

5a)

$$Z_n = \frac{1}{\sqrt{n}} \left(\sum_{i=1}^n \frac{X_i - 1}{1} \right) = \frac{1}{\sqrt{n}} \left(\sum_{i=1}^n X_i - n \right)$$

$$P_{X_i}(k) = e^{-1} \frac{1^k}{k!} = \frac{1}{e k!}$$

$$Z_n \sqrt{n} + n = \sum_{i=1}^n X_i$$

$$\mu_{X_i}(s) = e^{(e^s - 1)}$$

$$E[e^{s(X_1 + X_2 + \dots + X_n)}] = (E[e^{sX_i}])^n = e^{n(e^s - 1)} \leftarrow \text{Transform of Poisson with } \mu = n$$

$\sqrt{n} Z_n + n$ is a poisson random variable with mean n .

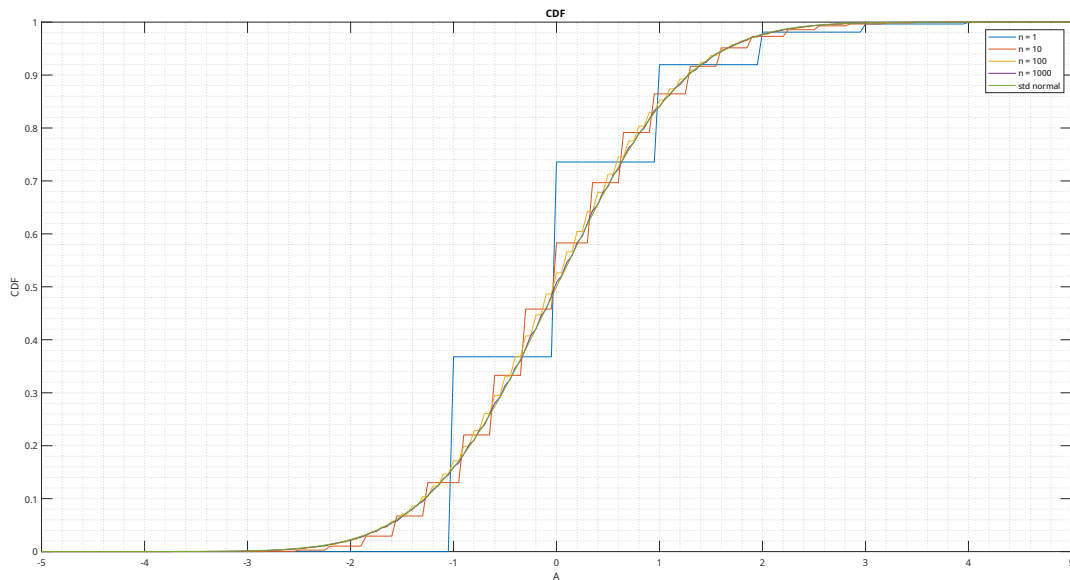


Figure 1: CDF of Z_n for $n = \{1, 10, 100, 1000\}$ and standard normal

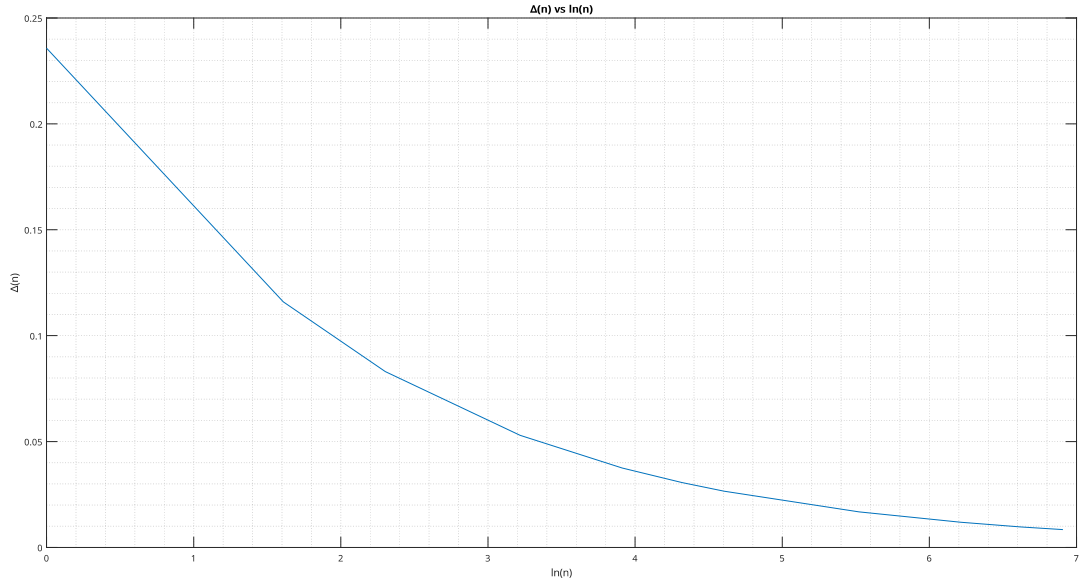


Figure 2: Graph of $\Delta(n)$ vs $\ln(n)$

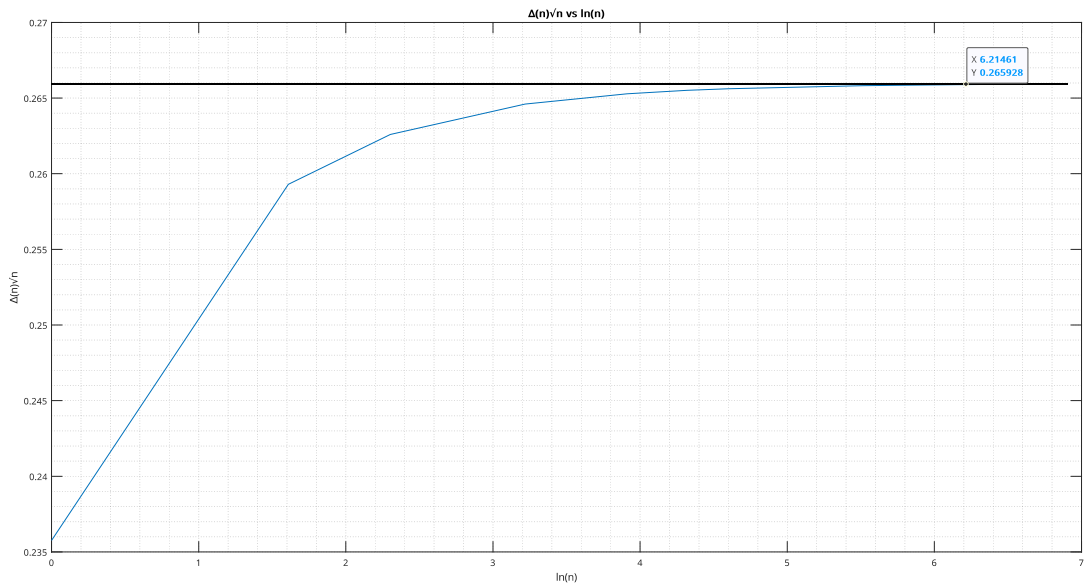


Figure 3: Graph of $\Delta(n) \cdot \sqrt{n}$ vs $\ln(n)$

From figure 1, we can see that as n approaches to infinity, cdf of Z_n approaches to cdf of standard normal.

From figure 2, we can see that the maximum difference between cdf of Z_n and cdf of standard normal for the values of A decreases as n increases.

From figure 3, we can see that one can find a $K > 0.27$ that satisfies the condition stated in step h for the values of n considered.