

Green University of Bangladesh

Department of Computer Science and Engineering (CSE) Semester: (Spring, Year: 2025), B.Sc. in CSE (Day)

Graph Coloring using Backtracking

Course Title: Artificial Intelligence Lab Course Code: CSE-316 Section: 221-D22

Students Details

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Lab Report Status	
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1 Introduction

Graph coloring is an important problem in graph theory and combinatorial optimization. It involves assigning colors to vertices of a graph such that no two adjacent vertices share the same color. This report presents an implementation of graph coloring using a backtracking approach.

2 Objectives

- Understand the graph coloring problem.
- Implement a backtracking solution to assign colors to vertices.
- Determine whether a valid coloring exists for a given number of colors.

3 Procedure

- 1. Accept user input for the number of vertices, edges, and available colors.
- 2. Construct the adjacency matrix representation of the graph.
- 3. Use a backtracking approach to attempt coloring the graph.
- 4. Display the color assignment if a valid coloring is found.
- 5. Indicate failure if the graph cannot be colored with the given colors.

4 Code

```
def is_safe(graph, vertex, colors, color, V):
    for i in range(V):
        if graph[vertex][i] == 1 and colors[i] == color:
            return False
    return True

def graph_coloring_util(graph, k, colors, vertex, V):
    if vertex == V:
        return True

for color in range(1, k + 1):
    if is_safe(graph, vertex, colors, color, V):
        colors[vertex] = color
        if graph_coloring_util(graph, k, colors, vertex + 1, V):
            return True
        colors[vertex] = 0
    return False
```

```
def solve_graph_coloring():
    print("Enter the number of vertices (N), edges (M), and colors (K):")
    N, M, K = map(int, input().split())
    graph = [[0] * N for _ in range(N)]
    print("\nEnter the edges (u v):")
    for _ in range(M):
        u, v = map(int, input().split())
        graph[u][v] = 1
        graph[v][u] = 1
    colors = [0] * N
    if graph_coloring_util(graph, K, colors, 0, N):
        print(f"\nColoring Possible with {K} Colors")
        print(f"Color Assignment: {colors}")
    else:
        print(f"\nColoring Not Possible with {K} Colors")
if __name__ == "__main__":
    solve_graph_coloring()
```

5 Output

```
idontbyte@TANVEER Lab Report 3 % python3 graph_coloring.py
Enter the number of vertices (N), edges (M), and colors (K):
4 5 3

Enter the edges (u v):
0 1
0 2
1 2
1 3
2 3

Coloring Possible with 3 Colors
Color Assignment: [1, 2, 3, 1]
```

Figure 1: Example Output of the Graph Coloring Algorithm

6 Conclusion

The graph coloring problem is effectively solved using backtracking. The algorithm successfully determines whether a valid coloring is possible for a given number of colors. The results demonstrate the efficiency of backtracking in solving constraint satisfaction problems.

7 GitHub Repository

The complete implementation can be found in the following repository: