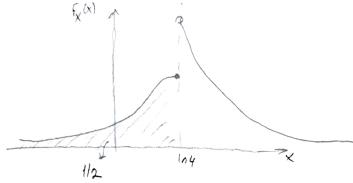
EE230 HW3

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$$\int_{-\infty}^{64} f_{x}(x)dx = \frac{1}{2}$$

$$\int_{104}^{64} f_{x}(x)dx = \frac{1}{2}$$

$$\int_{104}^{2} f_{x}(x)dx = \frac{1}{2}$$

$$\int_{104}^{\infty} x \lambda e^{\lambda x} dx = \int_{104}^{104} dx = \int$$

$$\frac{-\infty}{|n2-1|} \frac{|n4|}{|n2+1|}$$

$$\frac{|n4|}{|n2-1|} \frac{|n4|}{|n2+1|}$$

$$= \int_{\frac{x-n4}{pm}}^{\frac{x-n4}{pm}} \frac{e^{-\frac{(x-n4)^{2}}{2-2}}}{e^{-\frac{x}{2-2}}} dx + |n4| \int_{\frac{x-n4}{pm}}^{\frac{x-n4}{pm}} \frac{e^{-\frac{(x-n4)^{2}}{2-2}}}{e^{-\frac{x}{2-2}}} dx$$

$$-1 = \int \frac{x - \ln 4}{x - \ln 4} e^{\frac{-(x - \ln 4)^2}{2\sigma^2}} dx \qquad (x - \ln 4)^2 = \frac{1}{2\sigma^2}$$

$$= \frac{1}{2\sigma^2} \int \frac{1}{12\pi} \frac{e^{2\sigma^2}}{\sigma^2} dx \qquad (x - \ln 4)^2 = \frac{1}{2\sigma^2}$$

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$$= \frac{1}{2\sigma^2} \int \frac{1}{12\sigma^2} \frac{1}{\sigma^2} \frac{1}{\sigma^$$

$$Var(x) = E[x^{2}] - (E[x])^{2}$$

$$= \int_{0}^{h_{1}} \frac{x^{2}}{km} e^{-\frac{1}{2}\frac{(h_{1}h_{1})^{2}}{k}} dx + \int_{h_{1}h_{1}}^{h_{2}} x^{2} \lambda e^{-\lambda x} dx - (h_{1}h_{1})^{2}$$

$$= \int_{0}^{h_{1}} \frac{x^{2}}{km} e^{-\frac{1}{2}\frac{(h_{1}h_{1})^{2}}{k}} dx + \int_{h_{1}h_{1}}^{h_{2}} x^{2} \lambda e^{-\lambda x} dx - (h_{1}h_{1})^{2}$$

$$= \int_{0}^{h_{1}} \int_{0}^{h_{2}} x^{2} \lambda e^{-\lambda x} dx + 2h_{1}h_{2} \int_{0}^{h_{2}} x^{2} \lambda e^{-\lambda x} dx - (h_{1}h_{1})^{2}$$

$$= \int_{\frac{1}{2}}^{h_{1}} \int_{0}^{h_{2}} x^{2} \lambda e^{-\lambda x} dx + 2h_{1}h_{2} \int_{0}^{h_{2}} x^{2}$$

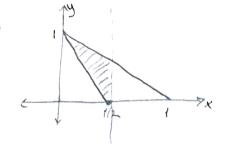
$$Var(x) = \pi + \ln 4$$

1d) For
$$x \le \ln 4$$

$$CDF = D\left(\frac{x-u}{\sigma}\right) = D\left(\frac{x-\ln 4}{2\pi u}\right)$$
For $x \ge 4$

$$CDF = \frac{1}{2} + \int_{104}^{x} e^{-\lambda x} dx = \frac{1}{2} + \left(-e^{-\lambda x}\right)\Big|_{104}^{\infty} = 1 - e^{-\lambda x}$$

$$F_{\chi}(x) = \left(\begin{array}{c} \Phi\left(\frac{x-\ln 4}{1/2\pi i}\right) \right) \times \leq \ln 4 \\ 1 - e^{-x/2} \right) \times 2 \ln 4 \end{array}$$



$$P(x \le \frac{1}{2}) = \int_{0}^{1/2} \int_{1-2x}^{1/2} dy dx$$

$$= \int_{0}^{1/2} (6y^{2}) \Big|_{1-2x}^{1-2x} dx$$

$$= \int_{0}^{1/2} \left(6y^{2}\right) \Big|_{1-2x}^{1-2x} dx$$

$$= \int_{0}^{1/2} \left(6y^{$$

2b)
$$f_{Y}(y) = \int f_{xy}(x,y) dx$$

$$= \int (2y) dx = |2y(1-y)|^{1-y}$$

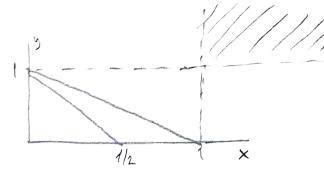
$$= \int 2 dx = |3y(1-y)|^{1-y}$$

$$F_{X,y}(\frac{1}{2},\frac{1}{2}) = \iint_{0}^{1/2} 12y \, dx \, dy$$

$$= \iint_{0}^{1/2} 12y \left(\frac{1+1+y}{2}\right) \, dy$$

$$= \iint_{0}^{1/2} 6y^{2} \, dy = \left(2y^{3}\right)\Big|_{0}^{1/2} = \left[\frac{1}{4}\right]$$

2d)



33)
$$f_{x}(\lambda) = \int_{-\infty}^{\infty} \frac{1}{2\pi |x_{x}|^{2} \sqrt{|x_{y}|^{2}}} e^{\frac{1}{2(x_{y}|x_{y}|^{2})}} e^{\frac{1}{2(x_{y}|x_{y}|x_{y}|^{2})}} e^{\frac{1}{2(x_{y}|x_{y}|x_{y}|^{2})}} e^{\frac{1}{2(x_{y}|x_{y}|x_{y}|x_{y}|^{2})}} e^{\frac{1}{$$

$$f_{X|Y}(x|y) = \frac{f_{X,Y}(xy)}{f_{Y}(xy)}$$

$$= \frac{1}{x_{X}} \underbrace{\frac{1}{x_{Y}} \underbrace{\frac{x^{2}}{x_{Y}^{2}} + \frac{x^{2}}{x_{Y}^{2}} - \frac{1}{x_{X}^{2}} \underbrace{\frac{y^{2}}{x_{X}^{2}}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}}}_{1} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} \underbrace{\frac{y^{2}}{x_{X}^{2}} + \frac{y^{2}}{x_{X}^{2}} + \frac{y$$

3d)

For siven 4,
$$(X-\hat{X})$$
 is a gaussian random while with $E[x-\hat{X}] = E[X] - \hat{X} = 0$ and $var(X-\hat{X}) = var(X) = (1-p^2) \sigma_X^2$.

Therefore, $E[(x-\hat{X})] = var(x-\hat{X}) + (E[x-\hat{X}])^2$

I) $MSE = (1-p)\sigma_X^2$

The MSE vs p curves obtained both theoretically and in simulation are plotted in the figure below.

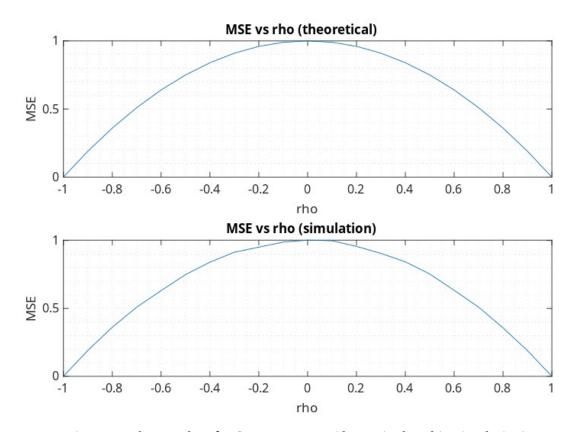


Figure 1: The graphs of MSE vs p curves (theoretical and in simulation)

We obtained similar graphs for analytical and numerical results. Since we used too many samples (N = 1E5) to calculate MSE numerically, we obtained almost smooth curve. From graph, we can observe that the MSE becomes smaller as ρ becomes greater in magnitude.