

Let $(a_n)_{n \in \mathbb{N}}$ be a sequence of integers

Let $P = \max(\{a_i \cdot a_j \cdot a_k \mid a_i, a_j, a_k \in (a_n) : i < j < k\})$

Let $a_{i_1}, a_{i_2}, a_{i_3}$ be the three largest integers s.t
(+) $a_{i_1} \leq a_{i_2} \leq a_{i_3}$

if $0 \leq a_{i_1}$ then the only option for P is
 $\{a_{i_1}, a_{i_2}, a_{i_3}\}$ or $\{a_{s_1}, a_{s_2}, a_{i_3}\}$ s.t $a_{s_1} \leq a_{s_2}$ (**) are the two smallest integers in (a_n) and $a_{s_2} < 0$

because if $a_{i_1} \cdot a_{i_2} < a_{s_1} \cdot a_{s_2} = |a_{s_1}| \cdot |a_{s_2}|$ then
 $a_{i_1} \cdot a_{i_2} \cdot a_{i_3} < a_{s_1} \cdot a_{s_2} \cdot a_{i_3}$

if $a_{i_3} \leq 0$ then $P \leq 0$ so the only option for P
see (*)

is $\{a_{i_1}, a_{i_2}, a_{i_3}\}$

if $0 < a_{i_3}$ and ($a_{i_1} \leq 0$ or $a_{i_2} \leq 0$) then,

if $0 < a_{i_2}$ then

From (**) we get $0 < a_{s_1} \cdot a_{s_2}$, so $\prod_{i=1}^3 a_{i_1} < 0$ (Δ)

if $a_{s_2} \leq 0$ then again $0 \leq a_{s_1} \cdot a_{s_2}$ and we get
(Δ)

There are no more options for P , from here we need only
to implement the code according to the cases above.