

Iterative solution:

minPayment($X, C[n]$)

/* Assume C is given as an array
each index $0 \leq i \leq n$
represent an amount of
payment x */

2. initialize $A[n+1]$
3. do $A[0] \leftarrow 0$,
4. for amount $\leftarrow 1$ to x
5. do $\min \leftarrow x+1$
6. for coinIndex $\leftarrow 0$ to n do

$j \leftarrow \text{amount} - C[\text{coinIndex}]$

if $0 \leq j$ and $A[j] < \min$ then do

$\min \leftarrow A[j]$

7. do $A[\text{amount}] \leftarrow 1 + \min$
same meaning as in f

8. if $A[x] = x+1$ then print "we can't pay an amount of x with any number of coins given the coins in $C[n]$ " /* should return NIL, but I chose to write this to make the meaning of " $A[x] = x+1$ " clearer */
9. else return $A[\text{amount}]$

Notice that after we have calculated $A[i]$ for some i then we don't need to calculate $A[p]$ again, for any $p \leq i$

Time complexity =
Space complexity = $O(X)$

$O(n \cdot X)$