



# Parkour

Time limit: 2500 ms  
Memory limit: 256 MB

Catom is practicing parkour in the scaffolding of the new building in the city. The floor of the scaffolding is a grid. The cell in the  $x$ -th position to the right and the  $y$ -th position to the top has coordinates  $(x, y)$ . Each cell should contain a floor tile. But as the building is not finished, there are only  $N$  cells numbered from 1 to  $N$  that currently contains a floor tile at positions  $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$ . These tiles are glued to the floor and called *stable tiles*.

In the entrance of the building there are  $k$  floor tiles waiting to be put on the floor. These tiles are called *movable tiles*. The movable tiles are very heavy and can only be moved using a crane. Catom has a remote control for the crane but it is very complicated to operate. Catom can thus only use the crane to move a movable tile when he is on a stable tile, because he needs the balance. When a movable floor tile is placed on a cell, it does not become glued to it, so it may be moved again. In other words, Catom can replace the movable floor tiles wherever he likes when standing on a stable tile.

Parkour is the art of getting from one point to another in a complex environment. Catom starts at stable tile  $s$  and wishes to reach stable tile  $t$  under the following constraints:

- Catom can only step on floor tiles on his way.
- Catom can move from one floor tile to another only if they share a common edge.
- Catom can only move the movable tiles, and only when he is on a stable tile.

Help Catom complete his parkour training by determining for some  $(s, t, k)$  values whether or not Catom can go from stable tile  $s$  to stable tile  $t$ . You need to answer  $Q$  such queries  $(s_1, t_1, k_1), (s_2, t_2, k_2), \dots, (s_Q, t_Q, k_Q)$ .

## Standard input

To reduce the size of the input file, not all input data will be given explicitly. Instead, a set of parameters will be provided to generate the data.

The input has four integers  $N, Q, S_Q, M_k$  on the first line.  $S_Q$  is the number of queries that are explicitly given.  $M_k$  is a modulus used for generating the data.

The following  $N$  lines each have two integers as the position of one stable tile. The  $i$ -th line has  $x_i$  and  $y_i$ .

The next line has nine integer parameters  $A_s, B_s, C_s, A_t, B_t, C_t, A_k, B_k, C_k$ . These are followed by  $S_Q$  lines that each contain three integers as one query. The  $i$ -th line has  $s_i, t_i, k_i$ . The remaining queries with  $S_Q < i \leq Q$  are generated using the following rules:

- $s_i = (A_s \cdot s_{i-1} + B_s \cdot s_{i-2} + C_s) \bmod N + 1$
- $t_i = (A_t \cdot t_{i-1} + B_t \cdot t_{i-2} + C_t) \bmod N + 1$
- $k_i = (A_k \cdot k_{i-1} + B_k \cdot k_{i-2} + C_k) \bmod M_k$

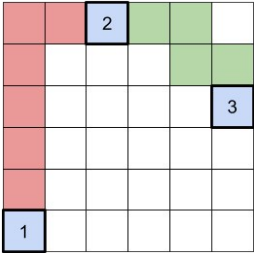
## Standard output

Let the answer to the  $i$ -th query be  $R_i$ . If Catom can reach stable tile  $t$  from stable tile  $s$  then  $R_i = 1$ , and otherwise  $R_i = 0$ . Output a single integer  $\sum_{1 \leq i \leq Q} R_i \cdot 2^i \bmod (10^9 + 7)$ , which is the combined answers to all queries.

## Constraints and notes

- $1 \leq N \leq 10^5$
- $1 \leq Q \leq 10^7$
- $2 \leq S_Q \leq Q$
- $1 \leq M_k \leq 10^9$
- $0 \leq x_i, y_i < 10^9$  for  $1 \leq i \leq N$ , all  $(x_i, y_i)$  are unique.
- $1 \leq s_i, t_i \leq N, 0 \leq k_i < M_k$  for  $1 \leq i \leq Q$
- $0 \leq A_s, B_s, C_s, A_t, B_t, C_t, A_k, B_k, C_k \leq 10^9$

- For 25% of the test data,  $N, Q \leq 500$ .
- For another 25% of the test data,  $N, Q \leq 10^5$  and  $1 \leq M_k \leq 4$ .
- For another 25% of the test data,  $N, Q \leq 10^5$ .

Input	Output	Explanation
<pre>3 2 2 100 0 0 2 5 5 3 0 0 0 0 0 0 0 0 1 3 6 2 1 5</pre>	<pre>2</pre>	<p>All stable tile positions and queries are explicitly given. The three stable tiles are illustrated below in blue.</p>  <p>For the query <math>s_1 = 1, t_1 = 3, k_1 = 6</math> the answer should be <math>R_1 = 1</math>, because Catom can put the 6 movable floor tiles in a path from stable tile 1 to stable tile 2 (shown in red), go to stable tile 2, then move 4 of the movable tiles to connect stable tile 2 and stable tile 3 (shown in green) and finally get to stable tile 3.</p> <p>For the query <math>s_2 = 2, t_2 = 1, k_2 = 5</math> the answer should be <math>R_2 = 0</math> since Catom can not reach stable tile 1 with fewer than 6 movable tiles.</p> <p>The answer is therefore <math>(R_1 \cdot 2^1 + R_2 \cdot 2^2) \bmod (10^9 + 7) = (1 \cdot 2 + 0 \cdot 4) \bmod (10^9 + 7) = 2</math></p>
<pre>3 7 2 9 0 0 2 5 5 3 7 8 10 3 2 1 5 4 59 1 3 6 2 1 5</pre>	<pre>242</pre>	<p>Just 2 queries are explicitly given. The three stable tiles are the same as in test case #1.</p> <p>The 7 queries are</p> <pre>1 1 3 6 2 2 1 5 3 3 2 0 4 3 1 7 5 2 3 4 6 1 1 8 7 1 2 7</pre> <p><math>R_1, R_4, R_5, R_6, R_7 = 1</math></p> <p><math>R_2, R_3 = 0</math></p>

Input	Output	Explanation
		<p>The answer is therefore <math>(R_1 \cdot 2^1 + R_2 \cdot 2^2 + \dots + R_7 \cdot 2^7) \bmod (10^9 + 7)</math></p> <p><math>= (1 \cdot 2 + 0 \cdot 4 + 0 \cdot 8 + 1 \cdot 16 + 1 \cdot 32 + 1 \cdot 64 + 1 \cdot 128) \bmod (10^9 + 7)</math></p> <p><math>= 242</math></p>