



DÉVELOPPEMENT DE SYSTÈMES CRITIQUES AVEC LA MÉTHODE EVENT-B LA VALIDATION D'UN MODÈLE EVENT-B AVEC PROB

3A cursus ingénieurs - Mention Sciences du Logiciel

m CentraleSupelec - Université Paris-Saclay - 2024/2025



OUTLINE

- Introduction
- Model-checking
- Model-checking with ProB plugin
- Conclusion about ProB plugin

Back to the begin - Back to the outline



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- There are two main proof activities in the **Event-B** method:
 - 1. the proof of consistency used to show that the events of a machine preserve the invariant,
 - 2. the proof of refinement used to show that one machine is a valid refinement of another.



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 - the Rodin platform generates the list of proof obligations (PO)
 - the Atelier-B plugin is an automatic prover
- In some cases, the most complex **POs** are not proved automatically and *must be proved interactively*.



HISTORY OF FORMAL VERIFICATION METHODS

Before...

- Software code was sequential
- Properties were expressed in First-Order Predicate Logic
- Theorem provers → partial/total correctness
- Hardly automated → semi-decidable (e.g. B/Event-B Method)



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After 80's

- Software is concurrent and reactive
- Properties are expressed in Temporal Logic
- Solving accurate properties like safety, liveness, fairness...
- Push-Button → decidable (e.g. Model Checking)



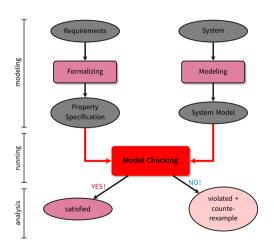
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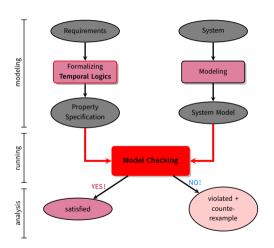


PRINCIPLE OF MODEL-CHECKING





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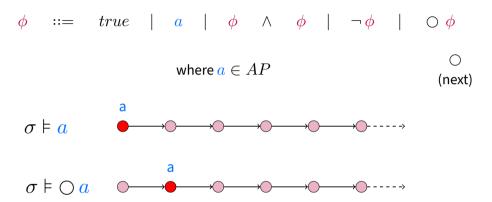
PROPOSITIONAL LOGIC

 ϕ ::= true | a | ϕ \wedge ϕ | $\neg \phi$

where $a \in AP$

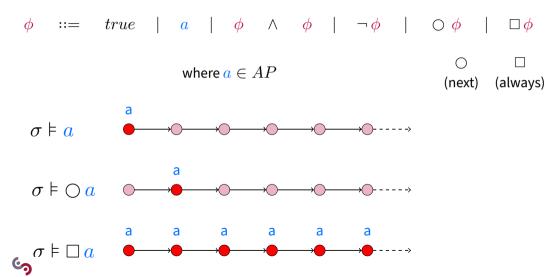


PROPOSITIONAL LINEAR TEMPORAL LOGIC

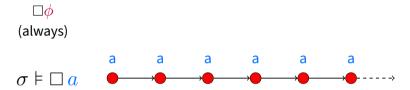




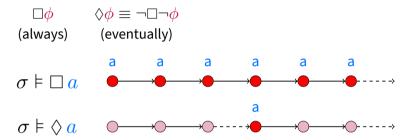
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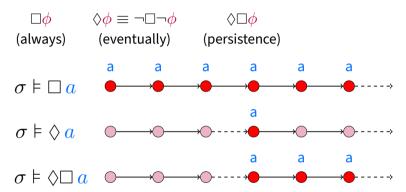
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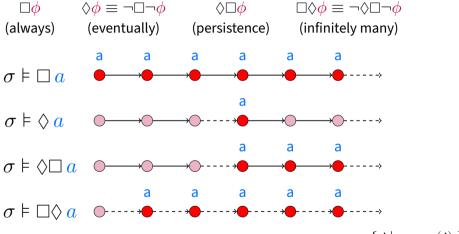














- Safety:
 - mutual exclusion :

 $\Box \neg (crit_1 \wedge crit_2)$

elevator:

 $\Box(moving \Rightarrow doors_{closed})$

traffic light:

 $\Box(yellow \Rightarrow \bigcirc red)$



- Safety:
 - mutual exclusion :
 - elevator:
 - traffic light:
- Liveness:
 - progress:
 - response:
 - termination:

- $\Box \neg (crit_1 \wedge crit_2)$
- $\Box(moving \Rightarrow doors_{closed})$
 - $\Box(yellow \Rightarrow \bigcirc red)$

- $\lozenge \, progress$
- $\Box(try_to_send \Rightarrow \Diamond delivered)$
 - $\Diamond \Box terminated$



- Safety:
 - cooling:
 - alarm:
 - saving:

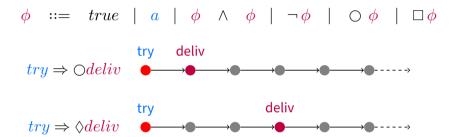
- nuclear plant
- $\Box \neg (temp_{high} \land cooling_{low})$
 - $\Box(temp_{high} \Rightarrow alarm)$
 - $\Box(temp_{high} \Rightarrow \bigcirc react_{low})$



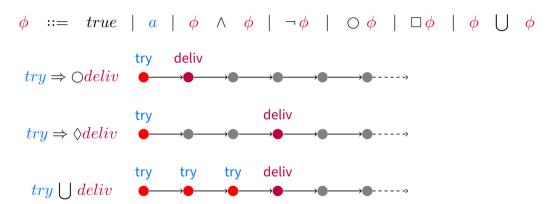
- Safety:
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- Liveness:
 - reactivity:
 - temperature:

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 - nuclear plant
 - $\Box \Diamond \ react_{high}$
 - $\Box(react_{low} \Rightarrow \Diamond temp_{low})$











$$\phi ::= true \mid a \mid \phi \land \phi \mid \neg \phi \mid \bigcirc \phi \mid \Box \phi \mid \phi \bigcup \phi$$

$$try \Rightarrow \bigcirc deliv$$

$$try \Rightarrow \Diamond deliv$$

$$try \Rightarrow \Diamond deliv$$

$$try \downarrow deliv$$



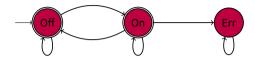
 $\lozenge \phi \equiv \mathsf{true} \cup \phi$

 $\Diamond \phi \equiv \text{true} \cup \phi$

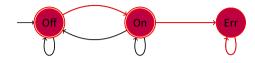


and

 $\Box \phi \equiv \neg \Diamond \neg \phi$



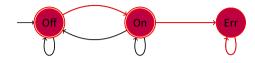




have a path $\pi = OffOn \, Err \, Err \, Err \, ... = OffOn \, Err^{\omega}$

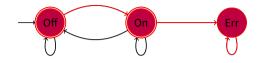
•
$$\pi \vDash Off$$





have a path $\pi = OffOn \ Err \ Err \ Err \ \dots = OffOn \ Err^{\omega}$ $\bullet \ \pi \ \vDash \ Off, \qquad \qquad \text{but } \pi \not \vDash \ On$

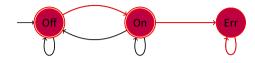




have a path
$$\pi = OffOn \ Err \ Err \ Err \ \dots = OffOn \ Err^{\omega}$$

• $\pi \models Off$, but $\pi \not\models On$,





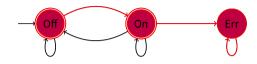
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• $\pi \vDash Off$,

but $\pi \nvDash On$,

• $\pi \vDash \bigcirc On$





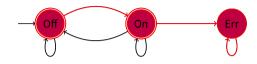
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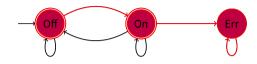
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•
$$\pi \vDash (Off \lor On) \cup Err$$





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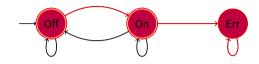
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$$\pi \vDash \Box(Err \Rightarrow \bigcirc Err)$$





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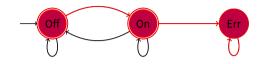
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$$\pi \vDash (Off \lor On) \cup Err$$

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$$\pi \vDash \Box(Err \Rightarrow \Box Err)$$

so
$$\pi \vDash \neg On$$





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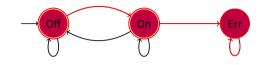
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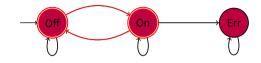
$$\pi \models \bigcirc \bigcirc \Box Err$$

so $\pi \vDash \neg On$

(persistence)



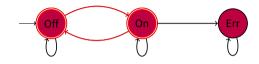




have a path $\pi = Off On \ Off On \ Off \dots = (Off On)^{\omega}$

•
$$\pi \stackrel{?}{\vDash} (Off \lor On) \cup Err$$

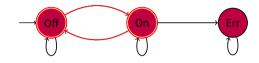




have a path $\pi = Off On \, Off On \, Off \dots = (Off On)^{\omega}$

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- $\pi \nvDash (Off \lor On) \cup Err$
- $\pi \stackrel{?}{\vDash} \Diamond Err \Rightarrow ((Off \lor On) \cup Err)$



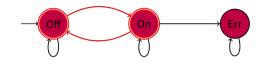


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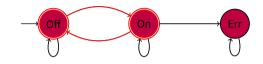


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 $(infinitely\, many)$





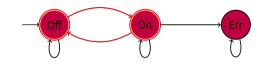
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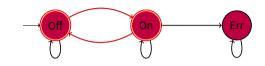
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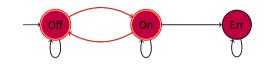
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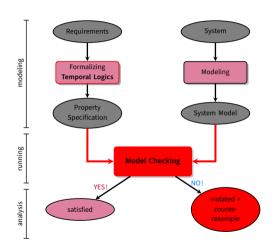
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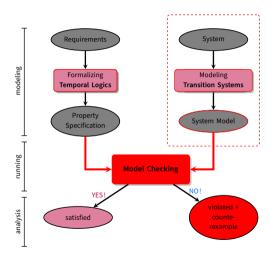
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SYSTEM MODELING





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TRANSITION SYSTEMS

- model to describe the behaviour of systems
- digraphs where nodes represent states, and edges represent transitions
- states
 - the current colour of a traffic light: red, green, orange.

- transitions ("state change")
 - a switch from one colour to another



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 - hardware: the current value of the registers + the input bits
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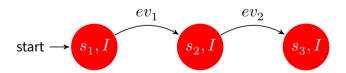


- An Event-B specification contains :
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 - invariant properties (first order predicates logic)



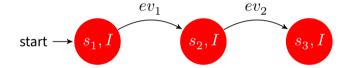


- An Event-B specification contains :
 - a state (data, sets, relationships, ...)
 - invariant properties (first order predicates logic)
 - transitions (initialisation and events) to update the state (substitutions)





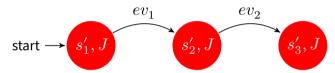
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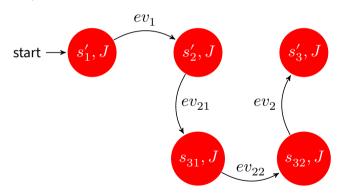
 Refining a specification consists of enriching it and reformulating it with another more concrete specification.





THE REFINEMENT OF AN EVENT-B MODEL

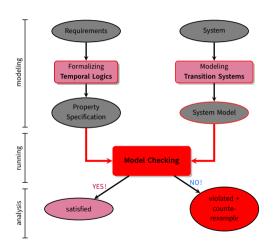
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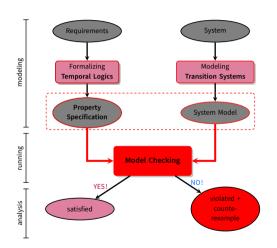
Behavior refinement (events)

PROPERTY SPECIFICATION





PROPERTY SPECIFICATION





INVARIANTS, SAFETY AND LIVENESS PROPERTIES

- Safety properties → "nothing bad should happen"
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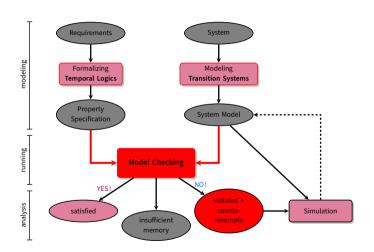


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- Safety properties are complemented by Liveness properties
 - that require some progress
 - that assert: "something good" will happen eventually
 - e.g. Eventually: $\Diamond crit_1 \land \Diamond crit_2$



MODEL CHECKING PROCESS





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1. Modeling phase

- Model the system under consideration into a formal representation
- Formalize the property to check using a temporal logic



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MODEL CHECKING PROCESS

1. Modeling phase

- Model the system under consideration into a formal representation
- Formalize the property to check using a temporal logic

2. Running phase

- run automatically the model checker to check the validity of the property in the model
- 3. Analysis phase (3 cases)
 - property satisfied : check next property (if any)
 - property violated :
 - analyze generated counterexample by simulation
 - modify the model and repeat the entire procedure
 - out of memory: try to reduce the model (abstraction) and try again





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- ✓ in case of property violation, a counter-example is provided



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- ✓ in case of property violation, a counter-example is provided
- ✓ sound and interesting mathematical foundations



- ✓ widely applicable (hardware, software, protocol systems, ...)
- ✓ potential "push-button" technology (software-tools)
- ✓ rapidly increasing industrial interest
- ✓ in case of property violation, a counter-example is provided
- ✓ sound and interesting mathematical foundations
- ✓ not biased to the most possible scenarios (such as testing)





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OUTLINE

- Introduction
- Model-checking
- Model-checking with ProB plugin
- Conclusion about ProB plugin

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ProB Main Page



 ProB is an animator, constraint solver and model checker for the Event-B Method.

ProB Main Page o



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ProB Main Page •



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- ProB's animation features allow developers to control and validate the behavior of their specifications.
- Animation features are useful for infinite state machines, not for verification, but for debugging and testing.

ProB Main Page •





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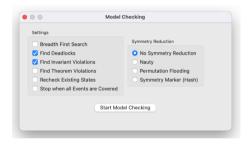
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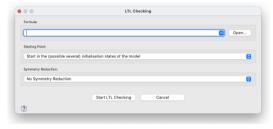


- The ProB plugin allows automatic verification of the consistency of Event-B machines through animation and model checking.
- For exhaustive model verification, the given sets must be limited to finite sets.
 - allows ProB to browse through the reachable states of the machine.
- The ProB plugin graphically displays a counterexample when it discovers a property violation.



THE PROB PLUGIN





- Tutorial Rodin First Step •
- Tutorial First Model Checking •
- LTL Model Checking •



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- As the interactive proof process can be quite long, the ProB plugin can be used as a complement to the interactive proof.
- Some errors will be discovered sooner and designers will waste less effort proving incorrect POs.



THANK YOU

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