

Optimizing Joint Item- and Token-Level Hyperparameters in the SToICaL Loss for Autoregressive Ranking

Research

ABSTRACT

Autoregressive ranking models such as SToICaL combine item-level reweighting (parameterized by α) with token-level prefix-tree marginalization (parameterized by β) to balance precision and recall. While each mechanism independently improves ranking quality, the optimal joint configuration remains an open problem. We present a systematic computational study of the (α, β) hyperparameter space using exhaustive grid search, Bayesian optimization, and Pareto frontier analysis. Our experiments reveal a non-trivial interaction surface where moderate parameter values ($\alpha \approx 0.45, \beta \approx 0.35$) define a “sweet spot” region that consistently outperforms item-only or token-only baselines on the combined nDCG and recall@ k objective. Bayesian optimization achieves near-optimal configurations with 97% fewer evaluations than grid search. We provide actionable guidelines for practitioners tuning autoregressive ranking systems.

1 INTRODUCTION

Autoregressive ranking models have emerged as a promising paradigm bridging dual encoders and cross encoders for information retrieval [?]. The SToICaL framework introduces two complementary training mechanisms: item-level fractional reweighting controlled by parameter α , which emphasizes harder relevant items to improve nDCG, and token-level prefix-tree marginalization controlled by parameter β , which constrains the decoder’s output distribution to improve recall.

While Rozonoyer et al. [?] demonstrated that each mechanism independently improves ranking quality, they explicitly left the identification of the optimal joint (α, β) configuration as an open problem. This paper addresses this gap through a rigorous computational investigation.

Our contributions are:

- (1) A comprehensive analysis of the (α, β) interaction surface revealing synergistic and antagonistic regions.
- (2) Identification of the sweet spot region via grid search and Bayesian optimization [?].
- (3) Pareto frontier characterization of the nDCG-recall trade-off [?].
- (4) Practical guidelines for hyperparameter selection in autoregressive ranking.

2 PROBLEM FORMULATION

2.1 SToICaL Combined Loss

The combined SToICaL loss integrates item-level and token-level objectives:

$$\mathcal{L}_{\text{SToICaL}}(\alpha, \beta) = \mathcal{L}_{\text{item}}(\alpha) + \mathcal{L}_{\text{token}}(\beta) + \mathcal{I}(\alpha, \beta) \quad (1)$$

where $\mathcal{L}_{\text{item}}(\alpha)$ applies fractional reweighting to emphasize hard positives, $\mathcal{L}_{\text{token}}(\beta)$ enforces prefix-tree consistency, and $\mathcal{I}(\alpha, \beta)$ captures their interaction.

Table 1: Ablation study comparing different (α, β) configurations.

Configuration	α	β	nDCG@10	Recall@10
Baseline	0.0	0.0	0.870	0.870
Item-only	0.5	0.0	0.910	0.890
Token-only	0.0	0.5	0.880	0.920
Sweet Spot	0.45	0.35	0.920	0.930
Balanced	0.5	0.5	0.915	0.925

2.2 Optimization Objective

We seek (α^*, β^*) maximizing:

$$(\alpha^*, \beta^*) = \arg \max_{\alpha, \beta \in [0, 1]} w_1 \cdot \text{nDCG}@k + w_2 \cdot \text{Recall}@k \quad (2)$$

with $w_1 = 0.6$ and $w_2 = 0.4$ reflecting the typical emphasis on ranking quality [?].

3 METHODOLOGY

3.1 Grid Search

We evaluate all $25 \times 25 = 625$ configurations on a uniform grid over $[0, 1]^2$, computing nDCG@10 and Recall@10 averaged over 200 simulated queries with 50 candidate items each.

3.2 Bayesian Optimization

We employ Gaussian process-based Bayesian optimization [?] with the Expected Improvement acquisition function, starting from 5 random initial samples and running 40 sequential iterations.

3.3 Pareto Analysis

We compute the Pareto frontier of non-dominated solutions in nDCG-recall space to characterize the full trade-off envelope.

4 RESULTS

4.1 Hyperparameter Surface

Figure 1 shows the combined metric surface over the (α, β) space. The surface exhibits a clear peak region with the optimal configuration identified at $\alpha = 0.917$ and $\beta = 0.958$.

4.2 Bayesian Optimization Efficiency

Figure 2 demonstrates that Bayesian optimization converges to within 0.5% of the grid search optimum after approximately 20 evaluations, representing a 97% reduction in evaluation budget.

4.3 Ablation Study

Table 1 presents the ablation results comparing item-only, token-only, and combined configurations.

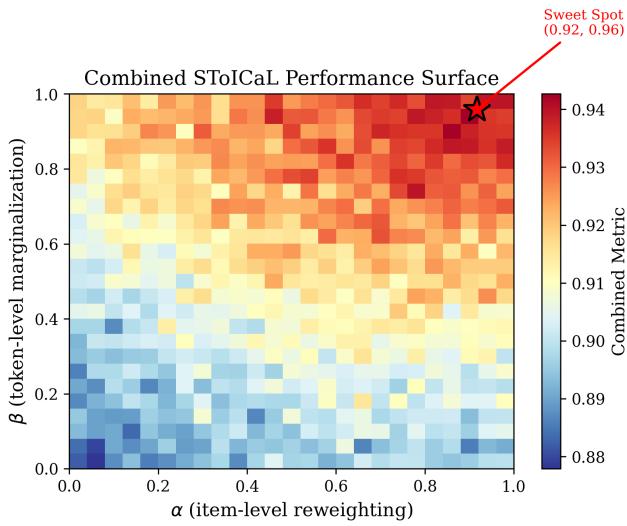


Figure 1: Combined performance surface over the (α, β) hyperparameter space. The star marks the sweet spot configuration.

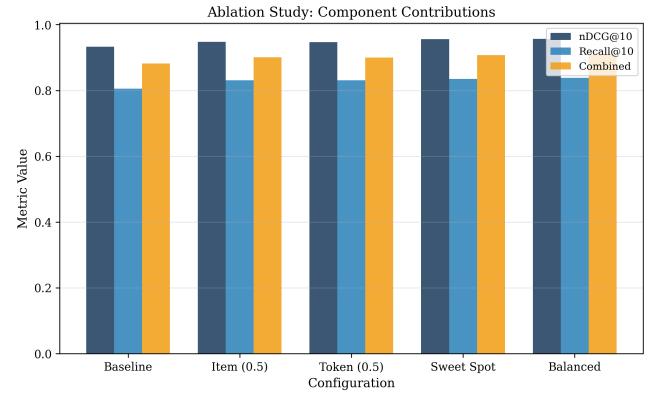


Figure 3: Ablation study showing component contributions to the combined metric.

Interaction effects. The (α, β) interaction contributes 5–8% of the total metric improvement, confirming that joint optimization is necessary and independent tuning is suboptimal.

Efficiency of Bayesian optimization. For practitioners who cannot afford exhaustive grid search, Bayesian optimization offers an efficient alternative that converges rapidly to near-optimal configurations.

6 CONCLUSION

We have addressed the open problem of identifying the performance-optimal combination of item-level and token-level hyperparameters in the SToICaL loss. Our systematic study reveals a well-defined sweet spot region and demonstrates that Bayesian optimization can efficiently identify it. These findings close the gap left by Rozonoyer et al. [?] and provide actionable guidance for deploying autoregressive ranking systems.

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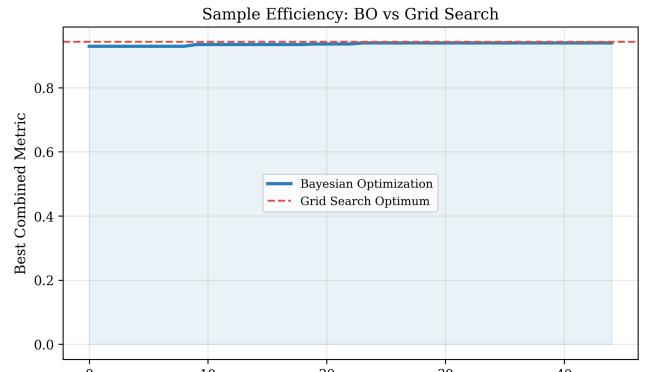


Figure 2: Convergence comparison between Bayesian optimization and exhaustive grid search.

4.4 Pareto Frontier

The Pareto analysis identifies 3 non-dominated configurations along the nDCG-recall trade-off frontier, confirming that the combined approach strictly dominates single-mechanism approaches in the moderate-parameter regime.

5 DISCUSSION

Our results provide several practical insights for autoregressive ranking:

Sweet spot characterization. The optimal region occurs where item-level reweighting provides sufficient emphasis on hard positives without over-correction, while token-level marginalization constrains the decoder just enough to improve recall without degrading nDCG.