

- The magnitude of resultant of two vectors \vec{A} and \vec{B} ,
 $R = \sqrt{A^2 + B^2 + 2AB \cos \theta}$
- The direction (β) of resultant vector \vec{R} with respect to vector \vec{A} ,
 $\beta = \tan^{-1} \left(\frac{B \sin \theta}{A + B \cos \theta} \right)$
- The scalar product of two vectors \vec{A} and \vec{B} ,
 $\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$
- Vector product of two vectors \vec{A} and \vec{B} ,
 $\vec{A} \times \vec{B} = |\vec{A}| |\vec{B}| \sin \theta \hat{n}$
- The components of two vectors \vec{A} and \vec{B} ;
 $\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$
and, $\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$
Then $\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$
and angle, $\cos \theta = \frac{\vec{A} \cdot \vec{B}}{|\vec{A}| |\vec{B}|} = \frac{A_x B_x + A_y B_y + A_z B_z}{|\vec{A}| |\vec{B}|}$
 $|\vec{A}| = \sqrt{A_x^2 + A_y^2 + A_z^2}$
 $|\vec{B}| = \sqrt{B_x^2 + B_y^2 + B_z^2}$
- In vector resolution,
X-component of $\vec{A} = |\vec{A}| \cos \theta$
Y-Component of $\vec{A} = |\vec{A}| \sin \theta$
- The dot product of mutually perpendicular vectors,
 $\hat{i} \cdot \hat{j} = 0, \hat{j} \cdot \hat{k} = 0, \hat{k} \cdot \hat{i} = 0$
 $\hat{i} \cdot \hat{i} = 1, \hat{j} \cdot \hat{j} = 1, \hat{k} \cdot \hat{k} = 1$
- The cross product of mutually perpendicular vectors,
 $\hat{i} \times \hat{j} = \hat{k}, \hat{j} \times \hat{k} = \hat{i}, \hat{k} \times \hat{i} = \hat{j}$, reverses are negative in sign
 $\hat{i} \times \hat{i} = 0, \hat{j} \times \hat{j} = 0, \hat{k} \times \hat{k} = 0$



- The gravitational force, $F = G \frac{m_1 m_2}{r^2}$
 - The acceleration due to gravity, $g = \frac{GM}{R^2}$
 - The mean density of the earth, $\rho = \frac{3g}{4\pi GR}$
 - Acceleration due to gravity g at height h , $g' = g \left(1 - \frac{2h}{R} \right)$, for $h \ll R$
 - Acceleration due to gravity g at depth x , $g' = g \left(1 - \frac{x}{R} \right)$
 - Acceleration due to gravity g due to the rotation of the earth, $g' = g \left(1 - \frac{R \omega^2 \cos^2 \phi}{g} \right)$
 - The intensity of gravitational field, $E = \frac{GM}{r^2}$
 - The gravitational potential, $V = -\frac{GM}{r}$
 - Gravitational potential energy is, $U = -\frac{GMm}{r}$
 - Total gravitational energy,
 $T.E. = K.E. + P.E. = \frac{1}{2} m v^2 + \left(-\frac{GMm}{r} \right)$
 $v = \text{orbital velocity}$
 - Escape velocity, $v_e = \sqrt{2gR}$
 - Motion of satellite,
Orbital velocity, $v = R \sqrt{\frac{g}{R+h}}$
Time period, $T = \frac{2\pi}{R} \sqrt{\frac{(R+h)^3}{g}}$
Height, $h = \left(\frac{T^2 R^2 g}{4\pi^2} \right)^{1/3} - R$
 - The Schwarzschild radius of black hole is, $R_s = \frac{2GM}{c^2}$
- Heat gained or heat lost by a body,
i. $Q = m \Delta \theta$, (For same phase)
ii. $Q = mL$, (for same temperature)
 - Principle of calorimetry, Heat gained = Heat lost

- Stress = $\frac{\text{Force}}{\text{Area}} = \frac{F}{A}$
- Strain = $\frac{\text{Change in configuration}}{\text{original configuration}}$
- Longitudinal strain = $\frac{\text{Change in length}}{\text{Original length}} = \frac{\Delta L}{L} = \frac{e}{L}$
- Volumetric strain = $\frac{\text{Change in volume}}{\text{Original volume}} = \frac{\Delta V}{V}$
- Shear strain = angle of deviation from the original position = θ
- Hooke's law, Stress \propto strain
- Moduli of elasticity,
i. Young's modulus of elasticity,
 $Y = \frac{\text{Normal stress}}{\text{Longitudinal strain}} = \frac{FL}{Ae}$
ii. Bulk modulus of elasticity, $K = \frac{\text{Normal stress}}{\text{volume strain}} = \frac{-dP}{\Delta V}$
iii. Modulus of rigidity, $\eta = \frac{\text{tangential stress}}{\text{shear strain}} = \frac{F}{A\theta}$
- Total potential energy stored in the stretched wire,
 $W = \frac{1}{2} F \cdot e = \frac{1}{2} \text{ stress} \times \text{strain} \times \text{volume of wire}$
Energy density, $U = \frac{1}{2} \text{ stress} \times \text{strain}$. For a missile, we use, $\frac{1}{2} F \cdot e = \frac{1}{2} m v^2$
- The Poisson's ratio, $\sigma = \frac{\text{lateral strain}}{\text{longitudinal strain}} = \frac{-\Delta D/D}{\Delta L/L}$

Ritik Yadav

"If you found science boring then you are learning it from wrong teachers."

- Work done, $W = \vec{F} \cdot \vec{s} = F s \cos \theta$
- Kinetic energy, $E_k = \frac{1}{2} m v^2 = \frac{p^2}{2m}$
- Work energy theorem,
 $W = \text{change of kinetic energy} = \frac{1}{2} m v^2 - \frac{1}{2} m u^2$
- Gravitational potential energy, $E_p = mgh$
- Power,
 $P = \frac{\text{Work done}}{\text{Time taken}} = \frac{W}{t} = \vec{F} \cdot \vec{v} = F v \cos \theta$
- For explosion of a body,
 $\frac{E_1}{E_2} = \frac{m_1}{m_2}$ i.e., $E \propto \frac{1}{m}$
- Work done by frictional force,
 $W = \text{Frictional force} \times \text{displacement}$
- The angular displacement, $\theta = r$
- Angular velocity, $\omega = \frac{\text{angular displacement}}{\text{time taken}} = \frac{\theta}{t}$
- The relation of linear velocity and angular velocity: $v = r\omega$
- Angular acceleration, $\alpha = \frac{\text{angular velocity}}{\text{time taken}} = \frac{\omega}{t}$
- Let T , f and ω are related as, $\omega = 2\pi f$, $f = \frac{1}{T}$ and $\omega = \frac{2\pi}{T}$
- Centripetal acceleration, $\alpha = \frac{v^2}{r} = \omega^2 r$
- Centripetal force, $F = \frac{m v^2}{r} = m \omega^2 r$
- Motion in vertical circle,
i. At the lowest point, the maximum tension,
 $T_{\max} = \frac{m v^2}{r} + mg$
ii. At the highest point, the minimum tension,
 $T_{\min} = \frac{m v^2}{r} - mg$
iii. At horizontal diametrical points
 $T_{av} = \frac{m v^2}{r}$
- Motion of Cyclist, $\tan \theta = \frac{v^2}{rg}$
- Motion at Banked Road,
 $R \sin \theta = \frac{m v^2}{r}$, $R \cos \theta = mg$, $\tan \theta = \frac{v^2}{rg}$, $v_{\max} = \sqrt{\mu r g}$
- Motion of Conical Pendulum, $T \sin \theta = \frac{m v^2}{r}$
 $T \cos \theta = mg$, $\tan \theta = \frac{v^2}{rg}$ and $t = 2\pi \sqrt{\frac{l \cos \theta}{g}}$
- Rate of heat conduction, $\frac{dQ}{dt} = \frac{kA(\theta_1 - \theta_2)}{x}$
- Stefan's law, $E = \sigma T^4$ here,
 $E = \frac{Q/t}{A} = \frac{\text{Power radiated}}{\text{Surface area}} = \frac{P}{A}$
Then, $P = \sigma A T^4$
In general form, $P = e \sigma A T^4$, where e is called emissivity of a black body
- Stefan-Boltzmann law, $E = \sigma(T^4 - T_0^4)$,
For any black body, $P = e \sigma A (T^4 - T_0^4)$
- Surface temperature of the sun, $T = \left[\frac{P}{R \sigma} \right]^{1/4}$

- Equation of Motions,

Equations of motion in straight line	Equations of motion under gravity For downward motion	For upward motion
$v = u + at$	$v = u + gt$	$v = u - gt$
$s = ut + \frac{1}{2} at^2$	$h = ut + \frac{1}{2} gt^2$	$h = ut - \frac{1}{2} gt^2$
$v^2 = u^2 + 2as$	$v^2 = u^2 + 2gh$	$v^2 = u^2 - 2gh$
- Distance travelled in n^{th} second,
 $s_n^{\text{th}} = u + \frac{a}{2} (2n - 1)$
- Relative velocity of object A with respect to object B,
 $\vec{v}_{AB} = \vec{v}_A - \vec{v}_B$
Similarly, relative velocity of B with respect to A,
 $\vec{v}_{BA} = \vec{v}_B - \vec{v}_A$
- Relative velocity when two objects are inclined,
 $v_{AB} = \sqrt{v_A^2 + v_B^2 - 2v_A v_B \cos \theta}$
Direction of resultant,
 $\tan \beta = \frac{v_B \sin \theta}{v_A - v_B \cos \theta}$
- A projectile when fired horizontally from certain height,
Time of flight, $T = \sqrt{\frac{2H}{g}}$
Horizontal range, $R = u \sqrt{\frac{2H}{g}}$
Velocity at any instant, $v = \sqrt{u^2 + g^2 t^2}$
and direction of velocity with respect to x direction,
 $\theta = \tan^{-1} \left(\frac{at}{u} \right)$
- Projectile fired at an angle with the horizontal,
Time of flight, $T = \frac{2u \sin \theta}{g}$
Horizontal range, $R = \frac{u^2 \sin 2\theta}{g}$
Maximum height attained, $H = \frac{u^2 \sin^2 \theta}{2g}$
Maximum horizontal range, $R_{\max} = \frac{u^2}{g}$ at $\theta = 45^\circ$
- Lens formula, $\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$
- Lens maker's formula, $\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$
- Linear magnification, $m = \frac{h_i}{h_o} = \frac{v}{u}$
- Power of a lens, $P = \frac{1}{f \text{ (in metre)}}$
- R.I. of a prism, $\mu = \frac{\sin \left(\frac{A + \delta_m}{2} \right)}{\sin \frac{A}{2}}$
- For a small angled prism, angle of deviation, $\delta = (\mu - 1) A$
- $\frac{\sin i}{\sin r} = \frac{\mu_2}{\mu_1} = \mu^2$
- Lateral displacement, $d = \frac{t \sin (i - r)}{\cos r}$
- Apparent shift, $d = t \left(1 - \frac{1}{\mu} \right)$
- Refractive index = $\frac{\text{Real depth}}{\text{Apparent depth}}$
- $\mu = \frac{1}{\sin c}$, c is the critical angle
- Relationship between focal length and radius of curvature, $f = \frac{R}{2}$
- Mirror formula, $\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$
- Magnification, $m = \frac{h_i}{h_o} = \frac{v}{u}$
- Boyle's law, $PV = \text{constant}$, or, $P_1 V_1 = P_2 V_2$
- Charles' law, $\frac{V}{T} = \text{constant}$, or, $\frac{V_1}{T_1} = \frac{V_2}{T_2}$
- Equation of state, $\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$
- Ideal gas equation, $PV = nRT$, where R is the universal gas constant
- The Boltzmann's constant, $k_B = \frac{R}{N_A} = 1.38 \times 10^{-23} \text{ J K}^{-1}$
- Rms speed of gas molecules,
 $c_{rms} = \sqrt{\frac{c_1^2 + c_2^2 + c_3^2 + \dots + c_N^2}{N}}$
- Pressure exerted by a gas, $P = \frac{1}{3} \frac{m}{V} c^2$
- The rms speed of gas molecules, $c_{rms} = \sqrt{\frac{3P}{\rho}}$
- The mean kinetic energy per molecule of a gas,
 $E_k = \frac{1}{2} m \bar{c}^2 = \frac{3}{2} k_B T$
- Avogadro's number,
 $N_A = \frac{\text{Molar mass}}{\text{Mass of 1 molecule}} = 6.023 \times 10^{23}$
- Number of mole of substance, $n = \frac{\text{total mass of gas}}{\text{molar mass}} = \frac{m}{M}$
- Variation of rms speeds,
 $\frac{c_1}{c_2} = \sqrt{\frac{T_1}{T_2}}$, $\frac{c_1}{c_2} = \sqrt{\frac{\rho_2}{\rho_1}}$ and $\frac{c_1}{c_2} = \sqrt{\frac{M_2}{M_1}}$

1. Quantization of charge, $q = \pm ne$

2. The electric field intensity, $E = \frac{F}{q_0}$

3. Electric force, $F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$

1. Electric field intensity, $E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$

2. Electric flux, $\phi = EA \cos \theta$

3. Gauss's theorem, $\phi = \frac{q}{\epsilon}$

4. Electric field intensity due to a charged hollow conducting sphere of radius R ,

i. $E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$ (outside the sphere)

ii. $E = \frac{1}{4\pi\epsilon_0} \frac{q}{R^2}$ (on the sphere)

iii. $E = 0$ (inside sphere)

5. Electric field intensity due to a plane sheet of charges,

$$E = \frac{\sigma}{2\epsilon_0}$$

6. Electric field intensity due to a line charge, $E = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r}$

1. Electric current (I) = $\frac{dq}{dt} = \frac{Ne}{t}$, where N is total number of charge particles.

2. Drift Velocity, $I = v_d e n A$, Where, v_d is drift velocity of electron.

3. Current density (J): $J = \frac{I}{A} = nev_d$

4. Combination of resistors:

i. Series combination: $R = R_1 + R_2 + R_3 + \dots$

ii. Parallel combination, $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$

iii. The equivalent resistance of n equal resistors of equal resistance (r) when connected in series is $R = nr$.

iv. The equivalent resistance of n equal resistors of equal resistance (r) when connected in parallel, $R = \frac{r}{n}$.

v. The ratio of n identical resistors of equal resistance when connected in series to parallel is,

$$\frac{R_{\text{series}}}{R_{\text{parallel}}} = n^2$$

5. Variation of resistance with temperature:

i. The resistance at $\theta^\circ\text{C}$, $R_\theta = R_0(1 + \alpha\theta)$, where

R_0 = resistance of conductor at 0°C and

α = temperature coefficient of resistance = $\frac{R_\theta - R_0}{R_0\theta}$

6. Conversion of galvanometer into ammeter

i. Internal resistance of ammeter is very small, $R_a = \frac{GS}{G+S}$

ii. Value of shunt is, $S = \frac{I_a G}{I - I_a}$

7. Conversion of galvanometer into voltmeter:

i. Internal resistance is very large; $R_v = R + G$

ii. Value of multiplier, $R = \frac{V}{I_g} - G$

8. Electric power: $P = \frac{qV}{t} = IV = I^2 R = \frac{V^2}{R}$

9. Electric energy: $(E) = I^2 R t = V I t = P t = \frac{V^2 t}{R}$

10. Emf, terminal potential and internal resistance:

i. Relation, $E = V + Ir$

ii. Efficiency of a source of emf, $\eta = \frac{P_o}{P_i} = \frac{V}{E} = \frac{R}{R+r}$

11. Terminal potential difference,

i. While charging, $V > E$, $E = V - Ir$

ii. While discharging, $V < E$, $E = V + Ir$

1. Capacitance, $C = \frac{q}{V}$

2. Capacitance of sphere, $C = 4\pi\epsilon_0 k R = 4\pi\epsilon_0 R$

3. Capacitance of a parallel plate capacitor, $C = \frac{\epsilon_0 A}{d}$

4. Equivalent capacitance of series combination,

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

5. Equivalent capacitance of parallel combination,

$$C = C_1 + C_2 + C_3$$

6. Energy stored in a charged capacitor, $U = \frac{1}{2} \frac{q^2}{C} = \frac{1}{2} C V^2$

7. Common potential, $V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2}$

8. Dielectric constant, $K = \frac{\epsilon}{\epsilon_0}$

1. The radius (R) of nucleus, $R = R_0 A^{\frac{1}{3}}$, where $R_0 = 1.2 \times 10^{-15} \text{ m}$

2. Volume (V) of nucleus, $V = \frac{4}{3} \pi R_0^3 A$

3. Einstein's mass energy relation, $m = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}}$

4. Mass defect (Δm), $(Zm_p + (A - Z)m_n) - M$.

5. Packing fraction = $\frac{\Delta m}{A}$

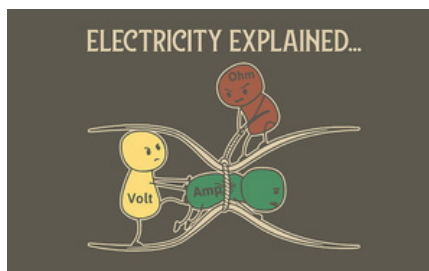
6. Binding energy (BE) = $\Delta m \times 931 \text{ MeV}$, [$\therefore 1 \text{ amu} = 931 \text{ MeV}$]

7. Binding energy per nucleon = $\frac{B.E.}{A}$

8. Equation for nuclear reaction is, ${}_Z^A X + {}_Z^A Y \rightarrow {}_Z^A X' + {}_Z^A Y' + Q$, where Q is energy released or observed.

9. Example of nuclear fission, ${}_{92}^{235}\text{U} + {}_0^1\text{n} \rightarrow {}_{92}^{236}\text{U} \rightarrow {}_{56}^{141}\text{Ba} + {}_{36}^{92}\text{Kr} + 3{}_0^1\text{n} + Q$, $Q = 200 \text{ MeV}$

10. Example of nuclear fusion, ${}_1^2\text{H} + {}_1^2\text{H} \rightarrow {}_2^4\text{He} + Q$, $Q = 24 \text{ MeV}$



Rifik Yadav
“~_(_)_/”

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Values of Physical Constants

Charge of electron	$= 1.6 \times 10^{-19} \text{ C}$
Mass of electron	$= 9.1 \times 10^{-31} \text{ kg}$
Permittivity of free space (ϵ_0)	$= 8.854 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

1. Cauchy's formula, $\mu = A + \frac{B}{\lambda^2} + \frac{C}{\lambda^4}$

2. Angular dispersion, $\delta_v - \delta_r = (\mu_v - \mu_r) A$

3. Dispersive power, $\omega = \frac{\delta_v - \delta_r}{\delta} = \frac{\mu_v - \mu_r}{\mu - 1}$, where $\mu = \frac{\mu_v + \mu_r}{2}$

4. For achromatism, $\frac{\omega_1}{f_1} + \frac{\omega_2}{f_2} = 0$, $\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2}$

5. Rayleigh's scattering law, $I \propto \frac{1}{\lambda^4}$

1. Relationship between C , F and K ,

$$\frac{C}{100} = \frac{F - 32}{180} = \frac{K - 273}{100}$$

2. The coefficient of linear, superficial and cubical expansions, $\alpha = \frac{\Delta l}{l_1 \Delta \theta}$, $\beta = \frac{\Delta A}{A_1 \Delta \theta}$ and $\gamma = \frac{\Delta V}{V_1 \Delta \theta}$

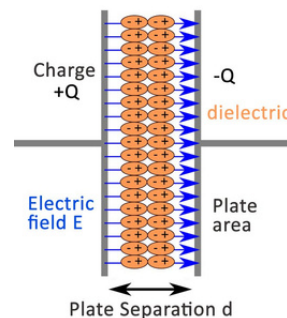
3. Relation between α , β and γ be, $\alpha = \frac{\beta}{3} = \frac{\gamma}{3}$

4. Tension on a wall due to the expansion of rod, $F = Y A \alpha (\theta_2 - \theta_1)$

5. The relation of real expansivity, apparent expansivity and expansivity of vessel, $\gamma_r = \gamma_a + \gamma_v$, since $\gamma = 3\alpha$

6. Variation of density with temperature,

$$\rho_t = \frac{\rho_0}{1 + \gamma \Delta \theta} = \rho_0 (1 - \gamma \Delta \theta)$$



Values of Physical Constants

Coefficient linear expansion of aluminium	$= 2.4 \times 10^{-5} \text{ K}^{-1}$
Coefficient linear expansion of brass	$= 2.0 \times 10^{-5} \text{ K}^{-1}$
Cubical expansivity of benzene	$= 1.2 \times 10^{-3} \text{ K}^{-1}$
Cubical expansivity of wood	$= 1.5 \times 10^{-4} \text{ K}^{-1}$
Density of mercury (ρ)	$= 13600 \text{ kg/m}^3$
Linear expansivity of brass (α)	$= 2 \times 10^{-5} \text{ K}^{-1}$
Linear expansivity of glass	$= 1.8 \times 10^{-6} \text{ K}^{-1}$
Linear expansivity of steel	$= 1.2 \times 10^{-5} \text{ K}^{-1}$
Cubical expansivity of mercury	$= 1.8 \times 10^{-4} \text{ K}^{-1}$
Young's modulus of steel	$= 2 \times 10^{11} \text{ N/m}^2$
Specific heat capacity of ice	$= 2100 \text{ J/kg}^\circ\text{K}^{-1}$
Specific heat capacity of water	$= 4200 \text{ J/kg}^\circ\text{K}^{-1}$
Specific latent heat of melting of ice	$= 3.36 \times 10^5 \text{ J/kg}^\circ\text{K}^{-1}$
Specific latent heat of vaporization	$= 2.268 \times 10^6 \text{ J/kg}^\circ\text{K}^{-1}$

