

학습 목표

최소힙(Min-heap)을 다루는 작업들을 학습하고 구현할 수 있다



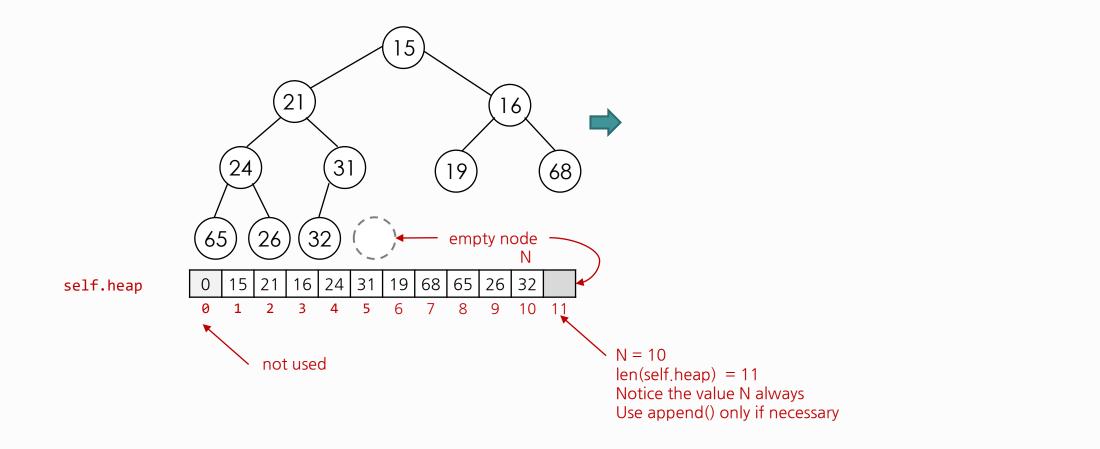
Data Structures in Python Chapter 8

- Heap and Priority Queue
- Heap Coding
- Min/MaxHeap and Heap sort

Agenda & Readings

- Heap and Priority Queue
 - Heap Class and Constructor
 - Heap ADT:
 - Insert(), Delete()
 - HeapBuild(), Heapify()
 - Helper functions swim(), swap(), sink()
- Reference:
 - Problem Solving with Algorithms and Data Structures

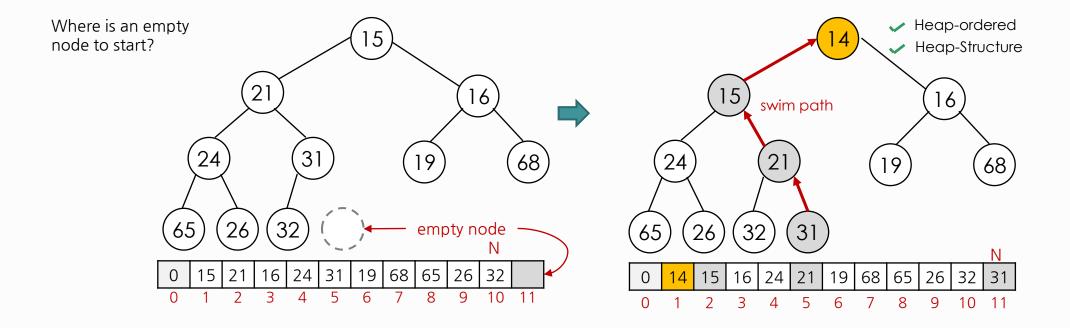
Heap Class and Constructor



min-heap: insert(heap, 14)

- Insert a new element while maintaining a heap-structure
- swim(): Move the element up the heap while not satisfying heap-ordered

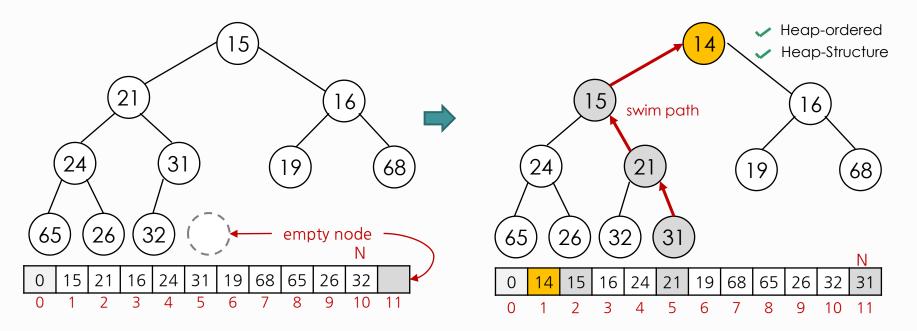
```
class BinHeap:
...
def insert(self, key):  # check N and len(heap) before using
    self.heap.append(key)  # append() if necessary, otherwise use list index
    self.N += 1
    self.swim(self.N)
```



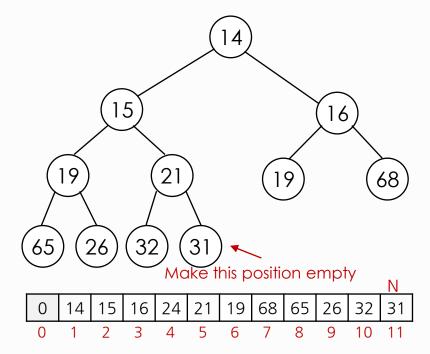
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- Insert a new element while maintaining a heap-structure
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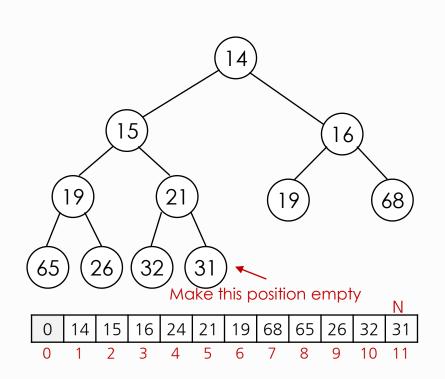
```
class BinHeap:
...
def swim(self, k):  # append key and swim up
    while k // 2 > 0:  # if not reached root
    if self.heap[k/2] > self.heap[k]:  # if parent is more than kid (minheap)
        self.swap(k//2, k)  # swap(parent, kid)
    k = k // 2  # swim up - move to the parent node
```



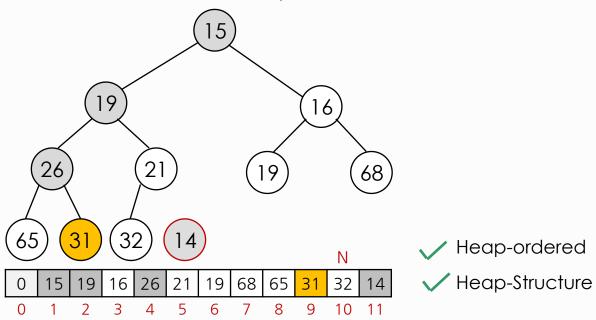
- Swap the root and the last element.
- Heap decreases by one in size.
- Move down (sink) the root while not satisfying heap-ordered.
 - Minimum element is always at the root (by min-heap definition).

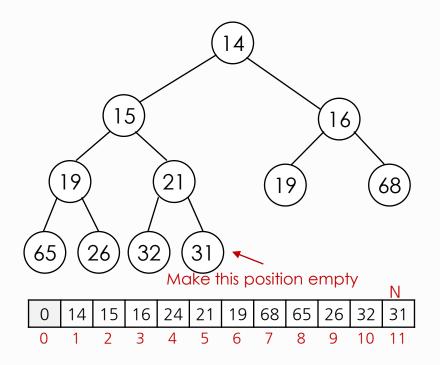


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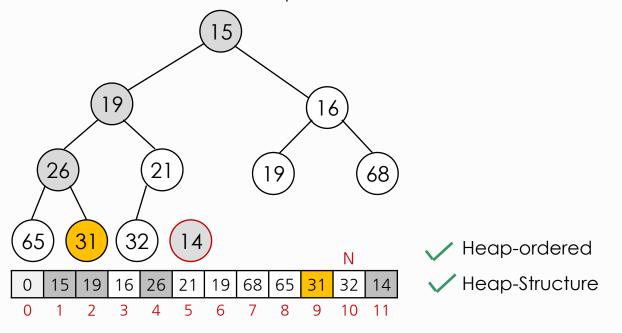


- heap-ordered?
- sink(): select one of two children and compare

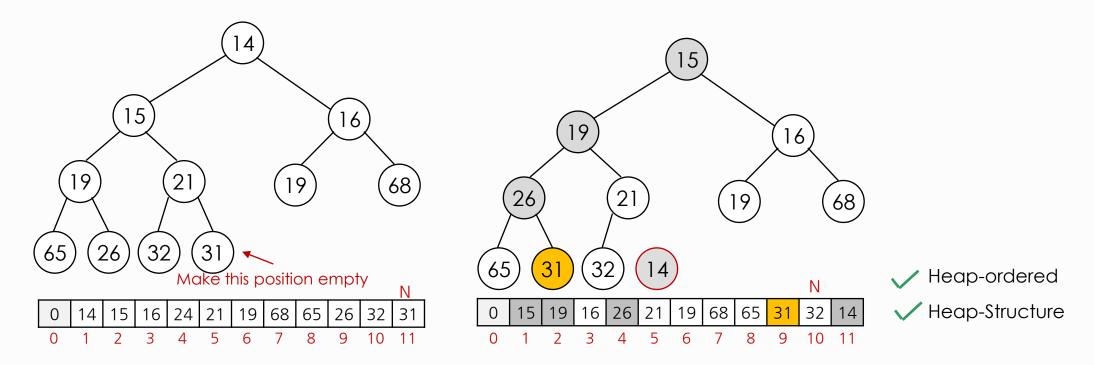




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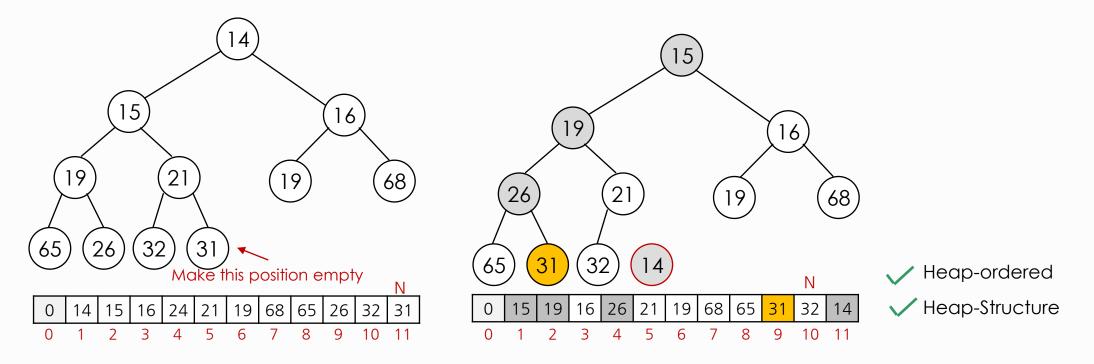


```
class BinHeap:
    def sink(self, i):
                                                               # start sink at node i
        while (i * 2) \leftarrow self.N:
                                                               # not bottom of tree yet?
            k = 2 * i
                                                               # left child
            if k < self.N and self.heap[k] > self.heap[k+1]:
                                                               # select one of two kids to compare
                k += 1
                                                               # right child is selected
            if not self.heap[i] > self.heap[k]: break
                                                               # break if node i and kid are heap-ordered
            self.swap(i, k)
                                                               # if not heap-ordered, swap i and k
            i = k
                                                               # i becomes k & continue sink process
```

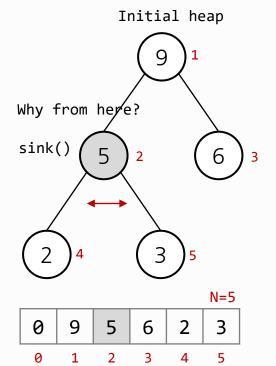


What do you expect from the following code snippet?

```
result = [ bh.delete() for x in range(bh.N) ]
print(' result:', result)
print('number of elements N:', bh.N)
print(' lengh of heap list:', len(bh.heap))
print(' heap list stored:', bh.heap)
```

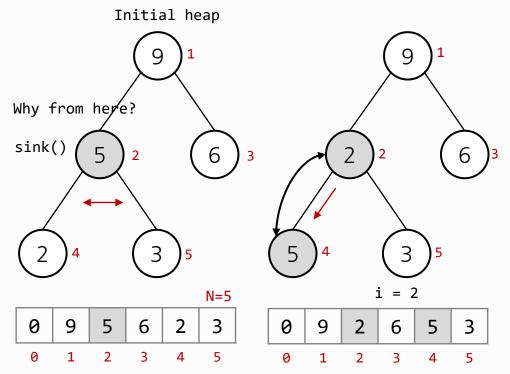


```
class BinHeap:
...
def buildHeap(self, arr):  # build heap from input arr list
    self.heap = [0] + arr[:]  # set the initial heap
    self.N = len(arr)  # set the size
    i = len(arr) // 2  # get the last internal node
    while i > 0:  # sink from the last internal node to root 1
        self.sink(i)
        i -= 1
```

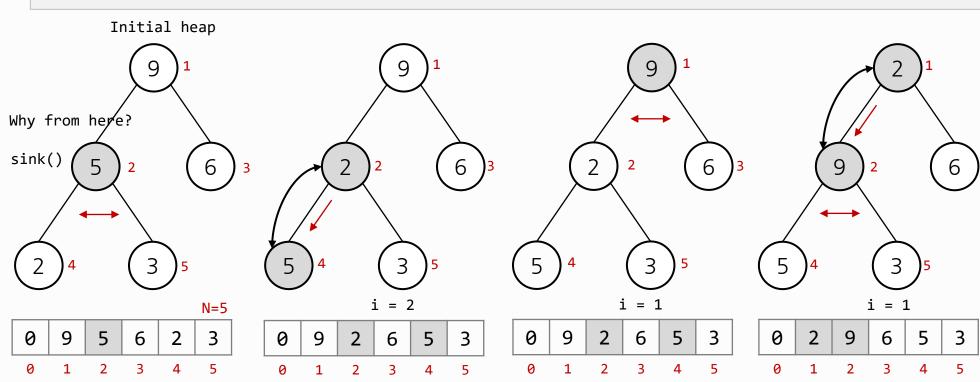


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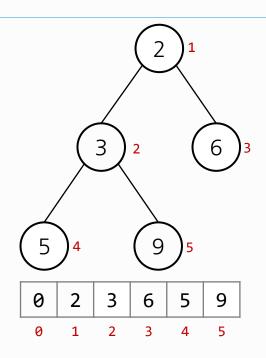


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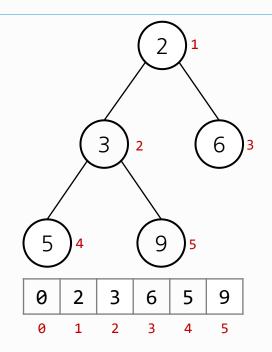


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class BinHeap:
       def buildHeap(self, arr):
                                            # build heap from input arr list
           self.heap = [0] + arr[:]
                                            # set the initial heap
           self.N = len(arr)
                                            # set the size
           i = len(arr) // 2
                                            # get the last internal node
           while i > 0:
                                            # sink from the last internal node to root 1
               self.sink(i)
               i -= 1
                                                                                                            heap-ordered
          Initial heap
Why from here?
sink()
                                    i = 2
                                                             i = 1
                                                                                      i = 1
                   N=5
                              9
     9
```

```
if __name__ == '__main__':
   bh = BinHeap()
    bh.buildHeap([9, 5, 6, 2, 3])
    print('number of elements N:', bh.N)
    print(' lengh of heap list:', len(bh.heap))
    print(' heap list stored:', bh.heap)
    bh.draw()
    print('\ninserting: 7 - already heap-ordered')
    bh.insert(7)
```

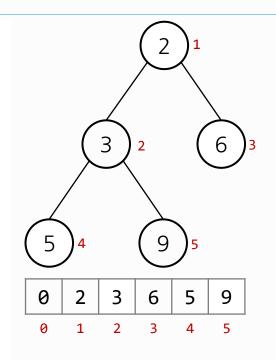


```
if name == ' main ':
   bh = BinHeap()
    bh.buildHeap([9, 5, 6, 2, 3])
    print('number of elements N:', bh.N)
    print(' lengh of heap list:', len(bh.heap))
    print(' heap list stored:', bh.heap)
   bh.draw()
    print('\ninserting: 7 - already heap-ordered')
    bh.insert(7)
   bh.draw()
    print('\ninserting: 1 - swim up, become root')
    bh.insert(1)
    bh.draw()
```



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    print('\ninserting: 1 - swim up, become root')
   bh.insert(1)
   bh.draw()
   print('\ndeleting root to sort - heap depleted')
   bh sorted = [ bh.delete() for x in range(bh.N) ]
    print('bh sorted:', bh sorted)
    print('number of elements N:', bh.N)
    print(' lengh of heap list:', len(bh.heap))
    print(' heap list stored:', bh.heap)
```

```
number of elements N: 5
 lengh of heap list: 6
   heap list stored: [0, 2, 3, 6, 5, 9]
inserting: 7 - already heap-ordered
inserting: 1 - swim up, become root
deleting root to sort - heap depleted
bh sorted: [1, 2, 3, 5, 6, 7, 9]
number of elements N: 0
 lengh of heap list: 1
   heap list stored: [0]
```



heap elements are deleted need to change not to delete to have .

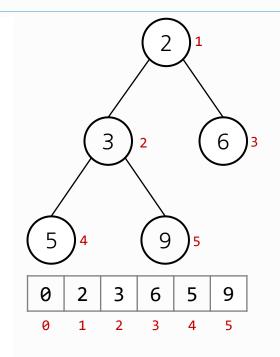
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if name == ' main ':
   bh = BinHeap()
    bh.buildHeap([9, 5, 6, 2, 3])
    print('number of elements N:', bh.N)
    print(' lengh of heap list:', len(bh.heap))
    print(' heap list stored:', bh.heap)
   bh.draw()
    print('\ninserting: 7 - already heap-ordered')
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    bh sorted = [ bh.delete() for x in range(bh.N) ]
    print('bh sorted:', bh sorted)
   print('number of elements N:', bh.N)
    print(' lengh of heap list:', len(bh.heap))
    print(' heap list stored:', bh.heap)
```

```
deleting root to sort - heap depleted
bh_sorted: [1, 2, 3, 5, 6, 7, 9]

number of elements N: 0
  lengh of heap list: 8
  heap list stored: [0, 9, 7, 6, 5, 3, 2, 1]
```

```
number of elements N: 5
 lengh of heap list: 6
   heap list stored: [0, 2, 3, 6, 5, 9]
inserting: 7 - already heap-ordered
inserting: 1 - swim up, become root
deleting root to sort - heap depleted
bh_sorted: [1, 2, 3, 5, 6, 7, 9]
number of elements N: 0
 lengh of heap list: 1
```

heap list stored: [0]



heap elements are deleted need to change not to delete to have .

학습 정리

- 1) 힙(Heap)에서 swim() 메소드는 노드를 move up할 때 사용하고 sink() 메소드는 노드를 move down 할 때 사용한다
- 2) 힙(Heap)에서 root를 연속적으로 삭제한 node를 list로 만들면, 정렬된 list가 된다.

3) Min-Heap으로 Heapsort를 진행하면 내림차순으로 정렬되고, Max-Heap으로 Heapsort를 진행하면 올림차순으로 정렬된다.

