

List of some common linear data structures along with their average time complexities for insert, remove, and search operations:

1. **Arrays:**
 - Insert: $O(1)$
 - Remove: $O(1)$
 - Search: $O(n)$
2. **Hash Tables:**
 - Insert: $O(1)$ [On average, assuming a good hash function and proper handling of collisions]
 - Remove: $O(1)$ [On average]
 - Search: $O(1)$ [On average]
3. **Bit Array (Bitset):**
 - Insert: N/A [using masks]
 - Remove: N/A [using masks]
 - Search: $O(1)$ [using masks]
4. **Stacks:**
 - Using Array:
 - Insert (Push): $O(1)$
 - Remove (Pop): $O(1)$
 - Search: $O(n)$ [If you want to find an element other than the top]
 - Using Linked List:
 - Insert (Push): $O(1)$
 - Remove (Pop): $O(1)$
 - Search: $O(n)$ [If you want to find an element other than the top]
5. **Vectors (Dynamic Arrays):**
 - Insert at End: $O(1)$ [Amortized constant time]
 - Insert at Middle/Beginning: $O(n)$
 - Remove at End: $O(1)$ [Amortized constant time]
 - Remove at Middle/Beginning: $O(n)$
 - Search: $O(n)$
6. **Circular Buffer (Circular Queue):**
 - Insert (Enqueue): $O(1)$
 - Remove (Dequeue): $O(1)$
 - Search: $O(n)$ [In worst case]
7. **Linked Lists:**
 - 7.a Singly Linked List:
 - Insert / Remove at End: $O(1)$ [if dummy node is available]
 - Insert / Remove at Beginning: $O(n)$ [If no dummy, and no amortized update of head during inser & remove operations]
 - Search: $O(n)$
 - 7.b Doubly Linked List: [2 constant dummy nodes are available as strucs fields]
 - Insert at Beginning: $O(1)$
 - Insert at End: $O(1)$
 - Remove at Beginning: $O(1)$
 - Remove at End: $O(1)$
 - Search: $O(n)$
8. **Sorted List:**
 - Insert: $O(\log n)$ [On average, for self-balancing trees like AVL or Red-Black

Trees]

- Remove: $O(\log n)$ [On average]
- Search: $O(\log n)$ [On average]

9. ****Queues:****

- Using Array:
 - Insert (Enqueue): $O(1)$
 - Remove (Dequeue): $O(1)$
 - Search: $O(n)$
- Using Linked List:
 - Insert (Enqueue): $O(1)$
 - Remove (Dequeue): $O(1)$
 - Search: $O(n)$

The best time complexity for a search operation is $O(1)$, which means constant time complexity. This indicates that the time taken for the search operation does not depend on the size of the input data.

Data structures that achieve $O(1)$ search time complexity are those that provide direct access to the desired element without requiring any significant computation or traversal. Some examples include:

1. ****Hash Tables:**** When using a well-designed hash function, hash tables provide constant-time average case lookup, insertion, and deletion.
2. ****Direct Address Tables:**** When the range of possible keys is limited, direct address tables can achieve $O(1)$ search by directly indexing into an array.
3. ****Bit Arrays (Bitsets):**** Bit arrays allow for constant-time access to individual bits, which is equivalent to looking up the presence of an element.

It's important to note that while these data structures can provide constant-time search in the average case, real-world performance might vary based on factors such as hash collisions, memory layout, and the quality of the hash function. Additionally, these structures might have higher time complexities in worst-case scenarios or when certain conditions are not met.