

EE230 Homework-1

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1.

a)

$$\Omega = \{x | x \in N, x > 0\}$$

The sample space consists of natural numbers greater than 0. The number represents number of total flipping before someone wins. For example, 2 represents that Ayşe get tail in the first trial, and Bora get head in his first trial. Any number represents that Ayşe wins if the remainder from the division of the number by 3 is 1, and represents Bora wins if the remainder is 2, and represents Ceyda wins otherwise.

b)

$$A = \{x | x \in \Omega, x \% 3 = 1\}$$

$$B = \{x | x \in \Omega, x \% 3 = 2\}$$

$$A \cup B = \{x | x \in \Omega, x \% 3 \neq 0\}$$

$$(A \cup B)^c = \{x | x \in \Omega, x \% 3 = 0\}$$

c)

Let the events E_k be defined as follows:

E_k : the event for the case that first $k-1$ trial is tail and k th trial is head.

Then we can write events A and B in terms of E_k as follows:

$$A = E_1 \cup E_4 \cup E_7 \cup \dots$$

$$B = E_2 \cup E_5 \cup E_8 \cup \dots$$

Since these events are disjoint, we can calculate the probabilities as follows:

$$P(A) = P(E_1) + P(E_4) + P(E_7) + \dots$$

$$P(B) = P(E_2) + P(E_5) + P(E_8) + \dots$$

The probability of E_k can be calculated as:

$$P(E_k) = (1 - p)^{k-1} * p$$