

Vilnius University  
Mathematics and Informatics Faculty  
Institute of Informatics  
Bioinformatics study program

**Protein thermostability prediction using sequence  
representations from protein language models**

**Baltymų termostabilumo nusakymas naudojant sekų  
reprezentacijas iš baltymų kalbos modelių**

Author: Ieva Pudžiuvėlytė  
Supervisor: Dr. Kliment Olechnovič

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# Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>Materials and methods</b>	<b>4</b>
2.1	Protein language models . . . . .	4
2.2	ESM-1b embeddings . . . . .	4
2.3	ProtTrans embeddings . . . . .	5
2.4	Training and evaluation data set . . . . .	6
2.5	Components' correlation analysis . . . . .	7
2.6	Analysed representations . . . . .	7
2.7	Analysed architectures . . . . .	9
<b>3</b>	<b>Results</b>	<b>11</b>
3.1	Correlation analysis of embeddings' components . . . . .	11
3.2	Representation analysis . . . . .	17
3.3	Architecture analysis . . . . .	20
<b>4</b>	<b>Conclusions</b>	<b>21</b>
<b>5</b>	<b>Availability</b>	<b>22</b>
<b>6</b>	<b>Abstract in Lithuanian (Santrauka)</b>	<b>23</b>

# 1 Introduction

This work is a continuation of the previous work - the model that performed binary classification into thermostability classes. The model, which was a single-layer perceptron (SLP), took protein language model’s ESM-1b [1] protein embeddings as input and provided prediction for each protein, how likely it belongs to the thermostable class.

The classes of thermostability were defined the following way: proteins that were considered as stable in lower than 65 degrees of Celsius were labelled with '0' and the remaining proteins were labelled with '1'.

The classifier was trained on the data set [2] that contained proteome identifiers, which were used to collect proteins. The data set also contained information about organism’s growth temperature, therefore proteins that belonged to a particular proteome were labelled accordingly.

Although the classifier showed promising results, yet an important downside of the developed method was emphasized - since ESM-1b embeddings generation was limited by the size of the protein, the model could not provide predictions for proteins that were longer than 1022 amino acids. For this reason, it was decided to try ProtTrans [3] embeddings as an input for the classification model.

Furthermore, it was interesting to exploit not only mean embeddings, but also to check whether a different summarisation of per residue embeddings would improve the performance of the classification model.

In addition to these fixed tasks, another objective of this work was to examine whether other variants of model architectures would improve the classifier’s results.

The results of this analysis showed that the best embeddings representations to use until the final training data set is established are ProtTrans mean and octiles representations. Additionally, it was observed that the most suitable model of those that were tested in this work for protein classification in terms of thermostability is the feed-forward neural network with two hidden layers.

These results contribute to the further development of the final method for binary protein classification into thermostability classes.

## 2 Materials and methods

### 2.1 Protein language models

Protein language models are transformer models trained on protein sequences. The transformer is a neural network model, which is made of encoder-decoder architecture that relies entirely on self-attention [4]. Attention in deep learning is a mechanism that finds the most influential factors in the data and focuses on them when it processes the input. Particularly, self-attention is a component of the network’s architecture that quantifies dependencies between the input elements.

The encoder part provides continuous representations of the input composed of sequences of symbols, meanwhile the decoder part generates output for each symbol in the input sequence. For this principle of architecture, transformers can be trained in an unsupervised fashion and be applied to natural language processing (NLP) tasks at which they produce state-of-the-art results [5].

Since amino acid sequences can be considered as a particular language, transformer architectures were applied to solve tasks related to protein biology or molecule modelling *in silico*. Attention mechanisms in models of transformer architecture, taking BERT-like model as an example [6], are capable to capture the folding structure, binding sites, and complex biophysical properties of proteins.

This work continues to exploit the transfer learning by taking protein representations from the last layer of protein language models and passing them as input to the classification model (Figure 1).

### 2.2 ESM-1b embeddings

Due to the novelty of embeddings, a considerably good performance of protein language models, and a recently emerged availability of embeddings, it was decided to develop a neural network model that would take protein embeddings as input and give the thermostability class label as output.

ESM-1b is one of evolutionary scale models trained by Facebook Research [1]. The model

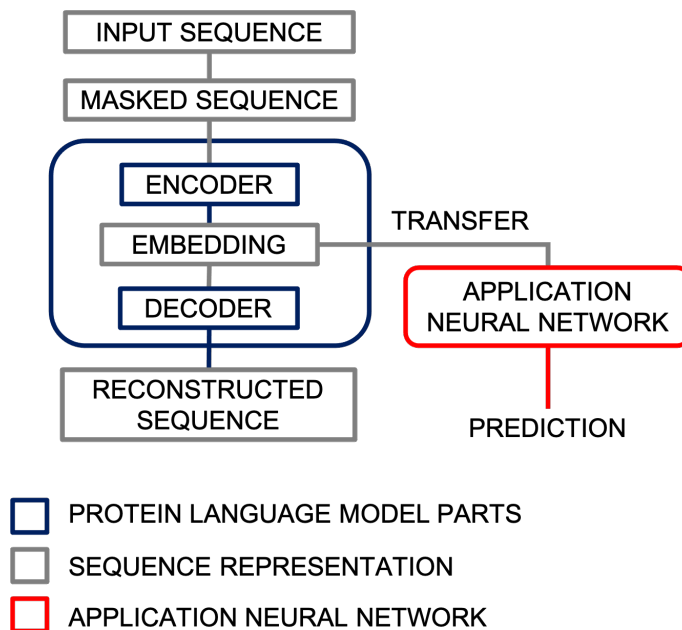


Figure 1: The scheme of embeddings from protein language model usage in the application neural network model

has 33 layers and 650 million parameters. The model was trained in an unsupervised fashion on UniRef50 data set (accessed March 28, 2018)[7]. In order to ensure determinism in the validation set, authors removed protein sequences that were longer than 1024 amino acids.

The authors made a script to extract model’s embeddings available in the repository "Evolutionary Scale Modelling". The script allows to choose from which model and layer embeddings will be taken, what embeddings (mean, per amino acid, or beginning of the sequence token) to keep. In the result of using the script, a vector of 1280 dimensions for each protein is generated.

The fact that sequences longer than 1024 amino acids were removed from the validation data set for ESM-1b model’s training implies to the limitation of model’s embeddings, which cannot be generated for sequences longer than 1022 amino acids (two more amino acids are removed due to beginning and end tokens needed for the encoding).

## 2.3 ProtTrans embeddings

ProtTrans [3] is a collection of protein language models (LMs) that were trained to learn information about proteins and encode it. ProtTrans embeddings are vector representations

taken from the last hidden state of the protein LM.

In particular, ProtT5-XL model was used in this work and exactly this model will be referred to by the name of 'ProtTrans'. Overall, this model has 24 layers. In particular, the size of the hidden layer, from which the embedding is taken, is 1024. This model was trained on BFD-100 data set [8], [9] and fine-tuned on UniRef50. Since ProtT5-XL model was considered by the authors as the best-performing model, it was chosen to be applied in this work. Additionally, this model does not have positional encoding limit, which means that there is no predetermined limitation for the protein's size to generate its embedding.

Furthermore, according to the article, in which ProtTrans project was published, ProtT5-XL models (trained on BFD-100 and UniRef50 data sets separately) outperformed ESM-1b [1] model.

## 2.4 Training and evaluation data set

In this work two types of data sets were used: for the analysis of principal components' the data set was directly inherited from the previous work: a subset of the data set of 21498 annotated organisms [2], which is identified as '003' data set, and the filtered version of it.

'003' was constructed to be balanced and that a single taxonomy identifier from the collection of annotated organisms would be present only in either training, validation, or testing subset. Proportions that were chosen to divide '003' data set were 70%, 15%, and 15% for training, validation, and testing sets respectively. Additionally, since this data set was first created with an intention to test the classifier that used ESM-1b embeddings as input, all sequences included in '003' are no longer than 1022 amino acids.

However, the analysis of other representations was carried out using '003' data set that was filtered from identically matching sequences to get more accurate evaluations.

Table 1: Number of sequences with embeddings before and after filtering the data set

Subset	Original	After filtering
Training	284309	283360
Validation	65156	63158
Testing	73662	73308

Table 2: Number of sequences with embeddings in each class before and after filtering the data set

Class	Original	After filtering
0	216595	212129
1	212729	207697

## 2.5 Components’ correlation analysis

As a consequence of the former work, this thesis includes analysis of ProtTrans protein language model’s mean embeddings usage in protein classification. Yet also, since one of the tasks of this work (given in the section 2.6) is to try joined ESM-1b and ProtTrans representations as an input to the thermostability classification model, the correlation coefficients between the components of mean embeddings were analysed.

For this analysis only a small subset of ‘003’ data set was chosen (Table 3).

Table 3: Number of sequences with embeddings used for correlation analysis

Class ‘0’	Class ‘1’	Overall
6096	6150	12246

Besides the original mean embeddings, principal components that explain 95% of variance of ESM-1b and ProtTrans mean embeddings (527 and 443 components for each language model respectively) were retrieved and taken for the correlation analysis.

## 2.6 Analysed representations

Both protein language models - ESM-1b and ProtTrans - provide per token or per residue representations - each amino acid of the protein gets a 1280 or 1024-dimensional vector from ESM-1b or ProtTrans model respectively. Therefore, each protein is originally represented by the  $m \times n$  matrix, where  $m$  is the number of dimensions of the chosen type of embedding and  $n$  is the number of amino acids that compose the protein. These representations are processed to get vectors with the same dimension for each protein in the data set.

Additionally, it was decided to analyse whether a normalisation of embeddings determines better results. Both ESM-1b and ProtTrans embeddings were normalised using the standard score principle for each element of the embedding (Eq. 1). The procedure was executed for

both types of protein language models’ embeddings separately. The training set’s embeddings were used to calculate means and standard deviations of each component, which resulted in 1024 and 1280 means and standard deviations for ProtTrans and ESM-1b cases respectively.

$$z_i = \frac{x_i - \mu_i}{\sigma_i}, \text{ where } i \in \{1, 2, \dots, m\} \subset \mathbb{N}, \text{ where } m \in \{1024, 1280\} \quad (1)$$

The normalised mean embeddings of protein language models were used separately and joined together.

Eventually, the representations included in the analysis were:

1. Mean ESM-1b and ProtTrans
2. Joined mean ESM-1b and ProtTrans
3. Normalised mean ESM-1b and ProtTrans
4. Joined normalised mean ESM-1b and ProtTrans
5. Median ESM-1b and ProtTrans
6. Minimum, median, and maximum ESM-1b and ProtTrans
7. Quantiles (including minimum and maximum) ESM-1b and ProtTrans
8. Quantiles (including minimum and maximum) and mean ESM-1b and ProtTrans
9. Octiles (including minimum and maximum) ESM-1b and ProtTrans

Table 4: Sizes of the analysed representations’ vectors

Representation	ESM-1b	ProtTrans
Mean	1280	1024
Joined mean	2304	
Median	1280	1024
Minimum, median, maximum	3840	3072
Quantiles	6400	5120
Quantiles and mean	7680	6144
Octiles	11520	9216



## 2.7 Analysed architectures

All representations that were described in the previous section were taken as input for the baseline single-layer perceptron models, although another important part of this work was to explore several different model architectures.

Architectures that were chosen to run experiments with had one or two hidden layers. The sizes of hidden layers were chosen to be original embeddings size divided by several multiples of 2 (Tables 5 and 6, Figures 3 and 4). That is, since the size of the ESM-1b embedding is 1280, there were models defined with one hidden layer of size 640, 320, or 160 that take ESM-1b embeddings as input. For models with two hidden layers, sizes of hidden layers were assigned by combining two sequential sizes received from division. Analogously, the same operation was done for models adjusted for ProtTrans.

In order to compare the SLP results with the results of new architectures, for all models batch size equal to 24, and Adam optimiser [10] with learning rate of 0.0001 were chosen. Activation function was chosen to be sigmoid (coinciding with the previous work) and loss function - cross entropy loss adjusted for binary classification case (the main reason for it was to unify loss functions between binary and multiclass classification, which was put to the test out of this work’s scope). The later change determined insignificantly different prediction values compared to the prediction values from the earlier work.

As previously, the output of all models is a number from the interval between 0 and 1 (both included). The binary class label is assigned using the threshold of 0.5: if the prediction is greater than or equal to 0.5, the protein is considered as thermostable (gets a label '1'), otherwise the protein’s label is assigned to be '0'.

Table 5: Models that were tested with ESM-1b embeddings input

Model	Number of hidden layers	Size of hidden layers
C2H2_h640-320	2	640, 320
C2H2_h320-160	2	320, 160
C2H1_h640	1	640
C2H1_h320	1	320
C2H1_h160	1	160
SLP_ESM-1b	0	-

Table 6: Models that were tested with ProtTrans embeddings input

Model	Number of hidden layers	Size of hidden layers
C2H2_h512-256	2	512, 256
C2H2_h256-128	2	256, 128
C2H1_h512	1	512
C2H1_h256	1	256
C2H1_h128	1	128
SLP_ProtTrans	0	-

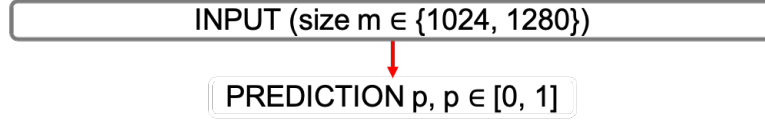


Figure 2: A scheme of a single layer perceptron classification model

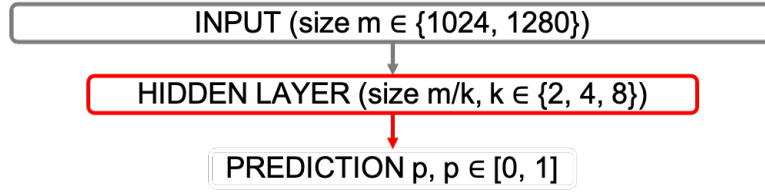


Figure 3: A scheme of classification model with one hidden layer

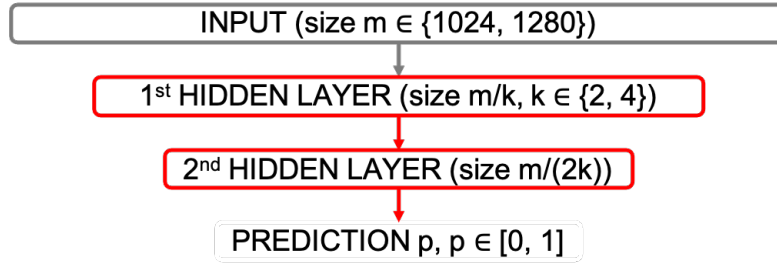


Figure 4: A scheme of classification model with two hidden layers

## 3 Results

### 3.1 Correlation analysis of embeddings' components

The results of the analysis showed that there are five ESM-1b embeddings' components that have absolute correlation coefficients higher than 0.5 with more than 10 ProtTrans embeddings' components (Figure 5). However, overall the majority of components' pairs had correlation coefficients close to zero (Figure 6).

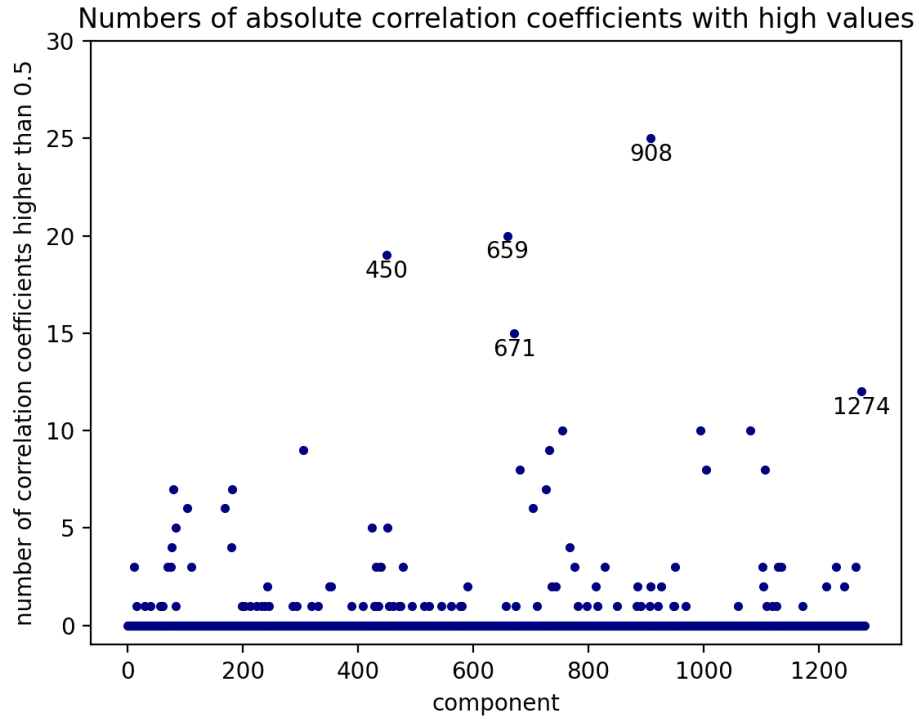


Figure 5: Plot of ESM-1b components that have got high absolute correlation coefficients with ProtTrans components

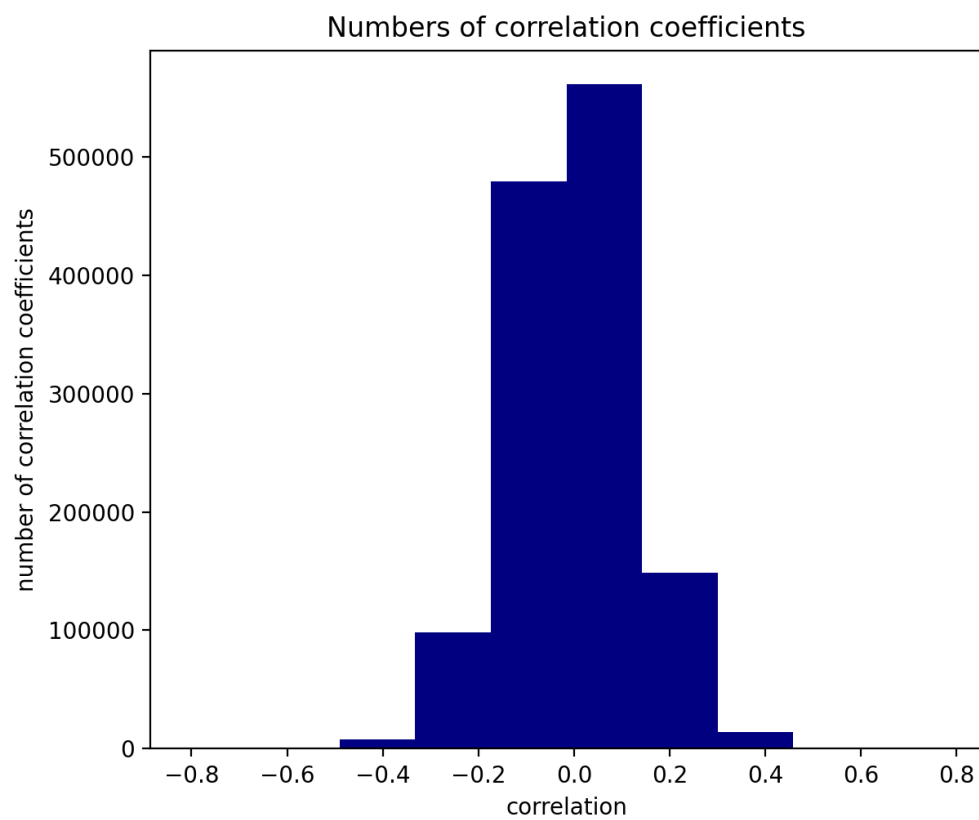


Figure 6: Histogram of correlation coefficients between ESM-1b and ProtTrans components

The plot that visualises absolute maximum correlation coefficients between pairs of components (Figure 7) shows that there are peaks at ESM-1b positions that correspond with positions that have the biggest number of high (absolute value above 0.5) correlation coefficients (Figure 5). Therefore, it can be concluded that there are no intervals of ESM-1b components that have a considerably high correlation with ProtTrans components.

The observations that can be made from the plot of averaged correlation coefficients (Figure 7) do not change the overview of the correlation between ESM-1b and ProtTrans components - the overall mean of correlation coefficients is around 0.1.

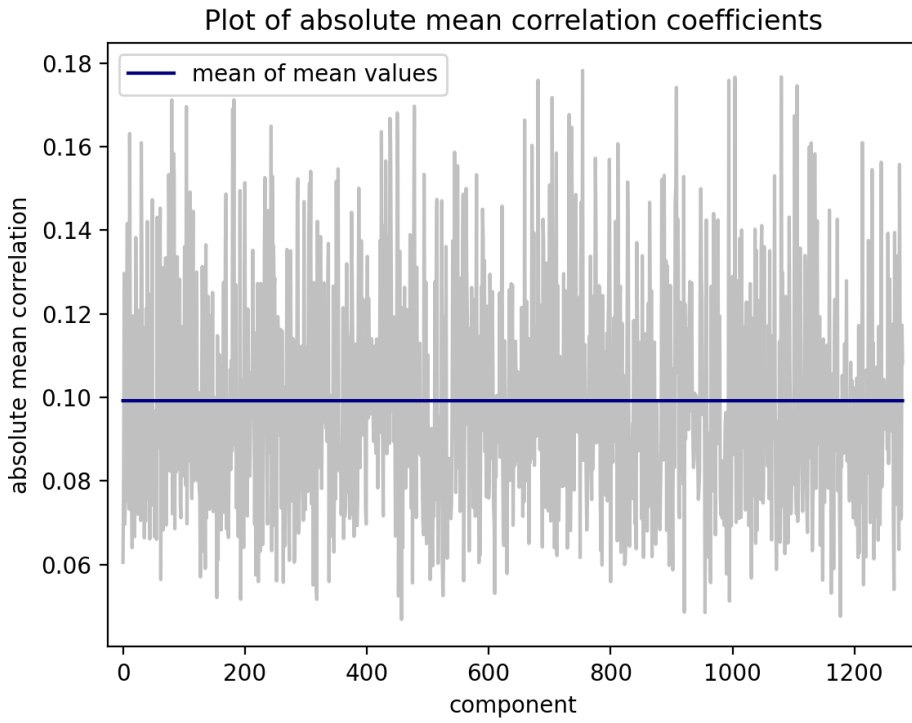
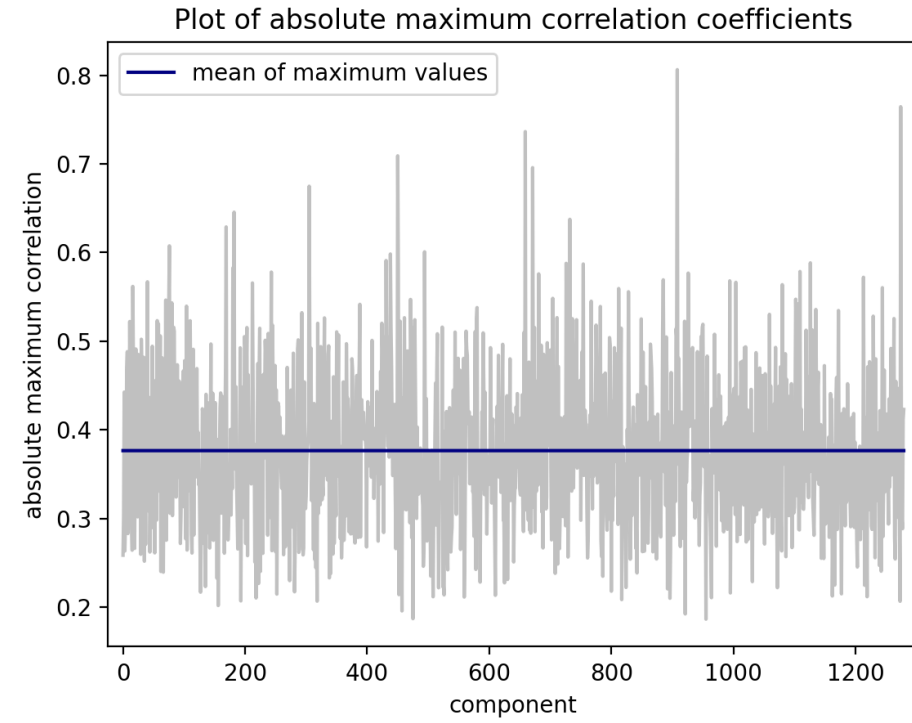


Figure 7: Plots of ESM-1b components' maximum and mean absolute correlation coefficients with ProtTrans components

Additionally, it was attempted to analyse correlation coefficients between embeddings' principal components that explain 95 percent of data variation.

The analogous scatter plot of the number of absolute correlation coefficients higher than 0.5 was drawn for principal components. The analysis implied that there are only few high correlation coefficients between components' pairs overall.

The curve of absolute maximum correlation coefficients shows that there is a trend of correlation coefficients to decrease as the index of ESM-1b component is increasing (Figure 8). The following plot of mean correlation coefficients (Figure 8) supports the statement that high maximum values are not dominating because the mean of absolute mean correlation coefficients is very small (close to zero) between the pairs.

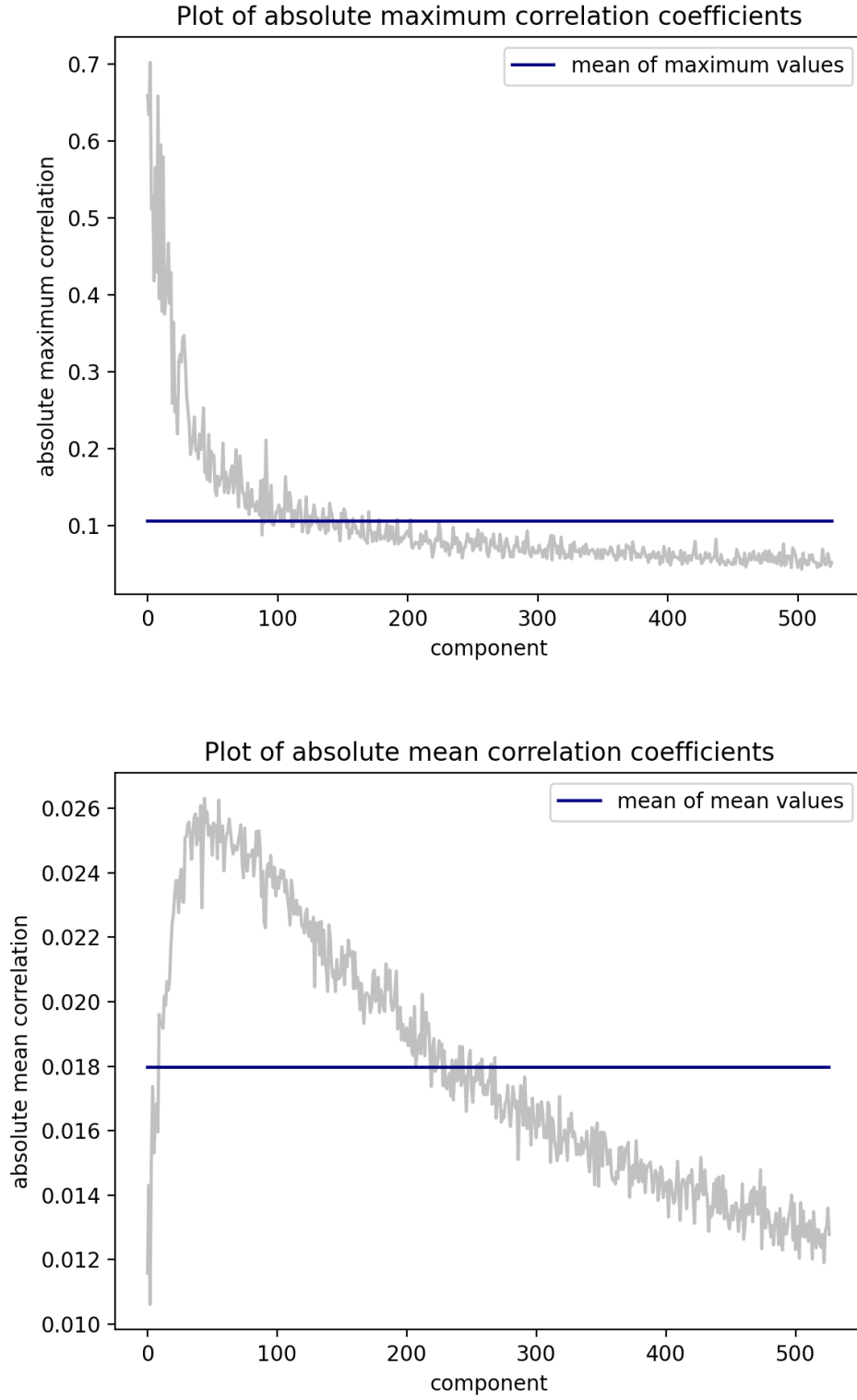


Figure 8: Plot of ESM-1b principal components' (95%) mean and maximum correlation coefficients with ProtTrans principal components (95%)



### 3.2 Representation analysis

The first step of the analysis was to try ProtTrans embeddings as input for the SLP model and compare its results with the testing metrics of model trained with ESM-1b. For the comparison, the primary model with ESM-1b was trained again using the filtered data set. The comparison disclosed that the model, which uses ProtTrans embeddings as input, performs better (Table 8).

Out of the scope of this representation and model architecture analysis for binary classification, there were several attempts made to overtrain the classification model to predict three thermostability classes (one more class was added after dividing the zero-labelled class at the temperature threshold of 40 degrees Celsius). The purpose of overtraining was to check whether the selected architecture has a potential to be trained for the multiclass classification problem. The usage of principal components of protein embeddings showed that overfitting can be done successfully.

Therefore, it was decided to check whether a vector of principal components could be a suitable input for the binary classification task. The testing stage metrics showed worse model’s performance than using the original representations (Table 7).

Table 7: The comparison of scores between models trained with ESM-1b and ProtTrans mean representations and their principal components that account for 95% and 100% of the unfiltered data set variance

	Mean ESM-1b	Mean ProtTrans	ESM-1b (95%)	ProtTrans (95%)	ESM-1b (100%)	ProtTrans (100%)
MCC	0.843	0.902	0.699	0.767	0.698	0.766
Accuracy	0.922	0.951	0.845	0.880	0.845	0.879
Loss	0.208	0.128	0.383	0.442	0.382	0.443
Precision	0.919	0.949	0.910	0.940	0.909	0.939
Recall	0.921	0.951	0.768	0.813	0.767	0.812
ROC AUC	0.979	0.990	0.901	0.945	0.901	0.943

Before joining the embeddings, the normalisation of ESM-1b and ProtTrans vectors was done. Normalised representations were taken as input to the model with the same SLP architecture. For both types of embeddings the results were improved (Table 8).

After joining ESM-1b and ProtTrans mean embeddings, an SLP was trained using these joined representations. The results of this model were similar to the scores of the model that was trained using only ProtTrans embeddings, though the results did not improve (Table 8).

Table 8: The comparison of testing stage scores between models trained with mean, normalised mean, joined mean, and normalised joined ESM-1b and ProtTrans representations

	ESM-1b	Normalised ESM-1b	ProtTrans	Normalised ProtTrans	Joined	Normalised joined
MCC	0.843	0.858	0.901	0.915	0.899	0.920
Accuracy	0.921	0.929	0.951	0.957	0.949	0.960
Loss	0.208	0.248	0.128	0.143	0.131	0.139
Precision	0.921	0.923	0.949	0.951	0.945	0.954
Recall	0.917	0.931	0.949	0.962	0.951	0.964
ROC AUC	0.979	0.982	0.990	0.991	0.991	0.992

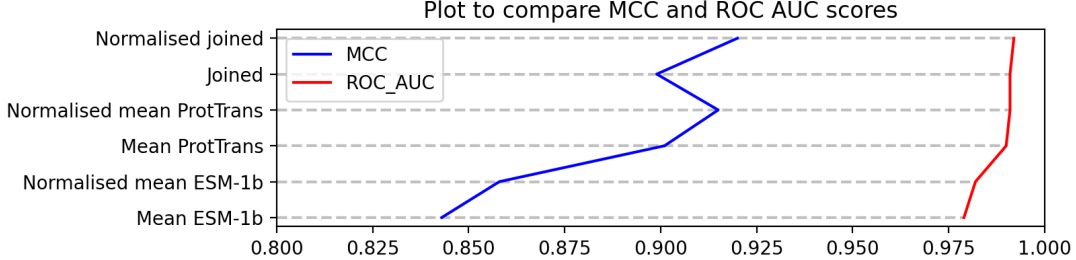


Figure 9: Comparison of SLP models', which were trained with mean and normalised mean ESM-1b, ProtTrans, and joined representations, MCC and ROC AUC scores

However, joining the normalised ESM-1b and ProtTrans mean representations showed the best results. Since joined representations require generation of ESM-1b embeddings, this type of representation does not solve the length limitation problem that was noticed in the previous work. Nevertheless, slightly improved results can be observed when normalised representations are used, the process of normalisation depends on the data set, which is not convenient in the process of development until the final data set is established. Therefore, the optimal choice for this stage of development was mean ProtTrans embeddings.

Nonetheless, ProtTrans already demonstrated the impact for the model's improvement

on the performance, it was decided to finish up the different representation and architecture analysis using embeddings of both protein language models for completeness. The results of the consequent analysis did not change the conclusion regarding ProtTrans influence for the results using any variation of analysed representations (listed in the section 2.6) - in all cases the model that took ProtTrans embeddings as input performed significantly better (Figure 10).

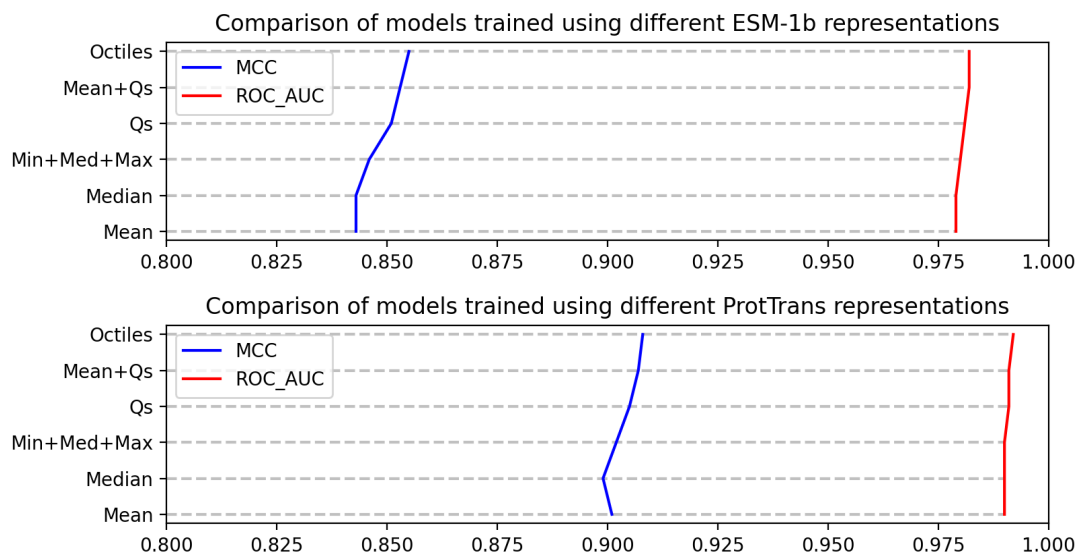


Figure 10: Comparison of SLP models', which were trained with different ESM-1b and ProtTrans representations, MCC and ROC AUC scores

### 3.3 Architecture analysis

The final stage of work was to analyse, which architecture of the model gives the best prediction results.

The results of SLP models were compared with the new models trained with mean embeddings of ESM-1b and ProtTrans (Figure 11). Models with hidden layers achieved better results than the single-layer models: the best model that used ProtTrans embeddings reached MCC of 0.916, meanwhile the SLP using ProtTrans embeddings reached MCC of 0.901.

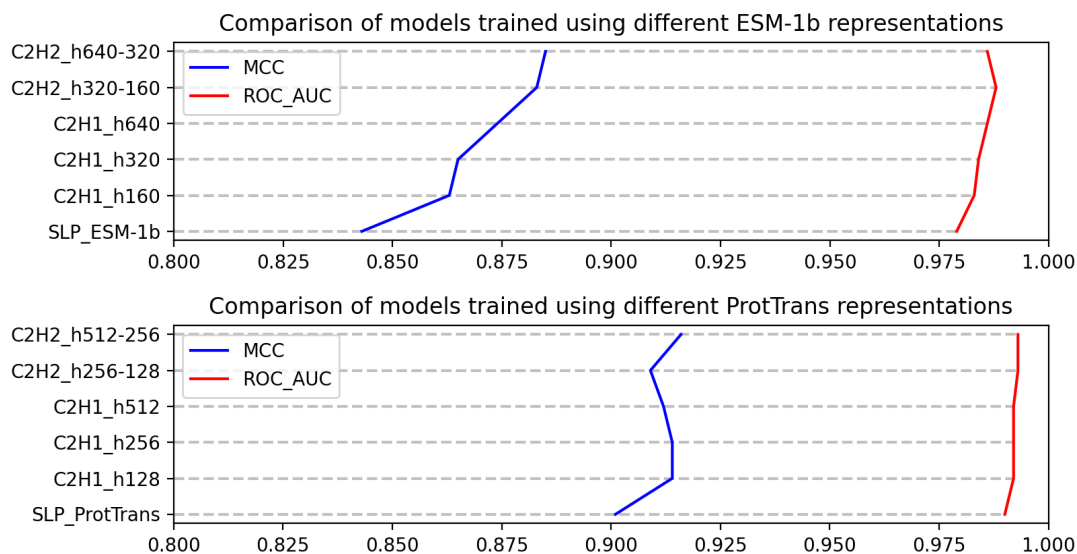


Figure 11: Comparison of different architecture models', which were trained using ESM-1b or ProtTrans embeddings, MCC and ROC AUC scores

## 4 Conclusions

The results of this work provided following conclusions: for further development of the final method ProtTrans mean and octiles embeddings will be used. Although models that used mean ProtTrans embeddings did not provide as good results as the octiles representations in this work, due to more efficient training procedure with mean embeddings, both these representations will be used for the further development of the tool.

Additionally, this work showed that it is worth to use the model's architecture with two hidden layers with sizes 512 and 256.

Table 9: The comparison of testing stage scores between SLP models trained with mean, normalised mean, and octiles ProtTrans representations and model's with 2 hidden layers trained with mean ProtTrans representations

	Mean (SLP)	Normalised mean (SLP)	Octiles (SLP)	Mean (MLP h512-256)
MCC	0.901	0.915	0.910	0.919
Accuracy	0.951	0.957	0.955	0.960
Loss	0.128	0.143	0.125	0.192
Precision	0.949	0.951	0.959	0.954
Recall	0.949	0.962	0.947	0.963
ROC AUC	0.990	0.991	0.992	0.993

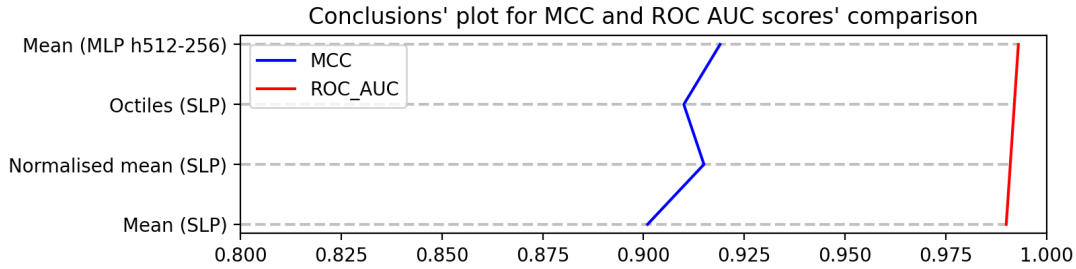


Figure 12: Comparison of different models', which were trained using ProtTrans embeddings, MCC and ROC AUC scores

The next steps of the development will be to generate the mentioned representations for the bigger data set, which will be used to train the binary classification model with the architecture of two hidden layers.

## 5 Availability

The code that was used to receive the results of this work can be found in the designated Github repository: [https://github.com/ievapudz/Course\\_Work\\_Project](https://github.com/ievapudz/Course_Work_Project).

## 6 Abstract in Lithuanian (Santrauka)

Šis darbas yra ankstesnio darbo - binarinę baltymų klasifikaciją pagal termostabilumą vykdančio modelio vystymo - tęsinys. Vystomas modelis buvo vieno sluoksnio perceptronas, kurio įvestis ESM-1b [1] baltymų kalbos modelio generuojamos skaitinės reprezentacijos, o išvestis - prognozė kiekvienam baltymui, kaip tikėtina, kad jis priklauso termostabilių baltymų klasei.

Termostabilumo klasės buvo atskirtos 65 Celsijaus laipsnių riba: baltymai, kurie yra stabilūs žemesnėje nei nurodyta riba temperatūroje, priskiriami klasei su žyme '0', o stabilūs baltymai 65 laipsnių ir aukštesnėje temperatūroje yra laikomi klasės '1' nariais.

Minėtas klasifikatorius buvo apmokytas naudojant duomenų rinkinį, kuriame saugomos organizmų augimo temperatūros [2]. Į duomenų rinkinį taip pat buvo įtraukti organizmų proteomų identifikatoriai, kurie buvo panaudoti surinkti proteomui priklausančius baltymus ir juos sužymėti pagal organizmo augimo temperatūrą.

Nepaisant to, kad klasifikatorius pateikė neblogus rezultatus, testuojant metodą išryškėjo svarbus trūkumas: kadangi ESM-1b skaitinių reprezentacijų kūrimas buvo apribotas baltymo ilgiu, nebuvo galima sugeneruoti reprezentacijų baltymams, kurie buvo ilgesni nei 1022 aminorūgštys. Dėl šios priežasties buvo nutarta išmėginti ProtTrans [3] skaitines reprezentacijas kaip klasifikatoriaus įvestį, nes šis baltymų kalbos modelis buvo apmokytas be apribojimo baltymo ilgiui.

Taip pat domino išmėginti ne tik suvidurkintas skaitines reprezentacijas, bet ir išnaudoti galimybę išgauti kitaip apibendrintas kiekvienos aminorūgšties reprezentacijas bei patikrinti, ar kitokie įvesties vektoriai suteikia geresnius rezultatus.

Apart reprezentacijų analizės, taip pat buvo atlikti eksperimentai patikrinimui, ar kitokios modelių architektūros turės ženklios įtakos modelio veikimui.

Šios analizės rezultatai parodė, kad geriausia naudoti ProtTrans vidurkių bei oktilių skaitines reprezentacijas, kol bus nustatytas galutinis duomenų rinkinys modelio apmokymui. Taip pat, remiantis gautais rezultatais, galima teigti, kad geriausia modelio architektūra baltymų klasifikavimo pagal termostabilumą problemos sprendimui yra neuroninio tinklo modelis su dviem paslėptais sluoksniais.

Gautos analizių išvados suteiks naudingų įžvalgų galutinio metodo baltymų klasifikacijai pagal termostabilumą apibrėžimui.



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