

```
import pandas as pd
import statsmodels.formula.api as smf
```

```
# Load data set
df = pd.read_csv('swp_optimized.csv')
```

```
# Define and fit the model with state fixed effects
formula_a = 'employed ~ social_program + hsggrad + city + woman + C(region_id)'
model_a = smf.ols(formula=formula_a, data=df).fit()
```

```
# Print the summary of the model
print(model_a.summary())
```

C(region_id)[T.7]	0.0253	0.007	3.857	0.000	0.012	0.038
C(region_id)[T.8]	0.0521	0.007	7.718	0.000	0.039	0.065
C(region_id)[T.9]	-0.0150	0.007	-2.029	0.042	-0.029	-0.001
C(region_id)[T.10]	-0.0019	0.005	-0.386	0.700	-0.012	0.008
C(region_id)[T.11]	0.0519	0.006	8.342	0.000	0.040	0.064
C(region_id)[T.12]	0.0283	0.007	4.259	0.000	0.015	0.041
C(region_id)[T.13]	0.0487	0.006	7.700	0.000	0.036	0.061
C(region_id)[T.14]	0.0372	0.005	7.171	0.000	0.027	0.047
C(region_id)[T.15]	0.0430	0.006	6.946	0.000	0.031	0.055
C(region_id)[T.16]	0.0819	0.006	13.051	0.000	0.070	0.094
C(region_id)[T.17]	0.0471	0.006	7.407	0.000	0.035	0.060
C(region_id)[T.18]	-0.0038	0.006	-0.595	0.552	-0.016	0.009
C(region_id)[T.19]	-0.0211	0.007	-3.216	0.001	-0.034	-0.008
C(region_id)[T.20]	0.0096	0.006	1.489	0.137	-0.003	0.022
C(region_id)[T.21]	0.0508	0.007	7.724	0.000	0.038	0.064
C(region_id)[T.22]	0.0098	0.006	1.754	0.079	-0.001	0.021
C(region_id)[T.23]	0.0160	0.005	3.035	0.002	0.006	0.026
C(region_id)[T.24]	0.0829	0.006	13.115	0.000	0.071	0.095
C(region_id)[T.25]	-0.0014	0.006	-0.217	0.828	-0.014	0.011
C(region_id)[T.26]	0.0473	0.006	7.327	0.000	0.035	0.060
C(region_id)[T.27]	0.0019	0.007	0.298	0.766	-0.011	0.015
C(region_id)[T.28]	0.0911	0.006	14.459	0.000	0.079	0.103
C(region_id)[T.29]	0.0544	0.006	8.877	0.000	0.042	0.066
C(region_id)[T.30]	0.0645	0.007	9.615	0.000	0.051	0.078
C(region_id)[T.31]	0.0188	0.005	3.513	0.000	0.008	0.029
C(region_id)[T.32]	-0.0074	0.006	-1.205	0.228	-0.019	0.005
C(region_id)[T.33]	-0.0313	0.005	-6.362	0.000	-0.041	-0.022
C(region_id)[T.34]	0.0519	0.005	9.591	0.000	0.041	0.062
C(region_id)[T.35]	0.0461	0.006	7.188	0.000	0.034	0.059
C(region_id)[T.36]	0.0152	0.005	2.906	0.004	0.005	0.025
C(region_id)[T.37]	0.0026	0.006	0.409	0.682	-0.010	0.015
C(region_id)[T.38]	0.0221	0.006	3.405	0.001	0.009	0.035
C(region_id)[T.39]	-0.0106	0.005	-2.053	0.040	-0.021	-0.000
C(region_id)[T.40]	0.0119	0.007	1.820	0.069	-0.001	0.025
C(region_id)[T.41]	0.0346	0.006	5.363	0.000	0.022	0.047
C(region_id)[T.42]	0.0735	0.006	11.756	0.000	0.061	0.086
C(region_id)[T.43]	0.0272	0.006	4.237	0.000	0.015	0.040
C(region_id)[T.44]	0.0482	0.005	9.665	0.000	0.038	0.058
C(region_id)[T.45]	0.0722	0.006	11.262	0.000	0.060	0.085
C(region_id)[T.46]	0.0594	0.007	8.644	0.000	0.046	0.073
C(region_id)[T.47]	0.0489	0.006	7.979	0.000	0.037	0.061
C(region_id)[T.48]	0.0163	0.006	2.576	0.010	0.004	0.029
C(region_id)[T.49]	-0.0940	0.006	-14.998	0.000	-0.106	-0.082
C(region_id)[T.50]	0.0743	0.006	12.183	0.000	0.062	0.086
C(region_id)[T.51]	0.0505	0.007	7.655	0.000	0.038	0.063
social_program	-0.0367	0.001	-31.286	0.000	-0.039	-0.034
hsggrad	0.2723	0.001	242.616	0.000	0.270	0.274
city	0.0447	0.001	30.029	0.000	0.042	0.048
woman	-0.1311	0.001	-124.846	0.000	-0.133	-0.129

```
=====
Omnibus:                    4417537.097    Durbin-Watson:                    1.997
Prob(Omnibus):                0.000    Jarque-Bera (JB):                91439.248
Skew:                        -0.282    Prob(JB):                        0.00
Kurtosis:                     1.457    Cond. No.                        107.
=====
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
!pip install linearmodels
```

```

Requirement already satisfied: linearmodels in /usr/local/lib/python3.10/dist-packages (5.3)
Requirement already satisfied: numpy>=1.19.0 in /usr/local/lib/python3.10/dist-packages (from linearmodels) (1.23)
Requirement already satisfied: pandas>=1.1.0 in /usr/local/lib/python3.10/dist-packages (from linearmodels) (1.5)
Requirement already satisfied: scipy>=1.5.0 in /usr/local/lib/python3.10/dist-packages (from linearmodels) (1.11)
Requirement already satisfied: statsmodels>=0.12.0 in /usr/local/lib/python3.10/dist-packages (from linearmodels)
Requirement already satisfied: mpy-extensions>=0.4 in /usr/local/lib/python3.10/dist-packages (from linearmodels)
Requirement already satisfied: Cython>=0.29.34 in /usr/local/lib/python3.10/dist-packages (from linearmodels) (3)
Requirement already satisfied: pyhdf>=0.1 in /usr/local/lib/python3.10/dist-packages (from linearmodels) (0.2.0)
Requirement already satisfied: formulaic>=0.6.5 in /usr/local/lib/python3.10/dist-packages (from linearmodels) (0)
Requirement already satisfied: setuptools-scm[toml]<8.0.0,>=7.0.0 in /usr/local/lib/python3.10/dist-packages (fro
Requirement already satisfied: astor>=0.8 in /usr/local/lib/python3.10/dist-packages (from formulaic>=0.6.5->line
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Requirement already satisfied: typing-extensions>=4.2.0 in /usr/local/lib/python3.10/dist-packages (from formulai
Requirement already satisfied: wrapt>=1.0 in /usr/local/lib/python3.10/dist-packages (from formulaic>=0.6.5->line
Requirement already satisfied: python-dateutil>=2.8.1 in /usr/local/lib/python3.10/dist-packages (from pandas>=1.
Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.10/dist-packages (from pandas>=1.1.0->linea
Requirement already satisfied: packaging>=20.0 in /usr/local/lib/python3.10/dist-packages (from setuptools-scm[to
Requirement already satisfied: setuptools in /usr/local/lib/python3.10/dist-packages (from setuptools-scm[toml]<8
Requirement already satisfied: tomli>=1.0.0 in /usr/local/lib/python3.10/dist-packages (from setuptools-scm[toml]
Requirement already satisfied: patsy>=0.5.2 in /usr/local/lib/python3.10/dist-packages (from statsmodels>=0.12.0-
Requirement already satisfied: six in /usr/local/lib/python3.10/dist-packages (from patsy>=0.5.2->statsmodels>=0.

```

```

import pandas as pd
from linearmodels import PanelOLS
# Equivalent to Stata's xtreg
import statsmodels.api as sm

# Set the index for panel data analysis
df = df.set_index(['region_id', 'year'])

# Define the model with state fixed effects
mod = PanelOLS.from_formula('employed ~ social_program + hsgrad + city + woman + EntityEffects', df)

# Fit the model
res = mod.fit()

# Print the summary of the model
print(res)

```

#### PanelOLS Estimation Summary

```

=====
Dep. Variable:      employed      R-squared:      0.0842
Estimator:          PanelOLS      R-squared (Between): 0.3825
No. Observations:    812789      R-squared (Within):  0.0842
Date:                Tue, Nov 21 2023  R-squared (Overall): 0.2528
Time:                05:03:16      Log-likelihood      -5.427e+05
Cov. Estimator:      Unadjusted

Entities:            51      F-statistic:      1.867e+04
Avg Obs:              1.594e+04  P-value          0.0000
Min Obs:              6506.0     Distribution:      F(4,812734)
Max Obs:              7.05e+04   F-statistic (robust): 1.867e+04
Time periods:         16      P-value          0.0000
Avg Obs:              5.08e+04   Distribution:      F(4,812734)
Min Obs:              3.991e+04
Max Obs:              6.291e+04

```

#### Parameter Estimates

```

=====
Parameter  Std. Err.  T-stat  P-value  Lower CI  Upper CI
-----
social_program  -0.0367  0.0012  -31.286  0.0000  -0.0390  -0.0344
hsgrad         0.2723  0.0011  242.62   0.0000  0.2701  0.2745
city           0.0447  0.0015  30.029   0.0000  0.0418  0.0476
woman         -0.1311  0.0010  -124.85  0.0000  -0.1331  -0.1290
=====

```

```

F-test for Poolability: 74.888
P-value: 0.0000
Distribution: F(50,812734)

```

Included effects: Entity

```
# Define the model with time fixed effects
mod = PanelOLS.from_formula('employed ~ social_program + hsgrad + city + woman + TimeEffects', df)

# Fit the model
res = mod.fit()

# Print the summary of the model
print(res)
```

#### PanelOLS Estimation Summary

```
=====
Dep. Variable:      employed    R-squared:      0.0905
Estimator:          PanelOLS    R-squared (Between): 0.4981
No. Observations:    812789    R-squared (Within):  0.0819
Date:                Tue, Nov 21 2023    R-squared (Overall): 0.3192
Time:                05:03:49    Log-likelihood      -5.42e+05
Cov. Estimator:      Unadjusted

                        F-statistic:      2.021e+04
                        P-value           0.0000
Entities:              51                Distribution:  F(4,812769)
Avg Obs:              1.594e+04
Min Obs:              6506.0
Max Obs:              7.05e+04
                        F-statistic (robust): 2.021e+04
                        P-value           0.0000
Time periods:         16                Distribution:  F(4,812769)
Avg Obs:              5.08e+04
Min Obs:              3.991e+04
Max Obs:              6.291e+04
```

#### Parameter Estimates

```
=====
              Parameter  Std. Err.    T-stat    P-value    Lower CI    Upper CI
-----
social_program    0.0094    0.0022    4.1962    0.0000    0.0050    0.0138
hsgrad           0.2893    0.0011   253.60    0.0000    0.2871    0.2916
city             0.0478    0.0014   33.788    0.0000    0.0450    0.0505
woman           -0.1319    0.0010  -125.79    0.0000   -0.1340   -0.1299
=====
```

F-test for Poolability: 339.18  
P-value: 0.0000  
Distribution: F(15,812769)

Included effects: Time

```
# Define the model with both time and state fixed effects
mod = PanelOLS.from_formula('employed ~ social_program + hsgrad + city + woman + TimeEffects + EntityEffects', df)

# Fit the model
res = mod.fit()

# Print the summary of the model
print(res)
```

#### PanelOLS Estimation Summary

```
=====
Dep. Variable:      employed    R-squared:      0.0889
Estimator:          PanelOLS    R-squared (Between): 0.4733
No. Observations:    812789    R-squared (Within):  0.0825
Date:                Tue, Nov 21 2023    R-squared (Overall): 0.3049
Time:                05:20:57    Log-likelihood      -5.403e+05
Cov. Estimator:      Unadjusted

                        F-statistic:      1.984e+04
                        P-value           0.0000
Entities:              51                Distribution:  F(4,812719)
Avg Obs:              1.594e+04
Min Obs:              6506.0
Max Obs:              7.05e+04
                        F-statistic (robust): 1.984e+04
                        P-value           0.0000
Time periods:         16                Distribution:  F(4,812719)
Avg Obs:              5.08e+04
```

Min Obs: 3.991e+04  
 Max Obs: 6.291e+04

## Parameter Estimates

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
social_program	0.0014	0.0025	0.5541	0.5795	-0.0035	0.0063
hsgrad	0.2880	0.0011	251.98	0.0000	0.2857	0.2902
city	0.0429	0.0015	28.827	0.0000	0.0400	0.0458
woman	-0.1313	0.0010	-125.44	0.0000	-0.1334	-0.1293

F-test for Poolability: 133.59

P-value: 0.0000

Distribution: F(65,812719)

Included effects: Entity, Time