# Quiz week 3

**Due** 25 Sep at 23:59 Points 7 **Questions** 7

**Available** 19 Sep at 0:00 - 25 Sep at 23:59 Time limit None

## Attempt history

	Attempt	Time	Score
LATEST	Attempt 1	7,023 minutes	0 out of 7

## Submitted 25 Sep at 19:19

# 0 / 1 pts **Jnanswered Question 1** Regarding minimum variance unbiased estimator (MVUE) and Cramer-Rao Lower Bound (CRLB), which of the following statement is FALSE. MVUE does not always exist. Even it exists, we may not be able to find it. If an estimator exists whose variance equals the CRLB, then it must be the MVUE. orrect answer If no estimator has a variance that equals the CRLB, the MVUE doesn't exist.

#### **Jnanswered**

**Question 2** 

0 / 1 pts

The Cramer-Rao Lower Bound (CRLB) provides an lower bound on the variance of the estimate. Regarding CRLB, which of the following statement is **FALSE**.

In CRLB, the regularity condition is violated if the region of integration depends on the parameter  $\theta$ .

orrect answer

The variance of estimator  $\mathbf{var}(\hat{\theta})$  is always larger than  $\mathcal{I}(\theta)^{-1}$ , where  $\mathcal{I}(\theta) = \mathbf{E}\Big[\frac{\partial^2 \ln p(\theta;\mathbf{x})}{\partial \theta^2}\Big]$  represents the Fisher information.

If the Fisher information from each single observation  $x_n$  is  $i(\theta)$ , the Fisher information from N such identical but independent observations is  $\mathcal{I}(\theta) = Ni(\theta)$ .

An efficient estimator  $\hat{\theta} = g(\mathbf{x})$  may be found if  $\frac{\partial \ln p(\mathbf{x}; \theta)}{\partial \theta} = \mathcal{I}(\theta)(g(x) - \theta).$ 

**Jnanswered** 

**Question 3** 

0 / 1 pts

Let  $x_0, x_1, \ldots, x_{N-1}$  be IID and uniformly distributed in the interval [0, A], i.e.,  $x_n \sim \operatorname{Uniform}(0, A)$ . The unknown parameter A determines the length of the interval. The PDF of the observations is

$$p(\mathbf{x};A) = egin{cases} rac{1}{A^N}, & ext{for } 0 \leq x_n \leq A & n=0,1,\dots N-1, \ 0, & ext{else}. \end{cases}$$

Check whether the CRLB for an estimate of  $m{A}$  exists and if so, calculate it.

- $\bigcirc \ \operatorname{Var}(g(\mathbf{x})) \geq rac{N}{A^2}$
- $\bigcirc \ \operatorname{Var}(g(\mathbf{x})) \geq rac{N^2}{A^2}$
- $\bigcirc \operatorname{Var}(g(\mathbf{x})) \geq -\frac{N}{A^2}$

orrect answer

The CRLB does not exist.

#### **Jnanswered**

## **Question 4**

0 / 1 pts

Which of the following statements about the maximum likelihood estimator is **FALSE**?

○ The maximum likelihood is asymptotically unbiased.

orrect answer

If the likelihood function has a maximum, it is unique.

The maximum likelihood estimator is the value of  $\theta$  that maximized the likelihood function  $p(\mathbf{x}; \theta)$  for a given observation  $\mathbf{x}$ .

If an efficient estimator exists, it is also the maximum likelihood estimator.

#### **Jnanswered**

## **Question 5**

0 / 1 pts

If we observe  ${\bf N}$  independent and identically distributed samples  $x_n$  from  ${\bf Binomial}(M,q)$  distribution with the probabilities  $p(x_n;q)=\binom{M}{x_n}q^{x_n}(1-q)^{M-x_n}$ , which of the following expression correctly describes the log-likelihood function  $\ln p({\bf x};q)$ .

There is not enough information to calculate.

#### orrect answer

$$0 \ln p(\mathbf{x};q) = \sum_{n=0}^{N-1} \ln inom{M}{x_n} + \ln rac{q}{1-q} \sum_{n=0}^{N-1} x_n + \ln (1-q) M N$$

$$0 \ln p(\mathbf{x};q) = \sum_{n=0}^{N-1} \ln \binom{M}{x_n} + \ln rac{1-q}{q} \sum_{n=0}^{N-1} x_n + \ln (1-q) MN$$

$$\ln p(\mathbf{x};q) = \sum_{n=0}^{N-1} \ln \binom{M}{x_n} + \ln rac{q}{1-q} \sum_{n=0}^{N-1} x_n + \ln(q)(M-1)N$$

#### **Jnanswered**

## **Question 6**

0 / 1 pts

Continue with above question, which of the following expression is the correct maximum likelihood estimate of q.

#### prrect answer

$$igcirc$$
  $\hat{q}_{ ext{ML}} = rac{\sum_{n=0}^{N-1} x_n}{MN}$ 

$$igcirc$$
  $\hat{q}_{ ext{ML}} = rac{\sum_{n=0}^{N-1} x_n}{MN-1}$ 

There is not enough information to calculate.

$$igcap \hat{q}_{
m ML} = rac{\sum_{n=0}^{N-1} x_n}{M(N-1)}$$

$$igcirc \hat{q}_{
m ML} = rac{\sum_{n=0}^{N-1} x_n}{(M-1)N}$$

**Jnanswered** 

## **Question 7**

0 / 1 pts

Regarding efficient estimators for linear models, which of the following statement is **FALSE**.

#### orrect answer

The efficient estimator is available when the signal model is linear.

If the model is linear with additive white Gaussian noise of variance  $\sigma^2$ , the covariance of the estimate is proportional to  $\sigma^2$ .

When colored Gaussian noise is added to the linear signal model, the noise covariance of MVUE can be expressed as  $\mathbf{C}_{\hat{\boldsymbol{\theta}}} = (\mathbf{H}^T \mathbf{C}^{-1} \mathbf{H})^{-1}$ . Here,  $\mathbf{C}$  is the covariance matrix of the colored noise.