
Assignment 4 Part 1

```
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%In this part of the assignment, we are repeating the work completed
in
%pa9 and reporting on it.

%In part a) the C, G matrices and the F vector was created to describe
the
%circuit network

%In part b), the input voltage was DC swept from -10V to 10V and Vo and
V3 was
%plotted. Then for the AC case, Vo was plotted as a function of w, and
the
%gain, Vo/V1 was plotted in dB. Then, for the AC case, the gain was
plotted
%as a function of random perturbations on C using a normal
distribution
%with stf = 0.5 at w = pi. The gain was then plotted using histograms

% Definition of variables based on the components present in the
circuit
R1 = 1;
G1 = 1/R1;
C = 0.25;
R2 = 2;
G2 = 1/R2;
L = 0.2;
R3 = 10;
G3 = 1/R3;
alpha = 100;
R4 = 0.1;
G4 = 1/R4;
RO = 1000;
GO = 1/RO;

% Definition of Matrices
C_matrix = [0 0 0 0 0 0 0;
            -C C 0 0 0 0 0;
             0 0 -L 0 0 0 0;
             0 0 0 0 0 0 0;
             0 0 0 0 0 0 0;
             0 0 0 0 0 0 0;
             0 0 0 0 0 0 0];

G_Matrix = [1 0 0 0 0 0 0;
            -G2 G1+G2 -1 0 0 0 0;
             0 1 0 -1 0 0 0;
             0 0 -1 G3 0 0 0;
             0 0 0 0 -alpha 1 0;
```

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        0 0 0 G3 -1 0 0;
        0 0 0 0 0 -G4 G4+G0];

% Defining DC and AC voltage matrices, as well as the F matrix

V_DC = zeros(7,1);
V_AC = zeros(7,1);
F_Matrix = zeros(7,1);

% DC Sweep Plot
for vol = -10:0.1: 10

    F_Matrix(1,1) = vol;
    V_DC = G_Matrix\F_Matrix; % DC sweep
    calculation

    figure(1)
    plot(vol, V_DC(7,1), 'g.')
    hold on

    plot(vol, V_DC(4,1), 'r.')
    hold on
    title('DC sweep of Vo (green) and V3 (red)')
    xlabel('Vin')
    ylabel('V')

end

% AC Sweep and Gain Plot
w = logspace(1,2,500);
F_Matrix(1) = 1;

for i = 1:length(w)

    V_AC = (G_Matrix+C_matrix*1j*w(i))\F_Matrix; % calculating the
    voltage matrix using AC sweep
    figure(2)
    semilogx(w(i), abs(V_AC(7,1)), 'b.')
    hold on
    title('AC sweep of Vo')

    dB = 20*log(abs(V_AC(7,1))/F_Matrix(1)); % Calculating the gain
    figure(3)
    plot(i, dB, 'r.')
    hold on
    title('Gain Vo/Vin in dB')
end

% AC case: voltage gain calculation as a function of random
perturbations
% on C using a normal distribution with std = .05 and w = pi
pert = 0.25 + 0.05.*randn(1,1000);
w = pi;
Gain = zeros(1000,1);

```

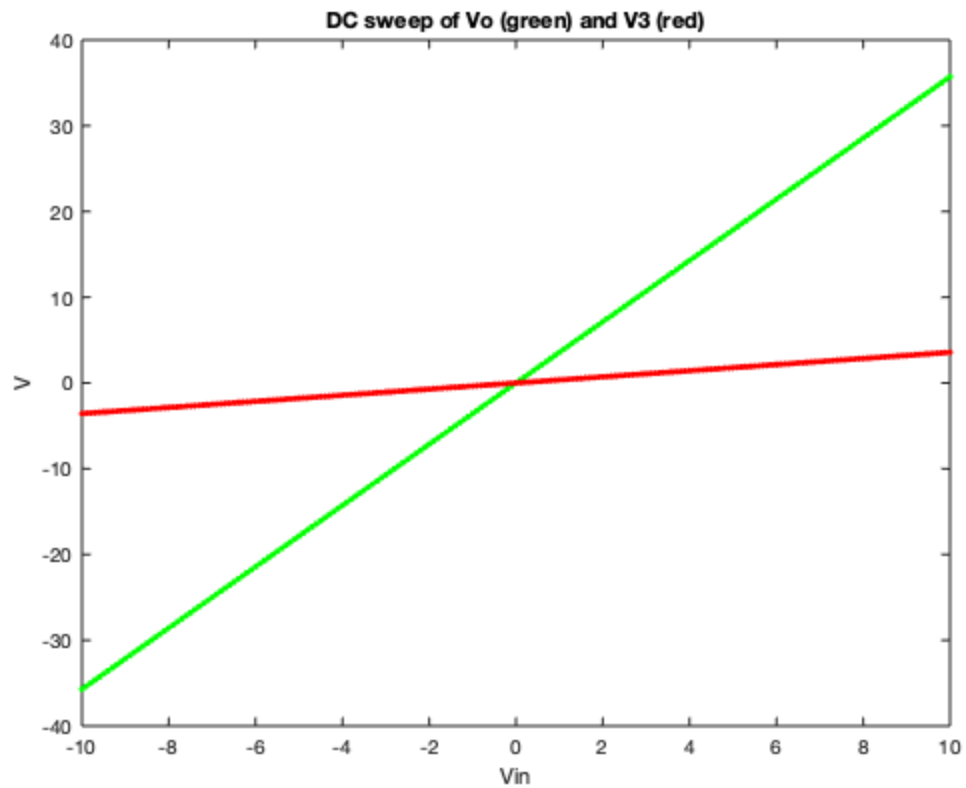
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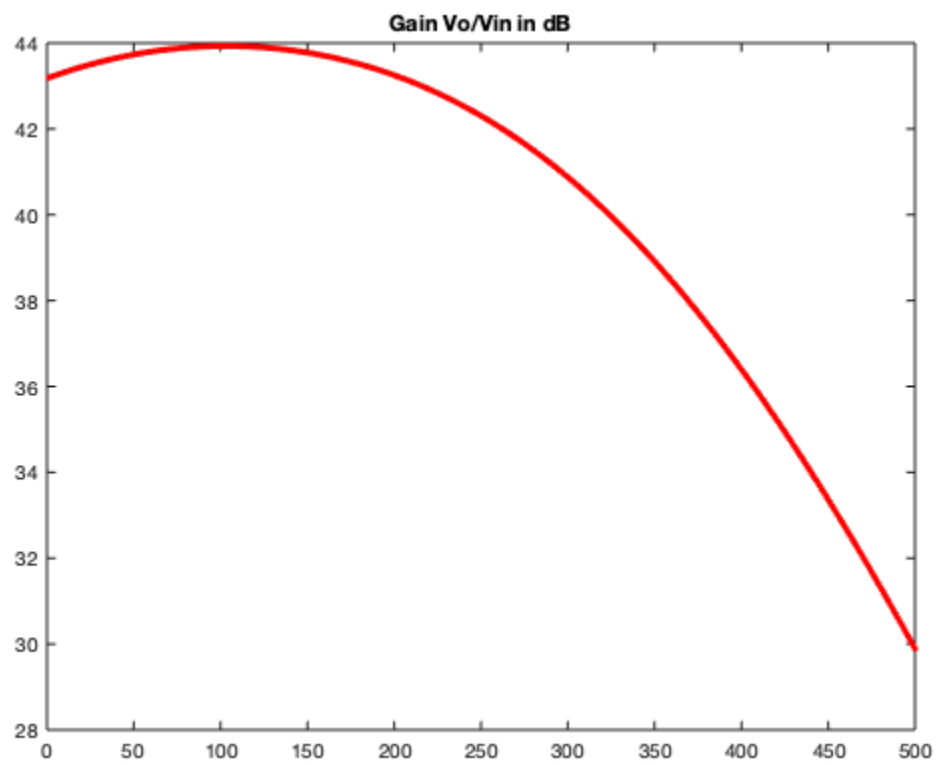
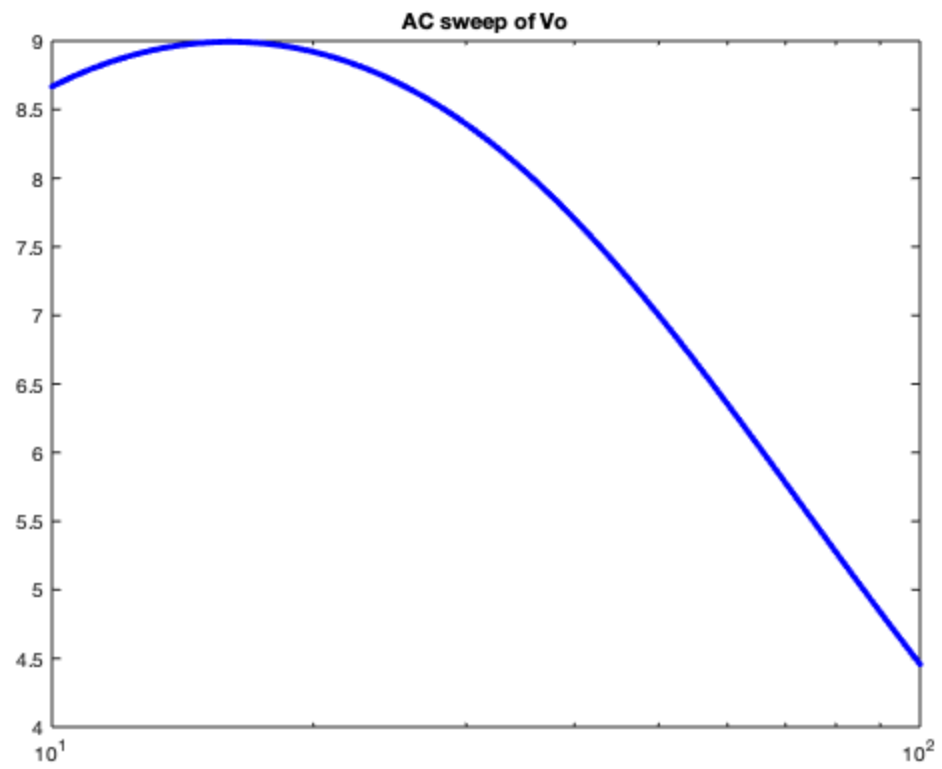
for n = 1:length(Gain)

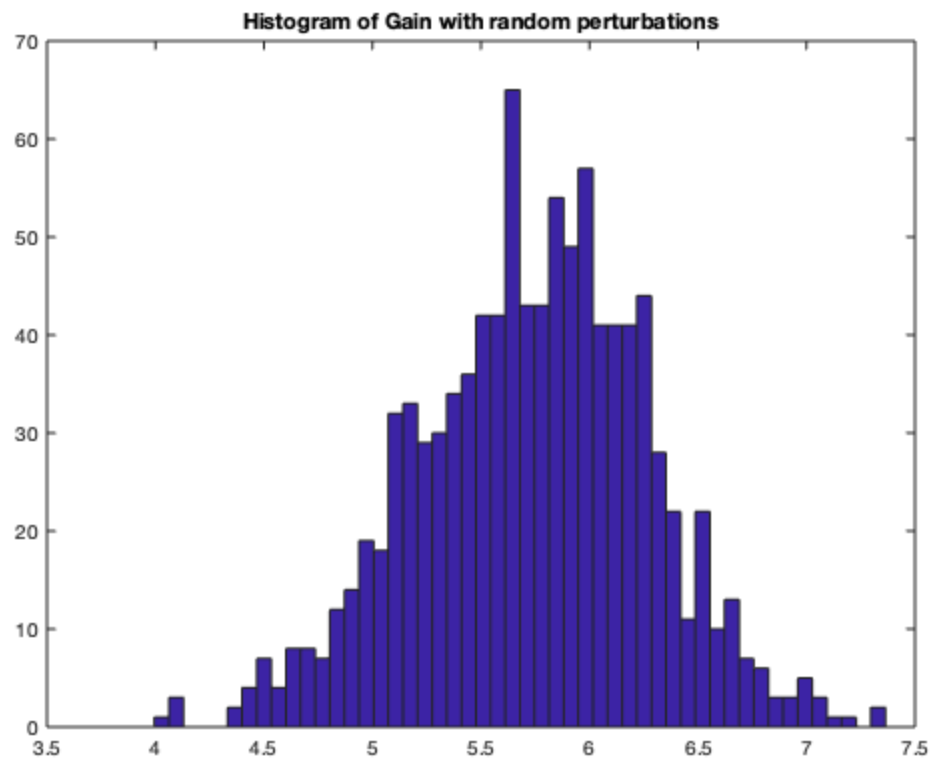
    C = pert(n);
    C_matrix(2,1) = -C;
    C_matrix(2,2) = C;
    V_AC = (G_Matrix+C_matrix*1j*w)\F_Matrix;    % Voltage calculation
    using AC sweep
    Gain(n,1) = abs(V_AC(7,1))/F_Matrix(1);    % Gain calculation
    using AC voltage
end

% Gain histogram
figure(4)
hist(Gain,50);
title('Histogram of Gain with random perturbations')

```







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Assignment 4 Part 2

```
% In this part of the assignment, the transient response of the
circuit was
% simulated

% Part a) Upon inspection of the circuit, this is a RLC circuit, due
to the
% presence of capacitors, resistors and and inductors. DC transient
response
% in RLC circuits can be observed when a sudden voltage or current is
% applied to it, which is what we will be doing in part 2

%Part b) In simple terms, RLC circuits experience "resonance" at a
certain
%frequency. This frequency point is where the reactive inductance of the
the
%inductor equals the value of the capacitance reactance of the
capacitor
%( $x_L = x_C$ ). At this frequency the gain of the circuit sharply rises,
and is
%low at other frequencies. For this reason, this circuit has a very
sharp
%bandpass response, and can be used as a filter or an amplifier
functioning
%at a certain frequency.

% Definition of variables based on the components present in the
circuit
R1 = 1;
G1 = 1/R1;
C = 0.25;
R2 = 2;
G2 = 1/R2;
L = 0.2;
R3 = 10;
G3 = 1/R3;
alpha = 100;
R4 = 0.1;
G4 = 1/R4;
RO = 1000;
GO = 1/RO;
Vin = 1;

% Define Matrices
C_Matrix = [0 0 0 0 0 0 0;
            -C C 0 0 0 0 0;
            0 0 -L 0 0 0 0;
            0 0 0 0 0 0 0;
            0 0 0 0 0 0 0;
            0 0 0 0 0 0 0;
            0 0 0 0 0 0 0];
```

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G_Matrix = [1 0 0 0 0 0 0;
            -G2 G1+G2 -1 0 0 0 0;
            0 1 0 -1 0 0 0;
            0 0 -1 G3 0 0 0;
            0 0 0 0 -alpha 1 0;
            0 0 0 G3 -1 0 0;
            0 0 0 0 0 -G4 G4+G0];

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F_Matrix = [Vin;
            0;
            0;
            0;
            0;
            0;
            0];

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F0_Matrix = [Vin-Vin;
            0;
            0;
            0;
            0;
            0;
            0];

```

```

%d) we will be simulating the circuit for 1 second using 1000 steps
step = 1000;

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vol_1 = zeros(7, step);
vol_start = zeros(7, 1);
dt = 10^-3;
    %setting up the plot for the first input signal, a step that
    %transitions
    %from 0 to 1 at 30 milliseconds
for i = 1:step

    if i < 30
        vol_1(:,i) = (C_Matrix./dt+G_Matrix)\(F0_Matrix
+C_Matrix*vol_start/dt);

    elseif i == 30
        vol_1(:,i) = (C_Matrix./dt+G_Matrix)\(F_Matrix
+C_Matrix*vol_start/dt);

    else
        vol_1(:,i) = (C_Matrix./dt+G_Matrix)\(F_Matrix
+C_Matrix*vol_old/dt);

    end

    vol_old = vol_1(:, i);

end

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```

figure(1)
plot(1:step, vol_1(7,:), 'g')
hold on
plot(1:step, vol_1(1,:), 'm')
title('Vin and Vo with a step that transitions 0-1 at 0.03s')
xlabel('Time in milliseconds')
ylabel('Voltage in volts')
grid on

vol_2 = zeros(7, step);
function_F = zeros(7,1);

%setting up the plot for the second input signal, a sin(2*pi*f*t)
    signal,
%at a frequency of 1/(30) 1/ms.

for i_2 = 1:step

    function_vol = sin(2*pi*(1/0.03)*i_2/step);
    function_F(1,1) = function_vol;
    if i_2 == 1
        vol_2(:,i_2) = (C_Matrix./dt+G_Matrix)\(function_F
+C_Matrix*vol_start/dt);
    else
        vol_2(:,i_2) = (C_Matrix./dt+G_Matrix)\(function_F
+C_Matrix*vol_old/dt);
    end
    vol_old = vol_2(:, i_2);

end

figure(2)
plot(1:step, vol_2(7,:), 'b')
hold on
plot(1:step, vol_2(1,:), 'g')
title('Vin and Vo with input signal function sin(2pift),f = 1/30 1/
ms')
xlabel('Time in milliseconds')
ylabel('Voltage in volts')
grid on

%setting up the plot using a gaussian pulse with mag=1, std dev = 30ms
    and
%delay of 60 ms

vol_3 = zeros(7, step);
Gaussian_F = zeros(7,1);

for i_3 = 1:step

    Gaussian_vol = exp(-1/2*((i_3/step-0.06)/(0.03))^2);

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    Gaussian_F(1,1) = Guassian_vol;

    if i_3 == 1
        vol_3(:,i_3) = (C_Matrix./dt+G_Matrix)\(Gaussian_F
+C_Matrix*vol_start/dt);

    else
        vol_3(:,i_3) = (C_Matrix./dt+G_Matrix)\(Gaussian_F
+C_Matrix*vol_old/dt);

    end

    vol_old = vol_3(:, i_3);

end

figure(3)
plot(0:step-1, vol_3(7,:), 'r')
hold on
plot(0:step-1, vol_3(1,:), 'b')
title('Vin and Vo with Guassian pulse (mag =1, std dev= 30ms, delay =
    60ms')
xlabel('Time in milliseconds')
ylabel('Voltage in volts')
grid on

% Part d) iv. Now that the simulation is complete, the frequency
    content of
% the input and output signals will be plotted using the built-in
    matlab
% functions fft() and fftshift().

freq = (-step/2:step/2-1);

%Plot of Vin, Vo with first input signal in f-domain

fft_voll_in = fft(vol_1(1, :));
fft_voll_out = fft(vol_1(7, :));
ffts_voll_in = fftshift(fft_voll_in);
ffts_voll_out = fftshift(fft_voll_out);

figure(4)
plot(freq, abs(ffts_voll_in), 'r')
hold on
plot(freq, abs(ffts_voll_out), 'b')
title('Vin and Vo in f-domain with a step 0-1 at 30ms')
xlabel('frequency in 1/ms')
ylabel('Voltage in volts')
grid on

%Plot of Vin, Vo with second input signal in f-domain

fft_vol2 = fft(vol_2.);
ffts_vol2 = fftshift(fft_vol2);

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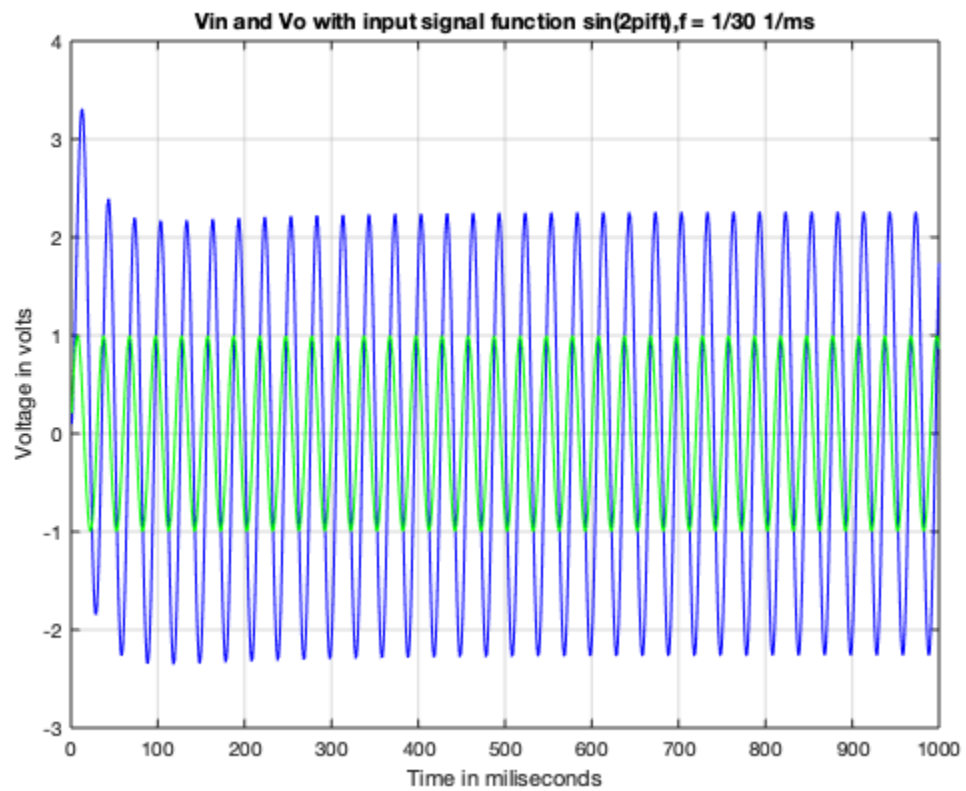
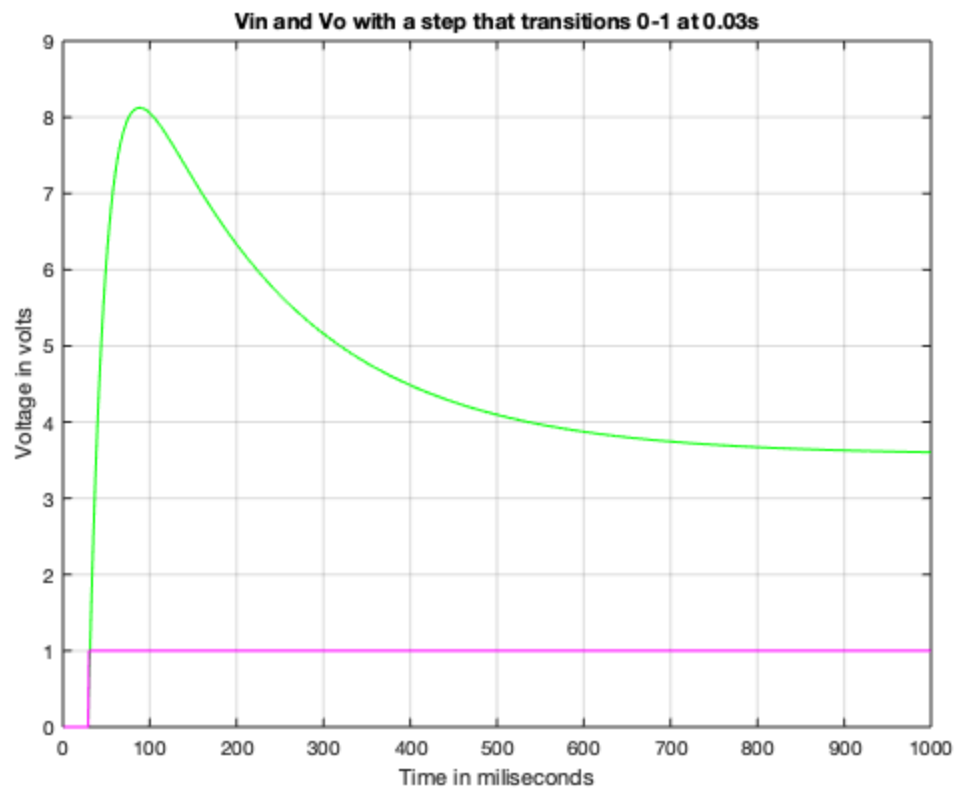
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figure(5)
plot(freq, abs(ffts_vol2(:, 1)), 'r')
hold on
plot(freq, abs(ffts_vol2(:, 7)), 'b')
title('Vin and Vout in f-domain with function sin(2pift), f = 1/30ms')
xlabel('frequency in 1/ms')
ylabel('Voltage in v')
grid on

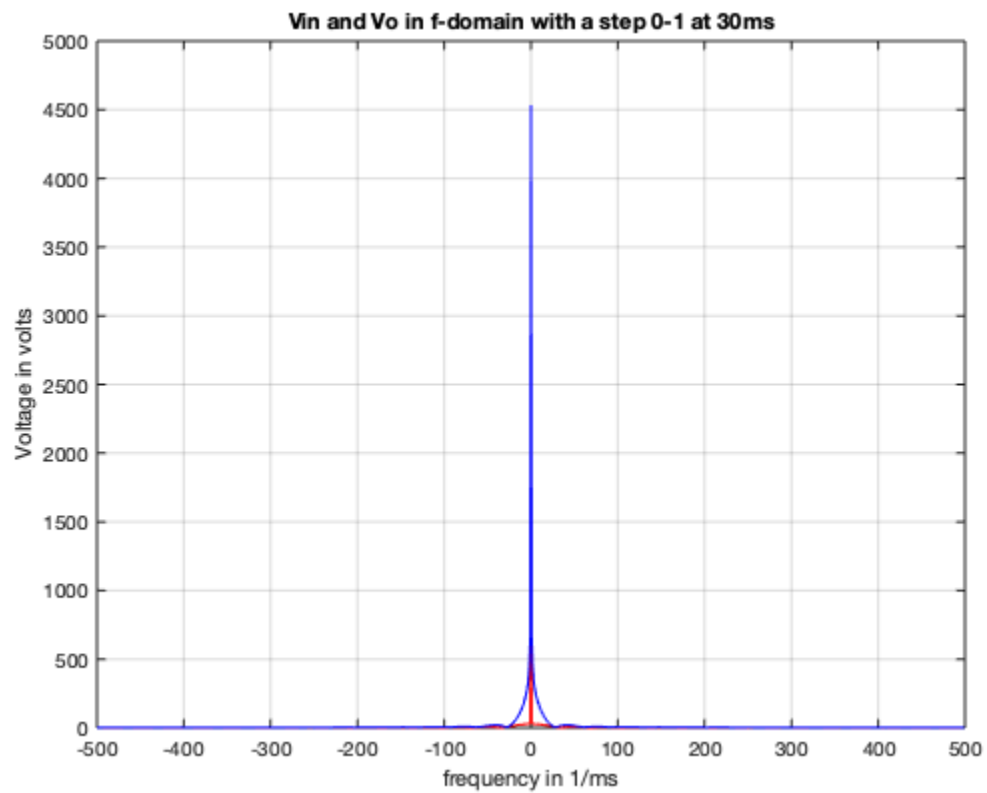
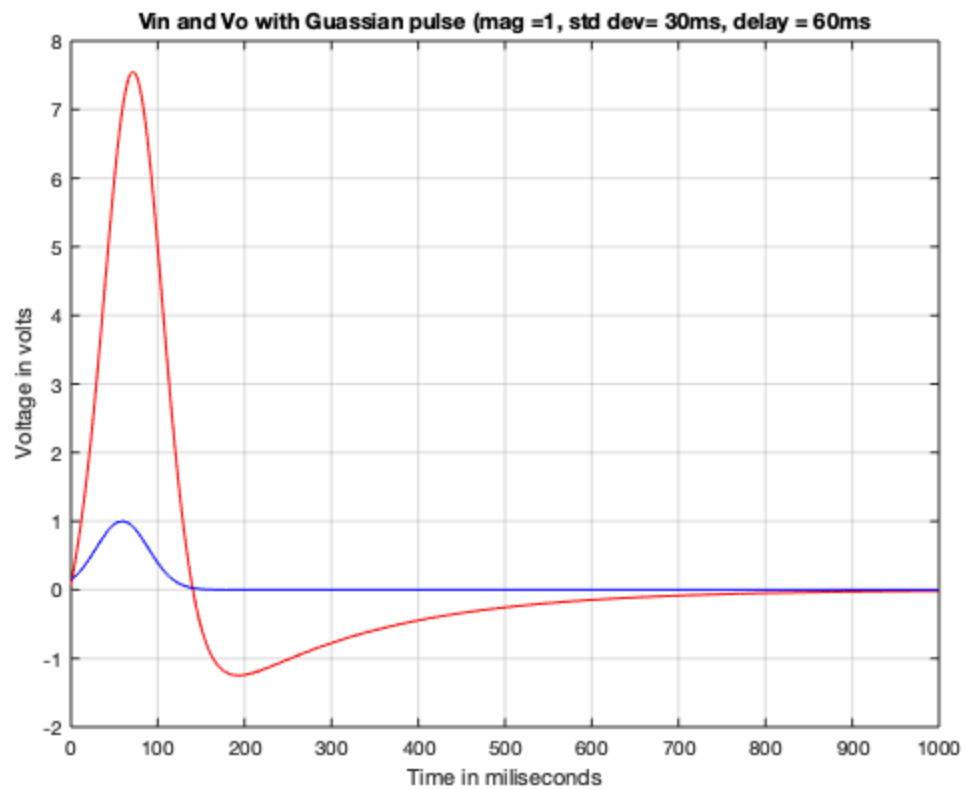
%Plot of Vin, Vo with third input signal in f-domain

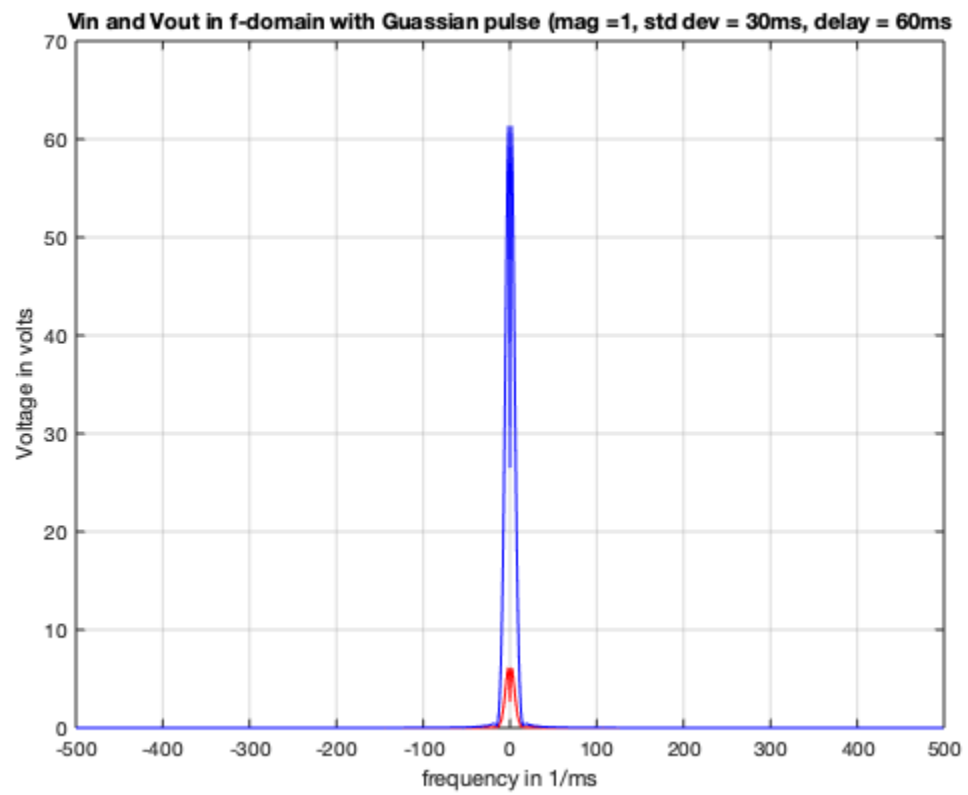
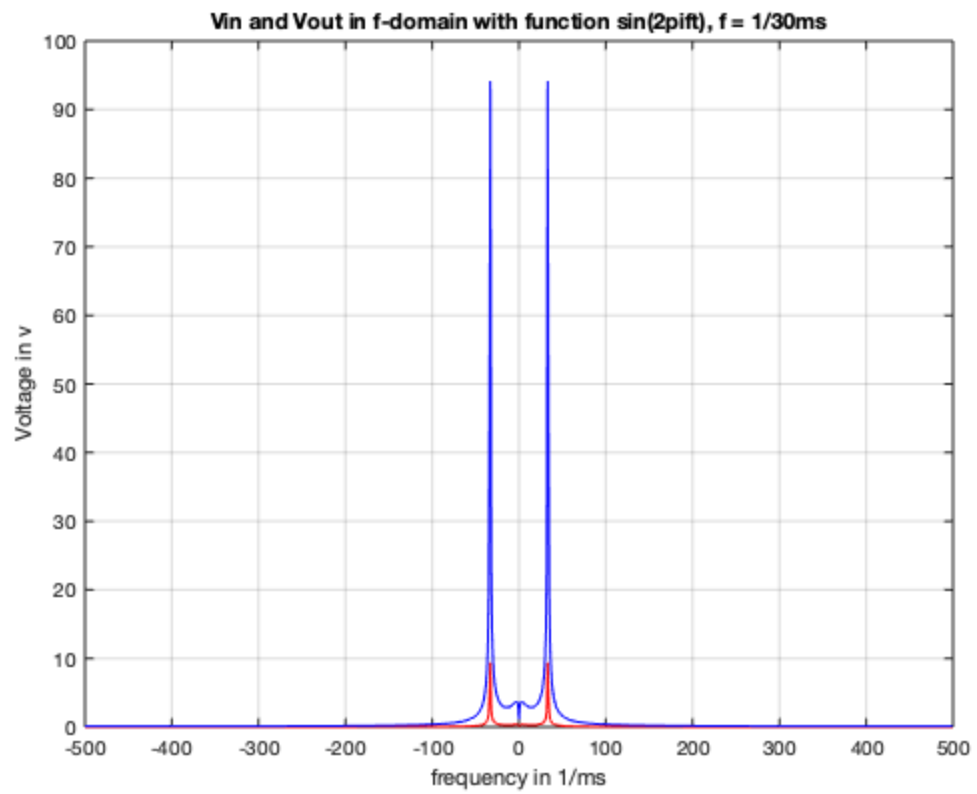
fft_vol3 = fft(vol_3.');
ffts_vol3 = fftshift(fft_vol3);

figure(6)
plot(freq, abs(ffts_vol3(:, 1)), 'r')
hold on
plot(freq, abs(ffts_vol3(:, 7)), 'b')
title('Vin and Vout in f-domain with Guassian pulse (mag =1, std dev =
    30ms, delay = 60ms')
xlabel('frequency in 1/ms')
ylabel('Voltage in volts')
grid on

%%%%%%%%end of part 2%%%%%%%%
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Assignment 4 Part 3

```
% In this part of the assignment, noise was added to the circuit, and
the
% response to this noise was observed

% In part a), a current source In was added to the circuit, in
parallel
% with R3. This causes thermal noise to be generated in resistor R3.

%In part b), a capacitor Cn = 0.00001 added in parallel with resistor
to
%BW limit the noise. This causes changes to C matrix

% Definition of variables based on the components present in the
circuit
R1 = 1;
G1 = 1/R1;
c = 0.25;
R2 = 2;
G2 = 1/R2;
L = 0.2;
R3 = 10;
G3 = 1/R3;
alpha = 100;
R4 = 0.1;
G4 = 1/R4;
RO = 1000;
GO = 1/RO;
Vin = 1;
Cn_1 = 0.00001;           % Capacitance value given in part b)
Cn_2 = 10^-8;             % Cn_2 and Cn_3 are for part d) vi.
    where
Cn_3 = 2.6*2e-5;          % we change Cn to observe the change
    in BW

% part a) Updating the C matrices

C_Matrix1 = [0 0 0 0 0 0 0;
             -c c 0 0 0 0 0;
              0 0 -L 0 0 0 0;
              0 0 0 -Cn_1 0 0 0;
              0 0 0 0 0 0 0;
              0 0 0 -Cn_1 0 0 0;
```

```

        0 0 0 0 0 0 0;];

C_Matrix2 = [0 0 0 0 0 0 0;
             -c c 0 0 0 0 0;
              0 0 -L 0 0 0 0;
              0 0 0 -Cn_2 0 0 0;
              0 0 0 0 0 0 0;
              0 0 0 -Cn_2 0 0 0;
              0 0 0 0 0 0 0;];

C_Matrix3 = [0 0 0 0 0 0 0;
             -c c 0 0 0 0 0;
              0 0 -L 0 0 0 0;
              0 0 0 -Cn_3 0 0 0;
              0 0 0 0 0 0 0;
              0 0 0 -Cn_3 0 0 0;
              0 0 0 0 0 0 0;];

GO = [1 0 0 0 0 0 0;
      -G2 G1+G2 -1 0 0 0 0;
       0 1 0 -1 0 0 0;
       0 0 -1 G3 0 0 0;
       0 0 0 0 -alpha 1 0;
       0 0 0 G3 -1 0 0;
       0 0 0 0 0 -G4 G4+GO];

F_Matrix = [Vin;
            0;
            0;
            0;
            0;
            0;
            0;];

F0_Matrix = [Vin-Vin;
            0;
            0;
            0;
            0;
            0;
            0;];

step_1 = 1000;
step_2 = 1.9898e4;
given
value
% time step 1 was the numer of time steps
% in part 2, step 2 is used
% to observe the effects of varying this
% on the simulation

vol_1 = zeros(7, step_1);
vol_start = zeros(7, 1);

```

```

dt_1 = 10^-3;
dt_2 = 1.9898*10^-4; %varying the timestep to observe the effects on
    the sim

% Circuit with Noise simulation with default time step
% Time domain simulation
%vol_1 = zeros(7, step_1);
Guassian_F = zeros(7,1);

for i = 1:step_1

    Guassian_F(1,1) = exp(-1/2*((i/step_1-0.06)/(0.03))^2);
    Guassian_F(4,1) = 0.001*randn();
    Guassian_F(7,1) = 0.001*randn();

    if i == 1
        vol_1(:,i) = (C_Matrix1./dt_1+GO)\(Guassian_F
+C_Matrix1*vol_start/dt_1);

    else
        vol_1(:,i) = (C_Matrix1./dt_1+GO)\(Guassian_F
+C_Matrix1*vol_old/dt_1);

    end

    vol_old = vol_1(:, i);

end

% Part b)i. modelling Vo signal with noise using the Guassian
    excitation

figure(1)
plot(1:step_1, vol_1(7,:), 'r')
hold on
plot(1:step_1, vol_1(1,:), 'b')
title('Plot of Vout with Noise Source')
xlabel('Time in miliseconds')
ylabel('Voltage in volts')
grid on

freq = (-step_1/2:step_1/2-1);

fft_voll = fft(vol_1. ');
ffts_voll = fftshift(fft_voll);

%Part c) Fourier Transform plot
figure(2)
plot(freq, abs(ffts_voll(:, 1)), 'r')
hold on
plot(freq, abs(ffts_voll(:, 7)), 'b')
title('Fourier-Transform Plot of Vout')
xlabel('frequency in 1/ms')

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ylabel('Voltage in volts')
grid on

vol_2 = zeros(7, step_1);
Guassian_F = zeros(7,1);

for i_2 = 1:step_1

    Guassian_F(1,1) = exp(-1/2*((i_2/step_1-0.06)/(0.03))^2);
    Guassian_F(4,1) = 0.001*randn();
    Guassian_F(7,1) = 0.001*randn();

    if i_2 == 1

        vol_2(:,i_2) = (C_Matrix2./dt_1+GO)\(Guassian_F
+C_Matrix2*vol_start/dt_1);

    else

        vol_2(:,i_2) = (C_Matrix2./dt_1+GO)\(Guassian_F
+C_Matrix2*vol_old/dt_1);

    end

    vol_old = vol_2(:, i_2);

end

% e) in part e), 3 plots of vout will be made, with each plot made
% using
% a different value of Cout. A discussion on my findings is placed
% at the
% end of this document.

% plotting Vout using smaller value of Cout
figure(3)
plot(1:step_1, vol_2(7,:), 'r')
hold on
plot(1:step_1, vol_2(1,:), 'b')
title('Vout plot using smaller value of Cout')
xlabel('Time in milliseconds')
ylabel('Voltage in volts')
grid on

vol_3 = zeros(7, step_1);
Guassian_F = zeros(7,1);

for i_3 = 1:step_1

    Guassian_F(1,1) = exp(-1/2*((i_3/step_1-0.06)/(0.03))^2);
    Guassian_F(4,1) = 0.001*randn();
    Guassian_F(7,1) = 0.001*randn();

```

```

        if i_3 == 1

            vol_3(:,i_3) = (C_Matrix3./dt_1+GO)\(Guassian_F
+C_Matrix3*vol_start/dt_1);

        else

            vol_3(:,i_3) = (C_Matrix3./dt_1+GO)\(Guassian_F
+C_Matrix3*vol_old/dt_1);

        end

        vol_old = vol_3(:, i_3);

    end

figure(4)
plot(1:step_1, vol_3(7,:), 'r')
hold on
plot(1:step_1, vol_3(1,:), 'b')
title('Vout plot using bigger value of Cout')
xlabel('Time in milliseconds')
ylabel('Voltage in volts')
grid on

%Now we will plot Vout using the value of Cout given
for i_4 = 1:step_1

    Gaussian_F(1,1) = exp(-1/2*((i_4/step_1-0.06)/(0.03))^2);
    Gaussian_F(4,1) = 0.001*randn();
    Gaussian_F(7,1) = 0.001*randn();

    if i_4 == 1

        vol_3(:,i_4) = (C_Matrix1./dt_1+GO)\(Guassian_F
+C_Matrix1*vol_start/dt_1);

    else

        vol_3(:,i_4) = (C_Matrix1./dt_1+GO)\(Guassian_F
+C_Matrix1*vol_old/dt_1);

    end

    vol_old = vol_3(:, i_4);

end

figure(5)
plot(1:step_1, vol_3(7,:), 'r')
hold on

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```

plot(1:step_1, vol_3(1,:), 'b')
title('Vout plot using original of Cout of 0.00001')
xlabel('Time in milliseconds')
ylabel('Voltage in volts')
grid on

vol_7 = zeros(7, step_1);
Guassain_F = zeros(7,1);

%In part f), we are observing the effects of plotting Vout with
differet
%time steps. A discussion on my findings will take place at the end of
this
%document.

%Note that the original timestep was used in part b), and will not be
%replotted to avoid redundancy.

%using the timestep given

for i_5 = 1:step_1

    Guassain_F(1,1) = exp(-1/2*((i_5/step_1-0.06)/(0.03))^2);
    Guassain_F(4,1) = 0.001*randn();
    Guassain_F(7,1) = 0.001*randn();

    if i_5 == 1
        vol_7(:,i_5) = (C_Matrix1./dt_1+GO)\(Guassain_F
+C_Matrix1*vol_start/dt_1);
    else
        vol_7(:,i_5) = (C_Matrix1./dt_1+GO)\(Guassain_F
+C_Matrix1*vol_old/dt_1);
    end

    vol_old = vol_7(:, i_5);

end

figure(6)
plot(1:step_1, vol_7(7,:), 'r')
hold on
plot(1:step_1, vol_7(1,:), 'b')
title('Vout plot using original timestep of 10^-3')
xlabel('Time in picoseconds')
ylabel('Voltage in volts')
grid on

%using a smaller timestep

for i_6 = 1:step_2

    Guassain_F(1,1) = exp(-1/2*((i_6/step_2-0.06)/(0.03))^2);

```

```

    Guassian_F(4,1) = 0.001*randn();
    Guassian_F(7,1) = 0.001*randn();

    if i_6 == 1
        vol_4(:,i_6) = (C_Matrix1./dt_2+GO)\(Guassian_F
+C_Matrix1*vol_start/dt_2);

    else
        vol_4(:,i_6) = (C_Matrix1./dt_2+GO)\(Guassian_F
+C_Matrix1*vol_old/dt_2);

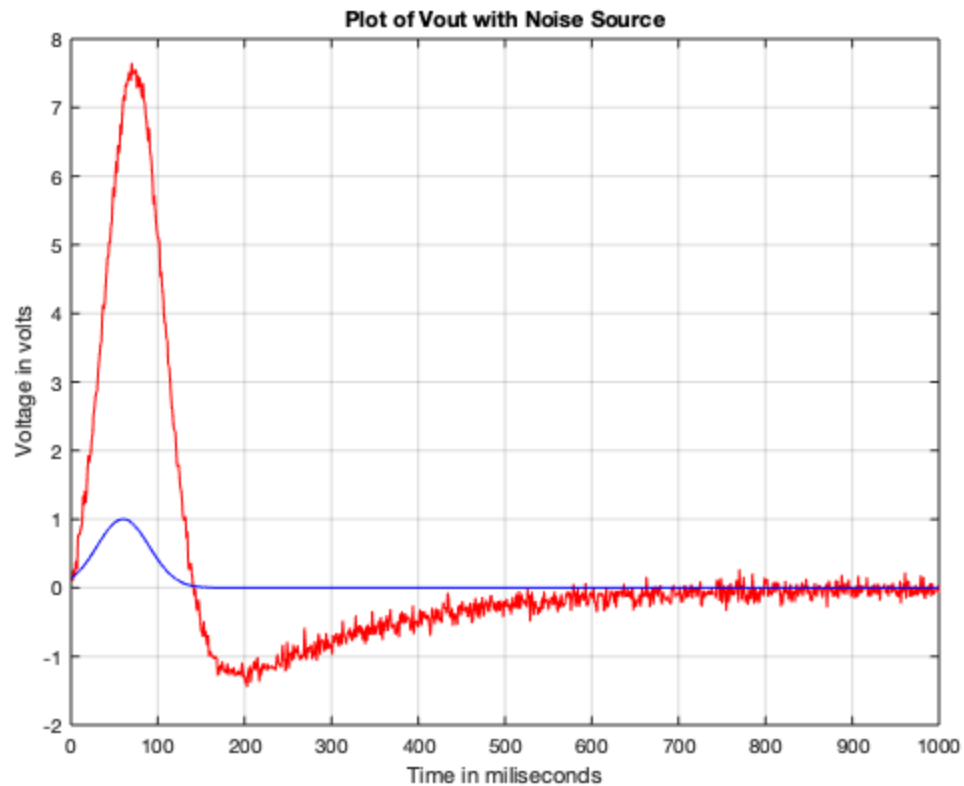
    end

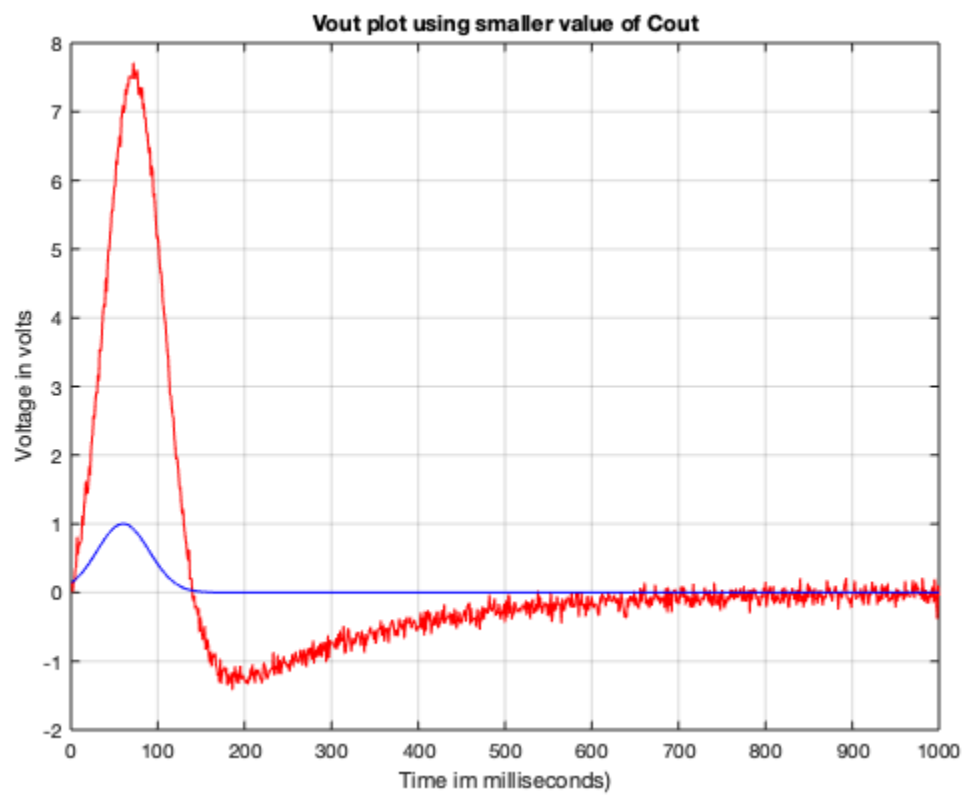
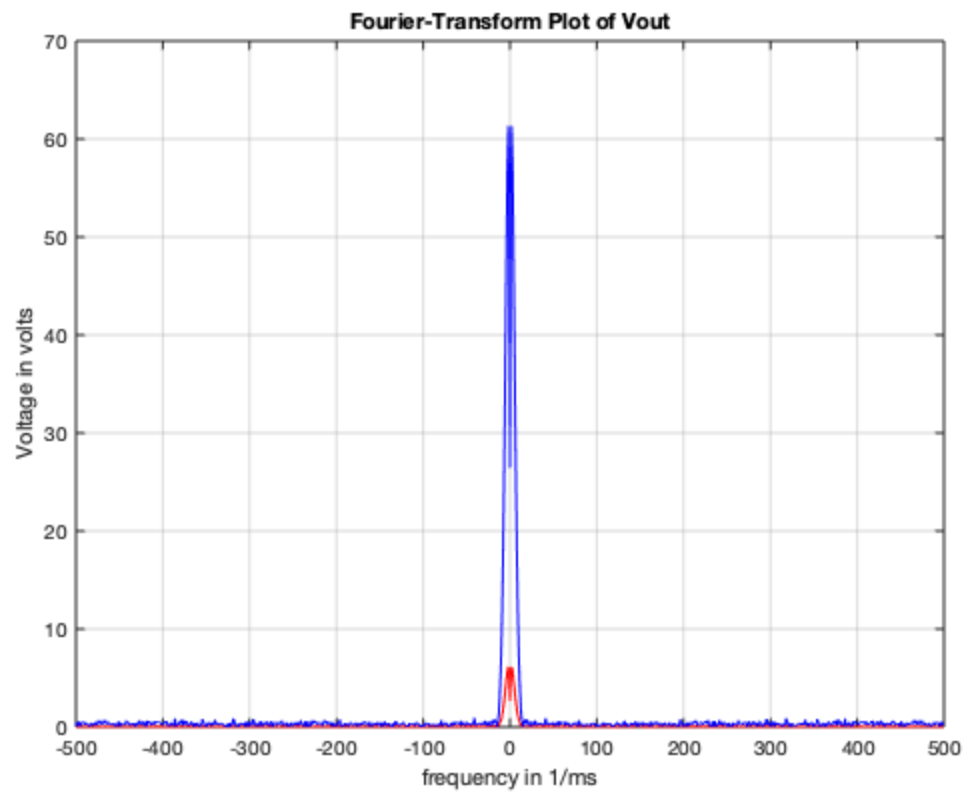
    vol_old = vol_4(:, i_6);

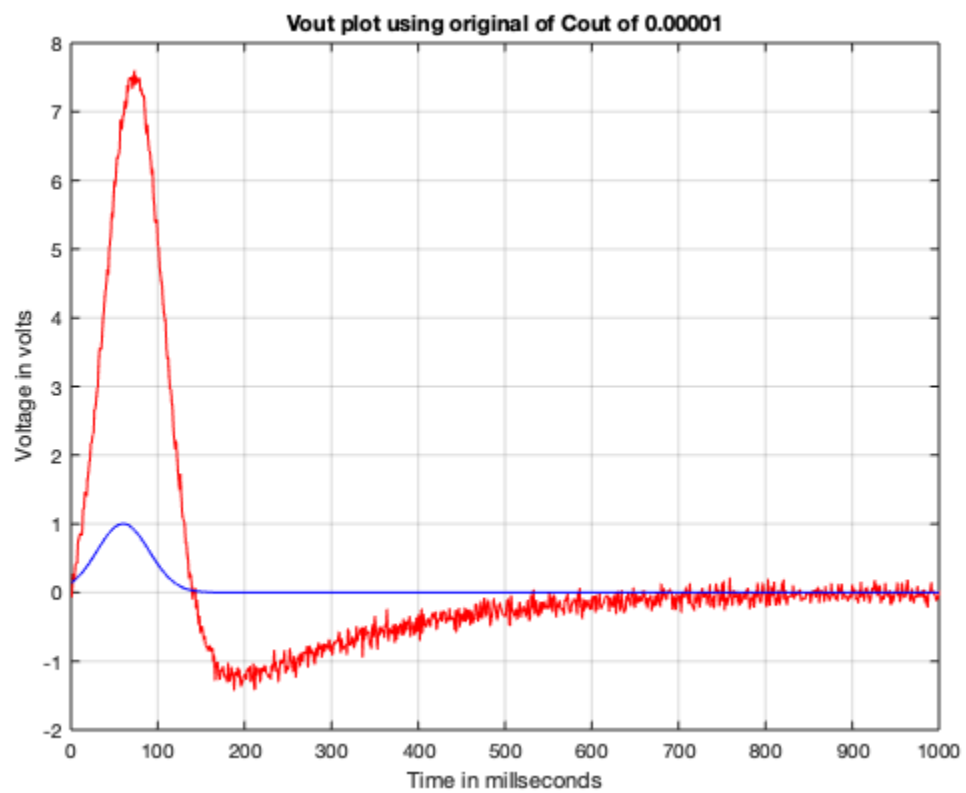
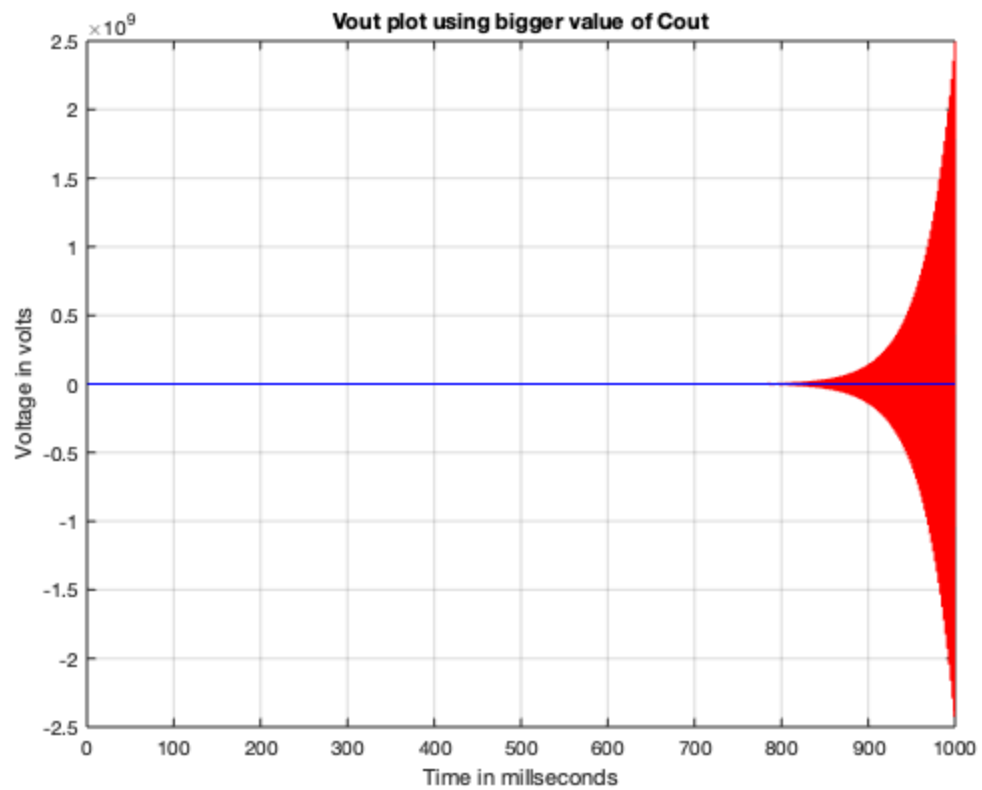
end

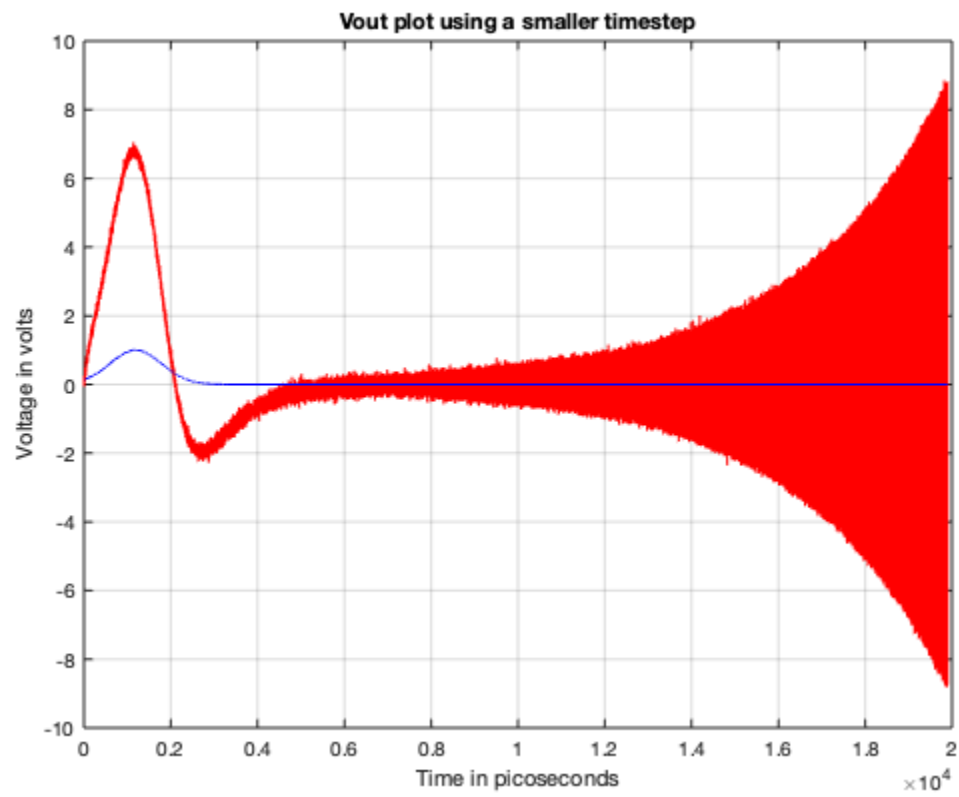
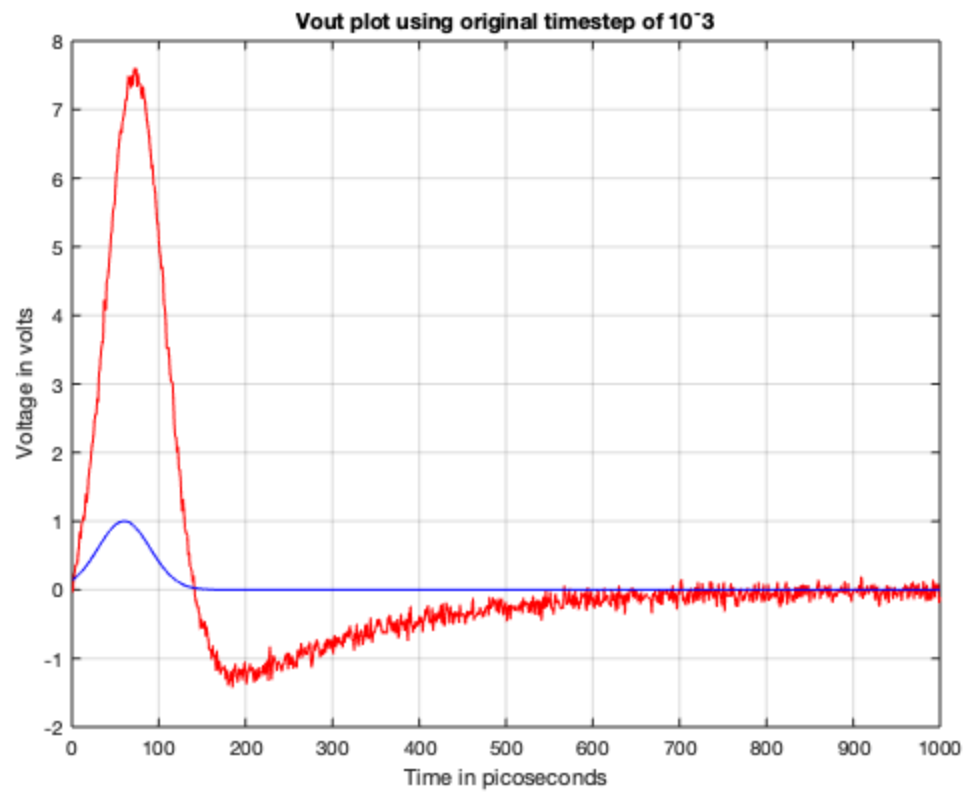
figure(7)
plot(1:step_2, vol_4(7,:), 'r')
hold on
plot(1:step_2, vol_4(1,:), 'b')
title('Vout plot using a smaller timestep')
xlabel('Time in picoseconds')
ylabel('Voltage in volts')
grid on

```









Discussion

```
% In part e), 3 plots of Vout were made using 3 values of Cout. It is
% noticed that using a smaller value of Cout does not change the plot.
% However, a larger value of Cout causes the simulation to break down.
% This
% is because the circuit becomes trapped in a feedback loop.

% In part f), 2 plots of Vout were made using different timesteps.
% Using a
% smaller timestep than the original timestep of 10^-3 causes the
% simulation to break down because the circuit becomes trapped in a
% feedback loop.
```

PART 4

```
% If the e voltage source on the output stage described by the
% transconductance equation
%  $V = ?I_3$  was instead modeled by  $V = \alpha \cdot I_3 + \beta \cdot I_2^2 + \gamma \cdot I_3^3$ ,
% the changes
% required in my simulator are more than just simply changing the
% matrices
% we used in the simulation for part 3. This new equation would need
% to be
% fitted, And new matrices would have to be created for the Jacobian
% method
% for the simulation of the new equation in the circuit. Note that the
% inclusion of this equation would in turn increase the size of the
% matrix
% and the iterations required to traverse through it. The values of
% alpha
% and beta that we define will have to be considerably large, as if  $i_3$ 
% is smaller
% than 1 this will be too small to have a noticeable effect on the
% simulation.
```

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