$$T_p^*/\mathrm{PGL}_2(\mathbb{Q}_p) = \bullet$$