

Assume indexes range from 1 to n

$$A = (a_1, a_2, \dots, a_n)$$

$$\forall a (a \in A \rightarrow a \in \mathbb{Z}_+)$$

$$(1) \text{ leaders} = \{a_i \mid a_i \in A ; (\forall j (i < j \rightarrow a_j < a_i) \text{ or } i = n)\}$$

$$(2) (1) \rightarrow a_i = \max(A[i, i + 1, \dots, n])$$

From (1) it's logical to start iterate A from index n to index 1

The initial value of max is $A[n]$.

At each iteration we compare the current element to max .

If we changed max then the current element will be added to $leaders$

$Leaders(A[n])$

1. initialize List $leaders = \emptyset$

2. do: $max \leftarrow A[n]$; $leaders.addToHead(max)$

3. for $i \leftarrow n - 1$ downto 1 do:

3.1. if $max < A[i]$ then do:

$$max \leftarrow A[i]$$

$$leaders.addToHead(max)$$

Correctness:

(*) Loop Invariant:

$$\forall 1 \leq k \leq n$$

Before the k' th iteration $max = \max(A[n - k + 1, n - k + 2, \dots, n])$

Base case:

$$((1) + \text{line } 2) \rightarrow \text{before the first iteration } max = A[n - 1 + 1] = A[n]$$

Let $1 < k \leq n$ assume (*) for k , therefore, before the k' th iteration

$$max = \max(A[n - k + 1, n - k + 2, \dots, n])$$

Observe the k' th iteration:

We compare $A[n - k]$ to max and update max if needed.

In any case we get that after the k' th iteration (before iteration $k + 1$)

$$max = \max(A[n - k, n - k + 1, \dots, n]) = \max(A[n - (k + 1) + 1, n - (k + 1) + 2, \dots, n])$$

As required.

Now, it's clear that if at some iteration we changed max then this element should be added to $leaders$ (at (3.1))