



DÉVELOPPEMENT DE SYSTÈMES CRITIQUES AVEC LA MÉTHODE EVENT-B LA VALIDATION D'UN MODÈLE EVENT-B AVEC PROB

3A cursus ingénieurs - Mention Sciences du Logiciel

m CentraleSupelec - Université Paris-Saclay - 2024/2025



OUTLINE

- Introduction
- Model-checking
- Model-checking with ProB plugin
- Conclusion about ProB plugin

Back to the begin - Back to the outline



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 - 1. the proof of consistency used to show that the events of a machine preserve the invariant,
 - 2. the proof of refinement used to show that one machine is a valid refinement of another.



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- In the Rodin platform, proof activities are supported by tools, such as the Atelier-B plugin.
 - the Rodin platform generates the list of proof obligations (PO)
 - the Atelier-B plugin is an automatic prover
- In some cases, the most complex **POs** are not proved automatically and *must be proved interactively*.



HISTORY OF FORMAL VERIFICATION METHODS

Before...

- Software code was sequential
- Properties were expressed in First-Order Predicate Logic
- Theorem provers → partial/total correctness
- Hardly automated → semi-decidable (e.g. B/Event-B Method)



HISTORY OF FORMAL VERIFICATION METHODS

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After 80's

- Software is concurrent and reactive
- Properties are expressed in Temporal Logic
- Solving accurate properties like safety, liveness, fairness...
- Push-Button → decidable (e.g. Model Checking)

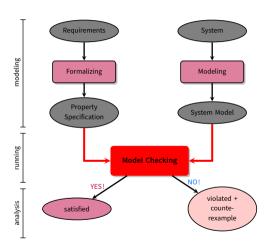
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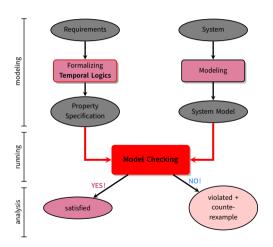


PRINCIPLE OF MODEL-CHECKING





PRINCIPLE OF MODEL-CHECKING





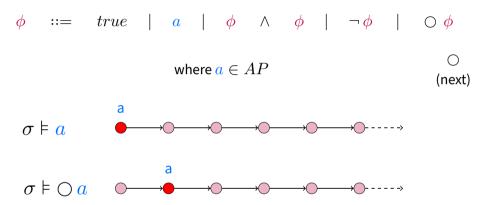
PROPOSITIONAL LOGIC

 ϕ ::= $true \mid a \mid \phi \land \phi \mid \neg \phi$

where $a \in AP$

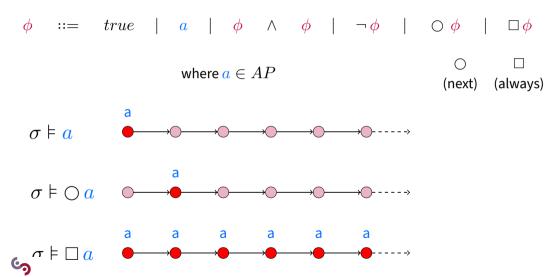


PROPOSITIONAL LINEAR TEMPORAL LOGIC



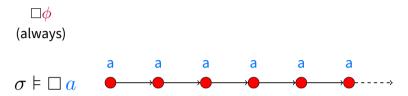


PROPOSITIONAL LINEAR TEMPORAL LOGIC

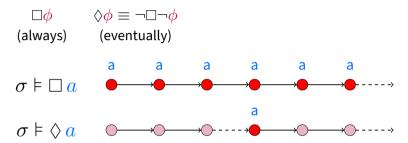


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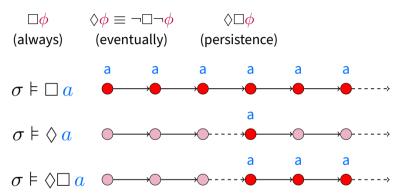
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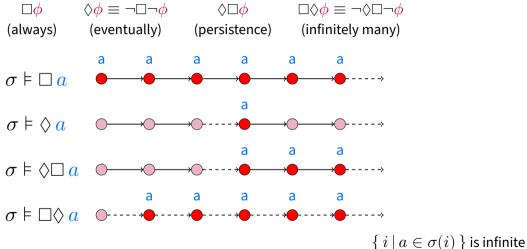














- Safety:
 - mutual exclusion :

 $\Box \neg (crit_1 \land crit_2)$

elevator:

 $\Box(moving \Rightarrow doors_{closed})$

traffic light:

 $\Box(yellow \Rightarrow \bigcirc red)$



- Safety:
 - mutual exclusion :
 - elevator:
 - traffic light:
- Liveness:
 - progress:
 - response:
 - termination:

- $\Box \neg (crit_1 \wedge crit_2)$
- $\Box(moving \Rightarrow doors_{closed})$
 - $\Box(yellow \Rightarrow \bigcirc red)$

- $\lozenge \, progress$
- $\Box(try_to_send \Rightarrow \Diamond delivered)$
 - $\Diamond \Box terminated$



- Safety: nuclear plant
 - cooling:
 - alarm:
 - saving:

- $\Box \neg (temp_{high} \land cooling_{low})$
 - $\Box(temp_{high} \Rightarrow alarm)$
 - $\Box(temp_{high} \Rightarrow \bigcirc react_{low})$



- Safety:
 - cooling:
 - alarm:
 - saving:

- Liveness :
 - reactivity:
 - temperature:

- nuclear plant
- $\Box \neg (temp_{high} \land cooling_{low})$
 - $\Box(temp_{high} \Rightarrow alarm)$
 - $\Box(temp_{high} \Rightarrow \bigcirc react_{low})$
 - nuclear plant
 - $\Box \Diamond \ react_{high}$
 - $\Box(react_{low} \Rightarrow \Diamond temp_{low})$

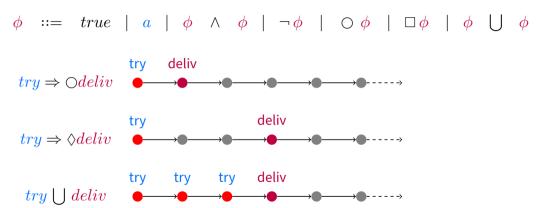


$$\phi ::= true \mid a \mid \phi \land \phi \mid \neg \phi \mid \bigcirc \phi \mid \Box \phi$$

$$try \Rightarrow \bigcirc deliv \qquad try \qquad deliv$$

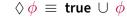
$$try \Rightarrow \Diamond deliv \qquad deliv$$











$$\phi ::= true \mid a \mid \phi \land \phi \mid \neg \phi \mid \bigcirc \phi \not \mapsto \phi \quad \bigcirc \phi$$

$$try \Rightarrow \bigcirc deliv$$

$$try \Rightarrow \Diamond deliv$$

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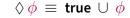
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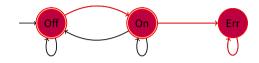


and

 $\Box \phi \equiv \neg \Diamond \neg \phi$



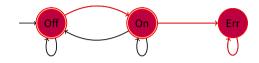




have a path $\pi = Off On \, Err \, Err \, Err \, \dots = Off \, On \, Err^\omega$

•
$$\pi \vDash Off$$

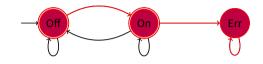




have a path
$$\pi = OffOn \ Err \ Err \ Err \ \dots = OffOn \ Err^{\omega}$$

$$\bullet \ \pi \ \models \ Off, \qquad \qquad \text{but } \pi \not \models \ On$$



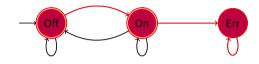


have a path
$$\pi = OffOn \ Err \ Err \ Err \ \dots = OffOn \ Err^{\omega}$$

• $\pi \models Off$, but $\pi \not\models On$,

so $\pi \vDash \neg On$





have a path $\pi = Off\,On\,Err\,Err\,Err\,Err\,\dots = Off\,On\,Err^\omega$

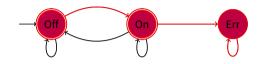
• $\pi \models Off$,

but $\pi \nvDash On$,

• $\pi \vDash \bigcirc On$

so $\pi \vDash \neg On$





have a path $\pi = Off\,On\,Err\,Err\,Err\,... = Off\,On\,Err^\omega$

•
$$\pi \models Off$$
,

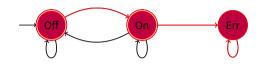
but
$$\pi \nvDash On$$
,

•
$$\pi \vDash \bigcirc On$$

•
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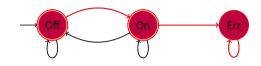
•
$$\pi \vDash \bigcirc On$$

•
$$\pi \vDash \bigcirc \bigcirc Err$$

•
$$\pi \vDash (Off \lor On) \cup Err$$

so $\pi \vDash \neg On$





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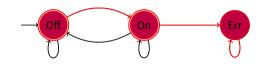
•
$$\pi \vDash \bigcirc \bigcirc Err$$

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•
$$\pi$$
 \vDash $\Box(Err \Rightarrow \bigcirc Err)$

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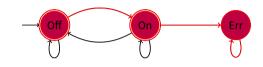
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$$\pi \vDash (Off \lor On) \cup Err$$

•
$$\pi \vDash \Box(Err \Rightarrow \bigcirc Err)$$

•
$$\pi \vDash \Box(Err \Rightarrow \Box Err)$$



 $so \pi \models \neg On$



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•
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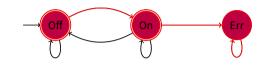
•
$$\pi \vDash \Box(Err \Rightarrow \Box Err)$$

•
$$\pi \models \Diamond \Box Err$$

(persistence)

so $\pi \models \neg On$

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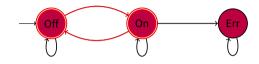




have a path $\pi = Off On \ Off On \ Off \dots = (Off On)^{\omega}$

•
$$\pi \stackrel{?}{\vDash} (Off \lor On) \cup Err$$





have a path $\pi = Off On \, Off On \, Off \dots = (Off On)^{\omega}$

• $\pi \nvDash (Off \vee On) \cup Err$





have a path $\pi = OffOn OffOn Off... = (OffOn)^{\omega}$

- $\pi \nvDash (Off \lor On) \cup Err$ $\pi \vDash \Diamond Err \Rightarrow ((Off \lor On) \cup Err)$

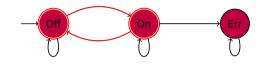




have a path $\pi = Off On \ Off On \ Off \dots = (Off On)^{\omega}$

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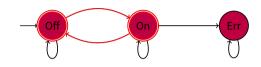




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- $\bullet \ \pi \, \vDash \, \Box(On \vee Off)$
- $\pi \stackrel{?}{\vDash} \Box \Diamond On \wedge \Box \Diamond Off$

 $as \pi \nvDash \Diamond Err$

 $(infinitely\, many)$



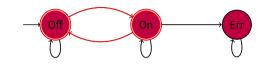


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- $\pi \vDash \Box(On \lor Off)$
- $\pi \vDash \Box \Diamond On \land \Box \Diamond Off$







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•
$$\pi \vDash \Box (On \lor Of f)$$

•
$$\pi \vDash \Box \Diamond On \land \Box \Diamond Off$$

$$\bullet \ \pi \stackrel{?}{\vDash} \Diamond \Box On \lor \Diamond \Box Off$$

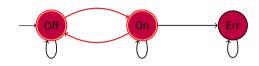
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V

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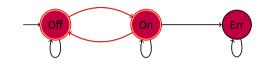
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$$\pi \nvDash \Diamond \Box On \lor \Diamond \Box Off$$

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(infinitely many)

(persistence)





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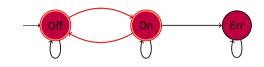
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$$\pi \nvDash \Diamond \Box On \lor \Diamond \Box Off$$

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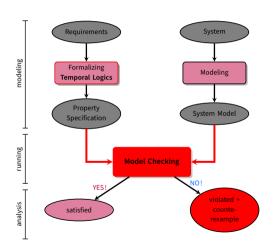
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 $(infinitely\, many)$

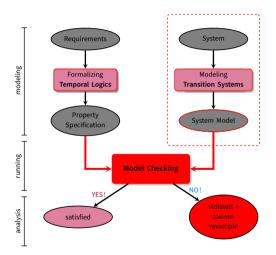
(persistence)

SYSTEM MODELING





SYSTEM MODELING





TRANSITION SYSTEMS

- model to describe the behaviour of systems
- digraphs where nodes represent states, and edges represent transitions
- states
 - the current colour of a traffic light: red, green, orange.

- transitions ("state change")
 - a switch from one colour to another



TRANSITION SYSTEMS

- model to describe the behaviour of systems
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 - hardware: the current value of the registers + the input bits
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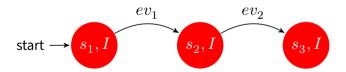


- An Event-B specification contains:
 - a state (data, sets, relationships, ...)
 - invariant properties (first order predicates logic)



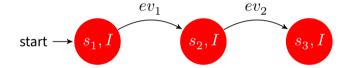


- An Event-B specification contains :
 - a state (data, sets, relationships, ...)
 - invariant properties (first order predicates logic)
 - transitions (initialisation and events) to update the state (substitutions)





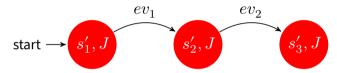
THE REFINEMENT OF AN EVENT-B MODEL





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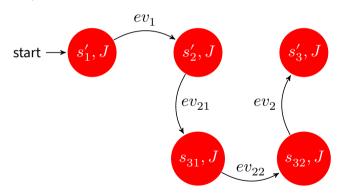
 Refining a specification consists of enriching it and reformulating it with another more concrete specification.





THE REFINEMENT OF AN EVENT-B MODEL

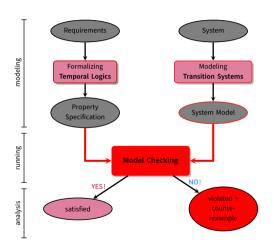
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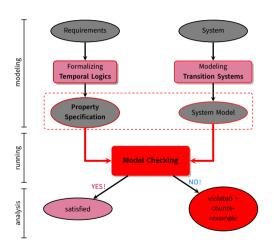
Behavior refinement (events)

PROPERTY SPECIFICATION





PROPERTY SPECIFICATION





INVARIANTS, SAFETY AND LIVENESS PROPERTIES

- Safety properties → "nothing bad should happen"
 - Typical safety property: mutual exclusion property
 - the bad thing (having > 1 process in the critical section) never occurs



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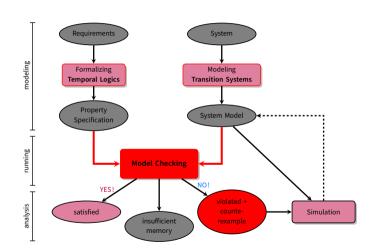


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 - that is given by a condition ϕ over AP
 - requires that condition ϕ holds for all states (reachable ones)
 - e.g. for mutual exclusion property $\phi = \neg (crit_1 \wedge crit_2)$
- Safety properties are complemented by Liveness properties
 - that require some progress
 - that assert: "something good" will happen eventually
 - e.g. Eventually: $\Diamond crit_1 \land \Diamond crit_2$



MODEL CHECKING PROCESS





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1. Modeling phase

- Model the system under consideration into a formal representation
- Formalize the property to check using a temporal logic



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2. Running phase

run automatically the model checker to check the validity of the property in the model



MODEL CHECKING PROCESS

1. Modeling phase

- Model the system under consideration into a formal representation
- Formalize the property to check using a temporal logic

2. Running phase

- run automatically the model checker to check the validity of the property in the model
- 3. Analysis phase (3 cases)
 - property satisfied : check next property (if any)
 - property violated :
 - analyze generated counterexample by simulation
 - modify the model and repeat the entire procedure
 - out of memory: try to reduce the model (abstraction) and try again



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- ✓ not biased to the most possible scenarios (such as testing)





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OUTLINE

- Introduction
- Model-checking
- Model-checking with ProB plugin
- Conclusion about ProB plugin

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ProB Main Page •



 ProB is an animator, constraint solver and model checker for the Event-B Method.

ProB Main Page

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ProB Main Page •



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- ProB's animation features allow developers to control and validate the behavior of their specifications.
- Animation features are useful for infinite state machines, not for verification, but for debugging and testing.

ProB Main Page





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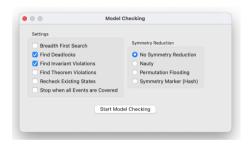
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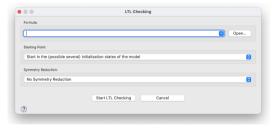


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 - allows ProB to browse through the reachable states of the machine.
- The ProB plugin graphically displays a counterexample when it discovers a property violation.



THE PROB PLUGIN





- Tutorial Rodin First Step •
- Tutorial First Model Checking •
- LTL Model Checking •



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- As the interactive proof process can be quite long, the **ProB plugin** can be used as a complement to the interactive proof.
- Some errors will be discovered sooner and designers will waste less effort proving incorrect POs.



THANK YOU

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