RESEARCH A tale of lock-free Agents: Towards Software Transactional Memory in parallel Agent-Based Simulation Jonathan Thaler* and Pee⁸-Olaf Siebers

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Abstract

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With the decline of Moore's law and the ever increasing availability of cheap massively parallel hardware, it becomes more and more important to embrace parallel programming methods to implement Agent-Based Simulations (ABS). This has been acknowledged in the field a while ago and numerous research on distributed parallel ABS exists, focusing primarily on Parallel Discrete Event Simulation as the underlying mechanism. However, these concepts and tools are inherently difficult to master and apply and often an excess in case implementers simply want to parallelise their own, custom agent-based model implementation. However, with the established programming languages in the field, Python, Java and C++, it is not easy to address the complexities of parallel programming due to unrestricted side effects and the intricacies of low-level locking semantics. Therefore, in this paper we propose the use of a lock-free approach to parallel ABS using Software Transactional Memory (STM) in conjunction with the pure functional programming language Haskell, which in combination, removes some of the problems and complexities of parallel implementations in imperative approaches.

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We present two case studies, in which we compare the performance of lock-based and lock-free STM implementations in two different well known Agent-Based Models, where we investigate both the scaling performance under increasing number of CPU cores and the scaling performance under increasing number of agents. We show that the lock-free STM implementations consistently outperform the lock-based ones and scale much better to increasing number of CPU cores both on local hardware and on Amazon EC. Further, by utilizing the pure functional language Haskell we gain the benefits of immutable data and lack of unrestricted side effects guaranteed at compile-time, making validation easier and leading to increased confidence in the correctness of an implementation, something of fundamental importance and benefit in parallel programming in general and scientific computing like ABS in particular.

Keywords: Agent-Based Simulation; Software Transactional Memory; Parallel Programming; Haskell

³¹1 Introduction

The future of scientific computing in general and Agent-Based Simulation (ABS) in particular is parallelism: Moore's law is declining as we are reaching the physical

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¹limits of CPU clocks. The only option is to go massively parallel due to availability ¹ ²of cheap parallel local hardware with many cores, or cloud services like Amazon EC.² ³This trend has been already recognised in the field of ABS as a research challenge³ ⁴for Large-scale ABMS [1] was called out and as a substantial body of research for ⁴ ⁵parallel ABS shows [2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13]. In this body of work it has been established that parallelisation of autonomous ⁶ ⁷agents, situated in some spacial, metric environment can be particularly challeng-⁸ing. The reason for this is that the environment constitutes a key medium for the ⁸ ⁹agents interactions, represented as a passive data structure, recording attributes of the environment and the agents [4]. Thus, the problem of parallelising ABS boils 10 ¹¹down to the problem of how to synchronise access to shared state without violat-¹¹ ing the causality principle and resource constraints [3, 2]. Various researchers have 12 ¹³ developed different techniques, where most of them are based on the concept of Par-¹³ ¹⁴ allel Discrete-Event Simulation (PDES). The idea behind PDES is to partition the ¹⁴ shared space into logical processes, which run at their own speed, processing events 15 ¹⁶coming from themselves and other logical processes. To deal with inconsistencies ¹⁶ ¹⁷there exists a conservative approach, which does not allow to process events with ¹⁷ ¹⁸ a lower timestamp than the current time of the logical process; and an optimistic ¹⁸ ¹⁹approach, which deals with inconsistencies through rolling back changes to state. Adopting PDES to ABS is challenging as agents are autonomous, which means 20 that the topology can change in every step, making it hard to predict the topology of logical processes in advance [4], posing a difficult problem for parallelisation in general [13]. The work [2, 5] discusses this challenge by giving a detailed and in-²⁴depth discussion of the internals and implementation of their powerful and highly ²⁴ complex PDES-MAS system. The rather conceptual work [3] proposes a general, ²⁵ ²⁶ distributed simulation framework for multiagent systems and addresses a number of ²⁶ key problems: decomposition of the environment, load balancing, modelling, communication and shared state variables, which the authors mention as the central 28 problem of parallelisation. In addition, various distributed simulation environments for ABS have been developed and their internals published in research papers: the SPADES system $\begin{bmatrix} 6 \end{bmatrix}^{31}$ manages agents through UNIX pipes using a parallel sense-think-act cycle employing a conservative PDES approach; Mace3J [7] a Java based system running on

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¹ single- or multicore workstations implements a message passing approach to paral-
$^2\mathrm{lelism};$ James II [8] is also a Java based system and focuses on PDEVS simulation 2
$^3\mathrm{with}$ a plugin architecture to facilitate reuse of models; the well known RePast-HPC 3
$^{4}[9, 10]$ framework is using a PDES engine under the hood.
5 The baseline of this body of research is that parallelisation is possible and we 5
6 know how to do it. However, the complexity of these parallel and distributed simu- 6
7 lation concepts and toolkits is high and the model development effort is hard $\left[12\right].^{7}$
$^8\mathrm{Further},$ this sophisticated and powerful machinery is not always required as ABS^8
$^{9}\mathrm{does}$ not always need to be run in a distributed way but the implementers 'simply, 9
want to parallelise their models locally. Although these existing distributed ${ m ABS}^{10}$
$^{11}\mathrm{frameworks}$ could be used for this, they are an excess and more straightforward 11
$^{12}\mathrm{concepts}$ for parallelising ABS would be appropriate. However, for this case there 12
$^{13}\mathrm{does}$ not exist much research, and implementers either resort to the distributed 13
$^{14}\mathrm{ABS}$ frameworks, implement their own low-level concurrency plumbing, which can^{14}
$^{15}\mathrm{be}$ considerably complex - or simply refrain from using parallelism due to the high 15
16 complexity involved and accept a longer execution time. What makes it worse is 16
$^{17}\mathrm{that}$ parallelism always comes with the danger of additional, very subtle bugs, which 17
18 might lie dormant, potentially invalidating significant scientific results of the model. 18
19 Therefore something simpler is needed for local parallelism. Unfortunately, the es- 19
20 tablished imperative languages in the ABS field, Python, Java, C++, don't make 20
21 adding parallelism easy, due to their inherent use of unrestricted side effects. Fur- 21
ther, they mostly follow a lock-based approach to concurrency which is error prone 22
²³ and does not compose.
24
This paper proposes Software Transactional Memory (STM) in conjunction with 25
the functional programming language Haskell [14] as a new underlying concept for 26
27 local parallelisation of ABS. We hypothesise that by using STM in Haskell, imple- 27
menting local parallel ABS is considerably easier than with lock-based approaches, 28
less error prone and easier to validate. Although STM exists in other languages as ²⁹
well by now, Haskell was one of the first to natively build it into its core. Further, it 30
has the unique benefit that it can guarantee the lack of persistent side effects at com- 31
32 pile time, allowing unproblematic retries of transactions, something of fundamental 32
importance in STM. This makes the use of STM in Haskell very compelling. Our

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¹hypothesis is supported by [15], which gives a good indication of how difficult and ¹ ²complex constructing a correct concurrent program is and shows how much easier, ² ³concise and less error-prone an STM implementation is over traditional locking with³ ⁴mutexes and semaphores. Further, it shows that STM consistently outperforms the ⁴ ⁵lock-based implementation. To the best of our knowledge we are the first to systematically discuss the use of, sTM in the context of ABS. However, the idea of applying transactional memory to osimulation in general is not new and was already explored in the work [11], where the authors looked into how to apply Intel's hardware transactional memory to 10 to 11 simulations in the context of a Time Warp PDES simulation. The results showed ₁₂that their approach generally outperformed traditional locking mechanisms. The master thesis [16] investigates Haskell's parallel and concurrency features to 13 $_{14}$ implement (amongst others) HLogo, a Haskell clone of the NetLogo [17] simulation, $_{15}$ package, focusing on using STM for a limited form of agent interactions. HLogo is $_{15}$ $_{16}$ basically a re-implementation of NetLogos API in Haskell, where agents run within $_{16}$ ₁₇an unrestricted side effect context (known as IO, see more below in section 2.2.1) and ₁₇ therefore can also make use of STM functionality. The benchmarks show that this .. approach does indeed result in a speedup especially under larger agent populations. Despite the parallelism aspect our work share, our approach is rather different: we 21 avoid unrestricted side effects through IO within the agents and explore the use of ₂₂STM more generally rather than implementing an ABS library. The aim of this paper is to experimentally investigate the benefits of using STM^{23} over lock-based approaches for concurrent ABS models. Therefore, we follow $\left[15\right]^{24}$ and compare the performance of lock-based and STM implementations and expect that the reduced complexity and increased performance will be directly applicable to ABS as well. We present two case studies in which we employ an agent-based spatial SIR [18, 19] and the well known SugarScape [20] model to test our hypothesis. 29 The latter model can be seen as one of the most influential exploratory models in ABS, which laid the foundations of object-oriented implementation of agent-based models. The former one is an easy-to-understand explanatory model, which has the advantage that it has an analytical theory behind it, which can be used for verification and validation.

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1 The contribution of this paper is a systematic investigation of the usefulness 1
$^2\mathrm{of}$ STM over lock-based approaches, therefore giving implementers a new method^2
$^3\mathrm{of}$ locally parallelising their own implementations without the overhead of a $\mathrm{dis}\text{-}^3$
$^4\mathrm{tributed},$ parallel PDES system or the error-prone low-level locking semantics of a^4
$^5\mathrm{custom}$ built parallel implementation. Therefore, our paper directly addresses the 5
$^6Large\text{-}scale\ ABMS\ \text{challenge}\ [1],$ which focuses on efficient modelling and simulat- 6
$^7\mathrm{ing}$ large-scale ABS. Further, using STM, which restricts side effects, and makes^7
$^8\mathrm{parallelism}$ easier, can help in the validation challenge [1] $\mathit{H5: Requirement\ that\ all}^8$
⁹ models be completely validated.
We start with Section 2, where we discuss the concepts of STM and side effects 10
11 in Haskell. In Section 3 we show how to apply STM to ABS in general. Section 4^{11}
12 contains the first case study using a spatial SIR model, whereas Section 5 presents 12
$^{13}{\rm the~second~case~study~using~the~SugarScape~model}.$ We conclude in Section 6 and 13
¹⁴ give further research directions in Section 7.
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¹⁶ 2 Background
¹⁷ 2.1 Software Transactional Memory
$^{18}\mathrm{Software\ Transactional\ Memory\ (STM)}$ was introduced by [21] in 1995 as an alter- 18
¹⁹ native to lock-based synchronisation in concurrent programming which, in general, ¹⁹
²⁰ is notoriously difficult to get right. This is because reasoning about the interac-
21 tions of multiple concurrently running threads and low level operational details of 21
²² synchronisation primitives is <i>very hard</i> . The main problems are:
• Race conditions due to forgotten locks;
• Deadlocks resulting from inconsistent lock ordering;
• Corruption caused by uncaught exceptions;
• Lost wake ups induced by omitted notifications.
Worse, concurrency does not compose. It is very difficult to write two functions 27
28 (or methods in an object) acting on concurrent data which can be composed into a
larger concurrent behaviour. The reason for it is that one has to know about internal
details of locking, which breaks encapsulation and makes composition dependent on
knowledge about their implementation. Therefore, as an example it is impossible 31
to compose two functions where one with draws some amount of money from an 32
33 account and the other denosits this amount of money into a different account: one

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ends up with a temporary state, where the money is in none of either accounts,
$^2\mathrm{creating}$ an inconsistency - a potential source for errors because threads can be^2
³ rescheduled at any time.
STM promises to solve all these problems for a low cost by executing actions
atomically, where modifications made in such an action are invisible to other threads
and changes by other threads are invisible as well until actions are committed - this
means that STM actions are atomic and isolated. When an STM action exits, either
one of two outcomes happen: if no other thread has modified the same data as the
thread running the STM action, then the modifications performed by the action
will be committed and become visible to the other threads. If other threads have
modified the data then the modifications will be discarded, the action block rolled
back and automatically restarted.
STM in Haskell is implemented using optimistic synchronisation, which means 14
$_{15}^{14}$ that instead of locking access to shared data, each thread keeps a transaction \log_{15}
₁₆ for each read and write to shared data it makes. When the transaction exits, the ₁₆
₁₇ thread checks if it had a consistent view to the shared data by verifying whether ₁₇
18 other threads have written to memory it has read or not.
¹⁹ However, STM does not come without issues. The authors of [22] analyse several ¹⁹
20 Haskell STM programs with respect to their transactional behaviour and identified 20
²¹ the roll-back rate as one of the key metric, which determines the scalability of ²¹
$^{22}{\rm an}$ application. Although STM might promise better performance, they also warn 22
23 of the overhead it introduces, which could be quite substantial in particular for 23
$^{24}\mathrm{programs}$ which do not perform much work inside transactions as their commit 24
24 programs which do not perform much work inside transactions as their commit 24 25 overhead appears to be high.
²⁵ overhead appears to be high.
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25 overhead appears to be high. 26 27 282.2 Parallelism, Concurrency and Software Transactional Memory in Haskell 28
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¹2.2.1 Side Effects

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One of the fundamental strengths of Haskell is its way of dealing with side effects in functions. A function with side effects has observable interactions with some state outside of its explicit scope. This means that the behaviour depends on history and that it loses its referential transparency character. With referential transparency a computation does not depend on its context within the system but will produce the same result when run repeatedly with similar inputs, which makes understanding and debugging much easier. Examples for side effects are (amongst others): modifying a global variable, awaiting an input from the keyboard, reading or writing to a file, opening a connection to a server, drawing random numbers, etc.

The unique feature of Haskell is that it allows to indicate in the type of a function $_{12}$ that it does have side effects and what kind of effects they are. There are a broad $_{13}$ trange of different effect types available, to restrict the possible effects a function $_{14}$ can have, for example drawing random numbers, sharing read/write state between $_{15}$ functions, etc. Depending on the type, only specific operations are available, which $_{16}$ then checked by the compiler. This means that a program which tries to read $_{17}$ from a file in a function which only allows drawing random numbers will fail to $_{18}$ topompile.

In this paper we are only concerned with two effect types: The IO effect context can²⁰
²¹be seen as completely unrestricted as the main entry point of each Haskell program²¹
²²runs in the IO context which means that this is the most general and powerful²²
²³one. It allows all kind of input/output (IO) related side effects: reading/writing²³
²⁴a file, creating threads, write to the standard output, read from the keyboard,²⁴
²⁵opening network connections, mutable references, etc. Also, the IO context provides²⁵
²⁶functionality for concurrent locks and global shared references. The other effect²⁶
²⁷context we are concerned with is STM and indicates the STM context of a function²⁷
²⁸- we discuss it more in detail below in sections 2.2.3 and 2.2.4.

A function with a given effect type needs to be executed with a given effect runner which takes all necessary parameters depending on the effect and runs a given function with side effects returning its return value and depending on the effect also an effect related result. Note that we cannot call functions of different effect types from a function with another effect type, which would violate the guarantees.

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¹A function without any side effect is called *pure*. Calling a *pure* function is always ¹ ²allowed because it has, by definition, no side effects. ³ Although such a type system might seem very restrictive at first, we get a number ³ ⁴of benefits by making the type of effects we can use explicit. First, we can restrict ⁴ ⁵the side effects a function can have to a very specific type, which is guaranteed at ⁵ ⁶compile time. This means we can have much stronger guarantees about our program ⁶ ⁷and the absence of potential run time errors. Second, by the use of effect runners, ⁷ ⁸we can execute effectful functions in a very controlled way, by making the effect⁸ ⁹context explicit in the parameters to the effect runner. 10 112.2.2 Parallelism & Concurrency ₁₉Haskell makes a very clear distinction between parallelism and concurrency. Paral-₁₉ 13 lelism is always deterministic and thus pure without side effects because although 13 ₁₄parallel code can be run concurrently, it does by definition not interact with data₁₄ $_{15}$ of other threads. This can be indicated through types: we can run pure functions $_{15}$ ₁₆in parallel because for them it doesn't matter in which order they are executed, the ₁₆ ₁₇result will always be the same due to the concept of referential transparency. Concurrency on the other hand is potentially nondeterministic because of nondeterministic interactions of concurrently running threads through shared data. Al-10 20 though data in functional programming is immutable, Haskell provides primitives 20 21 which allow to share immutable data between threads. Accessing these primitives 21 22 is only possible from within an IO or STM context, which means that when we are 23 using concurrency in our program, the types of our functions change from pure to 23 24 either a IO or STM effect context. Note that spawning tens of thousands or even millions of threads in Haskell is $_{25}$ 26 no problem, because threads in Haskell have a very low memory footprint due to 26 ₂₇being lightweight user space threads, also known as green threads, managed by the $_{28}$ Haskell Runtime System, which maps them to physical operating system worker $_{28}$ threads [23]. ³⁰ 2.2.3 Software Transactional Memory 30 $^{31}\mathrm{The}$ work of [24, 25] added STM to Haskell, which was one of the first programming languages to incorporate STM into its main core and added the ability to composable operations. In the Haskell implementation, STM actions run within the

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¹ STM context. This restricts the operations to only STM primitives as shown below, ¹
$^2\mathrm{which}$ allows to enforce that STM actions are always repeatable without $\mathrm{persistent}^2$
$^3 \mathrm{side}$ effects because such persistent side effects (e.g. writing to a file, launching a^3
$^4\mathrm{missile})$ are not possible in an \mathtt{STM} context. This is also the fundamental difference 4
$^5{\rm to}~10,$ where we lose static guarantees because $\it everything$ is possible as there are 5
$^6{\rm basically}$ no restrictions because ${\tt IO}$ can run everything. Thus, the ability to ${\it restart}^6$
$^7\mathrm{a}$ block of actions without any visible effects is only possible due to the nature of 7
$^8\mathrm{Haskells}$ type system: by restricting the effects to \mathtt{STM} only, prevents uncontrolled 8
⁹ effects which cannot be rolled back.
10 STM comes with a number of primitives to share transactional data. Amongst 10
others the most important ones are:
• TVar A transactional variable which can be read and written arbitrarily;
• Tarray A transactional array where each cell is an individual shared data,
allowing much finer grained transactions instead of having the whole array in 14
15 a TVar;
• TChan A transactional channel, representing an unbounded FIFO channel;
• TMVar A transactional $synchronising$ variable which is either empty or full.
To read from an empty or write to a full $TMVar$ will cause the current thread
to block and retry its transaction when the TMVar was updated by another
thread.
To execute an STM action the function atomically :: STM a $ ightarrow$ IO a is pro-
vided, which performs a series of STM actions atomically within an 10 context. It
takes the STM action which returns a polymorphic value of type \mathtt{a} and returns an
10 action which returns a value of type a.
25
²⁶ 2.2.4 STM examples
We provide two examples to demonstrate the use and semantics of STM. The first 27
example is an implementation of the aforementioned functionality, where money is 28
withdrawn from one account and transferred to another. The implementing func-
tion transferFunds takes two TVar, holding the account balances, and the amount
to exchange. It executes using atomically, therefore running in the IO context. It
uses the two functions withdraw and deposit which do the work of withdrawing
some amount from one account and depositing some amount to another. This ex-

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$^{1}\mathrm{ample}$ demonstrates how easy STM can be used: the implementation looks qu	ite^1
² straightforward, simply swapping values, without any locking involved or spec	ial^2
³ handling of concurrency, other than the use of atomically.	3
4	4
5transferFunds :: TVar Integer -> TVar Integer -> Integer -> IO ()	5
transferFunds from to n = atomically \$ do	
6 withdraw from n	6
7 deposit to n	7
⁸ withdraw :: TVar Integer -> Integer -> STM ()	8
gwithdraw account amount = do	9
balance <- readTVar account	
10 writeTVar (balance - amount)	10
l1 deposit :: TVar Integer -> Integer -> STM ()	11
12deposit account amount = do	12
balance <- readTVar account	
WriteTVar (balance + amount)	13
14	14
15	15
In the second example we show the retry semantics of STM, by combining the S	
context with a StateT context. A StateT context allows to read and write so	ne 16
state, available to the function, which in this example we simply set to be an \mathtt{I}	nt ¹⁷
value. The combination of both contexts is reflected in the type of the function	on, 18
which bedsides taking a transactional variable TVar holding an Int, is StateT I	nt ¹⁹
20 STM Int which means that the function has access to both the StateT and S	TM ²⁰
functionality. The first Int indicates that the StateT context allows to read a	nd ²¹
write an Int value, available to the function; the second Int indicates that t	22
23	23
function is also an STM action and will return an Int value.	24
²⁵ stmAction :: TVar Int -> StateT Int STM Int	25
estmAction v = do	26
print a debug output and increment the value in StateT 27 Debug.trace "increment!" (modify (+1))	27
read from the TVar	
28 n <- lift (readTVar v)	28
29 await a condition: content of the TVar >= 42	29
if n < 42	30
condition not met, therefore retry: block this thread	30
until the TVar v is written by another thread, then try again	31
try again 32 then lift retry	32
condition met: return content ot TVar	20
else return n	33

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```
When stmAction is run, it prints an 'increment!' debug message to the console 1
 <sup>2</sup>and increments the value in the StateT context. Then it awaits a condition for as <sup>2</sup>
 <sup>3</sup>long as TVar is less then 42 the action will retry whenever it is run. If the condition<sup>3</sup>
 <sup>4</sup>is met, it will return the content of the TVar. To run stmAction we need to spawn<sup>4</sup>
 <sup>5</sup>a thread:
                                                                                               6
 7stmThread :: TVar Int -> IO ()
 stmThread v = do
                                                                                               8
    -- the initial state of the StateT effect
   let s = 0
    -- run the state with initial value of s (0)
                                                                                               10
   let ret = runStateT (stmAction v) s
    -- atomically run the STM action
                                                                                               11
    (a, s') <- atomically ret</pre>
12 -- print final result
                                                                                               12
    putStrLn("final StateT state
                                       = " ++ show s' ++
                                                                                               13
              ", STM computation result = " ++ show a)
                                                                                               14
14
<sup>15</sup> The thread first runs the StateT context using the effect runner function <sup>15</sup>
<sup>16</sup>runStateT which takes the stmAction and the initial value of the effect context. <sup>16</sup>
<sup>17</sup>This results in an STM computation, which is executed through atomically. Finally, <sup>17</sup>
<sup>18</sup>the result is printed to the console. The value of a is the result of stmAction and s, <sup>18</sup>
<sup>19</sup> is the final state of the StateT computation. To actually run this example we need <sup>19</sup>
<sup>20</sup>the main thread to update the TVar until the condition is met within stmAction: <sup>20</sup>
22main :: IO ()
                                                                                               22
 main = do
                                                                                               23
   -- create a new TVar with initial value of 0
    v <- newTVarIO 0
                                                                                               24
    -- start the stmThread and pass the TVar
   forkIO (stmThread v)
    -- do 42 times...
                                                                                               26
    forM_ [1..42] (\i -> do
      -- use delay to 'make sure' that a retry is happening for every increment
      threadDelay 10000
                                                                                               28
      -- write new value to TVar using atomically, will cause the STM
      -- thread to wake up and retry
      atomically (writeTVar v i))
                                                                                               30
    If we run this program, we will see 'increment!' printed 43 times, followed
by 'final StateT state = 1, STM computation result = 42'. This clearly
^{33} demonstrates the retry semantics where stmAction is retried 42 times and thus
```

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¹prints 'increment!' 43 times to the console. The StateT computation however is ¹ ²always rolled back when a retry is happening. The rollback is easily possible in pure ² ³functional programming due to persistent data structures, by simply throwing away ⁴the new value and retrying with the old value. This example also demonstrates that ⁴ 5 any IO actions which happen within an STM action are persistent and can obviously 5 ⁶not be rolled back. Debug.trace is an IO action masked as pure by the Haskell⁶ ⁷implementation, to support debugging of pure functions. If it would not have been ⁷ ⁸masked as pure, the compiler would have not accepted the program, because the ⁸ ⁹STM context does not allow the execution of IO actions. 10 ₁₁3 Software Transactional Memory in Agent-Based Simulation ₁₂In this section we give a short overview of how to apply STM in ABS. We fundamentally follow a time-driven approach in both case studies, where the simulation ₁₄ is advanced by some given Δt and in each step all agents are executed. To employ ₁₄ $_{15}$ parallelism, each agent runs within its own thread and agents are executed in lock- $_{15}$ step, synchronising between each Δt , which is controlled by the main thread. This 16 ₁₇way of stepping the simulation is introduced in [26] on a conceptual level, where ₁₇ $_{18}$ the authors name it concurrent update-strategy. See Figure 1 for a visualisation of $_{18}$ our concurrent, time-driven lock-step approach. An agent thread will block until the main thread sends the next Δt and runs the STM action atomically with the given Δt . When the STM action has been committed, 20 the thread will send the output of the agent action to the main thread to signal it 20 23 has finished. The main thread awaits the results of all agents to collect them for 23 24 output of the current step, for example visualisation or writing to a file. As will be described in subsequent sections, central to both case studies is an $_{25}$ environment which is shared between the agents using a TVar or TArray primitive 26 27 through which the agents communicate concurrently with each other. To get the $_{28}$ environment in each step for visualisation purposes, the main thread can access the $_{28}$ 20 TVar and TArray as well. $^{30}3.1$ Adding STM to agents 30 A detailed discussion of how to add STM to agents on a technical level is beyond the focus of this paper as it would require to give an in-depth technical explanation of how our agents are actually implemented [19].

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¹ However	the concepts are	e similar to the example in Section 2.2.4. The	ne agent ¹
² behaviour	is an STM action ar	nd has access to the environment either through	h a TVar ²
³ or TArray	and performs read	l and write operations directly on it. Each age	ent itself ³
⁴ is run with	hin its own thread,	and synchronises with the main thread. Thus,	it takes ⁴
⁵ Haskells M	War synchronisatio	on primitives to synchronise with the main thr	ead and ⁵
	Ţ.	ehaviour each time it receives the next tick DT	
7	is the 211 agent s		7
8agentThrea	d :: RandomGen g		8
- 3	=> Int	Number of steps to compute	
9	-> SIRAgent g	Agent behaviour	9
	-> g	Random-number generator of the agent	
10	-> MVar SIRState		10
11	-> MVar DTime	Receiving DTime for next tick	11
		Receiving Dilme for next tick	
12	-> IO ()	. ()	12
_		n () all steps computed, terminate thread	
•	d n agent rng retVa		13
14	for dt to compute c	urrent step	14
dt <- tal	keMVar dtVar	N	
	te output of current		15
16	tSTMAction = runAge	-	16
run ci	•	n atomically within IO	10
11		omically agentSTMAction	17
	result to main threa	ad	40
-	retVar ret		18
19	recursion to next st	-	19
agentThre	ead (n - 1) agent'	rng' retVar dtVar	
20			20
Comput	ing a simulation s	tep is quite trivial within the main thread. A	all agent ²¹
threads M	Vars are signalled	to unblock, followed by an immediate block	on the 22
²³ MVars into	which the agent t	hreads post back their result. The state of the	e current ²³
24		he environment, which is stored within the TVa	24
25	41 1. 1 1.	4-1	25
tne agent	threads have upda	ted:	26
20			20
27simulation	Step :: TVar SIREnv	environment	27
28	-> [MVar DTime]] sync dt to threads	28
20	-> [MVar SIRSta	ate] sync output from threads	20
29	-> DTime	time delta	29
	-> IO SIREnv		
30 simulations	Step env dtVars ret	Wars dt = do	30
		ute next tick with the corresponding DTime	31
mapM_ (']	putMVar' dt) dtVars		
32 wait :	for results but igno	ore them, SIREnv contains all states	32
mapM_ tal	keMVar retVars		33
	n state of environme	ent when step has finished	30

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1 readTVarIO env	1
	2
34 Case Study 1: Spatial SIR Model	3
$_4\mathrm{Our}$ first case study is the SIR model which is a very well studied and understood	4
$_{5}\mathrm{compartment}$ model from epidemiology [27], which allows to simulate the dynamics	5
$_{6}\mathrm{of}$ an infectious disease like influenza, tuberculosis, chicken pox, rubella and measles	; 6
₇ spreading through a population [28].	7
$_{8}$ In it, people in a population of size N can be in either one of three states $Suscep$ -	-8
$_9tible$, $Infected$ or $Recovered$ at a particular time, where it is assumed that initially	9
othere is at least one infected person in the population. People interact on average	³ 10
, with a given rate of β other people per time unit and become infected with a given	l 11
probability γ when interacting with an infected person. When infected, a person	l 12
$_{3}$ recovers on average after δ time units and is then immune to further infections.	13
An interaction between infected persons does not lead to re-infection, thus these) 14
5 interactions are ignored in this model.	15
$_{.6}$ We followed in our agent-based implementation of the SIR model the work [18] but	; 16
$_{7}\mathrm{extended}$ it by placing the agents on a discrete 2D grid using a Moore (8 surrounding	17
$_{8}{\rm cells})$ neighbourhood [19]. A visualisation can be seen in Figure 2.	18
9 Due to the continuous-time nature of the SIR model, our implementation follows	; 19
the time driven $[29]$ approach. This requires us to sample the system with very small	20
$_{11}\Delta t$, which means that we have comparatively few writes to the shared environment	; 21
which will become important when discussing the performance results.	22
	23
4.1 Experiment Design	
In this case study we compare the performance of five (5) implementations under	25
varying numbers of CPU cores and agent numbers. The code of all implementations	26
can be accessed freely from the code repository [30].	
1 Sequential - This is the reference implementation as discussed in [19], where	
the agents are executed sequentially within the main thread without any con-	
currency. The discrete 2D grid is represented using an indexed array [31] and	29
shared amongst all agents as read-only data, with the main thread updating	30
the array for the next time step.	31
2 Lock-Based Naive - This is the same implementation as Sequential, but the	32
agents now run concurrently in the IO context. The discrete 2D grid is also	33)

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1		represented using an indexed array but now modified by the agents themselves
2		and therefore shared using a global reference. The agents acquire and ${\rm release}^2$
3		a lock when accessing the shared environment.
4	3	Lock-Based Read-Write Lock - This is the same implementation as $Lock$ -
5		Based Naive, but uses a read-write lock from concurrent-extra library [32] ⁵
6		for a more fine-grained locking strategy. This implementation exploits ${\rm the}^6$
7		fact that in the SIR model, reads outnumber writes by far, making a read-
8		write lock much more appropriate than a naive locking mechanism, which 8
9		unconditionally acquires and releases the lock. However, it is important to note 9
10		that this approach works only because the semantics of the model support it: 10
11		agents read any cells but only write their own cell.
12	4	Atomic IO - This is the same implementation as $Lock$ -Based $Read$ -Write $Lock$ ¹²
13		but uses an atomic modification operation to both read and write the shared 13
14		environment. Although it runs in the IO context, it is not a lock-based ap-14
15		proach as it does not acquire locks but uses a compare-and-swap hardware 15
16		instruction. A limitation of this approach is that it is only applicable when 16
17		there is just a single reference in the program and that all operations need 17
18		to go through the atomic modification operation. As in the case of the $Lock$ -18
19		$Based\ Read\text{-}Write\ Lock}$ implementation, this approach works only because 19
20		the semantics of the model support it.
21	5	STM - This is the same implementation as $\operatorname{Lock-Based}$ Naive but agents run^{21}
22		in the ${\tt STM}$ context. The discrete 2D grid is also represented using an indexed 22
23		array but shared amongst all agents through a transactional variable ${\tt TVar.}^{23}$
24	Ea	ch experiment was run on our hardware (see Table 1) under no additional work-
²⁵ 1	oad	until $t=100$ and stepped using $\Delta t=0.1$. In the experiments we varied the ²⁵
26 I	num	ber of agents (grid size) as well as the number of cores when running concur-
27 I	entl	y. We checked the visual outputs and the dynamics and they look qualitatively 27
28 t	he s	same as the reference $Sequential$ implementation [19]. A rigorous, statistical 28
29	comp	parison of all implementations, to investigate the effects of concurrency on the 29
30	lyna	amics, is quite involved and therefore beyond the focus of this paper but as a^{30}
31 I	eme	edy we refer to the use of property-based testing, as shown in [33].
32		$^{\rm 32}$ r robust performance measurements we used the microbenchmarking library
33	Crite	erion [34, 35]. It allows the definition and running of benchmark suites, mea-

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1	Model	Dell XPS 13 (9370)	1
	OS	Ubuntu 19.10 64-bit	
2	RAM	16 GByte	2
3	CPU	Intel Core i7-8550U @ 3.6GHz x 8	3
	HD	512Gbyte SSD	
4	Haskell	GHC 8.4.3 (stack resolver lts-12.4)	4

Table 1: Hardware and software details for all experiments

6

16

30

7	Cores	Sequential	Lock-Based Naive	Lock-Based Read-Write	Atomic IO	STM	7
8	1	73.9 (2.06)	59.2 (0.16)	55.0 (0.22)	51.0 (0.11)	52.2 (0.23)	=
0-	2	-	46.5 (0.05)	40.8 (0.18)	32.4 (0.09)	33.2 (0.03)	_0
9	3	-	44.2 (0.08)	35.8 (0.06)	25.5 (0.09)	26.4 (0.05)	9
10-	4	-	47.4 (0.12)	34.0 (0.32)	22.7 (0.08)	23.3 (0.19)	_ _10
	5	-	48.1 (0.13)	34.5 (0.06)	22.6 (0.03)	23.0 (0.06)	-10
11	6	-	49.1 (0.09)	34.8 (0.03)	22.3 (0.09)	23.1 (0.05)	11
12-	7	-	49.8 (0.09)	35.9 (0.15)	22.8 (0.07)	23.4 (0.22)	- -12
12-	8	-	57.2 (0.06	40.4 (0.21)	25.8 (0.02)	26.2 (0.22)	-12

Table 2: Performance comparison of Sequential, Lock-Based, Atomic IO and STM¹³
 SIR implementations under varying cores with grid size of 51x51 (2,601) agents.
 Timings in seconds (lower is better), standard deviation in parentheses.

17

 $_{18}$ suring performance by executing them repeatedly, fitting actual against expected $_{18}$ $_{19}$ runtime, reporting mean and standard deviation for statistically robust results. By $_{19}$ $_{20}$ running each benchmark repeatedly, fitting it using linear regression analysis, Cri- $_{20}$ $_{21}$ terion is able to robustly determine whether the measurements fall within a normal $_{21}$ $_{22}$ range or are outliers (and therefore should be re-run) due to some external in- $_{22}$ $_{23}$ fluences like additional workload on the machine. Therefore, we made sure to only $_{23}$ $_{24}$ include measurements Criterion labelled as normal, which meant we re-ran measure- $_{24}$ $_{25}$ ments where goodness-of-fit was $R^2 < 0.99$. Criterion ran each of our benchmark $_{25}$ $_{26}$ 10 times with increasing increments of 1, 2, 3 and 4 times. In the results we report $_{26}$ $_{27}$ the estimates of ordinary least squares (OLS) regression together with the standard $_{27}$ and $_{28}$ deviation because it gives the most reliable results in terms of statistical robustness.

25

³⁰4.2 Constant Grid Size, Varying Cores

6

16

 31 In this experiment we held the grid size constant at 51 x 51 (2,601 agents) and 32 varied the cores where possible. The results are reported in Table 2 and visualised 32 in Figure 3.

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1	Grid Size	Lock-Based Read-Write	Atomic IO	STM	1
2	101 × 101 (10,201)	139.0 (0.15)	91.1 (0.14)	96.5 (0.27)	
2	151 × 151 (22,801)	314.0 (0.67)	204.0 (0.36)	212.0 (0.16)	. 2
3	201 × 201 (40,401)	559.0 (1.22)	360.0 (0.61)	382.0 (0.85)	3
Δ	251 × 251 (63,001)	861.0 (0.62)	571.0 (0.71)	608.0 (1.20)	. 4

 $_5$ Table 3: Performance comparison of *Lock-Based Read-Write*, *Atomic IO* and $STM_{_5}$ SIR implementations with varying grid sizes on 4 cores. Timings in seconds (lower $_6$ is better), standard deviation in parentheses.

3

9 Comparing the performance and scaling to multiple cores of the *STM* and both9

10 Lock-Based implementations shows that the *STM* implementation significantly out-10

11 performs the Lock-Based ones and scales better to multiple cores. The Lock-Based11

12 implementations perform best with 3 and 4 cores respective, and shows decreasing12

13 performance beyond 4 cores as can be seen in Figure 3. This is no surprise because13

14 the more cores, the more contention for the central lock, thus the more likely syn-14

15 chronisation happening, ultimately resulting in reduced performance. This is not15

16 an issue in *STM* because no locks are taken in advance due to optimistic locking,16

17 where a log of changes is kept allowing the runtime to trigger a retry if conflicting17

18 changes are detected upon transacting.

¹⁹ A big surprise however is that the *Atomic IO* implementation is slightly out-¹⁹ 20 performing the STM one, which is something we would not have anticipated. We²⁰ 21 attribute this to the lower overhead of the atomic modification operation.

Both the *STM* and *Atomic IO* implementations are running into decreasing re-²² turns after 5 to 6 cores, which we attribute to our hardware. Although virtually it²³ ²⁴ comes across as 8 cores it has only 4 physical ones, implementing hyper threading²⁴ ²⁵ to simulate 4 additional cores. Due to the fact that resources are shared between²⁵ ²⁶ two threads of a core, it is only logical that we are running into decreasing returns²⁶ ²⁷ in all implementations on more than 5 to 6 cores on our hardware.

28

²⁹4.3 Varying Grid Size, Constant Cores

 30 In this experiment we varied the grid size and used constantly 4 cores. The results 30 are reported in Table 3 and plotted in Figure 4.

It is clear that the STM implementation outperforms the Lock-Based implemen-

tation by a substantial factor. However, the *Atomic IO* implementation outperforms

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1	Grid Size	Commits	Retries	Ratio	1
2	51 × 51 (2,601)	2,601,000	1306	0.0	2
3	101 × 101 (10,201)	10,201,000	3712	0.0	3
	151 × 151 (22,801) 201 × 201 (40,401)	22,801,000 40,401,000	8189 13285	0.0	
4	251 × 251 (63,001)	63,001,000	21217	0.0	4
⁵ Table 4: Retry rat	tios of the SIR STA	I implement	tation wi	th vary	ring grid sizes on 4 ⁵
6 cores.					6
7					7
8					8
the STM one again	in, where this time	the difference	e is a bit	t more p	pronounced due to
the higher worklo	ad of the experimen	nts.			10
11					11
4.4 Retries					
Of very much inte	rest when using ST	M is the retr	y ratio, v	which in	*
of the total STM a	actions had to be r	e-run. A hig	gh retry	ratio sl	hows that a lot of
work is wasted on	re-running STM act	tions due to	many co	ncurren	nt read and writes.
Obviously, it is hi	ghly dependent on	the read-wri	te patte	rns of th	ne implementation
16	well an STM appr		_		16
17				_	17
18	s [36] library to reco	ord statistics	s of colli	mus, reu	ries and the ratio.
The results are re	-		1		19
20	the number of ager				20
dicates that this r	model is <i>very</i> well s	suited to ST	M, which	h is also	o directly reflected
in the much bette	er performance over	r the Lock-E	Based im	plemen	tations. Obviously
this ratio stems fi	rom the fact, that i	in our imple	ementatio	on we h	have very few con-
	hich happen only in	case when	an agent	change	es from $Susceptible$
to <i>Infected</i> or from	m Infected to Recov	vered.			24
25					25
²⁶ 4.5 Going Large-S	cale				26
²⁷ To test how far w		number of c	ores in t	he best	performing cases, ²⁷
$^{28}Atomic\ IO\ {\rm and}\ S$					
20	ge instance with 10				20
decreasing returns	3				30
31	implementation is			rforms	nco from 16 to 32
32	_				32
33	of 51x51 but fails				33
haviour to an inc	creased number of	retries of the	ne atomi	c modif	ication operation,

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16 18.0 (0.21) 638.0 (8.24)
2 Atomic IO
32 15.6 (0.07) 720.0 (1.70)
STM 16 14.5 (0.03) 307.0 (1.12)
32 14.7 (0.17) 269.0 (1.05)

 $_5$ Table 5: Performance comparison of $Atomic\ IO$ and STM SIR implementations on $_6$ 16 and 32 cores on an Amazon EC2 m5ad.16xlarge instance. Timings in seconds $_6$ 2 (lower is better), standard deviations in parentheses.

8

which obviously increases when the number of agents increases. The *STM* implementation performance on the other hand nearly stays constant on 16 and 32 cores
in the 51x51 case. In both cases we measured a retry ratio of 0, thus we conclude that with 32 cores we become limited by the overhead of STM transactions [22] because the workload of an STM action in our SIR implementation is quite small.
On the other hand, with heavy load as in the 251x251 case, we see an increased performance with 32 cores.

What is interesting is that on more cores, the *STM* implementations has an edge over the *Atomic IO* approach, and performs better in all cases. It seems that for our problem at hand, the atomic modification operation seems to be not as efficient on many cores as an STM approach.

21

22

²²4.6 Summary

The timing measurements speak a clear language. Running in STM and sharing state using a transactional variable TVar is much more time efficient than the Sequential and both Lock-Based approaches. On 5 cores STM achieves a speedup factor of 3.2 over the Sequential implementation, which is a big improvement compared to the simplicity of the approach. What came as a surprise was that the Atomic IO approach slightly outperforms the STM implementation. However, the Atomic IO approach, which uses an atomic modification operation, is only applicable in case there is just a single reference in the program and requires that all operations go through this atomic modification operation. Whether the latter condition is possible or not, is highly dependent on the model semantics, which support it in the case of the SIR model but unfortunately not in the case of Sugarscape.

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1 Obviously both $Lock\mbox{-}Based,\ Atomic\ IO\ \mbox{and}\ STM\ \mbox{sacrifice}$ determinism, which 1
² means that repeated runs might not lead to same dynamics despite same initial ²
³ conditions. However, when sticking to STM, we get the guarantee that the source ³
⁴ of this nondeterminism is concurrency within the STM context but <i>nothing else</i> . This ⁴
$^5{\rm can}$ not be guaranteed in the case of both $Lock\text{-}Based$ and $Atomic~IO~{\rm approaches}^5$
$^6\mathrm{as}$ we lose certain static guarantees when running within the 10 context. The fact 6
7 to have $both$ a substantial speedup and the stronger static guarantees, makes the 7
⁸ STM approach <i>very</i> compelling.
9
¹⁰ 5 Case Study 2: SugarScape
¹¹ One of the first models in Agent-Based Simulation was the seminal Sugarscape ¹²
$^{12}\mathrm{model}$ developed by Epstein and Axtell in 1996 [20]. Their aim was to grow an 12
13 artificial society by simulation and connect observations in their simulation to phe- 13
$^{14}\mathrm{nomenon}$ observed in real-world societies. In this model a population of agents move 14
$^{15}\mathrm{around}$ in a discrete 2D environment, where sugar grows, and interact with each 16
$^{16}\mathrm{other}$ and the environment in many different ways. The main features of this model $^{16}\mathrm{other}$
$^{17}\mathrm{are}$ (amongst others): searching, harvesting and consuming of resources, wealth and $^{17}\mathrm{are}$
$^{18}{\rm age}$ distributions, population dynamics under sexual reproduction, cultural pro- $^{18}{\rm age}$
$^{19}\mathrm{cesses}$ and transmission, combat and assimilation, bilateral decentralized trading 19
$^{20}({\rm bartering})$ between agents with endogenous demand and supply, disease processes $^{20}({\rm bartering})$
²¹ transmission and immunology.
We implemented the Carrying Capacity (p. 30) section of Chapter II of the book 22
²³ [20]. There, in each step agents search (move) to the cell with the most sugar they ²³
see within their vision, harvest all of it from the environment and consume $\operatorname{sugar}^{2^4}$
²⁵ based on their metabolism. Sugar regrows in the environment over time. Only one
26 agent can occupy a cell at a time. Agents don't age and cannot die from age. If 26
27 agents run out of sugar due to their metabolism, they die from starvation and are
removed from the simulation. The authors report that the initial number of agents 21
quickly drops and stabilises around a level depending on the model parameters. ²⁵
30 This is in accordance with our results as we show in Figure 5 and guarantees that 30
we don't run out of agents. The model parameters are as follows:
• Sugar Endowment: each agent has an initial sugar endowment randomly uni-
form distributed between 5 and 25 units;

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1	•	Sugar Metabolism: each agent has a sugar metabolism randomly uniform $\operatorname{dis-}^1$
2		tributed between 1 and 5;
3	•	Agent Vision: each agent has a vision randomly uniform distributed between ³
4		1 and 6, same for each of the 4 directions (N, W, S, E);
5	•	Sugar Growback: sugar grows back by 1 unit per step until the maximum ⁵
6		capacity of a cell is reached;
7	•	Agent Number: initially 500 agents; 7
8	•	Environment Size: 50 x 50 cells with toroid boundaries which wrap around in 8
9		both x and y dimension.
.0		10
¹ 5	.1 E	Experiment Design
.2 I1	ı th	is case study we compare the performance of four (4) implementations under 12
.3 V	aryi	ing numbers of CPU cores and agent numbers. The code of all implementations 13
.4 Ca	an l	be accessed freely from the code repository [37].
.5	1	Sequential - This is the reference implementation, where all agents are run
.6		after another (including the environment). The environment is represented
.7		using an indexed array [31] and shared amongst the agents using a read and 12
.8		write state context.
.9	2	Lock-Based - This is the same implementation as Sequential, but all agents are
20		run concurrently within the IO context. The environment is also represented
21		as an indexed array but shared using a global reference between the agents
22		which acquire and release a lock when accessing it. Note that the semantics
23		of Sugarscape do not support the implementation of either a read-write lock
24		or atomic modification approach as in the SIR model. In the SIR model,
25		the agents write conditionally to their own cell, but this is not the case in
26		Sugarscape, where agents need a consistent view of the whole environment
27		for the whole duration of an agent execution due to the fact that agents do
28		not only write their own locations but also to other locations. If this is not
29		handled correctly, data races are happening and threads overwrite data from
80		other threads, ultimately resulting in incorrect dynamics.
31	3	STM TVar - This is the same implementation as Sequential, but all agents are
32		run concurrently within the STM context. The environment is also represented
33		as an indexed array but shared using a TVar between the agents

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4 STM TArray - This is the same implementation as Sequential, but all agents
2 are run concurrently within the STM context. The environment is represented 2
and shared between the agents using a TArray.
4
⁵ Ordering The model specification requires to shuffle agents before every step ([20], ⁵
6 footnote 12 on page 26). In the $Sequential$ approach we do this explicitly but in the
$^7Lock ext{-}Based$ and both STM approaches we assume this to happen automatically due 7
$^8{\rm to}$ race conditions from concurrency, thus we arrive at an effectively shuffled process- 8
9 ing of agents because we implicitly assume that the order of the agents is $effectively^{9}$
$^{10}\mathrm{random}$ in every step. The important difference between the two approaches is that 1
11 in the $Sequential$ approach we have full control over this randomness but in the 1
^{12}STM and $Lock\text{-}Based$ not. This has the consequence that repeated runs with the 1
$^{13}\mathrm{same}$ initial conditions might lead to slightly different results. This decision leaves 1
$^{14}{\rm the}$ execution order of the agents ultimately to Haskell's Runtime System and ${\rm the}^1$
¹⁵ underlying operating system. We are aware that by doing this, we make assump-
$^{16}\mathrm{tions}$ that the threads run uniformly distributed (fair) but such assumptions should 1
¹⁷ not be made in concurrent programming. As a result we can expect this fact to pro-
$^{18}\mathrm{duces}$ non-uniform distributions of agent runs but we assumed that for this model^1
$^{19}\mathrm{this}$ does not have a significance influence. In case of doubt, we could resort to 1
$^{20}\mathrm{shuffling}$ the agents before running them in every step. This problem, where also^2
$^{21}{\rm the}$ influence of nondeterministic ordering on the correctness and results of ${\rm ABS}^2$
$^{22}\mathrm{has}$ to be analysed, deserves in-depth research on its own and is therefore beyond 2
$^{23}{\rm the}$ focus of this paper. As a potential direction for such an investigation, we refer 2
²⁴ to the technique of property-based testing as shown in [33].
Note that in the concurrent implementations we have two options for running
the environment: either asynchronously as a concurrent agent at the same time 2
with the population agents or synchronously after all agents have run. We must 2
be careful though as running the environment as a concurrent agent can be seen 2
as conceptually wrong because the time when the regrowth of the sugar happens 2
is now completely random. In this case it could happen that sugar regrows in the 3
very first transaction or in the very last, different in each step, which can be seen 3
as a violation of the model specifications. Thus we do not run the environment 32
concurrently with the agents but synchronously after all agents have run.

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1	Cores	Sequential	Lock-Based	TVar	TArray	1
2	1	25.2 (0.36)	21.0 (0.12)	21.1 (0.25)	42.0 (2.20)	2
	2	-	20.0 (0.12)	22.2 (0.21)	24.5 (1.07)	2
3	3	-	21.9 (0.19)	23.6 (0.12)	19.7 (1.05)	3
4	4	-	24.0 (0.17)	25.2 (0.16)	18.9 (0.58)	4
	5	-	26.7 (0.17)	31.0 (0.24)	20.3 (0.87)	4
5	6	-	29.3 (0.57)	35.2 (0.12)	21.2 (1.49)	5
6	7	-	30.0 (0.12)	38.7 (0.42)	21.0 (0.41)	6
	8	-	31.2 (0.29)	49.0 (0.41)	21.1 (0.64)	ь

⁷Table 6: Performance comparison of Sequential, Lock-Based, TVar and TArray Sug-

 $^{8}{\rm arscape}$ implementations under varying cores with 50x50 environment and 500 ini- $^{8}{\rm core}$

⁹tial agents. Timings in seconds (lower is better), standard deviation in parentheses.

The experiment setup is the same as in the SIR case study, with the same hardware (see Table 1), with measurements done under no additional workload using the microbenchmarking library Criterion [34, 35] as well. However, as the Sugarscape model is stepped using natural numbers we ran each measurement until t=1000 and stepped it using $\Delta t=1$. In the experiments we varied the number of agents as well as the number of cores when running concurrently. We checked the visual outputs and the dynamics and they look qualitatively the same as the reference Sequential. As in the SIR case study, a rigorous, statistical comparison of all implementations, to investigate the effects of concurrency on the dynamics, is quite involved and therefore beyond the focus of this paper but as a remedy we refer to the use of property-based testing, as shown in [33].

²³5.2 Constant Agent Size

10

²⁴In a first approach we compare the performance of all implementations on varying ²⁵ numbers of cores. The results are reported in Table 6 and plotted in Figure 6.

23

As expected, the *Sequential* implementation is the slowest, with *TArray* being the fastest one except on 1 and 2 cores, where unexpectedly the *Lock-Based* implementation performed best. Interestingly the *TVar* implementation was the worst performing one of the concurrent implementations.

The reason for the bad performance of *TVar* is that using a **TVar** to share the environment is a very inefficient choice: *every* write to a cell leads to a retry independent whether the reading agent reads that changed cell or not, because the data structure can not distinguish between individual cells. By using a **TArray** we

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1	Cores	TVar	TArray	
2	1	0.00	0.00	
2	2	1.04	0.02	
3	3	2.15	0.04	
4	4	3.20	0.06	
7	5	4.06	0.07	
5	6	5.02	0.09	
6	7	6.09	0.10	
·	8	8.45	0.11	

⁷Table 7: Retry ratio comparison (lower is better) of the *TVar* and *TArray* Sug-⁸ arscape implementations under varying cores with 50x50 environment and 500 ini-⁸ tial agents.

10

 $_{12}$ can avoid the situation where a write to a cell in a far distant location of the en- $_{12}$ vironment will lead to a retry of an agent which never even touched that cell. The $_{13}$ $_{14}$ inefficiency of TVar is also reflected in the fact that the Lock-Based implementation $_{14}$ $_{15}$ outperforms it on all cores. The sweet spot is in both cases at 3 cores, after which $_{15}$ $_{16}$ decreasing performance is the result. This is due to very similar approaches because $_{16}$ $_{17}$ both operate on the whole environment instead of only the cells as TArray does. $_{17}$ $_{18}$ In case of the Lock-Based approach, the lock contention increases, whereas in the $_{18}$ $_{19}$ TVar approach, the retries start to dominate (see Table 7).

Interestingly, the performance of the TArray implementation is the worst amongst₂₀ $_{21}$ all on 1 core. We attribute this to the overhead incurred by STM, which dramatically $_{21}$ $_{22}$ adds up in terms of a sequential execution.

23

²⁴5.3 Scaling up Agents

²⁵So far we kept the initial number of agents at 500, which due to the model specifi-²⁵
²⁶cation, quickly drops and stabilises around 200 due to the carrying capacity of the²⁶
²⁷environment as can be seen in Figure 5b and which is also described in the book²⁷
²⁸[20] section Carrying Capacity (p. 30).

We now measure the performance of our approaches under increased number of agents. For this we slightly change the implementation: always when an agent dies it spawns a new one which is inspired by the ageing and birthing feature of Chapter III in the book [20]. This ensures that we keep the number of agents roughly constant (still fluctuates but doesn't drop to low levels) over the whole duration. This ensures

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Lock-Based

TVar

TArray

1

Agents

1

Sequential

-						-	
2	500	70.1 (0.41)	67.9 (0.13)	69.1 (0.34)	25.7 (0.42)	2	
3	1,000	145.0 (0.11) 220.0 (0.14)	130.0 (0.28) 183.0 (0.83)	136.0 (0.16) 192.0 (0.73)	38.8 (1.43) 40.1 (0.25)	3	
	2,000	213.0 (0.69)	181.0 (0.84)	214.0 (0.53)	49.9 (0.82)	Ü	
4	2,500	193.0 (0.16)	272.0 (0.81)	147.0 (0.32)	55.2 (1.04)	4	
⁵ Table 8: Per	formanc	e comparison	of Sequential	, Lock-Based	\overline{TVar} and T	Array Sug- ⁵	
arscape imp	olementa	tions with va	rying agent n	umbers and	50x50 enviror	ment on 4 ⁶	
⁷ cores (excep	ot Sequer	ntial). Timing	gs in seconds	(lower is bet	ter), standard	l deviation ⁷	
in parenthe	ses.					8	
9						9	
10						10	
₁₁ a constant l							
₁₂ also the abi	lity to te	erminate and	fork threads	dynamically	during the si	mulation. ₁₂	
13 Except for	the Sequ	uential appro	ach we ran all	experiments	with 4 cores.	We looked $_{13}$	
14into the per	formanc	e of 500, 1,00	00, 1,500, 2,00	00 and 2,500	(maximum p	ossible ca- ₁₄	
15pacity of th	e 50x50	environment)	. The results	are reported	l in Table 8 a	nd plotted $_{15}$	
16in Figure 7.						16	
¹⁷ As expect	ed, the 7	Array impler	nentation out	performs all	others substa	ntially and 17	
18 scales up much smother. Also, $Lock\text{-}Based$ performs better than the $TVar$.							
19 What see:	ms to be	very surpris	ing is that in	the Sequent	tial and TVar	r cases the 19	
²⁰ performance	e with 2,	500 agents is	better than t	he one with 2	2,000 agents.	The reason ²⁰	
²¹ for this is th	at in the	case of 2,500	agents, an ag	gent can't mo	ove anywhere	because all ²¹	
²² cells are alre	eady occi	ipied. In this	case the agen	t won't rank	the cells in or	der of their ²²	
²³ payoff (max	sugar) t	to move to bu	ıt just stays	where it is. V	Ve hypothesiz	te that due ²³	
²⁴ to Haskells	laziness t	the agents ac	tually never l	ook at the co	entent of the o	cells in this ²⁴	
²⁵ case but onl	y the nu	mber which n	neans that the	e cells themse	elves are never	evaluated ²⁵	
²⁶ which furth	er increa	ses performa	nce. This lead	ds to the bet	ter performa	nce in case ²⁶	
²⁷ of Sequentia	al and T	Var because b	ooth exploit la	aziness. In th	e case of the	Lock-Based ²⁷	
²⁸ approach w	e still arı	rive at a lowe	er performanc	e because th	e limiting fac	tor are the ²⁸	
²⁹ uncondition	al locks.	In the case of	of the TArrag	y approach w	ve also arrive	at a $lower^{29}$	
30 performance	e because	e it seems th	at STM perf	orm reads or	n the neighbor	ouring cells ³⁰	
³¹ which are n	ot subjec	ct to lazy eva	luation.			31	
In case of	In case of the $Sequential$ implementation with 2,000 agents we also arrive at a bet-						
ter perform	ance that	n with 1,500,	due to less sp	pace of the ag	gents for free	movement, ³³	

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1	Cores	Carrying Capacity	Rebirthing	1
2	16	11.9 (0.21)	46.6 (0.07)	2
2	32	12.8 (0.29)	76.4 (0.01)	Z
3	64	14.6 (0.09)	99.1 (0.01)	3

4Table 9: Sugarscape *TArray* performance on 16, 32 and 64 cores an Amazon EC4 5m5ad.16xlarge instance. Timings in seconds (lower is better). Retry ratios in paren-5 6theses.

7

 $_{9}$ exploiting laziness as in the case with 2,500 agents. In the case of the $Lock\text{-}Based_{9}$ $_{10}$ approach we see similar behaviour, where the performance with 2,000 agents is bet- $_{10}$ $_{11}$ ter than with 1,500. It is not quite clear why this is the case, given the dramatically $_{11}$ $_{12}$ lower performance with 2,500 agents but it seems that 2,000 agents create much $_{12}$ $_{13}$ less lock contention due to lower free space, whereas 2,500 agents create a lot more $_{13}$ $_{14}$ lock contention due to no free space available at all.

We also measured the average retries both for *TVar* and *TArray* under 2,500¹⁵ ¹⁶ agents where the *TArray* approach shows best scaling performance with 0.01 retries ¹⁶ ¹⁷ whereas *TVar* averages at 3.28 retries. Again this can be attributed to the better ¹⁷ ¹⁸ transactional data structure which reduces retry ratio substantially to near-zero ¹⁸ ¹⁹ levels.

20 20 21 21 225.4 Going Large-Scale 22

²³To test how far we can scale up the number of cores in the *TArray* case, we ran the²³
²⁴two experiments, carrying capacity (500 agents) and rebirthing (2500 agents), on²⁴
²⁵an Amazon EC m5ad.16xlarge instance with 16, 32 and 64 cores to see if we run²⁵
²⁶into decreasing returns. The results are reported in Table 9.

Unlike in the SIR model, Sugarscapes STM *TArray* implementation does not scale up beyond 16 cores. We attribute this to a mix of retries and Amdahl's law. As retries are much more expensive in the case of Sugarscape compared to SIR, even a small increase in the retry ratio (see Table 7), leads to reduced performance. On the other hand, although the retry ratio decreases as the number of cores increases, the ratio of parallelisable work diminishes and we get bound by the sequential part of the program.

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¹5.5 Comparison with other approaches

The paper [38] reports a performance of 2,000 steps per second on a GPU on a 128x128 grid. Our best performing implementation, TArray with 500 rebirthing agents, arrives at a performance of 39 steps per second and is therefore clearly slower. However, the very high performance on the GPU does not concern us here as it follows a very different approach than ours. We focus on speeding up implementations on the CPU as directly as possible without locking overhead. When following a GPU approach one needs to map the model to the GPU which is a delicate and non-trivial matter. With our approach we show that speed up with concurrency is very possible without the low-level locking details or the need to map to GPU. Also some features like bilateral trading between agents, where a pair of agents needs to come to a conclusion over multiple synchronous steps, is difficult to implement on a GPU whereas this should be not as hard using STM. Note that we kept the grid size constant because we implemented the environment as a single agent which works sequentially on the cells to regrow the sugar. Obviously this doesn't really scale up on parallel hardware and experiments which we haven't included here due to lack of space, show that the performance goes down dramatically when we increase the environment to 128x128 with same number of agents. This is the result of Amdahl's law where the environment becomes the limiting sequential factor of the simulation. Depending on the underlying data structure used for the environment we have two options to solve this problem. In the case of the Sequential and TVar implementation we build on an indexed array, which can be updated in parallel using the existing data-parallel support in Haskell. In the case of the TArray approach we have no option but to run the update of every cell within its own thread. We leave both for further research as it is beyond the scope of this paper.

²⁹5.6 Summary

28

This case study showed clearly that besides being substantially faster than the Se^{-31} quential implementation, an STM implementation with the right transactional data structure is also able to perform considerably better than a Lock-Based approach even in the case of the Sugarscape model which has a much higher complexity

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¹in terms of agent behaviour and dramatically increased number of writes to the ²environment.

Further, this case study demonstrated that the selection of the right transactional data structure is of fundamental importance when using STM. Selecting the right transactional data structure is highly model-specific and can lead to dramatically different performance results. In this case study the TArray performed best due to many writes but in the SIR case study a TVar showed good enough results due to the very low number of writes. When not carefully selecting the right transactional data structure, which supports fine-grained concurrency, a lock-based implementation might perform as well or even outperform the STM approach as can be seen when using the TVar.

Although the TArray is the better transactional data structure overall, it might 13 14come with an overhead, performing worse on low number of cores than a TVar, Lock-14 15Based or even Sequential approach, as seen with TArray on 1 core. However, it has 15 16the benefit of quickly scaling up to multiple cores. Depending on the transactional 16 17data structure, scaling up to multiple cores hits a limit at some point. In the case of 17 16the TVar the best performance is reached with 3 cores. With the TArray we reached 18 19th 18 limit around 16 cores.

The comparison between the *Lock-Based* approach and the *TArray* implementation seems to be a bit unfair due to a very different locking structure. A more suitable comparison would be to use an indexed Array with a tuple of (MVar, Indeed, Indeed

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cause they are taken after another and therefore subject to races where they end
² up holding a lock the other needs.
3
⁴ 6 Conclusion ⁴
⁵ In this paper we investigated the potential of using STM for parallel, large scale ⁵
$^6\mathrm{ABS}$ and come to the conclusion that it is indeed a very promising alternative over 6
$^7 {\rm lock\text{-}based}$ approaches as our case studies have shown. The STM implementations 7
$^8 {\rm all}$ consistently outperformed the lock-based ones and scaled much better to larger 8
$^9\mathrm{number}$ of CPU cores. Besides, the concurrency abstractions of STM are very pow- 9
$^{10}\mathrm{erful},$ yet simple enough to allow convenient implementation of concurrent agents 10
$^{11}\mathrm{without}$ the problems of lock-based implementation. Due to most ABS being pri- $^{11}\mathrm{without}$
$^{12}\mathrm{marily}$ pure computations, which do not need interactive input from the user, files 12
$^{13}\mathrm{or}$ network during simulation, the fact that no such interactions can occur within 13
¹⁴ an agent when running within STM is not a problem.
15 Further, STM primitives map nicely to ABS concepts. When having a shared envi- 15
16 ronment, it is natural either using TVar or TArray, depending on the environments 16
17 nature. Also, there exists the $TChan$ primitive, which can be seen as a persistent 17
$^{18}\mathrm{message}$ box for agents, underlining the message-oriented approach found in many 18
19 agent-based models [39, 40]. Also TChan offers a broadcast transactional channel,
20 which supports broadcasting to listeners which maps nicely to a proactive environ- 20
$^{21}\mathrm{ment}$ or a central auctioneer upon which agents need to synchronize. The benefits 21
$^{22}\mathrm{of}$ these natural mappings are that using STM takes a big portion of burden from 22
23 the modeller as one can think in STM primitives instead of low level locks and 23
²⁴ concurrent operational details.
The strong static type system of Haskell adds another benefit. By running in the 25
$^{26} STM$ instead of 10 context makes the concurrent nature more explicit and at the 26
$^{27}\mathrm{same}$ time restricts it to purely STM behaviour. So despite obviously losing the 27
reproducibility property due to concurrency, we still can guarantee that the agents ²⁸
can't do arbitrary IO as they are restricted to STM operations only.
Depending on the nature of the transactions, retries could become a bottle neck,
resulting in a live lock in extreme cases. The central problem of STM is to keep the 31
retries low, which is directly influenced by the read/writes on the STM primitives.
By choosing more fine-grained and suitable data structures, for example using a

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$^{1}\textsc{TArray}$ instead of an indexed array within a TVar, one can reduce retries and 1
² increase performance significantly and avoid the problem of live locks as we have ²
³ shown.
⁴ Despite the indisputable benefits of using STM within a pure functional setting ⁴
⁵ like Haskell, it exists also in other imperative languages (Python, Java and C++, ⁵
⁶ etc) and we hope that our research sparks interest in the use of STM in ABS in ⁶
7 general and that other researchers pick up the idea and apply it to the established 7
⁸ imperative languages Python, Java, C++ in the ABS community as well.
9
¹⁰ 7 Further Research
¹¹ So far we only implemented a tiny bit of the Sugarscape model and left out the later ¹¹
¹² chapters which are more involved as they incorporate direct synchronous commu-
$^{13}\mathrm{nication}$ between agents. Such mechanisms are very difficult to approach in GPU^{13}
$^{14}\mathrm{based}$ approaches [38] but should be quite straightforward in STM using TChan and $^{14}\mathrm{based}$
$^{15}\mathrm{retries}.$ However, we have yet to prove how to implement reliable synchronous agent 15
16 interactions without deadlocks in STM. It might be very well the case that a truly 16
17 concurrent approach is doomed due to the following [41] (Chapter 10. Software 17
$^{18} \rm Transactional \ Memory, \ \it What \ \it Can \ \it We \ \it Not \ \it Do \ \it with \ \it STM?): \it "In \ \it general, \ the \ \it class"$
of operations that STM cannot express are those that involve multi-way communi-
²⁰ cation between threads. The simplest example is a synchronous channel, in which
$^{21}both\ the\ reader\ and\ the\ writer\ must\ be\ present\ simultaneously\ for\ the\ operation\ to^{21}$
22 go ahead. We cannot implement this in STM, at least compositionally []: the op- 22
erations need to block and have a visible effect — advertise that there is a blocked 22
24 thread — simultaneously.".
A drawback of STM is that it is not fair because all threads, which block on a
transactional primitive, have to be woken up upon a change of the primitive, thus a
27 FIFO guarantee cannot be given. We hypothesise that for most models, where the
²⁸ STM approach is applicable, this has no qualitative influence on the dynamics as
agents are assumed to act conceptually at the same time and no fairness is needed. ²⁹
$^{30}\mathrm{We}$ leave the test of this hypothesis for future research. This is connected to our
assumption that concurrent execution has no qualitative influence on the dynamics. 31
Although repeated runs with same initial conditions might lead to different results
due to nondeterminism, the dynamics follow still the same distribution as the one

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from the sequential implementation. To verify this we can make use the technique	es
² of property-based testing as shown in [33] but we leave it for further research.	2
3	3
4Declarations	4
Availability of data and materials	
5 The datasets used and/or analysed during the current study are available from the corresponding author on	5
₆ reasonable request.	6
7Competing interests	7
The authors declare that they have no competing interests.	
8 Funding	8
⁹ Not applicable.	9
¹⁰ Authors' contributions	10
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writing. POS supervised the work, gave feedback and supported the writing process. All authors read and approve	
12the final manuscript.	12
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14 discussions.	14
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17 of using pure functional programming with Haskell for implementing Agent-Based Simulations.	17
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¹⁹ study human-centric complex adaptive systems. He is a strong advocate of Object Oriented Agent-Based Social	19
Simulation. This is a novel and highly interdisciplinary research field, involving disciplines like Social Science, 20	20
Economics, Psychology, Operations Research, Geography, and Computer Science. His current research focuses on	
21Urban Sustainability and he is a co-investigator in several related projects and a member of the university's	21
"Sustainable and Resilient Cities" Research Priority Area management team. 22	22
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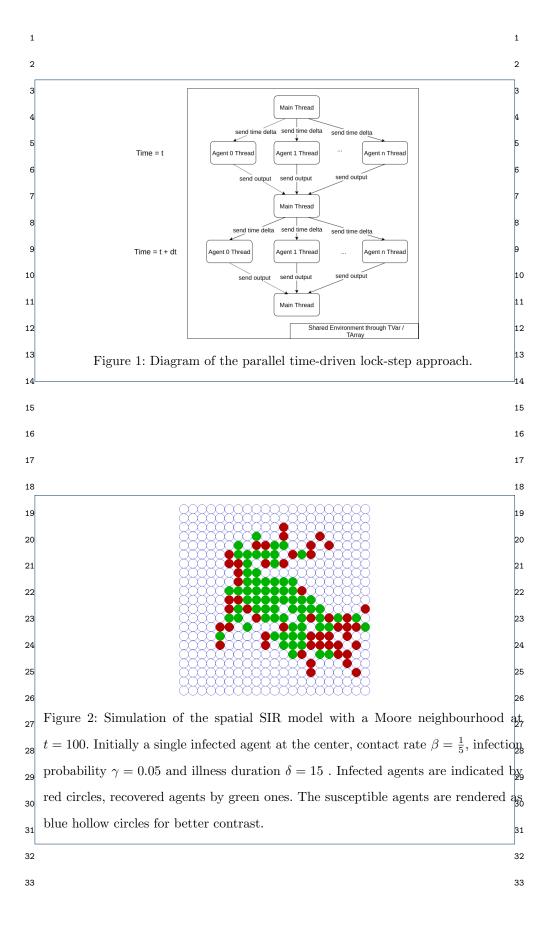
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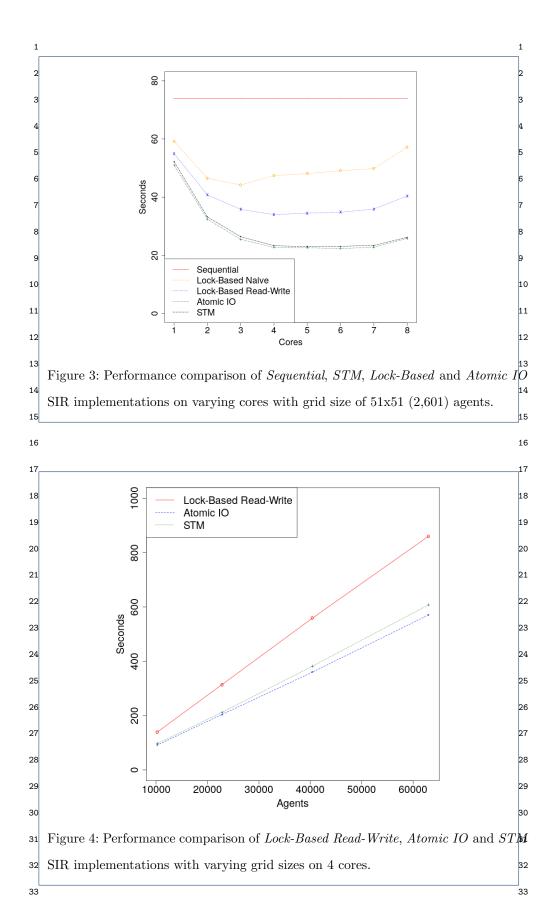
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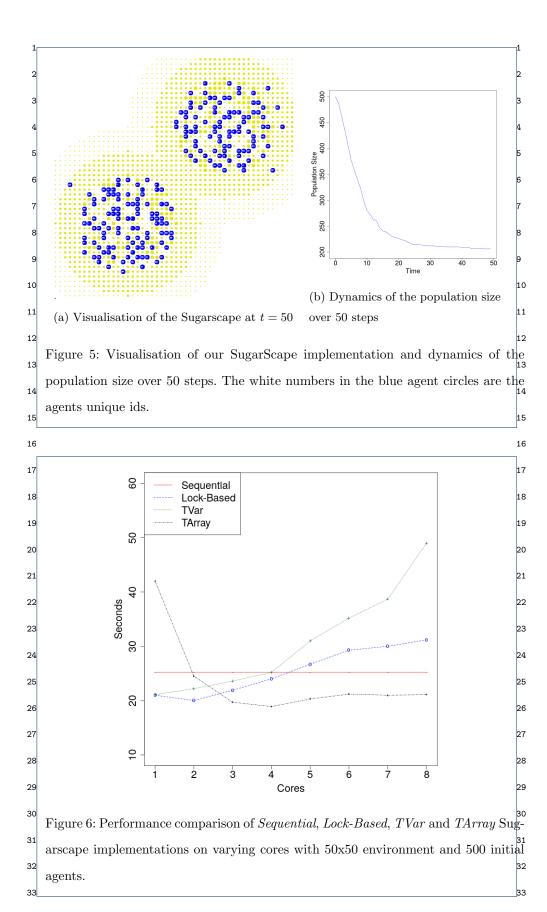
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