



The Agent's new Cloths

Towards functional programming in Agent-Based Simulation

[Anonymised review copy]

Abstract: TODO: parallelism for free because all isolated e.g. running multiple replications or parameter-variations
TODO: it is paramount not to write against the established approach but for the functional approach. not to try to come up with arguments AGAINST the object-oriented approach but IN FAVOUR for the functional approach. In the end: dont tell the people that what they do sucks and that i am the saviour with my new method but: that i have a new method which might be of interest as it has a few nice advantages.

So far, the pure functional paradigm hasn't got much attention in Agent-Based Simulation (ABS) where the dominant programming paradigm is object-orientation, with Java, Python and C++ being its most prominent representatives. We claim that functional programming using Haskell is very well suited to implement complex, real-world agent-based models and brings with it a number of benefits. In this paper we will introduce the reader to the functional programming paradigm and explain how it can be applied to implementing ABS. Further we discuss benefits and advantages. As use-case we implemented the seminal Sugarscape model in Haskell.

Keywords: Agent-Based Simulation, Functional Programming, Haskell

Introduction

- 1.1 The traditional approach to Agent-Based Simulation (ABS) has so far always been object-oriented techniques, due to the influence of the seminal work of Epstein et al Epstein & Axtell (1996) in which the authors claim "[...] object-oriented programming to be a particularly natural development environment for Sugarscape specifically and artificial societies generally [...]" (p. 179). This work established the metaphor in the ABS community, that *agents map naturally to objects* (North & Macal 2007) which still holds up today.
- 1.2 In this paper we challenge this metaphor and explore ways of approaching ABS using the functional programming paradigm as in the language Haskell. By doing this we expect to leverage the benefits of it (Hudak et al. 2007) to become available when implementing ABS functionally: expressing *what* a system is instead of *how* it works through declarative code, being explicit about the interactions of the program with the real world, explicit data-centric programming resulting in less sources of bugs and a strong static type system making type-errors at run-time obsolete.
- 1.3 We formulate the hypothesis that by using functional programming, the advantages can directly be transferred to implementing ABS. Therefore, we hypothesise, it is harder to make mistakes, the resulting simulations are easier to test and verify, guaranteed to be reproducible, have less sources of bugs and are ultimately more likely to be correct. All of this is of paramount importance in scientific computing, in which results need to be reproducible and correct.
- 1.4 We present case-studies in which we employ the well known SugarScape (Epstein & Axtell 1996) and agent-based SIR (Macal 2010) model to test our hypothesis. The former model can be seen as one of the most influential exploratory models in ABS which laid the foundations of object-oriented implementation of agent-based models. The latter one is an easy-to-understand explanatory model which has the advantage that it has an analytical theory behind it which can be used for verification and validation.
- 1.5 The aim of this paper is to show *how* to implement ABS in functional programming using Haskell and *why* it is of benefit of doing so. Further, we give the reader a good understanding of what functional programming is, what the challenges are in applying it to ABS and how we solve these in our approach. Although functional programming is a highly technical subject, we avoid technical discussions and follow a very high-level approach, focusing on the concepts instead of their implementation. For readers which are interested in technical details we refer to relevant literature in the respective parts of the paper.

1.6 The paper makes the following contributions:

- It is the first to *systematically* introduce the functional programming paradigm, as in Haskell, to ABS, identifying its benefits, difficulties and drawbacks.
- We show how functional ABS can be scaled up to massively large-scale without the problems of low level concurrent programming using Software Transactional Memory (STM). Although there exist STM implementations in non-functional languages like Java and Python, due to the nature of Haskell's type-system, the use of STM has unique benefits in this setting.
- Further we introduce a powerful and very expressive approach to testing ABS implementations using property-based testing. This allows a much more powerful way of expressing tests, shifting from unit-testing towards specification-based testing. Although property-based testing has been brought to non-functional languages like Java and Python as well, it has its origins in Haskell and it is here where it truly shines.

Concepts of Functional Programming

2.1 In our research we are using the functional programming language Haskell. The paper of (Hudak et al. 2007) gives a comprehensive overview over the history of the language, how it developed and its features and is very interesting to read and get accustomed to the background of the language. The main points why we decided to go for Haskell are:

- Rich Feature-Set - it has all fundamental concepts of the pure functional programming paradigm of which we explain the most important below.
- Real-World applications - the strength of Haskell has been proven through a vast amount of highly diverse real-world applications (Hudak et al. 2007), is applicable to a number of real-world problems (O'Sullivan et al. 2008) and has a large number of libraries available¹.
- Modern - Haskell is constantly evolving through its community and adapting to keep up with the fast changing field of computer science. Further, the community is the main source of high-quality libraries.

2.2 The roots of functional programming lie in the Lambda Calculus which was first described by Alonzo Church (Church 1936). This is a fundamentally different approach to computation than imperative and object-oriented programming which roots lie in the Turing Machine (Turing 1937). Rather than describing *how* something is computed as in the more operational approach of the Turing Machine, due to the more declarative nature of the Lambda Calculus, code in functional programming describes *what* is computed.

2.3 As a short example we give an implementation of the factorial function in Haskell: `factorial :: Integer -> Integer`
`factorial 0 = 1`
`factorial n = n * factorial (n-1)`

2.4 When looking at this function we can already see the central concepts of functional programming:

1. Declarative - we describe *what* the factorial function is rather than how to compute it. This is supported by *pattern matching* which allows to give multiple equations for the same function, matching on its input.
2. Immutable data - in functional programming we don't have mutable variables - after a variable is assigned, it cannot change its contents. This also means that there is no destructive assignment operator which can re-assign values to a variable. To change values, we employ recursion.
3. Recursion - the function calls itself with a smaller argument and will eventually reach the case of 0. Recursion is the very meat of functional programming because they are the only way to implement loops in this paradigm due to immutable data.
4. Static Types - the first line indicates the name and the types of the function. In this case the function takes one Integer as input and returns an Integer as output. Types are static in Haskell which means that there can be no type-errors at run-time e.g. when one tries to cast one type into another because this is not supported by this kind of type-system.

¹https://wiki.haskell.org/Applications_and_libraries

5. Explicit input and output - all data which are required and produced by the function have to be explicitly passed in and out of it. There exists no global mutable data whatsoever and data-flow is always explicit.
6. Referential transparency - calling this function with the same argument will *always* lead to the same result, meaning one can replace this function by its value. This means that when implementing this function one can not read from a file or open a connection to a server. This is also known as *purity* and is indicated in Haskell in the types which means that it is also guaranteed by the compiler.

- 2.5** It may seem that one runs into efficiency-problems in Haskell when using algorithms which are implemented in imperative languages through mutable data which allows in-place update of memory. The seminal work of (Okasaki 1999) showed that when approaching this problem from a functional mind-set this does not necessarily be the case. The author presents functional data structures which are asymptotically as efficient as the best imperative implementations and discusses the estimation of the complexity of lazy programs.
- 2.6** For an excellent and widely used introduction to programming in Haskell we refer to (Hutton 2016). For more in-depth discussion of functional programming we refer to: (Hughes 1989; MacLennan 1990; Hudak et al. 2007).

Side-Effects

- 2.7** One of the fundamental strengths of functional programming and Haskell is their way of dealing with side-effects in functions. A function with side-effects has observable interactions with some state outside of its explicit scope. This means that the behaviour it depends on history and that it loses its referential transparency character, which makes understanding and debugging much harder. Examples for side-effects are (amongst others): modifying a global variable, await an input from the keyboard, read or write to a file, open a connection to a server, drawing random-numbers,...
- 2.8** Obviously, to write real-world programs which interact with the outside-world we need side-effects. Haskell allows to indicate in the *type* of a function that it does or does *not* have side-effects. Further there are a broad range of different effect types available, to restrict the possible effects a function can have to only the required type. This is then ensured by the compiler which means that a program in which one tries to e.g. read a file in a function which only allows drawing random-numbers will fail to compile. Haskell also provides mechanisms to combine multiple effects e.g. one can define a function which can draw random-numbers and modify some global data. The most common side-effect types are:
- IO - Allows all kind of I/O related side-effects: reading/writing a file, creating threads, write to the standard output, read from the keyboard, opening network-connections,...
 - Rand - Allows to draw random-numbers.
 - Reader - Allows to read from an environment.
 - Writer - Allows to write to an environment.
 - State - Allows to read and write an environment.
- 2.9** A function with side-effects has to indicate this in their type e.g. if we want to give our factorial function for debugging purposes the ability to write to the standard output, we add IO to its type: `factorial :: Integer -> IO Integer`. A function without any side-effect type is called *pure*. A function with a given effect-type needs to be executed with a given effect-runner which takes all necessary parameters depending on the effect and runs a given effectful function returning its return value and depending on the effect also an effect-related result. For example when running a function with a State-effect one needs to specify the initial environment which can be read and written. After running such a function with a State-effect the effect-runner returns the changed environment in addition with the return value of the function itself. Note that we cannot call functions of different effect-types from a function with another effect-type, which would violate the guarantees. Calling a *pure* function though is always allowed because it has by definition no side-effects. An effect-runner itself is a *pure* function. The exception to this is the IO effect type which does not have a runner but originates from the *main* function which is always of type IO.
- 2.10** Although it might seem very restrictive at first, we get a number of benefits from making the type of effects we can use explicit. First we can restrict the side-effects a function can have to a very specific type which is guaranteed at compile time. This means we can have much stronger guarantees about our program and the absence

of potential errors already at compile-time which implies that we don't need test them with e.g. unit-tests. Second, because effect-runners are themselves *pure*, we can execute effectful functions in a very controlled way by making the effect-context explicit in the parameters to the effect-runner. This allows a much easier approach to isolated testing because the history of the system is made explicit.

- 2.11** For a technical, in-depth discussion of the concept of side-effects and how they are implemented in Haskell we refer to the following papers: (Moggi 1989; Wadler 1992, 1995, 1997; Jones 2002).

Functional Reactive Programming

- 2.12** Functional Reactive Programming (FRP) is a way to implement systems with continuous and discrete time-semantics in functional programming. The central concept in FRP is the Signal Function which can be understood as a process over time which maps an input- to an output-signal. A signal in turn, can be understood as a value which varies over time. Thus, signal functions have an awareness of the passing of time by having access to a Δt which are positive time-steps with which the system is sampled. In general, signal functions can be understood to be computations that represent processes, which have an input of a specific type, process it and output a new type. Note that this is an important building block to represent agents in functional programming: by implementing agents as signal functions allows us to implement them as processes which act continuously over time, which implies a time-driven approach to ABS. We have also applied the concept of FRP to event-driven ABS (Meyer 2014).
- 2.13** FRP provides a number of functions for expressing time-semantics, generating events and making state-changes of the system. They allow to change system behaviour in case of events, run signal functions, generate deterministic (after fixed time) and stochastic (exponential arrival rate) events and provide random-number streams.
- 2.14** For a technical, in-depth discussion on FRP in Haskell we refer to the following papers: (Wan & Hudak 2000; Hughes 2000, 2005; Nilsson et al. 2002; Hudak et al. 2003; Courtney et al. 2003; Perez et al. 2016; Perez 2017b)

Property-Based Testing

- 2.15** TODO: write this section
- 2.16** We found property-based testing particularly well suited for ABS. Although it is now available in a wide range of programming languages and paradigms, property-based testing has its origins in Haskell (Claessen & Hughes 2000, 2002) and we argue that for that reason it really shines in pure functional programming. Property-based testing allows to formulate *functional specifications* in code which then the property-testing library (e.g. QuickCheck (Claessen & Hughes 2000)) tries to falsify by automatically generating random test-data covering as much cases as possible. When an input is found for which the property fails, the library then reduces it to the most simple one. It is clear to see that this kind of testing is especially suited to ABS, because we can formulate specifications, meaning we describe *what* to test instead of *how* to test (again the declarative nature of functional programming shines through). Also the deductive nature of falsification in property-based testing suits very well the constructive nature of ABS.

Software Transactional Memory

- 2.17** TODO: refine this section (Harris et al. 2005) on STM ²
- 2.18** Concurrent programming is notoriously difficult to get right because reasoning about the interactions of multiple concurrently running threads and low level operational details of synchronisation primitives and locks is *very hard*. The main problems are:
- Race conditions due to forgotten locks.
 - Deadlocks resulting from inconsistent lock ordering.
 - Corruption caused by uncaught exceptions.
 - Lost wakeups induced by omitted notifications.

²We also make use of the excellent tutorial <http://book.realworldhaskell.org/read/software-transactional-memory.html>.

Worse, concurrency does not compose. It is utterly difficult to write two functions (or methods in an object) acting on concurrent data which can be composed into a larger concurrent behaviour. The reason for it is that one has to know about internal details of locking, which breaks encapsulation and makes composition depend on knowledge about their implementation. Also it is impossible to compose two functions e.g. where one withdraws some amount of money from an account and the other deposits this amount of money into a different account: one ends up with a temporary state where the money is in none of either accounts, creating an inconsistency - a potential source for errors because threads can be rescheduled at any time.

STM promises to solve all these problems for a very low cost. In STM one executes actions atomically where modifications made in such an action are invisible to other threads until the action is performed. Also the thread in which this action is run, doesn't see changes made by other threads - thus execution of STM actions are isolated. When a transaction exists one of the following things will occur:

1. If no other thread concurrently modified the same data as us, all of our modifications will simultaneously become visible to other threads.
2. Otherwise, our modifications are discarded without being performed, and our block of actions is automatically restarted.

Note that the ability to *restart* a block of actions without any visible effects is only possible due to the nature of Haskell's type-system which allows being explicit about side-effects: by restricting the effects to STM only ensures that no uncontrolled effects, which cannot be rolled-back, occur.

STM is implemented using optimistic synchronisation. This means that instead of locking access to shared data, each thread keeps a transaction log for each read and write to shared data it makes. When the transaction exists, this log is checked whether other threads have written to memory it has read - it checks whether it has a consistent view to the shared data or not. This might look like a serious overhead but the implementations are very mature by now, being very performant and the benefits outweigh its costs by far.

Applying this to our agents is very simple: because we already use Dunai / BearRiver as our FRP library, we can run in arbitrary Monadic contexts. This allows us to simply run agents within an STM Monad and execute each agent in their own thread. This allows then the agents to communicate concurrently with each other using the STM primitives without problems of explicit concurrency, making the concurrent nature of an implementation very transparent. Further through optimistic synchronisation we should arrive at a much better performance than with low level locking.

Related Research

- 3.1 The amount of research on using pure functional programming with Haskell in the field of ABS has been moderate so far. Most of the papers are related to the field of Multi Agent Systems and look into how agents can be specified using the belief-desire-intention paradigm (De Jong 2014; Sulzmann & Lam 2007; Jankovic & Such 2007).
- 3.2 A library for Discrete Event Simulation (DES) and System Dynamics in Haskell called *Aivika 3* is described in the technical report (Sorokin 2015). It is not pure, as it uses the IO under the hood and comes only with very basic features for event-driven ABS, which allows to specify simple state-based agents with timed transitions.
- 3.3 Using functional programming for DES was discussed in (Jankovic & Such 2007) where the authors explicitly mention the paradigm of FRP to be very suitable to DES.
- 3.4 A domain-specific language for developing functional reactive agent-based simulations was presented in (Vendrov et al. 2014). This language called FRABJOUS is human readable and easily understandable by domain-experts. It is not directly implemented in FRP/Haskell but is compiled to Haskell code which they claim is also readable. This supports that FRP is a suitable approach to implement ABS in Haskell. Unfortunately, the authors do not discuss their mapping of ABS to FRP on a technical level, which would be of most interest to functional programmers.
- 3.5 Object-oriented programming and simulation have a long history together as the former one emerged out of Simula 67 (Dahl 2002) which was created for simulation purposes. Simula 67 already supported Discrete Event Simulation and was highly influential for today's object-oriented languages. Although the language was important and influential, in our research we look into different approaches, orthogonal to the existing object-oriented concepts.

A functional approach

4.1 Due to the fundamentally different approaches of pure Functional Programming (pure FP) an ABS needs to be implemented fundamentally different as well compared to traditional object-oriented approaches (OO). We face the following challenges:

1. How can we represent an Agent?
In OO the obvious approach is to map an agent directly onto an object which encapsulates data and provides methods which implement the agents actions. Obviously we don't have objects in pure FP thus we need to find a different approach to represent the agents actions and to encapsulate its state.
2. How can we represent state in an Agent?
In the classic OO approach one represents the state of an Agent explicitly in mutable member variables of the object which implements the Agent. As already mentioned we don't have objects in pure FP and state is immutable which leaves us with the very tricky question how to represent state of an Agent which can be actually updated.
3. How can we implement proactivity of an Agent?
In the classic OO approach one would either expose the current time-delta in a mutable variable and implement time-dependent functions or ignore it at all and assume agents act on every step. At first this seems to be not a big deal in pure FP but when considering that it is yet unclear how to represent Agents and their state, which is directly related to time-dependent and reactive behaviour it raises the question how we can implement time-varying and reactive behaviour in a purely functional way.
4. How can we implement the agent-agent interaction?
In the classic OO approach Agents can directly invoke other Agents methods which makes direct Agent interaction *very* easy. Again this is obviously not possible in pure FP as we don't have objects with methods and mutable state inside.
5. How can we represent an environment and its various types?
In the classic OO approach an environment is almost always a mutable object which can be easily made dynamic by implementing a method which changes its state and then calling it every step as well. In pure FP we struggle with this for the same reasons we face when deciding how to represent an Agent, its state and proactivity.
6. How can we implement the agent-environment interaction?
In the classic OO approach agents simply have access to the environment either through global mechanisms (e.g. Singleton or simply global variable) or passed as parameter to a method and call methods which change the environment. Again we don't have this in pure FP as we don't have objects and globally mutable state.
7. How can we step the simulation?
In the classic OO approach agents are run one after another (with being optionally shuffled before to uniformly distribute the ordering) which ensures mutual exclusive access in the agent-agent and agent-environment interactions. Obviously in pure FP we cannot iteratively mutate a global state.
8. An Agent-Interface
How can we interface with the agent: how does the agent reveal information about itself? We will see that functional programming supports very strong encapsulation of local state which is not accessible and mutable from outside. This makes testing in some respect easier, in some harder.

Agent representation, state and proactivity

4.2 Whereas in imperative programming (the OO which we refer to in this paper is built on the imperative paradigm) the fundamental building block is the destructive assignment, in FP the building blocks are obviously functions which can be evaluated. Thus we have no other choice than to represent our Agents using a function which implements their behaviour. This function must be time-aware somehow and allow us to react to time-changes and inputs. Fortunately there exists already an approach to time-aware, reactive programming which is termed Functional Reactive Programming (FRP). This paradigm has evolved over the year and current modern FRP is built around the concept of a signal-function which transforms an input-signal into an output-signal. An input-signal can be seen as a time-varying value. Signal-functions are implemented as continuations which allows

to capture local state using closures. Modern FRP also provides feedback functions which provides convenient methods to capture and update local state from the previous time-step with an initial state provided at time = 0.

- 4.3** - pure functions don't have a notion of communication as opposed to method calls in object-oriented languages like java
- 4.4** - time is represented using the FRP concept: Signal-Functions which are sampled at (fixed) time-deltas, the dt is never visible directly but only reflected in the code and read-only. - no method calls => continuous data-flow instead
- 4.5** Viewing agent-agent interaction as simple method calls implies the following: - it takes no time - it has a synchronous and transactional character - an agent gives up control over its data / actions or at least there is always the danger that it exposes too much of its interface and implementation details. - agents equals objects, which is definitely NOT true. Agents
- 4.6** data-flow synchronous agent transactions
- 4.7** - still need transactions between two agents e.g. trading occurs over multiple steps (makeoffer, accept/refuse, finalize/abort) -> exactly define what TX means in ABS -> exclusive between 2 agents -> state-changes which occur over multiple steps and are only visible to the other agents after the TX has committed -> no read/write access to this state is allowed to other agents while the TX is active -> a TX executes in a single time-step and can have an arbitrary number of tx-steps -> it is easily possible using method-calls in OOP but in our pure functional approach it is not possible -> parallel execution is being a problem here as TX between agents are very easy with sequential -> an agent must be able to transact with as many other agents as it wants to in the same time-step -> no time passes between transactions => what we need is a 'all agents transact at the same time' -> basically we can implement it by running the SFs of the agents involved in the TX repeatedly with $dt=0$ until there are no more active TXs -> continuations (SFs) are perfectly suited for this as we can 'rollback' easily by using the SF before the TX has started

Environment representation and interaction

- 4.8** no global shared mutable environment, having different options: - non-active read-only (SIR): no agent, as additional argument to each agent - pro-active read-only (?): environment as agent, broadcast environment updates as data-flow - non-active read/write (?): no agent, StateT in agents monad stack - pro-active read/write (Sugarscape): environment as agent, StateT in agents monad stack
- 4.9** care must be taken in case of agent-transactions: when aborting/refusing all changes to the environment must be rolled back => instead of StateT use a transactional monad which allows us to revert changes to a save point at the start of the TX. if we drag the environment through all agents then we could easily revert changes but that then requires to hard-code the environment concept deep into the simulation scheduling/stepping which brings lots of inconveniences, also it would need us to fold the resulting multiple environments back into a single. If we had an environment-centric view then probably this is what we want but in ABS the focus is on the agents
- 4.10** question is if the TX sf runs in the same monad as the agent or not. i opt for identity monad which prevents modification of the Environment in a transaction
- 4.11** also need to motivate the $dt=0$ in all TX processing: conceptually it all happens instantaneously (although arbitration is sequential) but agents must act time-sensitive
- 4.12** for environment we need transactional and shared state behaviour where we can have mutual exclusive access to shared data but also roll back changes we made. it should run deterministic when running agents not truly parallel. solution: run environment in a transactional state monad (TX monad). although the agents are executed in parallel in the end it (map) runs sequentially. this passes a mutable state through all agents which can act on it and roll back actions e.g. in case of a failed agent TX. if we don't need transactional behaviour then just use StateT monad. this ensures determinism. pro active environment is also easily possible by writing to the state. this approach behaves like sequential transactional although the agents run in parallel but how is this possible when using mapMSF ?

Stepping the simulation

- 4.13** - parallel update only, sequential is deliberately abandoned due to: -> reality does not behave this way -> if we need transactional behaviour, can use STM which is more explicit -> it translates directly to a map which

is very easy to reason about (sequential is basically a fold which is much more difficult to reason about) -> is more natural in functional programming -> it exists for 'transactional' reasons where we need mutual exclusive access to environment / other agents -> we provide a more explicit mechanism for this: Agent Transactions

Case Study 1: SIR

- 5.1 TODO: write
- 5.2 - maps nicely to continuous time-semantics and state-transitions provided by FRP - STM results in considerable performance boost - property-testing can be used to directly express parts of the SD specification

Case Study 2: Sugarscape

- 6.1 TODO
- 6.2 - no need for continuous time-semantics as agents act in all time-step - main difficulty: synchronous agent-interactions - STM: not clear yet but retry factor of 5 - property-based testing: can we express hypotheses?

Conclusions

- 7.1 - being explicit and polymorph about side-effects: can have 'pure' (no side-effects except state), 'random' (can draw random-numbers), 'IO' (all bets are off), STM (concurrency) agents - hybrid between SD and ABS due to continuous time AND parallel dataFlow (parallel update-strategy)
- 7.2 Our approach is radically different from traditional approaches in the ABS community. First it builds on the already quite powerful FRP paradigm. Second, due to our continuous time approach, it forces one to think properly of time-semantics of the model and how small Δt should be. Third it requires one to think about agent interactions in a new way instead of being just method-calls.
- 7.3 Because no part of the simulation runs in the IO Monad and we do not use `unsafePerformIO` we can rule out a serious class of bugs caused by implicit data-dependencies and side-effects which can occur in traditional imperative implementations.
- 7.4 Also we can statically guarantee the reproducibility of the simulation, which means that repeated runs with the same initial conditions are guaranteed to result in the same dynamics. Although we allow side-effects within agents, we restrict them to only the Random and State Monad in a controlled, deterministic way and never use the IO Monad which guarantees the absence of non-deterministic side effects within the agents and other parts of the simulation.
- 7.5 Determinism is also ensured by fixing the Δt and not making it dependent on the performance of e.g. a rendering-loop or other system-dependent sources of non-determinism as described by Perez & Nilsson (2017). Also by using FRP we gain all the benefits from it and can use research on testing, debugging and exploring FRP systems Perez & Nilsson (2017); Perez (2017a).

Issues

- 7.6 Currently, the performance of the system is not comparable to imperative implementations but our research was not focusing on this aspect. We leave the investigation and optimization of the performance aspect of our approach for further research.
- 7.7 In our pure functional approach, agent identity is not as clear as in traditional object-oriented programming, where an agent can be hidden behind a polymorphic interface which is much more abstract than in our approach. Also the identity of an agent is much clearer in object-oriented programming due to the concept of object-identity and the encapsulation of data and methods.
- 7.8 We can conclude that the main difficulty of a pure functional approach evolves around the communication and interaction between agents, which is a direct consequence of the issue with agent identity. Agent interaction is straight-forward in object-oriented programming, where it is achieved using method-calls mutating the internal

state of the agent, but that comes at the cost of a new class of bugs due to implicit data flow. In pure functional programming these data flows are explicit but our current approach of feeding back the states of all agents as inputs is not very general. We have added further mechanisms of agent interaction which we had to omit due to lack of space.

Further Research

- 8.1 - event-driven approach - can we do DES? e.g. single queue with multiple servers? also specialist vs. generalist

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