $t_c$ )
= let  $\{[t_{start}, t_{end}]\} \leftarrow \text{MAP}[t_c]_{\leq}$ 
     $\{v\} \leftarrow \text{MAP}[t_c]$ 
     $\text{MAP}' \leftarrow \text{MAP} \setminus [t_{start}, t_{end})$ 
    in  $\text{MAP}'[t_{start}, t_c) \leftarrow v$ 

```

Figure 2.11

```

clampIntervalValue(MAP,  $t_c, v$ )
= let  $\{[t_{start}, t_{end}]\} \leftarrow \text{MAP}[t_c]_{\leq}^v$ 
     $\text{MAP}' \leftarrow \text{MAP} \setminus^v [t_{start}, t_{end})$ 
    in  $\text{MAP}'[t_{start}, t_c) \xleftarrow{\cup} v$ 

```

Figure 2.12

```

clampSetInterval(IS,  $t_c$ )
= let  $\{[t_{start}, t_{end}]\} \leftarrow \text{IS}[t_c]_{\leq}$ 
     $\text{IS}' \leftarrow \text{IS} \setminus [t_{start}, t_{end})$ 
    in  $\text{IS}' \cup \{[t_{start}, t_c)\}$ 

```

Figure 2.13

```

clampFeature( $((F_e, F_n, F_t, F_p, F_c), t_c)$ )
= (clampSetInterval( $F_e, t_c$ )
  , clampInterval( $F_n, t_c$ )
  , clampInterval( $F_t, t_c$ )
  , clampInterval( $F_p, t_c$ )
  ,  $F_c$ )

```

Figure 2.14

```

clampGroup( $((G_e, G_t, G_p, G_c), t_c)$ )
= (clampSetInterval( $G_e$ )
  , clampInterval( $G_t, t_c$ )
  , clampInterval( $G_p, t_c$ )
  ,  $G_c$ )

```

Figure 2.15

```

removeFeatureAt( $((G_e, G_t, G_p, G_c), \text{featureID}, t_c)$ )
= ( $G_e, G_t, G_p$ 
  , clampIntervalValue( $G_c, t_c, \text{featureID}$ ))

```

Figure 2.16

```

removeGroupAt( $((F_e, F_t, F_p, F_c), \text{groupID}, t_c)$ )
= ( $F_e, F_n, F_t, F_p$ 
  , clampIntervalValue( $F_c, t_c, \text{groupID}$ ))

```

Figure 2.17

containing  $t_c$  to end at  $t_c$ . `clampIntervalValue` does the same, but for interval maps with overlapping keys and set values. It takes an interval map, a time point  $t_c$ , and a value  $v$ , and shortens the interval key containing  $t_c$  and  $v$  to end at  $t_c$ . `clampSetInterval` takes an interval set with non-overlapping values and a time point  $t_c$ , and shortens the interval containing  $t_c$ .

### (Remove-Group)

$$\begin{array}{l}
G_e[t_n]_{\leq} = \{[t_{e_1}, t_{e_2}]\} \quad G_c[t_n, t_{e_2}] = \emptyset \\
G_t[t_n, t_{e_2}] = \{\text{type}\} \quad G_p[t_n, t_{e_2}] = \{\text{parentFeatureID}\} \\
\text{GROUPS}[\text{groupID}] = (G_e, G_t, G_p, G_c) \\
\text{FEATURES}[\text{parentFeatureID}] = (F_e, F_n, F_t, F_p, F_c) \\
\hline
\text{removeGroup}(\text{groupID}) \text{ at } t_n \triangleright \\
(\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
\longrightarrow \\
(\text{NAMES}[\text{name}] \leftarrow \text{clampInterval}(\text{NAMES}[\text{name}], t_n), \\
\text{FEATURES}[\text{parentFeatureID}] \leftarrow \text{removeGroupAt}(\text{FEATURES}[\text{parentFeatureID}], \text{groupID}, t_n), \\
\text{GROUPS}[\text{groupID}] \leftarrow \text{clampGroup}(\text{GROUPS}[\text{groupID}], t_n))
\end{array}$$

Figure 2.18

## 2.3.5 Algorithm for detecting cycles resulting from move operations

Compared with the other operations (e.g. add feature, remove feature, etc.), move feature requires extensive verification. Following is a description of an algorithm intended to ensure that adding a **moveFeature** or **moveGroup** operation results in a sound plan. For simplicity, we abstract away from groups and features and view the combination of the two as nodes.

Let  $n$  be the node to be moved and  $c_1$  the target node, i.e.  $n$ 's new parent node. Furthermore, let  $t_1$  be the time point at which this operation is inserted, and  $t_e$  the time point where  $n$  is moved next or removed, or  $\infty$ . We use the function `ancestors(TFM, node, time)` which takes the temporal feature model, a node and a time point and returns a list of node's ancestors at time point `time`.

First, check whether  $n \in \text{ancestors}(\text{TFM}, c_1, t_1)$ . If this is the case, report that the move causes a cycle and terminate.

Next, find a list of critical nodes. Let  $A_n = \text{ancestors}(\text{TFM}, n, t_1) = [a_1, a_2, \dots, SN, \dots, r]$  and  $A_{c_1} = \text{ancestors}(\text{TFM}, c_1, t_1) = [c_2, c_3, \dots, c_n, SN, \dots, r]$  with  $SN$  the first common ancestor of  $n$  and  $c_1$ . The list of critical nodes

is then  $C = [c_1, c_2, \dots, c_n]$ , which is essentially the list of  $n$ 's new ancestors after the move.

**Repeat this step until the algorithm terminates:**

Look for the first move of one of the critical nodes. If no such moves occur until  $t_e$ , the operation causes no paradoxes, and the algorithm terminates successfully. Suppose there is a 'move' operation scheduled for  $t_k$ , with  $t_1 < t_k < t_e$ , where  $c_i$  is moved to  $k$ . There are two possibilities:

1.  $k$  is in  $n$ 's subtree, which is equivalent to  $n \in \text{ancestors}(TFM, k, t_k)$ . Report that the move caused a cycle and terminate.
2.  $k$  is not in  $n$ 's subtree, so this move is safe. Let  $A_k = \text{ancestors}(TFM, k, t_k) = [k_1, k_2, \dots, k_n, SN', \dots, r]$ , with  $SN'$  the first common element of  $A_k$  and  $A_n$ . Update the list of critical nodes to  $[c_1, \dots, c_i, k_1, \dots, k_n]$ .

```

ancestors((NAMES, FEATURES, GROUPS), featureID, t_n)
= let (F_e, F_n, F_t, F_p, F_c) ← FEATURES [featureID]
    parentGroup ← F_p [t_n]
in
    case parentGroup of
    { parentGroupID } →
        parentGroupID : ancestors((NAMES, FEATURES, GROUPS), parentGroupID, t_n)
    ∅ → []
ancestors((NAMES, FEATURES, GROUPS), groupID, t_n)
= let (G_e, G_t, G_p, G_c) ← GROUPS [groupID]
    { parentFeatureID } ← G_p [t_n]
in
    parentFeatureID : ancestors((NAMES, FEATURES, groups), parentFeatureID, t_n)

```

Figure 2.19

### 2.3.6 Move feature rule

See figure 2.20 on the next page for the semantics of the **moveFeature** operation. The premise  $\neg \text{createsCycle}$  refers to the algorithm described in subsection 2.3.5 on the preceding page. The algorithm is not described as a function here, as it is easier to understand written in natural language. An implementation of it can be found in the **TODO: appendix**.

### 2.3.7 Move group rule

See figure 2.21 on the next page for the semantics of the **moveGroup** operation. The semantics is similar to the one for the **moveFeature** operation, but it differs in that it does not have a check for types. This is because there can only be a conflict between a parent group and a

**(Move-Feature)**

$$\begin{array}{c}
\neg \text{createsCycle} \quad F_p[t_n]_{\leq} = \{[t_{p_1}, t_{p_2}]\} \quad F_p[t_n, t_{p_2}] = \{\text{oldParentID}\} \\
\forall \text{gt} \in G_t[t_n, t_m] (\text{compatibleTypes}(\text{gt}, \text{type})) \\
\text{FEATURES}[\text{featureID}] = (F_e, F_n, F_t, F_p, F_c) \\
\text{GROUPS}[\text{newParentID}] = (G_e, G_t, G_p, G_c) \\
\hline
\text{moveFeature}(\text{featureID}, \text{newParentID}) \text{ at } t_n \triangleright \\
(\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
\longrightarrow \\
(\text{NAMES}, \\
\text{FEATURES}[\text{featureID}] \leftarrow (F_e, F_n, F_t, \text{clampInterval}(F_p, t_n)[t_n, t_{p_2}] \leftarrow \text{newParentID}, F_c), \\
(\text{GROUPS}[\text{newParentID}] \\
\leftarrow \text{addChildFeature}(\text{GROUPS}[\text{newParentID}], [t_n, t_{p_2}], \text{featureID})) [\text{oldParentID}] \\
\leftarrow \text{removeFeatureAt}(\text{GROUPS}[\text{oldParentID}], \text{featureID}, t_n)
\end{array}$$

Figure 2.20

child feature, not a parent feature and a child group. Since only the latter relation changes in this rule, it is not necessary to check that the types are compatible.

**(Move-Group)**

$$\begin{array}{c}
\neg \text{createsCycle} \quad G_p[t_n]_{\leq} = \{[t_{p_1}, t_{p_2}]\} \quad G_p[t_n, t_{p_2}] = \{\text{oldParentID}\} \\
\text{GROUPS}[\text{groupID}] = (G_e, G_t, G_p, G_c) \\
\text{FEATURES}[\text{newParentID}] = (F_e, F_n, F_t, F_p, F_c) \\
\hline
\text{moveGroup}(\text{groupID}, \text{newParentID}) \text{ at } t_n \triangleright \\
(\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
\longrightarrow \\
(\text{NAMES}, \\
(\text{FEATURES}[\text{newParentID}] \\
\leftarrow \text{addChildGroup}(\text{FEATURES}[\text{newParentID}], [t_n, t_{p_2}], \text{groupID})) [\text{oldParentID}] \\
\leftarrow \text{removeGroupAt}(\text{FEATURES}[\text{oldParentID}], \text{groupID}, t_n), \\
\text{GROUPS}[\text{groupID}] \leftarrow (G_e, G_n, G_t, \text{clampInterval}(G_p, t_n)[t_n, t_{p_2}] \leftarrow \text{newParentID}, G_c)
\end{array}$$

Figure 2.21

TODO: This is hard

### 2.3.8 Change feature variation type rule

The rule in figure 2.22 on the following page shows the semantics of changing the feature variation type of the feature with ID featureID at time  $t_n$ . The first expression above the line ( $F_t[t_n]_{\leq} = \{[t_{t_1}, t_{t_2}]\}$ ) identifies



**(Change-Feature-Variation-Type)**

$$\begin{array}{c}
 \text{featureID} \neq \text{rootID} \quad F_t[t_n]_{\leq} = \{[t_1, t_2]\} \\
 \forall [t_{p_1}, t_{p_2}] \in F_p[t_n, t_2]_{\cong} \forall p \in F_p[t_{p_1}, t_{p_2}] \forall t \in \text{getTypes} \left( \text{GROUPS}[p], \langle [t_{p_1}, t_{p_2}] \rangle_{t_n}^{t_2} \right) \cdot (\text{compatibleTypes}(t, \text{type})) \\
 \text{FEATURES}[\text{featureID}] = (F_e, F_n, F_t, F_p, F_c) \\
 \hline
 \text{changeFeatureVariationType}(\text{featureID}, \text{type}) \text{ at } t_n \triangleright \\
 (\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
 \longrightarrow \\
 (\text{NAMES}, \\
 \text{FEATURES}[\text{featureID}] \leftarrow (F_e, F_n, \text{clampInterval}(F_t, t_n)[t_n, t_2] \leftarrow \text{type}, F_p, F_c), \\
 \text{GROUPS})
 \end{array}$$

Figure 2.22

$$\begin{array}{l}
 \text{getTypes}((G_e, G_t, G_p, G_c), [t_n, t_m]) = G_t[t_n, t_m] \\
 \text{getTypes}((F_e, F_n, F_t, F_p, F_c), [t_n, t_m]) = G_t[t_n, t_m]
 \end{array}$$

Figure 2.23

the upper bound of the temporal scope,  $t_2$ . This is when the feature type was originally planned to change. The next line may be hard to read, but its intent is easier to understand. It checks that all the types a parent group has *while it is the parent of the feature* has a type which is compatible with the new type of the feature. If everything above the line is true, then the FEATURES map is updated at featureID by shortening the interval key for the original type at  $t_n$ , and assigning the new type to the affected interval  $[t_n, t_2]$ .

TODO: make it more readable

### 2.3.9 Change group variation type rule

The rule in figure 2.24 on the next page is similar to the **changeFeatureVariationType** rule in figure 2.22, and shows the semantics of changing the type of a group. In a similar way to the aforementioned **changeFeatureVariationType** rule, it verifies that the types of all the child groups during the affected interval are compatible with the new group type.

### 2.3.10 Change feature name

The semantics of changing the name of a feature are shown in the **Change-Feature-Name** rule in figure 2.25 on page 25. The old name and the next planned name change are identified on the first line ( $F_n[t_n] = \{\text{oldName}\}$  and  $F_n[t_n]_{\leq} = \{[t_{n_1}, t_{n_2}]\}$  respectively). Since the name must not be in

**(Change-Group-Variation-Type)**

$$\begin{array}{c}
G_t[t_n]_{\leq} = \{[t_{t_1}, t_{t_2})\} \\
\\
\forall [t_{c_1}, t_{c_2}) \in G_c[t_n, t_{t_2})_{\cong} \\
\forall c \in \bigcup G_c[t_{c_1}, t_{c_2}) \\
\forall t \in \text{getTypes}\left(\text{FEATURES}[c], \langle [t_{c_1}, t_{c_2}) \rangle_{t_n}^{t_{t_2}}\right) \\
\quad (\text{compatibleTypes}(\text{type}, t)) \\
\\
\hline
\text{GROUPS}[\text{groupID}] = (G_e, G_t, G_p, G_c) \\
\\
\text{changeGroupVariationType}(\text{groupID}, \text{type}) \text{ at } t_n \triangleright \\
\quad (\text{NAMES}, \text{FEATURES}, \text{GROUPS}) \\
\quad \longrightarrow \\
\quad (\text{NAMES}, \text{FEATURES}, \\
\text{GROUPS}[\text{groupID}] \leftarrow (G_e, \text{clampInterval}(G_t, t_n)[t_n, t_{t_2}) \leftarrow \text{type}, G_p, G_c))
\end{array}$$

Figure 2.24

use during the temporal scope, we verify that looking up the new name in the NAMES map returns an empty set. The NAMES map is updated by shortening the interval for the old name to end at  $t_n$ , and assigning the feature ID to the new name during the temporal scope. Furthermore, the FEATURES map is updated at the feature ID, shortening the interval for the old name and assigning the new name to the temporal scope.

**(Change-Feature-Name)**

$$\begin{array}{l}
 F_n[t_n] = \{\text{oldName}\} \quad F_n[t_n]_{\leq} = \{[t_{n_1}, t_{n_2})\} \\
 \text{NAMES}[\text{name}][t_n, t_{n_2}) = \emptyset \\
 \text{FEATURES}[\text{featureID}] = (F_e, F_n, F_t, F_p, F_c)
 \end{array}$$


---

**changeFeatureName**(featureID, name) at  $t_n \triangleright$   
 (NAMES, FEATURES, GROUPS)

$$\begin{array}{l}
 \longrightarrow \\
 ((\text{NAMES}[\text{name}][t_n, t_{n_2}) \leftarrow \text{featureID}][\text{oldName}] \leftarrow \text{clampInterval}(\text{NAMES}[\text{oldName}], t_n), \\
 \text{FEATURES}[\text{featureID}] \leftarrow (F_e, \text{clampInterval}(F_n, t_n)[t_n, t_{n_2}) \leftarrow \text{name}, F_t, F_p, F_c), \\
 \text{GROUPS})
 \end{array}$$

Figure 2.25

# Chapter 3

## Soundness

TODO: and completeness? The operations in themselves are not complete, in the sense that there is not a one-to-one correspondence between the operations defined on temporal feature models (temporal operations) and the operations defined on feature models (model operations). However, the temporal operations are more restricted than the model operations, and any valid change within that subset to an evolution plan would be accepted by the rules. Should I try to prove completeness as well?

TODO: Root feature requirements

### 3.1 Soundness for temporal feature models

The temporal feature model can be viewed as a sequence of feature models associated with time points. A feature model has strict structural requirements, and the definition of a paradox is a feature model that violates these requirements. In this context, soundness means that if a rule accepts a modification, realising the modified plan results in a sequence of feature models where each is structurally sound. The soundness analysis in this chapter assumes that the original plan is sound; i.e. all resulting feature models fulfil the structural requirements.

According to Motzfeldt et al. 2020, the structural requirements (well-formedness rules) are

**WF1** A feature model has exactly one root feature.

**WF2** The root feature must be mandatory.

**WF3** Each feature has exactly one unique name, variation type and (potentially empty) collection of subgroups.

**WF4** Features are organized in groups that have exactly one variation type.

**WF5** Each feature, except for the root feature, must be part of exactly one group.

**WF6** Each group must have exactly one parent feature.

**WF7** Groups with types `ALTERNATIVE` or `OR` must not contain `MANDATORY` features.

**WF8** Groups with types `ALTERNATIVE` or `OR` must contain at least two child features.

One of these requirements is not upheld in this thesis, namely **WF8**. This is because it would cause unnecessary clutter in the rules, although it could be verified quite easily in an actual implementation.

**TODO:** This may not be a good idea, since the reasoning for scope blends with the reasoning for the other checks. Maybe divide into *validate* and *apply*, like in the implementation? The proof for soundness includes two parts:

- (i) proving that the temporal and spatial scopes are correct, and
- (ii) that the checks within those scopes are sufficient for soundness.

For each rule, the proofs are divided into these two parts.

### 3.1.1 Soundness for the Add feature rule

See figure 2.3 on page 15 for the **Add-Feature** rule. Let

**addFeature**(fid, name, type, parentGroupID) at  $[t_n, t_m) \triangleright (\text{NAMES}, \text{FEATURES}, \text{GROUPS})$

be the initial state. Recall that this operation adds the feature with ID fid to the temporal feature model  $(\text{NAMES}, \text{FEATURES}, \text{GROUPS})$  from  $t_n$  to  $t_m$ .

We argue that the temporal scope is  $[t_n, t_m)$ , since this is the only interval in which the temporal feature model is affected by the change. In other words, if we look at the temporal feature model as a sequence of feature models, the only models that may break as a result of this modifications, are the ones associated with time points between  $t_n$  and (but not including)  $t_m$ .

The well-formedness rules must hold for each feature model in the sequence; that is, for any time point  $t_k$  within the scope, the feature model at  $t_k$  must uphold all the rules.

Since we give a parent group in the operation, the new feature cannot be a root feature, so **WF1** is not violated. It is also obvious that the root feature does not change its type in this rule, so **WF2** is upheld.

However, **WF3** must be looked at more closely for this rule. Since we check that no other feature has the name name during the temporal scope, the name is unique for each affected time point. The variation type is given in the operation, and a newly added feature does not have child groups. Thus, **WF3** is upheld. Since the rule does not change the type of a group, **WF4** is not affected. As for **WF5**, since the ID of the parent group (parentGroupID) is also specified in the operation, the feature is part of exactly one group. **TODO: WF6!!!**

# Chapter 4

## Application

Say something about implementation without showing the code, maybe giving pseudocode. Talk about distance between formalization and implementation. Describe examples, error messages, practical applications, how it can be used, how it detects paradoxes, how warnings can be given to users.

# Chapter 5

## Implementation

TODO: Move to appendix

# **Part III**

## **Conclusion**



How I have addressed the questions, and how I have *not* addressed the questions. Based on the assumption etc. Pinpoint other work that can be done to address the questions I don't tackle. Another master thesis can focus on presenting the input and output to the user

# Bibliography

Motzfeldt, Ida Sandberg et al. (2020). “Consistency-preserving evolution planning on feature models”. In: *SPLC '20: 24th ACM International Systems and Software Product Line Conference, Montreal, Quebec, Canada, October 19-23, 2020, Volume A*. Ed. by Roberto Erick Lopez-Herrejon. ACM, 8:1–8:12. DOI: 10 . 1145/3382025 . 3414964. URL: <https://doi.org/10.1145/3382025.3414964>.