

# Towards pure functional agent-based simulation

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## Abstract

So far, the pure functional paradigm hasn't got much attention in Agent-Based Simulation (ABS) where the dominant programming paradigm is object-orientation, with Java, Python and C++ being its most prominent representatives. We claim that pure functional programming using Haskell is very well suited to implement complex, real-world agent-based models and brings with it a number of benefits. To show that we implemented the seminal Sugarscape model in Haskell in our library *FrABS* which allows to do ABS the first time in the pure functional programming language Haskell. To achieve this we leverage the basic concepts of ABS with functional reactive programming using Yampa. The result is a surprisingly fresh approach to ABS as it allows to incorporate discrete time-semantics similar to Discrete Event Simulation and continuous time-flows as in System Dynamics. In this paper we will show the novel approach of functional reactive ABS through the example of the SIR model, discuss implications, benefits and best practices.

## Index Terms

Agent-Based Simulation, Functional Programming, Functional Reactive Programming, Haskell

## I. INTRODUCTION

In this paper we investigate how agent-based simulation can be approached from a pure functional direction using the programming language Haskell. So far no in-depth research has been conducted on this subject because so far agent-based simulation was always thought of as being best implemented in object-oriented languages like C++, Java and Python. As will become apparent throughout this paper, a pure functional approach needs to approach various concepts of ABS very differently which leads to a very different approach to ABS but makes concepts which were blurred and implicit very explicit and clear. This paper's major contribution is that it reveals these implicit concepts and provides a formal view on ABS and a pure functional implementation of these concepts.

## II. BACKGROUND

In this background section we will introduce the concepts behind functional programming and functional reactive programming as they form the very foundation of our approach to pure functional Agent-Based Simulation. Note that both fields build on each other and are vast and complex. A more in-depth handling of both subjects are out of scope of this paper and we refer the reader to additional resources where appropriate. In this paper we try to avoid too much technical details and present only the fundamental concepts behind our approach.<sup>1</sup>

### A. Functional Programming

MacLennan [1] defines Functional Programming as a methodology and identifies it with the following properties (amongst others):

- 1) It is programming without the assignment-operator.
- 2) It allows for higher levels of abstraction.
- 3) It allows to develop executable specifications and prototype implementations.
- 4) It is connected to computer science theory.
- 5) Suitable for Parallel Programming.
- 6) Algebraic reasoning.

[2] defines Functional Programming as "a computer programming paradigm that relies on functions modelled on mathematical functions." Further they explicate that it is

- in Functional programming programs are combinations of expressions
- Functions are *first-class* which means they can be treated like values, passed as arguments and returned from functions.

[1] makes the subtle distinction between *applicative* and *functional* programming. Applicative programming can be understood as applying values to functions where one deals with pure expressions:

<sup>1</sup>For interested readers, we refer to our companion paper TODO: cite / refer to existing repository. In it we introduce the functional programming community to ABS by deriving our approach step-by-step by implementing an agent-based implementation of the SIR model. In this companion paper we assume good knowledge and beyond of the fundamental concepts of FP and FRP and provide in-depth discussions of technical details.

- Value is independent of the evaluation order.
- Expressions can be evaluated in parallel.
- Referential transparency.
- No side effects.
- Inputs to an operation are obvious from the written form.
- Effects to an operation are obvious from the written form.

Note that applicative programming is not necessarily unique to the functional programming paradigm but can be emulated in an imperative language e.g. C as well. Functional programming is then defined by [1] as applicative programming with *higher-order* functions. These are functions which operate themselves on functions: they can take functions as arguments, construct new functions and return them as values. This is in stark contrast to the *first-order* functions as used in applicative or imperative programming which just operate on data alone. Higher-order functions allow to capture frequently recurring patterns in functional programming in the same way like imperative languages captured patterns like GOTO, while-do, if-then-else, for. Common patterns in functional programming are the map, fold, zip, operators. So functional programming is not really possible in this way in classic imperative languages e.g. C as you cannot construct new functions and return them as results from functions <sup>2</sup>.

The equivalence in functional programming to the ; operator of imperative programming which allows to compose imperative statements is function composition. Function composition has no side-effects as opposed to the imperative ; operator which simply composes destructive assignment statements which are executed after another resulting in side-effects. At the heart of modern functional programming is monadic programming which is polymorphic function composition: one can implement a user-defined function composition by allowing to run some code in-between function composition - this code of course depends on the type of the Monad one runs in. This allows to emulate all kind of effectful programming in an imperative style within a pure functional language. Although it might seem strange wanting to have imperative style in a pure functional language, some problems are inherently imperative in the way that computations need to be executed in a given sequence with some effects. Also a pure functional language needs to have some way to deal with effects otherwise it would never be able to interact with the outside-world and would be practically useless. The real benefit of monadic programming is that it is explicit about side-effects and allows only effects which are fixed by the type of the monad - the side-effects which are possible are determined statically during compile-time by the type-system. Some general patterns can be extracted e.g. a map, zip, fold over monads which results in polymorphic behaviour - this is the meaning when one says that a language is polymorphic in its side-effects.

TODO: explain closures TODO: explain continuations TODO: explain monads (explicit about side-effects), what are effects  
 TODO: explain the term 'pure'

## B. Functional Reactive Programming

TODO: explain streams TODO: Yampa, BearRiver, Dunai

Functional Reactive Programming (FRP) is a paradigm for programming hybrid systems which combine continuous and discrete components. Time is explicitly modelled: there is a continuous and synchronous time flow.

there have been many attempts to implement FRP in frameworks which each has its own pro and contra. all started with fran, a domain specific language for graphics and animation and at yale FAL, Frob, Fvision and Fruit were developed. The ideas of them all have then culminated in Yampa which is the reason why it was chosen as the FRP framework. Also, compared to other frameworks it does not distinguish between discrete and synchronous time but leaves that to the user of the framework how the time flow should be sampled (e.g. if the sampling is discrete or continuous - of course sampling always happens at discrete times but when we speak about discrete sampling we mean that time advances in natural numbers: 1,2,3,4,... and when speaking of continuous sampling then time advances in fractions of the natural numbers where the difference between each step is a real number in the range of [0..1])

[?] give a good overview of Yampa and FRP. Quote: "The essential abstraction that our system captures is time flow". Two *semantic* domains for progress of time: continuous and discrete.

The first implementations of FRP (Fran) implemented FRP with synchronized stream processors which was also followed by [?]. Yampa is but using continuations inspired by Fudgets. In the stream processors approach "signals are represented as time-stamped streams, and signal functions are just functions from streams to streams", where "the Stream type can be implemented directly as (lazy) list in Haskell...":

<sup>2</sup>Object-Oriented languages like Java let you to partially work around this limitation but are still far from *pure* functional programming.

”A major design goal for FRP is to free the programmer from ‘presentation’ details by providing the ability to think in terms of ‘modeling’. It is common that an FRP program is concise enough to also serve as a specification for the problem it solves” [?]. This quotation describes exactly one of the strengths using FRP in ACE

### III. AGENT-BASED SIMULATION DEFINED

Agent-Based Simulation (ABS) is a methodology to model and simulate a system where the global behaviour may be unknown but the behaviour and interactions of the parts making up the system is of knowledge. Those parts, called agents, are modelled and simulated out of which then the aggregate global behaviour of the whole system emerges. Epstein [3] identifies ABS to be especially applicable for analysing “*spatially distributed systems of heterogeneous autonomous actors with bounded information and computing capacity*”. Thus in the line of the simulation methods *Statistic*<sup>†</sup>, *Markov*<sup>‡</sup>, *System Dynamics*<sup>§</sup>, *Discrete Event*<sup>¶</sup>, ABS is the most recent development and the most powerful one as it subsumes its predecessors features and goes beyond:

- Linearity & Non-Linearity<sup>†‡¶</sup> - the dynamics of the simulation can exhibit both linear and non-linear behaviour.
- Time<sup>†§¶</sup> - agents act over time, time is also the source of pro-activity.
- States<sup>‡§¶</sup> - agents encapsulate some state which can be accessed and changed during the simulation.
- Feedback-Loops<sup>§¶</sup> - because agents act continuously and their actions influence each other and themselves, feedback-loops are the norm in ABS.
- Heterogeneity<sup>¶</sup> - although agents can have same properties like height, sex,... the actual values can vary arbitrarily between agents.
- Interactions - agents can be modelled after interactions with an environment or other agents, making this a unique feature of ABS, not possible in the other simulation models.
- Spatiality & Networks - agents can be situated within e.g. a spatial (discrete 2d, continuous 3d,...) or network environment, making this also a unique feature of ABS, not possible in the other simulation models.

#### A. Deriving central concepts

Before we can approach a functional view on ABS, we need to identify the central concepts of ABS on a more technical level. Unfortunately there does not exist a commonly agreed technical definition of ABS but we can draw inspiration from the closely related field of Multi-Agent Systems (MAS). It is important to understand that MAS and ABS are two different fields where in MAS the focus is much more on technical details implementing a system of interacting intelligent agents within a highly complex environment with the focus primarily on solving AI problems.

1) *Agents*: The central aspect of ABS is the concept of an agent. In MAS [4], [5] agents can be informally defined as:

- They are uniquely addressable entities with some internal state over which they have full, exclusive control.
- They are situated in an environment which they can observe and act upon.
- They can interact with other agents which are situated in the same environment.
- They are pro-active which means they can initiate actions on their own e.g. change their internal state, interact with other agents, create new agents, terminate themselves, interact with the environment,...

2) *Environment*: The other important concept is the one of an environment. In MAS [4], [5] one distinguishes between different types of environments (based on [6]):

- Accessible vs. inaccessible - in an accessible environment an agent can obtain complete and accurate information from the environment. In ABS environments are generally implemented as being accessible.
- Deterministic vs. non-deterministic - in a deterministic environment the actions of an agent have no uncertainty and are guaranteed to have a single effect. In ABS environments are generally implemented as being deterministic.
- Static vs. dynamic - a static environment only changes due to the agents actions whereas a dynamic one has other processes which operate on it. In ABS both static and dynamic environments are common.
- Discrete vs. continuous - a discrete environment has only a fixed, finite number of states and actions whereas a continuous is potentially unlimited. In ABS both discrete and continuous environments are common.

Note that in MAS the focus is much more on the environment rather than on the agents where the environment is almost always a highly complex one and the agents may intelligently act on it. In ABS the focus is rather on the agents and their interactions where the environment plays a role but is not of central interest as it is almost always deterministic.

#### B. Deriving a formal view

In order to explore how we can implement an ABS in a pure functional way we need a sufficiently formal view on it. This will help us expressing the concepts in Haskell as formal, mathematical specifications translate easily into functional programming. There exists formalisations of MAS [4] but unfortunately they are not very helpful in our context as its formalization is

tailored much more towards optimizing, intelligent and reasoning behaviour of agents within a highly complex and uncertain environment. What we need for ABS is a more agent-oriented approach:

- 1) An ABS is a simulation over time in which time is advanced either in discrete or continuous time-steps where discrete means advancing by a natural number time-delta and continuous by a real-valued time-delta. So we have a potentially infinite stream of time-steps starting at  $t=0$  advancing by some fixed time-delta.
- 2) At each time-step all agents are allowed to act which is the source of their proactivity because it allows them to initiate actions on their own. Of course such actions are always time-dependent - be it explicitly like executing actions *after* a specific time, or be it implicit like executing actions every time-delta - but this is the only way of implementing proactivity in a computer system.
- 3) In each step an agent should be able to read/write the environment. TODO: orderings? when are changes visible?
- 4) In each step an agent should be able to interact with other agents through communication.
- 5) In each step an agent should be able to update its internal state.
- 6) Depending on its type, the environment must also be allowed to act in each time-step.
- 7) In general we can thus see an agent to exhibit both time-dependent and reactive behaviour: it can act continuously or discretely, depending on how the time is advanced and exhibit reactive behaviour which means it can react to changing environment or agents.
- 8) The interactions between agents their update-state and environment forms a feedback as the state of time  $t_i$  forms the input state on which to act at time-step  $t_{i+1}$

#### IV. A FUNCTIONAL APPROACH

Due to the fundamentally different approaches of pure Functional Programming (pure FP) an ABS needs to be implemented fundamentally different as well compared to traditional object-oriented approaches (OO). We face the following challenges:

- 1) How can we represent an Agent?  
In OO the obvious approach is to map an agent directly onto an object which encapsulates data and provides methods which implement the agents actions. Obviously we don't have objects in pure FP thus we need to find a different approach to represent the agents actions and to encapsulate its state.
- 2) How can we represent state in an Agent?  
In the classic OO approach one represents the state of an Agent explicitly in mutable member variables of the object which implements the Agent. As already mentioned we don't have objects in pure FP and state is immutable which leaves us with the very tricky question how to represent state of an Agent which can be actually updated.
- 3) How can we implement proactivity of an Agent?  
In the classic OO approach one would either expose the current time-delta in a mutable variable and implement time-dependent functions or ignore it at all and assume agents act on every step. At first this seems to be not a big deal in pure FP but when considering that it is yet unclear how to represent Agents and their state, which is directly related to time-dependent and reactive behaviour it raises the question how we can implement time-varying and reactive behaviour in a purely functional way.
- 4) How can we implement the agent-agent interaction?  
In the classic OO approach Agents can directly invoke other Agents methods which makes direct Agent interaction *very* easy. Again this is obviously not possible in pure FP as we don't have objects with methods and mutable state inside.
- 5) How can we represent an environment and its various types?  
In the classic OO approach an environment is almost always a mutable object which can be easily made dynamic by implementing a method which changes its state and then calling it every step as well. In pure FP we struggle with this for the same reasons we face when deciding how to represent an Agent, its state and proactivity.
- 6) How can we implement the agent-environment interaction?  
In the classic OO approach agents simply have access to the environment either through global mechanisms (e.g. Singleton or simply global variable) or passed as parameter to a method and call methods which change the environment. Again we don't have this in pure FP as we don't have objects and globally mutable state.
- 7) How can we step the simulation?  
In the classic OO approach agents are run one after another (with being optionally shuffled before to uniformly distribute the ordering) which ensures mutual exclusive access in the agent-agent and agent-environment interactions. Obviously in pure FP we cannot iteratively mutate a global state.

##### A. Agent representation, state and proactivity

Whereas in imperative programming (the OO which we refer to in this paper is built on the imperative paradigm) the fundamental building block is the destructive assignment, in FP the building blocks are obviously functions which can be evaluated. Thus we have no other choice than to represent our Agents using a function which implements their behaviour. This

function must be time-aware somehow and allow us to react to time-changes and inputs. Fortunately there exists already an approach to time-aware, reactive programming which is termed Functional Reactive Programming (FRP). This paradigm has evolved over the year and current modern FRP is built around the concept of a signal-function which transforms an input-signal into an output-signal. An input-signal can be seen as a time-varying value. Signal-functions are implemented as continuations which allows to capture local state using closures. Modern FRP also provides feedback functions which provides convenient methods to capture and update local state from the previous time-step with an initial state provided at time = 0.

- time is represented using the FRP concept: Signal-Functions which are sampled at (fixed) time-deltas, the dt is never visible directly but only reflected in the code and read-only.
- no method calls = continuous data-flow instead

Viewing agent-agent interaction as simple method calls implies the following: - it takes no time - it has a synchronous and transactional character - an agent gives up control over its data / actions or at least there is always the danger that it exposes too much of its interface and implementation details. - agents equals objects, which is definitely NOT true. Agents

data-flow synchronous agent transactions

- still need transactions between two agents e.g. trading occurs over multiple steps (makeoffer, accept/refuse, finalize/abort)
- exactly define what TX means in ABS
- exclusive between 2 agents
- state-changes which occur over multiple steps and are only visible to the other agents after the TX has committed
- no read/write access to this state is allowed to other agents while the TX is active
- a TX executes in a single time-step and can have an arbitrary number of tx-steps
- it is easily possible using method-calls in OOP but in our pure functional approach it is not possible
- parallel execution is being a problem here as TX between agents are very easy with sequential
- an agent must be able to transact with as many other agents as it wants to in the same time-step
- no time passes between transactions = what we need is a 'all agents transact at the same time'
- basically we can implement it by running the SFs of the agents involved in the TX repeatedly with dt=0 until there are no more active TXs
- continuations (SFs) are perfectly suited for this as we can 'rollback' easily by using the SF before the TX has started

## B. Environment representation and interaction

pro-active vs. inactive read-only vs. read/write

no global shared mutable environment, having different options: - non-active read-only (SIR): no agent, as additional argument to each agent - pro-active read-only (?): environment as agent, broadcast environment updates as data-flow - non-active read/write (?): no agent, shared data as STM as additional argument to each agent - pro-active read/write (Sugarscape): environment as, shared data as STM as additional argument to each agent

## C. Stepping the simulation

- parallel update only, sequential is deliberately abandoned due to: - reality does not behave this way
- if we need transactional behaviour, can use STM which is more explicit
- it translates directly to a map which is very easy to reason about (sequential is basically a fold which is much more difficult to reason about)
- is more natural in functional programming
- it exists for 'transactional' reasons where we need mutual exclusive access to environment / other agents
- we provide a more explicit mechanism for this: Agent Transactions

## V. EXAMPLES

TODO: the main punch is that our approach combines the best of the three simulation methodologies: - SD part: it can represent continuous time (as well as discrete) with continuous data-flows from agents which act at the same time (parallel update), can express the formulas directly in code, there exists also a small EDSL for expressing SD in our approach, can guarantee reproducibility and no drawing of random-numbers in our approach- drawback over real SD: none known so far
- DES part: it can represent discrete time with events occurring at discrete points in time which cause an instant change in the system
- drawback over real DES: time does not advance discretely to the next event which results of course not in the performance of a real DES system
- ABS part: the entities of the system (=agents) can be heterogenous and pro-active in time and can have arbitrary neighbourhood (2d/3d discrete/continuous, network,...)
- drawback over classic ABS: none known so far

TODO: give examples of all 3 approaches: SD & ABS: SIR model, DES: simulation of a queuing system

## A. Library

In the course of the research for this paper we implemented the library *Chimera*<sup>3</sup> in Haskell which implements all the concepts introduced in this paper and allows to do ABS in a pure functional way in Haskell. As use-cases to drive the research and test our concepts we implemented a number of more or less well known examples from ABS, see Appendix A for a list of all the examples and the concepts used.

<sup>3</sup>The library is freely available on GitHub: <https://github.com/thalerjonathan/chimera>. It is planned that it will be put on Hackage in the future.

## VI. DISCUSSION

Our purely functional approach has a number of fundamental implications which change the way one has to think about agents and ABS in general as it makes a few concepts which were so far hidden or implicitly assumed, now explicit.

### A. Agents as Signals

Our approach of using signal-functions has the direct implication that we can view and implement agents as time-dependent signals. A time-dependent function should stay constant when time does not advance (when the system is stepped with time-delta of 0). For this to happen with our agents requires them to act only on time-dependent functions. TODO: further discussion using my work on agents as signals in the first draft on FrABS.

TODO: it doesn't make sense for an agent to act 'always', an agents behaviour needs to have some time-dependent parameter e.g. `doEvery 1.0`. If this is omitted then one makes one dependent directly on the Time-Delta.

### B. System Dynamics

Due to the parallel execution of the agents signal-functions, the ability to iterate the simulation with continuous time, the notion of continuous data-flow between agents and compile time guarantees of absence of non-deterministic side-effects and random-number generators allows us to directly express System Dynamic models. Each stock and flow becomes an agent and are connected using data-flows using hard-coded agent ids. The integrals over time which occur in a SD model are directly translated to pure functional code using the *integral* primitive of FRP - our implementation is then correct by definition. See Appendix TODO for an example which implements the SIR model (TODO: cite mckendrick) in SD using our continuous ABS approach.

## VII. CONCLUSIONS AND FUTURE WORK

### A. Advantages

- being explicit and polymorph about side-effects: can have 'pure' (no side-effects except state), 'random' (can draw random-numbers), 'IO' (all bets are off), STM (concurrency) agents
- hybrid between SD and ABS due to continuous time AND parallel dataFlow (parallel update-strategy)
- being update-strategy polymorph (TODO: this is just an assumption atm, need to prove this): 4 different update-strategies, one agent implementation
- parallel update-strategy: lack of implicit side-effects makes it work without any danger of data-interference
- recursive simulation - reasoning about correctness - reasoning about dynamics - testing with quickcheck much more convenient - expressivity: -> 1:1 mapping of SD to code: can express the SD formulas directly in code -> directly expressing state-charts in code

### B. Disadvantages

1) *Performance*: Performance is currently no where near imperative object-oriented implementations. The reason for this is that we don't have in-place updates of data-structures and make no use of references. This results in lots of copying which is simply not necessary in the imperative languages with implicit effects. Also it is much more difficult to reason about time and space in our approach. Thus we see performance clearly as the main drawback of the functional approach and the only real advantage of the imperative approach over our.

2) *Steep learning curve*: Our approach is quite advanced in three ways. First it builds on the already quite involved FRP paradigm. Second it forces one to think properly of time-semantics of the model, how to sample it, how small  $\Delta t$  should be and whether one needs super-sampling or not and if yes how many samples one should take. Third it requires to think about agent-interaction and update-strategies, whether one should use conversations which forces one to run sequentially or if one can run agents in parallel and use normal messaging which incurs a time-delay which in turn would need to be considered when setting the  $\Delta t$ .

### C. Future Work

TODO: what we need to show / future work - can we do DES? e.g. single queue with multiple servers? also specialist vs. generalist - reasoning about correctness: implement Gintis & Ionescous papers - reasoning about dynamics: implement Gintis & Ionescous papers

## ACKNOWLEDGMENTS

The authors would like to thank I. Perez, H. Nilsson, J. Greensmith for constructive comments and valuable discussions.

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## APPENDIX A EXAMPLES

In this appendix we give a list of all the examples we have implemented and discuss implementation details relevant <sup>4</sup>. The examples were implemented as use-cases to drive the development of *FrABS* and to give code samples of known models which show how to use this new approach. Note that we do not give an explanation of each model as this would be out of scope of this paper but instead give the major references from which an understanding of the model can be obtained.

We distinguish between the following attributes

- Implementation - Which style was used? Either Pure, Monadic or Reactive. Examples could have been implemented in all of them.
- Yampa Time-Semantics - Does the implemented model make use of Yampas time-semantics e.g. occasional, after,...? Yes / No.
- Update-Strategy - Which update-strategy is required for the given example? It is either Sequential or Parallel or both. In the case of Sequential Agents may be shuffled or not.
- Environment - Which kind of environment is used in the given example? Possibilities are 2D/3D Discrete/Continuous or Network. In case of a Parallel Update-Strategy, collapsing may become necessary, depending on the semantics of the model. Also it is noted if the environment has behaviour. Note that an implementation may also have no environment which is noted as None. Although every model implemented in *FrABS* needs to set up some environment, it is not required to use it in the implementation.
- Recursive - Is this implementation making use of the recursive features of *FrABS* Yes/No (only available in sequential updating)?
- Conversations - Is this implementation making use of the conversations features of *FrABS* Yes/No (only available in sequential updating)?

### A. *Sugarscape*

This is a full implementation of the famous Sugarscape model as described by Epstein & Axtell in their book [7]. The model description itself has no real time-semantics, the agents act in every time-step. Only the environment may change its behaviour after a given number of steps but this is easily expressed without time-semantics as described in the model by Epstein & Axtell <sup>5</sup>.

<b>Implementation</b>	Pure, Monadic
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Sequential, shuffling
<b>Environment</b>	2D Discrete, behaviour
<b>Recursive</b>	No
<b>Conversations</b>	Yes

### B. *Agent\_Zero*

This is an implementation of the *Parable 1* from the book of Epstein [8].

<b>Implementation</b>	Pure, Monadic
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Parallel, Sequential, shuffling
<b>Environment</b>	2D Discrete, behaviour, collapsing
<b>Recursive</b>	No
<b>Conversations</b>	No

### C. *Schelling Segregation*

This is an implementation of [9] with extended agent-behaviour which allows to study dynamics of different optimization behaviour: local or global, nearest/random, increasing/binary/future. This is also the only 'real' model in which the recursive features were applied <sup>6</sup>.

<sup>4</sup>The examples are freely available under <https://github.com/thalerjonathan/chimera/tree/master/examples>

<sup>5</sup>Note that this implementation has about 2600 lines of code which - although it includes both a pure and monadic implementation - is significant lower than e.g. the Java-implementation <http://sugarscape.sourceforge.net/> with about 6000. Of course it is difficult to compare such measures as we do not include *FrABS* itself into our measure.

<sup>6</sup>The example of Recursive ABS is just a plain how-to example without any real deeper implications.



<b>Implementation</b>	Pure
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Sequential, shuffling
<b>Environment</b>	2D Discrete
<b>Recursive</b>	Yes (optional)
<b>Conversations</b>	No

#### D. Prisoners Dilemma

This is an implementation of the Prisoners Dilemma on a 2D Grid as discussed in the papers of [10], [11] and TODO: cite my own paper on update-strategies.

TODO: implement

#### E. Heroes & Cowards

This is an implementation of the Heroes & Cowards Game as introduced in [12] and discussed more in depth in TODO: cite my own paper on update-strategies.

TODO: implement

#### F. SIRS

This is an early, non-reactive implementation of a spatial version of the SIRS compartment model found in epidemiology. Note that although the SIRS model itself includes time-semantics, in this implementation no use of Yampas facilities were made. Timed transitions and making contact was implemented directly into the model which results in contacts being made on every iteration, independent of the sampling time. Also in this sample only the infected agents make contact with others, which is not quite correct when wanting to approximate the System Dynamics model (see below). It is primarily included as a comparison to the later implementations (Fr\*SIRS) of the same model which make full use of *FrABS* and to see the huge differences the usage of Yampas time-semantics can make.

<b>Implementation</b>	Pure, Monadic
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Parallel, Sequential with shuffling
<b>Environment</b>	2D Discrete
<b>Recursive</b>	No
<b>Conversations</b>	No

#### G. Reactive SIRS

This is the reactive implementations of both 2D spatial and network (complete graph, Erdos-Renyi and Barbas-Albert) versions of the SIRS compartment model. Unlike SIRS these examples make full use of the time-semantics provided by Yampa and show the real strength provided by *FrABS*.

<b>Implementation</b>	Reactive
<b>Yampa Time-Semantics</b>	Yes
<b>Update-Strategy</b>	Parallel
<b>Environment</b>	2D Discrete, Network
<b>Recursive</b>	No
<b>Conversations</b>	No

#### H. System Dynamics SIR

This is an emulation of the System Dynamics model of the SIR compartment model in epidemiology. It was implemented as a proof-of-concept to show that *FrABS* is able to implement even System Dynamic models because of its continuous-time and time-semantic features. Connections between stocks & flows are hardcoded, after all System Dynamics completely lacks the concept of spatial- or network-effects. Note that describing the implementation as Reactive may seem not appropriate as in System Dynamics we are not dealing with any events or reactions to it - it is all about a continuous flow between stocks. In this case we wanted to express with Reactive that it is implemented using the Arrowized notion of Yampa which is required when one wants to use Yampas time-semantics anyway.

<b>Implementation</b>	Reactive
<b>Yampa Time-Semantics</b>	Yes
<b>Update-Strategy</b>	Parallel
<b>Environment</b>	None
<b>Recursive</b>	No
<b>Conversations</b>	No

### I. WildFire

This is an implementation of a very simple Wildfire model inspired by an example from AnyLogic™ with the same name.

<b>Implementation</b>	Reactive
<b>Yampa Time-Semantics</b>	Yes
<b>Update-Strategy</b>	Parallel
<b>Environment</b>	2D Discrete
<b>Recursive</b>	No
<b>Conversations</b>	No

### J. Double Auction

This is a basic implementation of a double-auction process of a model described by [13]. This model is not relying on any environment at the moment but could make use of networks in the future for matching offers.

<b>Implementation</b>	Pure, Monadic
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Parallel
<b>Environment</b>	None
<b>Recursive</b>	No
<b>Conversations</b>	No

### K. Policy Effects

This is an implementation of a model inspired by Uri Wilensky <sup>7</sup>: "Imagine a room full of 100 people with 100 dollars each. With every tick of the clock, every person with money gives a dollar to one randomly chosen other person. After some time progresses, how will the money be distributed?"

<b>Implementation</b>	Monadic
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Parallel
<b>Environment</b>	Network
<b>Recursive</b>	No
<b>Conversations</b>	No

### L. Proof of concepts

1) *Recursive ABS*: This example shows the very basics of how to implement a recursive ABS using *FrABS*. Note that recursive features only work within the sequential strategy.

<b>Implementation</b>	Pure
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Sequential
<b>Environment</b>	None
<b>Recursive</b>	Yes
<b>Conversations</b>	No

2) *Conversation*: This example shows the very basics of how to implement conversations in *FrABS*. Note that conversations only work within the sequential strategy.

<b>Implementation</b>	Pure
<b>Yampa Time-Semantics</b>	No
<b>Update-Strategy</b>	Sequential
<b>Environment</b>	None
<b>Recursive</b>	No
<b>Conversations</b>	Yes

<sup>7</sup><http://www.decisionsciencenews.com/2017/06/19/counterintuitive-problem-everyone-room-keeps-giving-dollars-random-others-youll-never-guess-happens-next/>

APPENDIX B  
FUNCTIONAL-REACTIVE CODE OF THE SYSTEM DYNAMICS SIR MODEL

```
1  totalPopulation :: Double
2  totalPopulation = 1000
3
4  infectivity :: Double
5  infectivity = 0.05
6
7  contactRate :: Double
8  contactRate = 5
9
10 avgIllnessDuration :: Double
11 avgIllnessDuration = 15
12
13 -- Hard-coded ids for stocks & flows interaction
14 susceptibleStockId :: StockId
15 susceptibleStockId = 0
16
17 infectiousStockId :: StockId
18 infectiousStockId = 1
19
20 recoveredStockId :: StockId
21 recoveredStockId = 2
22
23 infectionRateFlowId :: FlowId
24 infectionRateFlowId = 3
25
26 recoveryRateFlowId :: FlowId
27 recoveryRateFlowId = 4
28
29 -----
30 -- STOCKS
31 susceptibleStock :: Stock
32 susceptibleStock initValue = proc ain -> do
33   let infectionRate = flowInFrom infectionRateFlowId ain
34
35   stockValue <- (initValue+) ^<< integral -< (-infectionRate)
36
37   let ao = agentOutFromIn ain
38   let ao0 = setAgentState stockValue ao
39   let ao1 = stockOutTo stockValue infectionRateFlowId ao0
40
41   returnA -< ao1
42
43 infectiousStock :: Stock
44 infectiousStock initValue = proc ain -> do
45   let infectionRate = flowInFrom infectionRateFlowId ain
46   let recoveryRate = flowInFrom recoveryRateFlowId ain
47
48   stockValue <- (initValue+) ^<< integral -< (infectionRate - recoveryRate)
49
50   let ao = agentOutFromIn ain
51   let ao0 = setAgentState stockValue ao
52   let ao1 = stockOutTo stockValue infectionRateFlowId ao0
53   let ao2 = stockOutTo stockValue recoveryRateFlowId ao1
54
55   returnA -< ao2
56
57 recoveredStock :: Stock
58 recoveredStock initValue = proc ain -> do
59   let recoveryRate = flowInFrom recoveryRateFlowId ain
60
61   stockValue <- (initValue+) ^<< integral -< recoveryRate
62
63   let ao = agentOutFromIn ain
64   let ao' = setAgentState stockValue ao
65
66   returnA -< ao'
```

```

72 -----
73 -- FLOWS
74 infectionRateFlow :: Flow
75 infectionRateFlow = proc ain -> do
76     let susceptible = stockInFrom susceptibleStockId ain
77     let infectious = stockInFrom infectiousStockId ain
78
79     let flowValue = (infectious * contactRate * susceptible * infectivity) / totalPopulation
80
81     let ao = agentOutFromIn ain
82     let ao' = flowOutTo flowValue susceptibleStockId ao
83     let ao'' = flowOutTo flowValue infectiousStockId ao'
84
85     returnA -< ao''
86
87 recoveryRateFlow :: Flow
88 recoveryRateFlow = proc ain -> do
89     let infectious = stockInFrom infectiousStockId ain
90
91     let flowValue = infectious / avgIllnessDuration
92
93     let ao = agentOutFromIn ain
94     let ao' = flowOutTo flowValue infectiousStockId ao
95     let ao'' = flowOutTo flowValue recoveredStockId ao'
96
97     returnA -< ao''
98
99 -----
100 createSysDynSIR :: [SDDef]
101 createSysDynSIR =
102     [ susStock
103     , infStock
104     , recStock
105     , infRateFlow
106     , recRateFlow
107     ]
108 where
109     initialSusceptibleStockValue = totalPopulation - 1
110     initialInfectiousStockValue = 1
111     initialRecoveredStockValue = 0
112
113     susStock = createStock susceptibleStockId initialSusceptibleStockValue susceptibleStock
114     infStock = createStock infectiousStockId initialInfectiousStockValue infectiousStock
115     recStock = createStock recoveredStockId initialRecoveredStockValue recoveredStock
116
117     infRateFlow = createFlow infectionRateFlowId infectionRateFlow
118     recRateFlow = createFlow recoveryRateFlowId recoveryRateFlow
119
120 -----
121 runSysDynSIRSteps :: IO ()
122 runSysDynSIRSteps = print dynamics
123 where
124     -- SD run completely deterministic, this is reflected also in the types of
125     -- the createSysDynSIR and runSD functions which are pure functions
126     sdDefs = createSysDynSIR
127     sdObs = runSD sdDefs dt t
128
129     dynamics = map calculateDynamics sdObs
130
131 -- NOTE: here we rely on the fact the we have exactly three stocks and sort them by their id to access them
132 --     stock id 0: Susceptible
133 --     stock id 1: Infectious
134 --     stock id 2: Recovered
135 --     the remaining items are the flows
136 calculateDynamics :: (Time, [SDObservable]) -> (Time, Double, Double, Double)
137 calculateDynamics (t, unsortedStocks) = (t, susceptibleCount, infectedCount, recoveredCount)
138 where
139     stocks = sortBy (\s1 s2 -> compare (fst s1) (fst s2)) unsortedStocks
140     (_, susceptibleCount) : (_, infectedCount) : (_, recoveredCount) : _ = stocks

```