

$$Y = \beta_0 + \beta_1 \cdot X_1 + \frac{1}{2} \cdot X_1 + \beta_2 \cdot X_2 + 1$$

$$\text{var}(X) + \text{var}(Y) = \text{var}(X) + \text{var}(Y) - 2 \cdot \text{cov}(X, Y) \quad \text{var}(Y) = 2P$$

$$H_0 = \beta_1 - 3\beta_2 = 0$$

$$\text{var}(\beta_1 - 3\beta_2) = \text{var}(\beta_1) - \text{var}(3\beta_2) - 6 \cdot \text{cov}(\beta_1, \beta_2) = \text{var}(\hat{\beta}_1) - 9 \cdot \text{var}(\hat{\beta}_2) - 6 \cdot \text{cov}(\hat{\beta}_1, \hat{\beta}_2)$$

$$SE(\hat{\beta}_1 - 3\hat{\beta}_2) = \sqrt{\text{var}(\hat{\beta}_1) - 9 \text{var}(\hat{\beta}_2) - 6 \text{cov}(\hat{\beta}_1, \hat{\beta}_2)}$$

$$t = \frac{\beta_1 - 3\beta_2 - 0}{\sqrt{\text{var}(\hat{\beta}_1) - 9 \text{var}(\hat{\beta}_2) - 6 \text{cov}(\hat{\beta}_1, \hat{\beta}_2)}}$$

$$\theta_1 = \beta_1 - 3\beta_2, \quad \theta_1 = \beta_1 - 3\beta_2$$

$$\beta_1 = \theta_1 + 3\beta_2$$

$$Y = \beta_0 + \beta_1 \cdot X_1 + \beta_2 \cdot X_2 + \beta_3 \cdot X_3 + U$$

$$Y = \beta_0 + (\theta_1 + 3\beta_2) \cdot X_1 + \beta_2 \cdot X_2 + \beta_3 \cdot X_3 + U$$

$$Y = \beta_0 + \theta_1 \cdot X_1 + \beta_2 (3X_1 + X_2) + \beta_3 \cdot X_3 + U$$

معادله اول
معادله دوم
معادله سوم