

Here be Dragons: A Security Analysis of WPA3's SAE Handshake

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ABSTRACT

In this paper, we investigate the security of WPA3. Its goal is to secure Wi-Fi networks, and compared with WPA2, its two main advantages are that it protects against dictionary attacks, and that it provides forward secrecy. Unfortunately, we show that WPA3 is affected by several design and implementation flaws. We analyze these flaws both theoretically and practically. Most prominently, we show that WPA3's SAE handshake, commonly known as Dragonfly, is affected by password partitioning attacks. These allow an adversary to recover the password by abusing side-channel leaks (both timing and cache-based ones). Our novel side channel attacks target the protocol's password encoding method, for example SAE's Hash to Curve algorithm. Due to the current standardization work surrounding Hash to Curve variants, these results are also of independent interest. Finally, we discuss how to mitigate most attacks in a backwards-compatible way.

ACM Reference Format:

Anonymous Author(s). 2018. Here be Dragons: A Security Analysis of WPA3's SAE Handshake. In *Woodstock '18: ACM Symposium on Neural Gaze Detection*, June 03–05, 2018, Woodstock, NY. ACM, New York, NY, USA, 15 pages. <https://doi.org/10.1145/1122445.1122456>

1 INTRODUCTION

After the discovery of key reinstallation attacks (KRACKs) against WPA2, the Wi-Fi Alliance created the WPA3 certification without public review [79, 80]. This means experts could not critique WPA3's (admittedly few) new features before it was released. Moreover, although the new handshake of WPA3 was designed in a more open manner, its security guarantees are unclear. On one hand there is a security proof of a close variant of WPA3's handshake [55], but on the other hand another close variant received significant criticism during its standardization [64, 74]. These issues raise the question whether WPA3 is secure in practice.

We do remark that WPA3 does not define new protocols, but instead mandates which existing protocols a device must support. This means WPA3 is not a specification, but a certification. Put differently, devices can now become WPA3-certified, which assures they implement certain protocols in an interoperable manner. The only novelty in the WPA3 certification is a transition mode where WPA2 and WPA3 are simultaneously supported for backward compatibility (see Section 2.2). Although WPA3 follows recommended practice by using existing standards, we believe more openness to alternative protocols would have increased its security.

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Woodstock '18, June 03–05, 2018, Woodstock, NY

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ACM ISBN 978-1-4503-9999-9/18/06...\$15.00

<https://doi.org/10.1145/1122445.1122456>

In this paper we perform a security analysis of WPA3's Simultaneous Authentication of Equals (SAE) handshake. This handshake is designed to prevent dictionary attacks, and constitutes the biggest improvement over the WPA2 certification. We systematically analyzed its security by reading specifications, inspecting formal proofs, and auditing open-source implementations. This analysis revealed several design and implementation flaws. For instance, inspired by the assumptions in a formal proof of the SAE handshake by Lancrenon and Skrobot [55], we inspected whether the employed password encoding methods are in fact secure. Unfortunately, this revealed both a timing and cache-based side-channel vulnerability. We empirically confirmed all our findings against both open source and recently-released proprietary implementations of WPA3. All combined, our work resulted in the following contributions:

- We provide a self-contained and high-level description of WPA3 and its SAE handshake (Section 2 and 3).
- We show that in the context of broadcast networks, the anti-clogging mechanisms of SAE is unable to prevent denial-of-service attacks (Section 4). In particular, we show that a small resource-constrained device can overload the CPU of professional Access Points (APs).
- We present a dictionary attack against WPA3 when it is configured to operate in transition mode (Section 5). This is accomplished by trying to downgrade clients to WPA2. Although WPA2's 4-way handshake detects the downgrade and aborts the connection attempt, the frames sent during the partial 4-way handshake provide enough information for a dictionary attack. We also discuss a downgrade attack against the SAE handshake.
- We empirically investigate the feasibility of timing attacks against WPA3's SAE handshake (Section 6). This confirms timing attacks are possible and leak info about the password.
- We demonstrate a novel micro-architectural cache-based side-channel attacks against the SAE handshake (Section 7). This attack leaks information about the password being used. Our attack even works against Hash to Curve algorithm implementations that include countermeasures against side-channel attacks. We believe this type of attack against Hash to Curve algorithms is of independent interest in light of current standardization efforts [68].
- We explain how the recovered timing and cache info can be used to perform an offline password partitioning attack (Section 8). This enables an adversary to recover the password used by the target.

Finally, we will discuss related work in Section 9, and we give concluding remarks in Section 10.

1.1 Responsible Disclosure

We are currently in the process of contacting the Wi-Fi Alliance to disclose our vulnerabilities in a coordinated manner, and hope that

our work will influence the deployment of WPA3 before it becomes widely spread and hard to patch.

2 BACKGROUND

In this section we introduce the (relatively few) new features that are defined in the WPA3 certification [81], and we explain relevant aspects of the 802.11 standard [41].

2.1 An Overview of WPA3

The WPA3 certification was created with two types of networks in mind. The first one is a home network, where users authenticate using a pre-shared password. The second one is an enterprise network, where more advanced authentication methods can be used (e.g. certificates, smart cards, and so on). To differentiate both types, the term WPA3-SAE is used for home networks, and the term WPA3-Enterprise is used for enterprise networks.

The WPA3-Enterprise mode uses existing handshakes, but now requires that ciphers used during authentication provide at least 192 bits of security. That is, the permitted ciphersuites use 384-bit curves for elliptic curve cryptography, and use at least 3072-bit moduli when using RSA or DHE. There are no requirements on the length of session keys or hash functions that are used after authentication, so these can still be of a lower size such as 128-bit.

The WPA3-SAE mode for home networks is more interesting. It mandates support for the existing Simultaneous Authentication of Equals (SAE) handshake. This handshake is a Password Authenticated Key Exchange (PAKE), meaning authentication is performed based on a password. The SAE handshake provides forward secrecy and resistance against offline dictionary attacks, and was already part of the 802.11 standard in 2011 [43]. Several variants of this handshake are also used in other protocols (see Section 3.1). The output of WPA3's SAE handshake is a Pairwise Master Key (PMK), which is subsequently used to perform a 4-way handshake to derive a Pairwise Transient Key (PTK) (see Figure 1). Note that, even though WPA3 still uses WPA2's 4-way handshake, it is not vulnerable to dictionary attacks. This is because the PMK generated by the SAE handshake has much higher entropy than the password itself.

In both operation modes, the client and AP must use Management Frame Protection (MFP). Most notably, MFP prevents deauthentication attacks where an adversary forcibly disconnects victims from the network.

2.2 WPA3-SAE Transition Mode

Unfortunately, not all devices will be updated to support the SAE handshake. To accommodate these devices, the WPA3 certification defines how an Access Point (AP) can simultaneously support WPA2's 4-way handshake and WPA3's SAE handshake in a secure manner. In this transition mode, the AP advertises that MFP is optional, and that it supports both the 4-way and SAE handshake. Older WPA2 clients can then connect using the 4-way handshake without MFP, while new WPA3 clients can connect using SAE with MFP enabled. The only requirement placed on WPA3 clients is that they must use MFP when connecting to a WPA3-capable AP, even if the AP is operating in transition mode.

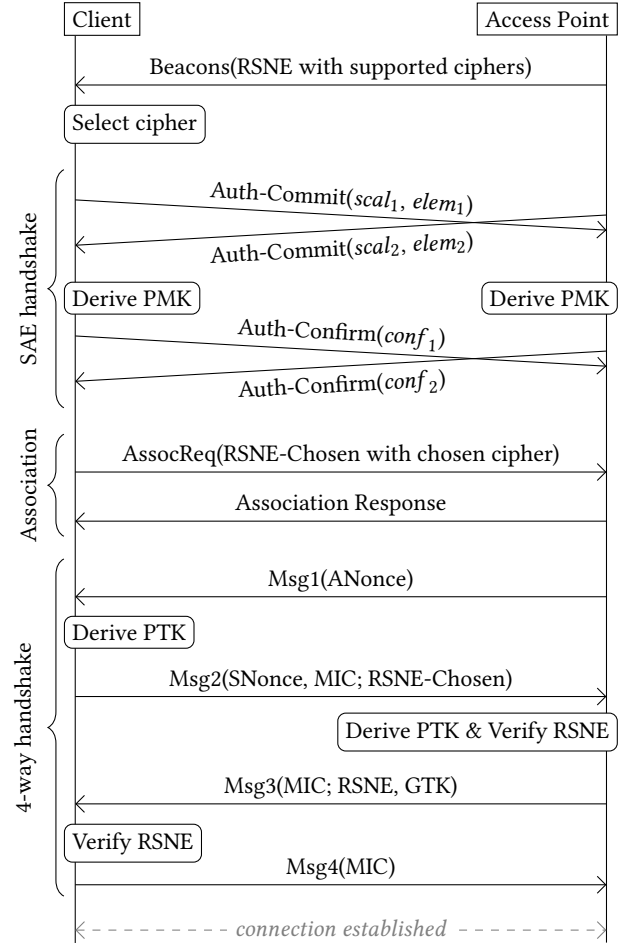


Figure 1: Connecting to an AP using WPA3. First the SAE handshake negotiates the master key (PMK), and then the 4-way handshake derives a session key (PTK). To support mesh networks, the SAE handshake was made so both parties can initiate it in parallel (hence the crossed arrows).

2.3 Downgrade Protection

An AP advertises its supported cipher suites, i.e., authentication and encryption algorithms, in the Robust Security Network Element (RSNE). The RSNE is included without authentication in beacons, and in turn beacons are transmitted periodically to advertise the presence of a network. Example authentication algorithms are the 4-way handshake, the 802.1X protocol, the SAE handshake, etc. Examples for the encryption algorithm are GCMP or (AES-)CCMP. Because the RSNE is not authenticated in beacons, an adversary can spoof this element in beacons. To detect this, WPA2's 4-way handshake cryptographically verifies the previously received RSNE. Since the 4-way handshake is always executed at some point when a station (i.e. a client or AP) connects for the first time to a network, this assures the RSNE is always verified. In particular, when the AP receives message 2 from the client, the AP verifies that the RSNE in the client's association request was not altered (see Figure 1). Similarly, when the client receives message 3 from the AP, the

client verifies that the RSNE that was advertised in beacons was genuine. In case a mismatch is detected, the handshake is aborted. This prevents an adversary from spoofing the RSNE, and thereby tricking the client into connecting using a weak cipher suite.

3 THE SAE “DRAGONFLY” HANDSHAKE

In this section we introduce WPA3's Simultaneous Authentication of Equals (SAE) handshake, and discuss the protections that were assumed to prevent downgrades from WPA3 to WPA2.

3.1 Background and History

The WPA3 certification mandates support for the SAE handshake. This handshake is based on the work of Harkins [30], and was added to the 802.11 standard in 2011 [43]. Several close variants of the SAE handshake are also used in other protocols. Commonly, the term Dragonfly is used to refer to these types of handshakes.

The SAE handshake is a balanced Password Authenticated Key Exchange (PAKE). It takes as input a pre-shared secret, and outputs a high-entropy Pairwise Master Key (PMK). Because it is balanced PAKE, both endpoints must store the pre-shared secret in plaintext. After performing the SAE handshake, the 4-way handshake is used to negotiate a session key called the PTK (recall Figure 1). Finally, the SAE handshake explicitly supports mesh networks, by allowing both endpoints to start the handshake in parallel.

3.2 Protocol Details

The SAE handshake supports both Finite Field Cryptography (FFC) using multiplicative groups modulo a prime (MODP groups), and it supports Elliptic Curve Cryptography (ECC) using elliptic curve groups modulo a prime (ECP groups). Unless otherwise mentioned, we will assume elliptic curves are used. This is a natural assumption, because all implementations of SAE (and therefore WPA3) must support elliptic curves [41, §12.4.4.1]. In particular, the 802.11 standard mandates that if a station advertises support for SAE, it must implement the NIST P-256 curve [1, 40]. Support for other groups is optional, meaning there is no mandated support for MODP groups.

When describing elliptic curve operations, we use lowercase letters to denote scalars (i.e. integers), and uppercase letters to denote elliptic curve points. With SAE, all elliptic curves are defined over the equation $y^2 = x^3 + ax + b \mod p$ where p is a prime and the values a , b , and p depend on the specific curve being used. We use q to denote the prime order of G , where G is the generator of the group. When executing the SAE handshake, the user-readable password is converted into a group element. For MODP groups this is done using a Hash to Group method, and for elliptic curves using a Hash to Curve method. The resulting password element is denoted by P , and its generation is described in detail in Section 3.3.

The handshake itself consists of two phases: the commit and confirm phase. These two phases are illustrated in Figure 2, along with the accompanying elliptic curve operations. Note that the handshake can be initiated in parallel by both participants (which may happen in mesh networks after connection loss). Nevertheless, in the more widely-used infrastructure mode, the client will initiate the handshake by sending the first Commit frame, and subsequently the AP will reply using a Commit and Confirm frame. In turn the client sends its Confirm frame, completing the handshake.

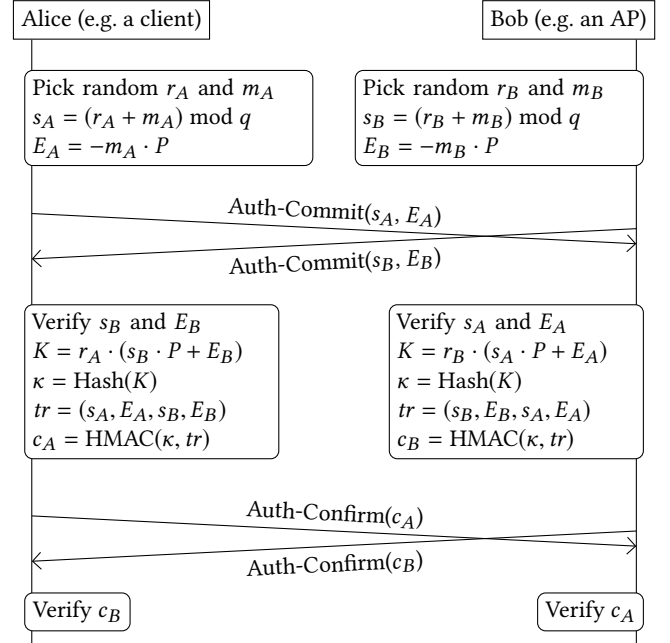


Figure 2: Details of the SAE handshake. Recall that it supports mesh networks where two stations may simultaneously initiate the handshake (hence the crossed arrows). We assume elliptic curves are used, since all implementations of SAE (and hence also WPA3) are required to support it.

In the commit phase, each participant first picks a random number $r_i \in [2, q]$ and a random mask $m_i \in [2, q]$ (see Figure 1). They then sum these numbers to obtain the public scalar $s_i \in \mathbb{Z}_q$, and they calculate the public group element $E_i = -m_i \cdot P$. Now they send both the scalar s_i and the group element E_i to the other participant using a Commit frame. On reception of these values, each participant verifies that the received scalar s_i is within the range $[1, q]$, and that the received group element E_i is a valid point on the curve being used [41, §12.4.5.4]. If one of these checks fails, the handshake is aborted. Note that SAE also provides forward secrecy, and this property relies on the difficulty of deriving m_i given P and E_i , i.e., it relies on the hardness of the elliptic curve discrete logarithm problem.

During the confirm phase, each participant calculates the shared secret point K (see Figure 2). This point is processed using a hash function to derive κ . Finally, a HMAC over the handshake transaction summary tr is calculated using the key κ . The result of this hash, denoted by c_i , is sent to the other participant in a Confirm frame. On reception of c_i , the receiver verifies its value. If it equals the expected value, the handshake succeeds, and the negotiated key κ becomes the Pairwise Master Key (PMK). Otherwise the Confirm frame is ignored, and the handshake eventually times out.

For details on how the SAE handshake negotiates which cryptographic group is used, we refer to Section 5.2. The handshake also has a mechanism to prevent denial-of-service (DoS) attacks. However, this mechanism is flawed (see Section 4).

Listing 1: Converting the pre-shared password into an elliptic curve point in Python-like pseudocode [41, §12.4.4.2.2].

```

1 def password_to_element_ecc(password, MAC1, MAC2, k=40):
2     found = False
3     counter = 0
4     base = password
5     while counter < k or not found:
6         counter += 1
7         seed = Hash(MAC1, MAC2, base, counter)
8         value = KDF(seed, "SAE Hunting and Pecking", p)
9         if value >= p: continue
10
11         if is_quadratic_residue(value^3 + a * value + b, p):
12             if not found:
13                 x = value
14                 save = seed
15                 found = True
16                 base = random()
17
18     y = sqrt(x^3 + a * x + b) mod p
19     if LSB(save) == LSB(y):
20         P = (x, y)
21     else:
22         P = (x, p - y)
23     return P

```

3.3 Password Derivation

When constructing the Commit frame, the pre-shared password must first be converted into a group element (e.g. into a point on the elliptic curve). The algorithm used to do this for elliptic curves is shown in Listing 1. Summarized, it first hashes the password, together with a counter and the MAC addresses of both stations, and uses the output of the hash as the x -coordinate of the curve point. It then tries to find a solution for y over the equation $y^2 = x^3 + ax + b \bmod p$. In case a solution is found, the point (x, y) becomes the password element P . If no solution is found, the counter is increased, and another attempt is made to find a solution for y using the new value for x . Finally, to mitigate timing attacks, the main loop is always executed k times, no matter when a solution for y is found. In the extra iterations, calculations are not based on the real password, but on a randomly generated one.

Interestingly, this algorithm underwent various changes throughout the years. All these changes attempt to mitigate timing attacks. In particular, the original 802.11s amendment that introduced the SAE handshake did not include the additional iterations [43, §8.2a.4.2.2]. Put differently, originally the algorithm would immediately stop once a solution for y had been found. An amendment proposed in 2011 added the extra iterations to mitigate timing attacks [31], and this amendment was incorporated into the 2012 version of the 802.11 standard [42, §11.3.4.2.2].

Unfortunately, sensitive information can also be leaked in the function on line 11 that tries to find a solution for y . In particular, the execution time of this function depends on whether or not there is a solution. To prevent timing attacks against this function, an amendment proposed in 2014 mitigated this attack by recommending the use of quadratic residue blinding [33]. This amendment got incorporated into the 2016 version of the 802.11 standard [41, §12.4.4.2.2]. We strongly recommend that developers implement these additional side-channel countermeasures.

We also note that the size of the counter value is only 1 byte. Although one might worry this variable could overflow, this is

near impossible in practice. The probability of finding a solution for y is approximately 50%, meaning there is only a 2^{-256} chance of executing more than 256 iterations. Even an adversary who can forge 2^{63} unicast MAC addresses in an attempt to cause an overflow, only has a chance of 2^{-193} of triggering an overflow and hence causing an infinite loop.

Another critical remark is that the 802.11 standard does not specify a minimum value for k . This parameter denotes the total number of iterations that must always be executed to mitigate timing attacks. In practice we found that version 2.4 of wpa_supplicant and hostapd use $k = 4$, while newer versions use $k = 40$. This increase was based on security advice given in a close variant of the SAE handshake [56]. Intel’s iwd client uses the value $k = 20$, and the reference implementation of SAE by Harkins uses value 40 [29]. For comparison, the Dragonfly specification in RFC 7664, which is a close variant of the SAE handshake, explicitly recommends a value of at least $k = 40$ [34, §4]. The value 40 is based on a back-of-the-envelope calculation by Igoe [46].

Given the above history of timing side-channels and corresponding defenses, one may wonder why a better design was not created for WPA3. For instance, a better option would be to exclude the MAC addresses from the curve point generation [44, 45]. With such a construction, it would be possible to generate the curve point offline, and reuse this point in every connection attempt (see Section 4.4 for more details).

4 THE FUTILITY OF SAE’S ANTI-CLOGGING

In this section we show that SAE’s anti-clogging mechanism is flawed by design, and does not deter resource consumption attacks. As a result, a resource consumption attack can be launched against any network that support WPA3-SAE (i.e. all home networks).

4.1 History on Anti-Clogging Techniques

Anti-clogging techniques were first used in IP-based networks to prevent resource exhaustion attacks against key exchange protocols [61]. Without them, resource exhaustion attacks were possible by abusing public key cryptography features that resulted in computationally expensive operations such as modular exponentiations [61]. By initiating several simultaneous key exchanges, an attacker can then exhaust the resources of the victim. More problematic, an attacker can initiate key exchanges using spoofed IP addresses, and thereby bypass basic IP-based throttling defenses. This made resource clogging a practical DoS attack.

A precursor of IPsec, called Photuris, used a cookie exchange procedure as an anti-clogging mechanism [50]. Although the Photuris protocol did not become part of IPsec, a simplified variant of this cookie mechanism did become part of IKEv2 [51]. In this scheme, a responder (e.g. a server) can request the initiator to echo a cookie value. This mechanism prevents simple clogging attacks that utilize forged IP source addresses. How a cookie is generated is implementation dependent, but it must satisfy the following requirements [50]: (1) the cookie depends on the identities of both parties; (2) only the responder (server) can generate valid cookies; and (3) the cookie generation and verification must be fast. The recommended method to meet these requirements, is to generate a secret value, and calculate the cookie as follows:

Cookie = Hash(ConnectionID || InitiatorID || secret)

The hash function should be a secure one-way hash such as SHA256. With this cookie exchange, an adversary can no longer initiate handshakes using spoofed IP addresses. Although the attacker can still use its real IP address to launch attacks, this reveals the identity of the attack, and therefore this is not considered a serious threat [61].

4.2 Defeating SAE’s Anti-Clogging

The SAE handshake of WPA3 also uses a cookie exchange procedure to mitigate clogging attacks. More precisely, this mechanism is supposed to prevent DoS attacks that flood the victim with bogus SAE Commit messages from forged MAC addresses [41, §12.4.6]. However, in contrast to spoofing IP addresses, it is trivial to spoof MAC addresses. When an adversary is in range of an AP, they will also be able to receive all replies. This means an attack can trivially capture all cookies (i.e. anti-clogging tokens), and replay them back to the AP to cause a denial-of-service attack.

The above resource utilization attack is especially effective against because of SAE’s side-channel mitigations. For example, when hostapd added the blinding techniques, processing and replying to Commit frames took significantly more processing time. This even caused timeouts on resource constrained devices [39]. To avoid such timeouts, the 802.11 standard was even updated to give stations 2 seconds (instead of 40 ms) to process Commit frames [9].

4.3 Experiments

We implemented a Proof-of-Concept (PoC) of our clogging attack. It is written in C for performance reasons, and build on top of the aircrack-ng tool suite. Our tool can forge Commit frames using both the NIST P-256 and P-521 curve. Each forged Commit frame uses the same scalar and curve point. It is essential that the adversary acknowledges all frames sent to forged MAC addresses. Otherwise the AP will retransmit replies up to eight times, making it impossible for the adversary to inject enough Commit frames to overload the CPU of the target. Fortunately, by relying on the virtual Wi-Fi interface support of Atheros chips, we can easily make it acknowledge frames sent to all forged MAC addresses [77, §5.3].

4.3.1 General Attack. Figure 3 shows the results of our clogging attacks. The attacker used a Raspberry Pi Model B+ with a 700 MHz processor. The Raspberry Pi used a WNDA3200 wireless dongle. The target is a LANCOM LN-1700 AP, which has a 1200 MHz processor.

In our first experiment, the attack is performed using curve P-256. We found that spoofing more than 70 commit exchanges every second causes the CPU of the LN-1700 to overload. As a result, clients that try to connect using WPA3 either face long delays, or cannot connect at all. In contrast, the CPU usage of the attacker is only 14.2%. Since all APs are required to support NIST curve P-256, this shows an adversary can cause a denial-of-service using cheap resource-constrained devices. In a second experiment, we forged Commit exchanges using the P-521 curve. With this curve the impact is an order of magnitude more catastrophic. Now the target’s CPU can be overloaded by forging merely 8 commit exchanges every second (see Figure 8 in the Appendix). On our Raspberry Pi, this attack consumes 2.7% of the CPU. In other words, a very weak adversary is able to clog a high-end AP. We consider it worrying that such a devastating attack is possible against a

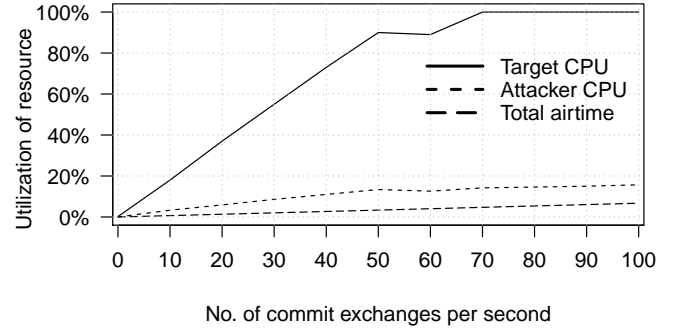


Figure 3: Clogging attack against a professional LANCOM LN-1700 AP using curve P-256. The attacker uses a Raspberry Pi 1 model B+, and its CPU usage is shown in the small dashed line. The total amount of airtime consumed by all SAE frames is shown in the long dashed line.

Table 1: Renewal interval of the secret that is used to generate anti-clogging tokens for various devices and standards.

Standard or impl.	Version	Renewal time
LANCOM	10.20.0168	threshold reached
Hostapd	v2.6	every 60 seconds
Reference Impl.	May 2014	never renewed
ISAKMP [57]	1998	not specified
Phorious [50]	1999	every 1 minute
IKEv2 [51]	2014	not specified
802.11 [41]	2016	threshold reached

protocol that was standardized multiple times, and is even mandated to be implemented as part of the WPA3 certification.

4.3.2 Discussion. Although devices can also use custom methods to generate anti-clogging tokens, all devices we inspected (mostly) follow the mechanism of the 802.11 standard. In particular, we were able to inspect the devices shown in Table 1. The first one is the LANCOM LN-1700, which generates anti-clogging tokens as recommended by the standard, meaning it is easy to bypass. The second implementation we tested is the open source hostapd. It also generates anti-clogging tokens as recommended by the standard, except that it renews the secret value every minute. Harkins’ reference implementation of SAE also follows the 802.11 standard, but it never renews the secret value [29]. Table 1 also shows when other protocols such as IKEv2 renew the secret value.

Finally, we remark that anti-clogging tokens are pointless in any broadcast protocol, since an attack can then trivially capture them.

4.4 Countermeasures

To reduce the impact of an attack, the derivation of the password element can be done in a low-priority background thread. Although legitimate WPA3 clients will be unable to connect during an attack, this at least assures other network functionality is not impacted.

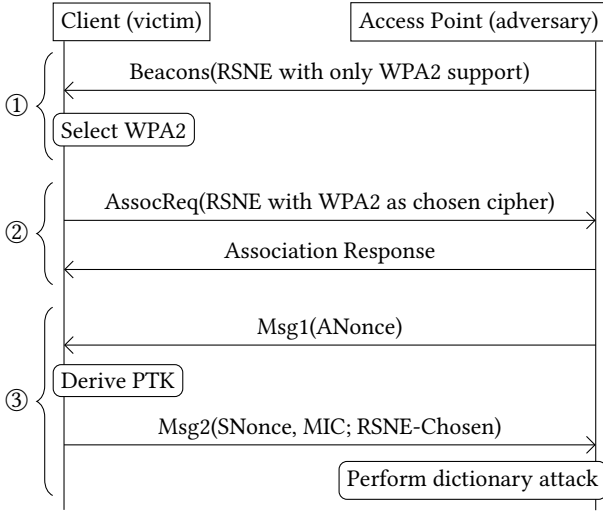


Figure 4: Dictionary attack against WPA3-SAE when it is operating in transition mode, by attempting to downgrade the client into directly using WPA2’s 4-way handshake.

Ideally, the SAE handshake is modified such that the password element is independent of MAC addresses. To the best of our knowledge, mixing in the MAC addresses has no security benefits, and can safely be dropped. This allows both the client and AP to calculate the password element offline, and reuse this result in all subsequent handshakes, preventing our attack.

5 DOWNGRADE & DICTIONARY ATTACKS

In this section we present a dictionary attack against WPA3-SAE when it is operating in transition mode. We also present a downgrade attack that works against WPA3-only networks.

5.1 Downgrade to Dictionary Attack

Our first attack is against WPA3-SAE transition mode. Recall from Section 2.2 that in this mode the AP is configured to accept connections using both WPA3-SAE and WPA2. This provides backward compatibility with older clients. Moreover, WPA2’s 4-way handshake detects downgrade attacks, meaning an attacker cannot trick a WPA3-capable client into (successfully) establishing a connection using WPA2. Put differently, if an adversary attempts to perform a man-in-the-middle against a WPA3-capable AP and client, and modifies beacons so the client thinks the AP only supports WPA2, the client will detect the downgrade and abort the 4-way handshake of WPA2. More precisely, message 3 of WPA2’s 4-way handshake contains all the supported cipher suites of the AP in the authenticated RSNE element (recall Figure 1). Because this handshake message is authenticated under the session key (PTK), the adversary cannot modify it. As a result, the client will detect that RSNE in message 3 does not match with the RSNE received in beacons, and will subsequently abort the handshake. Hence it is indeed not possible to force a WPA3-capable client and AP to use WPA2.

Table 2: Impact of the dictionary downgrade attack against WPA3-SAE when operating in transition mode (see Fig. 4).

Device	Software	Vulnerable
LANCOM	10.20.0168	Yes
RT-N10	dd-wrt v3.0-37305	Yes
Dell Latitude 7490	iwd v0.11	Yes
Dell Latitude 7490	wpa_supplicant v2.6	Yes

The problem is that, although downgrade attacks are detected by the 4-way handshake of WPA2, by that point an adversary has captured enough data to perform a dictionary attack. This is because an adversary only needs a single authenticated 4-way handshake message to carry out a dictionary attack [59]. Therefore, even though the downgrade is detected, by this point it is too late. Moreover, a man-in-the-middle position is not needed to carry out the attack (see Figure 4). The only requirement is that we know the SSID of the WPA3-SAE network, and that we are close to a client. If these conditions are met, the adversary can broadcast a WPA2-only network with the given SSID (stage ① in Figure 4). This causes the client to connect to our rogue AP using WPA2. The adversary can forge the first message of the 4-way handshake because it is not authenticated (stage ③ in Figure 4). In response, the victim will transmit message 2 of the 4-way handshake, which is authenticated. Based on this authenticated handshake message, a dictionary attack can be carried out [59].

We tested the above attack against four client-side implementations of WPA3 (see Table 2). This revealed that all devices were affected by the downgrade attack. We do remark that the fourth client, iwd, did not yet fully support automatically connecting to a WPA3-SAE network. After patching iwd such that it does automatically connect to WPA3 network, it was also possible to downgrade it to WPA2. We conjecture other implementations of WPA3 will also be vulnerable to our attack.

5.2 Attacking SAE’s Group Negotiation

The SAE handshake can be run using different elliptic curve or multiplicative groups mod p (i.e. ECP or MODP groups). The “Group Description” of [40] gives an overview of supported groups. Interestingly, the 802.11 standard allows station to prioritize groups in a user-configurable order [41, §12.4.4.1]. Although this provides flexibility, it requires a secure method to negotiate the group that will be used. Unfortunately, the mechanism that negotiates which curve is used during the SAE handshake is trivial to attack.

With SAE, the used group is negotiated as follows. When a client connects to an AP, it includes its desired group in the Commit frame, along with a valid scalar s_i and element E_i . In case the AP does not support this group, it will reply using a Commit frame with a status field equal to “unsupported finite cyclic group” (see stage ① in Figure 5). In turn the client will attempt to use its next preferred group, and send a new Commit frame with this group and corresponding new scalar s_i and element E_i . This process continues until the client selected a curve that the AP supports. Unfortunately, there is no mechanism that detects if someone interfered with this process. This makes it trivial to force the client into using a different

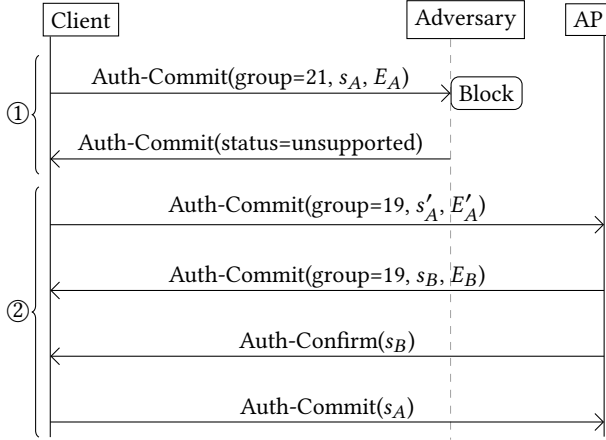


Figure 5: Downgrade attack against SAE's group selection: a man-on-the-side can force the client (initiator) into using a different cryptographic group during the SAE handshake.

group: simply forge a Commit frame that indicates the AP does not support the currently selected group.

Figure 5 illustrates the resulting downgrade attack. Here the client first constructs a Commit frame requested group 21 (i.e. curve P-521). However, the adversary blocks this frame from arriving at the AP (see stage ① in Figure 5). This can be accomplished by jamming the frame [77], or by forging channel-switch announcements [76]. The adversary then forges a Commit frame that indicates the AP does not support the request group. In response the client will pick its second preferred group, which in our example is group 19 (i.e. curve P-256). From this point onwards, a normal SAE handshake is executed using group 19 (see stage ② in Figure 5). Notice that the negotiated curve is never cryptographically validated, meaning the downgrade attack is not detected.

It is also possible to perform an upgrade attack, where the victim is forced to use a more secure cryptographic group. That is, if the victim prefers small cryptographic groups, our attack can force the victim into using bigger groups. This may be useful when performing denial-of-service attacks, or to amplify timing side-channels (see Section 6).

5.3 Countermeasures

To mitigate our downgrade and subsequent dictionary attack, a client should remember if a network supports WPA3-SAE. That is, after successfully connecting using SAE, the client should store that the network supports SAE. From this point onward, the client must never connect to this network using a weaker handshake. This trust-on-first-usage idea is similar to the one of SSH clients, and similar to the Strict-Transport-Security header of HTTPS [60].

In principle, group downgrade attacks can also be mitigated by remembering which groups a network supports. However, the supported groups of an AP are more likely to change over time, and therefore we do not recommend such a defense. Instead, the supported groups can be included as a bitmap in the RSNE during the 4-way handshake. This will enable a station to detect if a downgrade attack took place, and to subsequently abort the handshake.

Listing 2: Algorithm that converts the pre-shared password into a MODP group element [41, §12.4.4.3.2]. The variables (p, G, q) define the MODP group being used, with p a prime, G a generator, and q the prime order of $G \bmod p$.

```

1 def password_to_element_ffc(password, MAC1, MAC2, k=40):
2     found = False
3     counter = 0
4     while not found:
5         counter += 1
6         seed = Hash(MAC1, MAC2, password, counter)
7         value = KDF(seed, "SAE Hunting and Pecking", p)
8         if value >= p: continue
9
10        P = value(p-1)/q mod p
11        if P > 1: found = True
12    return P
  
```

6 TIMING ATTACKS ON MODP GROUPS

In this section we empirically demonstrate that the algorithm used to convert a password into a MODP element is vulnerable to timing attacks. The obtained info will later on be used in a password partitioning attack, allowing one to recover the victim's password.

6.1 Background

Up to this point, we assumed the SAE handshake is executed using elliptic curves. Although this is a natural assumption, since any station that supports SAE must implement the elliptic curve P-256, the SAE handshake can also be performed using multiplicative groups mod a prime p (MODP groups). When employing MODP groups, the algorithm in Listing 2 is used to convert the password into a group element. In contrast to the algorithm in Listing 1 for elliptic curves, the one for MODP groups does not employ any side-channel defenses such as performing extra iterations [41, §12.4.4.3.2].

Generally, elliptic curves are more performant than modular multiplicative groups. However, we found that with WPA3-SAE, using MODP groups is in fact slightly more efficient than elliptic curves. This is due to the extra iterations that are needed when generating the password element using elliptic curves. Recall from Section 3.3 that these extra iterations are needed to mitigate timing side-channels when using elliptic curves. As a result, users may prefer MODP groups over elliptic curves, especially because this would also reduce the impact of our clogging attack of Section 4. Unfortunately, we empirically demonstrate that the password element generation algorithm for MODP groups is also affected by timing side-channels. In practice this means that for certain MODP groups, extra iterations needed to be performed in order to mitigate timing attacks.

6.2 Variable Number of Iterations

When converting a password to a MODP element, the algorithm in Listing 2 performs a variable number of iterations. Although also pointed out in CFRG discussions, this was not analyzed properly, and ignored by the designers [21]. The first cause of extra iterations is when the output of the Key Derivation Function (KDF) on line 7 returns a number bigger than the prime p of the MODP group. Note that the number of bits returned by KDF is equal to the number of bits needed to represent p . That is, the number of bits returned by the KDF function depends on the MODP group being used. This also

Table 3: Overview of MODP groups that cause timing side-channels when deriving the password element. The third column shows the probability that an extra iteration is needed. The last column denotes the average number of iterations that are needed to derive the password element.

Group ID [40]	len(p)	Pr[<i>value</i> ≥ <i>p</i>]	$E[X]$
22	1024	30.84%	1.44
23	2048	32.40%	1.48
24	2048	47.01%	1.89

implies that the probability that *value* is bigger than *p* depends on the MODP group being used. Fortunately, for most MODP groups this probability is extremely small, because the prime *p* is only slightly smaller than a power of two. However, for the MODP groups shown in Table 3, the probability that the output of KDF is bigger than *p* is high. For example, for group 22 this probability equals 30.84%, and for group 24 the probability is 47.01% (see column 3 in Table 3). Finally, the if-condition on line 11 can in principle also cause an extra iteration to be executed. However, for all supported MODP groups, the probability of this happening is negligible.

Since the output of the KDF depends on the password, the number of performed iterations also depends on the password being used. If an adversary learns this number, they learn that passwords which require a different number of iterations are not used by the victim. Note that the number of executed iterations *X* follows a geometric distribution:

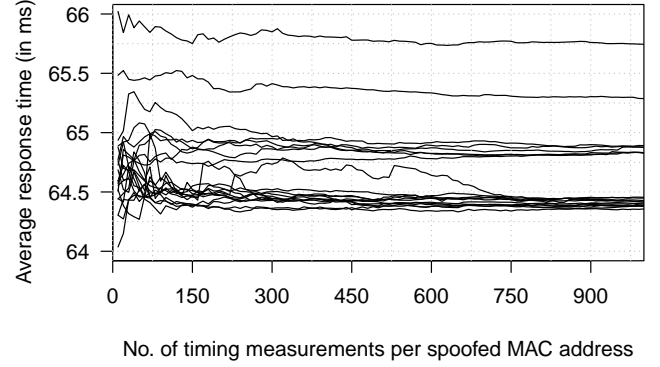
$$\Pr[X = n] = \Pr[\text{value} \geq p]^{n-1} \cdot (1 - \Pr[\text{value} \geq p]) \quad (1)$$

This means that the average number of iterations needed to derive the password element equals $E[X] = (1 - \Pr[\text{value} \geq p])^{-1}$. For MODP group 22, this equals 1.45, and for group 24 this equals 1.89 iterations. In other words, on average one timing measurement allows the adversary to learn the result of multiple iterations. Finally, observe that the MAC address of the client also influences the output of the KDF, and hence also influences the number of executed iterations (line 6 in Listing 2). This means that an adversary can spoof MAC addresses, and for each address measure the number of executed iterations. We will show in Section 8 how this information can be used to perform a password partitioning attack, allowing an adversary to recover the target’s password.

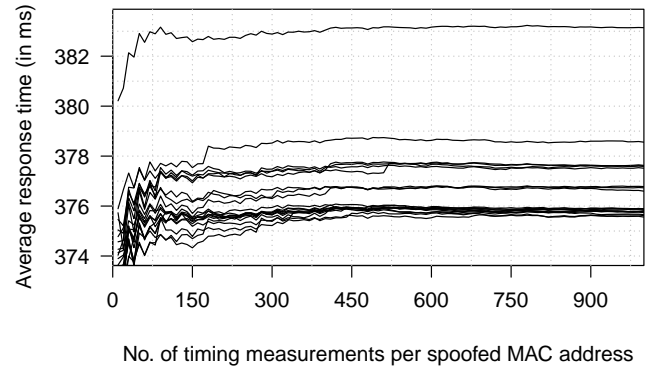
6.3 Experiments

To determine the feasibility of measuring the number of execution iterations, we performed the attack in a realistic setting. For the victim we used a Raspberry Pi 1 model B+ that was running hostapd version 2.6. We used a Raspberry Pi because its 700 MHz CPU matches the one in commodity home routers [82]. The Raspberry Pi was equipped it with a WNDA3200 Wi-Fi dongle. Picking hostapd to run the AP was an obvious choice, since it is the most widely used wireless daemon in both professional and home routers, and is the only one that supports MODP groups at the time of writing.

The adversary used a Dell Latitude 7490 with a WNDA3200 Wi-Fi dongle. To perform timing measurements, we wrote a tool on top of the aircrack-ng tool suite. It spoofs Commit frames, and measures



(a) Measurements of a timing attack using MODP group 22.



(b) Measurements of a timing attack using MODP group 24.

Figure 6: Recovering the number of iterations needed to generate the password element for MODP group 22 and 24. Each line denotes a spoofed MAC address. The lowest cluster of lines corresponds to a single iteration, the second cluster to two iterations, and so on. The victim device is a Raspberry Pi 1 model B+ running hostapd version 2.6.

how long it takes to receive the corresponding Commit reply. After each individual measurement, a deauthentication packet is injected towards the AP. This causes hostapd to clear all state related to the spoofed MAC address, and enables us to rapidly perform a new timing measurement with the same spoofed address.

Two optimizations were required to make the attack practical. First, similar to our clogging attack of Section 4.3, we had to use virtual interface support of Atheros chips to acknowledge all frames sent to a spoofed MAC address. This prevents the AP from retransmitting frames, making the attack faster and more reliable. More importantly, background Wi-Fi traffic influences the timing measurements. Additionally, periodic background tasks on the AP also influence the timing measurements. Both sources of noise are problematic because they are not constant throughout the attack. To handle this, we interleave the time measurements of all spoofed MAC addresses, instead of performing all measurements for each MAC address one by one. As a result, temporary noise equally influences the measurements of all MAC addresses, instead of only affecting the measurements of one address.

With the above setup and optimizations, we carried out an attack using MODP group 22, and another attack using group 24. We spoofed 20 addresses in each experiment, and performed 1000 measurements for each spoofed address. The attack against group 22 took 228 minutes, and the attack against group 24 took 607 minutes. Figure 6 shows the results of these experiments. Each line represents the average timing measurements of one spoofed MAC address. From these timings, it is straightforward to derive the number of executed iterations. For example, the cluster of lines (i.e. spoofed MAC addresses) at the bottom corresponds to one iteration. The cluster above that corresponds to two iterations, and so on. For the highest line in the MODP group 24 attack, careful inspection reveals that this corresponds to 9 iterations. The correctness of these results was confirmed by inspecting the debug output of `hostapd`. We conclude that timing attacks can accurately determine the number of executed iterations.

6.4 Countermeasures and Discussion

Ideally, the SAE handshake is modified to be independent of the MAC address and use a constant-time and jump-free Hash to Group method. In that case, the calculation can be done offline.

As an immediate countermeasure, we recommend to disable MODP groups where the prime is slightly larger than a power of two. More precisely, disabling groups 22, 23, and 24 prevents our timing attack. The other MODP groups use primes that are slightly smaller than a power of two, meaning it is extremely unlikely that the output of the KDF in line 7 of Listing 2 is bigger or equal to the prime p . Therefore, with these groups the password element is practically always found in the first iteration.

A backward-compatible countermeasure for groups 22 to 24 is to perform extra iterations after finding the MODP password element, so a fixed number of iterations are always executed. This is similar to the countermeasure for the elliptic curve case. We recommend to perform at least 40 iterations. Note that these extra iterations are only needed when using group 22, 23, or 24. For other MODP groups, no extra iterations are needed. Nevertheless, we conjecture that even with this defense, implementations may still be vulnerable to cache-based side-channel attacks.

7 CACHE-BASED ATTACKS ON ECC GROUPS

In this section we demonstrate that implementations of the Hash to Curve algorithm of SAE may be vulnerable to cache-based side-channel attacks. Similar to the timing attack against MODP groups, this will later on enable an adversary to recover a target's password.

7.1 Background and Attack Goal

The goal of our attack is to learn if the Quadratic Residue (QR) test in the first iteration of the hash to curve algorithm succeeded or not. This information will be used in the offline password partitioning attack of Section 8 to recover the target's password. Unlike the case of the MODP groups described in Section 6, the implementation of the hash to curve algorithm for ECC groups does include mitigations against side channel attacks. Those mitigations include performing extra dummy iterations on random data [41, §12.4.4.3.2], and blinding of the underlying cryptographic calculation of the quadratic residue test [33]. The resulting code of `wpa_supplicant` and

`hostapd` implementation we reviewed is pseudo-constant time, i.e., there might be some minor variation in run time, but they are too minute to be measured by an adversary. However, in many cases such pseudo-constant time implementations are still vulnerable to different types micro-architectural side-channel attacks [2, 47, 66].

7.1.1 Micro-Architectural Side-Channel Attacks. Modern processors try to optimize their behavior (e.g. memory access, branch prediction) by saving an internal state that depends on the past. Micro-architectural side-channel attacks exploit leaked information about the running of other programs due to sharing of this state [23]. Cache-based side channel attacks exploit the state of the memory cache (either instructions or data) and have been widely used to break cryptographic primitives [5, 14, 24, 63, 86].

In the different variants of the FLUSH+RELOAD attack [26, 27, 86, 88] the attacker starts by evicting (or flushing) a memory location from the cache. After waiting for a predetermined interval, he measures the time it takes to reload the flushed location. If during the interval the victim accesses this memory location, it will be cached, and the reload time for the attacker will be short. Otherwise, the reloading of the flushed memory location will be much slower. In this way, the attacker can trace the victim's memory access patterns.

7.2 Attack Scenario

Our attack requires the ability to monitor cache access patterns on the victim machine. However, unlike many cache attacks against TLS implementations [2, 47, 66], we can also target the client side. We can run our attack from any unprivileged user-mode process (or application on android). Oren et al. [62] even showed how to perform such attacks from the browser using JavaScript code (although browsers are now implementing mitigation for these types of attacks).

For our password partitioning attack, we need to record several handshakes with different MAC addresses. We can get handshakes with different MAC addresses by targeting multiple clients in the same network (e.g. convince multiple users to download the same malicious application). If we are only able to attack one client, we can set up rogue APs with the same SSID but a spoofed MAC address. We can force victims into connecting to our rogue AP by using a higher signal strength, or jamming the legitimate AP [77].

7.3 Attacking the hostapd Implementation

Our target implementation is the `sae_derive_pwe_ecc` function in the latest `hostapd` code (commit 0eb34f8f2 from Sat Jan 26) with the default curve P-256. Our test machine uses a 4-core Intel Core i7-7500 processor, with a 4 MiB cache and 16 GiB memory, running Ubuntu 18.04.1. To monitor access to the instruction cache we use the FLUSH+RELOAD attack [86], as implemented in the Mastik toolkit [85].

To learn the result of the first QR test, we can either attack the blinded QR test implementation, or the branch in the iteration loop that checks the result of the test. A simple cache attack against the blinded QR test is infeasible as the two possible code paths (see Listing 4 line 14) are compiled into a single cache line.¹

¹More advanced micro architectural attacks targeting the branch predictor [2, 6, 19] will fail due to the extra random iterations.

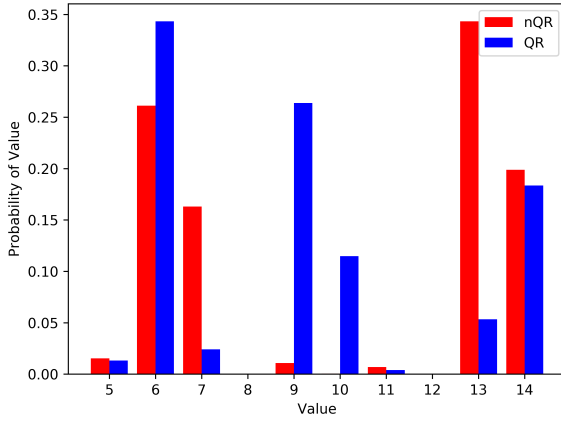


Figure 7: Probability distribution for attack results

The two code paths of the branch inside the iteration loop (see Listing 5 line 22) are compiled into two separate cache lines. Therefore we can monitor cache access to nQR cache line which is the target of the conditional jump (see Listing 6 line 9). To differentiate between the branches taken in the first and subsequent iterations, we created a synchronization “clock” by monitoring another cache line that is accessed once every iteration (similarly to what is done in [87]).

On our test platform, monitoring two cache lines repeatedly over time caused a high rate of false positives (i.e. false detection of access to cache lines). This error rate increases considerably if the monitored cache lines are close. Consequently, for our “clock” we choose to monitor a cache line far away from the nQR cache line (in our case the function `sha256_prf_bits`).

7.3.1 Classification of Cache Access Patterns. We want to classify our cache traces as one of two cases depending on the results of the QR test in the first iteration (non-QR or QR). The measured cache access patterns to the two monitored cache lines show a high variance between different traces of the same case. This might be due to OS related noise, speculative execution, or the way that the random dummy iterations affect the branch predictor behavior in the next run of the function. To overcome this we perform a simplified variant of a cache template attack [16, 27]. That is, we measure a trace of the cache access pattern by monitoring the two address (the “clock” and the non-QR case) in fixed intervals of 50000 clock cycles (each iteration takes ≈ 200000 clock cycles on our test machine). We encode each trace into two bits that correspond to the two memory locations. In each trace a bit is set to one if its corresponding memory location was accessed, and to zero otherwise.

In our attack we only keep active measurements with at least one non-zero bit. Our attack returns the value of the first two active measurements, meaning the return value consists of four bits (resulting in 9 possible return values). Figure 7 shows the distribution of these return values when the first iteration of the hash to curve algorithm results in a non-QR number (nQR), and when the first iteration results in a QR number (QR).

For our classification we repeat the attack 20 times for each MAC address. We created a training set for the non-QR and the QR cases

using $100 \cdot 20$ traces each. We used this training set to build a simple linear classifier that receives 20 traces as an input, and returns the input classification, namely either non-QR or QR. We then tested our attack and linear classifier on a larger test set of $400 \cdot 20$ traces for each case. For the non-QR case we have achieved a 100% success rate (400 out of 400), and for the QR case we have achieved a 99.5% success rate (398 out of 400). We can conclude that an adversary can reliably abuse cache-based side-channels to determine whether the password element was found in the first iteration or not.

7.4 Countermeasures and Discussion

As in the MODP case, the ideal solution is to modify the SAE handshake such that the password element is independent of MAC addresses, and use a constant-time hash to curve algorithm from the new standard [68]. Even if the attacker can attack the one-time offline calculation, and exploit some residual side-channel leakage, the expected number of password bits leaked is only two. A backward-compatible countermeasure is to replace the two vulnerable branches with a constant-time select utility, and use constant time Legendre symbol computation as defined in [68].

8 PASSWORD PARTITIONING

In this section we show how to perform password partition attacks, using the information obtained from our timing and cache attacks. This enables an adversary to recover the password of a target.

8.1 Partitioning a Dictionary

In the first attack variant, our goal is to recover the password from a given dictionary. We accomplish this by repeatedly partitioning the dictionary into correct and incorrect password candidates. Practically, this is implemented by removing incorrect passwords from the dictionary during each partitioning step. If the dictionary becomes empty, this means the target’s password was not in it. However, if after the partitioning steps only one password remains, then with high probability this is the target’s password.

The result of every element test that is performed in a (password-dependent) iteration of Listing 1 or 2 can be used to partition the dictionary. We use the term *element test* to refer to both the quadratic residue test for elliptic curves, and the if-test that checks whether the prime of the MODP group is bigger than the hash output. Recall that with one timing measurement against the MODP algorithm, we learn on average the result of multiple (failed) element tests. Considering element tests separately also has the advantage that, if for example we are unsure whether a spoofed address resulted in 4 or 5 iterations, this info still enables us to determine that the first three element tests failed. By representing our timing and cache attack measurements as a set of element tests, we can now use the same partitioning attack algorithm in both attack scenarios.

The algorithm illustrated in Listing 3 implements the password partitioning algorithm. As input it receives a dictionary, the set of element tests and their result, and the MAC address of the target. The algorithm uses this information to partition the dictionary by removing passwords that lead to a different result for the element test compared to the result that we measuring this the timing or cache-based attack. More importantly, this algorithm can be run offline, i.e., without requiring any interactions with the target device.

Listing 3: Password partitioning algorithm in Python-like pseudo code. It eliminates incorrect passwords based on the result of specific element tests for each spoofed MAC address. It returns a list of remaining candidate passwords.

```

1 def recover_password(dictionary, testdata, mactarget):
2     # dictionary: Set of possible passwords.
3     # testdata: Element test results for each spoofed MAC address and
4     #           counter value used in a specific element test.
5     # mactarget: MAC address of the target (e.g. a client or AP).
6
7     for macspoof, counter, result in testdata:
8         for p in dictionary:
9             if simulate_test(p, macspoof, mactarget, counter) != result:
10                dictionary.remove(p)
11             if len(dictionary) <= 1: break
12     return dictionary

```

8.2 Prerequisites and Success Analysis

To determine the performance of the password partitioning algorithm, we first calculate how many element tests are required to uniquely recover the password with high probability. Note that every element test is independent, because in each iteration the hash inputs are different, resulting in independent hash outputs. Let q denote the probability that the group element is not found, meaning another iteration and element test has to be performed. For the elliptic curve algorithm, q is close to 50%, and for MODP groups the values for q are listed in Table 3 under $\Pr[\text{value} \geq p]$.

We want to know the probability of eliminating d incorrect passwords, when given the result of n element tests. Let Z denote a random variable that equals the number of element tests that are required to eliminate d incorrect passwords. This means that if a dictionary of size $d + 1$ contains the correct password, and we use n element tests, the probability of uniquely recovering the password is $\Pr[Z \leq n]$. To derive this probability, we first introduce random variable Y as being the number of element tests where the password element was found. We have:

$$\Pr[Y = k] = \binom{n}{k} \cdot (1 - q)^k \cdot q^{n-k} \quad (2)$$

This is because the result of an element test does not eliminate an incorrect password when the incorrect password has the same result under the given MAC addresses and iteration count. For example, if the real password in a given iteration did not have a quadratic residue, and the incorrect password also did not, then the results of this element test does not eliminate the password. Given that in k out of n measured element tests the password element was found, the probability that all element tests do *not* eliminate a random password equals $(1 - q)^k \cdot q^{n-k}$. Now let random variable E denote the number of eliminated passwords. The probability that all d incorrect passwords are eliminated equals:

$$\Pr[E = d \mid Y = k] = \left(1 - (1 - q)^k \cdot q^{n-k}\right)^d \quad (3)$$

Finally, given the result of n random element tests, the probability that all d incorrect password are eliminated equals:

$$\Pr[Z \leq n] = \sum_{k=0}^n \Pr[Y = k] \cdot \Pr[E = d \mid Y = k] \quad (4)$$

We tested the above formula by running 100 000 runs of the partitioning algorithm on 1 000 passwords. Each run used random simulated element test results (i.e. simulated timing measurements). Our experimental results closely matched that of formula 4.

By trying various values for n with the RockYou password dump, we find that for MODP group 22, having $n \geq 35$ element tests gives us a probability above 95% of uniquely recovering the correct password. On average, we need to perform $35/1.44 = 24.3$ timing measurements to obtain 35 element tests (recall Table 3). For elliptic curve P-256, an adversary needs to obtain 29 element test results to uniquely recover the password with a probability above 95%. Given that our cache-based side-channel attack can detect a QR with 100% accuracy, and a non-QR with 99.5% accuracy, the probability of that on average all used non-QR measurement are correct equals $0.995^{12.5} = 0.939$. The probability of uniquely recovering the password then becomes at least $0.95 \cdot 0.939 = 0.892$. In other words, using 25 cache-based element test results, the probability of recovering the password from the RockYou dump is close to 90%.

Using formula 4, we can also determine the *average* number of element tests that are needed to eliminate all d incorrect passwords:

$$\ell = \sum_{i=1}^{\infty} i \cdot \Pr[Z = i] = \sum_{i=1}^{\infty} i \cdot (\Pr[Z \leq i] - \Pr[Z \leq i - 1]) \quad (5)$$

We tested the above formula by running 100 000 runs of the partitioning algorithm with each time 1 000 random passwords, assuming q equals 0.3084. Results closely matched the predicted ones.

Assuming the RockYou dump is used for the dictionary, and MODP group 22 as the target, formula 5 teaches us that on average an adversary needs to obtain 28.28 element tests to uniquely recover the password. For elliptic curve P-256, the adversary would need on average 25.11 element tests (i.e. quadratic residue test results).

8.3 Computational Requirements

To estimate the computational costs of running the partitioning algorithm in function of the dictionary size d , we derive the expected number of element tests that have to be simulated (see line 9 in Listing 3). From formula 5 we already know the expected number of element tests that are needed to eliminate all d incorrect passwords. In other words, the partitioning algorithm will execute on average ℓ iterations. During each of these iterations, a percentage of passwords are eliminated from the dictionary. More precisely, when taking a random element test as reference, and comparing it with an incorrect password, the chance of *not* being able to remove the incorrect password as a candidate is $f = q^2 + (1 - q)^2$. Hence, the amount of element tests that are performed on average is:

$$d + f^1 d + f^2 d + \dots + f^{-\lceil \ell \rceil} d = d \frac{1 - f^{\lceil \ell \rceil}}{1 - f} \quad (6)$$

We again tested the above formula by running 100 000 runs of the partitioning algorithm, with each time 1 000 random passwords, assuming $q = 0.3084$. Results closely matched the predictions. For MODP group 22 and the RockYou dictionary, this would mean that on average we have to perform 33 627 714 element tests. With elliptic curve P-256 this results in 28 689 748 element tests on average.

On a laptop with an Intel i7-8650U CPU running at 1.90GHz, performing an attack using the RockYou password list takes on

average around 11 minutes. This means ordinary users can perform this attack on their existing off-the-shelf hardware.

We can further optimize the partitioning algorithm if q differs from 0.5. That is, when attacking a MODP group, we can first process the dictionary using an element test result where the target did not find the password in the given iteration. Recall that this happens with probability q . A random incorrect password then has a probability $1 - q$ of being eliminated. Since on average $\ell \cdot q$ element tests can be used to eliminate an incorrect password with a probability of $1 - q$, formula 6 can be modified in the obvious way to take our new strategy into account. When using the RockYou dictionary under this new strategy, we need to perform only 20 742 225 element tests using MODP group 22, a reduction by 38%.

8.4 Brute-Force Attacks in the Cloud

In our second variant of the partitioning attack, we essentially perform an offline brute-force attack on the password. More concretely, our goal is to test all possible 26^8 lowercase passwords. Using formula 5 we know that on average this requires 38.36 element tests for MODP group 22, and 38.92 for elliptic curve P-256. Recall that for the MODP case, this means we need to make on average $38.36/1.44 = 26.64$ timing measurements. These are relatively modest requirements. For example, in our demonstration of the timing attack we already performed 20 timing measurements. As a result, we must assume an adversary can obtain the required number of element test results.

We now calculate the costs of running the offline partitioning phase on Amazon EC2 instances. For both the MODP and elliptic curve cases, we first performed repeated microbenchmarks where we simulated one million element tests on a single EC2 vCPU. On average, the MODP test took 3.04 microseconds, and the quadratic residue test took 23.25 microseconds. In macrobenchmarks of the partitioning algorithm on the RockYou dictionary, close to identical running times were observed. We now multiply these timings with the result from formula 6. In particular, for MODP group 22 we need to perform on average 301 947 836 620 element tests, and for curve P-256 we need to perform 417 654 129 151 tests. Fortunately, we can parallelize the code by splitting the brute-force search out over several workers. Every worker gets access to all the element test results, meaning if sufficient element tests were obtained, every worker skips all incorrect passwords. Only the real password will be detected as potentially valid.

Assuming we rent c5.18xlarge instances having 72 vCPUs, which costs \$3.06 an hour, we can perform the brute-force search against the MODP case for \$10.63 on average (within e.g. an hour). The brute-force attack against elliptic curves is would cost \$125 on average, which although more costly, is still a worryingly low amount.

9 RELATED WORK

After the introduction of WPA, it was quickly found to be vulnerable to dictionary attacks [59]. Later, He and Mitchell formally analyzed WPA's 4-way handshake, and discovered a DoS vulnerability [37, 58]. This resulted in the standardization of a slightly improved 4-way handshake [41]. He et al. continued to analyze the 4-way handshake, and proved its correctness [38]. However, implementations of the 4-way handshake were nevertheless vulnerable

to downgrade attacks [78]. Recently, Vanhoef and Piessens discovered that WPA2 was vulnerable to key reinstallation attacks [79, 80]. Finally, Kohlios and Hayajneh provide an overview of WPA2 and the differences with WPA3 [52].

Researchers also discovered several DoS attack against Wi-Fi networks. The most well-known is the deauthentication attack [11]. Other DoS attacks exploit weaknesses in TKIP [25]. Additionally, Könings et al. found several DoS vulnerabilities in the physical and MAC layer of 802.11 [53], and other researchers constructed jammers using commodity hardware [67, 77]. A detailed survey of DoS attacks at the physical and MAC layer is given by Bicakci and Tavli [15]. Aiello et al. show how susceptibility to denial-of-service attacks can be balanced with the need for perfect forward secrecy [7]. To the best of our knowledge, our clogging attack against WPA3 is the first that overloads the CPU of the victim.

An initial version of Dragonfly was vulnerable to an offline dictionary attack [20]. A modified variant was then specified in 2008 [30]. Several close variants of it have been defined over the years, and are commonly referred to as Dragonfly-type handshakes [32, 34–36]. Trevor Perrin did a review of an improved draft of the handshake [65], and later provided an overview of other people's comments on the handshake [64]. Struik reviewed a draft of the handshake [74]. Clarke and Hao discovered a small subgroup attack against a draft of the handshake, which was mitigated in a new draft [17]. Lancrenon and Skrobot provided a security proof of a close variant of the Dragonfly handshake [55]. Finally, Alharbi et al. designed a variant of Dragonfly that attempts to keep computational costs low [8].

Other types of PAKes have also been proposed by researchers over the years [3, 4, 10, 12, 13, 48, 49, 70, 72, 73, 84], of which some have been submitted as RFCs [28, 54, 54, 69, 71, 75, 83]. Finally, there is also research into post-quantum PAKes [18, 22].

10 CONCLUSION

We consider it very concerning that a modern security protocol is vulnerable to our presented attacks. Equally troublesome is that some of our attacks could have been prevented, if the designers incorporated all criticisms that the Dragonfly handshake received while it was being standardized. In particular, the designers were warned that timing attacks might be possible, but failed to incorporate proper defenses in the MODP hash to group method. On the other hand, we conjecture that, even if strong defenses against timing attacks were implemented, the protocol would still be vulnerable to other side-channel attacks. Instead, we recommend to modify the SAE handshake such that the password element is independent of MAC addresses. With this simple change, we remove the requirement to keep a plaintext copy of the password, reduce the impact of DoS attacks, and prevent online side-channel attacks.

All combined, we believe the Wi-Fi Alliance should have created the WPA3 certification in a more open manner. This would have prevented our downgrade attack against WPA3 transition mode. Additionally, being more open would have resulted in more scrutiny of the SAE handshake before it became part of WPA3's certification program. Nevertheless, although WPA3 is vulnerable to various attacks, we believe that when using proper countermeasures it remains an improvement over WPA2.

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A EXPERIMENTS

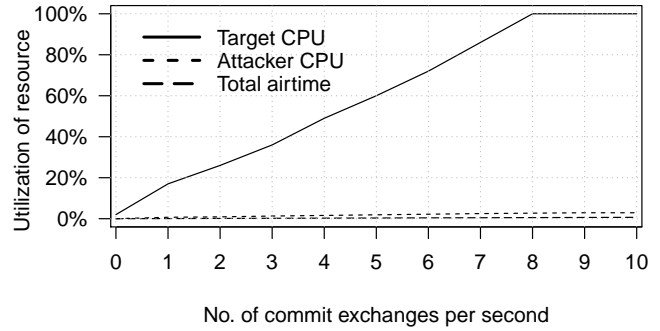


Figure 8: Clogging attack against a professional LANCOM LN-1700 AP using curve P-521. The attacker uses a Raspberry Pi 1 model B+, and its CPU usage is shown in the small dashed line. The total amount of airtime consumed by all SAE frames is shown in the long dashed line.

B SOURCE CODE

Listing 4: Side channel protected quadratic residuosity testing

```

1 static int is_quadratic_residue_blind(struct sae_data *sae,
2 const u8 *prime, size_t bits, const struct crypto_bignum *qr,
3 const struct crypto_bignum *qnr, const struct crypto_bignum *y_sqr){
4 struct crypto_bignum *r, *num;
5 int r_odd, check, res = -1;
6 /* Use the blinding technique to mask y_sqr while determining
7 * whether it is a quadratic residue modulo p to avoid leaking
8 * timing information while determining the Legendre symbol.
9 * v = y_sqr
10 * r = a random number between 1 and p-1, inclusive
11 * num = (v * r * r) modulo p */
12 r = get_rand_1_to_p_1(prime, sae->tmp->prime_len, bits, &r_odd);
13 ...
14 if (r_odd) {
15 /* num = (num * qr) modulo p
16 * LGR(num, p) = 1 ==> quadratic residue */
17 if (crypto_bignum_mulmod(num, qr, sae->tmp->prime, num) < 0)
18 goto fail;
19 check = 1;
20 } else {
21 /* num = (num * qnr) modulo p
22 * LGR(num, p) = -1 ==> quadratic residue */
23 if (crypto_bignum_mulmod(num, qnr, sae->tmp->prime, num) < 0)
24 goto fail;
25 check = -1;
26 }
27 res = crypto_bignum_legendre(num, sae->tmp->prime);
28 ...
29 res = res == check;
30 ...

```

Listing 5: SAE password derivation using hash to curve

```

1 static int sae_derive_pwe_ecc(struct sae_data *sae, const u8 *addr1,
2 const u8 *addr2, const u8 *password,
3 size_t password_len, const char *identifier){
4 ...
5 if (random_get_bytes(dummy_password, dummy_password_len) < 0)
6 return -1;
7 ...
8 /* Create a random quadratic residue (qr) and quadratic non-residue
9 * (qnr) modulo p for blinding purposes during the loop. */
10 if (get_random_qr_qnr(prime, prime_len, sae->tmp->prime, bits,

```

```

11    &qr, &qnr) < 0)
12    return -1;
13    ...
14    /* Continue for at least k iterations to protect against side-channel
15     * attacks that attempt to determine the number of iterations required
16     * in the loop. */
17    for (counter = 1; counter <= k || !x; counter++) {
18        ...
19        res = sae_test_pwd_seed_ecc(sae, pwd_seed, prime, qr, qnr, &x_cand);
20        if (res < 0)
21            goto fail;
22        if (res > 0 && !x) {
23            ...
24            x = x_cand; /* saves the current x value */
25            ...
26            /* Use a dummy password for the following rounds, if
27             * any. */
28            addr[0] = dummy_password;
29            len[0] = dummy_password_len;
30        } else if (res > 0) {
31            crypto_bignum_deinit(x_cand, 1);
32        }
33    }
34    ...

```

Listing 6: SAE password derivation using hash to curve assembly

```

1 000000000002efe0 <sae_derive_pwe_ecc>:
2 ...
3 2f2c8: e8 f3 17 05 00 callq 80ac0 <sha256_prf_bits>
4 ...
5
6 2f719: e8 f2 fa 04 00 callq 7f210 <crypto_bignum_legendre>
7 ...
8 2f751: e8 1a f7 04 00 callq 7ee70 <crypto_bignum_deinit>
9 2f75d: 0f 85 59 01 00 00 jne 2f8bc <sae_derive_pwe_ecc+0x8dc>
10 ... /* handle qr case code range */
11 2f7d2: 0f 86 60 fa ff ff jbe 2f238 <sae_derive_pwe_ecc+0x258>
12 ...
13 /* start nqr case code */
14 2f8bc: 48 8b 7c 24 40 mov 0x40(%rsp),%rdi
15 2f8c1: be 01 00 00 00 mov $0x1,%esi
16 2f8c6: e8 a5 f5 04 00 callq 7ee70 <crypto_bignum_deinit>
17 2f8cb: e9 94 fa ff ff jmpq 2f364 <sae_derive_pwe_ecc+0x384>
18 /* end nqr case code */
19 ...

```