

Graph Neural Networks for Social Recommendation

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Introduction

Graph Neural Networks (GNNs) can naturally integrate node information and topological structure, have been demonstrated to be powerful in learning on [graph data](#).

Their main idea is how to iteratively aggregate feature information from local graph neighborhoods using neural networks. Meanwhile, node information can be propagated through a graph after transformation and aggregation.

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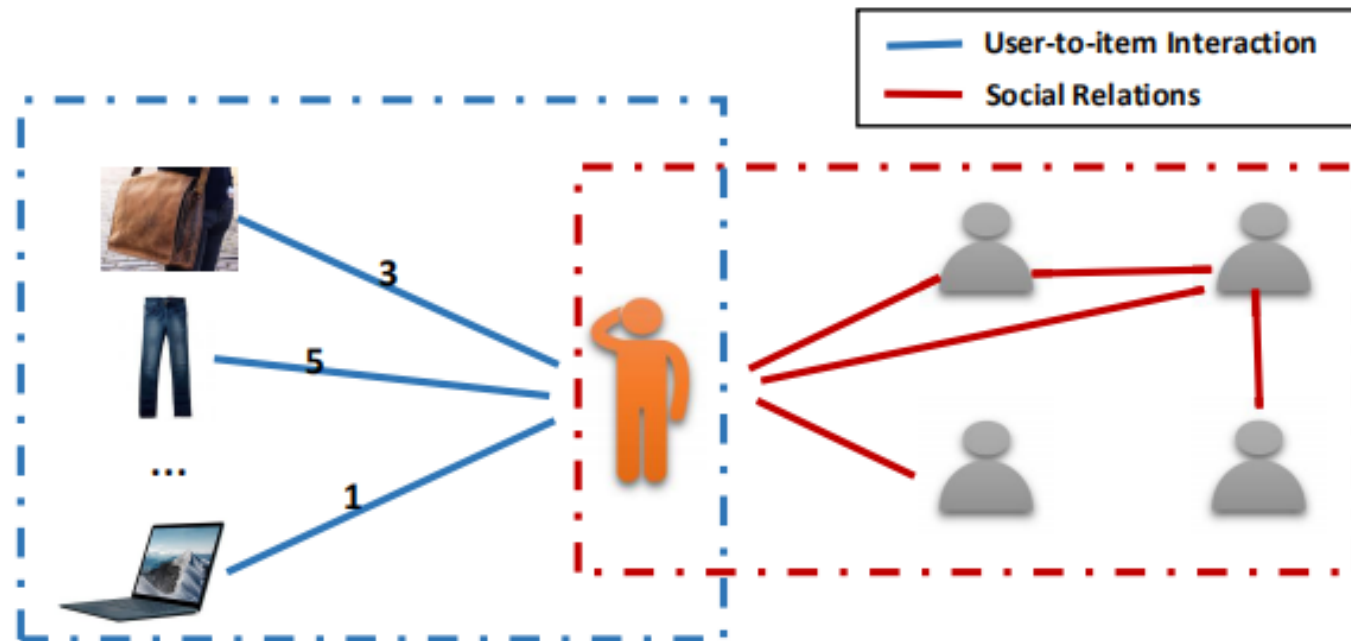


Figure 1: Graph Data in Social Recommendation. It contains two graphs including the user-item graph (left part) and the user-user social graph (right part). Note that the number on the edges of the user-item graph denotes the opinions (or rating score) of users on the items via the interactions.

The Challenge of GNNs Applied on Social Recommendation

- How to **inherently combine these two graphs**;
- How to **capture interactions and opinions between users and items jointly**;
- How to **distinguish social relations with heterogeneous strengths**(Users are likely to share more similar tastes with strong ties than weak ties)

We propose a novel graph neural network **GraphRec** for social recommendations, which can address three aforementioned challenges simultaneously

Contribution

- Propose a novel graph neural network GraphRec;
- Provide a principled approach to **jointly capture interactions and opinions in the user-item graph**;
- We introduce a method to **consider heterogeneous strengths of social relations mathematically**;
- We demonstrate the effectiveness of the proposed framework on various real-world datasets

The Proposed Framework

● Definitions and Notations

Table 1: Notation

Symbols	Definitions and Descriptions
r_{ij}	The rating value of item v_j by user u_i
\mathbf{q}_j	The embedding of item v_j
\mathbf{p}_i	The embedding of user u_i
\mathbf{e}_r	The opinion embedding for the rating level r , such as 5-star rating, $r \in \{1, 2, 3, 4, 5\}$
d	The length of embedding vector
$C(i)$	The set of items which user u_i interacted with
$N(i)$	The set of social friends who user u_i directly connected with
$B(j)$	The set of users who have interacted the item v_j
\mathbf{h}_i^I	The item-space user latent factor from item set $C(i)$ of user u_i
\mathbf{h}_i^S	The social-space user latent factor from the social friends $N(i)$ of user u_i

\mathbf{h}_i	The user latent factor of user u_i , combining from item space \mathbf{h}_i^I and social space \mathbf{h}_i^S
\mathbf{x}_{ia}	The opinion-aware interaction representation of item v_a for user u_i
\mathbf{f}_{jt}	The opinion-aware interaction representation of user u_t for item v_j
\mathbf{z}_j	The item latent factor of item v_j
α_{ia}	The item attention of item v_a in contributing to \mathbf{h}_i^I
β_{io}	The social attention of neighboring user u_o in contributing to \mathbf{h}_i^S
μ_{jt}	The user attention of user u_t in contributing to \mathbf{z}_j
r'_{ij}	The predicted rating value of item v_j by user u_i
\oplus	The concatenation operator of two vectors
\mathbf{T}	The user-user social graph
\mathbf{R}	The user-item rating matrix (user-item graph)
\mathbf{W}, \mathbf{b}	The weight and bias in neural network

and $\mathcal{T} = \{\langle u_i, v_j \rangle \mid r_{ij} = 0\}$ be the set of unknown ratings. Let $N(i)$ be the set of users whom u_i directly connected with, $C(i)$ be the set of items which u_i have interacted with, and $B(j)$ be the set of users who have interacted with v_j . In addition, users can establish social relations to each other. We use $T \in \mathbb{R}^{n \times n}$ to denote the user-user social graph, where $T_{ij} = 1$ if u_j has a relation to u_i and zero otherwise. Given the user-item graph R and social graph T , we aim to predict the missing rating value in R .

● Overview of the Proposed Framework

The model consists of three components: **user modeling**, **item modeling**, and **rating prediction**.

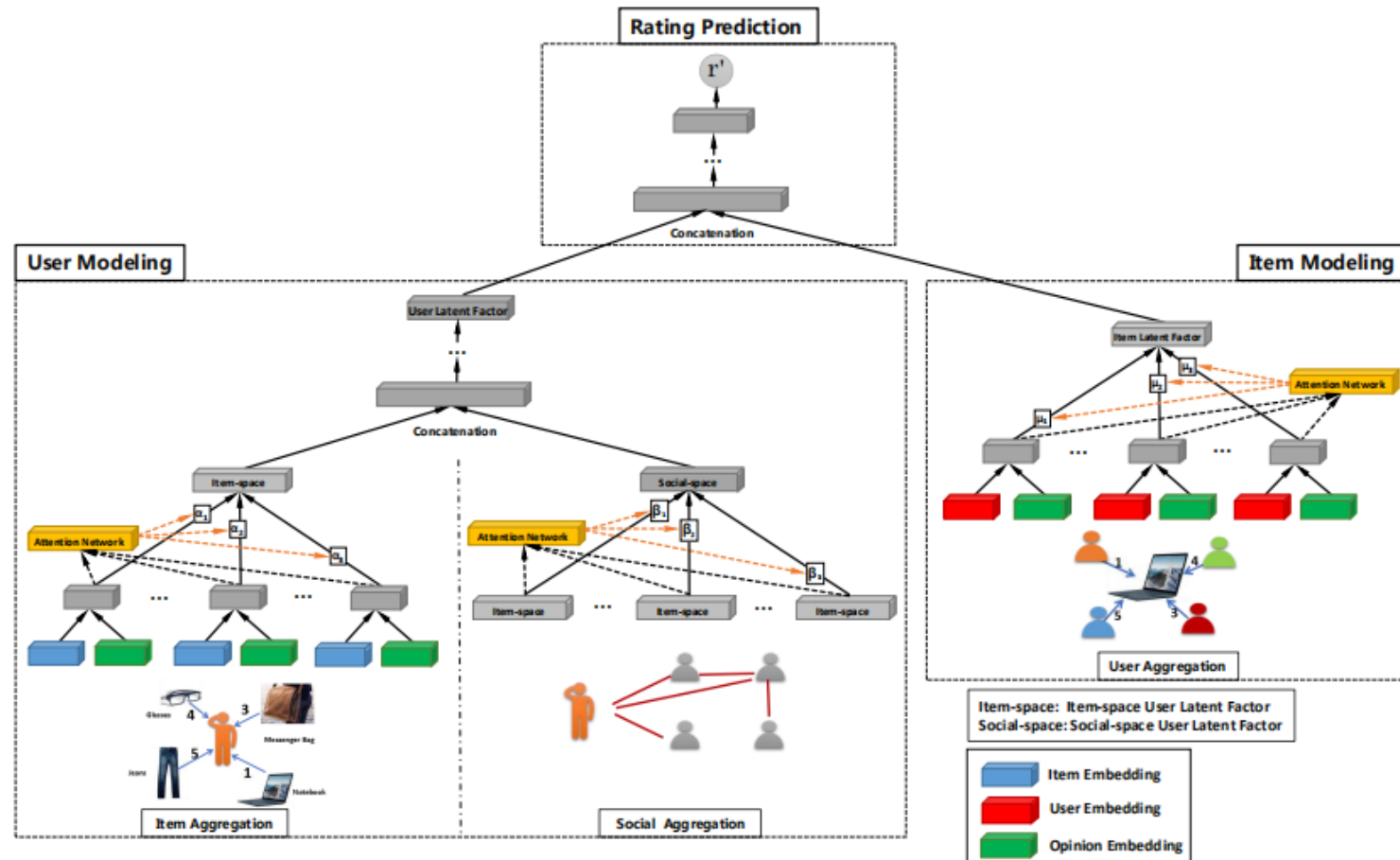
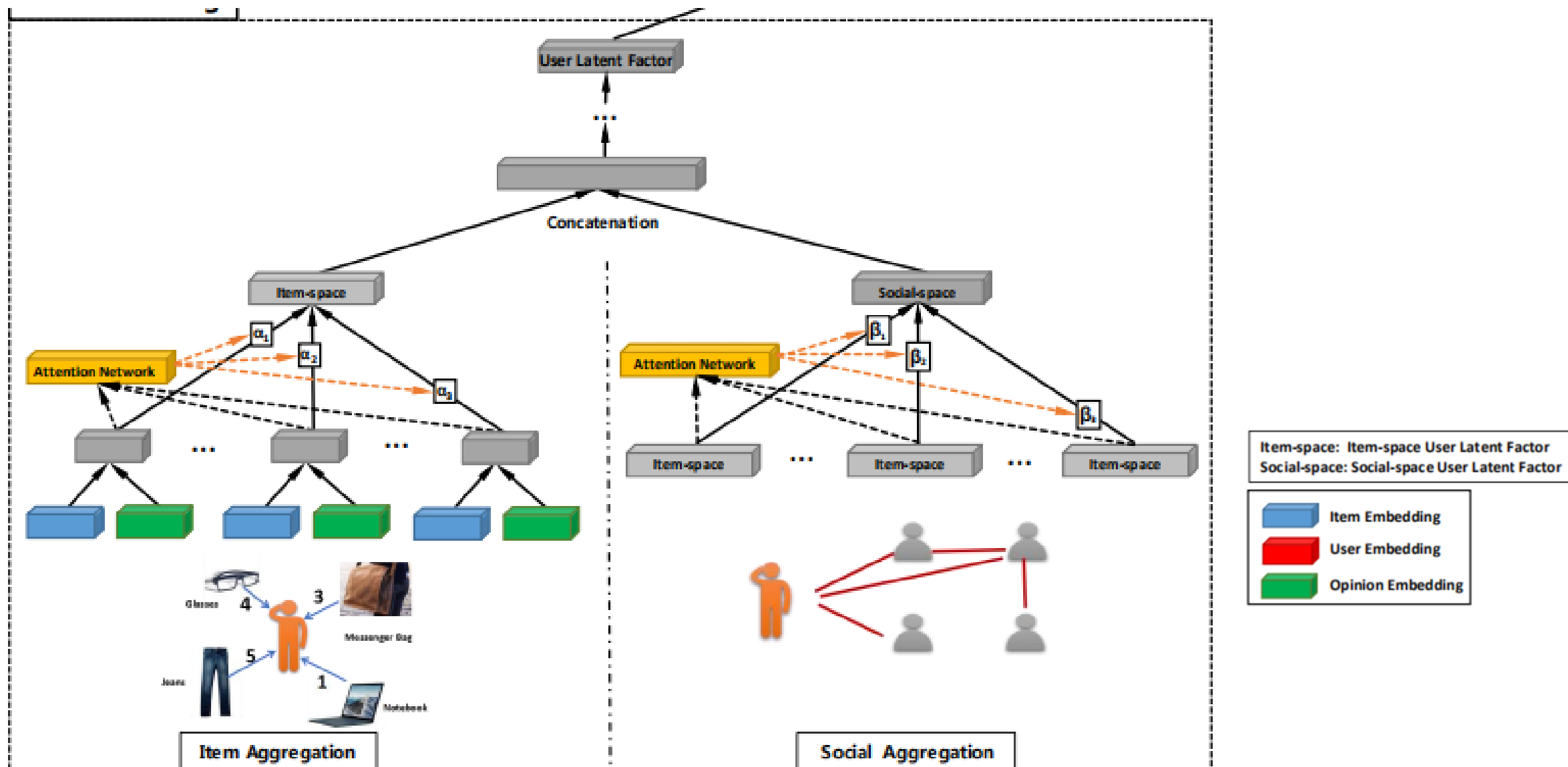


Figure 2: The overall architecture of the proposed model. It contains three major components: user modeling, item modeling, and rating prediction.

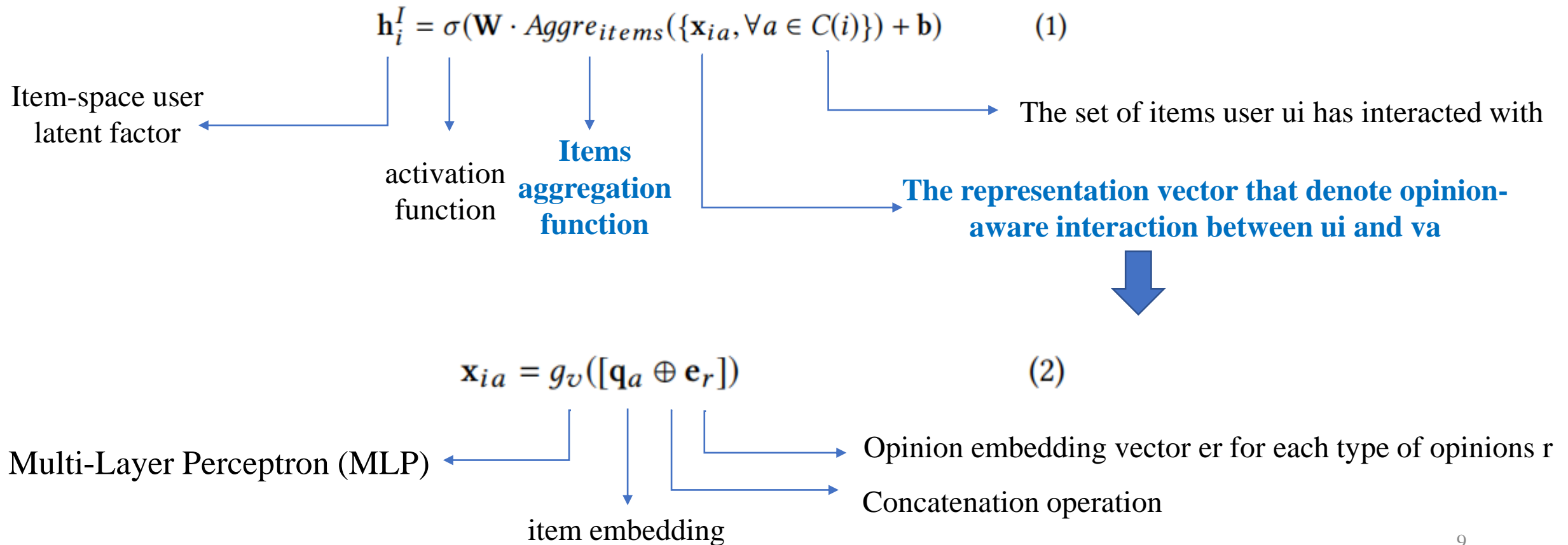
● user modeling



How to inherently combine the user-item graph and social graph.

Two types of aggregation to learn factors from two graphs

□ **item aggregation** jointly capture **interactions** and **opinions** in the user-item graph



One popular aggregation function for *Aggreitems* is **the mean operator**

$$\mathbf{h}_i^I = \sigma(\mathbf{W} \cdot \left\{ \sum_{a \in C(i)} \alpha_i \mathbf{x}_{ia} \right\} + \mathbf{b})$$

→ $\frac{1}{|C(i)|}$ for all items in the mean-based aggregator.

$$\mathbf{h}_i^I = \sigma(\mathbf{W} \cdot \left\{ \sum_{a \in C(i)} \alpha_{ia} \mathbf{x}_{ia} \right\} + \mathbf{b})$$

→ *Attention mechanisms*

where α_{ia} denotes the attention weight of the interaction with v_a in contributing to user u_i 's item-space latent factor

$$\alpha_{ia}^* = \mathbf{w}_2^T \cdot \sigma(\mathbf{W}_1 \cdot [\mathbf{x}_{ia} \oplus \mathbf{p}_i] + \mathbf{b}_1) + b_2$$

$$\alpha_{ia} = \frac{\exp(\alpha_{ia}^*)}{\sum_{a \in C(i)} \exp(\alpha_{ia}^*)}$$

□ **social aggregation** an **attention mechanism** to select social friends

aggregate the **item-space user latent factors** of neighboring users from the **social graph**

$$\mathbf{h}_i^S = \sigma(\mathbf{W} \cdot \text{Aggre}_{\text{neighbors}}(\{\mathbf{h}_o^I, \forall o \in N(i)\}) + \mathbf{b})$$

the aggregation function
on user's neighbors.

$$\mathbf{h}_i^S = \sigma(\mathbf{W} \cdot \left\{ \sum_{o \in N(i)} \beta_i \mathbf{h}_o^I \right\} + \mathbf{b})$$

where β_i is fixed to $\frac{1}{|N(i)|}$ for all neighbors for the mean-based aggregator. It assumes that all neighbors contribute equally to the representation of user u_i .

take the element-wise mean of the vectors

$$\mathbf{h}_i^S = \sigma(\mathbf{W} \cdot \left\{ \sum_{o \in N(i)} \beta_{io} \mathbf{h}_o^I \right\} + \mathbf{b})$$

$$\beta_{io}^* = \mathbf{w}_2^T \cdot \sigma(\mathbf{W}_1 \cdot [\mathbf{h}_o^I \oplus \mathbf{p}_i] + \mathbf{b}_1) + b_2$$

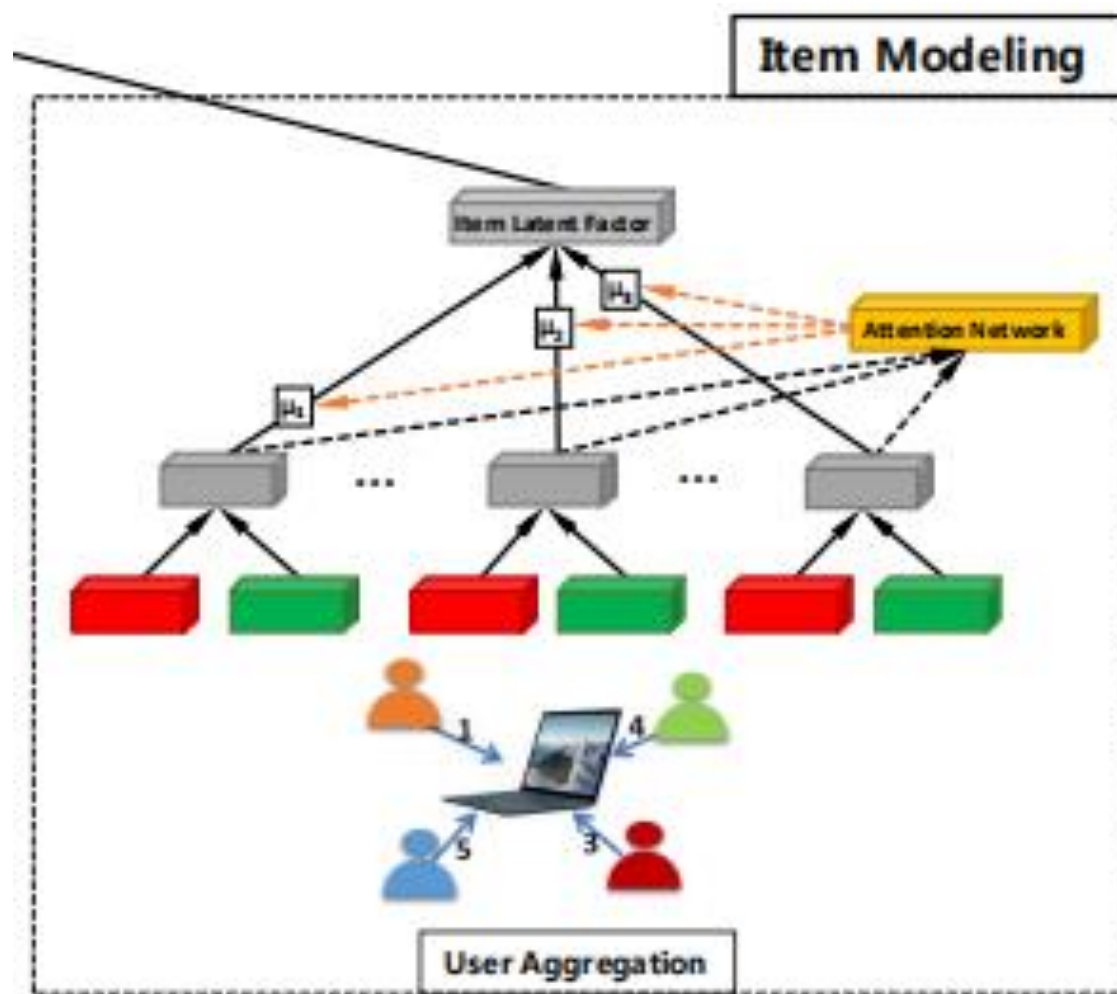
$$\beta_{io} = \frac{\exp(\beta_{io}^*)}{\sum_{o \in N(i)} \exp(\beta_{io}^*)}$$

□ Learning User Latent Factor

We propose to combine these two latent factors to the final user latent factor

$$\begin{aligned}\mathbf{c}_1 &= [\mathbf{h}_i^I \oplus \mathbf{h}_i^S] \\ \mathbf{c}_2 &= \sigma(\mathbf{W}_2 \cdot \mathbf{c}_1 + \mathbf{b}_2) \\ &\dots \\ \mathbf{h}_i &= \sigma(\mathbf{W}_l \cdot \mathbf{c}_{l-1} + \mathbf{b}_l)\end{aligned}$$

- item modeling

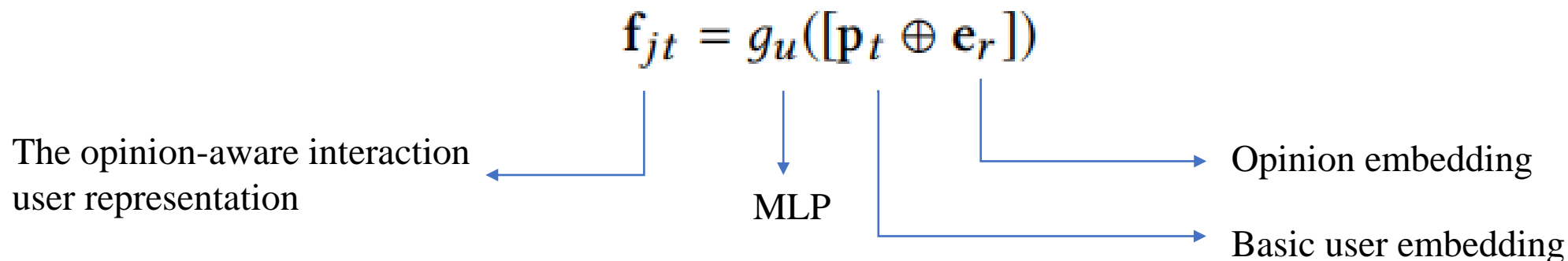


Item-space: Item-space User Latent Factor
Social-space: Social-space User Latent Factor

Item Embedding
User Embedding
Opinion Embedding

□ User Aggregation

For each item v_j , we need to aggregate information from the set of users who have interacted with v_j , **denoted as $B(j)$. Different users can capture the characteristics of the same item in different ways provided by users.**



$$\mathbf{z}_j = \sigma(\mathbf{W} \cdot \text{Aggre}_{users}(\{\mathbf{f}_{jt}, \forall t \in B(j)\}) + \mathbf{b})$$

$$\mathbf{z}_j = \sigma(\mathbf{W} \cdot \left\{ \sum_{t \in B(j)} \mu_{jt} \mathbf{f}_{jt} \right\} + \mathbf{b}) \quad (17)$$

$$\mu_{jt}^* = \mathbf{w}_2^T \cdot \sigma(\mathbf{W}_1 \cdot [\mathbf{f}_{jt} \oplus \mathbf{q}_j] + \mathbf{b}_1) + b_2 \quad (18)$$

$$\mu_{jt} = \frac{\exp(\mu_{jt}^*)}{\sum_{t \in B(j)} \exp(\mu_{jt}^*)} \quad (19)$$

capture heterogeneous influence from user-item interactions

● rating modeling

With the latent factors of users and items (i.e., \mathbf{h}_i and \mathbf{z}_j), we can first concatenate them $[\mathbf{h}_i \oplus \mathbf{z}_j]$ and then feed it into MLP for rating prediction as:

$$\mathbf{g}_1 = [\mathbf{h}_i \oplus \mathbf{z}_j] \quad (20)$$

$$\mathbf{g}_2 = \sigma(\mathbf{W}_2 \cdot \mathbf{g}_1 + \mathbf{b}_2) \quad (21)$$

...

$$\mathbf{g}_{l-1} = \sigma(\mathbf{W}_l \cdot \mathbf{g}_{l-1} + \mathbf{b}_l) \quad (22)$$

$$r'_{ij} = \mathbf{w}^T \cdot \mathbf{g}_{l-1} \quad (23)$$

where l is the index of a hidden layer, and r'_{ij} is the predicted rating from u_i to v_j .

● Model Training

$$Loss = \frac{1}{2|O|} \sum_{i,j \in O} (r'_{ij} - r_{ij})^2$$

the number of observed ratings Truth rating
Predicted rating

RMSPprop as the optimizer in our implementation 微分平方加权平均数

At each time, it randomly selects a training instance and updates each model parameter towards the direction of its negative gradient. There are three embedding in our model, including item embedding q_j , user embedding p_i , and opinion embedding e_r .

the **dropout strategy** has been applied to our model. The idea of dropout is to randomly drop some neurons during the training process.

EXPERIMENT

● Experimental Settings

□ *Datasets*

Table 2: Statistics of the datasets

Dataset	Ciao	Epinions
# of Users	7,317	18,088
# of Items	10,4975	261,649
# of Ratings	283,319	764,352
# of Density (Ratings)	0.0368%	0.0161%
# of Social Connections	111,781	355,813
# of Density (Social Relations)	0.2087%	0.1087%

□ *Evaluation Metrics*

Mean Absolute Error (MAE)

Root Mean Square Error (RMSE)

□ *Baselines*

three groups of methods including **traditional recommender systems**, **traditional social recommender systems**, and **deep neural network based recommender systems**.

- **PMF** [24]: **Probabilistic Matrix Factorization** utilizes user-item rating matrix only and models latent factors of users and items by Gaussian distributions.
- **SoRec** [17]: **Social Recommendation** performs co-factorization on the user-item rating matrix and user-user social relations matrix.
- **SoReg** [18]: **Social Regularization** models social network information as regularization terms to constrain the matrix factorization framework.
- **SocialMF** [13]: It considers the trust information and propagation of trust information into the matrix factorization model for recommender systems.
- **TrustMF** [37]: This method adopts matrix factorization technique that maps users into two low-dimensional spaces: truster space and trustee space, by factorizing trust networks according to the directional property of trust.
- **NeuMF** [11]: This method is a state-of-the-art matrix factorization model with neural network architecture. The original implementation is for recommendation ranking task and we adjust its loss to the squared loss for rating prediction.
- **DeepSoR** [8]: This model employs a deep neural network to learn representations of each user from social relations, and to integrate into probabilistic matrix factorization for rating prediction.
- **GCMC+SN** [1]: This model is a state-of-the-art recommender system with graph neural network architecture. In order to incorporate social network information into GCMC, we utilize the *node2vec* [9] to generate user embedding as user side information, instead of using the raw feature social connections ($T \in \mathbb{R}^{n \times n}$) directly. The reason is that the raw feature input vectors is highly sparse and high-dimensional. Using the network embedding techniques can help compress the raw input feature vector to a low-dimensional and dense vector, then the model can be easy to train.

□ *Parameter Settings*

For all neural network methods, we randomly initialized model parameters with a Gaussian distribution, where the mean and standard deviation is 0 and 0.1,

● Performance Comparison of Recommender Systems

Table 3: Performance comparison of different recommender systems

Training	Metrics	Algorithms								
		PMF	SoRec	SoReg	SocialMF	TrustMF	NeuMF	DeepSoR	GCMC+SN	GraphRec
Ciao (60%)	MAE	0.952	0.8489	0.8987	0.8353	0.7681	0.8251	0.7813	0.7697	0.7540
	RMSE	1.1967	1.0738	1.0947	1.0592	1.0543	1.0824	1.0437	1.0221	1.0093
Ciao (80%)	MAE	0.9021	0.8410	0.8611	0.8270	0.7690	0.8062	0.7739	0.7526	0.7387
	RMSE	1.1238	1.0652	1.0848	1.0501	1.0479	1.0617	1.0316	0.9931	0.9794
Epinions (60%)	MAE	1.0211	0.9086	0.9412	0.8965	0.8550	0.9097	0.8520	0.8602	0.8441
	RMSE	1.2739	1.1563	1.1936	1.1410	1.1505	1.1645	1.1135	1.1004	1.0878
Epinions (80%)	MAE	0.9952	0.8961	0.9119	0.8837	0.8410	0.9072	0.8383	0.8590	0.8168
	RMSE	1.2128	1.1437	1.1703	1.1328	1.1395	1.1476	1.0972	1.0711	1.0631

- (1) social network information is helpful for recommendations;
- (2) neural network models can boost recommendation performance
- (3) the proposed framework outperforms representative baselines.

● Model Analysis

□ *Effect of Social Network and User Opinions.*

The proposed framework provides model components to (1) integrate social network information and (2) incorporate users' opinions about the interactions with items.

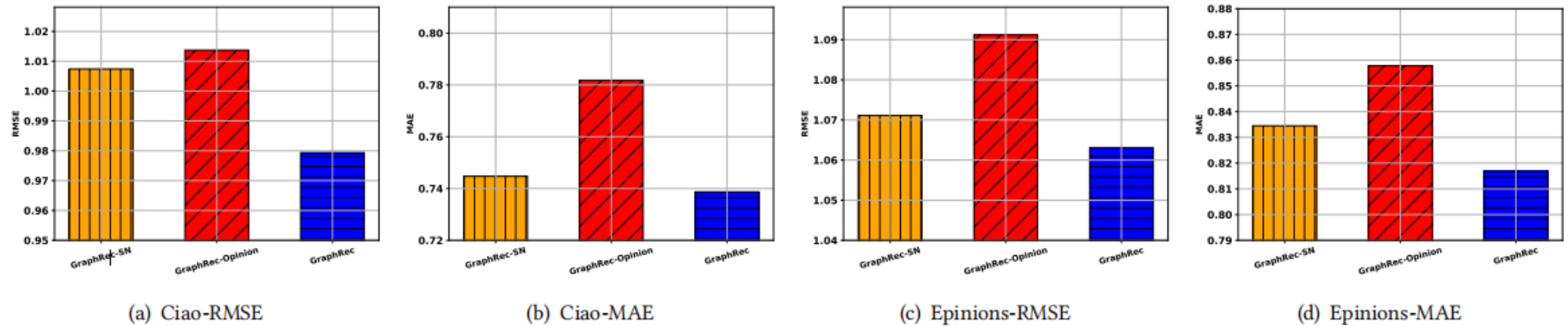


Figure 3: Effect of social network and user opinions on Ciao and Epinions datasets.

□ *Effect of Attention Mechanisms.*

We further evaluate the key components of GraphRec-*Attention mechanisms*, including **item attention α** , **social attention β** , and **user attention μ** .

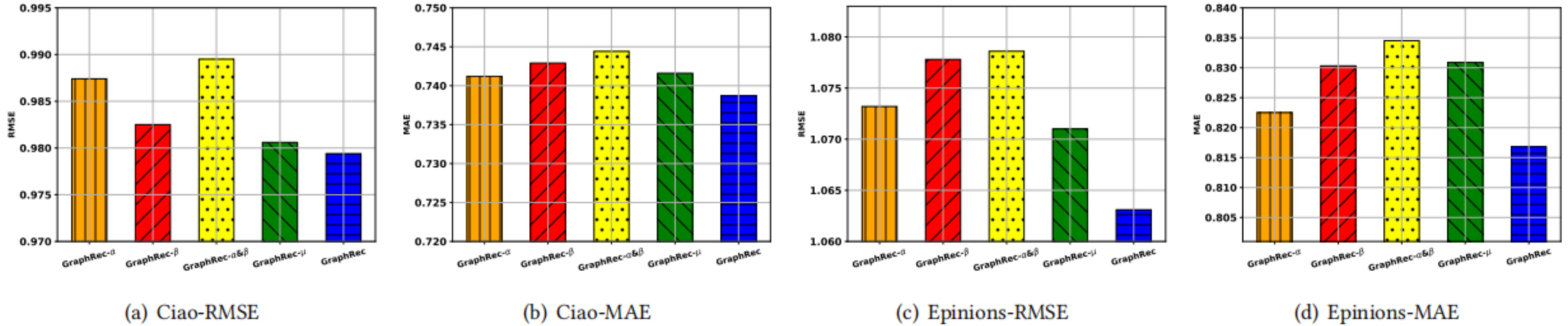


Figure 4: Effect of attention mechanisms on Ciao and Epinions datasets.

GraphRec can capture the heterogeneity in aggregation operations of the proposed framework via attention mechanisms, which can boost the recommendation performance

□ *Effect of Embedding Size.*

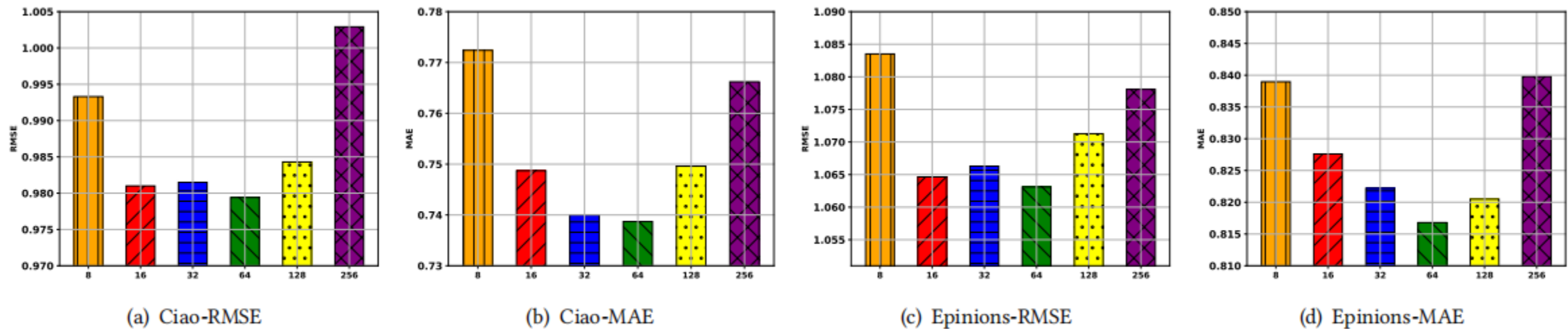


Figure 5: Effect of embedding size on Ciao and Epinions datasets.

to analyze the effect of embedding size of **user embedding p** , **item embedding q** , and **opinion embedding e** , on the performance of our model.

CONCLUSION AND FUTURE WORK

- Our experiments reveal that the opinion information plays a crucial role in the improvement of our model performance.
- our GraphRec can differentiate the ties strengths by considering heterogeneous strengths of social relations.
- Exploring graph neural networks for recommendation with attributes would be an interesting future direction.
- we will consider building dynamic graph neural networks for social recommendations with dynamic

New Idea

- GNN和GCN的应用
- 模型中各个部分的重要性的分析
- Attention机制的使用

谢 谢